



## MATHS

### BOOKS - CENGAGE

## QUADRATIC EQUATIONS

### Worked Examples

$$1. 8x^2 - 47 = 100 + 5x^2$$



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$$2. (x + 5)(x - 5) = 39$$



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3. Solve the following equation

$$\frac{x + 2}{x - 2} + \frac{x - 2}{x + 2} = \frac{5}{2}$$



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$$4. (x + 3)(x + 4) + (x - 2)(x - 5) = 30$$



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5.  $\sqrt{8x^2 - 12x + 29} = 3x - 2$



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6. Solve the following equation :  $x^2 - 5x + 6 = 0$



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7. Solve the following equation :

$$ab(x^2 + 1) = (a^2 + b^2)x$$



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8. Solve the following equation :

$$2x^2 - 7x + 6 = 0$$



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9. Solve for  $x \times x^2 - 5x + 6 = 0$  by completing the square.



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10. Solve the following by completing the square :

$$(x + 4)(x + 5) = 3(x + 1)(x + 2) + 2x$$



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11. Solve using the formula

$$3x^2 = 2x + 1$$



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12. Solve using the formula

$$x^2 - x - 1 = 0$$



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**13.** Solve the following reducing them to a quadratic equation.

$$4x^4 - 25x^2 + 36 = 0$$



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**14.** Solve the following reducing them to a quadratic equation.

$$8x^{3/2} - 8x^{-3/2} = 63$$



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15. Solve the following reducing them to a quadratic equation.

$$4.2^{2x+1} - 9.2^x + 1 = 0$$



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16. Solve the following reducing them to a quadratic equation.

$$\sqrt{\frac{x}{1-x}} + \sqrt{\frac{1-x}{x}} = 2\frac{1}{6}$$



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17. Solve the following :

$$x^2 - 12x + \sqrt{x^2 - 12x + 81} - 9$$



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18. Solve the following :

$$3x^4 - 20x^3 - 94x^2 - 20x + 3 = 0$$



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19. Find the nature of the roots of

$$x^2 - 5x - 2 = 0.$$





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20. For what value of  $m$  will the equation  $x^2 + mx - (m^2 + 3m - 32) = 0$  have equal roots ?



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21. If  $\alpha$  and  $\beta$  are the roots of  $lx^2 + mx + n = 0$ , find the value of  $\alpha^2 + \beta^2$  and  $\alpha^3 + \beta^3$ .

$$\alpha^2 + \beta^2$$



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22. If  $\alpha$  and  $\beta$  are the roots of  $lx^2 + mx + n = 0$ , find the value of  $\alpha^2 + \beta^2$  and  $\alpha^3 + \beta^3$ .

$$\alpha^3 + \beta^3$$



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23. If the roots of  $x^2 - px + 1 = 0$  are two consecutive integers, prove that  $p^2 = 4q + 1$ .



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**24.** If  $\alpha$  and  $\beta$  are the roots of the equation

$$4x^2 - 6x + 1 = 0, \text{ find the following :}$$

$$\alpha\beta^3 + \alpha^3\beta$$



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**25.** If  $\alpha$  and  $\beta$  are the roots of the equation

$$4x^2 - 6x + 1 = 0, \text{ find the following :}$$

$$\frac{\alpha^2}{\beta} + \frac{\beta^2}{\alpha}$$



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26. If  $\alpha$  and  $\beta$  are the roots of the equation  $4x^2 - 6x + 1 = 0$ , find the following :

$$\alpha^4 + \beta^4$$



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27. Find two even positive consecutive integers whose product is 288.

Note :

(a) Any general even number is  $2n$ .

(b) any general odd number is  $2n + 1$  or  $2n - 1$ .



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**28.** Find the length and breadth of a rectangular field, whose perimeter is 40 m and area is  $96 \text{ m}^2$ .



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**29.** The digit in the tens place of a two - digit number is equal to the square of the digit in the units place. If 54 is subtracted from the number, its digits are interchanged. Find the number.



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30. The product of four consecutive natural numbers is 360. Find the numbers.



