



MATHS

BOOKS - A N EXCEL PUBLICATION

INTRODUCTION TO THREE DIMENSIONAL GEOMETRY

Question Bank

1. A point is on the x-axis. What are its y-coordinates and z coordinates?



2. Name the octants in which the following points lie (1,2,3), (4,-2,3), (4,-2,-5), (4,2,-5), (-4,2,5), (-3,-1,6), (-2,-4,-7).



3. Fill in the blanks The x-axis and the y-axis

taken together determine a plane known as...



4. Fill in the blanks

The co-ordinates of point in XY plane are of

the form...

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5. Fill in the blanks

Co-ordinate planes divide the space into...

octants

6. Find the distance between the point P (1,4,2)

and Q (-1,2,0).

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7. Show that the triangle with vetices (1,2,5)

(2,5,3) and (-1,3,2) is an equilateral triangle.

8. Consider the points P (x,y,z), O (0,0,0),

A(a,0,0), B(0,b,0) and C (0,0,c)

Using distance formula find PO

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9. Consider the points P (x,y,z), O (0,0,0), A(a,0,0), B(0,b,0) and C (0,0,c)

If P is equidistant from O,A,B and C, find the co-

ordinates of P

10. Consider the points A (2,4,5), B(-1,2,6) and

C(-7,-2,8)

Find AB, BC and AC.

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11. Consider the points A (2,4,5), B(-1,2,6) and

C(-7,-2,8)

Prove that A,B,C are collinear. Also find the

ratio in which B divides AC

12. Find the distance between the following pair of points:

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\left(2,\,3,\,5
ight) and \left(4,\,3,\,1
ight)
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13. Find the distance between the following pair of points:

(-3, 7, 2) and (2, 4, -1)

14. Find the distance between the following pair of points:

 $(\,-1,\,3,\,-4)$ and $(1,\,-3,\,4)$

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15. Find the distance between the points

 $(2,\ -1,3)$ and $(\ -2,1,3)$

16. Show that the points (-2, 3, 5),(1, 2, 3)

and (7, 0, -1) are collinear.

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17. Verify the following:

$$(0,\,7,\,-10)$$
, $(1,\,6,\,-6)$ and $(4,\,9,\,-6)$ are

the

vertices of an isosceles triangle.

18. Verify the following:

 $(0,\,7,\,10)$, $(\,-\,1,\,6,\,6)$ and $(\,-\,4,\,9,\,6)$ are the

vertices of a right angled triangle.



19. Verify the following:

(-1, 2, 1),(1, -2, 5),(4, -7, 8) and

 $(2,\ -3,4)$ are

the vertices of a parllelogram.

20. Find the equation of set points which are equidistant from the points (1, 2, 3) and (3, 2, -1).



21. Find the equation of the set of points P, the

sum of whose distances from A (4,0,0) and B

(-4,0,0) is equal to 10.

22. Consider the points P (3,4,-5) and Q (1,-2,3).Find the co-ordinates of the point which divides the join of P and Q in the ratio a)1:2 internally b)3:2 externally

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23. Consider the points P (3,4,-5) and Q (1,-2,3).Find the ratio in which the YZ plane divides the line joining P and Q

24. Consider the points A (3,2,-4), B (5,4,-6) and C (9,8,-10).Find AB, BC and AC. Hence prove that A,B,C are collinear. Also find the ratio in which B divides AC.

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25. Consider the points A (3,2,-4), B (5,4,-6) and

C (9,8,-10) Using section formula, prove that A,

B, C are collinear.

26. Suppose that A (2,6,-4), B(4,-2,3) and C (x,y,z)

are the vertices of a ΔABC

Find the co-ordinates of the centroid of the triangle.

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27. Suppose that A (2,6,-4), B(4,-2,3) and C (x,y,z)

are the vertices of a ΔABC

If the centroid is (7,-2,5) find the co-ordinates

of C.



29. Suppose that three consecutive vertices of

a parallelogram ABCD are A (1,2,3), B(-1,-2,-1)

and C(2,3,2).Find the co-ordinates of D



30. Find the coordinate of the point which divides the line segment joining the points (-2, 3, 5) and (1, -4, 6) internally in the ratio of 2:3.

31. Find the co-ordinate of the point which divides the line segment joining the points (-2,3,5) and (1,-4,6) in the ratio 2:3 externally.



32. Given that P (3,2,-4), Q(5,4,-6) and R(9,8,-10)

are collinear. Find the ratio in which Q divides

PR.



33. Find the ratio in which the YZ-plane divides

the line segment formed by joining the points

$$(-2, 4, 7)$$
 and $(3, -5, 8)$.

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34. Using section formula, show that the points A (2,-3,4), B(-1,2,1) and C $(0,\frac{1}{3},2)$ are collinear.

