

India's Number 1 Education App

MATHS

BOOKS - TARGET PUBLICATION

CIRCLE



1. In the adjoining figure ,seg DE is a chord of a

circle with centre C.

seg CF \perp seg DE. If diameter of the circle is

20 cm, DE = 16 cm,

find CF. Recall and write theorems and properties which are useful

to find the solution of the above problem.

Using them solve the

above problems.





2. In the adjoining figure, seg QR is a chord of the circle with centre O.

P is the midpoint of the chord QR. If QR=24, OP=10, find radius of the circle. To find solutions of the problem ,

write the theorems that are useful , Using

them, solve the problem.



3. In the adjoining figure, M is the centre of the circle and seg AB is a diameter. Seg MS \perp

chord AD, seg MT \perp chord AC,

 $\angle DAB \cong \angle CAB.$

Prove that : chord AD \cong chord AC.



4. In the adjoining figure, M is the centre of the circle and seg AB is a diameter. Seg MS \perp chord AD, seg MT \perp chord AC, $\angle DAB \cong \angle CAB$.

Which of the following tests of congruence of

traingles will be

useful?



A. (a) SAS

B. (b) ASA

C. (c) SSS

D. (d) AAS

Answer: D



5. If two equal chords of a circle intersect within the circle, prove that the segments of one chord are equal to corresponding segments

of the other chord.

1. Take two points A and B on the page of your note book. Draw a circle with centre A which passes through B.

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2. How many circle can be draw to pass
through two given points

(a) 1 (b) 2 (c) 0 (d) as many as possible

3. There is one and only circle passing through

three non-collinear points.



4. Take any three non-collinear points. What should be done to draw a circle passing through all these points ? Draw a circle through these points.



5. Number of circles passing through 3 collinear points in a plane is

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Lets Recall

1. Which theorem do we use in proving that hypotenuse is the longest side of a right





1. The circles shown in the given figure are called externally touching circles. Why?



2. The circles shown in the given figure are called internally touching circles. Why?



3. In the given figure ,

(i) the radii of the circles with centres A and B

are 3cm and 4cm respectively.

(ii) the radii of the circles with centres A and B

are 4cm and 3cm respectively.

Find

(i) d(A,B) in figure (a)

(ii) d(A,B) in figure (b)





4. If one angle of a triangle is equal to the sum

of the other two,

show that the traingle is right angled.

Hint.

 $\angle A = \angle B + \angle C \Rightarrow \angle A + \angle B + \angle C + = 180^{\circ}$

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5. State and prove the Pythagoras theorem



In the above figure, seg AB is a diameter of a circle with centre P.C is any point on the circle. Seg CE \perp seg AB. Prove that CE is the geometric mean of AE and EB. Write the proof with the help of following steps:

(a) Draw ray CE. It intersects the circle at D.

(b) Show that CE = ED.

Write the result using theorem of intersection

of chords insides

a circle.

(d) Using CE = ED, complete the proof.



In the figure , S is the midpoint of seg PQ . Line

ST || side QR and

PT = 5 cm , then find PR. Justify your answer.

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8. State and prove the Pythagoras theorem



1. In the adjoining figure, the radius of a circle with centre C is 6cm,

line AB is a tangent at A. Answer the following question

(i) What is the measure of $\angle CAB$? Why?

(ii) What is the distance of point C from line AB? Why?

(iii) d(A,B)=6cm, find d(B,C).



2. In the figure, O is the center of the circle. From point R, seg RM and seg RN are tangent segments touching the circle at M and N.

If OR = 10cm and radius of the circle = 5 cm,

then

(i) What is the length of each tanget segment

?

(iii) What is the measure of $\angle MRO$?

(iii) Whatis the measure of $\angle MRN$?



3. In the figure,seg RM and seg RN are tangent segments of a circle with centre O.Prove that seg OR divides $\angle MRN$ as well as $\angle MON$.



4. What is the distance between two parallel tangents of a circle having radius 4.5 cm.

Justify your answer.

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Practice Set 3 2

1. Two circles having radii 3.5 cm and 4.8 cm touch each other internally.Find the distance

between their centres.





