



# MATHS

# **BOOKS - TARGET PUBLICATION**

# TRIGONOMETRY

Practice Set 61

**1.** If 
$$\sin \theta = \frac{7}{25}$$
 and  $\cos \theta = \frac{24}{25}$ , then find  $\tan \theta$ .

2. If 
$$an heta = 1$$
, then  $rac{\sin heta + \cos heta}{\sec heta + \cos heta heta} =$ 

A. 1

B. 
$$\frac{1}{2}$$
  
C.  $\frac{\sqrt{3}}{2}$ 

D. 0

Answer: B

View Text Solution

3. Prove that :

$$rac{\sin^2 heta}{\cos heta}+\cos heta=\sec heta$$

**4.** Prove that: 
$$\sqrt{\frac{1-\sin\theta}{1+\sin\theta}} = \{\sec\theta - \tan\theta\}, \text{if}$$
  
 $-\frac{\pi}{2} < \theta < \frac{\pi}{2}$   
 $= -\sec\theta + \tan\theta, \text{if } \frac{\pi}{2} < \theta < \frac{3\pi}{2}$ 

Watch Video Solution

5. prove that  $\cot heta + \tan heta$  =  $\cos e c heta$ .  $\sec heta$ 

#### 6. Prove that

$$egin{aligned} (i) & rac{\sin heta}{(1-\cos heta)} = (\csc heta + \cot heta) \ (ii) & rac{1}{(\sec heta - \tan heta)} = (\sec heta + \tan heta) \end{aligned}$$

7. Prove that  $\sin^4 heta - \cos^4 heta$  =  $1 - 2\cos^2 heta$ 

# Watch Video Solution

8. Prove that :

$$\sec \theta + \tan \theta = \frac{\cos \theta}{1 - \sin \theta} = \frac{1 + \sin \theta}{\cos \theta}$$

A. 
$$\frac{1}{1 + \sin \theta}$$
  
B. 
$$\frac{1}{1 - \sin \theta}$$
  
C. 
$$\frac{\cos \theta}{1 + \sin \theta}$$
  
D. 
$$\frac{\cos \theta}{1 - \sin \theta}$$

#### **Answer: D**



9. 
$$an heta+rac{1}{ an heta}=2$$
 then prove that  $an^2 heta+rac{1}{ an^2 heta}=2$ 

# Watch Video Solution

10. Prove: 
$$rac{ an A}{ig(1+ an^2 Aig)^2}+rac{ ext{cot}\,A}{ig(1+ ext{cot}^2 Aig)^2}=\sin A\cos A$$

**Watch Video Solution** 

11. prove that  $\sec^4 A \left(1 - \sin^4 A \right) - 2 \tan^2 A$ = 1.

**12.** prove that 
$$\frac{\tan\theta}{\sec\theta-1} = \frac{\tan\theta+\sec\theta+1}{\tan\theta+\sec\theta-1}$$





**1.** Solve the following question:(1) A person is stading at a distance of 80 m from a church looking at its top. The angle of elevation is of  $45^{\circ}$ . Find the height of the church.



**2.** From the top of a lighthouse, an observer looking at a boat makes an angle of depression of  $60^{\circ}$ . If the height of the lighthouse is 90m, then find how far is the boat from the lighthouse.

 $\left(\sqrt{3}=1.73
ight)$ 

**3.** Two buildings are facing each other on either side of a road of width 12m. From the top of the first building, which is 10 m high, the angle of elevation of the top of the second is  $60^{\circ}$ . What is the height of the second building?

Watch Video Solution

**4.** Two poles of heights 18 metre and 7 metere are erected on

a ground. The length of the wire fastened at their tops in 22

meters. Find the angle made by the wire with the horizontal.



5. A storm broke a tree and the treetop rested 20 m from the base of the tree, making an angle of  $60^{\circ}$  with the horizontal. Find the height of the tree.



