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## MATHS

## BOOKS - TARGET PUBLICATION

## CHALLENGING QUESTIONS

## Similarity

1. In $\square A B C D$, side $B C|\mid$ side $A D$. Digonals $A C$ and $B D$
intersect each other at $P$. If $A P=\frac{1}{3} A C$ then prove $D P=\frac{1}{2} B P$.

## Pythagoras Theorem

1. In $\triangle A B C, \angle A B C=135^{\circ}$. Prove that :
$A C^{2}=A B^{2}+B C^{2}+4 A(\Delta A B C)$.
A


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2. $\triangle P Q R$ is a right angled triangle, right angled at Q such that $\mathrm{QR}=\mathrm{b}$ and $A(\Delta P Q R)=\mathrm{a}$ if $\mathrm{QN} \perp \mathrm{PR}$ then show that $Q N=\frac{2 a . b}{\sqrt{b^{4}+4 a^{2}}}$


1. In the adjoining figure, $B C$ is a diameter of the circle with centre $M$.
$P A$ is a tangent at $A$ from $P$, which is a point on line $B C$.
$A D \perp B C$
prove that $D P^{2}=B P \times C P-B D \times C D$

2. Find the length of the longest chord of the circle of radius 5.2 cm .

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3. Radius of a circle with centre $O$ is 4 cm . if $/(O P)=4.2$
cm then state where point $P$ will lie with respect to
the circle.

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4. In the given figure, $O$ is the center and chord $P Q=$

Chord RS.

If $\mathrm{OT}=5 \mathrm{~cm}$, then find OU .


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5. If circumcentre of a triangle is outside the triangle, then what is the type of triangle?

# 6. The radius of a circle is 5 cm and the distance of a 

 chord from the centre is 3 cm . Find the length of the chord.D Watch Video Solution
7. In the given figure, centre of two circles is $\mathbf{O}$. Chord
$A B$ of bigger
circle intersects the smaller circle in points $P$ and $Q$.

Show that $\mathrm{AP}=\mathrm{BQ}$.


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## Co Ordinate Geometry

1. Points $A(-1, y)$ and $B(5,7)$ lie on a circle with centre
$\mathrm{O}(2,-3 y)$.

Find the values of $y$. Hence, find the radius of the circle.

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2. Prove that the points $(3,0),(6,4)$ and $(-1,3)$ are the vertices of a
right angled isosceles triangle.

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3. If the centre of a circle is (2a,a-7) ,then Find the value of a ,
if the circle passes through the point $(11,-9)$ and has diameter $10 \sqrt{2}$ units.

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4. Write the quadrant or on which axis the followning points lie.
i. $A(-6,2)$
ii. $B(0,-5)$

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5. If $P(-1,1), Q(3,-4), R(1,-1), S(-2,-3)$ and $T(-4,4)$ are plotted on the graph paper, then the point(s) in the fourth

## quadrant is/are

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6. The graphs of which of the equations given below will be
parallel of the X -axis ?
i. $x=3$
ii. $y-2=0$

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7. Write the equation of line parallel to $Y$-axis and at a distance of

5 units to its left.

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8. The point $A(-5,-4)$ lies on a line parallel to $X$ axis. Write its equation.

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9. Write the equation of $x$ axis.

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10. $Y$ - axis and line $x=-4$ are parallel lines. What is the distance
between them ?

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11. If ' $b$ ' is a real number, then what is the distance between lines
$y=b$ and $y=-b ?$
12. How many lines are there which are parallel to the $x$-axis and
having a distance 5 units ? Write their equations.

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## Trigonometry

1. 

Prove that
$(1+\tan \theta)^{2}+(1+\cot \theta)^{2}=(\sec \theta+\operatorname{cosec} \theta)^{2}$.
2. If $\sec \theta-\tan \theta=P$ then obtain the values of $\tan \theta \sec \theta$ and $\sin \theta$ in terms of $P$.

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3. 

Prove
that
$\frac{1+\sin x-\cos x}{1+\sin x+\cos x}+\frac{1+\sin x+\cos x}{1+\sin x-\cos x}=2+2 \operatorname{cosec}$

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4. The angle of elevation of a jet plane from a point $A$
on the ground
is $60^{\circ}$. After a flight of 30 seconds, the angle of
elevation changes
to $30^{\circ}$. If the jet plane is flying at a constant height of $3600 \sqrt{3} m$,
find the speed of the jet plane.

