



## MATHS

### BOOKS - S CHAND MATHS (ENGLISH)

### SELF ASSESSMENT PAPER 4

#### Section A

1. The number of proper subsets of  $A = \{1,2,3,4,5\}$  is .....

A. 16

B. 32

C. 15

D. 31

**Answer:**



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2. The maximum value of  $\sin x \cos x$  is .....

A. 1

B. 0

C.  $\frac{1}{2}$

D.  $-\frac{1}{2}$

**Answer:**



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3. The value of  $\frac{1 - \tan 15^\circ}{1 + \tan 15^\circ}$

A. 1

B.  $\sqrt{3}$

C.  $\frac{1}{\sqrt{3}}$

D.  $\infty$

**Answer:**



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4. The third term of a G.P is 3, then the product of its first five terms is .....

A. 9

B. 27

C. 81

D. 243

**Answer:**



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5. If  $\alpha$  and  $\beta$  are the root of the equation  $x^2 - 4x + 5 = 0$ , then  $\alpha^2 + \beta^2 =$  \_\_\_\_\_

A. 64

B. 4

C. 16

D. 256

**Answer:**



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6. Thrid term in the expansion of  $(2x - 3)^5$  is \_\_\_\_\_

A.  $= 240x$

B.  $720x^3$

C.  $720x^2$

D.  $240x$

**Answer:**



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7. The real part of  $(2 + 3i)^2$  is \_\_\_\_\_

A. 4

B. 2

C.  $-5$

D. 12

**Answer:**



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**8.** The distance of the centre of the circle

$x^2 + y^2 + 6x + 8y - 11 = 0$  from origin is \_\_\_\_\_

A. 3

B. 4

C. 5

D. 6

**Answer:**



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9. If the lines  $2x + y - 5 = 0$  and  $kx - 2y + 7 = 0$  are perpendicular, then  $k = \underline{\hspace{2cm}}$

A. 1

B. -1

C. 2

D. -2

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10.  $\lim_{x \rightarrow 0} \frac{1 - \cos 2x}{x^2} = \underline{\hspace{2cm}}$

A. 0

B. 1

C. 2

D.  $\frac{1}{2}$

**Answer:**



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11. Write the range of the signum function.



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12. How many words can be formed using all the letters of the word HEXAGON if repetition is not allowed?

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13. Find the co-efficient of  $x^2$  in the expansion of  $(x + 2)^6$ .

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14. Find the derivative of  $x^2 \sin x$  w.r.t.  $x$ .

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15. A and B are two sets such that  $n(A) = 20$ ,  $n(B) = 30$  and  $n(A \cup B) = 48$ , find  $n(A - B)$

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16. When a coin is tossed write two events which are mutually exclusive and exhaustitve.

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17. Write the sets in the roster form

$$A = \{x : x \in W \text{ and } 5 < x \leq 9\}$$



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18. Write the sets in the roster form

$$B = \{x : x \in N \text{ and } 4 < x^2 < 60\}$$



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19. Prove that :  $\cos 10^\circ + \cos 110^\circ + \cos 130^\circ = 0$ .



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20.

Show

that:

sin

$$(40^\circ + \theta)\cos(10^\circ + \theta) - \cos(40^\circ + \theta)\sin(10^\circ + \theta) = \frac{1}{2}$$

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21. Find the value of  $\sin 75^\circ$ .

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22. Find the value of  $i^4 + i^5 + i^6 + i^7$ .

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23. If  $\alpha$  and  $\beta$  are the roots of  $2x^2 + 5x - 4 = 0$  then

find the value of  $\frac{\alpha}{\beta} + \frac{\beta}{\alpha}$ .

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24. If  $f(x) = y = \frac{ax - b}{cx - a}$ , then prove that  $f(y) = x$ .

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25. Prove that :  $\tan 70^\circ = \tan 20^\circ + 2\tan 50^\circ$

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26. Prove that :  $\frac{\cos 4x \sin 3x - \cos 2x \sin x}{\sin 4x \cdot \sin x + \cos 6x \cdot \cos x} = \tan 2x$

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27. Prove by the principal of mathematica induction that  $3^n > 2^n$ , for all  $n \in \mathbb{N}$ .

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28. Prove by the principle of mathematical induction that for all  $n \in \mathbb{N}$ :

$$1^2 + 2^2 + 3^2 + \dots + n^2 = \frac{1}{6}n(n+1)(2n+1)$$

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29. The roots of the equation  $px^2 - 2(p+2)x + 3p = 0$  differ by 2 Find p and also

the roots.



