



MATHS

BOOKS - OMEGA PUBLICATION

RELATIONS AND FUNCTIONS

Questions

1. If $\left(\frac{x}{3} + 1, y - \frac{2}{3}\right) = \left(\frac{5}{3}, \frac{1}{3}\right)$, find the values of x and y



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2. If the set A has 3 elements and the set $B = \{3, 4, 5\}$, then find the number of elements in $(A \times B)$.

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3. If $G = \{7, 8\}$ and $H = \{5, 4, 2\}$, find $G \times H$ and $H \times G$.

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4. If $G = \{7, 8\}$ and $H = \{5, 4, 2\}$, find $G \times H$ and $H \times G$.

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5. If $A \times B = \{(a, x), (a, y), (b, x), (b, y)\}$. Find A and B.

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6. If $A = \{-1, 1\}$, find $A \times A \times A$.

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7. Let $A = \{1, 2\}$, $B = \{1, 2, 3, 4\}$, $C = \{5, 6\}$ and $D = \{5, 6, 7, 8\}$.

Verify that $A \times (B \cap C) = (A \times B) \cap (A \times C)$.

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8. Let $A = \{1, 2\}$, $B = \{1, 2, 3, 4\}$, $C = \{5, 6\}$ and $D = \{5, 6, 7, 8\}$.

Verify that $A \times C$ is a subset of $B \times D$.

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9. Let $A = \{1, 2\}$ and $B = \{3, 4\}$. Write $A \times B$. How many subsets will $A \times B$ have? List them.

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10. Let $A = \{1, 2, 3, \dots, 14\}$. Define a relation R from A to A by $R = \{(x, y) : 3x - y = 0, \text{ where } x, y \in A\}$. Write down its domain, codomain and range.

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11. $A = \{1, 2, 3, 5\}$ and $B = \{4, 6, 9\}$. Define a relation R from A to B by $R = \{(x, y) : \text{the difference between } x \text{ and } y \text{ is odd,}$

$x \in A, y \in B$. Write R in roster form.

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12. Determine the domain and range of the relation R defined by $R = \{(x, x + 5) : x \in \{0, 1, 2, 3, 4, 5\}\}$.

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13. Let $A = \{x, y, z\}$ and $B = \{1, 2\}$. Find the number of relations from A to B.

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14. Which of the following relation are function ? Given reason

$\{(2, 1), (5, 1), (8, 1), (11, 1), (14, 1), (17, 1)\}$

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15. Which of the following relations are functions? Give reasons. If it is a function, determine its domain and range.

$\{(1, 3), (1, 5), (2, 5)\}$.

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16. Find the range of $-|x|$

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17. Find the domain and range of the following real

$$\text{function:- } f(x) = \sqrt{9 - x^2}$$

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18. Find the range of the following function:-

$$f(x) = 2 - 3x, x \in R, x > 0.$$

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19. Find the range of the following function:-

$$f(x) = x^2 + 2, x \text{ is a real number.}$$

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Important Questions From Miscellaneous Exercise

1. Let $f, g : \mathbb{R} \rightarrow \mathbb{R}$ be defined, respectively by $f(x) = x + 1$, $g(x) = 2x - 3$. Find $f + g$, $f - g$ and $\frac{f}{g}$.

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2. Let $f(x) = \sqrt{x}$ and $g(x) = x$ be two functions defined over the set of non-negative real numbers. Find $(f + g)(x)$, $(f - g)(x)$, $(fg)(x)$ and $\left(\frac{f}{g}\right)(x)$.

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3. The relation 'f' is defined by $f(x) = \begin{cases} x^2 & 0 \leq x \leq 3 \\ 3x & 3 \leq x \leq 10 \end{cases}$

The relation 'g' is defined by $g(x) = \begin{cases} x^2 & 0 \leq x \leq 2 \\ 3x & 2 \leq x \leq 10 \end{cases}$

Show that 'f' is a function and 'g' is not a function.

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4. Find the domain of the function $f(x) = \frac{x^2 + 2x + 1}{x^2 - 8x + 12}$.

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5. Find the domain of the function $f(x) = \frac{x^2 + 3x + 5}{x^2 - 5x + 4}$

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6. Find the domain and the range of the real function 'f'

defined by $f(x) = \sqrt{(x - 1)}$.



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7. Find the domain and the range of the real function 'f'

defined by $f(x) = |x - 1|$.



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8. Find the domain and range of real function f defined by

$$f: R \rightarrow R \text{ such that } f = \left\{ \left(x, \frac{x^2}{1 + x^2} \right) : x \in R \right\}$$



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9. Let $f = \{(1,1), (2,3), (0,-1), (-1, -3)\}$ be a function from Z to Z defined by $f(x) = ax + b$, for some integers a, b . Determine a, b .

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10. Let R be a relation from N to N defined by $R = \{(a, b) : a, b \in N \text{ and } a = b^3\}$. Are the following true?

$(a, a) \in R$, for all $a \in N$

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11. Let R be a relation from N to N defined by $R = \{(a, b) : a, b \in N \text{ and } a = b^3\}$. Are the following

true ?

