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## MATHS

## BOOKS - PSEB

## AREAS RELATED TO CIRCLES

Exercise

1. The radii of two circles are 19 cm and 9 cm
respectively, Find ihe radius of the circle which
has circumference equal to the sum of the
circumferences of the two circles. Unless stated otherwise, use $\pi=\frac{22}{7}$.

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2. The radii of two circles are 8 cm and 6 cm respectively. Find the radius of the circle having area equal to the sum of the areas of the two circles. Unless stated otherwise, use $\pi=\frac{22}{7}$.
3. Fig. depicts an archery target marked with its five scoring areas from the centre outwards as Gold, Red, Blue, Black and White. The diameter of the region representing Gold score is 21 cm and each of the other bands is
10.5 cm wide. Find the area of each of the five scoring regions.

4. The wheels of a car are of diameter 80 cm each. How many complete revolutions does each wheel make in 10 minutes when the car is travelling at a speed of 66 km per hour ?

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5. Tick the correct answer in the following and
justify your choice : If the perimeter and area
of a circle are numerically equal, then the radius of the circle is
A. 2 units
B. $\pi$ units
C. 4 units
D. 7 units

Answer:
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6. Find the area of sector of a circle with radius

6 cm , if angle of the sector is $60^{\circ}$.

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7. Find the area of a quadrant of a circle whose circumference is 22 cm .

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8. The length of the minute hand of a clock is

14 cm . Find the area swept by the minute hand in 5 minutes.

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9. A chord of a circle of radius 10 cm subtends
a right angle at the centre. Find the area of
the corresponding :(i) minor segment
major sector. (Use $\pi=3.14$ )
10. In a circle of radius 21 cm , an arc subtends an angle of $60^{\circ}$ at the centre. Find the length of the arc

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11. In a circle of radius 21 cm , an arc subtends
an angle of $60^{\circ}$ at the centre. Find area of the sector formed by the arc.
12. In a circle of radius 21 cm , an arc subtends an angle of $60^{\circ}$ at the centre. Find area of the segment formed by the corresponding chord.

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13. A chord of a circle of radius 15 cm subtends
an angle of $60^{\circ}$ at the centre. Find the areas
of the corresponding minor and major segments of the circle. (Use $\pi=3.14$ and $\sqrt{3}=1.73)$
14. A chord of a circle of radius 12 cm subtends an angle of $120^{\circ}$ at the centre. Find the area of the corresponding segment of the circle.
(Use $\pi=3.14$ and $\sqrt{3}=1.73$ )

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15. A horse is tied to a peg at one corner of a square shaped grass field of side 15 m by means of a 5 m long rope ( see Fig, 12. 11 ). Find
(i) the area of that part of the field in which
the horse can graze,(ii) the increase in the grazing area if the rope were 10 m long instead of 5 m .(Use $\pi=3.14$ )


## Fig. 12.11

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16. A brooch is made with silver wire in the
form of a circle with diameter 35 mm .The wire is also used in making 5 diameters which divide the circle into 10 equal sectors as shown in Fig. 12.12. Find : (i) the total length of the silver wire required, (ii) the area of each

## sector of the brooch.



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17. A car has two wipers which do not overlap.

Each wiper has a blade of length 25 cmsweeping throughanangle of $115^{\circ}$. Find the total area cleaned at each sweep of the blades.

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18. To warn ships for underwater rocks, a
lighthouse spreads a red coloured light over a sector of angle $80^{\circ}$ to a distance of 16.5 km .

Find the area of the sea over which the ships are warned. (Use $\pi=3.14$ )

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19. A round table cover has six equal designs as shown in fig. If the radius of the cover is 28
cm , find the cost of making the designs at the
rate of ? 0.35 per $\mathrm{cm}^{2}$. (use $\sqrt{3}=1.7$ )


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20. Area of sector of angle $p$ (in degrees) of a circle with Radius R is :
A. $\frac{p}{180} \times 2 \pi R$
B. $\frac{p}{180} \times \pi R^{2}$
C. $\frac{p}{360} \times 2 \pi R$
D. $\frac{p}{720} \times 2 \pi R^{2}$

Answer:

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21. Find the area of the shaded region in Fig., if $P Q=24 \mathrm{~cm}, \mathrm{PR}=7 \mathrm{~cm}$ and O is the centre of
the circle.