**6.** A kite is flying at a height of 60 m above the ground. The string attached to the kite is temporarily tied to a point on the ground. The inclination of the string with the ground is 60o. Find the length of the string, assuming that there is no sl



Problem Set 6

**1.**  $\sin \theta$ .  $\cos ec\theta$  = ?

A. 1 B. 0 C.  $\frac{1}{2}$ D.  $\sqrt{2}$ 

#### Answer: A



**2.** 
$$\cos ec45^{\circ} = .....$$

A. 
$$\frac{1}{\sqrt{2}}$$

B. 
$$\sqrt{2}$$

C. 
$$\frac{\sqrt{3}}{2}$$
  
D.  $\frac{2}{\sqrt{3}}$ 

#### **Answer: B**



**3.** (3)  $1 + \tan^2 \theta$  =?

A.  $\cot^2 \theta$ 

 $\mathsf{B.}\cos ec^2\theta$ 

 $\mathrm{C.\,sec}^2\,\theta$ 

D.  $\tan^2 \theta$ 

#### Answer: C





**4.** What we see at a higher level from the horizontal line, angle formed is .....,

A. angle of elevation

B. angle of depression

C. 0

D. straight angle.

Answer: A

Watch Video Solution

5. If  $\sin \theta$  = 11/61 find the values of  $\cos \theta$  using trigonometric

identity.



7. If sec  $\theta$  = 13/12, find values of other trigonometric ratios.



8. Prove that :

 $\sec heta(1-\sin heta)(\sec heta+ an heta)=1$ 







12. Prove that :

$$an^4 heta+ an^2 heta=\sec^4 heta-\sec^2 heta$$



13. Prove 
$$rac{1}{1+\sin heta}+rac{1}{1-\sin heta}=2\sec^2 heta$$

Watch Video Solution



$$1+3\sec^2x imes an^2x$$

Watch Video Solution

**15.** Prove the following : 
$$\frac{ an heta}{\sec heta + 1} = \frac{\sec heta - 1}{ an heta}$$

**16.** Prove the following:

$$rac{ an^3 heta-1}{ an heta-1}=\sec^2 heta+ an heta$$



$$rac{\sin heta-\cos heta+1}{\sin heta+\cos heta-1}=rac{1}{(\sec heta- an heta)}.$$

#### Watch Video Solution

**18.** A boy standing at a distance of 48 meters from a building observes the top of the building and makes an angle of elevation of  $30^{\circ}$ . Find the height of the building.



**19.** From the top of a lighthouse, an observer looks at a ship and finds the angle of depression to be  $30^{\circ}$ . If the height of the lighthouse is 100 m, then find how far is that ship from the lighthouse.

Watch Video Solution

**20.** Two buildings are in front of each other on a road of width 15 meters. From the top of the first building, having a height of 12 meters, the angle of elevation of the top of the second building is  $30^{\circ}$ . What is the height of the second building?



**21.** A ladder on the platform of a firebrigade van can be elevated at an angel of  $70^{\circ}$  to the maximum. The length of the ladder can be extended upto 20m. If the platform is 2mabove the ground, find the maximum height from the ground upto which the ladder can reach ( $\sin 70^{\circ} = 0.94$ )



22. While landing at an airport, a pilot made an angle of derpession of  $20^{\circ}$ . Average speed of the plane was 200 km / h. The plane reached the ground after 54 seconds. Find the height at which the plane was when it started landing.  $(\sin 20^{\circ} = 0.342)$ 

**1.** If  $\sin \theta = 7/25$  then find  $\cos \theta$  and  $\tan \theta$ .

**Watch Video Solution** 

2. Solve the following question:(1) A person is stading at a distance of 80 m from a church looking at its top. The angle of elevation is of  $45^{\circ}$ . Find the height of the church.

Watch Video Solution

**3.** Prove :  $(\sec \theta + \tan \theta)(1 - \sin \theta) = \cos \theta$ .

1.  $\cos \theta$ .  $\sec \theta =$ 

A. 0

 $\mathsf{B}.\,\frac{1}{2}$ 

C. 1

D.  $\sqrt{2}$ 

Answer: C



**2.** 
$$\tan\theta$$
.  $\tan(90^{\circ} - \theta)$  =

$$\mathsf{B.} \frac{1}{\sqrt{3}}$$

C. 1

D.  $\sqrt{3}$ 

#### Answer: C



**3.** Choose the correct answer in each of the following questions:

If 
$$\cos \theta = \frac{4}{5}$$
 then  $\tan \theta = ?$   
A.  $\frac{3}{5}$   
B.  $\frac{3}{4}$   
C.  $\frac{4}{3}$ 

