



PHYSICS

NCERT - FULL MARKS PHYSICS(TAMIL)

SYSTEMS OF PARTICLES AND ROTATIONAL MOTION

Example

1. Find the centre of mass of three particle at the vertices of an equilateral triangle. The

masses of the particle are $100g$, $150g$, and $200g$ respectively. Each side of the equilateral triangle is $0.5m$ along.



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2. Find the centre of mass of a uniform triangular lamina.



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3. Find the centre of mass of a uniform L shaped lamina (a thin flat plate) with dimension as shown in Fig. The mass of the lamina is $3kg$.



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4. Find the scalar and vector products of two vectors.

$$a = (3\hat{i} - 4\hat{j} + 5\hat{k}) \text{ and } b = (-2\hat{i} + \hat{j} - 3\hat{k})$$



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5. Find the torque of a force $(7\hat{i} + 3\hat{j} - 5\hat{k})$ about the origin. The force acts on a particle whose position vector is $(\hat{i} - \hat{j} + \hat{k})$.



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6. Show that the angular momentum about any point of a single particle moving with constant velocity remains constant throughout the motion.



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7. Show that moment of a couple does not depend on the point about which you take the moments.



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8. A metal bar 70cm long and 4.00kg in mass is supported on two knife edges placed 10cm from each end. A 6.00kg weight is suspended

at 30cm from one end. Find the reactions at the knife edges. Assume the bar to be of uniform cross-section and homogeneous.



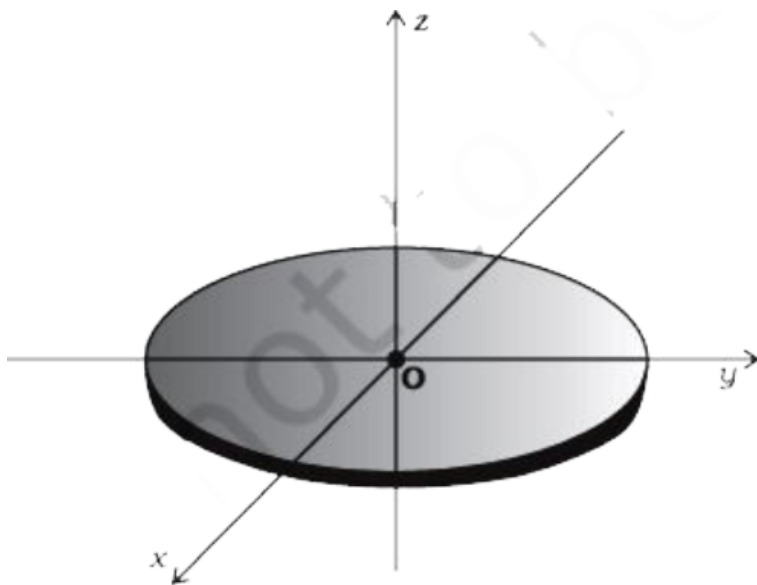
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9. A 3m long ladder weighing 20kg leans on a frictionless wall. Its feet rest on the floor 1m from the wall. Find the reaction forces of the wall and the floor.



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10. What is the moment of inertia of a disc about one of its diameters?



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11. Calculate the moment of inertia of a rod of mass M , and length l about an axis perpendicular to it passing through one of its ends.



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12. What is the moment of inertia of a ring about a tangent to the circle of the ring ?



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13. Obtain Eq. (7.38) $\omega = \omega_0 + \alpha t$ from first principles.