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22. Find the area of the shaded region in Fig.
12.20, if radii of the two concentric circles with
centre $O$ are 7 cm and 14 cm respectively and
$\angle A O C=40^{\circ}$.


## Fig. 12.20

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23. Find the area of the shaded region in fig, if
$A B C D$ is a square o fside 14 cm and APD and

## BPC are semicircles.



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24. Find the area of the shaded region in fig.,
where a circular arc of radius 6 cm has been
drawn with vertex O of an equilateral triangle

## OAB of side 12 cm as centre.



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25. From each corner of a square ofside 4 cm a quadrant of a circle of radius 1 cm is cut and also a circle of diameter 2 cm is cut asshown in
fig. Find the area of the remaining portion of the square.

26. In a circular table cover of radius 32 cm , a design is formed leaving an equilateral triangle $A B C$ in the middle as shown in fig.

Find the area of the design (shaded region).


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27. In fig., $A B C D$ is a square of side 14 cm . With centres $A, B, C$ and $D$, four circles are drawn
such that each circle touch externally two of
the remaining three circles. Find the area of the shaded region.


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28. Fig. depicts a racing track whose left and right ends are semicircular. The distance between the two inner parallel line segments
is 60 m and they are each 106 m long. If the track is 10 m wide, find the distance around the track along its inner edge and the area of the track.

29. In Fig. 12.27, $A B$ and $C D$ are two diameters of a circle (with centre O ) perpendicular to each other and OD is the diameter of the smaller circle. If $\mathrm{OA}=7 \mathrm{~cm}$, find the area of the shaded region.


Fig. 12.27
30. The area of an equilateral triangle $A B C$ is
$17320.5 \mathrm{~cm}^{2}$. With each vertex of the triangle
as centre, a circle is drawn with radius equal to
half the length of the side of the triangle (see
Fig. 12.28). Find the area of the shaded region.
(Use $\pi=3.14$ and $\sqrt{3}=1.73205$ )


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31. On a square handkerchief, nine circular designs each of radius 7 cm are made (see Fig.
12.29). Find the area of the remaining portion of the handkerchief.


Fig. 12.29
32. In Fig. $12.30, \mathrm{OACB}$ is a quadrant of a circle
with centre O and radius 3.5 cm . If $\mathrm{OD}=2 \mathrm{~cm}$,
find the area of the (i) quadrant OACB, (ii)
shaded region.


## Fig. 12.30

33. In Fig. 12.31, a square $O A B C$ is inscribed in a quadrant $O P B Q$. If $O A=20 \mathrm{~cm}$, find the area of the shaded region.(Use $\pi=3.14$ )


## Fig. 12.31

34. $A B$ and $C D$ are respectively arcs of two concentric circles of radii 21 cm and 7 cm and centre $O$. If $\mathrm{ZAOB}=30^{\circ}$, find the area of the

## shaded region.



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35. In fig., $A B C$ is a quadrant of a circle of radius 14 cm and a semi circle is drawn with $B C$
as diameter. Find the area of the shaded region.


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## 36. Calculate the area of the designed region

 in fig. common between the two quadrants of circles of radius 8 cm each.

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Example

1. The cost of fencing a circular field at the rate of ₹ 24 per metre is ₹ 5280 . The field is to be ploughed al the rate of ₹ 0.50 per $m^{2}$. Find the cost of ploughing the field (Take $\pi=\frac{22}{7}$ ).

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2. Find the area of the sector of a circle with ratdius 4 cm and of angle $30^{\circ}$. Also, find ihe area of the corresponding major sector (Use $\pi$ $=3.14)$.
3. Find the area of ihe segment AYB shown in

Fig. 12.9 if radius of the circle is 21 cm and
$\angle A O B=120^{\circ}$.(Use $\pi=\frac{22}{7}$ )


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4. In Fig, 12.15, two circular flower beds have been shown on two sides of a square lawn
$A B C D$ of side 56 m . If the centre of each circular flower bed is the point of intersection

O of the diagonals of the square lawn, find the
sum of the areas of the lawn and the flower beds.

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5. Find the area of the shaded region in Fig.
12.16. where $A B C D$ is a square of side 14 cm .


## Fig. 12.16

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6. Find the area of the shaded design in Fig.
12.17, where $A B C D$ is a square of side 10 cm and
semicircles are drawn with each side of the square as diameter. (Use $\pi=3.14$ )


## Fig. 12.17

$\square$

