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## MATHS

## BOOKS - SELINA MATHS (ENGLISH)

## SECTION AND MID-POINT FORMULA

Exercise 13 A

1. Calculate the co-ordinates of the point $P$
which divides the line segment joining:
$A(1,3)$ and $B(5,9)$ in the ratio $1: 2$
2. Calculate the co-ordinates of the point $P$ which divides the line segment joining:
$A(-4,6)$ and $B(3,-5)$ in the ratio 3:2.

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3. The ratio in which the line segment joining
$(2,-3)$ and $(5,6)$ is divided by the $x$ - axis is :

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4. In what ratio is the line joining (2, -4) and $(-3,6)$ divided by the $y$-axis ?

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5. In what ratio does the point $(1, a)$ divide the
join of $(-1,4)$ and (4, -1) ? Also, find the value of a.

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6. In what ratio does the point $(a, 6)$ divide the
join of $(-4,3)$ and $(2,8)$ ? Also, find the value of a

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7. In what ratio is the join of $(4,3)$ and $(2,-6)$
divided by the $x$-axis ? Also, find the coordinates of the point of intersection.

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8. Find the ratio in which the join of $(-4,7)$ and
$(3,0)$ is divided by the $y$-axis. Also, find the coordinates of the point of intersection.

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9. Points $A, B, C$ and $D$ divide the line segment
joining the point ( $5,-10$ ) and the origin in five equal parts. Find the co ordinates of $B$ and $D$.

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10. The line joining the points $A(-3,-10)$ and $B$
$(-2,6)$ is divided by the point $P$ such that $\frac{P B}{A B}=\frac{1}{5}$. Find the co-ordinates of P.
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11. $P$ is a point on the line joining $A(4,3)$ and $B$
$(-2,6)$ such that $5 A P=2 B P$. Find the coordinates of $P$.

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12. Calculate the ratio in which the line joining the points $(-3,-1)$ and $(5,7)$ is divided by the line $x=2$.

## D Watch Video Solution

13. Calculate the ratio in which the line segment $A(6,5)$ and $B(4,-3)$ is divided by the line $y=2$.

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14. The point $P(5,-4)$ divides the line segment

AB , as shown in the figure, $\mathrm{P}(5,4)$ in the ratio
2:5. Find the co-ordinates of points $A$ and $B$.
Given AP is smaller than BP.


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15. Find the co-ordinates of the points of tri section of the line joining the points $(-3,0)$ and (6, 6).

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16. Show that the line segment joining the points $(-5,8)$ and ( $10,-4$ ) is trisected by the coordinate axes.
17. Show that $A(3,-2)$ is a point of trisection of the line-segment joining the points $(2,1)$ and $(5,-8)$.

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18. Given a line segment $A B$ joining the points
$A(-4,6)$ and $B(8,-3)$. Find :
(iii) the length of $A B$.
19. If $A=(-4,3)$ and $B=(8,-6)$

In what ratio is the line joining $A$ and $B$, divided by the $x$-axis ?

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20. The line segment joining the points M (5,
7) and $N(-3,2)$ is intersected by the $y$-axis at point $L$. Write down the abscissa of L. Hence, find the ratio in which $L$ divides MN. Also, find the co-ordinates of L .
21. A $(2,5), B(-1,2)$ and $C(5,8)$ are the coordinates of the vertices of the triangle $A B C$.

Points $P$ and $Q$ lie on $A B$ and $A C$ respectively, such that : $A P: P B=A Q: Q C=1: 2$.

Calculate the co-ordinates of P and Q .

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22. A $(2,5), B(-1,2)$ and $C(5,8)$ are the coordinates of the vertices of the triangle $A B C$.

Points $P$ and $Q$ lie on $A B$ and $A C$ respectively, such that : $A P: P B=A Q: Q C=1: 2$.

Show that : $P Q=\frac{1}{3} B C$.

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23. A $(-3,4)$, B $(3,-1)$ and $C(-2,4)$ are the vertices of a triangle $A B C$. Find the length of
line segment $A P$, where point $P$ lies inside $B C$, such that $\mathrm{BP}: \mathrm{PC}=2: 3$.

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24. The line segment joining $A(2,3)$ and $B 6,-5)$
is intercepted by $x$-axis at the point K. Write down the ordinate of the point K . Hence, find the ratio in which $K$ divides $A B$. Also, find the co-ordinates of the point K .

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25. The line segment joining $A(4,7)$ and $B(-6$,
$-2)$ is intercepted by the $y$-axis at the point $K$.
Write down the abscissa of the point K. Hence,
find the ratio in which $K$ divides $A B$. Also, find the co-ordinates of the point $K$.

