



# MATHS

# **BOOKS - NAGEEN PRAKASHAN ENGLISH**

# LINEAR INEQUALITIES



**1.** Solve the inequation 3x-8 < -2 and represent the solution on the number line when





**6.** solve the inequation  $rac{x-2}{x+5} > 2.$ 



9. solve : 
$$|3x-2| \leq 1$$

10. Solve : 
$$\displaystyle rac{2}{|x-3|} > 1, x 
eq 3$$

11. Solve: 
$$rac{-1}{|x|-2} \geq 1, where x \in R, x 
eq \pm 2.$$

12. solve: 
$$|x-2|+|x-4|\geq 8$$

13. solve 
$$:rac{|x-1|}{x+1} < 1$$
  
A.  $x \in (-\infty, -1) \cup (0,\infty)$   
B.  $x \in (-\infty, -1] \cup (0,\infty)$   
C.  $x \in (-\infty, -1) \cup [0,\infty)$   
D.  $x \in (-\infty, \infty)$ 

#### **Answer: A**



**14.** Find all pairs of consecutive even numbers which are greater than 8 and their sum is smaller then 27.

Watch Video Solution

**15.** A student scores 65, 62 70 marks is 3 subjects. Find the minimum marks scored by him in 4th subject to get an average of 64 minimun.

**16.** The largest side of a triangle is twice the smallest side. Its largest side is 3 cm more than the third side. Find the minimum length of the smallest side if the minimum perimeter of the triangle is 62 cm.



17. IQ of a person is given by the formula  $IQ = \frac{MA}{CA} \times 100$  where MA = mental age and CA = chronological age. If IQ for a group of 10

years children is given by the inequation  $70 \leq IQ \leq 140$ , find the range of their mental age.

# Watch Video Solution

**18.** A solution is to be kept between  $59^{\circ}F$  and  $77^{\circ}$  F. What is the range of temperature in degree celcius (C) if the Celcius-farhenheit conversion formula is:

$$F=rac{9}{5}C+32$$

**19.** A manufacturer has 600 liters of 12% solution of acid. How many litres of a 30% acid solution must be added to it so that the acid content in the resulting mixture will be more then 15% but less than 18%?

Watch Video Solution

20. Solve the following inequation graphically:

 $2x + 3y \leq 6$ 

**21.** solve the inequation  $2x - y \geq 3$  by graphical

method.



**22.** Solve the inequation x + y < 5 by graphical

method.



**23.** Solve the following system of linear

inequation

graphically:





**1.** Solve the inequation 3x - 2 < 5 If (i)  $x \in N$ (ii)  $x \in R$  and represent the solution on the number line



- **2.** Solve the inequation  $12x\,<\,50$  lf (i) x  $\,\in\,$  Z (ii)
- $x~\in~R$  and represent the solution on the

number line



**3.** Solve the inequation 3x + 8 > 2 If (i)  $x \in N$ (ii)  $X \in R$  and represent the solution on the number line



**4.** Solve the inequation  $6x - 5 \le 7$  If (i)  $x \in I$ (ii)  $x \in R$  and represent the solution on the number line

5. Solve the inequation 30x < 200 If (i)  $x \in Z$ (ii)  $x \in N$  and represent the solution on the number line



- 6. Solve the inequation  $5x-5 \leq -5$  If (i) x  $\,\in\,$
- z (ii) x in R and represent the solution on the

