# ©゙doubtnut 

## MATHS

# BOOKS - S CHAND MATHS (ENGLISH) 

## SAMPLE QUESTION PAPER 5

Section A

1. If $f(x)=\frac{|x-2||x-1|}{|x-3|}$, then value of $f(-2)$ is
A. $\frac{12}{5}$
B. $\frac{-12}{5}$
C. 12
D. 5
2. If $\sin \theta=\frac{4}{5}$, then the value of $\sec \theta \cdot \tan \theta$ is
A. $-9 / 20$
B. $9 / 20$
C. $-20 / 9$
D. $20 / 9$

## Answer: D

## - Watch Video Solution

3. The value of $\cos (\pi+x) \cos (\pi+x) \sec ^{2} x$ is
A. 0
B. 1
C. -1
D. Not defined

## Answer: B

## - Watch Video Solution

4. the conjugate of $\frac{1}{5+7 i}$ is
A. $\frac{4}{74}+\frac{5 i}{74}$
B. $\frac{4}{74}-\frac{5 i}{74}$
C. $\frac{5}{74}+\frac{4 i}{74}$
D. $\frac{5}{74}-\frac{4 i}{74}$

Answer: A

## - Watch Video Solution

5. If $\alpha$ and $\beta$ are the roots of the quadratic equation $a x^{2}+b x+1$, then the value of $\frac{1}{\alpha}+\frac{1}{\beta}$ is
A. a
B. $-a$
C. b
D. $-b$

## Answer: D

## ( Watch Video Solution

6. The number of terms in the expansion of $\left(49 y^{2}-70 y+25\right)^{17}$ is
A. 34
B. 35
C. 36
D. 77

## D Watch Video Solution

7. The values of $m$ for which the numbers $4, m, 9$ are in G.P. is
A. 0
B. +6
C. -6
D. $\pm 6$

## Answer: D

## - Watch Video Solution

8. If the vertices of a triangle are $(1,2),(4, k)$ and $(7,8)$ and its area is

15 sq. units, then the value(s) of $k$ is
A. $-40,10$
B. $-40,-10$
C. $40,-10$
D. 40,10

## Answer: A

## - Watch Video Solution

9. The equation of the circle with centre $(6,0)$ and radius 6 is
A. $x^{2}+y^{2}-12=0$
B. $x^{2}+y^{2}+12=0$
C. $x^{2}+y^{2}-12 x=0$
D. $x^{2}+y^{2}+12 x=0$

## Answer: C

10. $\lim _{x \rightarrow 2} \frac{\sqrt{x+2}-\sqrt{x-2}}{x+2}$ is equal to
A. 2
B. 1
C. $1 / 2$
D. 0

## Answer: B

## - Watch Video Solution

11. How many permutations can be made out of the letters of the word 'TRIANGLE ' ? How many of these will begin with $T$ and end with E ?
12. If $y=\sqrt{\frac{1-\cos 2 x}{1+\cos 2 x}}, x \in\left(0, \frac{\pi}{2}\right) \cup\left(\frac{\pi}{2}, \pi\right)$, then find $\frac{d y}{d x}$.

## - Watch Video Solution

13. A bag contains 9 red and 12 white balls one ball is drawn at random.

Find the probability that the ball drawn is red.

## - Watch Video Solution

14. Solve $4 \leq 2 x-6 \leq 8$.

## - Watch Video Solution

15. find the sum of coefficient in $(x+y)^{8}$.

## - Watch Video Solution

16. If $A=\{1,3,5,7,9\}, B=\{2,4,6,8\}$ and $C=\{2,3,5,7,11\}$, find $(A \cap B)$ and $(A \cap C)$. What do you conclude?

## - Watch Video Solution

17. If A and B are two sets given in such a way that $A \times B$ consists of 6 elements and if three elements of $A \times B$ are (1,5), (2,3) and (3,5), what are the remaining elements?