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26. The line joining $P(-4,5)$ and $Q(3,2)$ intersects the $y$-axis at point R. $P M$ and QN are perpendiculars from $P$ and $Q$ on the $x$-axis.

Find:
the ratio PR: RQ

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27. The line joining $P(-4,5)$ and $Q(3,2)$ intersects the y -axis at point R. PM and QN are perpendiculars from $P$ and $Q$ on the $x$-axis.

Find:
the co-ordinates of $R$.

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28. The line joining $P(-4,5)$ and $Q(3,2)$
intersects the $y$-axis at point R. $P M$ and QN are perpendiculars from $P$ and $Q$ on the $x$-axis.

Find:
the area of the quadrilateral PMNQ .

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29. In the given figure, line APB meets the $x$ axis at point $A$ and $y$-axis at point $B$. $P$ is the point $(-4,2)$ and $A P: P B=1: 2$. Find the co-
ordinates $A$ and $B$.


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30. Given a line segment $A B$ joining the points
$A(-4,6)$ and $B(8,-3)$. Find :
(i) the ratio in which $A B$ is dividend by the $Y$ axis.

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31. Given a line segment $A B$ joining the points
$A(-4,6)$ and $B(8,-3)$. Find :
(ii) find the coordinates of the point of intersection. Divided by y-axis.
32. Given a line segment $A B$ joining the points
$A(-4,6)$ and $B(8,-3)$. Find :
(iii) the length of $A B$.

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33. If $P(9 a-2,-b)$ divides line segment joining $A$
$(3 a+1,-3)$ and $B(8 a, 5)$ in the ratio $3: 1$, then find
the values of $a$ and $b$.
34. Find the mid-point of the line segment joining the points :
$(-6,7)$ and $(3,5)$

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2. Find the mid-point of the line segment joining the points :
( $5,-3$ ) and ( $-1,7$ )
3. Points $A$ and $B$ have co-ordinates $(3,5)$ and ( $x, y$ ) respectively. The mid-point of $A B$ is (2, 3).

Find the values of $x$ and $y$.

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4. $A(5,3), B(-1,1)$ and $C(7,-3)$ are the vertices
of triangle $A B C$. If $L$ is the mid-point of $A B$ and
$M$ is the mid-point of $A C$, show
that $: L M=\frac{1}{2} B C$.

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5. Given $M$ is the mid-point of $A B$, find the coordinates of:
$A$, if $M=(1,7)$ and $B=(-5,10)$,

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6. Given $M$ is the mid-point of $A B$, find the coordinates of:

$$
B, \text { if } A=(3,-1) \text { and } M=(-1,3) \text {. }
$$

7. $P(-3,2)$ is the mid point of line segment $A B$ as shown in the given figure. Find the $P(-3,2)$ co-ordinates of points $A$ and $B$.

8. In the given figure, $P(4,2)$ is mid-point of line segment $A B$. Find the co-ordinates of $A$ and $B$.

9. $(-5,2),(3,-6)$ and $(7,4)$ are the vertices of a triangle. Find the length of its median through the vertex $(3,-6)$.

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10. Given a line $A B C D$ in which $A B=B C=C D, B=$
$(0,3)$ and $C=(1,8)$. Find the co-ordinates of $A$ and $D$.
11. One end of the diameter of a circle is $(-2,5)$.

Find the co-ordinates of the other end of it, if the centre of the circle is $(2,-1)$.

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12. $A(2,5), B(1,0), C(-4,3)$ and $D(-3,8)$ are the vertices of quadrilateral $A B C D$. Find the coordinates of the mid-points of AC and BD. Give a special name to the quadrilateral.
13. $P(4,2)$ and $Q(-1,5)$ are the vertices of parallelogram PQRS and $(-3,2)$ are the coordinates of the point of intersection of its diagonals. Find co-ordinates of R and S .

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14. $A(-1,0), B(1,3)$ and $D(3,5)$ are the vertices
of a parallelogram $A B C D$. Find the co-ordinates of vertex C .
15. The points $(2,-1),(-1,4)$ and $(-2,2)$ are midpoints of the sides of a triangle. Find its vertices.

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16. Points $A(-5, x), B(y, 7)$ and $C(1,-3)$ are collinear (i.e. lie on the same straight line) such that $A B=B C$. Calculate the values of $x$ and y .
17. Points $P(a,-4), Q(-2, b)$ and $R(0,2)$ are collinear. If lies between $P$ and $R$, such that $P R$
$=2 Q R$, calculate the values of $a$ and $b$.

