



# MATHS

# **BOOKS - V PUBLICATION**

# SETS

**Question Bank** 

**1.** Find the set of the equation  $x^2 + x - 2 = 0$ 

in roster form.



2. Write the set {x: x is a positive integer and

 $x^{2} = 40$  in the roster form.

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**3.** Consider the set A ={1,4,9,16,25,..}. Write A in

set-builder form

4. Write the following sets in Set builder form.

$$C = \left\{rac{1}{2}, rac{2}{3}, rac{3}{4}, rac{4}{5}, rac{5}{6}, rac{6}{7}
ight\}$$

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**5.** Match each of the set on the described in the roster form with the same.set on the described in the set-builder form :





**6.** Which of the following are sets? Justify your answer.

The collection of all the months of a year

beginning with the letter J

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7. Let A = {1,2,3,4,5,6}. Insert the appropriate

symbol  $\in$  or  $\notin$  in the blank spaces

8----A

8. Write the following sets in roster form

C={x:x is a two-digit natural number such that

the sum of its digits is 8}



## 9. Write the following sets in Set builder form.

 $B = \{2, 4, 8, 16, 32\}$ 



**10.** List all the elements of the following sets : (i) A={x: x is an odd natural number} (ii) 'B={x , x. is an integer,  $-rac{1}{2} < x < rac{9}{2}$ } (iii) 'C={x: x.'.is an integer,  $x^2 < 4$ } (iv) D=[x: x is a letter in the word 'LOYAL" } (v)  $E = \{x: x \text{ is a month of a year not having 31}$ days}` (vi) F= {x: x is a consonant in the English

alphabet which precedes k}.

**11.** Match each of the set in the roster form with the same set described in set-builder

#### form:

| i) {1,2,3,6}             | a) {x : x is a prime number and a divisor of 6}  |
|--------------------------|--|
| ii) {2,3}                | b) {x : x is an odd natural number less than 10} |
| iii) {M,A,T,H,E,I,C,S}   | c) {x : x is a natural number and divisor of 6}  |
| iv) {1,3,5,7,9}          | d) {x : x is a letter of the word MATHEMATICS}.  |
| · i) c, . ii) a, iii) d, | iv) b  |



12. Which of the following sets are null sets. (i)The set 'A' of all prime númbers lying between15 and 19.

(ii) 'A=  $\{x : x < 5, x > 6'\}(iii)$ 'A ={x:



(iv) 'A={x: |x|<-4, x in N}'



13. State which of the following sets are finite

or infinite

{x:x 
$$\in$$
 N and  $x^2$ -3x+2=0}

**14.** Write the following sets in roster form and identify equal sets ( if any) A={x:x  $\in$  R anfd  $x^2$  = 25} B= {x:x  $\in$  N and  $x^2$  = 25} C = {x:x  $\in$  R and  $x^2$  - 10x+25 = 0} D = {x:x  $\in$  N and  $x^2$  - 8x+15=0} Watch Video Solution

**15.** Which of the following pairs of sets are equal? Justity your answer. (i) 'X', the set of

letters in "ALLOY" and 'B', the set of letters in

'LOYAL"

(ii) 'A={n: dotn in Z and n^2 le 4} and 'B={x: x

in R. and  $x^2-3x+2=0$ 



16. Which of the following are examples of the

null set

Set of odd natural number divisible by 2

**17.** Which of the following sets are.finite or infinite

i) The set of months of a year

ii) {1,2,3, ....}

iii) {1,2,3, ... 99,100}

iv) The set of positive integers greater than

100

v) The set of prime numbers less than 99

**18.** State whether each of the following set is finite or infinite:

i) The set of lines which are parallel to the 'x' axis.

ii) The set of letters in the English alphabet
iii) The set of numbers which are multiple of 5
iv) The set of animals living on the earth
v). The set of circles passing through the origin '(0,0)'

**19.** Are the following pair of sets equal? Give reasons.

i) A={2,3} , B={x: x is a solution of

 $x^2 + 5x + 6 = 0$  }

ii) A={x: x is a letter in the word FOLLOW}, B={y:

y is a letter in the word WOLF ")



**20.** From the sets given below, select equal sets:

A={2,4,8,12},

B={1,2,3,4},

C={4, 8,12,14},

D={3,1,4,2},

E={-1,1},

F={0, a},

G={1,-1},

H={0,1}

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**21.** Which of the following are true?