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## Test Yourself Level 1

1. Solve the following equations :

$$5x^2 - 8 = 37$$



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2. Solve the following equations :

$$2x^2 - 2 = 18 - 3x^2$$



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3. Solve the following equations :

$$(x + 3)(x - 3) = 7$$



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4. Solve the following equations :

$$(6 + x)(6 - x) + (6 + x)(5 - x) = 0$$



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5. Solve the following equations :

$$(x + 3)(x + 4) + (x - 2)(x - 5) = 0$$



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6. Solve the following equations :

$$\sqrt{8x^2 - 12x + 29} = 3x - 2$$



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7. Solve the following equations by factorisation:

$$9x^2 + 15x - 14 = 0$$



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8. Solve the following equations by factorisation:

$$3x^2 + 16x + 5 = 0$$



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9. Solve the following equations by factorisation:

$$x + \frac{1}{x} = 5\frac{1}{5}$$



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**10.** Solve the following equations by factorisation:

$$ab(x^2 + 1) = (a^2 + b^2)x$$



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**11.** Solve the following equations by factorisation:

$$x^2 + 2bx - 1 = -b^2$$



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## Test Yourself Level 2

1. Solve the equation:

$$\frac{x - a}{x - b} + \frac{x - b}{x - a} = \frac{a}{b} + \frac{b}{a}$$



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2. 
$$\frac{16}{x^{3/2}} + \frac{x^{1/2}}{2} = \frac{6}{x^{1/2}}$$



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3. Solve the following equations by completing the square :

$$x^2 - 2x = 15$$



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4. Solve the following equations by completing the square :

$$x^2 + 10x = 24$$



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5. Solve the following equations by completing the square :

$$(x - 1)(x - 2) = 20$$



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6. Solve the following equations by completing the square :

$$\frac{8 - x}{2} - \frac{2x - 11}{x - 3} = \frac{x - 2}{6}$$



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7. Solve the following equations by completing the square :

$$\frac{(x - 1)}{(x - 2)} - \frac{x - 3}{x - 4} = \frac{x - 5}{x^2 - 6x + 5}$$



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8. Solve the following equations by completing the square :

$$ax(x - a) = (a - x)$$



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**9.** Solve the following equations by completing the square :

$$x^2 - 2ax = 1 - a^2$$



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**10.** Solve the following using formula :

$$x^2 + 3x - 4 = 0$$



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**11.** Solve the following using formula :

$$x^2 = 4(x - 1)$$



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**12.** Solve the following using formula :

$$2x^2 + \frac{3}{4}x = \frac{5}{16}$$



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**13.** Solve the following using formula :

$$12x^2 + 9x = 9^2$$





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**14.** Solve the following using formula :

$$(a - b)^2 x^2 - (a - b)^2 x - ab = 0$$



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**15.** Solve the following :

$$9x^4 - 148x^2 + 64 = 0$$



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**16.** Solve the following :

$$8\sqrt{\frac{x}{x+3}} + \sqrt{\frac{x+3}{x}} = 6$$



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**17.** Solve the following :

$$x^{-2} - 2x^{-1} = 63$$



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**18.** Solve the following :

$$x^{2/3} - 2x^{1/3} - 15 = 0$$



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19. Solve the following :

$$7^{x+1} + 7^{1-x} = 50$$



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$$20. 2\left(x^2 + \frac{1}{x^2}\right) - 9\left(x + \frac{1}{x}\right) + 14 = 0$$



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**21.** Solve the following :

$$6\left(x^2 + \frac{1}{x^2}\right) - 25\left(x - \frac{1}{x}\right) + 12 = 0$$



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**22.** Solve the following :

$$(x + 1)(x + 2)(x + 3)(x + 4) = 24$$



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**23.** Solve the following :

$$x(x + 2)(x + 3)(x + 5) = 72$$



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**24.** Solve the following :

$$x(x + 1)^2(x + 2) = 72$$



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**25.** Solve the following :

$$x(2x + 1)(x - 2)(2x - 3) = 63$$



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26. Solve the following :

$$\sqrt{2x + 1} - \sqrt{x} = 1$$



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27. Solve the following :