#### Answer: B

# Watch Video Solution

**4.** If 
$$\cot heta = rac{7}{8}$$
 , then  $an^2 heta$  =

A. 
$$\frac{7}{8}$$
  
B.  $\frac{8}{7}$   
C.  $\frac{49}{64}$   
D.  $\frac{64}{49}$ 

#### Answer: D

5. If 
$$an heta = rac{4}{3}$$
 , then  $3\sin heta - 4\cos heta$  =



#### Answer: A



6. Which of the following is the value of  $\sec 30^\circ\,$ ?

A. 
$$\sqrt{3}$$

$$\mathsf{B}.\,\frac{1}{\sqrt{3}}$$

C. 
$$\frac{\sqrt{3}}{2}$$
  
D.  $\frac{2}{\sqrt{3}}$ 

#### Answer: D



7. 
$$\frac{2 \tan 30^{\circ}}{1 + \tan^2 30^{\circ}}$$
 =

A.  $\sin 30^{\circ}$ 

B.  $\sin 60^{\circ}$ 

C.  $\cos 60^{\circ}$ 

D.  $an 60^{\,\circ}$ 

#### Answer: B





**8.** 
$$\frac{1 - \cot^2 45^\circ}{1 + \cot^2 45^\circ}$$
 =

A.  $\cos 90^{\circ}$ 

B.  $\sin 90^{\circ}$ 

C.  $\sin 45^{\,\circ}$ 

D.  $\cos 45^{\,\circ}$ 

Answer: A



$$9.1 + \cot^2 \theta = \dots$$

A.  $\sec^2 \theta$ 

 $B.\cos^2\theta$ 

 $C. \cos ec^2 \theta$ 

D.  $\tan^2 \theta$ 

#### Answer: C



10. 
$$an^2(90^\circ- heta)-\cos ec^2 heta=$$

A. 0

B. 1

C. -1

D. 2

#### Answer: C



11. If 
$$\cos heta = rac{24}{25}, ext{ then the value of } \sin heta ext{ is }$$

A. 
$$\frac{7}{24}$$
  
B.  $\frac{7}{25}$   
C.  $\frac{25}{7}$   
D.  $\frac{24}{7}$ 

#### Answer: B



12. If 
$$an heta=rac{3}{4}$$
, then  $\cos^2 heta-\sin^2 heta=rac{7}{25}$  (b) 1 (c)  $-rac{7}{25}$  (d)  $rac{4}{25}$ 

A. 
$$\frac{3}{25}$$
  
B.  $\frac{4}{25}$   
C.  $\frac{7}{25}$   
D.  $\frac{9}{25}$ 

#### Answer: C



A. 
$$\frac{1}{7}$$

B. 
$$\frac{2}{7}$$
  
C.  $\frac{1}{4}$   
D.  $\frac{3}{4}$ 

#### Answer: A



14. Find the value of 
$$\frac{1 + \tan^2 \theta}{1 + \cot^2 \theta}$$
  
A.  $\sec^2 \theta$   
B.  $\cos^2 \theta$   
C.  $\cos ec^2 \theta$   
D.  $\tan^2 \theta$ 

#### Answer: D



15. 
$$(1-\cos^2 heta)\cot^2 heta$$

A.  $\sec^2 \theta$ 

 $B.\cos^2\theta$ 

 $C. \cos ec^2 \theta$ 

D.  $\sin^2 heta$ 

#### Answer: B



**16.** (Sec<sup>2</sup> θ – 1) (Cosec<sup>2</sup> θ – 1) =

A. 0

B.1

C.  $2 \sec^2 \theta$ 

D.  $2\cos ec^2\theta$ 

#### **Answer: B**



17. Write the value of  $\csc^2 \theta (1 + \cos \theta) (1 - \cos \theta)$ .

A. 0

 $\mathsf{C.} \sec^2 \theta$ 

D.  $\sin^2 heta$ 

Answer: B



$$18. \frac{5}{\cot^2 \theta} - \frac{5}{\cos^2 \theta} =$$
A. 5
B.  $\frac{1}{5}$ 
C. -5
D.  $-\frac{1}{5}$ 

