# ©゙" doubtnut 

India's Number 1 Education App

## MATHS

## BOOKS - V PUBLICATION

## STRAIGHT LINES

## Questionbank

1. Find the slope of a line which passes
through the points $(3,2)$ and $(-1,5)$
2. Find the slope of the lines passing through the points
(3,-2) and (-1,4)

D Watch Video Solution
3. If the angle between two lines is $\frac{\pi}{4}$ and slope of one of the lines is $\frac{1}{2}$, find the slope of the other line.
4. Line through the points $(-2,6)$ and $(4,8)$ is perpendicular to the line through the points $(8,12)$ and ( $x, 24$ ). Find the value of $x$.

## - Watch Video Solution

5. Three points $P(h, k), Q\left(\dot{x}_{1}, y_{1}\right)$ and
$R\left(x_{2}, y_{2}\right)$ lie on a line. Show that

$$
\left(h-x_{1}\right)\left(y_{2}-y_{1}\right)=\left(k-y_{1}\right)\left(x_{2}-x_{1}\right)
$$

6. In the Figure, time and distance graph of a
linear motion is given. Two positions of time and distance are recorded as, when
$T=0, D=2 . \quad$ and $\quad$ when $\quad T=3, D=8$.

Using the concept of slope, find law of motion, i.e., how distance depends upon time.

7. Draw a quadrilateral in the Cartesian plane, whose vertices are $(-4,5),(0,7),(5,-5)$. and $(-4,-2)$. Also find its area.

## - Watch Video Solution

8. The base of an equilateral triangle with side

2a lies along the $y$ - axis such that the midpoint of the base is at the origin. Find vertices of the triangle.

## Watch Video Solution

9. Find the distance between $P\left(x_{1}, y_{1}\right)$ and
$Q\left(x_{2}, y_{2}\right)$ when : (i) $P Q$ is parallel to the $y$ axis, (ii) $P Q$ is parallel to the $x$-axis.

## - Watch Video Solution

10. Find the point on the $x$-axis which equidistant from the points $(7,6)$ and $(3,4)$

## - Watch Video Solution

11. Find the slope of a line, which passes
through the origin, and the mid-point of the
line segment joining the points $P(0,-4)$ and $B(8,0)$.

## D Watch Video Solution

12. Without using the pythagoras theorem,
show that the points $(4,4),(3,5)$ and
$(-1,-1)$ are the vertices of a right angled triangle
13. Find the slope of the line, which makes' angle of $30^{\circ}$ with the positive direction of $y$ axis measured anticlockwise.

## - Watch Video Solution

14. Find the value of $x$ for which the points
$(x,-1),(2,1)$ and $(4,5)$ are collinear.
15. Without using distance formula, show that
points $(-2,-1),(4,0),(3,3)$ and $(-3,2)$
are the vertices of a parallelogram.

## D Watch Video Solution

16. Find the angle between the positive $x$-axis
and the line joining the points ( $3,-1$ ) and (4,-2).

## D Watch Video Solution

17. The slope of a line is double of the slope of another line. If tangent of the angle between
them is $\frac{1}{3}$, find the slopes of the lines.

## - Watch Video Solution

18. A line passes through $\left(x_{1}, y_{1}\right)$ and $(h, k)$.

If slope of the line is $m$, show that $k-y_{1}=m\left(h-x_{1}\right)$
19. If three points $(h, 0),(a, b)$ and $(0, k)$ lie
on a line. Show that $\frac{a}{h}+\frac{b}{k}=1$

## D Watch Video Solution

20. Find the equations of the lines parallel to axes and passing through $(-2,3)$

## D Watch Video Solution

21. Find the equation of the line through
$(-2,3)$ with siope -4

## D Watch Video Solution

22. Find the equation of the line passing through the two points $(1,-1)$ and $(3,5)$.

## D Watch Video Solution

23. Write the equation of the line for which $\tan \theta=\frac{1}{2}$, where $\theta$. is the inclination of the line and (i) $y$-intercept is $-\frac{3}{2}$ (ii) $x$-intercept is 4 .

## - Watch Video Solution

24. Find equation of the line which makes intercepts -3 and 2 on the $X$ and $Y$ axes respectively. Find its slope.
25. Find the equation of the line whose perpendicular distance from origin is 4 units and the angle which the normal makes with. positive direction of $x$ - axis is $15^{\circ}$

## - Watch Video Solution

26. The Fahrenheit temperature $F$ and absolute temperature $K$ satisfy a linear equation. Given that $K=273$ when $F=32$ and that $K=373$ when $F=212$. Express $K$
in terms of F and find the value of $F$, when $K=0$.

