



## MATHS

### BOOKS - PATHFINDER MATHS (BENGALI ENGLISH)

## FUNCTION

#### Question Bank

1. Let the question  $f(x) = \log x^2$  and  $\phi(x) = 2\log x$ , then

A. a)  $f(x) \leq \phi(x)$

B. b)  $f(x) \neq \phi(x)$

C. c)  $f = \phi$

D. d)  $f \neq \phi$

**Answer: D**



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2. If  $f(x) = (p - x^n)^{\frac{1}{n}}$ ,  $p > 0$  and  $n$  is positive integer, then the value of  $f[f(x)]$

- A. a)  $-x$
- B. b)  $x^2$
- C. c)  $x$
- D. d)  $x + a$

**Answer: C**



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3. The range of the function  $\frac{x}{2 + x^2}$  is

- A.  $\left[ \frac{1}{2\sqrt{2}}, -\frac{1}{2\sqrt{2}} \right]$
- B.  $\left[ -\frac{1}{2\sqrt{2}}, -\frac{1}{2\sqrt{2}} \right]$

C.  $\left[ -\frac{1}{2\sqrt{2}}, \frac{1}{2\sqrt{2}} \right]$

D.  $\left[ \frac{1}{2\sqrt{2}}, \frac{1}{2\sqrt{2}} \right]$

**Answer: C**



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4. The function  $x$  and  $\frac{x^2}{x}$  are identical for

A.  $x \geq 0$

B.  $x \leq 0$

C.  $x > 0$  or  $x < 0$

D.  $x = 0$

**Answer: C**



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5. The inverse function of  $\log_e x$  is

A. a)  $e^x$

B. b)  $1/x$

C. c)  $\frac{1}{\log_e x}$

D. d)  $\frac{x}{\log_e x}$

**Answer: A**



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6. If  $f(x + y) = f(x) + f(y)$ , then the value of  $f(0)$

A. a) -1

B. b) 0

C. c) 1

D. d) None of these

**Answer: B**



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7. If the function  $f(x)$  satisfies the condition  $f\left(x + \frac{1}{x}\right) = x^2 + \frac{1}{x^2}$ ,  $x \neq 0$  then  $f(x)$  is

A. a)  $x^2 + 2$

B. b)  $x^2 - 2$

C. c)  $2 - x^2$

D. d)  $\frac{x^2}{2}$

**Answer: B**



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8. The domain of definition of  $f(x) = \sin^{-1}\left(\frac{\log_3 x}{3}\right)$  is

A. a)  $1 \leq x \leq 9$

B. b)  $0 \leq x \leq 9$

C. c)  $3 \leq x < 9$

D. d)  $1 < x < 9$

**Answer: A**

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9. The domain of definition of  $f(x) = \sqrt{\log_e \left( \frac{4x - x^2}{3} \right)}$  is

A.  $0 < x < 3$

B.  $x > 1$

C.  $1 \leq x \leq 3$

D.  $x < 3$

**Answer: C**

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10. The range of the function  $f(x) = \sin x + \cos x$  is

A. a)  $-\sqrt{2} < f(x) < \sqrt{2}$

B. b)  $-\sqrt{2} \leq f(x) \leq \sqrt{2}$

C. c)  $f(x) \leq \sqrt{2}$

D. d)  $0 < f(x) < \sqrt{2}$

**Answer: B**



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11. If  $f(x) = \frac{a^x + a^{-x}}{2}$ , ( $a > 2$ ) then the value of  $f(x + y) + f(x - y)$  is equal to

A. a)  $2f(x) \cdot f(y)$

B. b)  $f(x) \cdot f(y)$

C. c)  $\frac{f(x)}{f(y)}$

D. d)  $f(xy)$

**Answer: A**



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12. If  $f(x) = \frac{1}{1-x}$ , then  $f[f\{f(x)\}]$  is

A. a) 0

B. b)  $x$

C. c)  $-x$

D. d)  $\frac{1}{1+x}$

**Answer: B**



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13. If  $f(x) = x^2$  and  $g(x) = \sqrt{x}$ , then the correct relation will be

A.  $g\{f(4)\} = 4$

B.  $g\{f(3)\} = 6$

C.  $g\{f(-2)\} = -2$

D.  $g\{f(2)\} = 4$

**Answer: A**



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14. If  $f(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}} + 2$ , then the inverse function will be

A.  $\frac{1}{2} \frac{\log_e(x-2)}{x-1}$

B.  $\frac{1}{2} \frac{\log_e(x-1)}{3-x}$

C.  $\frac{1}{2} \frac{\log_e x}{2-x}$

D.  $-2 \log_e \left( \frac{x-1}{1+x} \right)$

**Answer: B**



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15. If  $f(x + 2) = 2x^2 + 5x + 7$ , then the value of  $f(1)$

A. 0

B. -2

C. 2

D. 4

**Answer: D**



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16. The range of the function  $f(x) = \frac{1}{4 + 2 \sin x}$  is

A.  $(1/6, 1/2)$

B.  $[1/6, 1/2]$

C.  $[1/6, 1/2]$

D.  $(1/6, 1/2]$

**Answer: C**

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17. Domain of definition of  $f(x) = \sin^{-1}\left(\frac{3 - 2x}{5}\right)$

A. a)  $[-1, 4]$

B. b)  $(-1, 4)$

C. c)  $[0, \infty]$

D. d)  $(-\infty, 4)$

**Answer: A**

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18. If  $f(x) = \frac{Kx}{1+x}$ ,  $x \neq -1$  and  $f\{f(x)\} = x$ , then the value of  $k$

A. a)  $-\sqrt{2}$

B. b)  $-1$

C. c)  $1$

D. d)  $\sqrt{2}$

**Answer: B**



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19. If  $f(x) + 2f(1-x) = x^2 + 2$ ,  $\forall x \in R$ , then  $f(x)$  is

A. a)  $x^2 - 2$

B. b)  $1$

C. c)  $\frac{1}{3}(x-2)^2$

D. d)  $\frac{1}{2}(x-2)$

**Answer: C**

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20. Let  $f: (-\infty, 1] \rightarrow (-\infty, 1]$  such that  $f(x) = x(2-x)$ , then  $f^{-1}(x)$  is

A.  $1 + \sqrt{1-x}$

B.  $1 - \sqrt{1-x}$

C.  $\sqrt{1-x}$

D.  $\sqrt{1+x}$

**Answer: B**

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21. Let  $f$  be a function such that  $f(x+y) = f(x) + f(y) \quad \forall x, y \in R$ , if  $f(1) = k$ , then show that  $f(n)$  is equal to  $nk$ .

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22.  $f$  is a function such that  $f(x + y) = f(x) \cdot f(y), \forall x, y \in R$ , if  $f(1) = 3$ , then

find  $\sum_{r=1}^n f(r)$ .

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23. Find domain of  $f(x) = \sqrt{1 - \sqrt{1 - \sqrt{1 - x^2}}}$ .

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24. If  $f(x) = \sin x + \cos x$ ,  $g(x) = x^2 - 1$  then show that  $g(f(x))$  is invertible in

the domain  $\left[-\frac{\pi}{4}, \frac{\pi}{4}\right]$ .

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25. If  $f(x) = \frac{4^x}{4^x + 2}$ , then find  $f(x) + f(1 - x)$ .

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26. If  $2f(x) - 3f(1/x) = x^2$  ( $x \neq 0$ ), then find  $f(2)$ .

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27. If  $f(x) = \cos[\pi^2]x + \cos[-\pi^2]x$ , where  $[x]$  stands for the greatest integer function, then find  $f\left(\frac{\pi}{2}\right)$ ,  $f\left(\frac{\pi}{4}\right)$ .

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28. Find the range of  $f(x) = \frac{x^2 + x + 2}{x^2 + x + 1}$  ( $-\infty < x < \infty$ )

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29. Find the domain of definition of the function  $f(x) = \frac{1}{\sqrt{|x| + x}}$ .

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30. If  $f : \mathbb{R} \rightarrow \mathbb{R}$  such that  $f(x) = x - [x]$ , where  $[p]$  denotes the greatest integer less than or equal to  $p$ , then find  $f^{-1}(x)$ , if exists.

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31. Find the range of the function  $f(x) = x^2 + \frac{1}{x^2 + 1}$ .

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32. Find the range of the function  $\phi$  where  $\phi(x) = \cos^{-1}\left(\frac{x^2}{1+x^2}\right)$ .

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33. Find the range of the function  $f(x) = |x - 1| + |x - 2|$ ,  $-1 \leq x \leq 3$

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34. Find the range of the function  $y = \log_3(5 + 4x - x^2)$ .



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35. If  $f(x + y) = f(x) - f(y), \forall x, y \in \mathbb{R}$ , then show that  $f(3) = f(1)$



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36. Find the range of the function  $f(x) = (e^x - e^{-x})$ .



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37. Find the inverse function of the function  $f(x) = \left[4 - (x - 7)^3\right]^{\frac{1}{5}}$ .



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38. If  $f(x) = e^{x+a}$ ,  $g(x) = x^{b^2}$  and  $h(x) = e^{b^2x}$ , then find the value of  $\frac{g\{f(x)\}}{h(x)}$



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39. Find domain of the function  $f(x) = 2^{\sin^{-1}(-1)x + 1/\sqrt{x-2}}$ .



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40. Prove that the domain of  $g(x) = \frac{\cot^{-1} x}{\sqrt{x^2 - [x]}}$ ,  $x \in R$  is  $R - \{\sqrt{n} : n \geq 0, n \in z\}$ .



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41. Find the range of the function  $y = \frac{1}{2 - \cos 2x}$ .



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42. Find the range of the function  $y = \frac{\log_2(\sin x + \cos x + 3\sqrt{2})}{\sqrt{2}}$

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43. Find the value of  $x$  which  $f(x) = \frac{1}{\sqrt{|x| - x}}$  is not defined.

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44. Find the range of  $y = \frac{x}{1 + x^2}$

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45. If  $f(x) = \cos(\log_e x)$ , then find the value of  $f(x) \cdot f(y) - \frac{1}{2} \left[ f\left(\frac{x}{y}\right) + f(xy) \right]$

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46. Find the domain of  $f(x) = \sin^{-1} \left[ \log_9 \left( \frac{x^2}{4} \right) \right]$



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47. Without using graph paper the graph of the function  $y = f(x) = |x - 1| + |x + 1|$  for  $-2 \leq x \leq 2$  and examine whether the function has any point of discontinuity.



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48. Without using graph paper draw a sketch graph of the function  $f(x) = 2 + |x^2 - 4|$ .



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49. Find the domain of the function  $F(x) = \tan^{-1} \sqrt{x(x+1)} + \sin^{-1} \sqrt{x^2 + x + 1}$



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50. Find the range of the function  $f(x) = \frac{\sec^2 x - \tan x}{\sec^2 x + \tan x}$ ,  $\left(-\frac{\pi}{2} < x < \frac{\pi}{2}\right)$ .

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51. Find the domain of function  $f(x) = \cos^{-1}\left(\frac{2 - |x|}{4}\right) + \frac{1}{\log(3 - x)} + \sqrt{x}$ .

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52. If  $2f(x) + 3f(-x) = 15 - 4x$  for all real values of  $x$ , then show that  $f(x) = 3 + 4x$ .

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53. If  $2f(x - 1) - f\left(\frac{1 - x}{x}\right) = x$  find  $f(x)$ .

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54. Find the inverse function of the function  $f(x) = \left[4 - (x - 7)^3\right]^{\frac{1}{5}}$ .

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55. If  $f(n + 1) = \frac{2f(n) + 1}{2}$ ,  $n = 1, 2, 3, \dots$  and  $f(1) = 2$ , then find the value of  $f(101)$

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56.  $f(x) = \frac{\alpha x}{x + 1}$  ( $x \neq -1$ ), then for what value of  $\alpha$ ,  $f\{f(x)\} = x$ ?

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57. Find the range of  $f(x) = {}^{7-x}P_{x-3}$ .

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58. Find the inverse function of the function  $f(x) = 2^{x(x-1)}$  ( $x > 0$ ).

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59. If  $f(x) = \log_e \frac{1+x}{1-x}$  and  $g(x) = \frac{3x+x^3}{1+3x^2}$ , then prove that  $f[g(x)] = 3 \cdot f(x)$ .

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60. If  $f(x) = ax^2 + bx + c$  find  $a, b$  so that  $f(x+1) = f(x) + x + 1$  may hold identically.

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61.  $c$  is any real number and  $c \neq 0$ . Prove that  $|f(c) - f(-c)| = 2$ ,

where  $f(x) = \frac{|x|}{x}$

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62. Find the range of  $f(x) = 3 \sin \sqrt{\frac{\pi^2}{16} - x^2}$ .

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63.  $2f(1/x) - f(x) = 5x$ , find the value of  $f(x + 1/x)$ .

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64. Find the Domain of definition of the function  $f(x) =$

$$\sqrt{\log_{10} \left( \frac{3x - x^2}{2} \right)} + \sqrt{x - \frac{3}{2}}$$

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65. If  $g(x) = \frac{1}{x^2}$ , show that  $g(x) - g(x + 1) = \frac{2x + 1}{x^2(x + 1)^2}$ .

