

India's Number 1 Education App

MATHS

BOOKS - S CHAND MATHS (ENGLISH)

BINOMIAL THEOREM



1. The number of terms in the expansion of

$$\left(1+2x+x^2
ight)^5+\left(1+4y+4y^2
ight)^5$$
 after

simplification is

A. (a) 12

B. (b) 120

C. (c) 21

D. (d) 22

Answer: C

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2. If the middle term in the expansion of $\left(x^2+rac{1}{x} ight)^{2n}$ is $184756x^{10}$, then the value of

in is

A. 10 B. 8

C. 5

D. 4

Answer: A

3. If the coefficient of middle term of the binomial expansion of $\left(1+x
ight)^{2n}$ is lpha and those of two middle terms of the binomial expansion of $(1+x)^{2n-1}$ if β and γ , then which one of the following is correct? (i) $\alpha > \beta + \gamma$ (ii) $\alpha < \beta + \gamma$ (iii) $\alpha = \beta + \gamma$ (iv) $\alpha = \beta \gamma$ A. $\alpha > \beta + \gamma$ B. $\alpha < \beta + \gamma$

C.
$$lpha=eta+\gamma$$

D.
$$lpha=eta\gamma$$

Answer: C



4. If the coefficient of (2r+1) th and (r+2)th terms in the expansion of $(1+x)^{43}$ are equal, then the value of $r(r \neq 1)$ is B. 14

C. 21

D. 22

Answer: B

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5. Find the number of terms in the following expansions.

$$(2x-3y)^5$$

6. Find the number of terms in the following expansions.

(ii)
$$\left(5x-rac{1}{x^3}
ight)^{17}$$

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7. Find the number of terms in the following expansions.

$$\left(1+6x+9x^2
ight)^{23}$$

8. Find the number of terms in the following expansions.

$$\left(\sqrt{3}+\sqrt{5}
ight)^7 \left(\sqrt{3}-\sqrt{5}
ight)^7$$

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9. Find the number of terms in the following expansions.

(v)
$$(3x+7)^8+(3x-7)^8$$

10. Find the number of terms in the following expansions.

(vi)
$$\left(1+3\sqrt{5}x
ight)^9-\left(1-3\sqrt{5}x
ight)^9$$

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11. Find the number of terms in the following

expansions.

$${(x+y)}^{100} + {(x-y)}^{100}$$





14. Expand
$$\left(x+rac{1}{x}
ight)^6.~(x
eq 0)$$

15. Find the value of $(\sqrt{2}+1)^6 + (\sqrt{2}-1)^6$ and show that the value of $(\sqrt{2}+1)^6$ lies between 197 and 198.



16. Use the binomial theorem to find the exact value of $(10.1)^5$.



17. Expand
$$\left(2+x+x^2
ight)^3$$
.



18. Prove that
$$\sum_{r=0}^n 3^r {}^n C_r = 4^n.$$

$$rac{{}^8C_0}{6} - {}^8C_1 + {}^8C_2.\ 6 - {}^8C_3.\ 6^2 + ... + {}^8C_8.6^7$$
 is equal to (i) 0 (ii) 6^7 (iii) 6^5 (iv) $rac{5^8}{6}$

A. 0

B. 6^7 C. 6^5 D. $\frac{5^8}{6}$

Answer: D

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20. Find the tenth term in the expansion $(2x - y)^{11}$.



21. Write the middle term or terms in the expansion of $(1 + 1)^6$

(i)
$$\left(x^2-rac{1}{x}
ight)$$

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22. Write the middle term or terms in the

expansion of

$$\left(3a-rac{a^3}{6}
ight)^9$$



23. Find the rth term from the end in $(x + a)^n$.

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24. (ii) Find the 4th term from the end in the

expansion of
$$\left(rac{3}{x^2}-rac{x^3}{6}
ight)^7$$
.

25. Find the coefficient of x^{15} in the expansion

of
$$\left(x-x^2
ight)^{10}$$
 .

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26. If for positive integers r > 1, n > 2, the coefficients of the (3r)th and (r+2)th powers of x in the expansion of $(1+x)^{2n}$ are equal, then prove that n = 2r + 1.

27. Find the term independent of
$$x$$
 in the expansion of $\left(\frac{3}{2}x^2 - \frac{1}{3x}\right)^9$. **Vatch Video Solution**

28. The 2nd, 3rd and 4th terms in the expansion of $(x + y)^n$ are 240, 720 and 1080 respectively, find the values of x, y and n.