$$1 - \sqrt{7x^2 - 9x + 3} = x$$



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28. Solve the following using identity :

$$\sqrt{x^2 - 3x + 36} - \sqrt{x^2 - 3x + 9} = 3$$



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**29.** Form the quadratic equation whose roots are as follows :

$$-2, -3$$



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**30.** Form the quadratic equation whose roots are as follows :

$$a, -a$$



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**31.** Form the quadratic equation whose roots are as follows :

$$\frac{9}{2}, \frac{9}{2}$$



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**32.** Form the quadratic equation whose roots are as follows :

$$1 \pm \sqrt{2}$$



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**33.** Form the quadratic equation whose roots are as follows :

One of the roots is  $2 + \sqrt{3}$ .



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### Test Yourself Level 3

**1.** If  $\alpha$  and  $\beta$  are roots of the equation  $4x^2 - 6x + 1 = 0$ , find the following :

$$\alpha^3 + \beta^3$$



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2. If  $\alpha$  and  $\beta$  are roots of the equation

$4x^2 - 6x + 1 = 0$ , find the following :

$$\alpha^4\beta^5 + \alpha^5\beta^4$$



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3. Find the quadratic equation whose roots are  $\alpha$

and  $\beta$  having given the following :

$$\alpha + \beta = 9, \alpha\beta = -5$$



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4. Find the quadratic equation whose roots are  $\alpha$  and  $\beta$  having given the following :

$$\alpha + \beta = 5, \frac{1}{\alpha} + \frac{1}{\beta} = 8$$



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5. If  $\alpha$  and  $\beta$  are roots of  $x^2 - 5x + 6 = 0$ , form the equation whose roots are as follows :

$$\alpha^2, \beta^2$$



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6. If  $\alpha$  and  $\beta$  are roots of  $x^2 - 5x + 6 = 0$ , form the equation whose roots are as follows :

$$\frac{1}{\alpha}, \frac{1}{\beta}$$



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7. If  $\alpha$  and  $\beta$  are roots of  $x^2 - 5x + 6 = 0$ , form the equation whose roots are as follows :

$$\frac{\alpha}{\beta}, \frac{\beta}{\alpha}$$



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8. If  $\alpha$  and  $\beta$  are roots of  $x^2 - 5x + 6 = 0$ , form the equation whose roots are as follows :

$$\alpha^3, \beta^3$$



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9. If  $\alpha$  and  $\beta$  are roots of  $x^2 - 5x + 6 = 0$ , form the equation whose roots are as follows :

$$\frac{1}{\alpha^2}, \frac{1}{\beta^2}$$



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10. If  $\alpha$  and  $\beta$  are roots of  $x^2 - 5x + 6 = 0$ , form the equation whose roots are as follows :

$$\frac{\alpha^2}{\beta}, \frac{\beta^2}{\alpha}$$



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11. Solve the following :

$$2^{2x+3} - 57 = 65(2^x - 1)$$



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**12.** Solve the following :

$$3^{x+2} + 3^{-x} + 10 = 0$$



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**13.** Solve the following :

$$5^{x+1} + 5^{2-x} = 5^3 + 1$$



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**14.** Solve the following :

$$\sqrt{2x + 7} + \sqrt{3x - 18} = \sqrt{7x + 1}$$



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15. Solve the following :

$$\sqrt{x + 5} + \sqrt{x + 12} = \sqrt{2x + 41}$$



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16. Solve the following :

$$\sqrt{3x^2 + 7x + 2} - \sqrt{2x^2 + 7x + 11} = x - 3$$



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17. Solve the following :

$$\sqrt{x^2 - 11x + 30} - \sqrt{2x^2 - 21x + 55} = x - 5$$



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18. Discuss the nature of the roots of the following :

$$7x^2 - 11x + 4$$



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**19.** Discuss the nature of the roots of the following :

$$6x^2 - 13x - 15 = 0$$



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**20.** Discuss the nature of the roots of the following :

$$x^2 - 7x + 8 = 0$$



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21. Discuss the nature of the roots of the following :

$$x^2 + 9x + 27 = 0$$



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22. Discuss the nature of the roots of the following :

$$4x^2 - 12x + 15 = 0$$



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23. For what value of  $k$  will  $18x^2 - kx + 2 = 0$  have equal roots ?



