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## MATHS

## BOOKS - S CHAND MATHS (ENGLISH)

## MOVING AVERAGE

Example

1. The table below gives details of the
electricity generated in million kilowatt hours
in each quarter for the years 2002 to 2004.

| Year | Quarter |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | 1st | 2nd | 3rd | 4th |
| 2002 | 8 | 7 | 6 | 9 |
| 2003 | 10 | 7 | 7 | 10 |
| 2004 | 11 | 7 | 8 | 10 |

Calculate the 4-quarterly moving average and show these moving average on a graph.

## D View Text Solution

2. Coded monthly sales figures of a particular brand of T.V. for 18 months commencing January 1, 2005 are as follows:

| Year | Jan | Feb | Mar | Apr | May | June | July | Aug | Sept | Oct | Nov | Dee |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2005 | 18 | 16 | 23 | 27 | 28 | 19 | 31 | 29 | 35 | 27 | 28 | 24 |
| 2006 | 24 | 28 | 29 | 30 | 29 | 22 |  |  |  |  |  |  |

Calculate 6-monthly moving averages and
display these and the original figures on the same graph using the same axes for both.

## D View Text Solution

## Exercise 31

1. This table shows the number of students in
a school getting at least a grade $C$ in mathematics for the years 1994 to 2001.
(i) Represent this data as a time series.

| 1994 | 1995 | 1996 | 1997 | 1998 | 1999 | 2000 | 2001 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 97 | 118 | 115 | 117 | 121 | 125 | 111 | 125 |

## - View Text Solution

2. The profits of a soft drink firm in thousand of litres during each month of a year were:

| January | February | March | April | May | June |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1.2 | 0.8 | 1.4 | 1.6 | 2.0 | 2.0 |
| July | August | September | October | November | December |
| 3.6 | 4.8 | 3.4 | 1.8 | 0.7 | 1.2 |

Calculate 3-monthly moving averages and
illustrate graphically.

D View Text Solution
3. The number of traffic offences commited in
a certain city over a period of 3 years is given in the following table:

|  | Jan.-March | April-June | July-Sept. | Oct.-Dec. |
| :--- | :---: | :---: | :---: | :---: |
| 1968 | 74 | 56 | 48 | 69 |
| 1969 | 83 | 52 | 49 | 81 |
| 1970 | 94 | 60 | 48 | 79 |

Calculate 4-quarterly moving averages and illustrate these and original figures on one graph using the same axis for both. Comment briefly on a local politician's claim that traffic offences were on the increase.
4. Find the 4-quarterly moving averages in the following table which gives the quarterly index numbers of coal production (for the years 1936

- 1938). Also plot on the same graph the quarterly index numbers as well as the 4quarterly moving average. Comment on the nature of the general trend.

|  | Quarters |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Year | 1 | 2 | 3 | 4 |
| 1936 | 93.3 | 81.7 | 81.5 | 89.1 |
| 1937 | 93.8 | 92.3 | 86.5 | 93.7 |
| 1938 | 97.6 | 82.3 | 79.0 | 89.3 |

## D View Text Solution

## 5. The annual incomes of a firm were recorded

 every quarter for 4 years. The results are shown in this table.|  | 1999 | 2000 | 2001 | 2002 |
| :---: | :---: | :---: | :---: | :---: |
| 1st quarter | $₹ 18,00,000$ | $₹ \cdot 20,00,000$ | $₹ 21,00,000$ | $₹ 22,50,000$ |
| 2nd quarter | $₹ 14,50,000$ | $₹ 17,80,000$ | $₹ 19,50,000$ | $₹ 21,00,000$ |
| 3rd quarter | $₹ 13,50,000$ | $₹ 15,00,000$ | $₹ 18,00,000$ | $₹ 19,80,000$ |
| 4th quarter | $₹ 19,00,000$ | $₹ 18,30,000$ | $₹ 19,20,000$ | $₹ 20,50,000$ |

(i) Work out the 4-point moving average for the data.