2. Two circles of radii 5.5cm and 4.2cm touch

each other externally.



- 3. Two circles with centres at A and B, touch at
- T. BD is the tangent
- at D and TC is a common tangent. AT has
- length 3 and BT has
- length 2. The length of CD is:

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Practice Set 3 3

1. In the figure , points G,D,E,F are concyclic points of a cicle with centreC. $\angle ECF = 70^{\circ}$

m (arc DGF) $\,=\,200^{\,\circ}$,

find m(arc DE) and m(arc DEF) .



2. In the adjoining figure, $AB\cong CD$. Prove that $arcAC\cong arcBD$



Practice Set 3 4

1. In cyclic $\ \Box \, MRPN, \angle R = (5x-13)^{\,\circ}$ and

$\angle R$ and $\angle N$





2. In the adjoining figure, seg RS is the diameter of the circle with centre 'O'. Point T is in the exterior of the circle. Prove that $\angle RTS$ is an acute angle.





3. Prove that any rectangle is a cyclic quadrilateral.



4. In the adjoining figure, $m(arcNS)=125^{\,\circ}$,

 $m(arcEF)=37^{\circ}$. Find $m \angle NMS$.



5. In the adjoining figure,chord AC and chord DE intersect at point B.If $\angle ABE = 108^{\circ}$ and $m(arcAE) = 95^{\circ}$,then find m(arc DC).





1. In the adjoining figure, point Q is the point of contact of tangent and the circle. If PQ=12, PR=8, then find PS and RS.





2. In the adjoining figure, if PQ=6, QR=10, PS=8, then find TS.


3. In the adjoining figure, seg EF is the diameter of the circle with centre H. Line DF is tangent at point F. If r is the radius of the

circle, then prove that $DE imes GE = 4r^2.$



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1. Two circles of radii 5.5 cm and 3.3 cm respectively touch each other.What is the distance between their centres?

A. 4.4cm

B. 8.8cm

C. 2.2cm

D. 8.8 or 2.2cm

Answer: D



2. Two circles intersect each other such that each circles pass through the centre of the other.If the distance between their centres is 12,what is the radius of each circle?

A. 6cm

B. 12cm

C. 24cm

D. can't say

Answer: B



3. A circle touches all sides of a parallelogram.so the parallelogram must be a

A. rectangle

B. rhombus

C. square

D. trapezium

Answer: B



4. Length of a tangent segment drawn from a point which is at

a distnace 12.5 cm from the centre of a circle is

12cm , find the diameter of the circle.

A. (a) 25cm

B. (b) 24cm

C. (c) 7cm

D. (d) 14cm

Answer: C

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5. If two circles are touching externally,how many common tangents of them can be drawn?

A. One

B. Two

C. Three

D. Four

Answer: C



6. $\angle ACB$ is inscribed in arc ACB of a circle

with centre O.If $\angle ACB = 65^{\circ}$,find m(arc ACB)

A. $65^{\,\circ}$

B. 130°

C. 295°

D. 230°

Answer: D



7. Chords AB and CD of a circle intersect inside

the circle at point E. If AE=5.6, EB=10, CE=8, find

ED. a)7 b)8 c)11.2 d)9

B. 8

C. 11.2

D. 9

Answer: A

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8. In a cyclic $\Box ABCD$, twice the measure of $\angle A$ is thrice the measure of $\angle C$. Find the measure of $\angle C$ a)36° b)72° c)90° d)108°

A. 36°

B. 72°

C. 90°

D. 108°

Answer: B

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9. Points A,B,C are on circle, such that $m(arcAB) = m(arcBC) = 120^{\circ}$. No point, except point B, is common to the arcs. What is

the type of riangle ABC? a)Equilateral triangle b)Scalene triangle c)Right angled triangle d)Isosceles triangle

A. Equilateral traingle

B. Scalene traingle

C. Right angled traingle

D. Isosceles traingle

Answer: A

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10. Seg XZ is a diameter of a circle. Point Y lies

in its interor. How many

of the followint statements are true?

(1) It is a not possible that $\angle XYZ$ is an acute angle.

(2) $\angle XYZ$ can't be a right angle

(3) $\angle XYZ$ is an obtuse angle.

