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## MATHS

## BOOKS - MODERN PUBLICATION

## MATHEMATICAL REASONING

Example

1. Which of the following sentences are
statement? Give reason for your answer.

The sum of 5 and 7 is greater than 10
2. Whether the following sentence is statement. Give reason for your answer :

There are 35 days in a month.

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3. Which of the following sentences are statement? Give reason for your answer.

Mathematics is difficult

## Watch Video Solution

4. Which of the following sentences are statement? Give reason for your answer.

Answer this question

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5. Which of the following sentences are statement? Give reason for your answer.

All real numbers are complex numbers
6. Which of the following sentences are statement? Give reason for your answer.

The square of a number is an even number

## D Watch Video Solution

7. Whether the following sentence is statement. Give reason for your answer :

Mathematics is a fun.

- Watch Video Solution

8. Write the negation of the following statements.

Chennai is the capital of Tamil Nadu.

## D Watch Video Solution

9. Write the negation of the following statements
$\sqrt{2}$ is not a complex number
10. Write the negation of the following statements

All triangles are not equilateral triangle

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11. Write the negation of the following statements

The number 2 is greater than 7
12. Write the negation of the following statements

Every natural number is an integer.

## D Watch Video Solution

13. Write the negation of the following statement :

Both the diagonals of a rectangle have the same length.
14. Write the negation of the following statement:
$\sqrt{7}$ is rational.

## D Watch Video Solution

15. Write the negation of the following
statements and check whether the resulting statements are true,

Australia is a continent.
16. Write the negation of the following statements and check whether the resulting statements are true,

There does not exist a quadrilateral which has all its sides equal.

## D Watch Video Solution

17. Write the negation of the following statements and check whether the resulting
statements are true,

Every natural number is greater than 0.

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18. Write the negation of the following statements and check whether the resulting statements are true,

The sum of 3 and 4 is 9 .
19. Find the component statements of the following compound statements and check whether they are true or false.

Number 3 is prime or it is odd.

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20. Find the component statements of the following compound statements and check whether they are true or false :

All integers are positive or negative.
21. Find the component statements of the following compound statements and check whether they are true or false.

100 is divisible by 3,11 or 5 .

- Watch Video Solution

22. Find the component statement of the
following and check whether they are true or not.

A square is a quadrilateral and its four sides are equal.

## D Watch Video Solution

23. Find the component statements of the
following compound statements and check whether they are true or not:

All prime numbers are either even or odd.
24. Find the component statement of the
following and check whether they are true or not.

A person who has taken mathematics or computer science can go for MCA.

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25. Find the component statements of the
following compound statements and check
whether they are true or not :

Chandigarh is the capital of Haryana and U.P.

## D Watch Video Solution

26. Write the component statements of the following compound statements and check whether the compound statement is true or false.
$\sqrt{2}$ is a rational number or an irrational number.
27. Find the component statements of the following compound statements and check whether they are true or not:

24 is a multiple of 2,4 and 8 .

## D Watch Video Solution

28. Write the component statements of the following compound statement and check whether the compound statement is true or false.

A line is Straight and extends indefinitely in both directions.

## D Watch Video Solution

29. Write the component statements of the
following compound statement and check whether the compound statement is true or false.

0 is less than every positive integer and every negative integer.

D Watch Video Solution
30. Write the component statements of the following compound statement and check whether the compound statement is true or false.

All living things have two legs and two eyes.

## D Watch Video Solution

31. Write the component statements of the following compound statement and check whether the compound statement is true or
false.
$\sqrt{2}$ is a rational number or an irrational number.

## D Watch Video Solution

32. Find the component statements of the following compound statements and check whether they are true or false :

All integers are positive or negative.
( Watch Video Solution
33. Write the component statements of the following compound statement and check whether the compound statement is true or false.

All primes are either even or odd.

## D Watch Video Solution

34. For the following compound statement
first identify the connecting words and then break it into component statement :

All rational numbers are real and all real numbers are not complex.

## D Watch Video Solution

35. For each of the following compound statements first identify the connecting words and then break it into components statements Square of an integer is positive or negative.