## D View Text Solution

6. The annual incomes of a firm were recorded
shown in this table.

|  | 1999 | 2000 | 2001 | 2002 |
| :---: | :---: | :---: | :---: | :---: |
| 1st quarter | $₹ 18,00,000$ | $₹ 20,00,000$ | $₹ 21,00,000$ | $₹ 22,50,000$ |
| 2nd quarter | $₹ 14,50,000$ | $₹ 17,80,000$ | $₹ 19,50,000$ | $₹ 21,00,000$ |
| 3rd quarter | $₹ 13,50,000$ | $₹ 15,00,000$ | $₹ 18,00,000$ | $₹ 19,80,000$ |
| 4th quarter | $₹ 19,00,000$ | $₹ 18,30,000$ | $₹ 19,20,000$ | $₹ 20,50,000$ |

(iii) Comment on how the firm's incomes have changed over the 4-years.

## D View Text Solution

## 7. The following table shows the daily sales of

 milk at a local corner shop for a month.| Sun | Mon | Tue | Wed | Thut | Fri | Sat |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12 | 8 | 6 | 9 | 4 | 11 | 15 |
| 11 | 7 | 7 | 6 | 3 | 15 | 14 |
| 14 | 9 | 7 | 7 | 5 | 12 | 15 |
| 11 | 12 | 8 | 7 | 4 | 14 | 19 |

Make a table showing the moving average using a 7-day span, and draw a graph to show the trend of milk sales over the month.

## D View Text Solution

8. The following table gives the monthly expenditure on a motor car for a period of two
years.

| Year | January | February | - March | April | May | June |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1961 | $£ 18.2$ | 7.4 | 9.4 | 10.6 | 11.3 | 9.2 |
| 1962 | $£ 11.5$ | 11.0 | 6.9 | 14.1 | 9.0 | 8.3 |
| Year | July | August | September | October | November | December |
| 1961 | $£ 9.8$ | 10.6 | -8.2 | 7.7 | 19.2 | 8.7 |
| 1962 | $£ 13.9$ | 7.9 | 7.5 | 16.5 | 8.2 | 10.7 |

Calculate 12-monthly moving averages for the
two years and display them and the original table on the same graph.

## D View Text Solution

9. A new film was shown at a theatre and ran
for six weeks. The attendances are shown in the table.

|  | Mon | Tue | Wed | Thu | Fri | Sat |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| First week | 243 | 268 | 407 | 384 | 348 | 489 |
| Second week | 445 | 501 | 623 | 621 | 527 | 684 |
| Third week | 602 | 625 | 800 | 763 | 728 | 800 |
| Fourth week | 800 | 800 | 800 | 800 | 800 | 800 |
| Fifth week | 721 | 785 | 800 | 800 | 800 | 800 |
| Sixth week | 647 | 664 | 683 | 642 | 608 | 726 |

(ii) Calculate the 6-day moving average for the

Data and plot this on the same graph.

## D View Text Solution

10. A new film was shown at a theatre and ran
for six weeks. The attendances are shown in the table.

|  | Mon | Tue | Wed | Thu | Fri | Sat |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| First week | 243 | 268 | 407 | 384 | 348 | 489 |
| Second week | 445 | 501 | 623 | 621 | 527 | 684 |
| Third week | 602 | 625 | 800 | 763 | 728 | 800 |
| Fourth week | 800 | 800 | 800 | 800 | 800 | 800 |
| Fifth week | 721 | 785 | 800 | 800 | 800 | 800 |
| Sixth week | 647 | 664 | 683 | 642 | 608 | 726 |

(iii) Comment on the weekly attendances.

D View Text Solution
11. The table below given details of the electricity generated in million kilowatt hours
for public supply in each quarter of the years 1952 to 1955.

|  | Quarter |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| Year | 1 | 2 | 3 | 4 |
| 1952 | 8.9 | 7.1 | 6.7 | 9.3 |
| 1953 | 10.1 | 7.5 | 7.1 | 10.5 |
| 1954 | 11.7 | 7.5 | 8.3 | 10.9 |
| 1955 | 12.5 | 8.3 | 9.5 | 11.7 |

Draw a graph illustrating these figures.

Calculating a set of moving averages using the most suitable number of observations, give reasons of your choice. On the same diagram
as before draw a graph showing the moving averages.

## - View Text Solution

12. The number of letters, in hundreds, posted in a certain city on each day of a fortnight was as follows:

|  | Sunday | Monday | Tuesday | Wednesday | Thursday | Friday | Saturday |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| First Week | 35 | 70 | 36, | 59 | 62 | 60 | 71 |
| Second Week | 39 | 72 | 38 | 56 | 63 | 71 | 75 |

Calculate the 7-day moving averages and display these and the original figures graphically on the same diagram, using the same scale and axes.