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18. Calculate the co-ordinates of the centroid of the triangle $A B C$, if $A=(7,-2), B=(0,1)$ and $C$
$=(-1,4)$.
19. he co-ordinates of the centroid of a triangle $P Q R$ are $(2,-5)$. If $Q=(-6,5)$ and $R=(11$, 8), calculate the co-ordinates of vertex $P$.

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20. $A(5, x), B(-4,3)$ and $C(y,-2)$ are the vertices
of the triangle $A B C$ whose centroid is the origin. Calculate the values of $x$ and $y$.
21. Given a triangle $A B C$ in which $A=(4,-4) B=$
$(0,5)$ and $C=(5,10)$. A point $P$ lies on $B C$ such
that $B P: P C=3: 2$. Find the length of line segment AP.

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2. $A(20,0)$ and $B(10,-20)$ are two fixed points.

Find the co-ordinates of the point $P$ in $A B$ such
that : $3 \mathrm{~PB}=\mathrm{AB}$. Also, find the co-ordinates of some other Point $Q$ in $A B$ such that : $A B=6 A Q$.

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3. $A(-8, O), B(0,16)$ and $C(0,0)$ are the vertices of a triangle $A B C$. Point $P$ lies on $A B$ and $Q$ lies on $A C$ such that $A P: P B=3: 5$ and $A Q: Q C=3: 5$.

Show that : $\mathrm{PQ}=\frac{3}{8} \mathrm{BC}$.

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4. Find the co-ordinates of points of trisection of the line segment joining the point (6, -9) and the origin.

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5. A line segment joining $A\left(-1, \frac{5}{3}\right)$ and $B(a, 5)$ is divided in the ratio $1: 3$ at $P$, the point where the line segment $A B$ intersects the $y$ axis.

Calculate the value of $a^{\prime}$.
6. A line segment joining $A\left(-1, \frac{5}{3}\right)$ and $B(a, 5)$ is divided in the ratio $1: 3$ at $P$, the point where the line segment $A B$ intersects the $y$ axis.

Calculate the co-ordinates of ' P '.

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7. In what ratio is the line joining $A(0,3)$ and $B(4,-1)$ divided by the $x$-axis ?

Write the co-ordinates of the point where $A B$ intersects the $x$-axis.

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8. The mid-point of the $A$ segment $A B$, as
shown in diagram, is C $(4,-3)$. (4, -3) Write

## down the co ordinates of $A$ and $B$.



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9. $A B$ is a diameter of a circle with centre $C=$
$(-2,5)$. If $A=(3,-7)$. Find
the length of radius AC

## - Watch Video Solution

10. $A B$ is a diameter of a circle with centre $C=$
$(-2,5)$. If $A=(3,-7)$. Find
the coordinates of $B$.

## - Watch Video Solution

11. Find the co-ordinates of the centroid of a triangle $A B C$ whose vertices are :
$A(-1,3), B(1,-1)$ and $C(5,1)$

## D Watch Video Solution

12. The mid-point of the line segment joining
$(4 a, 23)$ and $(-4,3 b)$ is $(2,-2 a)$. Find the values of $a$ and $b$

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13. The mid-point of the line segment joining
$(2 a, 4)$ and $(-2,2 b)$ is $(1,2 a+1)$. Find the values

## of $a$ and $b$.

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14. Write down the co-ordinates of the point $P$
that divides the line joining $A(-4,1)$ and $B(17$,
10) in the ratio 1:2.

## D Watch Video Solution

15. write down the coordinate of the point $p$
that divides the line joining $A(-4,1)$ and $B(17,10)$
in the ratio $1: 2$

Calculate the distance $O P$, where $O$ is the origin.

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16. write down the coordinate of the point $p$
that divides the line joining $A(-4,1)$ and $B(17,10)$ in the ratio 1:2

In what ratio does the $y$-axis divide the line $A B$
?

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17. Prove that the points $A(-5,4), B(-1,-2)$ and
$C(5,2)$ are the vertices of an isosceles
rightangled triangle. Find the co ordinates of
$D$ so that $A B C D$ is a square.

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18. $M$ is the mid-point of the line segment
joining the points $A(-3,7)$ and $B(9,-1)$. Find the co-ordinates of point $M$. Further, if $R(2,2)$
divides the line segment joining $M$ and the origin in the ratio $\mathrm{p}: \mathrm{q}$, find the ratio $\mathrm{p}: \mathrm{q}$.

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19. Calculate the ratio in which the line joining
$A(-4,2)$ and $B(3,6)$ is divided by point $P(x, 3)$.

Also, find (i) $x$

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20. Determine the ratio in which the line $2 x+y$
$4=0$ divides the line segment joining the points $A(2,2)$ and $B(3,7)$.