## - Watch Video Solution

36. For each of the following compound statements first identify the connecting words and then break it into components statements The sand heats up quickly is the sun and does not cool down fast at night.

## D Watch Video Solution

37. For each of the following compound statements first identify the connecting words and then break it into components statements
$x=2$ and $x=3$ are the roots of the equation
$3 x^{2}-x-10=0$

D Watch Video Solution
38. State whether the OR used in the following statements is exclusive or inclusive
sun rises or moon sets

D Watch Video Solution
39. State whether the OR used in the following statements is exclusive or inclusive to apply for a driving license you should have a ration card or a passport.

## D Watch Video Solution

40. State whether the OR used in the following
statements is exclusive or inclusive

All integers are positive or negative.
41. Check whether "or" used in the following compound statement is exclusive or inclusive ?

Write the component statements of the compound statement and use them to check whether the compound statement is true or not. Justify your answer. t : you are wet when it rains or you are in a river.
42. Write the negation of the following compound statement :
$3+2=5$ and $7<9$.

## D Watch Video Solution

43. Write the negation of the following compound statement :

27 is divisible by 3 or sky is blue.

## D Watch Video Solution

44. Write the negation of the following compound statement :

Jaipur is in India and Washington is not in India.

## D Watch Video Solution

45. Identify the quantifier of the following
statement :

For every real number $x, x+3>x$.
46. Identify the quantifier of the following statement :

There exists a real number x such that $\sqrt{x}$ is a natural number.

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47. Identify the quantifier of the following
statement:

Some real numbers are rational.
48. Identify the quantifier of the following
statement :

All birds can fly.

## - Watch Video Solution

49. Identify the quantifier in the following
statements and write the negation of the statements

There exists a number is which is equal to its square.
50. Identify the quantifier in the following statements and write the negation of the statements

For every real number $\mathrm{x}, \mathrm{x}$ is less than $\mathrm{x}+1$

## - Watch Video Solution

51. Identify the quantifier in the following statements and write the negation of the

## statements

There exists a capital for every state in india.

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52. Write each of the statement in the form if
$p$ and then $q$
p: It is necessary to have a password to log on
to the server.

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53. Write each of the following statements in
the form "if $p$ then $q$ "
$\mathrm{q}:$ There is traffic Jam whenever it rain.

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54. Write each of the statement in the form if
$p$ and then $q$
q: you can access the website only if you pay a subscription fee.
55. Write each of the statements in the form if then

To get an $A^{+}$in the class it is necessary that you do all the exercises of all the book.

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56. Which of the following statemennts jare true?

If a number is divisible by 9 ,it must be divisible by 3.
57. Write the contra positive of the following statements:

If you are born in India, then you are a citizen of India.

## - Watch Video Solution

58. Write the contrapositive of the following statement:

If a triangle is equilateral, it is isosceles.

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59. Write the converse of the following
statement:

If a number n is odd, then $n^{2}$ is odd.

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60. Write the converse of the following
statement :

If two integers $a$ and $b$ are such that $a>b$, then (a-b) is always a positive integer.

## D Watch Video Solution

61. state the converse and contapositive of the given following statement :

If you live in Delhi, then you have winter clothes.
62. Given the following statement :

If you do not have winter clothes, then you do not live in Delhi. write its converse.

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63. Given the following statement :

If you have winter clothes, then you live in

Delhi Identify these as contrapositive or converse of each other.
64. Given below are two pairs of statements.

Combine these two statements using if and only if:
p : If a rectangle is a square, then all its four sides are equal. q : If all the four sides of a rectangle are equal, then the rectangle is a square.
65. Given below are two pairs of statements.

Combine these two statements using if and only if :
$p$ : If the sum of digits of a number is divisible by 3 , then the number is divisible by 3 . $q$ : If a number is divisible by 3 , then the sum of its digits is divisible by 3.

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66. For the given statements identify the necessary and sufficient conditions. t: If you drive over 80 km per hour, then you will get a fine.

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67. Determine the truth value of the following :
$5+4=9$ iff $8-2=6$.

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68. Determine the truth value of the following

Apple is a fruit iff Delhi is in Japan.