35. Find the coordinates of the points which trisect the line segment joining the points P(4, 2, -6) and Q(10, -16, 6).

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36. Find the distance between the points (x,-2,-3) and (3,1,-9)

37. If the distance between the points (x,-2,-3)

and (3,1,-9) is 7 units, find the values of x

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38. Consider the points A (1,2,3), B(2,3,1) and

C(3,1,2).Find AB,BC and CA

39. Consider the points A (1,2,3), B(2,3,1) and

C(3,1,2)

Prove that ΔABC is equilateral

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40. Let A (0,4,1), B(2,3,-1) and C(4,5,0) be the

vertices of a ΔABC . Find AB,BC and AC

41. Let A (0,4,1), B(2,3,-1) and C(4,5,0) be the vertices of a ΔABC .Prove that ΔABC is isosceles and right angled



42. Consider the points A (1,-1,3), B(2,-4,5) and

C(5,-13,11).Find AB, BC and AC



43. Consider the points A (1,-1,3), B(2,-4,5) and

C(5,-13,11).Prove that A,B,C are collinear



44. Consider the points A(1,2,8), B(0,3,4), C

(1,1,3) and D(2,0,7)

Find the mid points of AC and BD

45. Consider the points A(1,2,8), B(0,3,4), C

(1,1,3) and D(2,0,7)

Prove that ABCD is a parallelogram

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46. Consider the points A(1,-1,1), B(5,-5,4),

C(5,0,8) and D(1,4,5)

Find AB,BC,CD and DA

47. Consider the points A(1,-1,1), B(5,-5,4), C(5,0,8) and D(1,4,5) Prove that ABCD is a rhombus

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48. Consider the points A(-5,6,8), B(1,8,11),C(4,2,9) and D(-2,0,6). Find the mid points of AC and the mid point of BD and prove that ABCD is a parallelogram

49. Consider the points A(-5,6,8),
B(1,8,11),C(4,2,9) and D(-2,0,6)
Find AC and BD and prove that ABCD is a square also

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50. Let A (2,3,5), B(-1,5,-1) and C(4,-3,2) be the

vertices of a ΔABC

Find the sides AB,BC and AC

51. Let A (2,3,5), B(-1,5,-1) and C(4,-3,2) be the vertices of a $\triangle ABC$ Prove that the area of $\triangle ABCis \frac{49}{2}$ Watch Video Solution

52. Consider the points A(2,-3,0) and B (-1,1,c)

Find the distance between A and B

53. Consider the points A(2,-3,0) and B (-1,1,c)

If the distance is 13 units, find the values of c



54. Consider the point A(3,2,-4) and B (9,8,-10)

Find the co-ordinates of the points which

divides AB internally in the ratio 1:2



55. Consider the point A(3,2,-4) and B (9,8,-10)

Find the co-ordinates of the points which divides AB internally in the ratio 2:3



56. suppose that the mid point of the sides BC,CA and AB of a triangle $\triangle ABC$ are (5,7,11), (0,8,5) and (2,3,-1) If the vertices of the triangle are $A(x_1, y_1, z_1), B(x_2, y_2, z_2)$ and $C(x_3, y_3, z_3)$



in

 $x_1, x_2, x_3, y_1, y_2, y_3, z_1, z_2, \text{ and } z_3$



57. Suppose that the midpoints of the sides BC,CA and AB of a triangle ABC are (5,7,11), (0.8,5), and (2,3,-1).

Find the co-ordinates of A,B and C.

58. Given the vertices A(2,-1,4), B(3,2,-6) and

C(-5,0,2) of a triangle ABC

Find the mid point of BC



59. Given the vertices A(2,-1,4), B(3,2,-6) and

C(-5,0,2) of a triangle ABC

Find the length of the median drawn from the

vertex A



60. Given the points P(1,-1,3), Q(2,-4,5) and R(5,-13,11)

Prove that P,Q,R are collinear

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61. Given the points P(1,-1,3), Q(2,-4,5) and

R(5,-13,11)

Find the ratio in which Q divides PR

62. The vertices of a parallelogram ABCD are A(3,-1,2), B(1,2,-4) and C(-1,1,2). Find the 4th vertex.



63. Find the lengths of the medians of the triangle with vertices A(0,0,6), B(0,4,0) and C(6,0,0)



64. If the origin is the centroid of the triangle PQR with vertices P(2a,2,6), Q(-4,3b,-10) and R(8,14,2c) then find the values of a,b and c

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65. Find the co-ordinates of a point on y-axis which are at a distance of $5\sqrt{2}$ from the point P(3,-2,5)

66. A point R with x-coordinate 4 lies on the line segment joining the points P(2,-3,4) and Q(8,0,10) find the co-ordinates of R.

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67. If A and B are the points (3,4,5) and (-1,3,-7) respectively, find the equation of the set of points P such that $PA^2 + PB^2 = k^2$ where k is a constant.