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5. A pilot in an aeroplane observes that Vashi bridge is one side of the plane and Worli sea - link is just on
the oposite side. The angles of depressions of Vashi bridge and Wrli sea - link are $60^{\circ}$ and $30^{\circ}$ respectively
. If the aeroplane is at a height of $5500 \sqrt{3} m$ at that
time, what is the distance between Vashi bridge and
Wrli sea - link ?
6. If in $\triangle A B C, \angle B=90^{\circ}$ and $\angle C=\theta$, then write the ratios
$\sin \theta$ and $\tan \theta$


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## 7. Find the Values of $\frac{\sin 36^{\circ}}{\cos 54^{\circ}}$.

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8. Fill in the blanks : $\tan 30^{\circ} \times \tan _{-}=1$

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9. If $\sin \theta=\frac{5}{13}$, then find $\cos \theta$ if $\theta$ is in 1st quadrant.
10. Find the value of $\frac{\tan 60^{\circ}}{\sin 30^{\circ}+\cos 60^{\circ}}$

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## Mesuration

1. A cylindrical tub of radius 5 cm and length 9.8 cm is
full of water. A solid in the form of right circular cone mounted on a hemisphere is immersed into the tub.

The radius of the hemisphere is 3.5 cm and height of
cone outside the hemisphere is 5 cm . Find the volume of water left in the tub. (Take $\pi=\frac{22}{7}$ )

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2. A cylindrical jar of radius 10 cm is filled with water
upto a height of 15 cm .14 sphercal balls of radius 3 cm each are immersed in the jar. Find the new level to which water is filled in the jar.

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3. An oil funnel of tin sheet consists of a cylindrical
portion 10 cm long attached to a frustum of cone. The
diameters of the top and bottom of the frustum are 18 cm and 8 cm respecti8vely. If the slant height of the frustum of the cone is 13 cm , find the area of the tin required to make the funnel from the given information in the figure
$(\pi=3.14)$


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1. If the co-ordinates of points $A$ and $B$ are $(-5,0)$ and
$(2,0)$ respectively, then find $d(A, B)$

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2. Which figure is formed by three non-collinear points?

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3. point $C$ is the midpoint of seg $A B$. If $A C=5.5$,
then find the length of $A B$.
4. If $A B=5 \mathrm{~cm}, \mathrm{BP}=2 \mathrm{~cm}$ and $\mathrm{AP}=3.4 \mathrm{~cm}$, then compare the segments.

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5. Answer the following question with the help of the figure given below .

Write the pairs of points equidistant from $P$.

6. Write the following statement in if -then form .

Diangonals of a rhombus bisect each other.

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7. Write the converse of the following statement.

The alternate angles formed by two parallel lines and
their
transversal are congruent.
8. Write the converse of 'if' the number is a prime, then it is even or odd' .

Also state if the converse is true or not.

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9. From the information given below,find which of the point is
between the other two. If the points are not collinear,
state so.
$d(P, Q)=10, d(Q, R)=3, d(P, R)=7$.
10. Points $X, Y$ and $Z$ are collinear such that $d(X, Y)=17$, $d(Y, Z)=8$, find $d(X, Z)$.

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11. The co-ordinate of point $B$ on the number line is
-3 . Find the co-ordinates
of the points which are at a distance of 6 units from B.
12. The following table shows points on a numberline and their co-ordinates.

Decide whether the pair of segments given below the table are congruent or not.
Point
L M N
P $\mathrm{Q} \quad R$
Co-ordinate $\begin{array}{lllllll}-5 & 0 & 8 & -1 & 7 & 4\end{array}$
seg QR and seg LM.

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13. Answer the following question with the help of figure given below .

(i) Write the intersection of ray DB and ray AD.
(ii) Write the union set of ray AC and ray BE .

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## Paralles Lines

1. As shown in the figure, if lines /and $m$ are parallel, then write algebraic equations using the property of
interior angles.


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2. If two lines are parallel, then what can you say about the pairs
of corresponding angles formed by their transversal ?