(i) If A={3,6,7}, B={2,3,7 ,8,10}, then  $A \subset B$ 

(ii) If A={1, 5, 5, 5},  $B = \{1, 3, 5\}'$ , then A sub B.  $(iii)IfA = \{x : x^2+4 x-21=0, x \text{ in } N\}, B =$ {-7,3}then A sub B.  $(iv)IfA = \{x: x^3-1=0, x \text{ in } N\}, B = \{x: x^2-4 x+3=0, x \text{ in } N\}, then A sub B`$ 



#### 22. Consider the sets

*φ*, A={1,3}, B={1,5,9}, C={1,3,5,7,9}'

Insert the symbol subset and not subset between each of the following pair of sets.

(i)  $\phi$  .... B

' (ii) A ... B

(iii) A ... C

(iv) B ... C

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**23.** Let A={a, e, i, 0, u} and B={a, b, c, d} . Is A a subset of 'B' ? No. (Why?). Is B a subset of A? No. (Why?)

24. In each of the following , determine whether the statement is true or false. If it is true, prove it. If it is false, give an example. If  $A \subset B$  and  $B \subset C$ , then  $A \subset C$ Watch Video Solution

**25.** Make correct statements by filling in the symbols 'subset' or 'not a subset' in the blank spaces:

i) '{2,3,4} ....{1,2,3,4,5}'

ii) '{a, b, c} ....., {b,c, d}' iii) '{x: x' is a student of Class XI of, your school} ' . .{x: x' is a student of your school}'

iv) '{x: x' is a circle in the plane} ' ....{x: x' is a circle in the same plane with radius 1 unit}'
v) '{x: x' is a triangle in a plane} ' ....{x: x' is a rectangle in the plane}'

vi) '{x: x' is an equilateral triangle in a plane}

'.....{x: x' is a triangle in the same plane)



**26.** Examine whether the following statements

are true or false:

- i) '{a, b} not a subset of {b, c, a}'
- ii) '{a,e} is a subset of {x: x' is a vowel in the

English alphabet}

iii) '{1,2,3} is a subset of {1,3,5}'

iv) '{a} is a subset of {b,c}'

v) '{a}is a subset of {a, b, c}'

vi) {x: x is an even natural number less than 6}is a subset of ` {x: x is a natural number which divides 36}

# **27.** Let A={1,2,{3,4},5}. Which of the following

statement are incorrect and why?

{3,4} ⊂ A

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# 28. Write down all the subsets of the following

sets

{a}

**29.** How many elements has P(A), if  $A=\phi$ ?





**31.** Write the following intervals in set-builder

form: (i) '(-3,0)'

(ii) '[6,12]'

(iii) '(6,12]'

(iv) '[-23,5)'

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**32.** Write the following intervals in set-builder

form: (i) (-3,0)

(ii) [6,12]

(iii) (6,12]

(iv) [-23,5)



33. What universal set(s) would you propose

for each of the following.

(i) The set of triangles:

(ii) The.set of isosceles triangles.

**34.** Given the set A={1,3,5},B={2,4,6} and C= {0,2,4,6,8}, which of the following may be considered as universal set(s) for all the three sets A,B and C

 $\phi$ 

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# **35.** Let A={2,4,6,8} and B={6,8,10,12}. Find $A \cup B$ .

**36.** Let  $A = \{a, e, i, o, u\}$  and  $B = \{a, i, u\}$ . Show that  $A \cup B = A$ **Vatch Video Solution** 

**37.** Let A= {Ram,Geeta, Akbar} be the set of students of class XI, who are in school hockey team. Let B ={Geeta, David , Ashok} be the set of students from class XI who are in the scholl foot ball team. Find  $A \cup B$  and interpret the set.

38. Consider the sets 'A' and 'B' of Example 12.

Find 'A nn B'.