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24. If  $p$  and  $q$  are the roots of  $x^2 - ax + b = 0$ , find the value of  $\frac{1}{p^3} + \frac{1}{q^3}$ .



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25. Find the quadratic equation one of whose roots is  $p + \sqrt{q}$ .



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**26.** The sum of the squares of two consecutive natural numbers is 145. Find the numbers.



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**27.** The length of a rectangle is greater than twice its breadth by 2 cm. The length of its diagonal is 13 cm. Find the length and breadth of the rectangle.



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**28.** In a rectangular mango grove, the number of trees lengthwise is 5 more than the number of trees breadthwise. If the total number of trees is 1400, find the number of trees lengthwise and breadthwise.



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**29.** The sum of the reciprocals of two consecutive odd natural numbers is  $\frac{12}{35}$ . Find the numbers.



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**30.** A car covers a distance of 300 km with the same speed, it will cover the same distance in 1 hour less if its speed is increased by 10 km/h. Find the speed of the car.



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**31.** A cistern can be filled by two pipes in  $33\frac{1}{3}$  minutes, if the larger pipe takes 15 minutes less than the smaller to fill the cistern, find in what time it will be filled by each pipe separately.



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**32.** One - fourth of a herd of camels was seen in the forest. Twice the square root of the herd had gone to mountains and the remaining 15 camels were seen on the bank of a river. Find the total number of camels.



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**33.** a motorboat, whose speed in still water is 15 km/h, goes 30 km downstream and returns to the



starting point in a total time of 4 hours 30 minutes. Find the speed of the stream.



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**34.** A passenger train takes 3 hours less for a journey of 360 km. If its speed is increased by 10 km/h from its usual speed, what is the usual speed ?



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**35.** In a flight of 600 km, an aircraft was slowed down due to bad weather. Its average speed for the trip was reduced by 200 km/h and the time of flight increased by 30 minutes. Find the duration of flight.



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**36.** Find the roots of the following, drawing the graphs in two ways :

$$x^2 + 4x - 12 = 0$$



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**37.** Find the roots of the following, drawing the graphs in two ways :

$$2 - 2x + x^2 = 0$$



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**38.** Find the roots of the following, drawing the graphs in two ways :

$$x^2 - 4x + 3 = 0$$



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**39.** Find the roots of the following, drawing the graphs in two ways :

$$x^2 + x - 6 = 0$$



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**40.** Find the roots of the following, drawing the graphs in two ways :

$$2x^2 - 5x - 3 = 0$$



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**41.** Find the minimum value of the following and find the value of  $x$  for which the expression takes the minimum value :

$$4x^2 + 8x + 25$$



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**42.** Find the minimum value of the following and find the value of  $x$  for which the expression takes the minimum value :

$$9x^2 - 8x - 8$$



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**43.** Find the minimum value of the following and find the value of  $x$  for which the expression takes the minimum value :

$$16x^2 - 24x - 26$$



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## Test Yourself Multiple Choice Questions

1. Sum of roots of the equation

$$4^x - 3(2^{x+3}) + 128 = 0, \text{ is}$$

A. 0

B. 7

C. 5

D. 8

**Answer: B**



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2. If  $\alpha$  and  $\beta$  are the zeros of the polynomial

$f(x) = x^2 - 5x + k$  such that  $\alpha - \beta = 1$ , find

the value of  $k$ .