number line



7. Solve the inequation 3x-7 < 5x-3 lf x  $\,\in\,$ 

R and represent the solution on the number line



**8.** Solve the inequation  $3(x-1) \leq 2(x-3)$  If x

 $\in \ {
m R}$  and represent the solution on the number

line

9. Solve the inequation  $5x-2 \geq 3x-1$  If  $\mathsf{x}~\in$ 

R and represent the solution on the number line



10. Solve the inequation 2x + 5 > -5x + 12 If

 $x \in R$  and represent the solution on the

number line

11. Solve : 
$$rac{5-2x}{3}+5\leq rac{x}{6}$$



12. solve : 
$$rac{3x-4}{2}+1 \geq rac{x+1}{4}$$

13. Solve : 
$$3\left(rac{3x}{5}+4
ight)\geq 2(x-6)$$

14. Solve the inequalities for real x :  

$$\frac{x}{4} < \frac{(5x-2)}{3} - \frac{(7x-3)}{5}$$
Watch Video Solution



16. Solve 
$$:rac{x}{6} \geq rac{8-3x}{2}+4$$

17. Solve 
$$: x + rac{x}{2} + rac{x}{3} > 11$$

18. Solve : 
$$rac{3x}{5} - rac{2(x-2)}{3} \leq 1$$

Watch Video Solution

**19.** Solve : 
$$2(5x - 7) \ge 3(4x - 5)$$

20. Solve : 
$$\frac{5x}{4} - 1 \le \frac{4x - 1}{3}$$
  
Watch Video Solution  
21. Solve :  $\frac{5x - 2}{3} < \frac{4x - 7}{2}$   
Watch Video Solution

22. Solve : 
$$rac{x}{4}-1 < rac{x}{5}+2$$

23. Solve : 
$$rac{1}{x-3} < 0$$

24. Solve : 
$$\displaystyle rac{x-1}{x-2} > 1$$

25. Solve : 
$$rac{2}{x+3} \geq 0$$

26. Solve : 
$$rac{x+2}{x+1} < 0$$

27. Solve : 
$$rac{2x-1}{x+2} \leq 3$$









**31.** Solve 
$$:rac{2x-1}{2}\leq 2x+rac{1}{2}\leq rac{11}{2}+x$$

**32.** Solve : 
$$6 \leq -3(2x-4) < 12$$



33. Solve : 
$$-12 \leq 4 + rac{3x}{5} \leq 2$$



34. Solve : 
$$|x-3| \leq 1$$

#### A.

C.

D.

Answer: N/a

Watch Video Solution

#### **35.** Solve : |x+2| < 3



**36.** Solve : 
$$|2x - 1| > 2$$



37. Solve : 
$$\left|rac{1}{2x-1}
ight|\leq 3, x
eq 1/2$$

38. Solve : 
$$\displaystyle rac{2}{|x-3|} > 1, x 
eq 3$$

39. Solve 
$$: rac{|x|-1}{|x|-2} \ge 0, x 
eq \pm 2$$



40. Solve : 
$$\frac{|x+4|+x}{x+1} > 1, x \neq -1$$
  
Watch Video Solution  
41. Solve :  $|x-1|+|x-2| \ge 3$   
Watch Video Solution  
42. If x satisfies  
 $|x-1|+|x-2|+|x-3| > 6$ , then



**44.** Find all pairs of consecutive odd integers both of which are smaller than 12 and their sum is more than 11.



**45.** Find all pairs of consecutive even integers both of which are greater than 7 and their sum is less than 25.

Watch Video Solution

**46.** Find all pairs of consecutive even integers both of which are greater than 6 and their sum is less than 27.

**47.** A student obtained 60, 62, 64 and 66 marks in 4 subjects in an examination. Find the minimum marks he should get in 5th subject to have an average of at least 65 marks.

Watch Video Solution

**48.** A student obtained 62 and 48 marks in the first and secound examinations of class XI. Find the minimum marks he should get in annul examination to have an average of at least 60 marks.



**49.** The water acidity in a pool is considered normal when the average pH reading of three daily measurements is between 7.2 and 7.8. If the first tow pH reading are 7.48 and 7.85, find the range of pH value for the third reading that will result in the acidity level being normal.



**50.** The longest side of a triangle is three times the shortest side and the third side is 2 cm shorter than the longest side if the perimeter of the triangles at least 61 cm, find the minimum length of the shortest side.

Watch Video Solution

**51.** A man wants to cut three lengths from a single piece of board of length 91cm The second length is to be 3 cm longer than the shortest and the third length is to be twice as long as the

shortest. What are the possible lengths of the

shortest board



52. A solution is to be kept between  $50^{\circ}F$  and  $68^{\circ}F$ . What is the range of temperature in degree celcius if Celciusfarhenheit conversion formual is :  $F = \frac{9}{5}C + 32$ 

53. A solution is to be kept between  $40^{\circ}C$  and  $60^{\circ}C$ . What is the range of temperature in farhenheit if Celcius-farhenheit conversion formual is :  $F = \frac{9}{5}C + 32$ 



Watch Video Solution

54. How may litres of water will have to be added to 1125 litres of the 45% solution of acid so that the resulting mixture will contain more than 25% but less than 30% acid content?