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66. Find the domain of definition of the function  $f(x) = \log_{10} \log_{10} \log_{10} \{(x + 1)(x - 2)\}$ .

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67. For which  $y$  can be a function of  $x$ . ( $x \in R, y \in R$ )

$$(x - h)^2 + (y - k)^2 = r^2$$

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68. For which  $y$  can be a function of  $x$ . ( $x \in R, y \in R$ )

$$y^2 = 4ax$$

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69. For which  $y$  can be a function of  $x$ . ( $x \in R, y \in R$ )

$$x^4 = y^2$$



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70. For which  $y$  can be a function of  $x$ . ( $x \in R, y \in R$ )

$$x^6 = y^3$$



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71. For which  $y$  can be a function of  $x$ . ( $x \in R, y \in R$ )

$$3y = (\log x)^2$$



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72. If,  $f(x) = \log\left(\frac{1+x}{1-x}\right)$ , show that  $f(x) + f(y) = f\left(\frac{x+y}{1+xy}\right)$

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73. Let  $f: \left[-\frac{\pi}{2}, \frac{\pi}{2}\right] \rightarrow [-1, 1]$ , where  $f(x)=\sin x$ . Find whether  $f(x)$  is one-one or not.

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74. Show  $f: \mathbb{R} \rightarrow \mathbb{R}$  defined by  $f(x)=x^2 + x$  for all  $x \in \mathbb{R}$  is many one.

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75. Find number of surjection from A to B where  $A=\{1,2,3,4\}$ ,  $B=\{a,b\}$

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76.  $f(x) = \frac{x^5}{5} - \frac{8}{3}x^3 + (16 + c)x$ , then find the range of  $c$ , so that function is one-one function.

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77. Find Domain of the following function :

$$f(x) = \sqrt{\log_{0.4} \left( \frac{x-1}{x+5} \right)}$$

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78. Find Domain of the following function :

$$f(x) = \sin^{-1} \left( \log_2 \left( \frac{x^2}{2} \right) \right)$$

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79. Find Domain of the following function :

$$f(x) = \log_{x-4} (x^2 - 11x + 24)$$

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**80.** Find Domain of the following function :

$$f(x) = \sin^{-1}[2x^2 - 3], \text{ where } [.] \text{ denotes G.I.F.}$$

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**81.** Find the range of the following function

$$f(x) = x^2 - 3x + 2$$

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**82.** Find the range of the following function

$$f(x) = \sin^2 x - 5 \sin x - 6$$

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**83.** Find the range of the following function

$$f(x) = (x - [x]) / (1 + x - [x])$$



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84. Find the range of the following function

$$y = \log_3 \left( \log_{1/2} (x^2 + 4x + 4) \right)$$

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85. Find the range of the following function

$$f(x) = \log_2 \left( \frac{\sin x - \cos x + 3\sqrt{2}}{\sqrt{2}} \right)$$

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86. Find the range of the following function

$$f(x) = \sin^{-1} \left[ x^2 + \frac{1}{2} \right] + \cos^{-1} \left[ x^2 - \frac{1}{2} \right], \quad [.] \text{ denotes the Greatest integer function.}$$

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87. Let  $f(x) = \sqrt{x - 2}$ ,  $g(x) = \sqrt{5 - x}$  find  $f(x)+g(x)$ ,  $f(x)-g(x)$ ,  $f \cdot g$ ,  $(f/g)$



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88. Find which of the following functions is even or odd ?

$$f(x) = x^2 + |\sin x| + \cos x$$



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89. Find which of the following functions is even or odd ?

$$f(x) = \log(x + \sqrt{1 + x^2})$$



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90. Find which of the following functions is even or odd ?

$$f(x) = \log\left(\frac{a + x}{a - x}\right)$$



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91. Find which of the following functions is even or odd ?

$$f(x) = \cos(1 + \cos x) + \cos(1 + \sin x)$$

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92. If  $f$  is an even function defined in the interval  $(-5, 5)$ , find four real values of  $x$  satisfying the equation  $f(x) = f\left(\frac{x+1}{x+2}\right)$

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93. If  $f(x+y) + f(x-y) = 2f(x).f(y) \forall x, y \in R$ .  $f(0) \neq 0$ , find if  $f(x)$  is even or odd function.

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94. Find whether the given function is even or odd function, where

$$f(x) = \frac{x(\sin x + \tan x)}{\left[ \frac{x+\pi}{\pi} - \frac{1}{2} \right]}, \text{ where, } [.] \text{ denotes greatest integer function.}$$

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95. If  $f: [-20, 20] \rightarrow R$  defined by  $f(x) = \left[ \frac{x^2}{a} \right] \sin x + \cos x$  is an even function. Then evaluate the set of values of 'a'

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96. Find the period of

$$f(x) = \sin x + \tan \frac{x}{2} + \sin \frac{x}{2^2} \tan \frac{x}{2^3} + \dots + \sin \frac{x}{2^{n-1}} + \tan \frac{x}{2^n}$$

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97. Find the period of the real valued function satisfying

$$f(x) + f(x+4) = f(x+2) + f(x+6)$$



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98. Let  $g(x)=1+x-[x]$  and  $f(x) = \begin{cases} -1 & x < 0 \\ 0 & x = 0 \\ 1 & x > 0 \end{cases}$  Then for all  $x$  find  $f(g(x))$



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99. Two functions are defined as under,  $f(x) = \begin{cases} x + 1 & x \leq 1 \\ 2x + 1 & 1 < x \leq 2 \end{cases}$   
 $g(x) = \begin{cases} x^2 & -1 \leq x < 2 \\ x + 2 & 2 \leq x \leq 3 \end{cases}$

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100. If  $f: [1, \infty) \rightarrow [2, \infty)$  given by  $f(x)=x+1/x$  then find  $f^{-1}(x)$ , (assume bijective).



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**101.** Let  $f: [1/2, \infty) \rightarrow [3/4, \infty)$  where  $f(x) = x^2 - x + 1$ . Find the inverse of  $f(x)$ . Hence or otherwise solve the equation,

$$x^2 - x + 1 = \frac{1}{2} + \sqrt{x - 3/4}$$

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**102.** Let  $g(x)$  be the inverse of  $f(x)$  and  $f'(x) = \frac{1}{1+x^3}$ . Then find  $g'(x)$  in terms of  $g(x)$ .

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**103.** If the function  $f: \mathbb{R} \rightarrow A$  is given by  $f(x) = \frac{e^x - e^{-|x|}}{e^x + e^{|x|}}$  is surjective, find  $A$ .

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**104.** Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  defined by  $f(x) = \frac{x^2}{1+x^2}$ . Prove that  $f$  is neither injective nor surjective.



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105. Let  $A = \mathbb{R} - \{3\}$ ,  $B = \mathbb{R} - \{1\}$  and  $f: A \rightarrow B$  defined by  $f(x) = \frac{x-2}{x-3}$ . Is 'f' bijective? Give reason.



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106. Let  $f: X \rightarrow Y$  be a function defined by  $f(x) = a \sin\left(x + \frac{\pi}{4}\right) + b \cos x + c$ . If  $f$  is both one-one and onto, find sets  $X$  and  $Y$ .



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107. Find the domain of the following :

$$f(x) = {}^{16-x}C_{2x-1} + {}^{20-3x}P_{4x-5}$$



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108. Find the domain of the following :

$$f(x) = \sin^{-1}\left(\frac{3-2x}{5}\right) + \sqrt{3-x}$$

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109. Find the domain of the following :

$$f(x) = \sqrt{x^2 - |x| - 2}$$

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110. Find the domain of the following :

$$f(x) = \frac{\log_{2x} 3}{\cos^{-1}(2x-1)}$$

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111. Find the range of the following function

$$f(x) = \max\{\sin x, \cos x\}$$



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112. Find the range of the following function

$$f(x) = |x - 1| + |x - 2|, \quad -1 \leq x \leq 3$$



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113. Find the domain and range for  $f(x) = \left[ \log \left( \sin^{-1} \sqrt{x^2 + 3x + 2} \right) \right]$ ,



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114. Determine whether even or odd:

$$f(x) = x \left( \frac{a^x + 1}{a^x - 1} \right)$$



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115. A function is defined for all real numbers is defined for  $x > 0$  as follows:

$$f(x) = \begin{cases} x|x| & 0 \leq x < 1 \\ 2x & x \geq 1 \end{cases}$$

How is  $f$  defined for  $x \leq 0$

If  $f$  is even

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**116.** A function is defined for all real numbers is defined for  $x > 0$  as follows:

$$f(x) = \begin{cases} x|x| & 0 \leq x < 1 \\ 2x & x \geq 1 \end{cases}$$

How is  $f$  defined for  $x \leq 0$

If  $f$  is odd

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**117.** Show that the function  $f(x) = \frac{2x(\sin x + \tan x)}{2\left[\frac{x+21\pi}{\pi}\right] - 41}$  is symmetric about origin.

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118. Find the period of following function

$$f(x) = [\sin 3x] + [\cos 6x]$$

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119. Find the period of following function

$$f(x) = \frac{1}{2} \left\{ \frac{|\sin x|}{\cos x} + \frac{|\cos x|}{\sin x} \right\}$$

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120. Find the period of following function

$$f(x) = e^{\ln(\sin x)} + \tan^3 x - \operatorname{cosec}(3x - 5)$$

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121. Let  $f(x+p) = 1 + \{2 - 3f(x) + 3(f(x))^2 - (f(x))^3\}^{1/3}$ , for all  $x$  in  $\mathbb{R}$  where  $p > 0$ , then prove  $f(x)$  is periodic.



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122. Let  $f(x)$  be defined on  $[-2,2]$  and is given by

$$f(x) = \begin{cases} -1 & -2 \leq x < 0 \\ x - 1 & 0 \leq x \leq 2 \end{cases} \text{ and}$$

$g(x)=f(|x|)+|f(x)|$ , then find  $g(x)$ .

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123.  $f(x) = \begin{cases} x - 1 & -1 \leq x < 0 \\ x^2 & 0 < x \leq 1 \end{cases}$  and  $g(x)=\sin x$ . Then find

$$h(x)=f(|g(x)|)+|f(g(x))|$$

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124. Find the inverse of the following function:

$$f(x) = \sin^{-1}\left(\frac{x}{3}\right), x \in [-3, 3]$$

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125. Find the inverse of the following function:

$$f(x) = \log_e(x^2 + 3x + 1), x \in [1, 3]$$

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126. Find the inverse of the following function:

$$f(x) = \log_e(x + \sqrt{x^2 + 1})$$

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127. If the function  $f: [1, \infty) \rightarrow [1, \infty)$  is defined by  $f(x) = 2^{x(x-1)}$ , then find  $f^{-1}(x)$

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128.  $f(x) = \sin^{-1}(x - 1) + \cos^{-1}(x - 2)$ , then domain of  $f(x)$  is

A.  $[0, 2]$

B. [1,2]

C. [0,3]

D. [1,3]

**Answer: D**



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**129.** The domain of definition of the function  $y(x)$  given by the equation

$$2^x + 2^y = 2 \text{ is}$$

A.  $0 < x \leq 1$

B.  $0 \leq x < 1$

C.  $-\infty < x \leq 0$

D.  $-\infty < x < 1$

**Answer: D**



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130. Domain of the function  $f(x) = \frac{1}{\sqrt{{}^{10}C_{x-1} - 3 \cdot {}^{10}C_x}}$  contains

the points

A.  $\{9,10,11\}$

B.  $\{9,10,12\}$

C. all natural numbers

D. none of these

**Answer: D**



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131. Domain of the function  $f(x) = \frac{x}{\sqrt{\sin(2nx) - \cos(2nx)}}$  is

A.  $\left(e^{2n\pi}, e^{3n + \frac{1}{2}\pi}\right)$

B.  $\left(e^{2n + \frac{1}{4}\pi}, e^{2n - \frac{5}{4}\pi}\right)$

C.  $\left(e^{(2n + \frac{1}{4})\pi}, e^{(2n + \frac{5}{4})\pi}\right)$

D. none of these

**Answer: C**

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132. If  $f(x) = \sqrt{\sec^{-1}\left(\frac{2 - |x|}{4}\right)}$ , then the domain of  $f(x)$  is

A.  $[-2, 2]$

B.  $[-6, 6]$

C.  $(-\infty, -6] \cup [6, \infty)$

D.  $[-6, -2] \cup [2, 6]$

**Answer: C**

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133. The range of the function  $f(x) = \sin^{-1}(\log[x]) + \log(\sin^{-1}[x])$ ,  
(where  $[.]$  denotes the greatest integer function) is

A.  $\mathbb{R}$

B.  $[1,2)$

C.  $\left\{ \log\left(\frac{\pi}{2}\right) \right\}$

D.  $\{ -\sin 1 \}$

**Answer: C**



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134. If

$$f(x) = \lim_{n \rightarrow \infty} \left[ \frac{x}{x+1} + \frac{x}{(x+1)(2x+1)} + \frac{x}{(2x+1)(3x+1)} + \dots + \frac{x}{(n-1)x+1} \right]$$

