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## MATHS

## BOOKS - A N EXCEL PUBLICATION

## INTRODUCTION TO THREE

## DIMENSIONAL GEOMETRY

## Question Bank

1. A point is on the $x$-axis. What are its $y$ coordinates and z coordinates?

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2. Name the octants in which the following points lie $(1,2,3),(4,-2,3),(4,-2,-5),(4,2,-5)$, $(-4,2,-5),(-4,2,5),(-3,-1,6),(-2,-4,-7)$.

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3. Fill in the blanks The $x$-axis and the $y$-axis taken together determine a plane known as...

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4. Fill in the blanks

The co-ordinates of point in XY plane are of the form...

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5. Fill in the blanks

Co-ordinate planes divide the space into... octants

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6. Find the distance between the point $P(1,4,2)$ and $Q(-1,2,0)$.

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7. Show that the triangle with vetices $(1,2,5)$
$(2,5,3)$ and $(-1,3,2)$ is an equilateral triangle.

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8. Consider the points $P(x, y, z), O(0,0,0)$,
$A(a, 0,0), B(0, b, 0)$ and $C(0,0, c)$

Using distance formula find PO

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9. Consider the points $P(x, y, z), O(0,0,0)$,
$A(a, 0,0), B(0, b, 0)$ and $C(0,0, c)$

If $P$ is equidistant from $O, A, B$ and $C$, find the coordinates of $P$
10. Consider the points $A(2,4,5), B(-1,2,6)$ and
$C(-7,-2,8)$

Find $A B, B C$ and $A C$.

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11. Consider the points $A(2,4,5), B(-1,2,6)$ and
$C(-7,-2,8)$
Prove that $A, B, C$ are collinear. Also find the ratio in which $B$ divides $A C$
12. Find the distance between the following pair of points:
$(2,3,5)$ and $(4,3,1)$

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13. Find the distance between the following
pair of points:
$(-3,7,2)$ and $(2,4,-1)$
14. Find the distance between the following pair of points:
$(-1,3,-4)$ and $(1,-3,4)$

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15. Find the distance between the points
$(2,-1,3)$ and $(-2,1,3)$
16. Show that the points $(-2,3,5),(1,2,3)$
and $(7,0,-1)$ are collinear.

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17. Verify the following:
$(0,7,-10),(1,6,-6)$ and $(4,9,-6)$ are
the
vertices of an isosceles triangle.
18. Verify the following:
$(0,7,10),(-1,6,6)$ and $(-4,9,6)$ are the
vertices of a right angled triangle.

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19. Verify the following:
$(-1,2,1),(1,-2,5),(4,-7,8)$ and
$(2,-3,4)$ are
the vertices of a parllelogram.
20. Find the equation of set points which are equidistant from the points $(1,2,3)$ and $(3,2,-1)$.

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21. Find the equation of the set of points $P$, the
sum of whose distances from $A(4,0,0)$ and $B$
$(-4,0,0)$ is equal to 10 .
22. Consider the points $P(3,4,-5)$ and $Q$
(1,-2,3).Find the co-ordinates of the point which divides the join of $P$ and $Q$ in the ratio a)1:2 internally b)3:2 externally

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23. Consider the points $P(3,4,-5)$ and $Q$
(1,-2,3).Find the ratio in which the $Y Z$ plane divides the line joining $P$ and $Q$
24. Consider the points $A(3,2,-4)$, B $(5,4,-6)$ and
$C(9,8,-10)$.Find $A B, B C$ and $A C$. Hence prove that $A, B, C$ are collinear. Also find the ratio in which $B$ divides AC.

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25. Consider the points $A(3,2,-4)$, $B(5,4,-6)$ and

C ( $9,8,-10$ ) Using section formula, prove that A , B, C are collinear.
26. Suppose that $A(2,6,-4), B(4,-2,3)$ and $C(x, y, z)$ are the vertices of a $\triangle A B C$

Find the co-ordinates of the centroid of the triangle.

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27. Suppose that $A(2,6,-4), B(4,-2,3)$ and $C(x, y, z)$
are the vertices of a $\triangle A B C$

If the centroid is $(7,-2,5)$ find the co-ordinates of C.

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28. Suppose that three consective vertices of a parallelogram ABCD are
$A(1,2,3), B(-1,-2,-1)$ and $C(2,3,2)$
Taking $D(x, y, z)$, find the mid point of AC and BD
29. Suppose that three consecutive vertices of a parallelogram $A B C D$ are $A(1,2,3), B(-1,-2,-1)$ and $C(2,3,2)$.Find the co-ordinates of $D$

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30. Find the coordinate of the point which divides the line segment joining the points
$(-2,3,5)$ and $(1,-4,6)$ internally in the ratio of $2: 3$.
31. Find the co-ordinate of the point which divides the line segment joining the points $(-2,3,5)$ and (1,-4,6) in the ratio 2:3 externally.

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32. Given that $P(3,2,-4), Q(5,4,-6)$ and $R(9,8,-10)$ are collinear. Find the ratio in which Q divides PR.

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33. Find the ratio in which the YZ-plane divides
the line segment formed by joining the points
$(-2,4,7)$ and $(3,-5,8)$.

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34. Using section formula, show that the points $A(2,-3,4), B(-1,2,1)$ and $C\left(0, \frac{1}{3}, 2\right)$ are collinear.
35. Find the coordinates of the points which trisect the line segment joining the points
$P(4,2,-6)$ and $Q(10,-16,6)$.