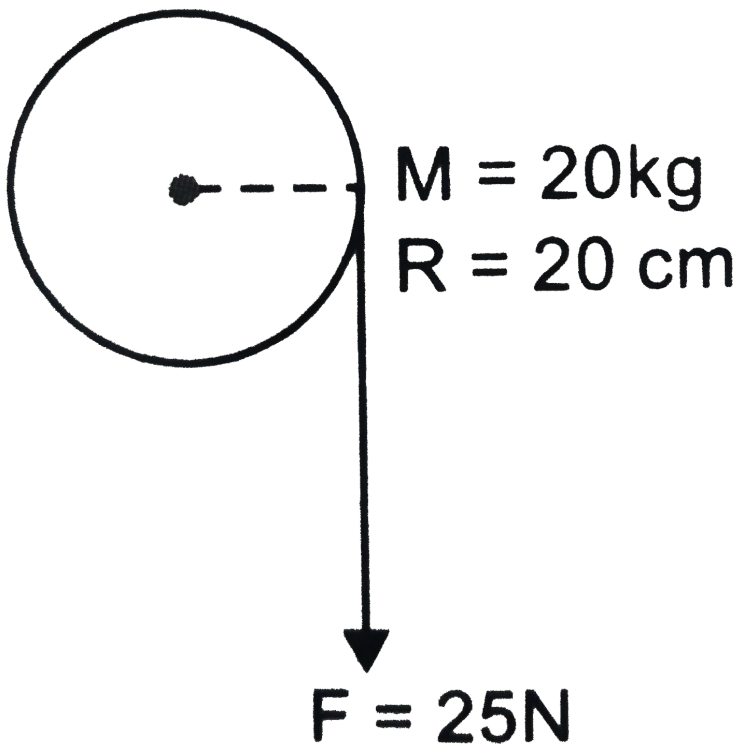
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14. The angular speed of a motion wheel is increased from 1200 rpm to 3120 rpm in 16 seconds. (i) What is the angular acceleration, assuming the acceleration to be uniform ? (ii) How many revolutions does the engine make during this time ?



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15. A cord of negligible mass is wound round the rim of a flywheel of mass 20kg and radius 20cm . A steady pull of 25N is applied on the cord as shown in Fig. The flywheel is mounted on a horizontal axle with frictionless bearings.



- (a) Compute the angular acceleration of the wheel.
- (b) Find the work done by the pull, when $2m$ of the cord is unwound.
- (c) Find also the kinetic energy of the wheel at this point. Assume that the wheel starts from

rest.

(d) Compare answers to parts (b) and (c).



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16. Three bodies, a ring, a solid cylinder and a solid sphere roll down the same inclined plane without slipping. They start from rest. The radii of the bodies are identical. Which of the bodies reaches the ground with maximum velocity?



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Exercises

1. Given the location of the centre of mass of a (i) sphere, (ii) cylinder, (iii) ring, and (iv) cube, each of uniform mass density. Does the centre of mass of a body necessarily lie on the body ?



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2. In the HCl molecule, the separation between the nuclei of the two atoms is about

1.27Å ($1\text{Å} = 10^{-10}m$). Find the approximate location of the c.m of the molecule, given that a chlorine atom is about 35.5 times as massive as a hydrogen atom and nearly all the mass of an atom is concentrated in its nucleus ?



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3. A child is standing at one end of a long trolley moving with a speed v on a smooth horizontal track. If the child starts running towards the other end of the trolley with a

speed u , the centre of mass of the system (trolley + child) will move with a speed :



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4. Show that the area of the triangle contained between the vectors a and b is one half of the magnitude of $a \times b$.



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5. Show that $\vec{a} \cdot (\vec{b} \times \vec{c})$ is equal in magnitude to the volume of the parallelepiped formed by the vectors \vec{a} , \vec{b} and \vec{c}



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6. Find the components along the x , y , z axes of the angular momentum \vec{L} of a particle, whose position vector is \vec{r} with components x , y , z and momentum is \vec{p} with components p_x , p_y and p_z . Show that if the particle moves

only in the $x - y$ plane, the angular momentum has only a z-component.



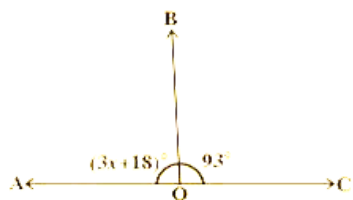
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7. Two particles each of mass m and speed v , travel in opposite direction along parallel lines separated by a distance d . Show that the vector angular momentum of this system of particles is the same about any point taken as origin.

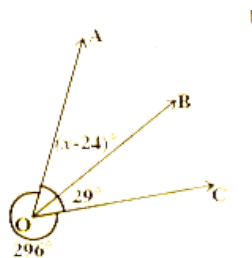


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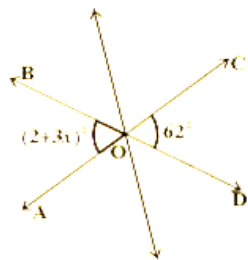
8. Find the value of x in the following figures.