, then range of  $f(x)$  is

A.  $\{0, 1\}$

B.  $\{-1, 0\}$

C.  $\{-1, 1\}$

D.  $[-1,1]$

**Answer: A**



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**135.** Find the range of the following function

$$f(x) = \log_2 \left( \frac{\sin x - \cos x + 3\sqrt{2}}{\sqrt{2}} \right)$$

A.  $[1,2]$

B.  $[0,1]$

C.  $(1,2)$

D.  $(0,1)$

**Answer: A**



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136. If  $-\frac{\pi}{2} < x < \frac{\pi}{2}$ , then the range of the function  $f(x) = \cos[x]$  is

A.  $\{1, \cos 1, \cos 2\}$

B.  $\{\cos 1, -\cos 1, 1\}$

C.  $\{-1, 0, 1\}$

D.  $\{-1, 1\}$

Answer: A



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137. If  $f: R \rightarrow R$  is defined by  $f(x) = \frac{1}{2 - \cos 3x}$  for each  $x \in R$ , then

the range of  $f$  is

A.  $(1/3, 1)$

B.  $[1/3, 1]$

C.  $(1, 2)$

D.  $[1, 2]$



**Answer: B**



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**138.** If  $f(x + y) = f(x)f(y) \forall x, y \in R, f(0) \neq 0$  then

$$F(x) = \left\{ \frac{f(x)}{(1 + (f(x)))^2} \right\} \text{ is}$$

A. even

B. odd

C. both even or odd

D. neither even nor odd

**Answer: A**



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**139.** A function satisfies the conditions

$$f(x + y) = f(x) + f(y), \forall x, y \in R \text{ then } f \text{ is}$$

- A. an even function
- B. an odd function
- C. neither even or odd
- D. none of these

**Answer: B**

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**140.** If the function  $f(x) = [3.5 + b \sin x]$  (where  $[.]$  denotes the greatest integer function) is an even function then complete set of values of 'b' is :

- A.  $(-0.5, 0.5)$
- B.  $[-0.5, 0.5]$
- C.  $(0,1)$
- D.  $[-1, 1]$

**Answer: A**

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141. Function  $f(x) = \log(x^3 + \sqrt{1+x^6})$  is

- A. even function
- B. odd function
- C. algebraic function
- D. discontinuous function

**Answer: B**

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142. If the function  $f$  satisfies the relation

$f(x+y) + f(x-y) = 2f(x) \times f(y), \forall x, y, \in R$  and  $f(0) \neq 0$ , then

- A. an even function
- B. an odd function

C. neither even or odd

D. none of these

**Answer: A**



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143. If  $\sum_{k=0}^n f(x + ka) = 0$  where  $a > 0$ , then the period of  $f(x)$  is

A.  $a$

B.  $(n + 1)a$

C.  $\frac{a}{n} + 1$

D.  $f(x)$  is non-periodic

**Answer: B**



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144. Function  $f$  satisfies the equation  $f(x + a) = \left\{ \frac{1 + f(x)}{1 - f(x)} \right\} \forall x \in R$

then the period of the function is

A.  $a$

B.  $2a$

C.  $4a$

D.  $8a$

Answer: C



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145. If  $f'(x) = \left\{ \frac{1 - 2 \sin^2 x}{f(x)} \right\}$ ,  $f(x) \geq 0$ ,  $\forall x \in R$  and  $f(0)=1$ , then  $f(x)$

is a periodic function with the fundamental period

A.  $\pi$

B.  $2\pi$

C.  $\frac{\pi}{2}$

D. none of these

**Answer: A**

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**146.** If  $a, b$  be two fixed positive integers such that  $f(a+x) = b + \left[ b^3 + 1 - 3b^2 f(x) + 3b f(x)^2 - (f(x))^3 \right]^{\frac{1}{3}}$  for all real  $x$ , then  $f(x)$  is a periodic function with period.

A.  $a$

B.  $2a$

C.  $b$

D.  $2b$

**Answer: B**

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147. Period of  $f(x) = \sin, \frac{\pi}{2}x + 2 \cos, \frac{\pi}{3}x - \tan, \frac{\pi}{4}x$  is equal to

- A. 4
- B. 8
- C. 12
- D. 16

**Answer: C**



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148. Polynomial function  $f(x)$  satisfying the condition

$f(x), f\left(\frac{1}{x}\right) = f(x) + f\left(\frac{1}{x}\right)$ . If  $f(10)=1001$ , then  $f(20)$  is

- A. 7001
- B. 8001
- C. 8000

D. none of these

**Answer: B**

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**149.** The function  $f(x)$  is defined for all real  $x$ . If  $f(a + b) = f(ab) \forall a$  and  $b$  and  $f\left(-\frac{1}{2}\right) = -\frac{1}{2}$ , then  $f(2009)$  equals

A. -2009

B. 2009

C.  $-\frac{1}{2}$

D.  $-\frac{2000}{2}$

**Answer: C**

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150.

If

$$f''(x) = -f(x) \text{ and } g(x) = -f'(x) \text{ and } F(x) = \left(f\left(\frac{x}{2}\right)\right)^2 + \left(g\left(\frac{x}{2}\right)\right)^2$$

and given that  $f(5)=5$ , then  $f(10)$  is equal to

- A. 5
- B. 10
- C. 0
- D. 15

**Answer: A**



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151. If  $f \circ g = |\sin x|$  and  $g \circ f = \sin^2 \sqrt{x}$  then  $f(x)$  and  $g(x)$  are

- A.  $f(x) = \sqrt{\sin x}$ ,  $g(x) = x^2$
- B.  $f(x) = |x|$ ,  $g(x) = \sin x$
- C.  $f(x) = \sqrt{x}$ ,  $g(x) = \sin^2 x$

D.  $f(x) = \sin \sqrt{x}$ ,  $g(x) = x^2$

**Answer: C**



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**152.** If  $f$  is a function such that  $f(0)=2$ ,  $f(1)=3$  and  $f(x + 2) = 2f(x) - f(x + 1)$  for every real  $x$  then  $f(5)$  is

A. 7

B. 13

C. 1

D. 5

**Answer: B**



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153. Let  $f(x) = \begin{cases} -1 + \sin K_1\pi x & \text{if } K_1 \text{ is rational} \\ 1 + \cos K_2\pi x & \text{if } K_2 \text{ is irrational} \end{cases}$  If  $f(x)$  is periodic function, then:

A. either  $K_1, K_2 \in \text{rational}$  or  $K_1, K_2 \in \text{irrational}$

B.  $K_1, K_2 \in \text{rational}$  only

C.  $K_1$  and  $K_2 \in \text{irrational}$  only

D.  $K_1$  and  $K_2 \in \text{irrational}$  such  $\frac{K_1}{K_2}$  is rational.

**Answer: B**



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154. Let  $f(1) = 1$  and  $f(n) = 2 \sum_{r=1}^{n-1} f(r)$ . Then  $\sum_{n=1}^m f(n)$  is equal to

A.  $3^{m-1} - 1$

B.  $3^m - 1$

C.  $3^m - 1$

D. none of these

**Answer: B**



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155. Given  $f(x) = \ln\left\{\frac{1+x}{1-x}\right\}$  and  $g(x) = \left\{\frac{3x+x^3}{1+3x^2}\right\}$ . Then  $f(g(x))$  is equal to

A.  $-f(x)$

B.  $3f(x)$

C.  $[f(x)]^2$

D. none of these

**Answer: B**



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156. If  $f: [2, 3) \rightarrow [0, 1)$  is defined by  $f(x) = x - [x]$ , the fractional part of  $x$ , then  $f^{-1}(x)$

- A. equals  $x+2$
- B. equals  $x-2$
- C. does not exist
- D. none of these

**Answer: A**



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157. The domain of  $y = \cos^{-1}\left(\frac{1 - 2|x|}{3}\right) + \log_{|x-1|} x$  is

- A. (0,2)
- B.  $(0, 1) \cup (1, 2)$
- C. (1,3)

D. (3,5)

**Answer: B**

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**158.** Let  $f: \left[-\frac{\pi}{3}, 2\frac{\pi}{3}\right] \rightarrow [0, 4]$  be a function defined as  $f(x) = \sqrt{3}\sin x - \cos x + 2$ . Then  $f^{-1}(x)$  is given by

A.  $\sin^{-1}\left(\frac{x-2}{2}\right) - \frac{\pi}{6}$

B.  $\sin^{-1}\left(\frac{x+2}{2}\right) + \frac{\pi}{6}$

C.  $2\frac{\pi}{3} - \cos^{-1}\left(\frac{x-2}{2}\right)$

D. none of these

**Answer: C**

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159. Let  $n$  be a positive integer with  $f(n) = 1! + 2! + 3! + \dots + n!$  and  $P(x)$  and  $Q(x)$  be polynomials in  $x$  such that  $f(n + 2) = Q(n)f(n) + P(n)f(n + 1)$ . Find  $P(2)$ .

A.  $P(x) = x + 3$

B.  $Q(x) = -1 + 2$

C.  $P(x) = -1 - 2$

D.  $Q(x) = x + 3$

Answer: A



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160. A function  $f: R \rightarrow R$  is defined by  $f(x + y) - kxy = f(x) + 2y^2$ ,  $\forall xy \in R$  and  $f(1) = 2$ ,  $f(2) = 8$ , where  $k$  is some constant, then  $f(x + y) \cdot f\left(\frac{1}{x + y}\right)$  is equal to (where  $x + y \neq 0$ )

A. 1

B. 4

C.  $f(1)$

D. none of these

**Answer: B**



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**161.** If  $f(x) = 1 + x^2$  and  $[g(x)] = 1 + x^2 - 2x^3 + x^4$ ,  $g(2) = 2$ , then

A.  $g(x)$  is one -one

B.  $g(2)=2$

C.  $g(x)=x$

D. none of these

**Answer: B**



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162.  $\pi$  is the FUNDAMENTAL period of

A.  $\frac{1 + \sin x}{\cos x(1 + \cos ex)}$

B.  $|\sin x| + |\cos x|$

C.  $\cos(\sin x) + \cos(\cos x)$

D. none of these

**Answer: A**



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163. If the range of the function  $y = \frac{x - 1}{a - x^2 + 1}$  does not contain any values belonging to the interval  $\left[-1, -\frac{1}{3}\right]$  then the integral value(s) of  $a$  can be

A. 5

B. 1

C. -5

D. none of these

**Answer: C**



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**164.** Let  $f: d \rightarrow R$  be defined by  $f(X) = \ln(\ln(\ln(\ln x)))$  then

A.  $f(X)$  is into

B.  $f(x)$  is many one

C.  $D = (e^e, \infty)$

D. none of these

**Answer: C**



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165.

Let

$f(x) = \max \{1 + \sin x, 1, 1 - \cos x\}$ ,  $x \in [0, 2\pi]$  and  $g(x) = \max \{1, |x|\}$ , then

A.  $g(f(0))=10$

B.  $f(g(0))=1+\sin 1$

C.  $f(g(1))=1$

D. none of these

**Answer: B**



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166. Let  $f(x) = \frac{e^{-x}}{1 + [x]}$ , then

A. Domain of definition of  $f(x)$  is  $\mathbb{R} - [-1, 0)$

B. Range of definition of  $f(x)$  is  $(-1/e, 1]$

C.  $f(x)$  is one-one in its domain

D. none of these

**Answer: A**



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167. The value(s) of a, for which  $\frac{x^3 - 6x^2 + 11x - 6}{x^3 + x^2 - 10x + 8} + \frac{a}{30} = 0$  does not have real solution is/are

A. -10

B. -12

C. 5

D. none of these

**Answer: C**



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168.  $f(x)$  is a real valued function, satisfying

$f(x + y) + f(x - y) = 2f(x)$ ,  $f(y) \neq 0$  or  $\forall y \neq 0$ , then

- A.  $f(x)$  is an even function
- B.  $f(x)$  is even if  $f(0) = 1$
- C.  $f(x)$  is odd if  $f(0) = 0$
- D.  $f(x)$  is even if  $f(0) = 0$

**Answer: B::C**



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169. If  $S$  is the set of all real numbers  $x$  for which  $\frac{2x - 1}{2x^3 + 3x^2 + x} > 0$ ,

and  $P$  is the subset of  $S$ , then  $P$  can be

- A.  $\left(\frac{3}{2}, 2\right)$
- B.  $\left(-\frac{1}{2}, 0\right)$
- C.  $\left(\frac{1}{2}, 3\right)$

D.  $(0, \infty)$

**Answer: A::B::C**



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170. If  $f'(x) = \frac{1 - 2 \sin^2 x}{f(x)}$ ,  $(f(x) \geq 0, \forall x \in R$  and  $f(0)=1)$  then  $f(x)$  is a periodic function with the period

A.  $\pi$

B.  $2\pi$

C.  $\frac{\pi}{2}$

D. none of these

**Answer:**



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171.