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Multiple Choice Questions

1. The number of terms in the expansion of $\left(x+a
ight)^{53}+\left(x-a
ight)^{53}$ after simplification is A. 106 B. 26 C. 27 D. 53

Answer: C



2. The number of terms in the expansion of $\left(x+a
ight)^{46}-\left(x-a
ight)^{46}$ after simplification is A. 23 B. 24 C. 46 D. 92 Answer: A

3. If the coefficients of x^7 and x^8 in the expansion of $\left(2+\frac{x}{3}\right)^n$ are equal then n =?

A. 56

B. 55

C. 45

D. 15

Answer: B

equal to

A.
$$\frac{3^{n}+1}{2}$$

B. $\frac{3^{n}-1}{2}$
C. $\frac{1-3^{n}}{2}$
D. $\frac{3^{n}}{2}-1$

Answer: B

5. If the coefficient of (r+1) th term and (r+3) th term in the expansion of $(1+x)^{20}$ are equal, then the value of r is

(i) 8

(ii) 9

(iii) 16

(iv) None of these

A. 8

B. 9

C. 16

D. None of these

Answer: B

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6. If the coefficients of rth term and (r+4) th term the expansion of $(1+x)^{34}$ are equal then the value of r is

(i) 15

(ii) 17

(iii) 16

(iv) None of these

A. 15

B. 17

C. 16

D. None of these

Answer: C

7. The 13 th term in the expansion of

$$\left(9x - \frac{1}{3\sqrt{x}}\right)^{18}, x > 0 \text{ is}$$
(i) ${}^{18}C_{12}x^3$
(ii) ${}^{18}C_{12}x^6$
(iii) ${}^{18}C_{12}\frac{1}{x^6}$
(iv) ${}^{18}C_{12}$
A. ${}^{18}C_{12}x^3$
B. ${}^{18}C_{6}x^6$
C. ${}^{18}C_{12}\frac{1}{x^6}$
D. ${}^{18}C_6$

Answer: D



8. If rth term in the expansion of
$$\left(2x^2-rac{1}{x}
ight)^{12}$$
 is independent of x, then the

value of r is

(i) 7

(ii) 8

(iii) 9

(iv) 10

A. 7

B. 8

C. 9

D. 10

Answer: C

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9. The term independent of x in the expansion

of
$$\left(2x-rac{1}{x}
ight)^{10}$$
 is

A.
$${}^{10}C_5.2^5$$

B.
$${}^{10}C_6.2^4$$

C.
$${}^{10}C_6.2^5(-1)^5$$

D. None of these

Answer: C



10. The coefficients of x^p and $x^q(p,q\in N)$ in

the expansion of $(1+x)^{p+q}$ are

A. equal

B. equal with opposite sign

C. reciprocal of each other

D. None of these

Answer: A



11. The coefficients of x^{11} in the expansion of

$$\left(2x^2+x-3
ight)^6$$
 is

A. 186

B. 190

C. 192

D. 196

Answer: C

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12. The ratio of the coefficient of x^3 to the term independent of x in $\left(2x+rac{1}{x^2}
ight)^{12}$ is

A. 9:8

B. 8:9

C. 8:1

D. 9:1

Answer: B



are

A. (a)
$$-3,3$$

D. (d)
$$-2, 2$$

Answer: C



14. If the seventh, terms from the beginning and the end in the expansion of $\left(\sqrt[3]{2}+rac{1}{\sqrt[3]{3}}
ight)^n$ are equal, then n is equal to (i) 10 (ii) 11 (iii) 12 (iv) 13 A. 10 B. 11 C. 12

D. 13

Answer: C

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15. If P be the sum of odd terms and Q be the sum of even terms in the expansion of $(x + a)^n$, then $(x + a)^{2n} + (x - a)^{2n}$ is (i) $P^2 - Q^2$ (ii) $P^2 + Q^2$

(iii)
$$2ig(P^2+Q^2ig)$$

(iv) 4PQ

A.
$$P^2-Q^2$$

- $\mathsf{B}.\,P^2+Q^2$
- C. $2 ig(P^2 + Q^2 ig)$

D. 4PQ

Answer: C

16. The coefficient of x^5 in the expansion of $1 + (1 + x) + (1 + x)^2 + \dots + (1 + x)^{10}$ is equal to A. 462 B. 450 C. 543 D. 446

Answer: A


17. Given the integers r > 1, n > 2 and coefficients of (3r) th and (r + 2) th terms in the expansion of $(1 + x)^{2n}$ are equal, then