A. 8

B. 4

C.  $13/2$

D. 6

**Answer: D**



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3. If  $p(x) = ax^2 + bx + c$  and  $Q(x) = -ax^2 + dx + c$ , where  $ac \neq 0$ , then  $P(x) \times Q(x) = 0$  has at least



- A. four real roots
- B. two real roots
- C. four imaginary roots
- D. only one real root

**Answer: B**



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4. If roots of the equation  $(q - r)x^2 + (r - p)x + (p - q) = 0$  are equal, then p,q and r are in

A. AP

B. GP

C. HP

D. AGP

**Answer: A**



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5. If  $3p^2 = 5p + 2$  and  $3q^2 = 5q + 2$  where  $p \neq q$ ,

then  $pq$  is equal to

A.  $\frac{2}{3}$

B.  $\frac{-2}{3}$

C.  $\frac{3}{2}$

D.  $\frac{-3}{2}$

**Answer: B**



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6. If  $\alpha$  and  $\beta$  are the roots of the quadratic equation  $x^2 + bx - c = 0$ , then the equation whose roots are  $b$  and  $c$ , is

A.  $x^2 + \alpha x - \beta = 0$

$$\text{B. } x^2 - [(\alpha + \beta) + \alpha\beta]x - \alpha\beta(\alpha - \beta) = 0$$

$$\text{C. } x^2 + [(\alpha + \beta) + \alpha\beta]x + \alpha\beta(\alpha + \beta) = 0$$

$$\text{D. } x^2 + [(\alpha + \beta) + \alpha\beta]x - \alpha\beta(\alpha + \beta) = 0$$

**Answer: C**



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7. Let  $p, q \in \{1, 2, 3, 4\}$ . The number of equations of the form  $px^2 + qx + 1 = 0$  having real roots, is

A. 15

B. 9

C. 8

D. 7

**Answer: D**



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**8.** Find the number of rational roots of the equation  $(x + 2)(x + 3)(x + 8)(x + 12) = 4x^2$

A. 4

B. 2

C. 0

D. 1

**Answer: B**



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9. Solutions of the equation

$$(6 - x)^4 + (8^4 - x)^4 = 16 \text{ are}$$

A. 8,6

B.  $-8, -6$

C. 8,9

D.  $-8, 6$

**Answer: A**



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**10.** Solution of the equation

$$\sqrt{2x^2 + 5x - 2} - \sqrt{2x^2 + 5x - 9} = 1 \text{ are}$$

A.  $-2, 9/2$

B.  $2, -9/2$

C.  $-2, -9/2$

D.  $2, 9/2$

**Answer: B**



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**11.** Solutions of the equation

$$64 \times 9^x - 84 \times 12^x + 27 \times 16^x = 0 \text{ are}$$

A.  $-1, -2$

B.  $-1, 2$

C.  $2, 3$

D.  $1, 2$

**Answer: D**





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12. Let  $\alpha, \beta$  be the roots of the equation

$$x^2 - x + p = 0$$

and  $\gamma, \delta$  be the roots of the equation

$$x^2 - 4x + 9 = 0.$$

If  $\alpha, \beta, \gamma, \delta$  are in GP then the integral value of p

and q, respectively, are

A.  $-2, -32$

B.  $-2, 3$

C.  $-6, 3$

D.  $-6, -32$

**Answer: A**



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**13.** If  $\alpha, \beta$  are the roots of the equation

$$x^2 - 3x + 5 = 0$$

and  $\gamma, \delta$  are the roots of the equation

$$x^2 + 5x - 3 = 0,$$

then the equation whose roots are  $\alpha\gamma + \beta\delta$  and

$\alpha\delta + \beta\gamma$ , is

A.  $x^2 - 15x - 158 = 0$

B.  $x^2 + 15x - 158 = 0$

C.  $x^2 - 15x + 158 = 0$

D.  $x^2 + 15x + 158 = 0$

**Answer: D**



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**14.** If  $\cos^4 \theta + p$ ,  $\sin^4 \theta + p$  are the roots at the equation  $x^2 + a(2x + 1) = 0$  and

$\cos^2 \theta + q, \sin^2 \theta + q$  are the roots of the equation  $x^2 + 4x + 2 = 0$  then  $a$  is equal to

A.  $-2$

B.  $-1/2$

C.  $1$

D.  $2$

**Answer: D**



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15. If  $\alpha$  and  $\beta$  roots of the equation

$$x^2 - p(x + 1) - c = 0$$

then

$$\frac{\alpha^2 + 2\alpha + 1}{\alpha^2 + 2\alpha + c} + \frac{\beta^2 + 2\beta + 1}{\beta^2 + 2\beta + c} =$$