## 39. Coňśider the sets 'X' and 'Y' of. Find 'X nn Y'

**40.** Let U = {1,2,3,4,5,6,7}, A = {1,5,6} and B = {1,2,6,7}Find  $A \cap B$ Watch Video Solution

#### **41.** Let ' V={a, e, i, o, u}' and 'B={a, i, k, u}.' Find

'V-B' and 'B-V`



**42.** Find the union of each of the following pairs of sets:

i) X={1,3,5} Y={1,2,3}

ii) A={a, e, i, o, u}, B={a, b, c}

'iii) A={x: x is-a natural number and multiple of3}

B={x: x is a natural number less than 6}

iv) 'A={x: x is a natural number and '1 < x  $\leq$  6}

B={x: x is a natural number and '6 < x < 10}'

v) 'A={1, 2,3}, B= $\{\phi\}$ 

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43. Let 'A={a, b}, B={a, b, c}.
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' Is 'A  $\subset$  B ?' What is 'A  $\cup$  B ?'.

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# **44.** If A and B are two sets such that $A \subset B$ ,

 $A \bigcup B$  is.....



{7,8,9,10}, find

 $B\cup C$ 



## **46.** If A = {1,2,3,4},B={3,4,5,6},C = {5,6,7,8} and D =

{7,8,9,10}, find

 $B\cup C\cup D$ 

**47.** If A = {3,5,7,9,11}, B = {7,9,11,13}, C = {11,13,15}

and D = {15,17}, find

 $A\cap B$ 

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48. Let U be universal set of all the students of

Class XI of a coeducational school and 'A' be

the set of all girls in Class XI. Find A'

**49.** Let U be universal set of all the students of Class, XI of a coeducational school and 'A' be

the set of all girls in Class XI. Find A!.

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**50.** Taking the set of natural number as the universal set, write down the complements of the following sets:

{x:x is an even natural number }

 $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9\},\$ 51. lf  $A = \{2, 4, 6, 8\}, \quad B = \{2, 3, 5, 7\}.$  Verify  $(A \bigcup B)$ '=A'  $\bigcap B'$ 

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## 52. Draw appropriate Venn diagram for each of

the following

 $(A\cup B)$  '

**53.** Let U be the set of all triangles in a plane. If A is the set of all triangles with atleast one

angle different from  $60^\circ$  , what is A'?

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**54.** Fill in the blanks to make each of the following a true statement:  $A \cup A' =$ 

55. If X and Y are two sets such that  $X \cup Y$ has 50 elements,X has 28 elements and Y has 32 elements,how many elements does  $X \cap Y$ have?

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**56.** In a school there are 20 teachers who teach mathematics or physics. Of these, 12 teach mathematics and 4 teach both physics and mathématics. How many teach physics?



**57.** In a class of 35 students , 24 likes to play cricket ,16 likes to play football. Also each student like to play at least one of the two game . How many likes to play both cricket and football?

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**58.** In a survey of 400 students in a school100 were listed as taking apple juice, 150 as taking

orange juice and 75 were listed as taking both apple as well as orange juice. Find how many students were taking neither apple juice nor orange juice.

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**59.** There are 200 individuals with a skin disorder, 120 had been exposed to the chemical A, 50 to chemical B and 30 to both chemical A and B, Find the number of

individuals exposed to

Chemical A but not chemical B.



**61.** If X and Y are two sets such that  $X\cup Y$  has

18 elements, X has 8 elements and Y has 15

elements, how many elements does  $X \cap Y$ 

have?



**62.** In a group of 400 people, 250 can speak Hindi and 200 can speak English. How many people can speak both Hindi and English?

63. If S and T are two sets such that S has 21 elements, T has 32 elements, and  $S \cap T$  has 11 elements, how many elements does  $S \cup T$  have?

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**64.** If X and Y are two sets such that X has 40 elements,  $X \cup Y$  has 60 elements and  $X \cap Y$  has 10 elements, how many elements does Y have?



**65.** In a group of 70 people, 37 like coffee, 52 like tea and each person likes at least one of the two drinks. How many people like both coffee and tea?

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**66.** In a group of 65 people, 40 like cricket, 10 like both cricket and tennis. How many like

tennis only and not cricket?How many like

tennis?