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21. If the abscissa of a point $P$ is 2 , find the ratio in which this point divides the line segment joining the points $(-4,3)$ and $(6,3)$. Also, find the co-ordinates of point $P$.
22. The line joining the points $(2,1)$ and $(5,-8)$ is trisected at the points $P$ and $Q$. If point $P$ lies on the line $2 x-y+k=0$, find the value of $k$. Also, find the co-ordinates of point Q .

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23. Find the image of the point $A(5,-3)$ under reflection in the point $\mathrm{P}(-1,3)$.
24. $M$ is the mid-point of the line segment joining the points $A(0,4)$ and $B(6,0) . M$ also divides the line segment $O P$ in the ratio 1:3. Find :

co-ordinates of $M$
25. $M$ is the mid-point of the line segment
joining the points $A(0,4)$ and $B(6,0) . M$ also divides the line segment $O P$ in the ratio 1:3.

Find :

co-ordinates of $P$
26. $M$ is the mid-point of the line segment joining the points $A(0,4)$ and $B(6,0)$. $M$ also divides the line segment $O P$ in the ratio 1:3.

Find :

length of BP

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27. $A(-4,2), B(0,2)$ and $C(-2,-4)$ are vertices of a triangle $A B C . P, Q$ and $R$ are mid-points of sides $B C, C A$ and $A B$ respectively. Show that the centroid of $\triangle P Q R$ is the same as the centroid of $\Delta \mathrm{ABC}$.

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28. $A(3,1), B(y, 4)$ and $C(1, x)$ are vertices of triangle $A B C$ and $G(3,4)$ is its centroid. Find the values of $x$ and $y$. Also, find the length of side $B C$.

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## Questions

1. Find the co-ordinates of point $P$ which divides the line joining $A(4,-5)$ and $B(6,3)$ in
the ratio $2: 5$.

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2. Find the ratio in which the point $(5,4)$ divides the line joining points $(2,1)$ and $(7,6)$

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3. In what ratio is the joining the points $(4,2)$
and $(3,-5)$ divided by the $x$-axia ? Also, find the
co-ordinates of the point of intersection.
4. Calcuate the ratio in which the line joining the points $(4,6)$ and $(-5,4)$ is divided by the line $y=3$. Also, find the co-ordinates of the point of intersection.

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5. The origin $O, B(-6,9)$ and $C(12,-3)$ are vertices of triangle $O B C$, Point $P$ divides $O B$ in the ratio
$1: 2$ and point Q divides OC in the ratio $1: 2$

Find the co-ordinates of points $P$ and $Q$. Also
show that $P Q=\frac{1}{3} \mathrm{BC}$.

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6. Find the co-ordinates of the points of trisection of the segment joining the points $A$ $(6,-2)$ and $(-8,10)$.

7. Show that $P(3, m-5)$ is a point of trisection of the line segment joining the points $A(4,-2)$ and $B(1,4)$. Hence, find the value of ' $m$ '.

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8. If the point $\mathrm{P}(-1,2)$ divides the join of points
$A(2,5)$ and $B(a, b)$ in the ratio $3: 4$, find the value of $a \times b-a$.
9. Find the co-ordinates of the mid point of
the line segment joining the points $P(4,-6)$ and ( $-2,4$ ).

## D Watch Video Solution

10. The mid - point of line segment $A B$ (shown
in the diagram) is $(-3,5)$, Find the co-ordinates
of $A$ and $B$.

(D) Watch Video Solution
11. Points $A(7,-4), B(-5,5)$ and $C(-3,8)$ are vertices of triangle $A B C$, Find the length of its median through vertex A .

## D Watch Video Solution

12. $A(14,-2), B(6,-2)$ and $D(8,2)$ are the three vertices of a parallelgram $A B C D$. Find the coordinates of the fouth vertex $C$.
13. The mid-point of the segment joining (3m,
$6)$ and $(-4,3 n)$ is $(1,2 m,-1)$. Find the values of $m$ and n .

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14. The point $A(3,-5)$ is reflected in the point $P$
$(-4,3)$ as point $\mathrm{A}^{\prime}$. Find the co-ordinates of point A'.
15. If the mid-point of the segment joining the points $A(3,4)$ and $B(k, 6)$ is $(x, y)$ and $x+y=10$, find the value of $k$ and the length of the line segment $A B$.

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16. Find the co-ordinates of the point of intersection of the medians of triangle $A B C$, given $A=(-2,3), B=(6,7)$ and $C=(4,1)$.
17. $A B C$ is a triangle and $G(4,3)$ is the centroid of the triangle. If $A=(1,3), B=(4, b)$ and $C=(a$,

1 ), find 'a' and 'b'.

Find the length of side $B C$.

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