If

$$f(x) = \sin^2 x + \sin^2\left(x + \frac{\pi}{3}\right) + \cos x \cdot \cos\left(x + \frac{\pi}{3}\right) \text{ and } g\left(\frac{5}{4}\right) = 1,$$

then

A.  $f\left(\frac{\pi}{12}\right) = \frac{5}{4}$

B.  $g \circ f\left(\frac{\pi}{10}\right) = 1$

C.  $g \circ f$  is a constant functionD.  $f \circ g$  is a constant function

Answer: A::B::C::D



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172. Let  $f: \left[-\frac{\pi}{3}, 2\frac{\pi}{3}\right] \rightarrow [0, 4]$  be a function defined as

$f(x) = \sqrt{3} \sin x - \cos x + 2$ . Then  $f^{-1}(x)$  is given by

A.  $\sin^{-1}\left(x - \frac{2}{2}\right) - \frac{\pi}{6}$

B.  $\sin^{-1}\left(\frac{x - 2}{2}\right) + \frac{\pi}{6}$

C.  $2\frac{\pi}{3} - \cos^{-1}\left(\frac{x-2}{2}\right)$

D. none of these

**Answer: B::C**



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173. If  $f(x) = \frac{x}{x^2 + 1}$  and  $f(A) = \left\{y: -\frac{1}{2} \leq y < 0\right\}$ , then set A is

A.  $[-1, 0)$

B.  $(-\infty, -1]$

C.  $(-\infty, 0)$

D.  $(-\infty, \infty)$

**Answer: A::B::C**



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174. If  $f(x) = \cos([\pi^2 | x]) + \cos([- \pi^2 | x])$ , where  $[x]$  stands for the greatest integer function, then

A.  $f\left(\frac{\pi}{2}\right) = -1$

B.  $f(\pi) = 1$

C.  $f(-\pi) = 0$

D.  $f\left(\frac{\pi}{4}\right) = 1$

**Answer: A:C**



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175. Domain of  $f(x) = \sin^{-1}[2 - 4x^2]$  is ( $[.]$  denotes the greatest integer function)

A.  $\left[-\frac{\sqrt{3}}{2}, \frac{\sqrt{3}}{2}\right] \sim \{0\}$

B.  $\left[-\frac{\sqrt{3}}{2}, 0\right)$

C.  $\left[-\frac{\sqrt{3}}{2}, 0\right) \cup \left(0, \frac{\sqrt{3}}{2}\right]$

D.  $\left[-\frac{\sqrt{3}}{2}, 8\right]$

**Answer: A::C**

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176.  $f(x) = \cos^2 x + \cos^2\left(\frac{\pi}{3} + x\right) - \cos x \cos\left(\frac{\pi}{3} + x\right)$  is

A. an odd function

B. an even function

C. a periodic function

D.  $f(0)=f(1)$

**Answer: B::C::D**

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177. If  $[x]$  denotes the greatest integer less than or equal to  $x$ , the extreme values of the function

$$f(x) = [1 + \sin x] + [1 + \sin 2x] + [1 + \sin 3x] + \dots + [1 + \sin nx], n \in \mathbb{N}$$

are

A.  $n-1$

B.  $n$

C.  $n+1$

D.  $n+2$

**Answer: B::C**



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178. Let  $y=f(x)$  is a parabola whose vertex is at  $\left(\frac{3}{4}, -\frac{1}{4}\right)$ , the length of latus rectum is 1 and axis is parallel to positive direction of y-axis

$$\text{Let } g(x) = f(|x|), h(x) = |g(x)|$$

Answer the following questions are based on above passage:

If  $g(x)+a=0$  has exactly two roots, then  $a$  belongs to

A. 2

B. 3

C. 4

D. 6

**Answer: C**



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179. Let  $y=f(x)$  is a parabola whose vertex is at  $\left(\frac{3}{4}, -\frac{1}{4}\right)$ , the length of latus rectum is 1 and axis is parallel to positive direction of y-axis

Let  $g(x) = f(|x|)$ ,  $h(x)=|g(x)|$

Answer the following questions are based on above passage:

If  $g(x)+a=0$  has exactly two roots, then  $a$  belongs to

A. (0, 2)

B.  $(-\infty, -2)$

C.  $(2, \infty)$

D.  $(-1, 2)$

**Answer: B**



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**180.** Let  $y=f(x)$  is a parabola whose vertex is at  $\left(\frac{3}{4}, -\frac{1}{4}\right)$ , the length of latus rectum is 1 and axis is parallel to positive direction of y-axis

Let  $g(x) = f(|x|), h(x)=|g(x)|$

Answer the following questions are based on above passage:

The number of solution of  $h'(x)=0$  is

A. one

B. two

C. three

D. four

**Answer: B**



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**181.** Let  $x \in R$  be any real number such that lies between any two consecutive integers say  $n-1$  and  $n$ , i.e.,  $n - 1 < x \leq n$  then we can always find this unique integer  $n$ .

Let us call this  $n$  as super integral value of  $x$ .

We denote it symbolically as  $(x)$

For example: if  $x=2.63$ , then  $(x)=3$ , if  $x=-2.63$ , then  $(x)=-2$

Answer the following questions are based on above passage: The range of

the function  $y = \frac{(x)}{x}$  if  $x \in (-\infty, 0)$ , is

A.  $(-\infty, 0]$

B.  $[-1, 0]$

C.  $[0, 1]$

D.  $[-1, 1]$

Answer: C



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**182.** Let  $x \in R$  be any real number such that lies between any two consecutive integers say  $n-1$  and  $n$ , i.e.,  $n - 1 < x \leq n$  then we can always find this unique integer  $n$ .

Let us call this  $n$  as super integral value of  $x$ .

We denote it symbolically as  $(x)$

For example: if  $x=2.63$ , then  $(x)=3$ , if  $x=-2.63$ , then  $(x)=-2$

Answer the following questions are based on above passage: The range of

the function  $y = \frac{(x)}{x}$  if  $x \in (-\infty, 0)$ , is

A. 0

B. 1

C. 2

D. -1

**Answer: B**



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**183.** If  $f(x) = \cos[\pi^2]x + \cos[-\pi^2]x$  then the value of  $f\left(\frac{\pi}{4}\right) + f\left(\frac{\pi}{2}\right)$  is

A.  $\frac{1}{\sqrt{2}}$

B.  $1 + \frac{1}{\sqrt{2}}$

C.  $1 - \frac{1}{\sqrt{2}}$

D.  $-1 + \frac{1}{\sqrt{2}}$

**Answer: D**



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184. Match List - I with List-II

List - I

List - II

- |   |                           |
|---|---------------------------|
| (1) Circular plate is expanded by heat from radius 5 cm to 5.06 cm. Approximate increase in area is   | (P) 4                     |
| (2) If an edge of a cube increases by 1%, then percentage increase in volume is   | (Q) $0.6\pi$              |
| (3) If the rate of decrease of $\frac{x^2}{2} - 2x + 5$ is twice the rate of decrease of $x$ , then $x$ is equal to (rate of decreases is non-zero) | (R) 3                     |
| (4) Rate of increase in area of equilateral triangle of side 15 cm, when each side is increasing at the rate of 0.1 cm/s, is                        | (S) $\frac{3\sqrt{3}}{4}$ |



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185. Match List - I with List-II

<u>List - I</u>	<u>List - II</u>
(1) Circular plate is expanded by heat from radius 5 cm to 5.06 cm. Approximate increase in area is	(P) 4
(2) If an edge of a cube increases by 1%, then percentage increase in volume is	(Q) $0.6\pi$
(3) If the rate of decrease of $\frac{x^2}{2} - 2x + 5$ is twice the rate of decrease of $x$ , then $x$ is equal to (rate of decreases is non-zero)	(R) 3
(4) Rate of increase in area of equilateral triangle of side 15 cm, when each side is increasing at the rate of 0.1 cm/s, is	(S) $\frac{3\sqrt{3}}{4}$



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186. The number of solutions of  $2\{x\} - 1 = nx$  where  $n \in (2, \infty)$  and  $\{ \}$  represents fraction part of  $x$  is

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**187.** Let  $f(x)$  and  $g(x)$  be one-one onto functions where  $f: \{a, b, c, d\} \rightarrow \{1, 2, 3, 4\}$  and  $g: \{3, 4, 5, 6\} \rightarrow \{w, x, y, z\}$  respectively. The number of elements in the range set of  $g(f(x))$  are

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**188.** A polynomial  $f(x)$  satisfies the condition  $f(x) \cdot f\left(\frac{1}{x}\right) = f(x) + f\left(\frac{1}{x}\right)$  and  $f(10) = 1001$ , then the value of  $f(2)$  = ?

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**189.** The number of solutions of  $\sin\left(\frac{x}{2}\right) + 2\pi x = x^2 + \pi^2 + 1$  must be

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**190.** Let  $f$  be a function from the set of positive integers to the set of real number i.e  $f: N \rightarrow R$ , such that  $f(1) = 1$  and  $r=1$  to  $n \sum$   
 $rf(r)=n(n+1)f(n), \forall n \geq 2'$

then the value of  $2126f(1063)$

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**191.** Let  $f$  be a function from the set of positive integers to the set of real number i.e  $f: N \rightarrow R$ , such that  
 $f(1) + 2f\{2\} + 3f\{3\} + \dots + nf\{n\} = n(n + 1)f(n)$  for  $n \geq 2$

Then the of  $\frac{1}{f(4)}$  must be

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**192.** A function  $f: R \rightarrow R$  is defined as  $f(x) = \frac{\alpha x^2 + 6x - 8}{\alpha + 6x - 8x^2}$ . Find the set of values of  $\alpha$  for which is onto.

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**193.** Find the domain of the following function :

$$f(x) = \sqrt{\sin^{-1}(\log_2 x)} + \sqrt{\cos(\sin x)} + \sin^{1 - \left(\frac{1 + x^2}{2x}\right)}$$

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**194.** Range of  $f(x) = \frac{\sin^2 x + \sin x - 1}{\sin^2 x - \sin x + 2}$

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**195.** If  $p$  and  $q$  are positive integers,  $f$  is a function defined for positive number and attain only positive value such that  $f(xf(y)) = x^p y^q$ , prove that  $q = p^2$

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196. Check whether the function defined

$f(x + \lambda) = 1 + \sqrt{2f(x) - f^2(x)} \forall x \in R$  is a periodic or not.

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197. Let  $f(x, y)$  be a periodic function satisfying the condition  $f(x, y) = f(2x + 2y), (2y - 2x) \forall x, y \in R$ . Now define a function  $g$  by  $g(x) = f(2^x, 0)$ . Then prove that  $g(x)$  is periodic function, find its period.

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198. If  $f(x) = 2x + |x|, g(x) = \frac{1}{3}(2x - |x|)$  and  $h(x) = f(g(x))$ , then find the domain of  $\frac{\sin^{-1}(h(h(h(h\dots h(x)\dots))))}{n\text{times}}$

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199. Find the domain and range of  $h(x) = g(f(x))$ , where

$$f(x) = \begin{cases} [x] & -2 \leq x \leq -1 \\ |x| + 1 & -1 < x \leq 2 \end{cases} \text{ and } g(x) = \begin{cases} [x] & -\pi \leq x \leq 0 \\ \sin x & 0 < x \leq \pi \end{cases}$$

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200. Determine all functions  $f: \mathbb{R} \rightarrow \mathbb{R}$  satisfying

$$f(x - f(y)) = f(f(y)) + xf(y) + f(x) - 1 \forall x, y \in \mathbb{R}$$

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201. Let  $\mathbb{R} \rightarrow f(x) = x^3 + ax^2 + bx + c \sin x$ ,  $a, b, c \in \mathbb{R}$  Find the condition that should be imposed on  $a, b, c$  so that the given function becomes invertible?

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202. If  $f(x)$  satisfies the relation  $f(x + y) = f(x) + f(y) \forall x, y \in R$  and  $f(1) = 5$ , Find  $\sum_{x=1}^m f(x)$  Also prove that  $f(x)$  is an odd function.