(4) Can't make a dfinite statement for measure

of $\angle XYZ$

A. (a) Only One

B. (b) Only two

C. (c) Only three

D. (d) All

Answer: C



11. In the adjoining figure, O is the centre of

the circle. Seg AB, seg AC

are tangent segments. Radius of the circle is r

and I(AB) = r.

Prove that , \Box ABOC is a square.



12. In the figure, $\Box ABCD$ is a parallalogram.

It circumscribes the

cirlcle with centre T. Point E,F,G,H are touching

points. If AE = 4.5,

EB = 5.5, find AD.





13. Two circles intersect each other at the points P and Q. Two straight lines through P and Q intersect one circle at the points A and C and

the other circle at B and D. Prove the AC|| BD

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14. In the adjoining figure, circles with centres

X and Y touch internally

at point Z. Seg BZ is a chord of bigger circle

and it intersects smallest

circle at point A. prove that, seg AX ||seg BY.



15. In the adjoining figure, line I touches the circle at P.O is the centre.Q is the mid point of

radius OP.Chord $RS \mid \ \mid l \in el$ RS=12,find

radius of the circle.



16. In the adjoining figure, seg AB is a diameter

of a circle with centre C.

Line PQ is a tangent, which touches the circle

at point T.

Seg AP \perp line PQ and seg BQ \perp line PQ.

Prove that seg CP \cong seg CQ.



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17. Prove that any three points on a circle cannot be collinear.Watch Video Solution

18. In the adjoining figure ,chord EF || chord GH.

Prove that, chord EG \cong chord FH.



19. A circle with centre C touches the circle with centre D internally in the point E. Point D lies on the smaller circle. Chord EB of the

external circle intersects internal circle at

point A. Prove that $segEA\cong segAB$





20. In the adjoining figure, seg AB is a diameter of a circle with centre O. the bisector of $\angle ACB$ intersects the circle at point D.

Prove that ,seg $AD \cong segBD$.





21. In the adjoining figure, two circles intersect each other at point M and N. Secants drawn from point M and N intersect cirlces at point R, S, P and Q as shown in the figure. Prove that seg PR || seg QS



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22. Two circles intersect each other at the points P and Q. Two straight lines through P and Q intersect one circle at the points A and C and

the other circle at B and D. Prove the AC BD

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23. In the adjoining figure, seg AD \perp side BC,

seg BE \perp side AC,

seg CF \perp side AB. Point O is the orthocentre.

Prove that , point O is the incentre of ΔDEF .



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Activities For Practice

1. Complete the activity by filling the boxes.

In the given figure , $\angle BAC = 80^\circ$, $\angle ABC = 30^\circ$ and $m(arcBQC) = 160^\circ.$

Find (i) m(arcAPC) (ii) m(arcAB).





In the figure □ ABCD is a cyclic quadrilateral.Seg AB is a diameter.

If $\angle ADC = 120^{\circ}$, find the measure of $\angle BAC$.





3. In the adjoining figure, point Q is the point of contact of tangent and the circle. If PQ=12, PR=8, then find PS and RS.





Multiple Choice Question

1. Concentric Circles have the same_____.

A. (a) Diameter

B. (b) Radius

C. (c) Centre

D. (d) Chord

Answer: C

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2. A tangent at any point of a circle is perpendicular to the

radius through the ____.

A. (a) Chord

B. (b) Diameter

C. (c) Point of contact

D. (d) All of the above

Answer: C





3. The maximum number of tangents that can be drawn to a circle from a point outside it is.....a)2 b)1 c) one and only one d)0

A. 0

B. 1

C. 2

D. 3

Answer: C





4. The number of tangents that can be drawnto a circle at a point on the circle is.....a)3 b)2c)1 d)0

- A. 0
- B. 1
- C. 2
- D. 3

Answer: B



5. If two circles are touching externally,how many common tangents of them can be drawn?

- A. 0
- B. 1
- C. 2
- D. 3

Answer: B



6. Tangents drawn at the endpoints of a diameter of a circle are.....a)Equal b)Perpendicular c)Parallel d)Intersecting each other