67. In a commifiee, 50 people speak French, 20

speak Spanish and 10 speak both Spanish and

French. How many speaks at least one of these

two languages?

68. Show that the set of letters needed to spell

"CATARACT" and the set of letters needed to

spell " TRACT" are equal.



## 69. Write down all the subsets of the following

sets

{1,2,3}





**72.** Decide, among the following sets, which, sets are subsets of one and another.

 $A = \{x \colon x \in R\}$  and x satisfy $\{x^2 - 8x + 12 = 0\}$   $B = \{2, 4, 6, \}$  $C = \{2, 4, 6, 8, \dots \}$ ,  $D = \{6\}$ 

**73.** In each of the following , determine whether the statement is true or false. If it is true, prove it. If it is false, give an example.

If  $x \in A$  and  $A \in B$ then  $x \in B$ 

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74. Let A,B and C be the sets such that  $A \cup B = A \cup C$  and  $A \cap B = A \cap C$ . Show that B = C.





76. Show that the following four conditions are equivalent: i)  $A \subset B$ ii)  $A - B = \phi$ iii)  $A \cup B = B$ iv)  $A \cap B = A$ 



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78. Is it true that for any sets A and  $B, P(A) \cup P(B) = P(A \cup B)$ ? Justify your answer



79. Show that for any sets A and B. A= $(A \cap B) \cup (A - B)$  and  $A \cup (B - A) = (A \cup B)$ 







83. Find sets A,B and C such that  $A\cap B,\,B\cap C$  and  $A\cap C$  are non-empty sets and  $A\cap B\cap C=\phi$ 

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**84.** In a survey of 600 students in a school,150 students were found to be taking tea and 225

students were taking coffee.100 were taking both tea and coffee. Find how many students were taking neither tea nor coffee.

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**85.** In a group of students, 100 students know Hindi, 50 know English and 33 know both. Each of the students knows either Hindi or English. How many students are there in the group?



**86.** In a survey of 60 people, it was found that 25 people read newspaper' 'H, 26' read newspaper 'T, 26' read newspaper 'I, 9' read both 'H' and 'I, 11' read both 'H' and 'T, 8' 'read both T and I, 3 read all three newspapers. Find. i) the number of people who read at least one of the newspapers.

ii) the number of people whó read exactly one newspaper.



**87.** In a survey it was found that 21 people liked product A,26 liked product B and 29 liked product C.If 14 people liked products A and B ,12 people liked products C and A. 14 people liked products B and C and 8 liked all the three products. Find how many liked product C only.



**88.** In a class of 35 students, 17 have taken mathematics, 10 have taken mäthematics but

not economics. Find the number of students who have 'taken both mathematics and economics and the number of students who hive taken economics but not mathematics, if it is given that each students has taken either mathematics.or economics or both,

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**89.** In a group of 800 people, 550 can speak Hindi and 450 can speak English. How many. can 'speak both Hindi and English?





**90.** If 'A' and 'B' ' be two sets containing 3 and 6

elements respectively, what can be the

minimum number of elements in 'A U B'.

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## **91.** If 'U={1,3,5,7,9,11,13,15}, A={1,5,11,13,15}', Find A'.

92. If 'A={1,2,3}, B={3,4,-5}, C={1,8,9}'. Construct a

universal set 'U'

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93. Which of the following sets are empty sets? i)  $A = \{x: x^2 - 3 = 0. \text{ and } x \text{ is rational}\}$ ii)  $B = \{x: x \text{ is an even prime number}\}$ iii)  $C = \{x: 4 < x < 5, x \in N\}$ iv)  $D = \{x: x^2 = 25 \text{ and } 'x' \text{ is an odd integer.}\}$ 

**94.** Write the following sets in roster form and identify equal sets ( if any) A={x:x  $\in$  R anfd  $x^2$  = 25} B= {x:x  $\in$  N and  $x^2$  = 25} C = {x:x  $\in$  R and  $x^2$  - 10x+25 = 0} D = {x:x  $\in$  N and  $x^2$  - 8x+15=0} Watch Video Solution

95. State which of the following sets are finite

and which are infinite:

- i) A={x: x in Z and x^2-5 x+6=0'}
- ii) 'B={x: x in Z' and 'x^2' is even}
- iii) 'C={x: x in Z.' and 'x^2=36'}
- iv) 'D={x .: x in Z' and 'xgt-10}

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## **96.** Write the set 'A={ x: x in Z, x<sup>2</sup> < 20}' in the

roster form.