- Watch Video Solution

27. In exercise 1 io 8 find the equation of the line which satisfy the given condions.

Write the equations for the $x$-and $y$ axes.

D View Text Solution
28. Find the equation the following lines satisfying the given conditions.
passing through the point $(-4,3)$ with slope $\frac{1}{2}$.

## D Watch Video Solution

29. Find the equation of the line passing
through $(0,0)$ with șlope $m$.

## D Watch Video Solution

30. Find the equation of the line passing through $(2,2 \sqrt{3})$ and inclined with the $x$-axis at an angle of $75^{\circ}$

## D Watch Video Solution

31. Find the equation of the line intersecting
the $x$-axis at a distance of 3 units to the left of origin with slope -2 .
32. Find the equation of the line Intersecting the $y$-axis at a distance of 2 units above the origin and making an angle of $30^{\circ}$ with positive direction of the $x$-axis

## D Watch Video Solution

33. Find the equation the following lines satisfying the given conditions.
passing through the point $(-1,1)$ and $(2,-4)$.

## - Watch Video Solution

34. Find the equation the following lines satisfying the given conditions.
perpendicular distance from origin is 5 units and the angle the perpendicular makes with the positive direction of x -axis is $30^{\circ}$.

## - Watch Video Solution

35. The vertices of $\triangle P Q R$ are
$P(2,1), Q(-2,3) \quad$ and $\quad R(4,5) . \quad$ Find equation of the median through the vertex $R$.
36. Find the equation of the line passing through the point $(-3,5)$ and perpendicular to the line through the points $(2,5)$ and $(-3,6)$.

## - Watch Video Solution

37. A line perpendicular to the line segment
joining the points $(1,0)$ and $(2,3)$ divides it in the ratio $1: n$. Find the equation of the line.
38. Find the equation of the line that cut off
equal intercepts on the coordinate axis and passes through the point $(2,3)$

## - Watch Video Solution

39. Find the equation of the line passing through the point $(2,2)$ and cutting off intercepts on the axis whose sum is 9 .
40. Find the equation of the line through the point $(0,2)$ making an angle $\frac{2 \pi}{3}$ with the positive $x$-axis. Also, find the equation of line parallel to it and crossing the $y$-axis at a distance of 2 units. below the origin.

## - Watch Video Solution

41. The perpendicular from the origin to a line meets it at the point $(-2,9)$,find the equation of the line.

## - Watch Video Solution

42. The length $L$ (in centimetres) of a copper rod is a linear function of its Celsius temperature C. In an experiment, if
$L=124.942$ when $C=20$ and $L=125.134$ when $C=110$, express $L$ in terms of $C$.

## - Watch Video Solution

43. The owner of a milk store finds that, he can sell: 980 litres of milk each week at Rs. 14/litre and. 1220 litres of milk each week at Rs. 16/litre.

Assuming a linear relationship, between selling price and demand, how many litres could be sell weekly at.Rs. 17/litre?

## - Watch Video Solution

44. $P(a, b)$ is the mid-point of a line segment between axis. Show that equation of the line is
$\frac{x}{a}+\frac{y}{b}=2$

## - Watch Video Solution

45. Point $R$ (h, k) divides a line segment between the axes in the ratio $1: 2$. Find the equation of the line.

## D Watch Video Solution

46. By using the concept of equation of a line, prove that the three points $(3,0),(-2,-2)$
and $(8,2)$ are collinear.

## - Watch Video Solution

47. Consider the equation of the line
$3 x-4 y+10=0$

Find its
$x$ and $y$ intercepts.

D Watch Video Solution
48. Reduce the equation $\sqrt{3} x+y-8=0$ into normal form. Find the values of $p$ and $\omega$.