A. coincident

B. parallel

C. intersecting

D. perpendicular




7. The number of parallel tangents atmost a circle can have on

a diameter is

A. (a) 1

B. (b) 2

C. (c) 0

D. (d) 3





8. Angles inscribed in the same arc are

A. (a) congruent

B. (b) complementary

C. (c) supplementary

D. (d) none of these

Answer: A



A. (a) $20 \mathrm{~cm}$

B. (b) $\sqrt{20}$ cm

C. (c) 10 cm

D. (d) $\sqrt{10}$ cm

Answer: B

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In the above figure, if lines AD and CD are tangents, then $m \angle B$ =_____

A. (a) $40^{\,\circ}$

B. (b) $130^{\,\circ}$

C. (c) 50°

D. (d) 220°

Answer: B



11. For the figure given below, which of the following options is correct?



- A. (a) AP = BP
- B. (b) $\angle APO = \angle BPO$
- C. (c) $\angle AOP = \angle BOP$

D. (d) all of the above

Answer: D

12. In the given figure , if TP and TQ are the two tangents to a circle with centre O so that $\angle POQ = 110^\circ$, then $\angle PTQ$ is equal

to



A. (a) $60^{\,\circ}$

B. (b) 70°

C. (c) 80°

D. (d) 90°

Answer: B



13. In the figure RQ is a tangent to the circle with centre O.

If SQ = 6cm, QR = 4cm, find OR.



- A. (a) 4cm
- B. (b) 5cm
- C. (c) 6cm
- D. (d) 3cm

Answer: B





14. PA and PB are tangents to the circle with centre O touching it

at A and B respectively. IF $\angle APO = 25^{\circ}$, then

 $\angle POB$ is



B. (b) 155°

C. (c) $130^{\,\circ}$

D. (d) 150°

Answer: A

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15. In figure, QR is a common tangent to the given circles, touching externally at the point T. The tangent at T meets QR at P.

If PT=3.8cm, then the length of QR(in cm) is



A. (a) 3.8

B. (b) 7.6

C. (c) 5.7

D. (d) 1.9

Answer: B





16. In figure, PQ and PR are two tangents to a circle with centre O.

IF $\angle QPR = 46^\circ$, then $\angle QOR$ equals

(a) 67°



A. (a) 67°

B. (b) 134°

C. (c) 44°

D. (d) 46°

Answer: B



17. Two circles touch each other externally at P

. AB is a common

tangent to the circle touching them at A and

The value of $\angle APB$ is

A. (a) 30°

B. (b) 45°

C. (c) 60°

D. (d) 90°

Answer: D

18. Two circles of radii 5 cm and 3 cm touch externally. Find the distance between their centres.

A. 2cm

B.4cm

C. 8cm

D. 16cm

Answer: C

19. IF two circles of radii r_1 and r_2 $(r_2 > r_1)$ touch internally,

then the distance between their centres will be

A. (a)
$$r_1-r_2$$

- B. (b) $r_2 r_1$
- C. (c) $r_1^2 r_2^2$

D. (d)
$$r_2^2 - r_1^2$$

Answer: B



20. The angle subtended by the diameter at any point on the circles is a/an_____angle.

A. (a) *acute*

B. (b) obtuse

C. (c) right

D. (d) reflex

Answer: C



21. In the given figure , ΔABC is an isosceles triangle,

then m(arc AQC)=



B. (b) 120°

C. (c) 60°

D. (d) 15°

Answer: A

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22. For the given figure, which of the following

is true?



A. (a) $\angle ABC \cong \angle APC$

B. (b) $\angle ABC \cong \angle BCP$

C. (c) $\angle BAP \cong \angle APC$

D. (d) $\angle ABP \cong \angle ACP$

Answer: A



23. In the given figure, □ PQRS is a cyclic quadrilateral

such that $\angle PQR = 50^{\,\circ}$ then $\angle PSR$ =

(a) 50° (b) 100° (c) 120° (d) 130°



A. (a) 50°

B. (b) $100^{\,\circ}$

C. (c) $120^{\,\circ}$

D. (d) 130°

Answer: D

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24. For the cyclic quadrilateral shown below, which of the

following is always true?