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203. In the function  $f(x)$  is defined for  $x \in [0, 1]$  then the function  $f(2x+3)$  is defined for

A.  $(-\infty, \infty)$

B.  $[-3/2, -1]$

C.  $[-2/3, 1]$

D.  $x > 0$

Answer: B



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204. The domain of the function  $f(x) = \frac{\sin^{-1}(x - 3)}{\sqrt{9 - x^2}}$  is

A. [1,2]

B. [2,3)

C. [2,3]

D. (1,2)

**Answer: B**



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205. The domain of the real valued function  $f(x) = 3e^{\sqrt{x^2-1}} \log(x - 1)$  is

A.  $\mathbb{R} - \{1\}$

B.  $\mathbb{R} - [-1,1]$

C.  $[1, \infty)$

D.  $(1, \infty)$

**Answer: D**



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**206.** Domain of the function

$$f(x) = \sin^{-1}\left(\frac{2 - |x|}{4}\right) + \cos^{-1}\left(\frac{2 - |x|}{4}\right) + \tan^{-1}\left(\frac{2 - |x|}{4}\right) \text{ is}$$

A.  $\mathbb{R} - \{1\}$

B.  $[0, 6]$

C.  $[-6, 6]$

D.  $[-3, 3]$

**Answer: C**



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207. The domain of the function

$$f(x) = \sin^{-1} \frac{1}{|x^2 - 1|} + \frac{1}{\sqrt{\sin^2 x + \sin x + 1}} \text{ is :}$$

- A.  $(-\infty, \infty)$
- B.  $(-\infty, -\sqrt{2}] \cup [\sqrt{2}, -\infty)$
- C.  $(-\infty, -\sqrt{2}] \cup [\sqrt{2}, \infty) \cup \{0\}$
- D. None of these

Answer: C



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208. The range of function  $f(x) = \sqrt{x^2 + 4x} C_{2x^2+3}$

- A.  $\{1, 2\sqrt{3}\}$
- B.  $\{1, 2\sqrt{3}, 3\sqrt{5}\}$
- C.  $\{1, 2, 3\}$

D. {1, 2}

**Answer: A**



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**209.** Let  $n$  be a natural number. Then the range of the function

$$f(n) = {}^{8-n}P_{n-4}, 4 \leq n \leq 6, \text{ is}$$

A. {1, 2, 3, 4}

B. {1, 2, 3, 4, 5, 6}

C. {1, 2, 3}

D. {1, 2, 3, 4, 5}

**Answer: C**



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210. If  $x^2 + y^2 + z^2 = 1$ , then  $xy + yz + zx$  lies in

- A.  $[-1/2, 1]$
- B.  $[1/2, 1]$
- C.  $[-1/2, -1]$
- D.  $[1/2, -1]$

**Answer: A**



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211. The range of the function

$$f(x) = \sin^{-1} \left[ x^2 + \frac{1}{2} \right] + \cos^{-1} \left[ x^2 - \frac{1}{2} \right],$$

where  $[.]$  is the greatest integer function, is

- A.  $\left\{ \frac{\pi}{2}, \pi \right\}$
- B.  $\left\{ 0, \frac{\pi}{2} \right\}$
- C.  $\{ \pi \}$

D.  $\left(0, \frac{\pi}{2}\right)$

**Answer: C**



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**212.** The range of the function  $f(x) = \sqrt{3x^2 - 4x + 5}$  is

A.  $\left[-\infty, \sqrt{\frac{11}{3}}\right]$

B.  $\left(-\infty, \sqrt{\frac{11}{3}}\right)$

C.  $\left[\sqrt{\frac{11}{3}}, \infty\right)$

D.  $\left(\sqrt{\frac{11}{3}}, \infty\right)$

**Answer: C**



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213. If the graph of the function  $f(x) = \frac{a^x - 1}{x^n(a^x + 1)}$  is symmetric about y-axis, then n equals

A. 2

B. 1/2

C. 1/4

D. -1/3

**Answer: D**



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214. If the graph of the function  $f(x)$  is symmetrical about  $x = 20$  then

A.  $f(x+20)=f(20-x)$

B.  $f(x)=f(-x)$

C.  $f(x+20)=f(x-20)$

D. None of these

**Answer: A**



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**215.** If  $f$  is even function defined on the interval  $(-5, 5)$ , then real values of  $x$  satisfying the equation  $f(x) = f\left(\frac{x+1}{x+2}\right)$  are

A.  $\left(\frac{3-\sqrt{5}}{2}, \frac{3+\sqrt{5}}{2}\right)$

B.  $\left(\frac{-5-\sqrt{3}}{2}, \frac{-3+\sqrt{5}}{2}\right)$ ,

C.  $\left(\frac{-3-\sqrt{5}}{2}, \frac{5+\sqrt{3}}{2}\right)$

D.  $3-\sqrt{5}, 3+\sqrt{5}$

**Answer: A**



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216. Which of the following function is even function

A.  $f(x) = \frac{a^x + 1}{a^x - 1}$

B.  $f(x) = x \left( \frac{a^x - 1}{a^x + 1} \right)$

C.  $f(x) = \frac{a^x - a^{-x}}{a^x + a^{-x}}$

D.  $f(x) = \sin x$

Answer: B



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217. If  $f(x)$  and  $g(x)$  be two given function with all real numbers as their

domain, then  $h(x) = \{f(x) + f(-x)\}\{g(x) - g(-x)\}$  is

A. an even function

B. an odd function

C. even as well as odd function

D. None of these

**Answer: B**



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**218.** Period of  $f(x)=[x]+[x+1/3]+[x+2/3]-3x+10$ , where  $[.]$  denotes the greatest integer function.

A. 1

B. 0.6666666666666667

C. 0.3333333333333333

D. 0.5

**Answer: C**



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**219.** The function  $f(x) = \frac{1}{2} \left\{ \frac{|\sin x|}{\cos x} + \frac{\sin x}{|\cos x|} \right\}$  is periodic with period

A.  $\pi$

B.  $\frac{\pi}{2}$

C.  $2\pi$

D.  $3\pi$

**Answer: C**



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**220.** The value of  $n \in \mathbb{N}$ , for which the function  $f(x) = \frac{\sin nx}{\sin \frac{x}{n}}$  has  $4\pi$  as

its period is equal to

A. 2

B. 3

C. 5

D. 4

**Answer: A**



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221. If  $f(x)$  is an odd periodic function with period 2, then  $f(4)$  equals

A. 0

B. 2

C. 4

D. -4

Answer: A



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222. Period of  $f(x) = \cos 2\pi\{x\}$  is , where  $\{x\}$  denote the fractional part of  $x$ )

A. 1

B.  $\frac{\pi}{2}$

C. 0.5

D.  $\pi$

**Answer:**



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223. The period of  $\sin\left(\frac{\pi\{x\}}{12}\right) + \cos\left(\frac{\pi x}{8}\right) + \tan\left(\frac{\pi\{x\}}{3}\right)$

A. 12

B. 4

C. 3

D. 144

**Answer: D**



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224. Let  $f : (4, 6) \rightarrow (6, 8)$  be a function defined by  $f(x) = x + \left[ \frac{x}{2} \right]$  (where  $[\cdot]$  denotes the greatest integer function).

$f^{-1}(x)$  is equal to

A.  $x - [x/2]$

B.  $-x - 2$

C.  $x - 2$

D.  $\frac{1}{x + \left[ \frac{\pi}{2} \right]}$

**Answer: C**

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225. The value of  $b$  and  $c$  for which the identity  $f(x+1) - f(x) = 8x + 3$  is satisfied, where  $f(x) = bx^2 + cx + d$ , are

A. 4, 1

B. 4, -1

C. -1, 4

D. None of these

**Answer: B**



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**226.** If  $f(x) = \sin \sqrt{[a]x}$ , (where  $[.]$  denotes the greatest integer function), has  $\pi$  as its fundamental period, then

A.  $a = 1$

B.  $a \in [1, 2)$

C.  $a \in [2, 3)$

D.  $a \in [4, 9)$

**Answer: D**



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227. If  $f: \mathbb{R} \rightarrow [-1, 1]$ , where  $f(x) = \sin\left(\frac{\pi}{2}[x]\right)$  (where  $[.]$  denotes the greatest integer function), then the range of  $f(x)$  is

- A.  $[-1, 1]$
- B.  $\{-1, 1\}$
- C.  $\{-1, 0, 1\}$
- D. None of these

**Answer: C**



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228. If  $[x]^2 - 5[x] + 6 = 0$  (where  $[.]$  denotes the greatest integer function), then  $x$  belongs to

- A.  $[2, 4)$
- B.  $[2, 4) - \{3\}$
- C.  $\{3\}$



D. {2}

**Answer: A**



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229. Let  $f: (-\infty, 1] \rightarrow (-\infty, 1]$  such that  $f(x)=x(2-x)$ . Then  $f^{-1}(x)$

A.  $1 + \sqrt{1 - x}$

B.  $1 - \sqrt{1 - x}$

C.  $\sqrt{1 - x}$

D. None of these

**Answer: B**



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**230.** Let  $f: R \rightarrow R$  be a function such that  $f(x) = x^3 + x^2 + 3x + \sin x$ . Then

- A.  $f$  is one-one and into
- B.  $f$  is one-one and onto
- C.  $f$  is many-one and into
- D.  $f$  is many-one and onto

**Answer: B**



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**231.** Let  $f: \left[ -\frac{\pi}{3}, \frac{2\pi}{3} \right] \rightarrow [0, 4]$  be a function defined as  $f(x) = \sqrt{3} \sin x - \cos x + 2$ . Then  $f^{-1}(x)$  is given by

- A.  $\sin^{-1} \left( \frac{x-2}{2} \right) - \frac{\pi}{6}$
- B.  $\sin^{-1} \left( \frac{x-2}{2} \right) + \frac{\pi}{6}$
- C.  $\frac{2\pi}{3} + \cos^{-1} \left( \frac{x-2}{2} \right)$

D. None of these

**Answer: B**



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**232.** Let  $f(x) = (ax+b) \cos x + (cx+d) \sin x$  and  $f'(x) = x \cos x$  be an identity in  $x$  then

A.  $a = 5, b = 2$

B.  $a = 5, b = 1$

C.  $a = 5, b = -5$

D.  $b = 1, c = 1$

**Answer: D**



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233. If  $f(x) = \cos|x| + \left[ \left| \frac{\sin x}{2} \right| \right]$  (where  $[.]$  denotes the greatest integer function), then  $f(x)$  is

- A. even
- B. odd
- C. odd as well as even
- D. None of these

**Answer: A**



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234. The number of points  $(x, y)$ , where the curves  $|y| = \ln|x|$  and  $(x - 1)^2 + y^2 - 4 = 0$  cut each other, is

- A. 2
- B. 3
- C. 1

D. 6

**Answer: B**

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235. Let  $f(x) = \left[ \frac{1}{2} + \frac{n}{100} \right]$ , where  $[.]$  denotes the greatest integer function, then the value of  $\sum_{n=1}^{151} f(n)$  is

A. 101

B. 102

C. 100

D. 103

**Answer: B**

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236. If  $y = \sqrt{e^{\sin^{-1}(\log_2 x^2)}}$ , then  $y$  is real if

A.  $x \in R - \{0\}$

B.  $x \in [-\sqrt{2}, \sqrt{2}]$

C.  $x \in \left(-\infty, -\frac{1}{\sqrt{2}}\right] \cup \left[\frac{1}{\sqrt{2}}, \infty\right)$

D.  $x \in \left[-\sqrt{2}, -\frac{1}{\sqrt{2}}\right] \cup \left[\frac{1}{\sqrt{2}}, \sqrt{2}\right]$

**Answer: D**



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237. If  $[2 \sin x] + [\cos x] = -3$  then the range of the function  $f(x) = \sin x + \sqrt{3} \cos x$  in  $[0, 2\pi]$  is, (where  $[.]$  denotes the greatest integer function)

A.  $(0, 2\pi)$

B.  $(-2, -1)$

C.  $(-1, -1/2)$

D. None of these

**Answer: B**



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238. If  $F(x + 1) = \frac{2F(x) + 1}{2}$ ,  $n = 1, 2, 3, \dots$  and  $F(1) = 2$  then  $F(101)$

A. 52

B. 49

C. 48

D. 51

**Answer: A**



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239. If  $f: R \rightarrow R$  satisfies  $f(x + y) = f(x) + f(y)$  for all  $x, y \in R$  and

$f(1)=7$ , then  $\sum_{r=1}^n f(r)$

A.  $\frac{7n(n + 1)}{2}$

B.  $\frac{7n}{2}$

C.  $\frac{7(n + 1)}{2}$

D.  $7n(n + 1)$

**Answer: A**



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240. If  $f(x+y, x-y)=xy$  then the arithmetic mean of  $f(y, x)$  &  $f(x, y)$

A. 0

B. x

C. y



D.  $\frac{x + y}{2}$

**Answer: A**



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241.  $f(x) = \sqrt{[\sin 2x] - [\cos 2x]}$  :[.]GIF, then range of  $f(x)$

A.  $\{0\}$

B.  $\{1\}$

C.  $\{0, 1\}$

D.  $\{0, 1, \sqrt{2}\}$

**Answer: A**



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242. If  $f(x) = \{(x^2, \text{"for"}, x \geq 0), (x, \text{"for"}, x < 0)\}$  then  $f \circ f(x)$  is given by

A.  $x^2$  for  $x \geq 0$ ,  $x$  for  $x < 0$

B.  $x^4$  for  $x \geq 0$ ,  $x^2$  for  $x < 0$

C.  $x^4$  for  $x \geq 0$ , for  $x < 0$

D.  $x^4$  for  $x \geq 0$ ,  $x$  for  $x < 0$

**Answer: D**



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**243.** Domain of  $f(x)$  is  $[-1, 2]$  then domain of  $f([\![x] - x^2 + 4)$  where  $[.]$

denotes the greatest integer function, is

A.  $[-1, \sqrt{7}]$

B.  $[-\sqrt{3}, -1] \cup [\sqrt{3}, \sqrt{7}]$

C.  $(-1, \sqrt{7}]$

D.  $[-\sqrt{3}, -1) \cup [\sqrt{3}, \sqrt{7})$

**Answer: B**

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**244.** Number of solution of the equation  $x^2 - 2 - 2[x] = 0$  ( $[.]$  denotes the greatest integer function) is

- A. one
- B. two
- C. zero
- D. infinity

**Answer: A**

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**245.** Let  $S_n = \sum_{t=1}^n t!(n > 6)$ , then  $S_n - 7 \left[ \frac{S_n}{7} \right]$  (where  $[.]$  denotes the greatest integer function) is equal to

- A.  $\left[ \frac{n}{7} \right]$

B.  $n! - 7 \left[ \frac{n!}{7} \right]$

C. 5

D. 3

**Answer: C**



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**246.** Range of

$$f(x) = [1 + \sin x] + \left[ 2 + \sin \frac{x}{2} \right] + \left[ 3 + \sin \frac{x}{3} \right] + \dots + \left[ n + \sin \frac{x}{n} \right]$$

AA  $x$  in  $[0, \pi]$  (where  $[.]$  denotes the greatest integer function).

