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## MATHS

# BOOKS - MODERN PUBLICATION 

## STATISTICS

## Example

1. Find the range of the series :
$75,85,95,105,115,125$.

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2. Find the range of the series:
$15,18,13,16,14,13,14,19,21$.

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3. Find the mean deviation from the mean for following the data $4,7,8,9,10,12,13,17$.

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4. Find the mean deviation from the mean for the following data : 12,3,18,17,4,9,17, 19, 20, 15, 8, 17, 2, 3, 16, 11,3,1,0,5 .
5. Calculate the mean deviation from mean for the following frequency distribution :


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6. Calculate the mean, mean deviation from mean for
the following data :
```
Class-Interval : 0-10 10-20 20-30 30-40 40-50 50-60 60-70 70-80
Frequency: 
```

7. If $\bar{x}$ is the mean and Mean Deviation from mean is
$M D(\bar{x})$, then find the number of observations lying between $\bar{x}-M D(\bar{x})$ and $\bar{x}+M D(\bar{x})$ from the following data : 22, 24, 30, 27, 29, 31, 25, 28, 41, 42.

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8. Find the mean deviation from the median for the following data: $3,9,5,3,12,10,18,4,7,19,21$.
9. The scores of a batsman in ten innings are: 55, 34, $48,38,70,44,54,46,63,42$. Find the mean deviation about the median.

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10. Find the mean deviation from the median for the following data:


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11. Calculate the mean deviation about median for the following data :


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12. Find the variance of the following data: $6,8,10,12$,

14, 16, 18, 20, 22, 24.

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13. Find the variance and standard deviation for the
following data :

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14. Calculate the mean and the standard deviation for
the following distribution:


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15. Calculate the Mean and the Standard Deviation for
the following data:

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16. Find the Standard Deviation of the following data:

## Class-Interval : 25-35 35-45 45-55 55-6565-75

## Frequency : <br> 21 <br> 20 <br> 16 <br> 25 <br> 18.

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17. Calculate the mean, variance and standard deviation
for the following distribution :
Class : $30-40$
Frequency:
F
3

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18. The measurements (in m.m.) of the diameters of the heads of 107 screws are as given below :

## Diameter

in (m.m.) : $\quad 33-35 \quad 36-38 \quad 39-41 \quad 42-44 \quad 45-47$
No. of screws : $\begin{array}{llllll}17 & 19 & 23 & 21 & 27 . & \text { Calculate }\end{array}$
the standard deviation.

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19. The mean and variance of 8 observations are 9 and 9.25 respectively. If six observations are $6,7,10,12,12$ and 13 , find the remaining two observations.

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20. The mean and standard deviation of 100 observations were calculated as 40 and 5.1 respectively by a student who took by mistake 50 instead of 40 for one observation. What are the correct mean and standard deviation?

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21. The variance of 20 observations is 5. If each observation is multiplied by 2 , find the new variance of the resulting observations.
22. The means and standard deviations of heights and weights of 50 students of a class are as follows :

## Weights Heights 63.2 kg <br> 5.6 kg <br> $63 \cdot 2$ inch <br> Standard deviation <br> 11.5 inch. <br> Which

shows more variability, heights or weights?

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23. Coefficient of variation of two distributions are 60\%
and $70 \%$ and their standard deviations are 21 and 16 respectively. What are their arithmetic means?
24. Calculate coefficient of variation for the following data :
```
Income (in Rs.) : 1000-1700 1700-2400 2400-3100 3100-3800
No, of families : 12 18 % 18
Income (in Rs.) : 3800-4500 4500 - 5200
No. of families : 35
    10.
```

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## Exercise

1. Find the mean deviation from the mean for the following data : 6,7,10,12,13,4,8,12.
2. Find the mean deviation from the mean for the following data : 6.5,5, 5.25, 5.5,4.75,4.5,6.25,7.75,8.5.

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3. Find the mean deviation from the mean for the following data : $13,15,16,15,18,15,14,18,17,10$.

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4. Find the mean deviation from the mean for the following data. 38, 70, 48, 40, 42, 55, 63, 46, 54, 44.
5. Find the mean deviation from the mean for the following data : 36, 72, 46, 42, 60, 45, 53, 46, 51, 49.

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6. Find the mean deviation from the mean for the following data : 37, 48, 50, 23, 47, 58, 29, 27, 31, 40.