A. $\angle BCE = \angle BAD$

B. $\angle BCE = \angle BCD$

 $\mathsf{C}. \angle BAD = \angle BCD$

D. $\angle ABC = \angle ADC$

Answer: A



B. $140\,^\circ$

C. 110°

D. 80°

Answer: B



26. In the following figure , m(arc PMQ)=110 $^{\circ}$,

then $\angle PQS$ =



A. (a) $50^{\,\circ}$

B. (b) 55°

C. (c) $110^{\,\circ}$

D. (d) $220^{\,\circ}$





27. A tangent segment PT touching a circle in T and

a secant PAB are as shown in the figure below.

IF TP=12 and PA=4, then AB=

(a) 36 units (b) 32 units (c) 3 units (d) 40 units



- A. (a) 36 units
- B. (b) 32 units
- C. (c) 3 units
- D. (d) 40 units





Additional Problems For Practice

1. Find the length of the tangent segment from a point which

is at a distance of 5 cm from the centre of the

circle of

radius 3cm.

2. In the adjoining figure, point A is the center of the circle. AN=10 cm. Line NM is tangent at M. MN=5 cm. Find the radius.



3. In the following figure ,Point A is the centre of the circle.

Line MN is tangent at point M. IF AN=12cm and

MN=6cm,

determine the radius of the circle.





4. In the given figure circle with centre D touches the sides

of $\angle ACB$ at A and B. If $\angle ACB = 52^{\circ}$,

find measure of $\angle ADB$.



5. In the adjoining figure , Q is the centre of

the circle and

PM, PN are tangent segments to the circle.

IF ${
m }{
m }MPN=40^{\circ}$, find ${
m }{
m }MQN.$





6. Find the angle between two radii at the centre of the circle as shown in the figure. Lines PA and PB are tangents to the circle at other ends of the radii and $\angle APR = 110^{\circ}$



7. Point O is the centre of a circle . Line a and

line b are

parallel tangents to the circle at P and Q. Prove

that

segment PQ is a diameter of the circle.


8. In the adjoining figure, the circle is the incircle of

isosceles ΔABC , where seg AB = seg AC.

Prove that M bisects BC.





9. In the adjoining figure, O is the centre and seg AB is a diameter. At point C on the circle, the tangent CD is drawn. Line BD is tangent at B. Prove that $segOD \mid segAC$





10. If two circles with radii 8 and 3 respectively touch

externally, then find the distance between their centres.

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11. A circle of radius 2 cm touches a circle of radius 10cm internally. Determine the length of a tangent

segment

drawn through the cente of the larger circle to

the smaller

circle.

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12. In the adjoining figure , line PQ is a common tangent to

the externally touching circles and the radii of

two circles

are 25cm and 9cm. Find the length of the

common tangent

segment of these circles.





13. As shown in the adjoining figure , two circles centred at A and B are touching at C. Line passing through C intersects the two circles at M and N

respectively.

Show that seg AM ||seg BN.



14. In the adjoining figure, points A, B,C and D

are on

the circle. The measures of $\angle AOB$ and $\angle BOC$

are 80°

and 75° respectively. Find measure of arc ABC,

arc ADB

and arc BAC.



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15. In the adjoining figure, P is the

circumcentre of the

 $\Delta ABC.m \measuredangle APC = 118^{\circ}$ and

 $m \angle PBC = 45^{\circ}$,

then find:

(i) m(arc BXC)

(ii) m(arc BCA)





16. In the adjoining figure, a rectangle PQRS is

inscribed in

a circle with centre T. Prove that,

(i) arc PQ \cong arc SR

(ii) arc SPQ \cong arc PQR





17. In the adjoining figure, chord LM \cong chord LN, $\angle L = 35^{\circ}$

find:

(i) m(arc MN)



18. In the adjoining figure, A,B and C are three points on

a circle with centre O such that $m ar{\angle} AOB = 110^{\circ}$,

 $m \angle AOC = 120^{\circ}$. Find $m \angle BAC$.





19. In the adjoining figure, O is the centre, seg PQ is diameter,

line AQ is a tangent. If OP=3 and m(arc PM)= 120° ,

determine AP.