A.
$$n=2r$$

B.
$$n=3r$$

$$\mathsf{C.}\,n=2r+1$$

$$\mathsf{D}.\,2r-1$$

Answer: A



18. The two consecutive terms in the expansion of $\left(1+x
ight)^{24}$ whose coefficients are in the ratio 1:4 are

A. (a) 3rd and 4th

B. (b) 4th and 5th

C. (c) 5th and 6th

D. (d) 6th and 7th

Answer: C



19. The coefficients fo x^n in the expansion of $\left(1+x
ight)^{2n}$ and $\left(1+x
ight)^{2n-1}$ are in the ratio A. 1:2 B. 1:3 **C**. 3:1 D. 2:1

Answer: D

20. If the sum of the binomial coefficient in the

expansion of
$$\left(2x+rac{1}{x}
ight)^n$$
 is 256, then the

term independent of x is

(i) 1120

(ii) 1024

(iii) 512

(iv) None of these

A. 1120

B. 1024

C. 512

D. None of these

Answer: A



21. If the middle term in the expansion of $\left(rac{1}{r}+x\sin x
ight)^{10}$ is equal to $7rac{7}{8}$, then the value of x is (i) $2n\pi + \frac{\pi}{6}$ (ii) $n\pi + \frac{\pi}{6}$ (iii) $n\pi + (-1)^n \frac{\pi}{6}$ (iv) $n\pi + (-1)^n \frac{\pi}{3}$

A.
$$2n\pi + \frac{\pi}{6}$$

B. $n\pi + \frac{\pi}{6}$
C. $n\pi + (-1)^n \frac{\pi}{6}$
D. $n\pi + (-1)^n \frac{\pi}{3}$

Answer: C



Exercise 13 A

1. What is the number of terms in the expansion of the following?

$$\left[(x-2)^3
ight]^3$$

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2. What is the number of terms in the expansion of each of the following?

(ii) $(5a + 7b)^3$

3. What is the number of terms in the

expansion of the following?

$$\left(6x-rac{1}{x^3}
ight)^{17}$$



4. What is the number of terms in the expansion of the following?

$$\left(4x^2+12xy+9y^2
ight)^9$$

5. What is the number of terms in the

expansion of

$$\left(3+2\sqrt{5}
ight)^{18}-\left(3-2\sqrt{5}
ight)^{18}$$

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6. What is the number of terms in the expansion of each of the following?

(vi)
$$\left(5+7x
ight)^{15}+\left(5-7x
ight)^{15}$$

7. What is the number of terms in the expansion of the following?

$$(a+bx)^{17}-(a-bx)^{17}$$

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8. Write out the expansions of the following:

$$\left(3x-y
ight)^4$$

9. Write out the expansions of the following:

$$\left(3+2x^2
ight)^4$$

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10. Write out the expansions of the following:

(c)
$$\left(x-rac{y}{2}
ight)^4$$

11. Write out the expansion of the following:

$$\left(2x+rac{y}{2}
ight)^5$$

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12. Write out the expansions of the following: (e) $\left(1+2x
ight)^7$

13. Write out the expansions of the following:

(f)
$$\left(rac{2}{x}-rac{x}{2}
ight)^5, x
eq 0$$

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14. Using binomial theorem, expand $\left[\left(x+y\right)^5+\left(x-y\right)^5\right]$ and hence find the value of $\left[\left(\sqrt{3}+1\right)^5-\left(\sqrt{3}-1\right)^5\right]$.

15. Expand $(2+x)^5 - (2-x)^5$ in ascending

powers of x and simplify your result.

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16. Evaluate the following: (i) $(2 + \sqrt{5})^5 + (2 - \sqrt{5})^5$ (ii) $(\sqrt{3} + 1)^5 - (\sqrt{3} - 1)^5$ Hence, show in (ii), without using tables, that the value of $(\sqrt{3} + 1)^5$ lies between 152 and 153.



- 17. If the first three terms in the expansion of $(1+ax)^n$ in ascending powers of x are
- $1 + 12x + 64x^2$, find n and a.

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18. Find the first three terms in the expansion of $[2 + x(3 + 4x)]^5$ in ascending powers of x.

19. Expand $\left(1+2x+3x^2\right)^n$ in a series of ascending powers of x up to and including the term in x^2 .



20. Write down the expansion by the binomial theorem of $\left(3x - \frac{y}{2}\right)^4$. By giving x and y suitable values, deduce the value of $(29.5)^4$ correct to four significant figures.