97. Write the set 'X={1, 1/4, 1/9, 1/16, 1/25, ...}.' in

the set builder form.

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#### 98. Match each of the set in A described in the

roster form with the same set in 'B' described

÷

#### in the set builder form

- (i) {P, R, I, N, C, A, L} (a) {x:x is a positive integer and is a divisor of 18}
- (ii) {0}
- (b) {x:x is an integer and  $x^2-9=0$ }
- (iii) {1,2,3,6,9,18}
- (c) {x:x is an integer and x+1=1}
- (iv) {-3, 3}
- (d) {x:x is a letter of the word 'PRINCIPAL'.}

**99.** A town has total population. 25000 out of which 13000 read "The Hindustan times" and 10500 read "The Indian Express" and 2500 read both papers. Find the percentage of population who read neither of these newspapers.

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**100.** In a class of 60 boys, there are 45 boys who play cards and 30 boys play carrom. Using

set theory, find:

(i) How many boys play both games.

(ii) How many'boys play cards only.

(iii) How many boys play carroms only.

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#### 101. Match each of the set in the roster form

with the same set described in set-builder

#### form:

| i) {1,2,3,6}             | a) {x : x is a prime number and a divisor of 6}                     |    |
|--------------------------|---|----|
| ii) {2,3}                | b) $\{x : \dot{x} \text{ is an odd natural number less than } 10\}$ | ,  |
| iii) {M,A,T,H,E,I,C,S}   | c) $\{x : x \text{ is a natural number and divisor of } 6\}$        | ۰. |
| iv) {1,3,5,7,9}          | d) {x : x is a letter of the word MATHEMATICS}.                     | ,  |
| · i) c, . ii) a, iii) d, | iv) b   |    |





**102.** Describe the following sets by roster method:

(i)  $\left\{x:x^2+5x+6=0, x\in N\right\}$ (ii)  $\left\{x:x^2+6x+8=0, x\in Z\right\}$ (iii)  $\left\{x:4x+7<25, x\in N\right\}$ (iv)  $\left\{x, x^3+1=0, x\in N\right\}$ (v) the set of all lettersin the word TRIGONOMETRY.

103. Assume that P (A) = P (B). Show that A = B









**107.** Show that  $A \cap B = A \cap C$  need not imply B = C

**108.** If A={4,5,8,12}, B={1,4,6,9} and C={1,2,4,7,8,10},

#### then find

(i) 
$$A - (B - A)$$

(ii) 
$$A - (C - B)$$

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109. Let  $U=\{1,2,3,\ldots,10\}$  be the universal set. If  $A=\{3,4,6,8\},$  find A' and show that  $A\cup A'=U$ ,  $A\cap A'=\phi$  and  $\left(A'
ight)'=A$ 

110. Find A' for A={3,6,7,8}, where universal set
'U' is given by :
(i) 'U={1,2, .....10}'.

(ii) 'U={1, 2, .. .,, 15}`.

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111. Let  $X = \{1, 2, 3, ..., 12\}, A = \{4, 5, 9, 11\}$  ,  $B = \{1, 2, 4, 5, 8, 9, 10, 11, 12\}$  Verify that B' is a subset of A'.



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**113.** Prove that  $A \cup B = A \cap B$  if A = B.





114. Let 'A' and 'B' be two finite set such 'that

n(A-B)=15,  $n(A \cup B)=90$ ,  $n(A \cap B)=30$ . Find n(B).

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**115.** In a survey of 600 students in a school,150 students were found to be taking tea and 225 students were taking coffee.100 were taking both tea and coffee. Find how many students were taking neither tea nor coffee.

**116.** Of the number of three athletic teams in a school, 21 are in the basket ball team , 26 in hockey team and 20 in the football team, 14 play hockey and basket ball , 15 play hockey and football, 12 play football and basket ball and 8 play all the games. How many members are there in all?