What is the general trend?
13. In an influenza epidemic the numbers of cases diagnosed were:

| Date (Marćh) | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Numbers | 2 | 0 | 5 | 12 | 20 | 27 | 46 | 30 | 31 | 18 | 11 | 5 | 0 | 1 |

On what days do the mode and upper and lower quartiles occurs?

Calculate 3 -day moving averages and display them and the original figures on the same graph.

|  | Date rate per thousand <br> Quarter ended |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| Year | March | June | September | December |
| 1953 | 13.9 | 10.3 | 8.1 | 10.6 |
| 1954 | 13.8 | 9.8 | 7.8 | 10.8 |
| 1955 | 14.2 | 10.1 | 7.8 | 10.0 |

Plot these figures on a graph.

Calculate the 4-quarterly moving averages and
plot on the same graph.

- View Text Solution

15. Registered unemployed (hundreds)

|  | 1957 | 1958 |
| :--- | :---: | :---: |
| January | 638 | 596 |
| February | 602 | 548 |
| March | 509 | 491 |
| April | 462 | 462 |
| May | 359 | 365 |
| June | 295 | 325 |
| July | 290 | 308 |
| August | 322 | 328 |
| September | 377 | 377 |
| October | 392 | 380 |
| November | 480 | 474 |
| December | 542 | 536 |
| Average for year | 439 | 432.5 |

Plot these monthly figures on a graph.

Calculate the 12 -monthly moving averages and plot these on the same graph.

## D View Text Solution

16. A Ballet Company gave a 6 -week's season at a large hall capable of seating 4000 people and the attendances in hundreds, at the evening performances, are recorded in the following table.

Attendance, in hundreds, to nearest hundred

|  | Monday | Tuesday | Wednesday | Thursday | Friday | Saturday |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| First week | 12 | 13 | 20 | 19 | 17 | 24 |
| Second week | 22 | 25 | 31 | 31 | 26 | 34 |
| Third week | 30 | 31 | 40 | 38 | 36 | 40 |
| Fourth week | 40 | 40 | 40 | 40 | 40 | 40 |
| Fifth week | 38 | 39 | 40 | 40 | 40 | 40 |
| Sixth week | 32 | 33 | 34 | 32 | 30 | 36 |

Plot a graph of the above time-series and include on the same diagram the graph of 6day moving averages.

Comment on the weekly cycle on aatendances and state, with reasons, if you think, an
extension of the season of the eight weeks, would have been justified.

## D View Text Solution

17. Production of passenger cars, U.S.A. (tens of
thousands)

| Year | Quarters |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
|  | $I$ | II | III | IV |
| 1927 | 26 | 36 | 24 | I1 |
| 1928 | 29 | 36 | 36 | 22 |
| 1929 | 40 | 52 | 43 | 17 |

Calculate the 4-quarterly moving averages and then draw the graphs of the given series and
the moving averages. Briefly comment on the general trend.

## D View Text Solution

18. The aggregate number, in millions, of working days lot in strikes during each year of the period 1950-60 was

| 1950 | $' 51$ | $' 52$ | $' 53$ | $' 54$ | ${ }^{\prime} 55$ | $' 56$ | $' 57$ | $' 58$ | $' 59$ | $' 60$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1.4 | 1.7 | 1.8 | 2.2 | 2.5 | 3.8 | 2.1 | 8.4 | 3.5 | 5.3 | 3.0 |

Draw a graph to represent this formation.

Calculate the 3-yearly moving averages and draw the 3-yearly moving averages graph,
using the same axes and scales. What is the main purpose in drawing moving average graph? Comment on whether the purpose is acheived in this case.

## D View Text Solution

19. The profits of a soft drink firm in thousands
of rupees during each month of a year were:

| Jan. | Feb. | Mar. | Apr. | May | June | July | Aug. | Sept. | Oct. | Nov | Dec. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.2 | 0.8 | 1.4 | 1.6 | 2.0 | 2.4 | 3.6 | 4.8 | 3.4 | 1.8 | 0.8 | 1.2 |

Plot these on a graph

Calculate 4-monthly moving averages and plot
these on the same graph. Comment on the general trend.