## D Watch Video Solution

69. Give below are two statements
$\mathrm{p}: 25$ is a multiple of $5 \mathrm{q}: 25$ is a multiple of 8 .

Write the compound statement connecting
these two statements with And and Or in both
cases check the validity of the compound
statement.
70. Check whether the following statement is true or not

If $x, y \in z$ are such that x and y are odd, then $x y$ is odd.

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71. Show that the statement

IF x is a real number such that $x^{3}+4 x=0$
then $x$ is 0 is true by

## direct method

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72. Show that the statement

IF x is a real number such that $x^{3}+4 x=0$
then $x$ is 0 is true by
method of contradiction

- Watch Video Solution


## 73. Show that the statement

IF x is a real number such that $x^{3}+4 x=0$
then $x$ is 0 is true by
method of contrapositive

## - Watch Video Solution

74. Show that the following statement is true by the method of contrapositive
$r$ : If is x is an integer and $x^{2}$ is even, then x is also even.
75. By giving a counter example, show that the following statement is not true : p: If the angles of a triangle are equal, then the triangle is an obtuse angled triangle.

## D Watch Video Solution

76. Verify by the method of contradiction that $\sqrt{7}$ is irrational.
77. Which of the following statements are true and which are false?

In each case give a valid reason for your answer.
p: Each radius of a circle is a chord of the circle.
78. Whether the following statement is true or false? Give a valid reason for saying so.
q : The centre of a circle bisects each chord of the circle.

## - Watch Video Solution

79. Whether the following statement is true or false? Give a valid reason for saying so.
$r$ : Circle is a particular case of an ellipse.
80. Whether the following statement is true or false? Give a valid reason for saying so.
s: If $x$ and $y$ are integers such that $x>y$, then $-x$
$<-y$.

## D Watch Video Solution

81. Whether the following statement is true or
false? Give a valid reason for saying so.
$\mathrm{t}: \sqrt{11}$ is a rational number.
82. Check in validity of the following statement
: Square of an integer is positive or negative .

## - Watch Video Solution

83. By giving a counter example, show that the
following statement is false. "If n is an odd integer, then n is prime."
84. Show that the statement : "For any real numbers a and $\mathrm{b}, a^{2}=b^{2}$ implies that $\mathrm{a}=\mathrm{b}$ " in not true by giving a counter example.

## D Watch Video Solution

85. By giving a counter example, show that
the following statement is not true.
r : The equation $x^{2}-1=0$ does not have a root lying between 0 and 2 .
86. Check whether the following statement is
true or false by proving its contrapositive : "If
$x, y \in Z$, such that xy is odd, then both x and y are odd."

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87. Check whether the following statement is
true or not : "If $x, y \in N$ are such that x and y are even, then $x y$ is even."
88. Show by contradiction $p=\sqrt{2}$ is irrational.

## D Watch Video Solution

89. Write the following statement in five different ways, conveying the same meaning :
p : If a triangle is equiangular, then it is an obtuse- angled triangle.
90. For the following compound statements, first identify the corresponding component Statements. Then check whether the statements are true or not :

If a triangle $A B C$ is equilateral, then it is isosceles.

## D Watch Video Solution

91. For the following compound statements,
first identify the corresponding component

Statements. Then check whether the

## statements are true or not :

If $a, b$ are integers, then $a b$ is $a$ rational number.

## D Watch Video Solution

92. Check the validity of the statement given
below by the method given against it.

The sum of an irrational number and a rational number is irrational.
93. Check the validity of the statement given below by the method given against it.
q : If n is areal number when $\mathrm{n}>3$ then $n^{2}>9$

## - Watch Video Solution

94. By giving a counter example, show that the following statement is false. "If n is an odd integer, then n is prime."
95. By giving a counter example, show that the
following statement is not true :
The equation $x^{2}-4=0$ does not have a root lying between 0 and 3 .

## - Watch Video Solution

96. Determine whether the argumentused to
check the validity of the following statement is
correct. p : "If $x^{2}$ is irrational, then x is ration."

## Exercise

1. Whether the following is statement or not ?

Give reason for your answer :

Rajendra Prasad was the first President of India.

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2. Whether the following is statement or not ?

Give reason for your answer :

The sun is a star.