## - Watch Video Solution

7. Find the mean deviation from the mean for the following data : $13,15,16,15,18,15,14,18,17,10$.

## - Watch Video Solution

8. Find the mean deviation from the mean for the
following data :


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9. Find the mean deviation from the mean for the

## following data :


10. Find the mean deviation from the mean for the following data :


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11. Find the mean deviation from the mean for the following data :

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12. Find the mean deviation from the mean for the following data :


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13. Find the mean deviation from the mean for the
following data :

| Classes : | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequencies : | 2 | 3 | 8 | 14 | 8 | 3 | 2. |

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14. Find the mean deviation from the mean for the

## following data :

| Height $(\mathrm{cm}):$ | $95-105$ | $105-115$ | $115-125$ | $125-135$ | $135-145$ | $145-155$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of Boys: | 9 | 13 | 26 | 30 | 12 | 10. |

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15. Find the mean deviation from the mean for the
following data :

| Income per day : |
| :--- |
| No. of <br> persons : |

16. If $\bar{x}$ is the mean and Mean Deviation from mean is
$M D(\bar{x})$, then find the number of observations lying between $\bar{x}-M D(\bar{x})$ and $\bar{x}+M D(\bar{x})$ from the following data : 22, 24, 30, 27, 29, 31, 25, 28, 41, 42.

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17. If $\bar{x}$ is the mean and Mean Deviation from mean is
$M D(\bar{x})$, then find the number of observations lying between $\bar{x}-M D(\bar{x})$ and $\bar{x}+M D(\bar{x})$ from the following data : 22, 24, 30, 27, 29, 31, 25, 28, 41, 42.
18. Find the mean deviation from the median for the following data : 9, 12, 18, 3, 5, 3, 10, 12, 21, 12, 21.

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19. Find the mean deviation from the median for the following data: $10,3,12,5,9,3,18,21,21,8,12,12$.

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20. Find the mean deviation from the median for the following data : 13,17, 16, 14, 11, 13, 10, 16, 11, 18, 12, 17.
21. Find the mean deviation from the mean for the following data : $36,72,46,42,60,45,53,46,51,49$.

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22. Find the mean deviation from the median for the following data : 38,70,48,34, 65, 42, 55, 44, 53, 47.

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23. Find the mean deviation from the median for the
following data :

## 6

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24. Find the mean deviation from the median for the

## following data :



## D Watch Video Solution

25. Find the mean deviation from the median for the
following data:

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26. The lengths (in cm.) of 10 rods in a shop are as below : 42.0,52.3,55.2,72.9,52.8,79.0,32.5,15.2,27.9,30.2 .

Find M.D. (Med.).

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27. The lengths (in cm.) of 10 rods in a shop are as below : 42.0,52.3,55.2,72.9,52.8,79.0,32.5,15.2,27.9,30.2

Find M.D. (Med.).

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28. Calculate the mean deviation about median age for the age distribution of 100 persons given below :


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29. Find the mean deviation about the median for the
following data :

| Marks | $:$ | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of girls $:$ | 6 | 8 | 14 | 16 | 4 | 2 |  |

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30. Find the mean deviation about the median for the following data :


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31. Find the mean deviation about the median for the

## following data :



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32. Given that $\bar{x}$ is the mean and $\sigma^{2}$ is the variance of n
observations $x_{1}, x_{2}, \ldots x_{n}$. Prove that the mean and
variance of the observations $a x_{1}, a x_{2}, \ldots, a x_{n}$, are $a \bar{x}$ and $a^{2} \sigma^{2}$ respectively $(a \neq 0)$.

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> 33. $\begin{gathered}\text { Prove } \\ \text { that }\end{gathered} \quad$ identity
> $\sum_{i=1}^{n}\left(x_{i}-\bar{x}\right)^{2}=\sum_{i=1}^{n} x_{i}^{2}-n \bar{x}^{2}=\sum_{i=1}^{n} x_{i}^{2}-\frac{\left(\sum_{i=1}^{n} x_{i}\right)^{2}}{n}$

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34. Find the mean and variance for the following data:

2, 4,5, 6, $8,17$.
35. Find the mean and variance for the following data:
$6,7,10,12,13,4,8,12$.

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36. Find the mean and variance for the following data:
first n natural numbers.

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37. Find the mean and variance for the following data :

First 10 multiples of 3.

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38. Find the variance and standard deviation for the following data :
$65,58,68,44,48,45,60,62,60,50$.

## - Watch Video Solution

39. The scores of batsman A were : $48,80,58,44,52,65$,
$73,56,64,54$. Find the variance.
40. The scores of batsman A were : $28,60,38,24,32,45$,
$53,36,44,34$. Find the variance.

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41. Find the Standard Deviation of the following data:


## D Watch Video Solution

42. Find the mean and standard deviation for the
following data :

## - Watch Video Solution

43. Find the mean and standard deviation for the following data :


## - Watch Video Solution

44. Find the mean and standard deviation for the following data :

## - Watch Video Solution

45. The scores of 10 students in a test, in which the maximum marks Were 50 as follows : $28,36,34,28,48$,

22, $35,27,19,41$. Find the Variance.

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46. Later on the maximum marks were increased to

100, and accordingly each Student's score was doubled.
Find the variance of the new scores .