## - Watch Video Solution

18. Prove : $\cos 3 x=4 \cos ^{3} x-3 \cos x$

## - Watch Video Solution

19. For any triangle ABC , prove that $a(b \cos C-\mathrm{os} B)=b^{2}-c^{2}$
20. Prove that $\frac{\sin 5 x-2 \sin 3 x+\sin x}{\cos 5 x-\cos x}=\cos e c 2 x-\cot 2 x$

## D Watch Video Solution

21. For complex value of $z$, solve $|z|+z=(2+i)$

## - Watch Video Solution

22. 

## Prove

that
$\left(1-\omega+\omega^{2}\right)\left(1-\omega^{2}+\omega^{4}\right)\left(1-\omega^{4}+\omega^{8}\right)\left(1-\omega^{8}+\omega^{16}\right) \ldots$ to $2^{n}$ factors $=2^{2 n}$.

## - Watch Video Solution

23. Find the domain and range of the real function $f(x)=\sqrt{9-x^{2}}$
24. If $a \cos A=b \cos B$, then either the triangle is isosceles or right angled.

## - Watch Video Solution

25. In any $\triangle A B C$, prove that

$$
\frac{(b-c)}{(b+c)}=\frac{\tan \frac{1}{2}(B-C)}{\tan \frac{1}{2}(B+C)}
$$

## - Watch Video Solution

26. Using the principle of mathematical induction, prove that
$1.2+2.3+3.4+\ldots \ldots+n(n+1)=\frac{1}{3} n(n+1)(n+2)$

## - Watch Video Solution

27. Find the derivative of $\tan 5 x$ using first principle of differentiation.
28. Evaluate $\lim _{x \rightarrow 0} \frac{(1-\cos x)}{x^{2}}$

## - Watch Video Solution

29. If the roots of $a x^{2}+x+b=0$ be real and unequal, show that the roots of $\frac{x^{2}+1}{x}=4 \sqrt{a b}$ are imaginary.

## - Watch Video Solution

30. If $\alpha$ and $\beta$ are the roots of equation $2 x^{2}-x-3=0$, then find a equation having roots $(2 \alpha+3)$ and $(2 \beta+3)$.
31. If the fourth and nineth terms of a G.P. are 54 and 13122 respectively, find the G.P. Also find its general term.

## Watch Video Solution

32. Find the equation of the bisector of $\angle A$ of $\triangle A B C$, whose vertices are $A(-2,4), B(5,5)$ and $C(4,2)$.

## - Watch Video Solution

33. Find the equation of a circle passing through the points $(5,7),(6,6)$ and $(2,-2)$. Find its centre and radius.

## - Watch Video Solution

34. Find the mean for the following data.

| Marks obtained | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Number of students | 8 | 6 | 12 | 5 | 2 | 7 |

## Section B

1. The eccentricity of the ellipse $\frac{x^{2}}{49}+\frac{y^{2}}{25}=1$ is
A. $\frac{2}{7}$
B. $\frac{\sqrt{6}}{7}$
C. $\frac{2 \sqrt{6}}{5}$
D. $\frac{2 \sqrt{6}}{7}$

## Answer: D

## - Watch Video Solution

2. If the distance between the points $(2, a, 1)$ and $(-1,-1,1)$ is 5 , then the value(s) of $a$ is
A. 3,5
B. $-3,5$
C. $3,-5$
D. $-3,-5$

## Answer: C

## - Watch Video Solution

3. If the parabola $y^{2}=4 a x$ passes through the point $(4,5)$, find the length of its latus rectum.

## - Watch Video Solution

4. Find the equation of the hyperbola whose foci are $( \pm 5,0)$ and vertices are $( \pm 3,0)$.
5. Write the negation of the statement, "difference of 7 and 4 is 3 "?

## - Watch Video Solution

6. Using contradiction method, check the validity of the following statement :

If n is real number with $n>3$ then $n^{2}>9$.