#### Answer: C



19. 
$$\frac{\sin \theta}{1 + \cos \theta} =$$
A. 
$$\frac{\cos \theta}{1 - \sin \theta}$$
B. 
$$\frac{1 - \cos \theta}{\sin \theta}$$
C. 
$$\frac{1 - \sin \theta}{\cos \theta}$$
D. 
$$\frac{1 - \cos \theta}{1 + \cos \theta}$$

#### Answer: B



20. If 
$$\cos e c heta - \cot heta = rac{1}{3}$$
 , then  $\cos e c heta + \cot heta$  =

B. 2

C. 3

D. 4

#### Answer: C



**21.** If  $\sin heta + \sin^2 heta = 1$  then  $\cos^2 heta + \cos^4 heta$  is equal to

A. 0

B. 1

C. -1

D. 2

#### Answer: B



22. If  $\sin heta + \cos heta = m$  and  $\sin heta - \cos heta = n$  , then

A. 
$$m^2+n^2=1$$

B. 
$$m^2-n^2=1$$

$$\mathsf{C}.\,m^2+n^2=2$$

D. 
$$m^2-n^2=2$$

#### Answer: C

**23.** When we see below the horizontal line , then the angle formed is ......

A. A Zero degree angle

B. the angle of depression

C. the angle of elevation

D. a straight angle

#### Answer: B



**24.** If a pole 12 m high casts a shadow  $4\sqrt{3}m$  long on the ground then the sun's elevation is

A.  $30^{\circ}$ 

B.  $45^{\circ}$ 

C.  $60^{\circ}$ 

D.  $90^{\circ}$ 

Answer: C

Watch Video Solution

**25.** A kite is flying at a height 80 m above the ground . The string of the kite which is temporarily attached to the ground makes an angle  $45^{\circ}$  with the ground. If there is no slack in the string, then the length of the string is

B.  $40\sqrt{2}$ 

C. 80 m

D.  $80\sqrt{2}$ 

Answer: D



**26.** The angle of elevation of top of the tower from a point P on the ground is  $30^{\circ}$ . If the points is 45 m away from the foot of the tower, then the height of the tower is

A. 45 m

B. 15 m

C.  $15\sqrt{3}$ 

D.  $20\sqrt{3}m$ 

#### Answer: C



**27.** The angle of depression of a ship as observed from the top of a lighthouse is  $45^{\circ}$ . If the height of the lighthouse is 200 m, then what is the distance of the ship from the foot of the lighthouse ?

A. 200 m

B. 400 m

C. 100 m

D.  $200\sqrt{3}m$ 

#### Answer: A

**Watch Video Solution** 

Additional Problems For Practice Based On Practice Set 61

1. If 
$$\sin heta = rac{20}{29}$$
 , then find the value of  $\cos heta.$ 

### Watch Video Solution

**2.** If  $\sin heta = rac{8}{17}$  , where heta is an acute angle, find the value of

 $\cos \theta$  by using identities.



**3.** If  $\cos \theta = \frac{3}{5}$ , where ' $\theta$ ' is an acute angle. Find the value of  $\sin \theta$ .

### Watch Video Solution

**4.** If 
$$\sec heta = rac{25}{7}$$
 then find the value of  $an heta$ 

Watch Video Solution

5. If  $\cot \theta = \frac{8}{15}$  then find the values of  $\sin \theta$  and  $\sec \theta$ .

6. If  $\sin heta = rac{5}{13}, \,$  where heta is an acute angle , find the values of

other trigonometric ratios using identities .

### Watch Video Solution

7. If  $an heta = rac{20}{21}$  , then find the values of other trigonometric

ratios .

Watch Video Solution

8. If  $5\sin heta-12\cos heta=0$  , find the values of

 $\sec \theta$  and  $\cos ec\theta$ .

9. If  $3\sin heta-4\cos heta=0$  , then find the values of

 $\tan \theta$ ,  $\sec \theta$  and  $\cos ec\theta$ .