## D Watch Video Solution

3. Whether the following is statement or not ?

Give reason for your answer :

The number 6 has three prime factors.

## D Watch Video Solution

4. Which of the following sentences are
statement? Give reason for your answer.

The sum of all interior angles of a triangles is $180^{\circ}$

## - Watch Video Solution

5. Whether the following is statement or not ?

Give reason for your answer :

There is no rain without clouds.

D Watch Video Solution
6. Whether the following is statement or not ?

Give reason for your answer :

8 is less than 6.

## D Watch Video Solution

7. Whether the following is statement or not ?

Give reason for your answer :
Who are you?

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8. Which of the following sentences are statement? Give reason for your answer.

Today is a windy day

- Watch Video Solution

9. Whether the following is statement or not ?

Give reason for your answer :
Where is your bag ?

D Watch Video Solution
10. Whether the following is statement or not
? Give reason for your answer :

Who are you?

D Watch Video Solution
11. Whether the following is statement or not ?

Give reason for your answer :

His birth day is 29th February.

D Watch Video Solution
12. Whether the following is statement or not
? Give reason for your answer :

Listen on me, John !

## D Watch Video Solution

13. Classify the following statement as 'true' or
'false' :

Congruent triangles are also similar.
14. Classify the following statement as 'true' or
'false':
$2+1=3$.

- Watch Video Solution

15. Classify the following statement as 'true' or
'false':
$2+7=6$.
16. Classify the following statement as 'true' or 'false':
$2+3<6$.

D Watch Video Solution
17. Classify the following statement as 'true' or
'false':

17 is a prime number.

D Watch Video Solution
18. Classify the following statement as 'true' or
'false':

Number of ways of seating two persons in two chairs out of n persons is ${ }^{n} P_{2}$.

## - Watch Video Solution

19. Classify the following statement as 'true' or
'false':

A triangle has four sides.
20. Classify the following statement as 'true' or 'false':
$\sin (A+B)=\sin A+\sin B$ for all values of $A$ and B.

## - Watch Video Solution

21. Classify the following statement as 'true' or 'false':

Moon is a heavenly body.
22. Whether the following is statement ? Write the truth value :

There are only finite number of rational numbers.

D Watch Video Solution
23. Whether the following is statement ? Write
the truth value :

Similar triangles are also congruent.

## Watch Video Solution

24. Which of the following sentences are statement? Give reason for your answer.

The square of a number is an even number

## D Watch Video Solution

25. Whether the following is statement ? Write the truth value :

Product of $(-1)$ and 8 is 8.
26. Whether the following is statement ? Write the truth value :

All integers are natural numbers.

## - Watch Video Solution

27. Whether the following is statement ? Write the truth value :

Zero is a complex number.
28. Whether the following is statement ? Write the truth value :

Every set is a finite set.

## D Watch Video Solution

29. Whether the following is statement ? Write
the truth value :

Sum of an even number and odd number is always an even number.
30. Whether the following is statement ? Write the truth value :

Sides of quadrilateral have equal length.

## D Watch Video Solution

31. Whether the following is statement ? Write the truth value :

He is an honest man.
32. Whether the following is statement ? Write the truth value :

How far is Chennai from here?

## D Watch Video Solution

33. Whether the following is statement ? Write the truth value :

Sky is blue.
34. Give three examples of sentences, which are not statements. Give reasons for your answers.

## D Watch Video Solution

35. Write the negation of the following
statement :
p : For every positive real number x , the number $\mathrm{x}-1$ is also positive.
36. Write the negation of the following statements
$p$ : all cats scratch.

## - Watch Video Solution

37. Write the negation of the following statements
q : For every real number x . either $x>1$ or $x<1$

## - Watch Video Solution

38. Write the negation of the following statement :
s : There exists a number x such that 0

## D Watch Video Solution

39. Write the negation of the following statement :
p: Hyderabad is the capital of Andhra.
40. Write the negation of the following statement :
q : The earth is round.

## - Watch Video Solution

41. Write the negation of the following statement :
$r$ : The sun is cold.
42. Write the negation of the following statement:
$s$ : Some even integers are prime.