A.  $\left\{ \frac{n^2 + n - 2}{2}, \frac{n(n + 1)}{2} \right\}$

B.  $\left\{ \frac{n(n + 1)}{2} \right\}$

C.  $\left\{ \frac{n^2 + n - 2}{2}, \frac{n(n + 1)}{2}, \frac{n^2 + n + 2}{2} \right\}$

D.  $\left\{ \frac{n(n + 1)}{2}, \frac{n^2 + n + 2}{2} \right\}$

**Answer: D**

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247. The number of solutions of  $\log_{\sin x} 2^{\tan x} > 0$  in the interval  $\left(0, \frac{\pi}{2}\right)$

is

A. 0

B. 1

C. 2

D. 3

**Answer: A**

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248. If  $f(x) = \ln\left(\frac{x^2 + e}{x^2 + 1}\right)$ , then range of  $f(x)$  is

A.  $(0, 1)$

B.  $[0, 1]$

C.  $[0, 1)$

D.  $(0, 1]$

**Answer: D**



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**249.** If  $f(x) = \{x\} + \sin ax$  (where  $\{.\}$  denotes the fractional part function) is periodic then

A. 'a' is a rational multiple of  $\pi$

B. 'a' is a natural number

C. 'a' is any real number

D. 'a' is any positive real number

**Answer: A**



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250. The value of  $a$  for which the range of the function

$$f(x) = \frac{x - 1}{1 - x^2 - a} \text{ does not contain the interval } [-1, 1]$$

A. 1

B. 0

C. -1

D. None of these

**Answer: D**



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251. If the graph of the function  $f(x)$  is symmetrical about two lines  $x = a$  and  $x = b$  then  $f(x)$  must be period

A.  $\frac{b - a}{2}$

B.  $b - a$

C.  $2(b - a)$

D. None of these

**Answer: C**

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252. If  $f(x) = 27x^3 + \frac{1}{x^3}$  and  $\alpha, \beta$  are the roots of  $3x + \frac{1}{x} = 2$  then

A.  $f(\alpha) = f(\beta)$

B.  $f(\alpha) = 10$

C.  $f(\beta) = 12$

D. None of these

**Answer: A**

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253. If  $A = \left\{ x : \frac{\pi}{6} \leq x \leq \frac{\pi}{3} \right\}$  and  $f(x) = \cos x - x(1 + x)$  then  $f(A)$  is equal to-

A.  $[\pi/6, \pi/3]$

B.  $\left[ -\frac{\pi}{3}, -\frac{\pi}{6} \right]$

C.  $\left[ \frac{1}{2} - \frac{\pi}{3} \left( 1 + \frac{\pi}{3} \right), \frac{\sqrt{3}}{2} - \frac{\pi}{6} \left( 1 + \frac{\pi}{6} \right) \right]$

D.  $\left[ \frac{1}{2} + \frac{\pi}{3} \left( 1 - \frac{\pi}{3} \right), \frac{\sqrt{3}}{2} + \frac{\pi}{6} \left( 1 - \frac{\pi}{6} \right) \right]$

**Answer: C**



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254. Find the domain of the function

$$f(x) = \frac{\cos^{-1}(1 + x^2)}{2x} + \sqrt{\sin(\cos x)}$$

A.  $[-1, 1]$

B.  $\phi$

C.  $\{-1, 1\}$

D.  $(-1, 1)$

**Answer: C**



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**255.** Consider the following relations  $R = \{(x,y) \mid x, y \text{ are real number and } x = wy \text{ for some rational number } w\}$ ,  $S = \left\{ \frac{m}{n} \quad \frac{p}{q} \right\}$   $m, n, p$  and  $q$  are integers such that  $n, q \neq 0$  and  $qm = pn$ . Then

- A. R is an equivalence relation but S is not an equivalence relation
- B. Neither R nor S is an equivalence relation
- C. S is an equivalence relation but R is not an equivalence relation
- D. R and S both are equivalence relations.

**Answer: C**



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**256.** Let  $W$  denotes the words in the English dictionary Define the relation  $R$  by  $R = \{(x, y) \in W \times W : \text{the words } x \text{ and } y \text{ have a least one letter in common}\}$  Then,  $R$  is

- A. reflexive, symmetric and not transitive
- B. reflexive, symmetric and transitive
- C. reflexive, not symmetric and transitive
- D. not reflexive, symmetric and transitive

**Answer: A**



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**257.** If  $f(x) = \sin x + \cos x$ ,  $g(x) = x^2 - 1$  then  $g(f(x))$  is invertible in the domain

- A.  $0, \frac{\pi}{2} \Big]$

B.  $\left[-\frac{\pi}{4}, \frac{\pi}{4}\right]$

C.  $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$

D.  $[0, \pi]$

**Answer: B**



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258. The domain of the function  $f(x) = \frac{1}{|x| - x}$

A.  $\mathbb{R}$

B. cannot contain a positive real

C.  $(-\infty, 0)$

D.  $(0, \infty)$

**Answer: B::C**



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259. If a function satisfies  $(x-y) f(x+y) - (x+y) f(x-y) = 2(x^2y - y^3)$ ,  $\forall x, y \in R$

and  $f(1) = 2$ , then

- A.  $f(x)$  must be polynomial function
- B.  $f(3) = 12$
- C.  $f(0) = 0$
- D.  $f(x)$  may not be differentiable

**Answer: A::B::C**



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260. If  $f(x) = ax + b$  and  $g(x) = cx + d$ , then  $f(g(x)) = g(f(x))$  implies

- A.  $f(a) = g(c)$
- B.  $f(b) = g(b)$
- C.  $f(d) = g(b)$
- D.  $ad + b = bc + d$

Answer: C::D

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261. Which of the following functions is not injective ?

A.  $f(x) = |x + 1|, x \text{ in } [-1, 0)$

B.  $f(x) = x + \frac{1}{x}, x \in [0, \infty)$

C.  $f(x) = x^2 + 4x - 5$

D.  $f(x) = e^{-x}, x \in [0, \infty)$

Answer: B::C

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262. If  $f(x)$  is defined on  $[0, 1)$  by  $f(x) = \begin{cases} x & \text{if } x \text{ is rational} \\ 1 - x & \text{if } x \text{ is irrational} \end{cases}$

then for all  $x$  in  $[0, 1]$ ,  $f(f(x))$  is

A. real

B.  $1 + x$

C.  $x$

D. None of these

**Answer: A::C**



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**263.** The function  $f(x) = [x] + \sin x$  ( $[x]$  denotes greatest integer  $\leq x$ )

A. can not take all real value

B. cannot take all the value 1

C. can take all real value

D. is defined for all  $x$

**Answer: A::B::D**



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264. Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  be defined by  $f(x) = [x]$  and  $g(x) = \frac{3 - 2x}{4}$  then

- A.  $f$  is neither one-one nor onto
- B.  $g$  is one-one but  $f$  is not one-one
- C.  $f$  is one-one and  $g$  is onto
- D. neither  $f$  nor  $g$  is onto

**Answer: A::B**



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265. If  $f(x) = \frac{1}{\sqrt{[\cos x] - [\sin x]}}$  ( $[x]$  denotes greatest integer  $\leq x$ )

then

- A. Domain of  $f = \mathbb{R}$
- B. Range of  $f = \{1\}$
- C. Domain of  $f = [2n\pi, (2n + 1)\pi]$



D. Domain of  $f = \left[ 2n\pi - \frac{\pi}{2}, 2n\pi \right]$

**Answer: B::D**



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**266.** The graph of the equation  $y + |y| - x - |x| = 0$  is represented by

- A. the x-axis
- B. the bisector line of the first quadrant
- C. a pair of lines bisecting all the quadrants
- D. all point of the third quadrant

**Answer: B::D**



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267. If  $f: R \rightarrow R$ , defined as  $f(x) = \frac{\sin([x]\pi)}{x^2 + xz + 1}$ , where  $[x]$  is the greatest integer less than or equal to  $x$ , then

A.  $f$  is one-one

B.  $f$  is many-one

C.  $f$  is into

D.  $f$  is onto

**Answer: B::C**



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268. Let  $g(x)$  be a function defined on  $[-1, 1]$  so that the area of the equilateral triangle with two of its vertices at  $(0, 0)$  and  $(x, g(x))$  is  $\frac{\sqrt{3}}{4}$ .

The function  $g(x)$  is equal to

A.  $\sqrt{1 - x^2}$

B.  $-\sqrt{1 - x^2}$

$$C. \frac{1}{2} \sqrt{1-x^2}$$

$$D. \frac{\sqrt{3}}{8} \sqrt{1-x^2}$$

**Answer: A::B**



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**269.** Let  $f(x) = \frac{x}{1+x^2}$  and  $g(x) = \frac{e^{-x}}{1+[x]}$ , where  $[x]$  is the greatest integer less than or equal to  $x$ . Then

A.  $\text{dom}(f+g) = \mathbb{R} \setminus [2, 0)$

B.  $\text{dom}(f \sim g) = \mathbb{R} \setminus [-1, 0)$

C.  $\text{range } f \cap \text{range } g = [-2, 1/2]$

D.  $\text{range of } f \cap \text{range } g = \mathbb{R}$

**Answer: B::D**



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270. Let  $f(x) = \frac{\log_{100} X (2 \log_{10} X + 2)}{-X}$  and  $g(X) = \{X\}$ , where  $\{x\}$  denotes the fractional part of  $x$ . If the function  $f \circ g(x)$  exists then the domain of  $f(x)$  contains

A.  $(0, 1/100)$

B.  $(1/100, 1/10)$

C.  $(1/10, 1)$

D.  $(1, \infty)$

**Answer: A:B**



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271. If  $y = f(x) = \frac{x+2}{x-1}$  then

A.  $x = f(y)$

B.  $f(1) = 3$

C.  $y$  increases with  $x$  for  $x < 1$

D.  $f$  is a rational function of  $x$

Answer: A::D



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**272.** Let  $f(x)$  be a real valued function satisfying the functional equation  $f(x) + f(1 - x) = k$  for all  $x \in Q$ , where  $k$  is a constant quantity. To evaluate the p and value at a point we use the relations to get the value of that function

Answer the following question based on above passage :

If  $f(x) = \frac{4^x}{4^x + 2}$  where  $x \in Q$  then

$f(1/2007) + f(2/2007) + \dots + f(2006/2007)$  equals to

A. 1003

B. 2006

C. 2007

D. None of these

**Answer: A**



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**273.** Let  $f(x)$  be a real valued function satisfying the functional equation  $f(x) + f(1 - x) = k$  for all  $x \in \mathbb{Q}$ , where  $k$  is a constant quantity. To evaluate the p and value at a point we use the relations to get the value of that function

Answer the following question based on above passage :

If  $f(x) = \frac{3^{x-3}}{3^{1-x} + 3^x}$  or  $ax$  in  $\mathbb{Q}$ , then the value of the sum  $f(1/55) + f(2/55) + \dots + f(54/55)$  is

- A. 1
- B. 27
- C. 54
- D. 55

**Answer: A**



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**274.** Let  $f(x)$  be a real valued function satisfying the functional equation  $f(x) + f(1 - x) = k$  for all  $x \in \mathbb{Q}$ , where  $k$  is a constant quantity. To evaluate the p and value at a point we use the relations to get the value of that function

Answer the following question based on above passage :

If  $f(x) = \frac{a^x}{a^x + \sqrt{a}}$  ( $a > 0$ ), then  $\sum_{r=1}^{2n-1} 2f\left(\frac{r}{2n}\right)$  is equal to

A. 1

B.  $2n$

C.  $2n - 1$

D.  $\frac{(2n - 1)a}{2}$

**Answer: C**

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275. Let  $(x) f_1(x) - 2f_2(x)$

where  $f_1(x) = \min\{x^2, |x|\}$  for  $-1 \leq x \leq 1$

$\max\{x^2, |x|\}$  for  $|x| > 1$

$f_2(x) = \max\{x^2, |x|\}$  for  $-1 \leq x \leq 1$

$\min\{x^2, |x|\}$  for  $|x| > 1$

$g(x) = \begin{cases} \min\{f(t) : -3 \leq t \leq x, -3 \leq x \leq 0\} \\ \max\{f(t) : 0 \leq t \leq x, 0 \leq x \leq 3\} \end{cases}$  Answer the follow  $\in g(x)$