## 3. In $\triangle A B C$, if $\angle A=62^{\circ}, \angle B=28^{\circ}$ then find $\angle C$

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4. In the given figure sides of $\angle P Q R$ and $\angle X Y Z$ are parallel to each other. Prove that, $\angle P Q R \cong \angle X Y Z$.

5. In the given figure, if $x=125^{\circ}$ and $y=54^{\circ}$ then are lines $m$ and $n$ parallel ? Justify.

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6. In the given figure, ray $A E \|$ ray $B D$, ray $A F$ is the bisector of $\angle E A B$ and ray BC is the bisector of $\angle A B D$. Prove that lineAF || line $B C$.


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7. In the given figure, if line $A B|\mid ~ l i n e ~ C F ~ a n d ~ l i n e ~ B C ~$
line ED,
then prove that $\angle A B C=\angle F D E$.


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Triangles

1. In the givne figure , $\angle P R S$ is the exterior angle of
$\triangle P Q R$. If $\angle P=55^{\circ}$ and $\angle Q=64^{\circ}$, then find $\angle P R S$.

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2. In the figures given below, equal parts of triangles are marked with
the same signs. Observe the figures and state the test
by which the
two triangles are congruent.


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3. The length of median on hypotenuse of a right angled
triangle is 7 cm . Find the length of the hypotenuse.
4. In the given figure, point $A$ is on the bisector of
$\angle X Y Z$.

If $A X=2 \mathrm{~cm}$, then find $A Z$.


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5. If $\Delta R S T \sim \Delta L M N$ then write the ratios of corresponding sides.
6. The measures of angles of a triangle are in the ratio

3:5:7.

Find the measure of the smallest angle.

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7. The measures of angles of a triangle are $2 x^{\circ}, 3 x^{\circ}$, and $4 x^{\circ}$.

What type of triangle is it ?
8. In the given figure, measures of some angles are given . Using the measures, find the values of $x$ and $y$.


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9. In the given figure, $\angle P \cong \angle R$, seg $\mathrm{PQ} \cong$ seg RQ . Prove that $\triangle P Q T \cong \Delta R Q S$.


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10. Find the values of $x$ and $y$ using the information shown in the figure.


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11. In $\triangle A B C, \angle B A C=120^{\circ}$ and $\mathrm{AB}=\mathrm{AC}$, then find measure of $\angle A B C$.
12. In $\triangle A B C, \angle B=90^{\circ}, \mathrm{AB}=8, \mathrm{BC}=6$ and BD is a median .

Find (BD).

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13. In the given figure point $G$ is the pointof
concurrence of the medians of $\triangle P Q R$. If $\mathrm{GT}=2.5$,
then find the length of PG.


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14. In $\triangle A B C, \mathrm{AB}=15 \mathrm{~cm}, \mathrm{BC}=12 \mathrm{~cm}$ and $\mathrm{AC}=17 \mathrm{~cm}$.

Find out the greatest and smallest angle of $\triangle A B C$.
15. In $\triangle L S N$, if $\angle L=80^{\circ}, \angle S=40^{\circ}$, then find out the greatest and smallest sides of $\Delta L S N$.

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16. If $\triangle A P C \sim \Delta B P D, \mathrm{BD}=2.4 \mathrm{~cm}, \mathrm{AC}=3.6 \mathrm{~cm}, \mathrm{PD}=4$
cm and
$B P=3.2 \mathrm{~cm}$, then find AP and PC.
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17. $\square P Q R S$ is a parallelogram. If $\angle P=60^{\circ}$ then find
$\angle Q$

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2. $\square A B C D$ is a rectangle. If $\mathrm{AC}=6 \mathrm{~cm}$, then find BD .

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3. Diagonals SU and TV of rhombus STUV intersect each other at point W. Find $\angle S W T$.
4. $\square L M N O$ is a square. Diagonlas LN and MO intersect each other at point S. Find $\angle S M N$

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5. If the diagonals of a quadrilateral are perpendcular bisectors of
each other, then what type of quadrilateral is it ?

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6. Points $D, E$ and $F$ are the midpoints of sides $A B, B C$, and AC of $\triangle A B C$. If $\mathrm{DE}=10 \mathrm{~cm}, \mathrm{EF}=12 \mathrm{~cm}$ and $\mathrm{DF}=8$ cm , then find $A B$.