20. As shown in the adjoining figure, two chords AB and CD

of the same circle are parallel to each other.

P is the centre of the circle. Show that $\angle CPA$ =

 $\angle DPB.$



21. In the adjoining figure, m (arc XAZ)=m(arc

YBW).

Prove that : XY||ZW



22. In a cyclic quadrilateral ABCD, $\angle B = (5x + 40)^{\circ}$ and $\angle D = (8x + 23)^{\circ}$, then find the measures of $\angle B$ and $\angle D$.

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23. The quadrilateral formed by angle

bisectors of a cyclic quadrilateral is also cyclic.



24. Prove that in a cyclic trapezium, angles at

the base are congruent.



25. In the figure , if m (arc DXE = 100° and

m (arc AYC) $\,=\,40^{\,\circ}$, find $igstar{DBE}$.







26. In the given figure PA=6, PB=4 and PC=8. Find PD.





27. In the adjoining figure. Chord MN and chord RS intersect

each other at point P. If PR=6,Ps=4, MN=11, find PN.





28. In the adjoining figure , chords HI and KJ intersect at

point L. If KL=8,LJ=5 and HI=14, then find the

length of HL.



29. In the adjoining figure, chords CB and ED intersect each

other in point A in the exterior of the circle.

IF CB=5,AB=7,EA=20 and IF ED exceeds AD,

determine ED-AD.





30. In the adjoining figure ,seg PS is a tangent segment.

Line PR is a secant. If PQ=3.6, and QR=6.4, find PS.





31. In the given figure, a tangent segment PA

touching a circle

in A and a secant PBC are shown If AP=15 cm

and

BP=10cm , find the Length of PC.





32. In the following figure , ray PA is the tangent to the circle at point A and PBS is secant . If AP=14,BP=10, find BC.







33. In the adjoining figure, line AP is tangent to

the circle at A,

secant through P intersects chord AY in point

X such that

AP=PX=XY.

IF PQ=1 and QZ=8, then find AX.





Chapter Assessment

1. If two circles with diameter 8cm and 6 cm touch externally,

then the distance between their centres is

A. (a) 2 cm

B. (b) 7 cm

C. (c) 10 cm

D. (d) 14 cm

Answer: B



2. In the given figure , O is the centre of the circle. If m(arc AXB)= 80° ,

then $m \angle AOB$ =



A. (a) 40°

B. (b) 80°

C. (c) $160\,^\circ$

D. (d) 120°

Answer: B



3. In the given figure ,secants AP and CP intersect in point P. If AP=12,PB=5,CP=20, then

DP=



- A. (a) 8
- B. (b) 6
- C. (c) 4

D. (d) 3

Answer: D



B. (b) 50°

C. (c) $100\,^\circ$

D. (d) 150°

Answer: B

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5. In the figure, point A is the centre of the circle and its tangent CD touches the circle at point B, The radius of the circle is 4cm .If

 $m ar{>} BAC = 30^\circ$, then find AC





6. Find the radius of the circle passing through the vertices of a right angled traingle the
lengths of whose perpendicular sides are 8

and 15.



7. In the adjoining figure ,two circles intersect

at points M and N.

Secants drawn through M and N intersect the

circles at points R,S

and P,Q respectively. Prove that: seg SQ||seg





8. In the following figure, a tangent segment PA touching a circle

in A and a secant PBC are shown. If AP=12,BP=9,

find BC.





9. In the given figure, Q is the centre of the circle and PM ,PN are tangent segments to the circle. If

 $\angle MPN = 50^{\circ}$ find $\angle MQN$.





10. In the given figure , O is the centre of the

circle. AB and AC are

tangents to the circle such that BA \perp CA.





11. In the figure, two circles intersect each other in points P and Q. If tangent from point

R touch the circles at S and T, then prove that

RS=RT.



12. Prove that the opposite sides of a quadrilateral circumscribing a

circle subtend supplementary angles at the

centres of the circle.



13. If two equal chords of a circle intersect

within the circle, prove that

the segments of one chord are equal to

corresponding segments

of the other chord.

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14. Prove that, "If chords of congruent circles subtend equal angles at their centre, then the chords are equal."