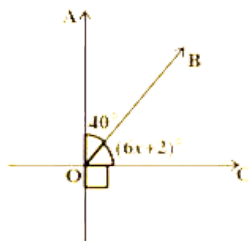
(i)



(ii)



(iii)



(iv)



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9. A car weighs 1800kg . The distance between its front and back axles is 1.8m . Its centre of gravity is 1.05m behind the front axle. Determine the force exerted by the level ground on each front wheel and each back wheel.



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10. (a) Find the moment of inertia of a sphere about a tangent to the sphere, given the

moment of inertia of the sphere about any of its diameters to be $\frac{2MR^2}{5}$, where M is the mass of the sphere and R is the radius of the sphere.

(b) Given the moment of inertia of a disc of mass M and radius R about any of its diameters to be $\frac{1}{4}MR^2$, find the moment of inertia about an axis normal to the disc passing through a point on its edge.



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11. Torques of equal magnitude are applied to hollow cylinder and a solid sphere, both having the same mass and same radius. The cylinder is free to rotate about its standard axis of symmetry, and the sphere is free to rotate about an axis passing through its centre. which of the two will acquire a greater angular speed after a given time ?



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12. A solid cylinder of mass 20kg rotates about its axis with angular speed 100s^{-1} . The radius of the cylinder is 0.25m . What is the kinetic energy associated with the rotation of the cylinder ? What is the magnitude of angular momentum of the cylinder about its axis ?



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13. A child stands at the centre of a turn table with his two arms outstretched. The turn table

is set rotating with an angular speed of 40 rpm. How much is the angular speed of the child, if he folds his hands back reducing the moment of inertia to $(2/5)$ time the initial value ? Assume that the turn table rotates without friction.

(b) Show that the child's new $K.E.$ of rotation is more than the initial $K.E.$ of rotation. How do you account for this increase in $K.E.$?



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14. A rope of negligible mass is wound around a hollow cylinder of mass 3kg and radius 40cm . What is the angular acceleration of the cylinder, if the rope is pulled with a force of 30N ? What is the linear acceleration of the rope? Assume that there is no slipping.



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15. To maintain a rotor at a uniform angular speed of 100 rads^{-1} an engine needs to transmit a torque of 200 Nm . What is the

power required by engine ? Assume 100 % efficiency of engine.



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16. From a uniform disc of radius R , a circular section of radius $R/2$ is cut out. The centre of the hole is at $R/2$ from the centre of the original disc. Locate the centre of mass of the resulting flat body.



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17. A metre stick is balanced on a knife edge at its centre. When two coins, each of mass $5g$ are put one on one of the other at the $12cm$ mark, the stick is found to be balanced at $45cm$. The mass of the metre stick is.



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18. A solid wooden sphere rolls down two different inclined planes of the same height but of different inclinations. (a) Will it reach the bottom with same speed in each case ?

(b) Will it take longer to roll down one inclined plane than other ? Explain.



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19. A hoop of radius 2m, weight 100 kg. It rolls along horizontal floor so that its center of mass has a speed of $20c\frac{m}{s}$. How much work has to be done to stop it?



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20. The oxygen molecule has a mass of $5.30 \times 10^{-26} \text{ kg}$ and a moment of inertia of $1.94 \times 10^{-46} \text{ kgm}^2$ about an axis through its centre perpendicular to the line joining the two atoms. Suppose the mean speed of such a molecule in a gas is 500 m/s and that its kinetic energy of rotation is two thirds of its kinetic energy of translation. Find the average angular velocity of the molecule.



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21. A sphere rolls up an inclined plane whose inclination is 30° . At the bottom of the inclined plane, the center of mass of the sphere has a translational speed of 5ms^{-1} (a) How far does the sphere travel up the plane? (b) How long does it take to return to the bottom?