21. Using binomial theorem, evaluate : $(999)^3$.

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22. Write down in terms of x and n, the term containing x^3 in the expansion of $\left(1 - \frac{x}{n}\right)^n$ by the binomial theorem. if this term equals $\frac{7}{8}$ when x = -2, and n is a positive integer, calculate the value of n.

23. (i) Obtain the binomial expansion of $(2 - \sqrt{3})^6$ in the form $a + b\sqrt{3}$, where a and b are integers. State the corresponding result for the expansion $(2 + \sqrt{3})^6$

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24. Find the coefficient of x^5 in the expansion

of $(1+2x)^6(1-x)^7.$

25. If the coefficients of second, third and fourth terms in the expansion of $(1+x)^{2n}$ are in A.P., show that $2n^2 - 9n + 7 = 0$.

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26. Let n be a positive integer. If the coefficients of 2nd, 3rd, 4th terms in the expansion of $(1 + x)^n$ are in A.P., then find the value of n.

27. In the binomial expansion of $\left(\sqrt[3]{4} + \sqrt{2}
ight)^5$

find the term which does not contain Irrational

expression.





1. Find the specified term of the expression in each of the following binomials:

(i) Fifth term of $(2a + 3b)^{12}$. Evaluate it when

$$a=rac{1}{3},b=rac{1}{4}.$$

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2. Find the specified term of the expression in

each of the following binomials:

(ii) Sixth term of
$$\left(2x-rac{1}{x^2}
ight)^7$$
.

3. Find the specified term of the expression in

each of the following binomials:

(iii) Middle term of
$$\left(2x-rac{1}{y}
ight)^8$$
.

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4. Find the specified term of the expression in

each of the following binomials:

(iv) Middle term of
$$\left(x^4-rac{1}{x^3}
ight)^{11}$$

5. Find the specified term of the expression in

each of the following binomials:

(v) Middle term of
$$\left(rac{x^2}{4}-rac{4}{x^2}
ight)^{10}$$



6. Find the term independent of x in the

expansion of the following binomials:

(i)
$$\left(x-rac{1}{x}
ight)^{14}$$

7. Find the term independent of x in the

expansion of the following binomials:

(ii)
$$\left(\sqrt{\frac{x}{3}}-\frac{\sqrt{3}}{2x}\right)^{12}$$

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8. Find the term independent of x in the

expansion of the following binomials:

$$\left(2x^2-rac{1}{x}
ight)^{12}$$
 What is its value?





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10. Find the coefficient of

(ii) x^7 in the expansion of $\left(x^2+rac{1}{x}
ight)^{11}$

11. Find the coefficient of

(iii)
$$rac{1}{x^{17}}$$
 in the expansion of $\left(x^4-rac{1}{x^3}
ight)^{15}$.

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12. Find the coefficient of

(iv)
$$x^4$$
 in the expansion of $\left(rac{x}{2}-rac{3}{x^2}
ight)^{10}$

13. If the coefficients of x^2 and x^3 in the expansion of $(3 + ax)^9$ are the same, find the value of a.



14. Write down the fourth term in the binomial expansion of $\left(px + \frac{1}{x}\right)^n$. If this term is independent of x, find the value of n. With this value of n, calculate the value of p given that the fourth term is equal to $\frac{5}{2}$.



15. The expansion by the binomial theorem of

$$\left(2x+rac{1}{8}
ight)^{10}$$
 is

 $1024x^{10}+640x^9+ax^8+bx^7+$... Calculate

(i) the numerical value of a and b

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16. The expansion by the binomial theorem of

$$\left(2x+rac{1}{8}
ight)^{10}$$

is

 $1024x^{10}+640x^9+ax^8+bx^7+\ldots$ Calculate (ii) coefficient of x^8 in $(3x-2)\left(2x+rac{1}{8}
ight)^{10}$,

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17. The expansion by the binomial theorem of

$$\left(2x+rac{1}{8}
ight)^{10}$$
 is

 $1024x^{10}+640x^9+ax^8+bx^7+\dots$ Calculate

(iii) the value of x, for which the third \cdot and the fourth terms in the expansion of $\left(2x+\frac{1}{8}\right)^{10}$

are equal.

18. Find the coefficient of x^7 in $\left(ax^2 + \frac{1}{bx}\right)^{11}$ and the coefficient of x^{-7} in $\left(ax + \frac{1}{bx^2}\right)^{11}$.

If these coefficients are equal, find the relation

between a and b.