## D Watch Video Solution

43. Write the negation of the following
statement:
p: Each natural number is greater than 0.
44. Write the negation of the following statement :
q : The sum of 2 and 5 is 6 .

## - Watch Video Solution

45. Write the negation of the following
statement:
$r$ : The whole number is an integer.
46. Write the negation of the following statement:
s : A rectangle is a pentagon or a quadrilateral.

## - Watch Video Solution

47. Write the negation of the following statement :
t : Asia is a continent.
48. Write the negation of the following statement : Both the diagonals of a Rhombus have the same length .

- Watch Video Solution

49. Write the negation of the following statement :
$\mathrm{q}: \sqrt{5}$ is rational.

D Watch Video Solution
50. Write the negation of the following statement:
$r:-5$ is greater than -3.

## D Watch Video Solution

51. Write the negation of the following statement :
s: $5+3=7$.

D Watch Video Solution
52. Write the negation of the following statement :
p : For every real number $\mathrm{x}, x^{2}>x$.

## D Watch Video Solution

53. Write the negation of the following statement:
q : There exists a rational number x such that
$x^{2}=2$.
54. Write the negation of the following statement:
r: All birds have wings.

## D Watch Video Solution

55. Write the negation of the following statement :
s : All students study Mathematics at the elementary level.
56. Are the following pairs of the statement negation of each other

The number x is not a rational number

The number is $x$ is not an irrational number

## D Watch Video Solution

57. Are the following pairs of the statement negation of each other

The number x is not a rational number

The number is $x$ is not an irrational number

D Watch Video Solution
58. Find the component statements of the following compound statements:

0 is a positive number or a negative number.

D Watch Video Solution
59. Find the component statements of the following compound statements :

25 is a multiple of 5 and 8.

## D Watch Video Solution

60. Find the component statements of the following compound statements :

All rational numbers are real and all real numbers are complex.
61. Find the component statements of the following compound statements:

The sun shines or it rains.

## - Watch Video Solution

62. Find the component statements of the following compound statements:

The sky is blue and the grass is green.
63. Find the component statements of the following compound statements:

The earth is round or the sun is cold.

## D Watch Video Solution

64. Find the component statements of the following compound statements :

Roses are red and lilies are white.

## - Watch Video Solution

65. Find the component statements of the following compound statements :

It is raining and it is cold.

## D Watch Video Solution

66. Find the component statements of the following compound statements :

There is something wrong with the bulb or with wiring.
67. Find the component statement of the
following and check whether they are true or not.

All prime numbers are either even or odd.

## - Watch Video Solution

68. Find the component statement of the
following and check whether they are true or not.

24 is a multiple of 2,4 and 8 .
69. Find the component Statements of the following and check whether they are true or not :

45 is a multiple of 3,5 and 9.

## D Watch Video Solution

70. Find the component Statements of the following and check whether they are true or
not :
$\mathrm{x}=1$ and $\mathrm{x}=-1$ are roots of $x^{2}-1=0$.

## D Watch Video Solution

71. Find the component Statements of the following and check whether they are true or not :

A rhombus is a quadrilateral and a pentagon.
72. Find the component Statements of the following and check whether they are true or not :

India is a democracy and a monarchy.

## - Watch Video Solution

73. Find the component Statements of the
following and check whether they are true or not :

The earth revolves around the sun or the moon.

D Watch Video Solution
74. Find the component Statements of the following and check whether they are true or not :

Milk is solid or water is a liquid.

D Watch Video Solution
75. For each of the following compound statements first identify the connecting words and then break it into components statements $x=2$ and $x=3$ are the roots of the equation $3 x^{2}-x-10=0$

## D Watch Video Solution

76. For the following compound statements, identify the connecting words and then write the component statement :

13 is not a prime number or 15 is not a composite number.

## D Watch Video Solution

77. For the following compound statements, identify the connecting words and then write the component statement :
$2+3 i$ is a real number or $2+3 i$ is a complex number.
78. For the following compound statements, identify the connecting words and then write the component statement :

Anush is rich or happy.

## D Watch Video Solution

79. For the following compound statements, identify the connecting words and then write the component statement :

The sun is cold and the moon revolves around the sun.
80. For the following compound statements,
identify the connecting words and then write the component statement :

The school works or a holiday is declared.