A. 1

B. -1

C. 2

D. 3

**Answer: A**



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16. The quadratic equation, product of whose roots  $x_1$  and  $x_2$  is equal to 4 and are related as

$$\frac{x_1}{x_1 - 1} + \frac{x_2}{x_2 - 1} = 2, \text{ is}$$

A.  $x^2 + 2x + 4 = 0$

B.  $x^2 - 4x + 4 = 0$

C.  $x^2 - 2x + 4 = 0$

D.  $x^2 + 4x + 4 = 0$

**Answer: C**



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17. If one root of the equation  $x^2 - dx + 12 = 0$  is even prime, while  $x^2 + dx + \mu = 0$  has equal roots then  $\mu$  is

- A. 8
- B. 20
- C. 32
- D. 16

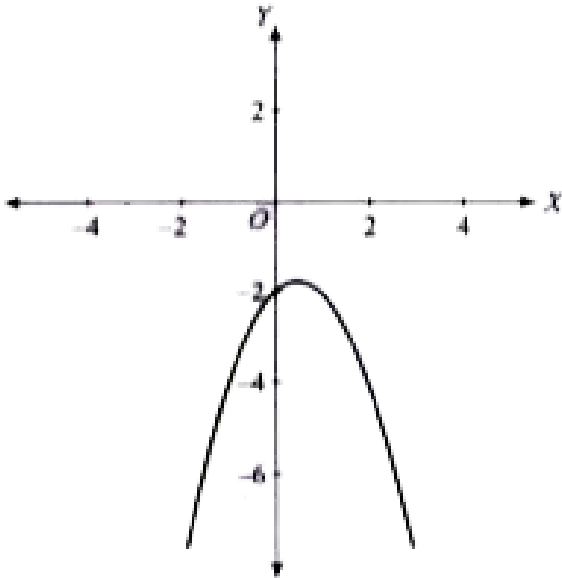
**Answer: D**



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18. The graph of a quadratic polynomial

$y = ax^2 + bx + c$ ,  $a, b, c \in R$  is as shown.



Which one of the is NOT correct ?

A.  $b^2 - 4ac < 0$

B.  $\frac{c}{a} < 0$

C.  $c$  is negative



D. abscissa corresponding to the vertex is

$$\left( \frac{-b}{2a} \right)$$

**Answer: B**



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19. If  $x + \frac{1}{x} = 5$  then

$$x^3 - 5x^2 + x + \frac{1}{x^3} - \frac{5}{x^2} + \frac{1}{x} =$$

A.  $-5$

B.  $0$

C.  $5$

D. 10

**Answer: B**



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**20.**

**If**

$$(a^2 - 1)x^2 + (a - 1)x + (a^2 - 4a + 3) = 0 \text{ is}$$

an identity in  $x$ , then the value of  $a$  is/are

A.  $-1$

B.  $3$

C.  $1$

D.  $-1, 1, 3$

**Answer: C**



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21. If  $\alpha$  and  $\beta$  are the roots of  $ax^2 + bx + c = 0$ , then which of the following are the roots of the equation  $ax^2 - bx(x - 1) + c(x - 1)^2 = 0$ ?

A.  $\frac{\alpha}{\alpha + 1}, \frac{\beta}{\beta + 1}$

B.  $\frac{\alpha + 1}{\alpha} + \frac{\beta + 1}{\beta}$

C.  $\frac{\alpha}{\alpha - 1}, \frac{\beta}{\beta - 1}$

D.  $\frac{\alpha - 1}{\alpha}, \frac{\beta - 1}{\beta}$

**Answer: A**



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22. The equation for

$$x: 3\sqrt{2x - 1} + 3\sqrt{x - 1} = 1 \text{ is}$$

A. 0

B. 0, 1

C. 1

D. None of these

**Answer: C**



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## Olympiad And Ntse Level Exercises