11. If 
$$\sin heta = rac{4}{5}$$
 , find the value of  $rac{4 an heta - 5 \cos heta}{\sec heta + 4 \cot heta}$ 

# Watch Video Solution

#### 12. Prove that :

$$rac{\sin heta}{1-\cos heta}=\cos ec heta+\cot heta$$



13. Prove that :

$$an heta-\cot heta=rac{2\sin^2 heta-1}{\sin heta\cos heta}$$



14. Prove that : 
$$\sqrt{rac{1+\cos heta}{1-\cos heta}}=\cos ec heta+\cot heta$$



16. Prove that 
$$\sec x + \tan x = \sqrt{rac{1 + \sin x}{1 - \sin x}}$$

Watch Video Solution

**17.** Prove that :

$$\sec^2 heta - \cos^2 heta = \sin^2 heta (\sec^2 heta + 1)$$

Watch Video Solution

18. Prove that :

$$\cos^4 heta-\cos^2 heta=\sin^4 heta-\sin^2 heta$$

19. Prove that  $\sin^6 heta + \cos^6 heta = 1 - 3\sin^2 heta\cos^2 heta$ 

**Watch Video Solution** 

20. Prove that :

$$\sin^4 heta+\cos^4 heta=1-2\cos^2 heta+2\cos^4 heta$$

Watch Video Solution

21. 
$$\frac{\tan\theta}{1-\cot\theta} + \frac{\cot\theta}{1-\tan\theta} = 1 + \sec\theta\cos ec\theta$$

# Watch Video Solution

22. 
$$\frac{\tan\theta}{1-\cot\theta} + \frac{\cot\theta}{1-\tan\theta} = 1 + \sec\theta\cos ec\theta$$



**26.** Eliminate heta if  $x = a \cot \theta + b \cos ec heta$ 

and  $y = a \cos ec\theta + b \cot \theta$ .



1. An observer at a distance of 10 m from a tree looks at the top of the tree , the angle of elevation is  $60^\circ$  .

What is the height of the tree ? (  $\sqrt{3}=1.73$  )



2. From the top of a building , an observer is looking at a

scooter

parked at some distance away , makes an angle of depression of  $30^\circ$  . If the height of the building is 40 m , find how far the scooter is from the building.  $\left(\sqrt{3}=1.73
ight)$ 



**3.** (8) From the top of a lighthouse, an observer looks at a ship and finds the angle of depression to be  $60^{\circ}$ . If the lighthouse is 90 m, then find how far is that ship from the lighthouse? ( $\sqrt{3} = 1.73$ )

Watch Video Solution

**4.** A person observed the angle of elevation of the top of a tower as  $30^{\circ}$ . He walked 50m towards the foot of the tower along level ground and found the angle of elevation of the

top

of the tower as  $60^\circ$  . Find the height of the tower.



5. A person standing on the bank of a river observes that the angle of elevation of the top of a tree standing on the opposite bank is  $60^{\circ}$ . When he moves 40 m away from the bank, he finds the angle of elevation to be  $30^{\circ}$ . Find the height of the tree and the width of the river. ( $\sqrt{3} = 1.73$ )



**6.** To find the width the river, a man observes the top of a tower on

the opposite bank making an angle of elevation  $61^{\,\circ}.$  When he

moves 50m backward from bank and observes the same top of the

tower, his line of vision makes an angle of elevation fo  $35\,^\circ$  .

Find the height of the tower and width of the river.  $( an 61^\circ = 1.8, 35^\circ = 0.7)$ 



**7.** Two buildings are in front of each other on either side of a road of width 10 metres. From the top of the first building which

is 30 metres high, the angle of elevation to the top of the second

is  $45^{\circ}$ . What is the height of the second building?