## - Watch Video Solution

49. Find the angles between the lines
$y-\sqrt{3} x-5=0$ and $\sqrt{3} y-x+6=0$

- Watch Video Solution

50. Show that two lines $a_{1} x+b_{1} y+c_{1}=0$ and $a_{2} x+b_{2} y+c_{2}=0 . \quad$ where $b_{1}, b_{2} \neq 0$ are:
(i) Parallel if $\frac{a_{1}}{b_{1}}=\frac{a_{2}}{b_{2}}$, and
(ii) Perpendicular if $a_{1} a_{2}+b_{1} b_{2}=0$

## - Watch Video Solution

51. Find the equation of the line parallel to $x-2 y+3=0$ and passing through the point (1,-2).
52. Find the distance of the point $(3,-5)$ from the line $3 x-4 y-26=0$

## - Watch Video Solution

53. Find the distance between the parallel
lines.
$3 x-4 y+7=0$ and $3 x-4 y+5=0$

- Watch Video Solution

54. Reduce the following equations into slope intercept form and find their slopes and the $y$ intercepts.
i) $x+7 y=0$
ii) $6 x+3 y-5=0$
(iii) $y=0$

## - Watch Video Solution

55. Reduce the following equations into
intercept form and find their intercepts on the
axes.
(i) $3 x+2 y-12=0$
ii) $4 x-3 y=6$
iii) $3 y+2=0$

## D Watch Video Solution

56. Reduce the equation $x-y=4$ into normal form.
57. Find the distance between the given point and the line.

Line $12(x+6)=5(y-2)$ and point (-1,1)

## D Watch Video Solution

58. Find the points on the $x$-axis, whose distances from the line $\frac{x}{3}+\frac{y}{4}=1$ are 4 units.
59. Find the distance between parallel lines
i) $15 x+8 y-34=0$ and $15 x+8 y+31=0$
ii) $l(x+y)+p=0$ and $l(x+y)-r=0$

## D Watch Video Solution

60. Find the equation of the line parallel to the
line $3 x-4 y+2=0$ and passing through
the point $(-2,3)$.

- Watch Video Solution

61. Find the equation of the line perpendicular to the line $x-7 y+5=0$ and having x intercept 3.

## D Watch Video Solution

62. Find the slope of the straight lines
$\sqrt{3} x+y=1, x+\sqrt{3} y=1$
Also find the angles between them.

## D Watch Video Solution

63. The line through the points $(h, 3)$ and $(4,1)$ intersects the line $7 x-9 y-19=0$ at right angle. Find the value of $h$.

## D Watch Video Solution

64. Prove that the line through the point
$\left(x_{1}, y_{1}\right)$ and parallel to the line
$A x+B y+C=0$ is
$A\left(x-x_{1}\right)+B\left(y-y_{1}\right)=0$
65. Find the equation of the perpendicular bisector of the line segment joining the points
$(3,4)$ and $(-1,2)$

## D Watch Video Solution

66. Find the coordinates of the foot of the perpendicủlar from the point $(-1,3)$, to the line $3 x-4 y-16=0$
67. The perpendicular from the origin to the
line $y=m x+c$ meets it at the point $(-1,2)$. Find the values of $m$ and $c$.

## D Watch Video Solution

68. In the triangle $A B C$ with vertices
$A(2,3), B(4,-1)$ and $C(1,2)$. Find the equation and length of altitude from the vertex $A$.
69. If' $p$ is the length of perpendicular from the origin to the line whose intercepts on. the axes are $a$ and $b$, then show that $\frac{1}{p^{2}}=\frac{1}{a^{2}}+\frac{1}{b^{2}}$

## - Watch Video Solution

70. 

If the lines
$2 x+y-3=0,5 x+k y-3=0$ and
$3 x-y-2=0$ are concurrent, find the value of $k$.
71. Find the distance of the line $4 x-\dot{y}=0$ from the point $P(4,1)$ measured along the line making an angle of $135^{\circ}$ with the positive $x$-axis.

## - Watch Video Solution

72. Assume that straight lines work as the plane mirror for a point,find the image of the
point $(1,2)$ in the line $x-3 y+4=0$

## - Watch Video Solution

73. Show that the path of a moving point such that its distance from two lines $3 x-2 y=5$ and $3 x+2 y=5$ are equal is a straight line.

## - Watch Video Solution

74. Find the values of $\theta$ and $p$ if the equation
$x \cos \theta+y \sin \theta=p$ is the normal form of the
line $\sqrt{3} x+y+2=0$

## - Watch Video Solution

75. Find the equations of the lines, which cut off intercepts on the axes whose sum and product are 1 and -6 . respectively.