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47. The scores of 48 children in an intelligence test are shown in the following :

the variance $\sigma^{2}$ and find out the percentage of children whose scores lie between $\bar{x}-\sigma$ and $\bar{x}+\sigma$.

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48. A sample of 25 variates has mean 40 and standand deviation 5 and a second sample of 35 variates has mean 45 and the standard deviation 2 . Find the mean
and standard deviation of the two samples of variates, taken together.

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49. The mean of 5 observation is 4.4 and their variance
is 8.24 . If three of the observations are 1,2 and 6 , find the other two observations

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50. The mean and variance of 7 observations are 8 and

16 respectively. If five observations are $2,4,10,12,14$, find the remaining two observations.

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51. The mean and standard deviation of 6 observations
are 8 and 4, respectively. If each observation is multiplied by 3, find the new mean and new standard deviation of the resulting observations.

## - Watch Video Solution

52. Calculate the standard deviation of the following
frequency distribution :

53. Calculate the standard deviation of the following frequency distribution :

| Marks | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ | $80-90$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of Students : | 3 | 6 | 13 | 15 | 14 | 5 | 4 . |

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54. Following is the distribution of the number of outdoor patients registered in a certain hospital in 100 days :


Find the
arithmetic mean and standard deviation.
55. Calculate the standard deviation of the following

## distribution :



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56. Calculate the mean and standard deviation for the

## following distribution :

| Class-Interval <br> Freauency | $\begin{gathered} 0-5 \\ 7 \end{gathered}$ | $\begin{gathered} 5-10 \\ 10 \end{gathered}$ | $\begin{gathered} 10-15 \\ 6 \end{gathered}$ | $\begin{gathered} 15-20 \\ 8 \end{gathered}$ | $\begin{gathered} 20-25 \\ 4 \end{gathered}$ | $\begin{gathered} 25-30 \\ 3 \end{gathered}$ | $\begin{gathered} 30-35 \\ 2 \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |

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57. Calculate the mean and standard deviation for the following distribution :

|  | $0-4$ | $4-8$ | $8-12$ | $12-16$ | $16-20$ | $20-24$ | $24-28$ | $28-32$ |  |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Class-Interval $:$ | $0-4$ | 5 | 8 | 16 | 14 | 10 | 8 | 3 |  |
| Frequency | $:$ | 2 | 5 |  |  |  |  |  | -2 |

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58. Calculate the mean and standard deviation for the
following distribution :


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59. Calculate the mean and standard deviation for the following distribution :


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60. Calculate the mean and standard deviation for the
following distribution :

| Class-Interval : | $8-10$ | $10-12$ | $12-14$ | $14-16$ | $16-18$ | $18-20$ | $20-22$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency $:$ | 8 | 10 | 18 | 30 | 12 | 10 | 2 |

61. Calculate the mean and standard deviation for the

## following distribution :



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62. In a study of patients, following data are obtained.

Find the arithmetic mean and the standard deviation of the, data :

| Age (in years | $:$ | $10-19$ | $20-29$ | $30-39$ | $40-49$ | $50-59$ | $60-69$ | $70-79$ | $80-89$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of cases | $:$ | 1 | 0 | 1 | 10 | 17 | 38 | 9 | 3. |

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63. Calculate the mean and variance of the following data:


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64. Calculate the mean and variance of the following data:

| Classes | $:$ | $0-30$ | $30-60$ | $60-90$ | $90-120$ | $120-150$ | $150-180$ | $180-210$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequencies | $:$ | 2 | 3 | 5 | 10 | 3 | 5 | 2 |

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65. Calculate the mean and variance of the following data:

| Classes | $:$ | $0-5$ | $5-10$ | $10-15$ | $15-20$ | $20-25$ | $25-30$ | $30-35$ | $35-40$ | $40-45$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequencies | $:$ | 20 | 24 | 32 | 28 | 20 | 11 | 26 | 15 | 24. |

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66. Calculate the mean and variance of the following

## distribution :

| Class-Interval : | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ | $80-90$ |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | $:$ | 3 | 61 | 132 | 153 | 140 | 51 | 2. |

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67. Calculate the mean and standard deviation of the distribution :

| Class-Interval : | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency $:$ | 15 | 17 | 19 | 27 | 19 | 12 |

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68. Calculate the mean and standard deviation of the distribution :

| Class-Interval : | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ | $80-90$ | $90-100$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | $:$ | 3 | 4 | 7 | 7 | 15 | 9 | 6 | 6 |

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69. Calculate the mean and standard deviation of the distribution :

| Class-Interval : | $10-25$ | $25-40$ | $40-55$ | $55-70$ | $70-85$ | $85-100$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency $:$ | 6 | 20 | 44 | 26 | 3 | 1 |