8. The horizontal distance between two poles is 15m. The angle of depression of the top of the first pole as seen from the top of the second pole is  $30^{\circ}$ . If the height of the second pole is 24 m, find the height of the first pole. ( $\sqrt{3} = 1.732$ )



**9.** Roshani saw an eagle on the top of a tree at an angle of elevation of  $61^{\circ}$ , while she was standing at the door of her house. She went on the terrace of the house so that she could see it clearly. The terrace was at a height of 4m. While observing the eagle from there the angle of elevation was  $52^{\circ}$ . At what height from the ground was the eagle?  $\tan 61^{\circ} = 1.8$ ,  $\tan 52^{\circ} = 1.28$ ,  $\tan 29^{\circ} = 0.55$ ,  $\tan 38^{\circ} = 0.78$ ) **10.** From the top of a building 60m high the angles of depression of

the top and the bottom of a tower are observed to be  $30^0$  and  $60^0$ 

. Find the height of the tower.

Watch Video Solution

11. A ship of height 24 m is sighted from a lighthouse. From the top of the lighthouse the angle of depression to the top of the mast and base of the ship is  $30^{\circ}$  and  $45^{\circ}$  respectively. How far is the ship from the lighthouse ? ( $\sqrt{3} = 1.73$ )

**12.** A tree breaks due to storm and the broken part bends so that the top

of the tree touches the ground making an angle of  $30^\circ$  with the ground.

The distance between the foot of the tree to the point where

the top

touches the ground is 10m. Find the height of the tree.

Watch Video Solution

**13.** A tree is broken by the wind. The top of that tree struck

the ground

at an angle of  $30^\circ$  and at a distance of 30 m from the root.

Find the height of the whole tree. (  $\sqrt{3}$  = 1.73)

1. 
$$\cot 60^\circ$$
 =

A. 
$$\sqrt{3}$$
  
B.  $\frac{1}{\sqrt{3}}$   
C.  $\sqrt{2}$   
D.  $\frac{1}{\sqrt{2}}$ 

#### Answer: B



**2.** 
$$\tan \theta$$
.  $\cot \theta =$ 

A. 0

B.  $\sqrt{3}$ 

$$\mathsf{C}.\,\frac{1}{\sqrt{3}}$$

D. 1

Answer: D

Watch Video Solution

3. When we see at a lower level , from the horizontal line ,

angle formed is .....

A. angle of elevation

B. angle of depression

C. 0

D. straight angle.

#### Answer: B



Watch Video Solution

**4.** If the distance of a point from the tower is equal to the height of the tower , then find the angle of elevation of the top of the tower from that point .

• Watch Video Solution  
5. If 
$$\cos ec\theta = \frac{13}{12}$$
, then find the values of  $\cot \theta$  and  $\sin \theta$ .

**6.** Prove the identity  $\sin^2 heta+\cos^2 heta=1$  with the help of

given figure .



Watch Video Solution

7. A person standing at a distance of 90 m from a church observes the angle of elevation of its top to be  $45^{\circ}$  . Find the height of the chruch .

**8.** 
$$\frac{ an heta + \sin heta}{ an heta - \sin heta} = rac{\sec heta + 1}{\sec heta - 1}$$

### Watch Video Solution

9. If 
$$\cos \theta + \frac{1}{\cos \theta} = 4$$
 , then prove that  $\cos^2 \theta + \frac{1}{\cos^2 \theta} = 14.$ 

Watch Video Solution

10. Prove that :

 $\operatorname{sec}^6 x - an^6 x = 1 + 3 \operatorname{sec}^2 x imes an^2 x$ 

**11.** A tree breaks due to storm and the broken part bends, so that

the top of the tree touches the ground making an angle of  $60^{\,\circ}$ 

with the ground . The distance from the foot of the tree to

the point

where the top touches the ground is 5 metres .

Find the height of the tree. ( $\sqrt{3}=1.73$ )



12. Two buildings are in front of each other on a road of width 15 metres. From the top of the first building , having a height of 12 metre , the angle of elevation of the top of the second building is  $30^{\circ}$ . What is the height of the second building ?





14. A straight highway leads to the foot of a tower. A man standing at the top of the tower observes a car at an angle of depression of  $30^0$ , which is approaching the foot of the tower with a uniform speed. Six seconds later, the angle of depression of the car is found to be  $60^0$ . Find the time taken by the car to reach the foot of the tower from this point.





 $y = a \cot \theta + b \cos ec \theta.$