7. Write the type of triangle formed by joining the midpoints of the sides of an equilateral triangle.

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8. In parallelogram ABCD , if $\angle A=(7 x+40)^{\circ}$ and

$$
\angle C=(2 x+80)^{\circ},
$$

then find $\angle A$.

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9. The lengths of adjacent sides of a parallelogram are 5 cm and 12 cm .
find the perimeter of the parallelogram.

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10. The diagonals of rectangle $A B C D$ intersect at $O$.

If $\angle A O D=40^{\circ}$, then find $\angle O A D$

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11. Adjacent sides of rectangle are 9 cm and 40 cm .

Find diagonal.
12. Find the length of the side of a square if the length of its diagonal is 12 cm .

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13. State with reason whether the given statement is true or false.

Every parallelogram is a rhombus.
14. State whether the statement 'every rectangle is a parallelogram, is true or false. Justify.

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15. In trapezium $A B C D$, side $B C \|$ side $A D$, side $A B \cong$ side $D C$.

If $\angle A=72^{\circ}$, then find the measures of $\angle B$ and $\angle D$


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Surface Area And Volume

1. Side of a cube is 4 cm . Find ratio of its total surface area and vertical surface area.
2. Find the volume of a cube with side 6 cm .

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3. The dimensions of a cuboid in $\mathrm{cm} 30 \times 18 \times 10$.

Find its volume.

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4. A cuboidal box open at the top has length, breadth and height
$20 \mathrm{~cm}, 16 \mathrm{~cm}$ and 10 cm respectively. Find its volume.
5. Volume of a cube is $1000 \mathrm{~cm}^{3}$. Find its side.

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6. How many surfaces does a cone have ?

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7. The radius and slant height of a cone are 4 cm and

25 cm
respectively. Find the curved surface area of that cone. $(\pi=3.14)$

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8. If the radius and the perpendicular height of a cone and cylinder is equal then write the ratio of their volumes.

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9. The diameter of a sphere is 6 cm . Find the total surface area of the sphere. $(\pi=3.14)$

# 10. The volume of a cube is $1,000 \mathrm{~cm}^{3}$. Find its total 

 surface area.
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11. If the edge of a cube is increased two times, then what will happen to tis volume?
12. Volume of a cuboid is $520 \mathrm{~cm}^{3}$. The length and breadth of the
cuboid are 10 cm and 6.5 cm respectively. Find its height.

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13. 2 cubes, each of volume $125 \mathrm{~cm}^{3}$, are joined end to
end . Find the surface area of the resulting cuboid.
14. If the height and volume of a cylinder are 15 cm and $3000 \mathrm{~cm}^{3}$ respectively. Find the area of its base.

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15. Curved surface area of a cylinder is $8800 \mathrm{~cm}^{2}$ and the radius of its
base is 7 cm . Find the height of the cylinder.

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16. If the radius and height of a road roller are 0.5 m and 1.4 m respectively, then find the area of field
pressed in 100 rotations.

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17. The radius of base and perpendiular height of a cone are 12 cm
and 16 cm respectively. Find its slant height .

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18. The total surface area of a cone is $704 \mathrm{~cm}^{2}$ and the radius of its base is 7 cm . Find its slant height .
19. The radius and slant height of a cone are 5 cm and 10 cm respectively. Find the ratio of the curved surface area to the
total surface area of cone.

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20. The radius of a cone is reduced to half. What should be done to its slant height so that curved surface area remains unchanged.
21. Find the volume of a sphere of radius $3.5 c m(\pi=3.14)$

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22. Find the radius of a hemisphere if its volume is
$144 \pi \mathrm{~cm}^{3}$.

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23. Is the following statement true or false.

The radius of a sphere and hemisphere is the same. If
the surface
area of the sphere is $400 \mathrm{~cm}^{2}$ then the total surface area of the hemisphere will be $200 \mathrm{~cm}^{2}$

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24. If the radius of a sphere is equal to the diameter of a hemisphere.

Find the ratio of volume of sphere to that of the hemisphere.

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25. The volume of a hemisphere is four times that of a sphere. Find the ratio of the radius of the hemisphere to that of the sphere.

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## Chapter 1 Linear Equations In Two Variable

1. Sum of two numbers is 97 . If the greater number is
divided by the the smaller, the quotient is 7 and the remainder is 1 . Find the numbers.