## - Watch Video Solution

81. Write the truth value of the following compound statement:

## $5+5=10$ and $4+8=12$.

## D Watch Video Solution

82. Write the truth value of the following compound statement :

$$
5+5=10 \text { or } 4+8=12 .
$$

## D Watch Video Solution

83. Write the truth value of the following
compound statement :

## $5+5=10$ and $4+8=13$.

## D Watch Video Solution

84. Write the truth value of the following compound statement :

$$
5+5=10 \text { or } 4+8=13
$$

## D Watch Video Solution

85. Write the truth value of the following
compound statement :

## $5+5=11$ and $4+8=12$.

## D Watch Video Solution

86. Write the truth value of the following compound statement :
$5+5=11$ or $4+8=12$.

## D Watch Video Solution

87. Write the truth value of the following
compound statement :

## $5+5=11$ and $4+8=13$.

## D Watch Video Solution

88. Write the truth value of the following
compound statement :
$5+5=11$ or $4+8=13$.

## D Watch Video Solution

89. Write the truth value of the following
compound statement :

Blue whale is a mammal or a raptitle.

## D Watch Video Solution

90. Write the truth value of the following compound statement :

Sri Lanka is an island country and Yamuna is a river.

- Watch Video Solution

91. Write the component statements of the
following compound statements and check
whether the compound statement is true or false.

All rational numbers are real and all real numbers are not complex.

## D Watch Video Solution

92. Write the component statements of the following compound statements and check
whether the compound statement is true or false.
$x=2$ and $x=3$ are the roots of
$3 x^{2}-x-10=0$.

## - Watch Video Solution

93. Write the component statements of the following compound statements and check whether the compound statement is true or false.

The sand heats up quickly in the sun and does not cool down fast at night.

## D Watch Video Solution

94. Write the component statements of the following compound statements and check whether the compound statement is true or false.

Bangalore is the capital of Andhra and Karnataka.
95. Write the component statements of the
following compound statements and check whether the compound statement is true or false.

125 is a multiple of 7 or 8.

## D Watch Video Solution

96. Write the component statements of the
following compound statements and check whether the compound statement is true or
false.

Mumbai is the capital of Gujarat or Maharashtra.

## D Watch Video Solution

97. Write the component statements of the
following compound statement and check whether the compound statement is true or false.
$\sqrt{2}$ is a rational number or an irrational number.

## Watch Video Solution

98. Write the component statements of the following compound statements and check whether the compound statement is true or false.

A square is a polygon or a parallelogram.

## - Watch Video Solution

99. Write the component statements of the
following compound statements and check
whether the compound statement is true or false.

A rectangle is a quadrilateral and hexagon.

## D Watch Video Solution

100. Identify the type of 'Or' used in the following statement and check whether the statement is true or false.
$\sqrt{2}$ is a rational number or an irrational number.
101. Identify the type of 'Or' used in the following statement and check whether the statement is true or false.

To enter into public library children need an identity card from the school or a letter from the school authorities.

## D Watch Video Solution

102. Identify the type of 'Or' used in the following statement and check whether the
statement is true or false.

A rectangle is a quadrilateral or a 5-sided polygon.

## D Watch Video Solution

103. For the following Statement, determine whether an inclusive 'Or' or exclusive 'Or' is used. Give reasons for your answer.

To enter a country, you need a passport or a voter registration card.
104. For the following Statement, determine whether an inclusive 'Or' or exclusive 'Or' is used. Give reasons for your answer.

The school is closed if it is a holiday or a Sunday.

## D Watch Video Solution

105. For the following Statement, determine whether an inclusive 'Or' or exclusive 'Or' is
used. Give reasons for your answer.

Two lines intersect at a point or are parallel.

## D Watch Video Solution

106. For the following Statement, determine whether an inclusive 'Or' or exclusive 'Or' is used. Give reasons for your answer.

Students can take French or Sanskrit as their third language.

## - Watch Video Solution

107. Write the negation of the following : $x>3$ or $x,<3$.
( Watch Video Solution
108. Write the negation of the following :

Sky is blue and $7<9$.