$(a, b) \in R$ implies $(b, a) \in R$

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12. Let R be a relation from N to N defined by $R = \{(a, b) : a, b \in N \text{ and } a = b^2\}$. Is the following true?
 $(a, b) \in R, (b, c) \in R$ implies $(a, c) \in R$. Justify your answer

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MCQ

1. If $A = \{2, 4, 5\}$, $B = \{7, 8, 9\}$ then $n(A \times B)$ is equal to

A. 6

B. 9

C. 3

D. 0

Answer: B



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2. If $A = \{0,1\}$ and $B = \{1,0\}$, then $A \times B$ is equal to

A. $\{0, 1, 1, 0\}$

B. $\{(0, 1), (1, 0)\}$

C. $\{0, 0\}$

D. $\{(0, 1), (0, 0), (1, 1), (1, 0)\}$

Answer: D



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3. Let $O(A) = m$, $O(B) = n$. Then the number of relations from A to B is

A. mn

B. $m + n$

C. 2^{mn}

D. 2^{m+n}

Answer: C



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4. A relation R on a set A is called an equivalence relation iff

- A. it is reflexive
- B. it is symmetric
- C. it is transitive
- D. it is reflexive, symmetric and transitive

Answer: D



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5. If r is a relation on a finite set having n elements, then the number of relation on A is

A. 2^n

B. 2^{n^2}

C. n^2

D. n^n

Answer: B



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6. Let A be a set containing 10 distinct elements. Then the total number of distinct functions from A to A is:

A. $10!$

B. 10^{10}

C. 2^{10}

D. $2^{10} - 1$

Answer: B



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7. The domain of the function

$$f(x) = \sqrt{x-1} + \sqrt{6-x} \text{ is}$$

A. $[1, \infty)$

B. $(-\infty, 6)$

C. [1,6]

D. none of these

Answer: C



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8. Find domain for $y = \frac{1}{\sqrt{|x| - x}}$.

A. $[1, \infty)$

B. $(-\infty, 0)$

C. $(-\infty, 0]$

D. $[1, \infty)$

Answer: B



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9. If the domain of the function $f(x) = x^2 - 6x + 7$ is $(-\infty, \infty)$, then the range of function is

A. (∞, ∞)

B. $[-2, \infty)$

C. $(-2, \infty)$

D. $(-\infty, -2)$

Answer: B



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10. The range of the function for real x of $y = \frac{1}{2 - \sin 3x}$ is

A. $\frac{1}{3} \leq y \leq 1$

B. $-\frac{1}{3} \leq y < 1$

C. $-\frac{1}{3} > y > 1$

D. $\frac{1}{3} > y > 1$

Answer: A



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11. The range of $f(x) = \frac{1 + x^2}{x^2}$

A. $[0,1]$

B. (0,1]

C. (1, ∞)

D. [1, ∞)

Answer: C



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12. $f(x) = \frac{|x|}{x}$, $x \neq 0$ then the value of function

A. 1

B. 0

C. -1

D. $f(x) = \begin{cases} 1, & x > 0 \\ -1, & x < 0 \end{cases}$

Answer: D



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13. If $x \neq 1$ and $f(x) = \frac{x + 1}{x - 1}$ is a real function, then

$f(f(f(2)))$ is

A. 1

B. 2

C. 3

D. 4

Answer: C



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14. If $f(x) = \frac{2x + 1}{3x - 2}$, then $(f \circ f)(2)$ is equal to

A. 1

B. 3

C. 4

D. none of these

Answer: D



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15. The relation R defined on N as

$\{(a, b) : a^2 + b^2 < 16\}$ is given by

A. $\{(1, 1), (1, 2), (1, 3), (1, 4), (1, 5)\}$

B. $\{(1, 1), (1, 2), (1, 3), (2, 3), (2, 4), (3, 2), (3, 3)\}$

C.

$\{(1, 1), (1, 2), (2, 1), (1, 3), (3, 1), (2, 2), (2, 3), (3, 2)\}$

D. none of these

Answer: C



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16.

If

$A = \{0, 1\}, B = \{1, 2\}, C = \{2, 3\}$, then $(A \times B) \cap (A \times C)$

=

A. $\{(0, 1), (1, 2)\}$

B. $\{(0, 2), (1, 3)\}$

C. $\{(1, 2), (1, 3)\}$

D. $\{(0, 2), (1, 2)\}$

Answer: D



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17. If A be an empty set and B be a finite set having n elements then the total number of mappings from A to B is

A. mn

B. n

C. 1

D. none of these

Answer: C



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18. If $f(x) = \frac{x - 1}{x + 1}$, then $f(2x)$ is

A. $\frac{f(x) + 1}{f(x) + 3}$

B. $\frac{3f(x) + 1}{f(x) + 3}$

C. $\frac{f(x) + 3}{f(x) + 1}$

D. $\frac{f(x) + 3}{3f(x) + 1}$

Answer: B



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19. The domain of definition of the function $f(x) = \log |x|$ is given by

A. $x \neq 0$

B. $x > 0$

C. $x < 0$

D. $x \in R$

Answer: D



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