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## MATHS

## BOOKS - S CHAND MATHS (ENGLISH)

## MEASURES OF DISPERSION

## Example

1. Find the mean deviation from the mean for following marks:
$37,48,50,23,47,58,29,31,40$.
2. The scores of a batsman in ten innings are:
$48,80,58,44,52,65,73,56,64,54$. Find the mean deviation from the median.

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3. Find the mean deviation from the mean for the followinng data:

| $x$ | 5 | 10 | 15 | 20 | 25 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $f$ | 7 | 4 | 6 | 3 | 5 |

4. Find the mean deviation from the median for the following data:
$34,66,30,38,44,50,40,60,42,51$.

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5. Calculate the mean deviation and coefft. of mean deviation for the following frequency distribution from both mean and median.

| Variable $(x)$ | $\mathbf{8}$ | $\mathbf{1 0}$ | $\mathbf{1 5}$ | 20 | 25 | 32 | 35 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency $(f)$ | 3 | 2 | 4 | 7 | 4 | 3 | 7 |

6. Find the mean deviation from the median for the following data:


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7. Calculate the mean deviation and coefficient of mean deviation for the following distribution:

| Class | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 7 | 3 | 5 | 2 | 8 |

## 8. Find the standard deviation of the first five even

 natural numbers.
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9. Calculate the standard deviation from the following following set of observations:
$8,9,15,23,5,11,19,8,10,12$

Watch Video Solution
10. Calculate the mean and standard deviation of
first n natural numbers.

## - Watch Video Solution

11. Compute the standard deviation for the following distribution.

| Variable $(x)$ | 10 | 15 | 18 | 20 | 25 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Frequency $(f)$ | 3 | 2 | 5 | 8 | 2 |

D Watch Video Solution
12. Calculate the standard deviation for the following distribution.

| $x$ | 8 | 11 | 17 | 20 | 25 | 30 | 35 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f$ | 2 | 3 | 4 | 1 | 5 | 7 | 3 |

## (D) Watch Video Solution

13. Find the variance and standard deviation for the following distribution.

| $x$ | 4.5 | 14.5 | 24.5 | 34.5 | 44.5 | 54.5 | 64.5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f$ | 1 | 5 | 12 | 22 | 17 | 9 | 4 |

14. Calculate the standard deviation of the following distribution:

| Age | $20-25$ | $25-30$ | $30-35$ | $35-40$ | $40-45$ | $45-50$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of persons | 170 | 110 | 80 | 45 | 40 | 35 |

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15. Calculate the standard deviation of the following given in the following table.

| Length of wire (in cm) | . No. of wires | Length of wire | No. of wires |
| :---: | :---: | :---: | :---: |
| $72.0-73.9$ | 7 | $82.0-83.9$ | 24 |
| $74.0-75.9$ | 31 | $84.0-85.9$ | 22 |
| $76.0-77.9$ | 42 | $86.0-87.9$ | 8 |
| $78.0-79.9$ | 54 | $88.0-89.9$ | 4 |
| $80.0-81.9$ | 33 |  |  |

16. A purchasing agent obtained samples of 60
watt bulbs from a standard company. He had the
samples tested in his own laboratory for length of
life with the following results:

| Length of life (in hours) | Number |
| :---: | :---: |
| 1700 and uíder 1900 | 10 |
| 1900 and under 2100 | 16 |
| 2100 and under 2300 | 20 |
| 2300 and under 2500 | 8 |
| 2500 and under 2700 | 6 |

Calculate the standard deviation for these samples.

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17. The mean of 200 items is 48 and their standard deviation is 3 . Find the sum of squares of all items.

## - Watch Video Solution

18. For the distribution given in the following table, find the mean and the standard deviation by the step deviation method.

| Marks | Frequency | Marks | Frequency |
| :---: | :---: | :---: | :---: |
| $0-4$ | 2 | $20-24$ | 21 |
| $5-9$ | 5 | $25-29$ | 16 |
| $10-14$ | 7 | $30-34$ | 8 |
| $15-19$ | 13 | $35-39$ | 3 |

19. A standard obtained the mean and standard deviation of 100 observations as 40 and 5.1 respectively. Later it was discovered that he had wrongly copied down and observation as 50 instead of 40. Calculate the true mean and standard deviation.

## - Watch Video Solution

20. In two factories $A$ and $B$ engaged in the same industrial area, the average weekly wages (in rupees) and the standard deviations are as
follows:

| Factory | Average | S.D. | No. of workers |
| :---: | :---: | :---: | :---: |
| A | 34.5 | 5 | 476 |
| B | 28.5 | 4.5 | 524 |

(i) Which factory, A or B, pays out a larger amount as weekly wages?
(ii) Which factory, A or B , has greater variability in individual wages?