1. If  $a, b, c \in Q$  then roots of the equation

$$(b + c - 2a)x^2 + (c + a - 2b)x + (a + b - 2c) = 0$$

are

A. irrational

B. non-real

C. rational

D. equal

**Answer: C**



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2. Solutions of the equation

$$(12x - 1)(6x - 1)(4x - 1)(3x - 1) = 5 \text{ are}$$

A.  $-\frac{1}{12}, \frac{1}{2}$

B.  $-\frac{1}{12}, -\frac{1}{2}$

C.  $\frac{1}{12}, \frac{1}{2}$

D.  $\frac{1}{12}, -\frac{1}{2}$

**Answer: A**



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3. If  $\alpha, \beta$  be the roots of the equation  $3x^2 + 2x + 1 = 0$ , then find value of

$$\left(\frac{1-\alpha}{1+\alpha}\right)^3 + \left(\frac{1-\beta}{1+\beta}\right)^3$$

A. 10

B. -9

C. 9

D.  $-10$

**Answer: D**



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4. The square of difference of the roots of the equation  $x^2 + px + 45 = 0$  is 144. The roots are

A.  $-3, -15$

B.  $2, 5$

C.  $-12, 12$

D.  $18, -18$



**Answer: A**



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5. Read the following statements.

Statements 1 : If  $\sqrt{\sqrt{\sqrt{x}}} = 4\sqrt{4\sqrt{4\sqrt{3x^4 + 4}}}$

then the value of  $x^4$  is 4.

Statements 2: If  $a$  and  $b$  are positive numbers and each of the equations  $x^2 + ax + 2b = 0$  and  $x^2 + 2bx + a = 0$  has real roots then the smallest possible value of  $(a + b)$  is 10.

A. Both Statement a and Statement 2 are true.

B. Statement 1 is true and Statement 2 is false.

C. Statement 1 is false and Statement 2 is true.

D. Both Statements 1 and Statement 2 are false.

**Answer: B**



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6. If  $x, y \in R$  satisfy the equation  $x^2 + y^2 - 4x - 2y + 5 = 0$  then the value of the

expression

$$\frac{(\sqrt{x} - \sqrt{y})^2 + 4\sqrt{xy}}{x + \sqrt{xy}} \text{ is}$$



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7. If one root of the equation  $x^2 + px + 12 = 0$  is 4, while the equation  $x^2 + px + q = 0$  has equal roots then the value of q is

A. 4

B.  $49/4$

C.  $4/49$

D. None of these

**Answer: B**



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8. If  $\alpha, \beta$  are the roots of  $x^2 - 2x + 4 = 0$ , then  $\alpha^5 + \beta^5$  is :

A. 32

B. 64

C. 16

D. None of these

Answer: A



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9. Match the following columns :

(a)	If $a, b, c$ and $d$ are four non-zero real numbers such that $(d + a - b)^2 + (d + b - c)^2 = 0$ and the roots of the equation $a(b - c)x^2 + b(c - a)x + c(a - b) = 0$ are real and equal then	(p)	$a + b + c = 0$
(b)	If $a, b$ and $c$ are non-zero positive real numbers such that $\log a, \log b$ and $\log c$ are in A.P. then	(q)	$a, b, c$ are in AP
(c)	If the equation $ax^2 + bx + c = 0$ and $x^3 - 3x^2 + 3x - 1 = 0$ have a common real root then	(r)	$a, b, c$ are in GP
(d)	If $a, b$ and $c$ are positive real numbers such that the expression $bx^2 + \left( \sqrt{(a+c)^2 + 4b^2} \right)x + (a+c)$ is non-negative $\forall x \in \mathbb{R}$ then	(s)	$a, b, c$ are in HP



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10. Column I contains rational algebraic expression and column II contains possible integers which lie in their ranges. Match the columns.

Column I		Column II	
(a)	$y = \frac{x^2 - 2x + 4}{x^2 + 2x + 4}, x \in R$	(p)	1
(b)	$y = \frac{x^2 - 3x - 2}{2x - 3}, x \in R$	(q)	4
(c)	$y = \frac{2x^2 - 2x + 4}{x^2 - 4x + 3}, x \in R$	(r)	-3
(d)	$x^2 - (a - 3)x + 2 < 0, \forall x \in (-2, 3)$	(s)	-10



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