## - Watch Video Solution

76. Find the points on the $x$-axis, whose distances from the line $\frac{x}{3}+\frac{y}{4}=1$ are 4
units.

## - Watch Video Solution

77. Find the equation of the line parallel to $y$ axis' and drawn thróugh the point of intersection of the lines $x-7 y+5=0$ and $3 x+y=0$

D Watch Video Solution
78. Find the equation of a line drawn perpendicular to the line $\frac{x}{4}+\frac{y}{6}=1$ through the point, where it meets the $y$-axis.

## - Watch Video Solution

79. Find the area' of the triangle formed by the
lines $y-x=0, x+y=0$ and $x-k=0$

## D Watch Video Solution

80. Find the value of $p$ so that the three lines
$3 x+y-2=0, p x+2 y-3=0 . \quad$ and
$2 x-y-3=0$ may intersect at one point.

## D Watch Video Solution

81. If three lines whose equations are
$y=m_{1} x+c_{1}, y=m_{2} x+c_{2} \quad$ and
$y=m_{3} x+c_{3}$ are concurrent, then show that

$$
m_{1}\left(c_{2}-c_{3}\right)+m_{2}\left(c_{3}-c_{1}\right)+m_{3}\left(c_{1}-c_{2}\right)=0
$$

## D Watch Video Solution

82. Find the equation of the lines through the point $(3,2)$ whịch make an angle $45^{\circ}$ with the line $x-2 y=3$

## - Watch Video Solution

83. Find the equation of the line passing through the point of intersection of the lines
$4 x+7 y-3=0$ and $2 x-3 y+1=0$ that has equal intercepts on the axes.
84. In what ratio, the line joining $(-1,1)$ and $(5,7)$ is divided by the line $x+y=4 ?$

## ( Watch Video Solution

85. Find the distance of the line
$4 x+7 y+5=0$ from the point $(1,2)$ along
the line, $2 x-y=0$

## - Watch Video Solution

86. Consider the line $x+3 y-7=0$

Find the image of the point $(3,8)$ with respect to the given line.

## D Watch Video Solution

87. A ray of light passing through the point
$(1,2)$ reflects on the $x$-axis at point $A$ and
the reflected ray passes through the point
$(5,3)$. Find the coordinates of $A$.

## D Watch Video Solution

88. A person standing at the junction
(crossing) of two straight paths represented
by. the equations $2 x-3 y+4=0$ and
$3 x+y-5=0$ wants to reach the path
whose equation is $6 x-7 y+8=0$ in the
least time. Find equation of the path that he should follow.

## D Watch Video Solution

89. In the Figure, time and distance graph of a
linear motion is given. Two positions of time and distance are recorded as, when
$T=0, D=2 . \quad$ and $\quad$ when $\quad T=3, D=8$.

Using the concept of slope, find law of motion,
i.e., how distance depends upon time.

:Time (T)

Watch Video Solution
90. If the slope of the .line joíning $(2,5)$ and $(3, \lambda)$ is -2 , find the value of $\lambda$.

## D Watch Video Solution

91. Find the slope of the line passing through
the points $(1,6)$ and $(-4,2)$.

## D Watch Video Solution

92. Without using the pythagoras theorem, show that the points $(4,4),(3,5)$ and $(-1,-1)$ are the vertices of a right angled triangle

## D Watch Video Solution

93. If the medians from $A$ and $B$ of the triangle with vertices $A(0, b), B(0,0)$ and
$C(a, 0)$ are mutually perpendicular then show that $a= \pm \sqrt{2} b$

# 94. <br> Show <br> that the <br> points <br> $\left(a t_{1}^{2}, 2 a t_{1}\right)\left(a t_{2}^{2}, 2 a t_{2}\right)$ and $(a, 0)$ are collinear <br> if $t_{1} t_{2}=-1$ 

## - Watch Video Solution

95. Find the equation of the straight line which makes angle $30^{\circ}$ with positive direction of $x$ - axis and cuts intercept 5 on the $y$-axis
96. Find the equation of the line which makes
intercepts -4 and 5 on the axes

## - Watch Video Solution

97. Find the equation of the line for which
$p=5$ and $\alpha=135^{\circ}$. Also sketch the line.

- Watch Video Solution

98. Reduce the equation $\sqrt{3} x+y-8=0$ into normal form. Find the values of $p$ and $\omega$.

## - Watch Video Solution

99. Which of the lines $2 x+7 y-9=0$ and
$4 x-y+11=0$ is farther from the point
$(2,3)$ ?

- Watch Video Solution