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30. Find the value of 'a' and 'b'  $\lim_{x \rightarrow 2}$  and  $\lim_{x \rightarrow 4}$  exists

where

$$f(x) \begin{cases} x^2 + ax + b & 0 \leq x < 2 \\ 3x + 2 & 2 \leq x \leq 4 \\ 2ax + 5b & 4 < x \leq 8 \end{cases}$$



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31. If  $y = \frac{x}{x+5}$ , then prove that  $x \frac{dy}{dx} = y(1-y)$



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**32.** Let the sum of  $n$ ,  $2n$ ,  $3n$  terms of an A.P. be  $S_1$ ,  $S_2$  and  $S_3$  respectively. Show that  $S_3 = 3(S_2 - S_1)$ .

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**33.** The sum of two numbers is 6 times their geometric mean, show that the numbers are in the ratio  $(3 + 2\sqrt{2}) : (3 - 2\sqrt{2})$

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34. If  $p$  and  $q$  are the lengths of perpendiculars from the origin to the lines  $x \cos \theta - y \sin \theta = k \cos 2\theta$  and  $x \sec \theta + y \operatorname{cosec} \theta = k$ , respectively, prove that  $p^2 + 4q^2 = k^2$ .



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35. Find the mean deviation about the mean for the following data :

Income per day	0-100	100-200	200-300	300-400	400-500	500-600	600-700	700-800
Number of Persons	4	8	9	10	7	5	4	3



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1. The eccentricity of the ellipse  $\frac{x^2}{16} + \frac{y^2}{4} = 1$  is \_\_\_\_\_

A.  $\frac{1}{2}$

B.  $\frac{\sqrt{3}}{2}$

C. 1

D. 0

**Answer:**



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2. XY plane divides the line segment joining the points (1,2,-3) and (0,1,5) in the ratio \_\_\_\_\_

A. 2 : 1 internally

B. 2 : 1 externally

C. 3 : 5 internally

D. 3 : 5 internally

**Answer:**



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**3.** Find the length of transverse axis of the hyperbola

$$4x^2 - 3y^2 = 24.$$



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4. The major axis of an ellipse is twice its minor axis.

Find its eccentricity.



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5. Write the converse : If 2 and 3 are even, then  $2 + 3 =$

6'.



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6. Write converse and inverse of the given statement if

$y^2$  is divisible by 4, then  $y$  is an even number.



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7. Show that the statement "For any real numbers  $a$  and  $b$ ,  $a^2 = b^2$  implies that  $a = b$ " is not true by giving a counter example.



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8. Find the foci, vertices and eccentricity of the ellipse  $36x^2 + 4y^2 = 144$ .



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9. If the origin is the centroid of the  $\Delta PQR$  with vertices  $P(2a, 2, 6)$ ,  $Q(-4, 3b, 10)$  and  $R(8, 14, 2c)$

then find the values of  $a + b + c$ .

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**10.** What are the coordinate of the vertices of a cube whose edge is 2 units, one of whose vertices coincides with the origin and three edge passing through the origin coincides with the positive direction of the axis  $\theta$  through the origin.

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1. The median of the 10 different observations is 46. If the observation 70 is replaced with 100 then the new median is \_\_\_\_\_

A. 70

B. 100

C. 46

D. can't be determined

**Answer:**



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2. The mean of 10 different observation is 46. If the observation 71 is replaced with 17 the new mean is \_\_\_\_\_



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3. Find the median of the following set of numbers : 10, 75, 3, 81, 18, 27, 4, 48, 12, 47, 9, 15



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4. The number of students in section X A and X B are 30 and 35 respectively. The mean scores of students in the

mathematices test are as follows:

$\bar{X}_A$	$\bar{X}_B$	$\bar{X}_A$ and $\bar{X}_B$ combined
70	?	62



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5. Construct Consumer Price Index number with the help of the following data :

Consumer Items	Price	Weight
Food	125	40
Fuel	120	10
Cloth	66.67	25
House Rent	120	15
Miscellaneous	150	10



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6. A school has four sections in Class XII having 50, 39, 42, 48 students of the four section. In a mathematics test the average marks were 60, 55, 57 and 48 respectively. What was the overall average of the marks per student?

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7. Given  $r = 0.8$ ,  $\sum xy = 60$ ,  $\sigma_y = 2.5$  and  $\sum x^2 = 90$ , find the number of items, where  $x$  and  $y$  are deviation from their respective means.

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8. The mean age of a combined group of men and women is 25 years. If the mean age of the group of men is 26 years and that of group that of women is 21 years, then find the percentage of men and women in the group.



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9. If  $\sum x_1 = 16$ ,  $\sum y_1 = 48$

$\sum (x_1 - 3)(y_1 - 4) = 22$  and  $n = 2$ , find the cov (x,y).



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10. Calculate five yearly moving average of the number of students of who have studied in a school given below.

Year	1993	1994	1995	1996	1997	1998	1999	2000	2001	2002
No. of Students	442	427	467	502	512	515	520	527	515	541



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