$-3 \leq x \leq -1$ , range of  $g(x)$  is

A.  $[-1, 3]$

B.  $[-1 + 15]$

C.  $[-1, 9]$

D. None of these

**Answer: A**



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276. Let  $f(x) = f_1(x) - 2f_2(x)$

where  $f_1(x) = \min\{x^2, |x|\}$  for  $-1 \leq x \leq 1$

$\max\{x^2, |x|\}$  for  $|x| > 1$

$f_2(x) = \max\{x^2, |x|\}$  for  $-1 \leq x \leq 1$

$\min\{x^2, |x|\}$  for  $|x| > 1$

$g(x) = \{( \min\{f(t) : -3 \leq t \leq x, -3 \leq x \leq 0 \}), ( \max\{f(t) : 0 \leq t \leq x, 0 \leq x \leq 3 \} )\}$

Answer the following question based on above passage :

Number of critical points of  $f(x)$  is

A. 1

B. 2

C. 3

D. None of these

**Answer: C**



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277. Let  $(x) f_1(x) - 2f_2(x)$

where  $f_1(x) = \min\{x^2, |x|\}$  for  $-1 \leq x \leq 1$

$\max\{x^2, |x|\}$  for  $|x| > 1$

$f_2(x) = \max\{x^2, |x|\}$  for  $-1 \leq x \leq 1$

$\min\{x^2, |x|\}$  for  $|x| > 1$

$g(x) = \begin{cases} \min\{f(t) : -3 \leq t \leq x, -3 \leq x \leq 0\} \\ \max\{f(t) : 0 \leq t \leq x, 0 \leq x \leq 3\} \end{cases}$  Answer the follow  $\in g(x)$

x in  $(-1, 0)$ ,  $f(x) - g(x)$  is

A.  $x^2 - 2x + 1$

B.  $x^2 + 2x - 1$

C.  $x^2 + 2x + 1$

D.  $x^2 - 2x - 1$

**Answer: C**



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278. Let  $f(x) = \frac{1}{2} \left[ f(xy) + f\left(\frac{x}{y}\right) \right]$  for  $x, y \in R^+$  such that  $f(1) = 0$

$$f'(1) = 2$$

Answer the following question based on above passage :

$f(x) - f(y)$  is equal to

A.  $f\left(\frac{y}{x}\right)$

B.  $f\left(\frac{x}{y}\right)$

C.  $f(2x)$

D.  $f(2y)$

**Answer: B**

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279. Let  $f(x) = \frac{1}{2} \left[ f(xy) + f\left(\frac{x}{y}\right) \right]$  for  $x, y \in R^+$  such that  $f(1) = 0$

$$f'(1) = 2$$

Answer the following question based on above passage :

$f'(3)$  is equal to

A.  $1/3$

B.  $2/3$

C.  $1/2$

D.  $1/4$

**Answer: B**



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**280.** Let  $f(x) = \frac{1}{2} \left[ f(xy) + f\left(\frac{x}{y}\right) \right]$  for  $x, y \in \mathbb{R}^+$  such that  $f(1) = 0$

$f'(1) = 2$

Answer the following question based on above passage :

$f''$  is equal to

A. 2

B. 1

C. 3

D. 4

**Answer: A**



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**281.** For all real values of  $x$  and  $y$ ,  $2f(x) \cos y = f(x + y) + f(x - y)$  and  $b$  are arbitrary constants.

Answer the following question based on above passage :

$$f(x) + f(\pi - x) =$$

A.  $2b \sin x$

B.  $-2b \sin x$

C.  $2b \cos x$

D.  $-2b \cos x$

**Answer: C**



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**282.** For all real values of  $x$  and  $y$ ,  $2f(x) \cos y = f(x + y) + f(x - y)$  and  $b$  are arbitrary constants.

Answer the following question based on above passage :

$$f(-x) + f(\pi - x) =$$

- A.  $2b \sin x$
- B.  $-2b \sin x$
- C.  $2b \cos x$
- D. None of these

**Answer: D**



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**283.** For all real values of  $x$  and  $y$ ,  $2f(x) \cos y = f(x + y) + f(x - y)$  and  $b$  are arbitrary constants.

Answer the following question based on above passage :

$$f(x) + f(-x) =$$

A. 0

B.  $2b \cos x$

C.  $2b \sin x$

D. None of these

**Answer: C**



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284. Match List - I with List-II

List - I

List - II

- |   |                           |
|---|---------------------------|
| (1) Circular plate is expanded by heat from radius 5 cm to 5.06 cm. Approximate increase in area is   | (P) 4                     |
| (2) If an edge of a cube increases by 1%, then percentage increase in volume is   | (Q) $0.6\pi$              |
| (3) If the rate of decrease of $\frac{x^2}{2} - 2x + 5$ is twice the rate of decrease of $x$ , then $x$ is equal to (rate of decreases is non-zero) | (R) 3                     |
| (4) Rate of increase in area of equilateral triangle of side 15 cm, when each side is increasing at the rate of 0.1 cm/s, is                        | (S) $\frac{3\sqrt{3}}{4}$ |



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285. Match List - I with List-II

<u>List - I</u>	<u>List - II</u>
(1) Circular plate is expanded by heat from radius 5 cm to 5.06 cm. Approximate increase in area is	(P) 4
(2) If an edge of a cube increases by 1%, then percentage increase in volume is	(Q) $0.6\pi$
(3) If the rate of decrease of $\frac{x^2}{2} - 2x + 5$ is twice the rate of decrease of $x$ , then $x$ is equal to (rate of decreases is non-zero)	(R) 3
(4) Rate of increase in area of equilateral triangle of side 15 cm, when each side is increasing at the rate of 0.1 cm/s, is	(S) $\frac{3\sqrt{3}}{4}$



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286. Let  $f(x)$  be function such that

$f(x + 2) - 5f(x + 1) + 6f(x) = 0 \forall x \in R$  match the following List-I



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287. Match List - I with List-II

List - I

List - II

- |   |                           |
|---|---------------------------|
| (1) Circular plate is expanded by heat from radius 5 cm to 5.06 cm. Approximate increase in area is   | (P) 4                     |
| (2) If an edge of a cube increases by 1%, then percentage increase in volume is   | (Q) $0.6\pi$              |
| (3) If the rate of decrease of $\frac{x^2}{2} - 2x + 5$ is twice the rate of decrease of $x$ , then $x$ is equal to (rate of decreases is non-zero) | (R) 3                     |
| (4) Rate of increase in area of equilateral triangle of side 15 cm, when each side is increasing at the rate of 0.1 cm/s, is                        | (S) $\frac{3\sqrt{3}}{4}$ |

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288. If maximum and minimum value of  $f(x) = {}^x C_{(2x-1)} + {}^{(20-3x)} C_{(4x-5)}$  are  $\lambda$  and  $\mu$  respectively, then the value of  $f(\lfloor \lambda + \mu \rfloor / 470)$  must be (where  $\lfloor \cdot \rfloor$  denotes the greatest integer function)

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289. Let  $f$  be the function from the set of positive integers to the set of real number such that

$$f(1) = 1$$

$$\sum_{r=1}^n r f(r) = n(n+1), \forall n \geq 2, \text{ then find the value of } 2126f(1063)$$

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290. The least period of the function  $\sin\left(\frac{x[x]}{12}\right) + \cos\left(\frac{nx}{4}\right) + \tan\left(\frac{\pi(x)}{3}\right)$  is  $\lambda$ , then the value of  $\left(\frac{\lambda}{3}\right)$  must be (where  $\lfloor \cdot \rfloor$  denotes the greatest integer function)





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291. If maximum and minimum value of  $f(x) = {}^x C_{(2x-1)} + {}^{(20-3x)} C_{(4x-5)}$  are  $\lambda$  and  $\mu$  respectively, then the value of  $\lfloor (\lambda + \mu) / 470 \rfloor$  must be (where  $\lfloor \cdot \rfloor$  denotes the greatest integer function)



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292. If the period of the function  $\cos(nx) \sin\left(\frac{5x}{n}\right)$  is  $3\pi$ , then the number of integral values of  $n$  must be



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293. If  $f(x + y) = f(x) + f(y) - xy - 1$  for all  $x, y$  in  $\mathbb{R}$  and  $f(1) = 1$ , then the value of  $\sum_{r=1}^5 f(r) / 3$  must be



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294. Let  $n(A)=4$  and  $n(B)=6$ , then the number of one one functions from A to B must be M. Then  $\sqrt{\frac{M}{10}}$  is equal to ?

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295. If  $f(x)f(y) + 2 = f(x) + f(y) + f(xy) \forall x, y \in R$  and  $f(1)=f'(1)=2$ , then  $\text{sgn}(f(x))$  equals

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296. Let  $f: [0, 1] \rightarrow [0, 1]$  defined by  $f(x) = \frac{1-x}{1+x}$  for  $0 \leq x \leq 1$  and let  $g: [0, 1] \rightarrow [0, 1]$  defined by  $g(x) = 4x(1-x)$ ,  $0 \leq x \leq 1$ . If range of  $f \circ g(x)$  is  $[\alpha, \beta]$ , then  $\alpha + \beta$  equals

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297. If  $f(x) = 1 + x^2$  and  $f(g(x)) = 1 + x^2 - x^3 + x^4$ ,  $g(2) = 2$ , then  $g(3)$  equals

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298.  $f(x)$  is a polynomial satisfying

$$f(x) \cdot f(y) = f(x) + f(y) + f(xy) = 2, \forall x, y \in \mathbb{R}$$

$f(1)=2, f(3)=10 \& f(4)=10 k_1+k_2$ . Then  $k_2$  is



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299. Find the domain of each of the following functions:

$$f(x) = \sqrt{x + 2}$$



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300. Find the domain of each of the following functions:

$$f(x) = \frac{1}{\sqrt{2x^2 - 7x - 4}}$$



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**301.** Find the domain of each of the following functions:

$$f(x) = \sqrt{x^2 - 3x + 2}$$



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**302.** Find the range of each of the following functions:

$$f(x) = (x^2 - 5x + 6)$$



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**303.** Find the domain of each of the following functions:

$$f(x) = \sqrt{\sin x - 1}$$



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**304.** Find the domain of each of the following functions:

$$f(x) = \frac{1}{\sqrt{x-1}}$$



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**305.** Find the range of the following function :

$$f(x) = (x^2 + 2x + 3)$$

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**306.** Find the range of the following function :

$$f(x) = \sqrt{x^2 - x + 1}$$

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**307.** Find the range of the following function :

$$f(x) = 3 \sin x + 4 \cos x - 5$$

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**308.** Find the range of the following function :

$$f(x) = \ln(x - [x]), \text{ where } [.] \text{ denotes the greatest integer function.}$$



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**309.** Which of the following functions are even/odd, and which are neither even or odd?

$$f(x) = \frac{x^2 + 1}{(x^4 + 1)^2}$$



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**310.** Which of the following functions are even/odd, and which are neither even or odd?

$$f(x) = x^3 + \sec x$$



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**311.** Which of the following functions are even/odd, and which are neither even or odd?

$$f(x) = \log \frac{1+x}{1-x}$$



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**312.** Which of the following functions are even/odd, and which are neither even or odd?

$$f(x) = \begin{cases} 0 & \text{if } x \text{ is rational} \\ 1 & \text{if } x \text{ is irrational} \end{cases}$$



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**313.** Examine whether the following functions are periodic or not. Write the periods of the following periodic functions.

$$f(x) = \sin(3x+5) + \cos(2x-5)$$



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**314.** Examine whether the following functions are periodic or not. Write the periods of the following periodic functions.

$$f(x) = f(x) = e^{3\{x - [x]\}}$$

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**315.** Examine whether the following functions are periodic or not. Write the periods of the following periodic functions.

$$f(x) = \cos[\pi^2]x - \cos[-\pi^2]x$$

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**316.** Examine whether the following functions are periodic or not. Write the periods of the following periodic functions.

$$f(x) = e^{ax} \sin bx$$

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317. Let  $g: [1, 3] \rightarrow Y$  be a function defined by  $g(x) = \ln(x^2 + 3x + 1)$ . Then determine whether  $g(x)$  is one-to-one or many-one.

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318. Let  $g: [1, 3] \rightarrow Y$  be a function defined by  $g(x) = \ln(x^2 + 3x + 1)$ . Then find the set of  $Y$  so that  $g(x)$  is onto.

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319. Let  $g: [1, 3] \rightarrow Y$  be a function defined by  $g(x) = \ln(x^2 + 3x + 1)$ . Then find  $g^{-1}(x)$  if it exists.

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320. Solve the following equations

$$x^2 - 4 - [x] = 0$$

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**321.** Solve the following equations

$$[x^2] + 2[x] = 3x, 0 \leq x \leq 2$$

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**322.** If the functions of  $f$  and  $g$  are defined from the set of real numbers  $\mathbb{R}$  to  $\mathbb{R}$  such that  $f(x) = e^x, g(x) = 3x - 2$ , then find the functions  $f \circ g$  and  $g \circ f$ . Define co-domain of  $f \circ g$  and  $g \circ f$  so that they become invertible and also  $(g \circ f)^{-1}$  and  $(f \circ g)^{-1}$ .