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19. In a binomial expansion, $(x + a)^n$, the first three terms are 1, 56 and 1372 respectively. Find values of x and a.



21. The coefficients of (2r + 1)th and (r + 2)th terms in the expansions of $(1 + x)^{43}$ are equal. Find the value of r.

22. The coefficient of the middle term in the binomial expansion in powers of x of $(1 + \alpha x)^4$ and of $(1 - \alpha x)^6$ is the same if α equals

A. A.
$$\frac{-3}{10}$$

B. B. $\frac{10}{3}$
C. C. $\frac{-5}{3}$
D. D. $\frac{3}{5}$

Answer: A



the third term from the end is 45.

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24. Show that the coefficient of the middle term in the expansion of $(1+x)^{2n}$ is the sum





26. Find the coefficient of x^5 in the expansion

of
$$1 + (1 + x) + (1 + x)^2 + \ldots + (1 + x)^{10}$$
.

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28. If P be the sum of odd terms and Q be the sum of even terms in the expansion of $(x + a)^n$, prove that (i) $p^2 - Q^2 = (x^2 - a^2)^n$ Watch Video Solution

29. If P be the sum of odd terms and Q be the sum of even terms in the expansion of $(x + a)^n$, prove that (ii) $4PQ = (x + a)^{2n} - (x - a)^{2n}$ and
30. If P be the sum of odd terms and Q be the sum of even terms in the expansion of $(x+a)^n$, prove that

(iii) $2ig(P^2+Q^2ig) = (x+a)^{2n} + (x-a)^{2n}.$

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31. If the coefficient of the rth, (r+1)th and (r+2)th terms in the expansion of $(1+x)^n$ are in A.P., prove that $n^2 - n(4r+1) + 4r^2 - 2 = 0.$



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33. The coefficient of x^n in the expansion of $(1+x)(1-x)^n$ is

A.
$$(-1)^{n-1}(n-1)^2$$

B. $(-1)^n(1-n)$
C. $n-1$
D. $(-1)^{n-1}$. n

Answer: B



Chapter Test

1. Expand
$$\left(rac{2}{x}-rac{x}{2}
ight)^5, x
eq 0.$$

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2. Using binomial theorem, write the value of

 $\left(a+b
ight)^6+\left(a-b
ight)^6$ and hence find the value of $\left(\sqrt{3}+\sqrt{2}
ight)^6+\left(\sqrt{3}-\sqrt{2}
ight)^6.$

3. Find the 9th term in the expansion of

$$\left(3x-rac{1}{2x}
ight)^8, x
eq 0.$$

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4. Find the term independent of x in $\left(2x^2-\frac{1}{x}\right)^{12}.$

5. Find the middle terms in the expansion of

$${\left(3-rac{x^3}{6}
ight)^7}.$$

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6. In the binomial expansion of $(1 + x)^{m+n}$, prove that the coefficients of x^m and x^n are equal.

7. Use binomial theorem to evaluate $(10.1)^5$.



9. In the binomial expansion of $(a-b)^n, n \ge 5$, the sum of 5th and 6th terms is zero, then $rac{a}{b}$ equals

A. (a)
$$\frac{n-5}{6}$$

B. (b) $\frac{n-4}{5}$
C. (c) $\frac{5}{n-4}$
D. (d) $\frac{6}{n-5}$

Answer: B

10. If $m = {}^{n}C_{2}$, then ${}^{m}C_{2}$ is equal to

A. 3. ${}^{n}C_{4}$

B. $^{n+1}C_4$

C. 3. $^{n+1}C_4$

D. 3. $^{n+1}C_3$

Answer: C



11. If the coefficient of r^{th} and $(r+4)^{th}$ terms are equal in the expansion of $(1+x)^{20}$, then the value of r will be

A. (a) 7

B. (b) 8

C. (c) 9

D. (d) 10

Answer: C



$$ig(1+x-2x^2ig)^6 = 1 + a_1x + a_2x^2 + ... + a_{12}x^{12}$$

, then find
$$a_2+a_4+...+a_{12}$$



13. If the coefficients of x^2 and x^3 in the expansion of $(3 + ax)^9$ be same, then the value of a is

A. (a)
$$\frac{3}{7}$$

B. (b) $\frac{7}{3}$

C. (c)
$$\frac{7}{9}$$

D. (d) $\frac{9}{7}$

Answer: D



14. Using binomial theorem, the value of $(0.999)^3$ correct to 3 decimal places is

A. (a) 0.999

B. (b) 0.998

C. (c) 0.997

D. (d) 0.995

Answer: C