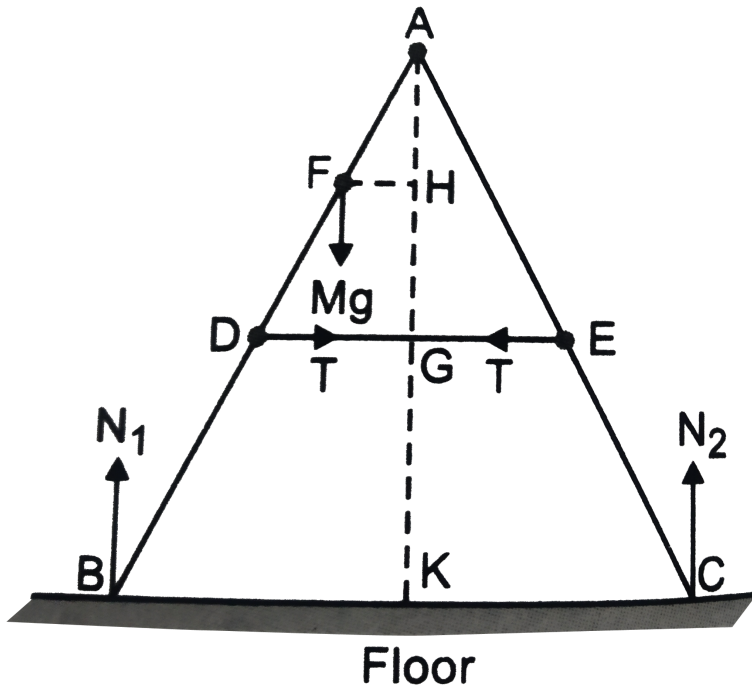
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22. As shown in Fig. the two sides of a step ladder BA and CA are 1.6m long and hinged

at A . A rope DE , $0.5m$ is tied half way up. A weight $40kg$ is suspended from a point F , $1.2m$ from B along the ladder BA . Assuming the floor to be frictionless and neglecting the weight of the ladder, find the tension in the rope and forces exerted by the floor on the ladder. (Take $g = 9.8m / s^2$)

(Hint. Consider the equilibrium of each side of

the ladder separately.)



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23. A man stands on a rotating platform, with his arms stretched horizontal holding a 5kg

weight in each hand. The angular speed of the platform is 30 revolutions per minute. The man then brings his arms close to his body with the distance of each weight from the axis changing from 90cm to 20cm . moment of inertia of the man together with the platform may be taken to be constant and equal to 7.6kgm^2 . (a) What is the his new angular speed ? (Neglect friction.)

(b) Is kinetic energy conserved in the process ? If not, from where does the change come about ?



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24. A bullet of mass $10g$ and speed $500m/s$ is fired into a door and gets embedded exactly at the centre of the door. The door is $1.0m$ wide and weight $12kg$. It is hinged at one end and rotates about a vertical axis practically without friction. Find the angular speed of the door just after the bullet embeds into it.(Hint. The moment of inertia of the door about the vertical axis at one end is $ML^2/3$)



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25. Two discs of moments of inertia I_1 and I_2 about their respective axes (normal to the disc and passing through the centre), and rotating with angular speed ω_1 and ω_2 are brought into contact face to face with their axes of rotation coincident . What is the angular speed of the two-disc system ?



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26. (a) Prove the theorem of perpendicular axes.

(Hint : Square of the distance of a point (x, y) in the x - y plane from an axis through the origin and perpendicular to the plane is $(x^2 + y^2)$).

(b) Prove the theorem of parallel axes.

(Hint : If the centre of mass of a system of n particles is chosen to be the origin $(\sum m_i r_i = 0)$).



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27. Prove the result that the velocity v of translation of a rolling body (like a ring, disc, cylinder or sphere) at the bottom of an inclined plane of a height h is given by

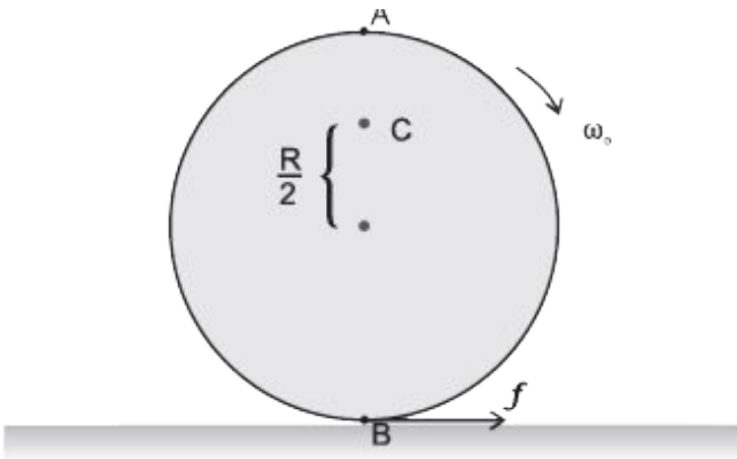
$$v^2 = \frac{2gh}{(1 + k^2 / R^2)} \quad \text{using dynamical}$$

consideration (i.e. by consideration of forces and torque). Note k is the radius of gyration of the body about its symmetry axis, and R is the radius of the body. The body starts from rest at the top of the plane.