## D View Text Solution

20. Calculate 5-yearly moving averages for the following data of the commercial and industrial failures in a country from 1982 to 1997.

| Year | No. of failures | Year | No. of failures |
| :---: | :---: | :---: | :---: |
| 1982 | 23 | 1990 | 9 |
| 1983 | 26 | 1991 | 13 |
| 1984 | 28 | 1992 | 11 |
| 1985 | 32 | 1993 | 14 |
| 1988 | 12 | 1996 | 3 |
| 1989 | 10 | 1997 | 1 |

Display the actual and trend values on the same graph using the same axes for both.

## D View Text Solution

21. The table given below shows the daily attendance in thousands as a certain exhibition over a period of two weeks:

| Week 1 | 52 | 48 | 64 | 68 | 52 | 70 | 72 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Week 2 | 55 | 47 | 61 | 65 | 58 | 75 | 81 |

Calculate 7-day moving averages and illustrate
these and original information on the same graph using the same scales.

## - View Text Solution

## 22. The profit of a soft-drink firm (in thousands

 of rupees) during each month of the year is as given below:| Jan. | Feb. | Mar. | Apr. | May | June | July | Aug. | Sept. | Oct. | Nov. | Dè. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $3.6^{\cdot}$ | 4.3 | 4.3 | 3.4 | 4.4 | 5.4 | 3.4 | 2.4 | 3.4 | 1.8 | 0.8 | 1.2 |

Calculate the 4-monthly moving averages and plot these and the original data on a graph sheet.

1. The following table gives the numbers of failures of commercial industries in a country during the years 1975 to 1990.

| Year | 1975 | 1976 | 1977 | 1978 | 1979 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of failures | 23 | 26 | 28 | 32 | 20 |  |
| Year | 1980 | 1981 | 1982 | 1983 | 1984 |  |
| No. of failures | 12 | 12 | 10 | 9 | 13 |  |
| Year | 1985 | 1986 | 1987 | 1988 | 1989 | 1990 |
| No. of failures | 11 | 14 | 12 | 9 | 3 | 1 |

Draw the graph illustrating the figures.
calculate the 4-yearly moveing average and plot them on the same graph.
2. The average number, in lakhs, of working days lost in strikes during each year of the period 1981-90 was

| 1981 | 1982 | 1983 | 1984 | 1985 | 1986 | 1987 | 1988 | 1989 | 1990 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.5 | 1.8 | 1.9 | .2 .2 | 2.6 | 2.7 | 2.2 | 6.4 | 3.6 | 5.4 |

Calculate the 3-yearly moving average and draw the moving average graph.

## D View Text Solution

3. The profit of a soft drink firm (in thousand of rupees) during each month of the year is as
given below:

| Month | Jan. | Feb. | Mar. | Apr. | May | June | July | Aug. | Scp. | Oct. | Nov. | Dec. |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Profits (in <br> thousands <br> of rupecs) | 3.6 | 4.3 | 4.3 | 3.4 | 4.4 | 5.4 | 3.4 | 2.4 | 3.4 | 1.8 | 0.8 | 1.2 |

Calculate the 4-monthly moving averages and plot these and the original data on a graph sheet.

## D View Text Solution

4. The quarterly profits of a small scale industry (in thousand of rupees) is as follows:

| Year | Quarter 1 | Quarter 2 | Quarter 3 | Quarter 4 |
| :---: | :---: | :---: | :---: | :---: |
| 2012 | 39 | 47 | 20 | 56 |
| 2013 | 68 | 59 | 66 | 72 |
| 2014 | 88 | 60 | 60 | 67 |

Calculate 4-quartely moving average. Display
these and the original figures garphically on the same graph sheet.

## D View Text Solution

5. The number of road accidents in the city
due to rash driving over a period of 3-years, is
given in the followong table:

| Year , | Jan. - Mar. | April - June | July - Sept. | Oct. - Dec. |
| :---: | :---: | :---: | :---: | :---: |
| 2010 | 70 | 60 | 45 | 72 |
| 2011 | 79 | .56 | 46 | 84 |
| 2012 | 90 | 64 | 45 | 82 |

Calculate four quarterly moving averages and
illustrate them and original figures on one graph using the same axes for both.

- View Text Solution