## - Watch Video Solution

## Exercise 21 A

1. From the following data, using mean, calculate
mean deviation and the coefficient of mean
deviation.
$15,17,19,25,30,35,48$

- Watch Video Solution

2. From the following data, using mean, calculate mean deviation and the coefficient of mean deviation.
$21,23,25,28,30,32,38,39,46,48$

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3. From the following data, using mean, calculate mean deviation and the coefficient of mean deviation.
$10,70,50,53,20,95,42,60,48,80$

## - Watch Video Solution

4. Calculate the mean deviation from the mean for
the following frequency distributions.

| $x_{i}$ | 3 | 9 | 17 | 23 | 27 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $f_{i}$ | 8 | 10 | 12 | 9 | 5 |

5. Calculate the mean deviation from the mean for the following frequency distributions.

| $x_{i}$ | 10 | 11 | 12 | 13 | 14 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $f_{i}$ | 3 | 12 | 18 | 12 | 3 |

## - Watch Video Solution

6. Calculate the mean deviation from the mean for
the following frequency distributions.

| Marks | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of students | 5 | 8 | 15 | 16 | 6 |

7. Calculate the mean deviation from the mean for the following frequency distributions.

| Scores | $140-150$ | $150-160$ | $160-170$ | $170-180$ | $180-190$ | $190-200$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of students | 4 | 6 | 10 | 18 | 9 | 3 |

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8. Calculate the mean deviation from the mean for the following frequency distributions.

| Class Interval | $0-20$ | $20-40$ | $40-60$ | $60-80$ | $80-100$ | $100-120$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 3 | 50 | 84 | 32 | 10 | 3 |

## D <br> Watch Video Solution

9. For the following, calculate mean deviation and coefficient of mean deviation.
$3,9,5,3,12,10,18,4,7,19,21$

## - Watch Video Solution

10. For the following, using median, calculate mean deviation and coefficient of mean deviation.

$$
100,150,200,250,360,490,500,600,671
$$

11. For the following, using median, calculate mean deviation and coefficient of mean deviation.

| $x$ | 10 | 11 | 12 | 13 | 14 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $f$ | 3 | 12 | 18 | 12 | 3 |

## - Watch Video Solution

12. For the following, using median, calculate mean deviation and coefficient of mean deviation.

| $x$ | 3 | 6 | 9 | 12 | 13 | 15 | 21 | 22 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f$ | 3 | 4 | 5 | 2 | 4 | 5 | 4 | 3 |

1. Five students secured marks as, $8,10,15,30,22$.

Find the standard deviation.

D Watch Video Solution
2. For a set of ungrouped values the following sums are found:

$$
n=15, \sum x=480, \sum x^{2}=15735
$$

Find the standard deviation.
3. The standard deviation of the numbers $2,3,11$,

2 x is $3 \frac{1}{2}$. Calculate the values of x .

## - Watch Video Solution

4. Calculate the variance and standard deviation of the observations : 11, 12, 13, . . .. 20.

## - Watch Video Solution

5. Find the standard deviation of the following set of numbers:
$25,50,45,30,70,42,36,48,34,50$

## D Watch Video Solution

6. Calculate the possible values of $x$, if the standard deviation of the numbers $2,3,2 x$ and 11 is 3.5 .

## D Watch Video Solution

7. Calculate the standard deviation for the following distribution:

| Class interval | $0-4$ | $4-8$ | $8-12$ | $12-16$ |
| :--- | :---: | :---: | :---: | :---: |
| Frequency | .4 | 8 | 2 | 1 |

## - Watch Video Solution

8. Calculate the standard deviation of the following data:

| Size | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Frequency | 6 | 12 | 15 | 28 | 29 | 14 | -15 |

## - Watch Video Solution

9. Calculate the standard deviation of the following data:

| Class interval | $0-6$ | $6-12$ | $12-18$ | $18-24$ | $24-30$ | $30-36$ | $36-40$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 19 | 25 | 36 | 72 | 51 | 43 | 28 |

10. Calculate the standard deviation for the following data giving the age distribution of persons.

| Age in years | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ | $80-90$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of persons | 3 | 61 | 132 | 153 | 140 | 51 | 2 |

Calculate the mean of these differences and their standard deviation.