- Watch Video Solution

109. Write the negation of the following :

Anil is cruel or he is strict.

## D Watch Video Solution

110. For each of the following compound statements first identify the connecting words and then break it into components statements

The sand heats up quickly is the sun and does not cool down fast at night.
111. Check whether the following pairs of statements are negation of each other. Give reasons for your answer.
$x+y=y+x$ is true for every real number x and $y$.

There exists real number $x$ and $y$ for which $x+y$
$=y+x$

- Watch Video Solution

112. Let p : It is raining to-day and q : There is no light in this room. Give a single vertal sentence, which describes the following :
$\sim \mathrm{q}$.

## D Watch Video Solution

113. Let p : It is raining to-day and q : There is
no light in this room. Give a single vertal sentence, which describes the following :
$\sim \mathrm{q}$.
114. Let p : It is raining to-day and q : There is no light in this room. Give a single vertal sentence, which describes the following :
$\sim \mathrm{q}$.

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115. Let p : It is raining to-day and q : There is no light in this room. Give a single vertal
sentence, which describes the following :
$\sim \mathrm{q}$.

D Watch Video Solution
116. Let p : It is raining to-day and q : There is
no light in this room. Give a single vertal sentence, which describes the following :
$\sim$ p or $\sim q$.

D Watch Video Solution
117. Identify the quantifier in the following statement and state its type :

For every $x \in N, x+3$ is greater than x .

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118. Identify the quantifier in the following statement and state its type :

There exists $x \in N, x+3=9$.
119. Identify the quantifier in the following statement and state its type :

Some real numbers are rational .

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120. Identify the quantifier in the following statement and state its type :

Any integer is either positive or negative.
121. Identify the quantifier in the following statement and state its type :

Every city in U.S.A. is clean.

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122. Identify the quantifier in the following statement and state its type :

There exists a living person who is 175 years old.
123. Write the negation of the following :

For every real number $x, x+0=x=0+x$.

## D Watch Video Solution

124. Write the negation of the following :

For every real number $x, x$ is less than $x+1$.

## D Watch Video Solution

125. Write the negation of the following :

There exists a real number which is equal to
its square.

## - Watch Video Solution

126. Write the negation of the following :

All the students have completed their home work.
127. Write the negation of the following statement.

Every child is naughty or intelligent.

- Watch Video Solution

128. Write the negation of the following statement.

Some diseases are curable and not infectious.
129. Identify the quantifier in the following statements and write the negation of the statements

There exists a capital for every state in india.

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130. Write the negation of the following statement.

All forms of carbon are not hard.

## - Watch Video Solution

131. Write the negation of the following statement.

All cars are not fast and sate.

## D Watch Video Solution

132. Rewrite the following statement if then in
five different ways conveying the same meaning

If a natural number is odd, then its square is also odd.
133. Write the following statement in the form
'if $p$, then $q$ ':

You get a job implies that your credentials are good.

## D Watch Video Solution

134. Write the following statement in the form
'if $p$, then $q$ ':

The Bannana tree will bloom if it stays warm for a month.

- Watch Video Solution

135. Write the following statement in the form
'if $p$, then $q$ ':

A number is even if it is a multiple of 2.

D Watch Video Solution
136. Write each of the statements in the form
if then

A quadrilateral is a paralleogram if its diagonals bisect each other.

## - Watch Video Solution

137. Write the following statement in the form
'if $p$, then $q$ ':
To pass in examination it is necessary that you work hard.
138. Write the following statement in the form
'if $p$, then $q$ ':

It is necessary to be rich in order to be happy.

## D Watch Video Solution

139. Write the following statement in the form
'if $p$, then $q$ ':

Whenever it rains it is cold.
140. Write the following statement in the form
'if $p$, then $q$ ':
You earn a living implies you work.

## D Watch Video Solution

141. Write the following statement in the form
'if $p$, then $q$ ':
The crops will be destroyed if there is a flood.
142. For the following compound statements,
first identify the corresponding component
statements. Then check whether the
statements are true or not.
If Kota is in India, then 7+7=14.

## - Watch Video Solution

143. For the following compound statements,
first identify the corresponding component statements. Then check whether the
statements are true or not.