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70. Calculate the mean and standard deviation of the distribution :

| Class-Interval : | $20-40$ | $40-60$ | $60-80$ | $80-100$ | $100-120$ | $120-140$ | $140-160$ | $160-180$ | $180-200$ |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | $:$ | 6 | 9 | 11 | 14 | 20 | 15 | 10 | 8 | 7 |

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71. Calculate the mean and standard deviation of the distribution :


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72. Calculate the mean and standard deviation of the

## distribution:

| Age (in years) <br> Number of | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ | $80-90$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Members: | 3 | 61 | 132 | 153 | 140 | 51 | 2 |

73. Calculate the mean and standard deviation of the distribution :

| Marks | $:$ | $5-10$ | $10-15$ | $15-20$ | $20-25$ | $25-30$ | $30-35$ | $35-40$ | $40-45$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of Students : | 5 | 6 | 15 | 10 | 5 | 4 | 2 | 2. |  |

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74. Calculate the mean and standard deviation of the

## following distribution :



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75. Calculate the mean and standard deviation of the following distribution :


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76. Find the mean , variance and standard deviation :


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77. In a survey of 950 families in a village, the following distribution of children was obtained:


Find the
mean and standard deviation of the distribution.

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78. The diameters of circles (in mm ) drawn in a design
are given below :


Calculate
the standard deviation and mean diameter of the circles.
79. From the data given below, state which group is more variable :


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80. In a study to test the effectiveness of new variety of
seeds, an experiment was performed with 50 experimental fields and the following results were obtained :


Find the
variance and standard deviation.

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81. The weights of a group of children at 6 month are given below:


Find the
standard deviation.

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82. In the study of 79 diabetic patients, the following data are obtained. Find the variance and the standard deviation without finding the average (i.e. using
deviation method).

| Age at Detection <br> (in years) | No. of cases | Age at Detection <br> (in years) | No. of cases |
| :---: | :---: | :---: | :---: |
| $10-19$ | 1 | $50-59$ |  |
| $20-29$ | 0 | $60-69$ | 17 |
| $30-39$ | 1 | $70-79$ | 38 |
| $40-49$ | 10 | $80-89$ | 9 |

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83. Two plants A and B of a factory show following
results about the number of workers and the wages
paid to them :


In which
plant, A or B , is there greater variability in individual wages ?

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84. The following values are calculated in respect of heights and weights of the students of a section of class XI.

say that the weights show greater variation than the heights?
85. The sum and sum of squares corresponding to
length x (in cm ) and weight y (in plant products are
given below:
$\sum_{i=1}^{50} x_{i}=212, \sum_{i=1}^{50} x_{i}^{2}=902.8, \sum_{i=1}^{50} y_{i}=261, \sum_{i=1}^{50} y_{i}^{2}=1457.6$
Which is more varying, the lengths or weight?

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86. From the data given below, state which group is more variable, A or B ?

87. From the prices of shares $X$ and $Y$ below, find out which is more stable in value :


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88. The following is the record of goals scored by team

A in a football session.


For the
team B, mean number of goals scored per match was 2
with a standard deviation 1.25 goals. Find which team
may be considered more consistent ?
89. The mean of first 11 terms of Fibonacci sequence :
$1,1,2,3,5,8,13,21,34,55,89$ is 21.1. Calculate the standard deviation.

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90. If each of the observations $x_{1}, x_{2}, \ldots . x_{n}$ is increased by an amount ' $a$ ', where ' $a$ ' is a negative or positive number, show that the variance remains unchanged.
91. Find the mean and standard deviation for the

## following data :



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92. Find the average earnings (using step-deviation
method) and the standard deviation of the group of

432 workers from the data given ahead:


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93. The yields of wheat for 50 experimental fields are
given below. Find the average yield and hence find its
variance.


## (D) Watch Video Solution

94. The mean and standard deviation of marks
obtained by 50 students of a class in three subjects-
Mathematics, Physics and Chemistry are given below :


Which of
the three subjects shows the highest variability in marks and which shows the lowest ?

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95. From a frequency distribution consisting of 18 observations, the mean and the standard deviation were found to be 7 and 4 respectively. But on comparison with the original data, it was found that a figure 12 was miscopied as 21 in calculations. Calculate the correct mean and standard deviation.
96. The mean and standard deviation of 20
observations are found to be 10 and 2 respectively. On rechecking, it was found that an observation 8 was incorrect. Calculate the correct mean and standard deviation if wrong item is omitted.

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97. The mean and standard deviation of 20
observations are found to be 10 and 2 respectively. On
rechecking, it was found that an observation 8 was
incorrect. Calculate the correct mean and standard deviation if wrong item is omitted.
98. The mean and standard deviation of a group of 100 observations were found to be 20 and 3 respectively.

Later on it was found that three observations were incorrect, which were recorded as 21,21 and 18 . Find the mean and standard deviation if the incorrect observations were omitted.