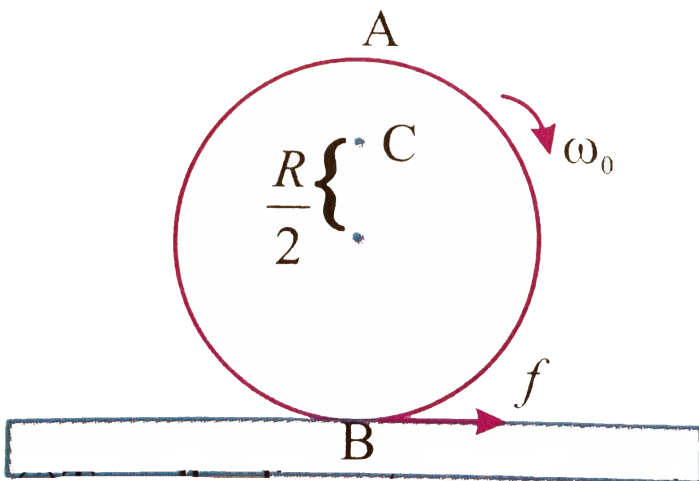
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28. A disc rotating about its axis with angular speed ω_0 is placed lightly (without any translational push) on a perfectly frictionless table. The radius of the disc is R . What are the linear velocities of the points A, B and C on the disc shown in Fig. 7.41? Will the disc roll in the direction indicated?



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29. (i) Explain why friction is necessary to make the disc to roll in the direction indicated. (ii) Give the direction of frictional force at B , and the sense of frictional torque, before perfect rolling begins. (iii) What is the force of friction after perfect rolling begins?





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30. A solid disc and a ring, both of radius 10cm are placed on a horizontal table simultaneously, with initial angular speed equal to $10\pi\text{rad/s}$. Which of the two will start to roll earlier? The coefficient of kinetic friction is $\mu_k = 0.2$.



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31. A cylinder of mass 10kg and radius 15cm is rolling perfectly on a plane of inclination 30° .

The coefficient of static friction is $\mu_s = 0.25$.

(a) How much is the force of friction acting on the cylinder ?

(b) What is the work done against friction during rolling ?

(c) If the inclination θ of plane is increased, at what value of θ does the cylinder begin to skid and not roll perfectly ?



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32. Separation of Motion of a system of particles into motion of the centre of mass and motion about the centre of mass :

(a) Show $p = p_i' + m_i V$

where p_i is the momentum of the i th particle (of mass m_i) and $p_i' = m_i v_i'$. Note v_i' is the velocity of the i th particle relative to the centre of mass.

Also, prove using the definition of the centre

of mass $\sum p_i' = 0$

(b) Show $K = K' + 1/2MV^2$

where K is the total kinetic energy of the

system of particles, K' is the total kinetic energy of the system when the particle velocities are taken with respect to the centre of mass and $MV^2/2$ is the kinetic energy of the translation of the system as a whole (i.e. of the centre of mass motion of the system). The result has been used in Sec. 7.14.

(c) Show $L = L' + R \times MV$

where $L' = \sum r'_i \times p'_i$ is the angular momentum of the system about the centre of mass with velocities taken relative to the centre of mass. Remember - $r'_i = r_i - R$, rest of the notation is the standard notation

used in the chapter. Note L and $MR \times V$ can be said to be angular momenta, respectively, about and of the centre of mass of the system of particles.

(d) Show
$$\frac{dL'}{dt} = \sum r'_i \times \frac{dp'}{dt}$$

Further, show that

$$\frac{dL'}{dt} = \tau'_{ext}$$

where τ'_{ext} is the sum of all external torques acting on the system about the centre of mass.



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Exercises True Or False

1. Read each statement below carefully and state with reasons, if it is true or false. (a) During rolling the force of friction acts in the same direction as the direction of motion of c.m of the body. (b) The instantaneous speed of the point of contact during rolling is zero. (c) The instantaneous acceleration of the point of contact during rolling is zero. (d) For perfect rolling motion, work done against friction is zero. (e) A wheel moving down a

perfectly frictionless inclined plane will undergo slipping (not rolling motion).



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