## D Watch Video Solution

11. The heights, to the nearest cm , of 30 men are given below:
$\begin{array}{llllllllll}159 & 170 & 174 & 173 & 175 & 160 & 161 & 164 & 163 & 165\end{array}$ $\begin{array}{llllllllll}164 & 171 & 162 & 170 & 177 & 185 & 181 & 180 & 175 & 165\end{array}$ $\begin{array}{llllllllll}186 & 174 & 168 & 168 & 176 & 176 & 165 & 175 & 167 & 180\end{array}$ Using class intervals 155-160, 160-165, ... draw up a grouped frequency distribution and use this to estimate the Arithmetic mean and standard deviation.

## - Watch Video Solution

12. Find the mean and the standard deviation from the following:

| Wages (in Rupees) | $120-200$ | $200-210$ | $210-220$ | $220-230$ |
| :--- | :---: | :---: | :---: | :---: |
| No. of workers | 10 | 12 | 18 | 20 |
| Wages (in Rupees) | $230-240$ | $240-250$ | $250-260$ | $260-270$ |
| No. of workers | 25 | 18 | 16 | 5 |

13. The following table shows the I.Q. of 480 schoolchildren. Find
(i) the mean.
(ii) the standard deviation using the step deviation method. Use Charlier's check to verify the computation of the standard deviation.

| $x$ | 70 | 74 | 78 | 82 | 86 | 90 | 94 | 98 | 102 | 106 | 110 | 114 | 118 | 122 | 126 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f$ | 4 | 9 | 46 | 28 | 45 | 66 | 85 | 72 | 54 | 38 | 27 | 18 | 11 | 5 | 2 |

14. In a certain test, the 30 scores were grouped as follows:

| $30-34$ | $35-39$ | $40-44$ | $45-49$ | $50-54$ | $55-59$ | $60-64$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 2 | 7 | 10 | 6 | 2 | 1 |

Calculate the mean and the standard deviation.

## D View Text Solution

15. The number of faults on the surface of each of 1000 tiles were distributed as follows:

| No. of faults | 0 | 1 | 2 | 3 | 4 | 5 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 760 | 138 | 67 | 25 | 8 | 2 |

Calculate the mean and the standard deviation.
16. The mean and the standard deviation of 25
observations are 60 and 3 . Later on it was decided
to omit an observation which was incorrectly recorded as 60. Calculate the mean and the standard deviation of the remaining 24 observations.
(D) Watch Video Solution
17. The scores of two golfers for 10 rounds each are:

| $A$ | 58 | 59 | 60 | 54 | 65 | 66 | 52 | 75 | 69 | 52 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $B$ | 84 | 56 | 92 | 65 | 86 | 78 | 44 | 54 | 78 | 68 |

Which may be regarded as the more consistent player?

## D Watch Video Solution

18. Goals scored by two teams $A$ and $B$ in $a$ football season were as follows:

| Number of goals scored <br> in a match | Number of matches |  |
| :---: | :---: | :---: |
| 0 | $A$ | $B$ |
| 1 | 27 | 17 |
| 2 | 9 | 9 |
| 3 | 8 | 6 |
| 4 | 5 | 5 |

By calculating the coefficient of variation in each
case find which team may be considered more consistent.

## D Watch Video Solution

19. The mean of the numbers $a, b, 8,5,10$ is 6 and
the variance is 6.80 . Then which one of the following gives possible values of $a$ and $b$ ?
A. $a=0, b=7$
B. $a=5, b=2$
C. $a=1, b=6$
D. $a=3, b=4$

Answer: D

## D Watch Video Solution

## Chapter Test

1. Find the mean deviation from the mean for the
following data:
$38,70,48,40,42,55,63,46,54,44$

D Watch Video Solution
2. Find the mean deviation from the mean for the following data:

| $x_{i}$ | 3 | 5 | 7 | 9 | 11 | 13 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f_{i}$ | 6 | 8 | 15 | 25 | 8 | 4 |

## - Watch Video Solution

3. Find the mean deviation for the mean for the
following data:

| Classes | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequencies | 6 | 8 | 14 | 16 | 4 | 2 |

4. Find the mean deviation about the median for the following data:
$11,3,8,7,5,14,10,2,9$

## - Watch Video Solution

5. Find the variance and standard deviation of the
following data:

| $x_{i}$ | 92 | 93 | 97 | 98 | 102 | 104 | 109 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $f_{i}$ | 3 | 2 | 3 | 2 | 6 | 3 | 3 |

6. Calculate the mean and variance after the following data:

| Classes | $0-30$ | $30-60$ | $60-90$ | $90-120$ | $120-150$ | $150-180$ | $180-210$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency $(f)$ | 2 | 3 | 5 | 10 | 3 | 5 | 2 |