## - Watch Video Solution

7. Check whether the following statement is true or not :

If $x$ and $y$ are odd integers, then $x y$ is an odd integer.'

## - Watch Video Solution

8. Find the equation of the ellipse with axes along the $x$-axis and the $y$ axis, which passes through the points $\mathrm{P}(4,3)$ and $\mathrm{Q}(6,2)$.
9. The foci of a hyperbola coincide with the foci of the ellipse $\frac{x^{2}}{25}+\frac{y^{2}}{9}=1$. Find the equation of the hyperbola, if its eccentricity is 2.

## - Watch Video Solution

10. Find the coordinates of the points which trisect the line segment joining the points $\mathrm{P}(4,2,-6)$ and $\mathrm{Q}(10,-16,6)$.

## - Watch Video Solution

## Section C

1. The wholesale price index (or price relative) of onions in 2019 compared to 2017 is 150 . If the cost of onion was ₹ 30 per kg in 2017, calculate the cost in 2019.
A. ₹ 20
B. ₹ 25
C. ₹ 45
D. ₹ 35

## Answer: C

## D Watch Video Solution

2. $D_{1}$ is always equal to
A. P5
B. P10
C. P2O
D. P50

Answer: B
3. The index number of the following data for the year 2019, taking 2018 as base year was found to be 116. The simple aggregate method was used for calculation. Find numerical value of $a, b$, if the sum of prices is, the year 2019 is ₹ 203.

Item Price (in ₹) for year 2019 Price in ₹ for year 2018

| $A$ | 30 |
| :--- | :--- |

$B \quad 25$
20
$C \quad 45$
25
D $\quad 15$
30
E $\quad 35$
$F \quad b$
$a$
50

## - Watch Video Solution

4. Find the $Q_{2}$ for the following distribution. $30,42,33,31,40,45,34,47$, 39

## - Watch Video Solution

5. Compute $D_{3}$ for the following distribution :

The third decile of the following data is.

| Marks | $0-5$ | $5-10$ | $10-15$ | $15-20$ | $20-25$ | Total |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No. of Students | 7 | $x$ | 25 | 40 | $y$ | 120 |

Find the value of $x$ and $y$.

## - View Text Solution

6. Find the median from the following frequency distribution.

| Number of students (f) | 12 | 8 | 32 | 14 | 16 | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Marks (x) | 40 | 18 | 50 | 100 | 80 | 160 |

## - Watch Video Solution

7. From the following frequency distribution, prepare the 'less than' ogive.

| Rainfall (in cm) | $5-15$ | $15-25$ | $25-35$ | $35-45$ | $45-55$ | $55-65$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Number of days | 22 | 10 | 8 | 15 | 5 | 6 |

## Watch Video Solution

8. If $\Sigma\left(x_{i}-2\right)=10, \Sigma\left(y_{i}-5\right)=20, \Sigma x_{i} y_{i}=148$ and $n=5$, find cov $(x, y)$

## - Watch Video Solution

9. The marks of ten intelligent students in two subjects as given below.

Students English Physics

| $A$ | 88 | 74 |
| :--- | :--- | :--- |
| $B$ | 74 | 66 |
| $C$ | 80 | 72 |
| $D$ | 76 | 90 |
| $E$ | 40 | 54 |
| $F$ | 65 | 50 |
| $G$ | 68 | 54 |
| $H$ | 80 | 43 |
| $I$ | 40 | 30 |
| $J$ | 43 | 38 |

Calculate the rank correlation coefficient and interpret your result.
10. The profit of a soft drink firm (in lakhs of rupees) during each month of the year is as given below.
Months Profit (in Lakhs Rupees)
January ..... 42
February ..... 40
March ..... 39
April ..... 35
May ..... 41
June ..... 32
July ..... 40
August ..... 50
September ..... 52
October ..... 56Calculate the four monthly moving averages and the original data on agraph sheet.