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36. Find the distance between the points
( $\mathrm{x},-2,-3$ ) and ( $3,1,-9$ )

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37. If the distance between the points ( $x,-2,-3$ )
and $(3,1,-9)$ is 7 units, find the values of $x$

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38. Consider the points $A(1,2,3), B(2,3,1)$ and
$C(3,1,2)$. Find $A B, B C$ and $C A$

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39. Consider the points $A(1,2,3), B(2,3,1)$ and
$C(3,1,2)$

Prove that $\Delta A B C$ is equilateral

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40. Let $A(0,4,1), B(2,3,-1)$ and $C(4,5,0)$ be the
vertices of a $\Delta A B C$. Find $\mathrm{AB}, \mathrm{BC}$ and AC

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41. Let $A(0,4,1), B(2,3,-1)$ and $C(4,5,0)$ be the vertices of a $\triangle A B C$.Prove that $\triangle A B C$ is isosceles and right angled

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42. Consider the points $A(1,-1,3), B(2,-4,5)$ and
$C(5,-13,11)$.Find $A B, B C$ and $A C$

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43. Consider the points $A(1,-1,3), B(2,-4,5)$ and
$C(5,-13,11)$. Prove that $A, B, C$ are collinear

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44. Consider the points $A(1,2,8), B(0,3,4), C$
$(1,1,3)$ and $D(2,0,7)$

Find the mid points of $A C$ and $B D$

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45. Consider the points $A(1,2,8), B(0,3,4), C$
$(1,1,3)$ and $D(2,0,7)$

Prove that $A B C D$ is a parallelogram

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46. Consider the points $A(1,-1,1), B(5,-5,4)$,
$C(5,0,8)$ and $D(1,4,5)$

Find $A B, B C, C D$ and $D A$
47. Consider the points $A(1,-1,1), B(5,-5,4)$, $C(5,0,8)$ and $D(1,4,5)$ Prove that $A B C D$ is a rhombus

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48. Consider the points $A(-5,6,8)$,
$B(1,8,11), C(4,2,9)$ and $D(-2,0,6)$. Find the mid points of $A C$ and the mid point of $B D$ and prove that $A B C D$ is a parallelogram
49. Consider the points $A(-5,6,8)$,
$B(1,8,11), C(4,2,9)$ and $D(-2,0,6)$

Find $A C$ and $B D$ and prove that $A B C D$ is $a$ square also

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50. Let $A(2,3,5), B(-1,5,-1)$ and $C(4,-3,2)$ be the vertices of a $\triangle A B C$

Find the sides $A B, B C$ and $A C$
51. Let $A(2,3,5), B(-1,5,-1)$ and $C(4,-3,2)$ be the vertices of a $\triangle A B C$

Prove that the area of $\triangle A B C i s \frac{49}{2}$

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52. Consider the points $A(2,-3,0)$ and $B(-1,1, \mathrm{c})$

Find the distance between $A$ and $B$
53. Consider the points $A(2,-3,0)$ and $B(-1,1, c)$

If the distance is 13 units, find the values of $c$

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54. Consider the point $A(3,2,-4)$ and $B(9,8,-10)$

Find the co-ordinates of the points which divides $A B$ internally in the ratio 1:2

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## 55. Consider the point $A(3,2,-4)$ and $B(9,8,-10)$

Find the co-ordinates of the points which divides $A B$ internally in the ratio 2:3

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56. suppose that the mid point of the sides $\mathrm{BC}, \mathrm{CA}$ and AB of a triangle $\triangle A B C$ are $(5,7,11)$,
$(0,8,5)$ and (2,3,-1)

If the vertices of the triangle are
$A\left(x_{1}, y_{1}, z_{1}\right), B\left(x_{2}, y_{2}, z_{2}\right)$ and $C\left(x_{3}, y_{3}, z_{3}\right)$

$$
x_{1}, x_{2}, x_{3}, y_{1}, y_{2}, y_{3}, z_{1}, z_{2}, \quad \text { and } z_{3}
$$

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57. Suppose that the midpoints of the sides $B C, C A$ and $A B$ of a triangle $A B C$ are $(5,7,11)$, ( $0,8,5$ ), and (2,3,-1).

Find the co-ordinates of $\mathrm{A}, \mathrm{B}$ and C .

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58. Given the vertices $A(2,-1,4), B(3,2,-6)$ and $C(-5,0,2)$ of a triangle $A B C$

Find the mid point of $B C$

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59. Given the vertices $A(2,-1,4), B(3,2,-6)$ and $C(-5,0,2)$ of a triangle $A B C$

Find the length of the median drawn from the vertex A
60. Given the points $P(1,-1,3), Q(2,-4,5)$ and $R(5,-13,11)$

Prove that $P, Q, R$ are collinear

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61. Given the points $P(1,-1,3), Q(2,-4,5)$ and $R(5,-13,11)$

Find the ratio in which $Q$ divides $P R$
62. The vertices of a parallelogram $A B C D$ are
$A(3,-1,2), B(1,2,-4)$ and $C(-1,1,2)$. Find the 4th
vertex.

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63. Find the lengths of the medians of the triangle with vertices $A(0,0,6), B(0,4,0)$ and $C(6,0,0)$
64. If the origin is the centroid of the triangle PQR with vertices $P(2 a, 2,6), Q(-4,3 b,-10)$ and $R(8,14,2 c)$ then find the values of $a, b$ and $c$

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65. Find the co-ordinates of a point on $y$-axis
which are at a distance of $5 \sqrt{2}$ from the point $P(3,-2,5)$
66. A point $R$ with $x$-coordinate 4 lies on the
line segment joining the points $P(2,-3,4)$ and $Q(8,0,10)$ find the co-ordinates of $R$.

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67. If $A$ and $B$ are the points $(3,4,5)$ and $(-1,3,-7)$
respectively, find the equation of the set of points P such that $P A^{2}+P B^{2}=k^{2}$ where k is a constant.

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