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**323.** Sketch the graph of the following functions:

$$f(x) = x + |x|$$

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**324.** Sketch the graph of the following functions:

$$f(x) = \sqrt{4 - x^2}$$



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**325.** Sketch the graph of the following functions:

$$f(x) = \sqrt{2x + 2}$$



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**326.** Sketch the graph of the following functions:

$$f(x) = I \neq x^2$$



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**327.** Sketch the graph of the following functions:

$$f(x) = \sin|x|$$





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**328.** Sketch the graph of the following functions:

$$f(x) = \sin|x|$$



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**329.** Sketch the graph of the following functions:

$$f(x) = |\sin|x||$$



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**330.** Sketch the graph of the following functions:

$$f(x) = \ln(1 + x^2)$$



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**331.** Sketch the graph of the following functions:

$$f(x) = e^{|x|}$$



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**332.** Sketch the graph of the following functions:

$$f(x) = |\ln|x||$$



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**333.** Sketch the graph of the following functions:

$$f(x) = \frac{8}{2 + x^2}$$



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**334.** Sketch the graph of the following functions:

$$f(x) = \frac{\sin x}{\sqrt{1 + \tan^2 2x}} + \frac{\cos x}{\sqrt{1 + \cot^2 2x}}$$







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**335.** Find the integral solutions to the equation  $[x][y] = x + y$ . Show that all the non-integral solutions lie on exactly two lines.



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**336.** Let  $f: \left[\frac{1}{2}, \infty\right) \rightarrow \left[\frac{3}{4}, \infty\right)$ , where  $f(x) = x^2 - x + 1$ . Find the inverse of  $f(x)$ . Hence or otherwise solve the equation,  
$$x^2 - x + 1 = \frac{1}{2} + \sqrt{x - \frac{3}{4}}.$$



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**337.** Find the domain of the function  $f(x) = \frac{1}{[|x - 1|] + [|7 - x|] - 6}$ ,  
[.] greatest integer functions.



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338. If  $f(x)$  is a real valued function which satisfied  $f(x+3/2)+f(x)+f(x+1)+f(x+1/2)$  and  $|f(x)| \leq 2A$   $x \in \mathbb{R}$ , then prove that  $f(x)$  is periodic.

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339. Let  $f(x) = \sin\left(\frac{\pi}{6}\sin\left(\frac{\pi}{2}\sin x\right)\right)$  for all  $x \in \mathbb{R}$  and  $g(x) = \frac{\pi}{2}\sin x$  for all  $x \in \mathbb{R}$ . Let  $(f \circ g)(x)$  denote  $f(g(x))$  and  $(g \circ f)(x)$  denote  $g(f(x))$ . Then which of the following is (are) true ?

A. Range of  $f$  is  $\left[-\frac{1}{2}, \frac{1}{2}\right]$

B. Range of  $f \circ g$  is  $\left[-\frac{1}{2}, \frac{1}{2}\right]$

C.  $\lim_{x \rightarrow 0} \frac{f(x)}{g(x)} = \frac{\pi}{6}$

D. There is an  $x \in \mathbb{R}$  such that  $(g \circ f)(x) = 1$

Answer: 1,2,3

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340. If  $[0, \pi/2) \rightarrow R$  is defined as

$$f(\theta) = \left| \begin{bmatrix} 1 & \tan \theta & 1 \\ -\tan \theta & 1 & \tan \theta \\ -1 & -\tan \theta & 1 \end{bmatrix} \right|$$

A.  $(2, \infty)$

B.  $(-\infty, -2]$

C.  $[2, \infty)$

D.  $(-\infty, 2]$

Answer: 3



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341.  $\{x \in R : |\cos x| \geq \sin x\} \cap \left[0, \frac{3\pi}{2}\right] =$

A.  $\left[0, \frac{\pi}{4}\right] \cup \left[\frac{3\pi}{4}, \frac{3\pi}{2}\right]$

B.  $\left[0, \frac{\pi}{4}\right] \cup \left[\frac{\pi}{2}, \frac{3\pi}{2}\right]$

C.  $\left[0, \frac{\pi}{4}\right] \cup \left[\frac{5\pi}{4}, \frac{3\pi}{2}\right]$

D.  $\left[0, \frac{3\pi}{2}\right]$

**Answer: 1**

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**342.** Let  $f[-2, 2] \rightarrow \mathbb{R}$  be a continuous function such that  $f(x)$  assumes only irrational values. If  $f(\sqrt{2}) = \sqrt{2}$ ,

A.  $f(0) = 0$

B.  $f(\sqrt{2} - 1) = \sqrt{2} - 1$

C.  $f(\sqrt{2} - 1) = \sqrt{2} + 1$

D.  $f(\sqrt{2} - 1) = \sqrt{2}$

**Answer: 4**

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**343.** Let  $f: N \rightarrow R$  be such that  $f(1) = 1$  and

$f(1) + 2f(2) + 3f(3) + \dots + nf(n) = n(n+1)f(n)$  for all  $n \in N$ ,  $n \geq 2$ , where  $N$  is the set of natural numbers and  $R$  is the set of real numbers. Then the value of  $f(500)$  is

A. 1000

B. 500

C.  $\frac{1}{500}$

D.  $\frac{1}{1000}$

**Answer: 4**



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**344.** For the function  $f(x) = \left[ \frac{1}{[x]} \right]$ , where  $[x]$  denotes the greatest integer less than or equal to  $x$ , which of the following statements are true?

- A. The domain is  $(-\infty, \infty)$
- B. The range is  $\{0\} \cup \{-1\} \cup \{1\}$
- C. The range is  $(-\infty, 0) \cup [1, \infty)$
- D. The range is  $\{0\} \cup \{1\}$

**Answer: 2,3**

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**345.** Let  $f: \left(-\frac{\pi}{2}, \frac{\pi}{2}\right) \rightarrow \mathbb{R}$  given by  $f(x) = (\log)(\sec x + \tan x)^3$

Then

- A.  $f(x)$  is an odd function
- B.  $f(x)$  is a one-one function
- C.  $f(x)$  is a onto function
- D.  $f(x)$  is an even function

**Answer: 1,2,3**

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**346.** If  $a \in R$  and the equation

$$-3(x - [x])^2 + 2(x - [x]) + a^2 = 0$$

(where  $[x]$  denotes the greatest integer  $\leq x$ ) has no integral solution, then all possible values of  $a$  lie in the interval:

- A.  $(-2, -1)$
- B.  $(-\infty, -2) \cup (2, \infty)$
- C.  $(-1, 0) \cup (0, 1)$
- D.  $(1, 2)$

**Answer: 3**

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**347.** Let  $R$  be the set of all real numbers  $f: R \rightarrow R$  be given by

$f(x) = 3x^2 + 1$ . Then the set  $f^{-1}(1, 6)$  is

A.  $\left\{ -\frac{\sqrt{5}}{3}, 0, \frac{\sqrt{5}}{3} \right\}$

B.  $\left\{ -\frac{\sqrt{5}}{3}, \frac{\sqrt{5}}{3} \right\}$

C.  $\left\{ -\frac{\sqrt{1}}{3}, \frac{\sqrt{1}}{3} \right\}$

D.  $\left( -\frac{\sqrt{5}}{3}, \frac{\sqrt{5}}{3} \right)$

**Answer: 2**



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**348.** The function  $f(x) = x^2 + bx + c$ , where  $b$  and  $c$  real constants , describes

A. One-to-one mapping

B. onto mapping

C. not one-to-one but onto mapping

D. neither one-to-one nor onto mapping

**Answer: 4**





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349. The range of the function  $y = \left( \frac{\pi^2}{16} + x^2 \right)$  is ?



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350. Let  $f(x) = 2^{100}x + 1$ ,  $g(x) = 3^{100}x + 1$

Then the set of real numbers  $x$  such that  $f(g(x)) = x$  is

- A. empty
- B. a singleton
- C. a finite set with more than one element
- D. infinite

Answer: 2



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351. Which of the following real valued functions is/are not even functions?

A.  $f(x) = x^3 \sin x$

B.  $f(x) = x^2 \cos x$

C.  $f(x) = e^x x^3 \sin x$

D.  $f(x) = x - [x]$ , where  $[x]$  denotes the greatest integer less than or equal to  $x$

Answer: 3,4



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352. Let  $f: R \rightarrow R$  be such that  $f$  is injective and  $f(x)f(y) = f(x+y)f$  or  $\forall x, y \in R$ . If  $f(x), f(y), f(z)$  are in G.P., then  $x, y, z$  are in

A. A.P. always

B.  $G. P. \text{ always}$

C.  $A. P. \text{ depend} \in \text{gonthevaluesof } x, y, z`$

D.  $G. P. \text{ depend} \in \text{gonthevaluesof } x, y, z`$

**Answer: 1**



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**353.** The function  $f[0, 3] \rightarrow [1, 29]$ , defined by

$$f(x) = 2x^3 - 15x^2 + 36x + 1, \text{ is}$$

A. one-one and onto

B. onto but not one-one

C. one-one but not onto

D. neither one-one nor onto

**Answer: 2**



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354. Let  $f(x) = ax^2 + bx + c$ ,  $g(x) = px^2 + qx + r$  such that  $f(1) = g(1)$ ,  $f(2) = g(2)$  and  $f(3) - g(3) = 2$ . Then  $f(4) - g(4)$  is

A. 4

B. 5

C. 6

D. 7

**Answer: 3**



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355. The total number of injections (one-one into mappings) from  $\{a_1, a_2, a_3, a_4\}$  to  $\{b_1, b_2, b_3, b_4, b_5, b_6, b_7\}$  is

A. 400

B. 420

C. 800

D. 840

**Answer: 4**



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**356.** Let  $R$  be the set of real numbers and the functions  $f: R \rightarrow R$  and  $g: R \rightarrow R$  be defined  $f(x) = x^2 + 2x - 3$  and  $g(x) = x + 1$ . Then the value of  $x$  for which  $f(g(x)) = g(f(x))$  is

A.  $-1$

B.  $0$

C.  $1$

D.  $2$

**Answer: 1**



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357. Let  $f(x) = x^2$  and  $g(x) = \sin x$  for all  $x \in \mathbb{R}$  then the set of all  $x$  satisfying  $(f \circ g \circ g \circ f)(x) = (g \circ g \circ f \circ f)(x)$ , where  $(f \circ g)(x) = f(g(x))$ , is

- A.  $\pm \sqrt{n\pi}, n \in \{0, 1, 2, \dots\}$
- B.  $\pm \sqrt{n\pi}, n \in \{1, 2, \dots\}$
- C.  $\frac{\pi}{2} + 2n\pi, n \in \{\dots, -2, -1, 0, 1, 2, \dots\}$
- D.  $2n\pi, n \in \{\dots, -2, -1, 0, 1, 2, \dots\}$

**Answer: A**

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358. Let  $f: (0, 1) \rightarrow \mathbb{R}$  be defined by  $f(x) = b - \frac{x}{1 - bx}$ , where  $b$  is a constant such that  $0 < b < 1$  Then

- A.  $f \circ f \circ f \circ f \in \text{vertib} \leq \text{on}(0,1)$

B.  $f \neq f^{-1}$  on  $(0, 1)$  and  $f(b) = 1/(f'(0))$

C.  $f = f^{-1}$  on  $(0, 1)$  and  $f(b) = 1/(f'(0))$

D.  $f^{-1}$  is differentiable on  $(0, 1)$

**Answer: A**

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359. The domain of the function  $f(x) = \sin^{-1}\left(\frac{8(3)^{x-2}}{1 - 3^{2(x-1)}}\right)$  is

A.  $(-\infty, -1) \cup (1, \infty)$

B.  $(-\infty, 0) \cup (0, \infty)$

C.  $[2, \infty)$

D.  $(-\infty, 0) \cup (2, \infty)$

**Answer: D**

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360. The domain of the function  $f(x) = \frac{1}{\sqrt{|x| - x}}$  is

- A.  $(0, \infty)$
- B.  $(-\infty, 0)$
- C.  $(-\infty, \infty) - \{0\}$
- D.  $(-\infty, \infty)$

Answer: B



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361. The even function of the following is

A.  $f(x) = \frac{a^x + a^{-x}}{a^x - a^{-x}}$

B.  $f(x) = \frac{a^x + 1}{a^x - 1}$

C.  $f(x) = x \cdot \frac{a^x - 1}{a^x + 1}$

D.  $f(x) = \log_2(x + \sqrt{x^2 + 1})$



**Answer: C**



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**362.** If  $f(x + 2y, x - 2y) = xy$ , then  $f(x, y)$  is equal to

A.  $\frac{1}{4}xy$

B.  $\frac{1}{4}(x^2 - y^2)$

C.  $\frac{1}{8}(x^2 - y^2)$

D.  $\frac{1}{8}(x^2 + y^2)$

**Answer: C**



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