If Kota is in England, then $7+7=14$.

## D Watch Video Solution

144. For the following compound statements, first identify the corresponding component statements. Then check whether the
statements are true or not.

If Kota is in India, then $7+7=15$.

## D Watch Video Solution

145. For the following compound statements,
first identify the corresponding component
statements. Then check whether the
statements are true or not.
If Kota is in India, then $7+7=14$.

## - Watch Video Solution

146. Let p : 'He is rich' and q : 'He is happy' be the given statements. Write the following statement in the symbolic form, using $p$ and $q$. If he is rich, then he is unhappy.

## - Watch Video Solution

147. Let p : 'He is rich' and q : 'He is happy' be the given statements. Write the following statement in the symbolic form, using $p$ and $q$. It is necessary to be happy in order to be poor.

## - Watch Video Solution

148. Let p : 'He is rich' and q : 'He is happy' be the given statements. Write the following
statement in the symbolic form, using $p$ and $q$.
To be poor is to be unhappy.

D Watch Video Solution
149. Write the contrapositive and coverse of the following :

IF x is a prime number, then x is odd.

- Watch Video Solution

150. Write the contrapositve and converse of the following statements

If the two lines are parallel, then they do not intersect in the same plane.

## - Watch Video Solution

151. Write the contrapositve and converse of the following statements

Something is cold implies that it has low temperature.
152. Write the contrapositive and converse of the following statement :

You cannot comprehend geometry if you do not know how to reason deductively.

## D Watch Video Solution

153. Write the contrapositve and converse of the following statements
$x$ is an even number implies that $x$ is divisible
by 4

## D Watch Video Solution

154. State the converse and contrapositive of the following statements
$\mathrm{p}:$ A positive interger is prime only if it has no divisors other than 1 and itself.
155. State the converse and contrapositive of the following statements
q : if it is hot outside then you feel thirsty.

## D Watch Video Solution

156. Given the following statement :

If a quadrilateral is a parallelogram, then its
diagonals bisect each other.
Identify these as contrapositive or converse of each other.
157. Given the following statement :

If the diagonals of a quadrilateral do not bisect each other, then the quadrilateral is not a parallelogram. Identify these as contrapositive or converse of each other.

## D Watch Video Solution

158. Given the following statement :

If the diagonals of a quadrilateral bisect each
other, then it is a parallelogram. Identify these as contrapositive or converse of each other.

## D Watch Video Solution

159. Rewrite each of the following statements in the form $p$ if and only if $q$
p: if you watch television then your mind is
free and if your mind is free then you watch television.
160. Rewrite each of the following statements in the form $p$ if and only if $q$
q: for you to get an A grade is necessary and sufficient that you do all the homework regularly.

## D Watch Video Solution

161. Rewrite the following statement in the
form ' $p$ if and only if $q$ '.
$r$ : If a quadrilateral is equiangular, then it is a
rectangle and if a quadrilateral is a rectangle, then it is equiangular.

## D Watch Video Solution

162. p: If a tumbler is half empty then it is half
full $q$ : if a tumbler is half full then it is half empty

Combination of these two statements is
163. Given below are pairs of statements.

Combine them using 'if and only if' :
p: if Anil is intelligent, then he scores $92 \%$. $q$ :
If Anil scores $92 \%$. then he is intelligent.

## D Watch Video Solution

164. Given below are pairs of statements.

Combine them using 'if and only if':
p: If two lines are parallel, then their slopes
are equal. q: If the slopes of two lines are equal, then they are parallel.

## - Watch Video Solution

165. Determine the truth value of the following statement:
$3+3=6$ iff $2+2=4$.

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166. Determine the truth value of the following
statement :
$3+3=6$ iff $4+3=8$.

## D Watch Video Solution

167. Determine the truth value of the following
statement :
$3+3=7$ iff $3+4=7$.

D Watch Video Solution

# 168. Determine the truth value of the following 

statement:
$3+3=7$ iff $5+2=6$.

- Watch Video Solution

169. Using the words necessary and sufficient rewrite the statement. The integer $n$ is odd if and only if $n^{2}$ is odd Also choice whether the statement is true.