**55.** A solution of 8% boric acid is to be diluted by adding a 2% boric acid solution to it. The resulting mixture is to be more than 4% but less than 6% boric acid. If there are 640litres of the 8% solution, how many litres of 2% solution will have to be added?



56. If the cost and revenue funcation of a product are respectively C(x)=5x+700 and R(x)=15x+100 , where x is the number of

products then what will be the value of x to get

profit ?



#### **59.** x + 4y > 8



**60.** 
$$3y - 5x < 15$$



**61.** 
$$2x + y \ge 0$$

62. 
$$2x + y \le 6$$
,  $x + 2y \le 8$ ,  $x \ge 0$ ,  $y \ge 0$   
Watch Video Solution  
63. Solve the following system of inequations  
graphically  
 $x + y \le 10$ ,  $x + 3y \le 15$ ,  $x \ge 0$ ,  $y \ge 0$   
Watch Video Solution

## **64.** $x + y \leq 10, 4x + 3y \leq 24, x \geq 0, y \geq 0$



#### 65. $x+2y\leq 40,$ $2x+y\leq 40,$ $x\geq 0,$ $y\geq 0$

# Watch Video Solution

#### **66.** $2x + y \ge 6, x + 2y \ge 8, x \ge 0, y \ge 0$

#### Watch Video Solution

67. Show that the following system of linear inequalities has no solutin $x+2y\leq 3,\,3x+4y\geq 12,\,x\geq 0,\,y\geq 1.$ 



**69.** Solve the Following System of Inequalities Graphically

 $3x+4y\leq 60, x\geq 2y, x\geq 1, y\geq 0$ 

70. Solve the Following System of Inequalities Graphically $3x + 2y \le 6, x \ge 1, y \ge 2$ 

Watch Video Solution

**71.** Solve the Following System of Inequalities Graphically

 $x+y\leq 9, x>y, x\geq 0, y\geq 0$ 

#### 72. $x-y\leq 2, x+y\leq 4, x\geq 0, y\geq 0$



#### Watch Video Solution







**76.** Solve the given linear inequality and specify the bounded region.

 $2x+y\geq 2, x-y\leq 1, x+2y\leq 8, x\geq 0, y\geq 0$ 



**Ncert Question** 

1. Solve 24x < 100, when (i) x is a natural number. (ii) x is an integer. Watch Video Solution **2.** Solve 12x > 30, when (i) x is a natural number. (ii) x is an integer Watch Video Solution

**3.** Solve 5x - 3 < 7, when (i) x is integer. (ii) x is

a real number.



5. solve the inequalities for real x ,

4x + 3 < 5x + 7



8. 
$$3(2-x)\geq 2(1-x)$$





11. solve the inequalities for real x : $rac{3(x-2)}{5} \leq rac{5(2-x)}{3}$ 



- **13.** Solve the inequalities for real x :
- 2(2x+3)-10 < 6(x-2)

14.37 
$$-(3x+5) \ge 9x-8(x-3)$$



15. 
$$rac{x}{4} < rac{(5x-2)}{3} - rac{(7x-3)}{5}$$

16. 
$$rac{(2x-1)}{3} \geq rac{(3x-2)}{4} - rac{(2-x)}{5}$$

17. 
$$3x - 2 < 2x + 1$$

**18.** 
$$5x - 3 \ge 3x - 5$$

#### Watch Video Solution

**19.** 
$$3(1-x) < 2(x+4)$$





**21.** Ravi obtained 70 and 75 marks in first two unit test. Find the minimum marks he should get in the third test to have an average of at least 60 marks.



**22.** To receive Grade A in a course, one must obtain an average of 90 marks or more in five examinations (each of 100 marks). If Sunita s marks in first four examinations are 87, 92, 94 and 95, find minimum marks that Sunita must obtain m fifth examin



**23.** Find all pairs of consecutive odd positive integers both of the which are taller than 10 such that their sum is more than 11.



**24.** Find all pairs of consecutive even positive integers, both of which are larger than 5, such that their sum is less than 23.



**25.** The longest side of a triangle is three times the shortest side and the third side is 2 cm shorter than the longest side. If the perimeter of

the triangle is at least 61 cm, find the minimum

length of the shortest side.



**26.** A man wants to cut three lengths from a single piece of board of length 91cm The second length is to be 3 cm longer than the shortest and the third length is to be twice as long as the shortest. What are the possible lengths of the shortest board



27. Shade the region given by inequality

x+y < 5



28. Shade the region given by inequality

· · · · ·

 $2x + y \ge 6$ 



**29.** 
$$3x + 4y \le 12$$

A 4 4 4 4 4 4 4 4



#### **30.** GIVEN INEQUATION: $y+8 \geq 2x$



31. 
$$x-y\leq 2$$

> Watch Video Solution

**32.** 
$$2x - 3y > 6$$

33. 
$$-3x+2y\geq -6$$

**34.** 
$$3y - 5x < 30$$



**35.** 
$$y < -2$$





37. plot 
$$x \geq 3, y \geq 2$$

38. 
$$3x+2y\leq 12, x\geq 1, y\geq 2$$

39. 
$$2x+y\geq 6,$$
  $3x+4y\leq 12$ 



**41.** Solve the linear inequalities

2x-y>1, x-2y<1

#### 42. $x+y\leq 6, x+y\geq 4$

#### Watch Video Solution

#### **43.** $2x + y \ge 8, x + 2y \ge 10$

#### Watch Video Solution

44. Find common region of given inequation

 $x+y\leq 9, x>y, x\geq 0$ 

45. Solve the system of inequalities graphically :

 $5x+4y\leq 20, x\geq 1, y\geq 2$ 

Watch Video Solution

46. Find the common region of given inequation

 $3x+4y\leq 60, x+3y\leq 30, x\geq 0, y\geq 0$ 

**47.** Solve the linear inequalities.

$$2x+y\geq 4, x+y\leq 3, 2x-3y\leq 6$$

#### Watch Video Solution

**48.** Show that the following system of linear inequalities has no solutin  $x+2y\leq 3, 3x+4y\geq 12, x\geq 0, y\geq 1.$ 

#### Watch Video Solution

49.  $4x+3y\leq 60, y\geq 2x, x\geq 3, x, y\geq 0$ 



**50.** Show the common solution of given inequalities and shade the region bounded by them .

 $3x+2y \leq 150, x+4y \leq 80, x \leq 15, y \geq 0, x \geq 0$ 

#### Watch Video Solution

51.

 $x+2y\leq 10, x+y\geq 1, x-y\leq 0, x\geq 0, y\geq 0$ 

**Miscellaneous Exercise** 

1. 
$$2 \leq 3x-4 \leq 5$$
 find x

Watch Video Solution

**2.** 
$$6 \leq -3(2x-4) < 12$$

**3.** 
$$-3 \le 4 - \frac{7x}{2} \le 10$$

$$4.-15 < \frac{3(x-2)}{5} \le 0$$

# Watch Video Solution

5. 
$$-12 < 4 - \frac{3x}{-5} \le 2$$

6.7 
$$\leq rac{(3x+11)}{2} \leq 11$$





## 8. 2(X-1) < X+5, 3(X+2) > 2-X



# **11.** A solution is to be kept between 68 oF and 77 oF . What is the range in temperature in

degree Celsius (C) if the Celsius / Fahrenheit (F) conversion formula is given by  $F=rac{9}{5}C+32?$ 



Watch Video Solution

**12.** A solution of 8% boric acid is to be diluted by adding a 2% boric acid solution to it. The resulting mixture is to be more than 4% but less than 6% boric acid. If there are 640litres of the 8% solution, how many litres of 2% solution will have to be added?

**13.** How may litres of water will have to be added to 1125 litres of the 45% solution of acid so that the resulting mixture will contain more than 25% but less than 30% acid content?



14. IQ of a person is given by formula: IQ  $= \frac{MA}{CA} \times 100, \text{ where } MA \text{ is mental age and}$ CA is chronological age. If  $80 \leq IQ \leq 140$  for a group of 12 year children, find the range of their mental age.

