



# MATHS

## BOOKS - JBD PUBLICATION

### MODEL PAPER (15)

#### Exercise

1. What is the set builder form of the set  $\{1,2,3\}$ .



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2. The range of the function  $f(x) = \frac{x+2}{|x+2|}, x \neq -2$  is:

A.  $\{-1,1\}$

B.  $\{-1,-1\}$

C.  $\{1\}$

D.  $(0, \infty)$

**Answer:**



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3. The solutions of the equation  $\sin^2 x + 3 \sin x = 0$  is:

A.  $\frac{\pi}{3}$

B.  $\frac{3\pi}{3}$

C.  $\pi$

D. none of these

**Answer:**



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4. The value of  $(2 + \sqrt{3})(2 - \sqrt{3})$  is:

A. 7

B. 3

C. -7

D. none of these

**Answer:**



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5.  $nC_r + {}^nC_{r+1} = {}^{n+1}C_x$ , then x is equal to:

A.  $2r$

B.  $\frac{r-1}{2}$

C.  $r+1$

D. none of these

**Answer:**

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6. The  $n$ th term of a G.P. is 128 and the sum of its  $n$  terms is 225. If its common ratio is 2, then its first term is:

A. 1

B. 2

C. 3

D. none of these

**Answer:**

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7. The three straight lines  $ax+by=c$ ,  $bx+cy=a$  and  $cx+ay=b$  are collinear if:

A.  $a+b-c=0$

B.  $a-b+c=0$

C.  $a+b+c=0$

D. none of these

**Answer:**



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8. If the circle  $x^2 + y^2 + 2ax + 8y + 16 = 0$  touches x axis, then the value of a is:

A.  $\pm 1$

B.  $\pm 4$

C.  $\pm 8$

D. none of these

**Answer:**



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**9.** In a single toss of three coins, the probability of getting head and tail alternatively is:

A.  $\frac{1}{4}$

B.  $\frac{1}{2}$

C.  $\frac{1}{8}$

D. none of these

**Answer:**



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10. Prove that:  $\frac{\sin x + \sin 3x}{\cos x + \cos 3x} = \tan 2x$



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11. Prove that  $\frac{\sin(x + y)}{\sin(x - y)} = \frac{\tan x + \tan y}{\tan x - \tan y}$



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12. If  $z_1 = 2 - i$ ,  $z_2 = 1 + i$ , find  $\left| \frac{z_1 + z_2 + 1}{z_1 - z_2 + 1} \right|$ .



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13. Show that  $9^{n+1} - 8n - 9$  is divisible by 64, whenever  $n$  is a positive integer.



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14. Compute  $(98)^5$



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**15.** Using distance formula, show that the points A(6,-7,1), B(2,-3,1) and C(4,-5,0) are collinear.



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**16.** Show that the statement is true by the method of contradiction. If  $x$  is an integer and  $x^2$  is even, then  $x$  is also even.



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**17.** Find the component statement of the following and check whether they are true or not.

24 is a multiple of 2,4 and 8.



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18. Prove that  $A^c - B^c = B - A$ .



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19. If  $f(x) = \log\left(\frac{x}{x-1}\right)$ , show that

$$f(x+1) + f(x) = \log\left(\frac{x+1}{x-1}\right)$$



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20. Prove that:  $\cos 15^\circ - \sin 15^\circ = \frac{1}{\sqrt{2}}$



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21. Prove that :

$$\cos 24^\circ + \cos 55^\circ + \cos 125^\circ + \cos 204^\circ + \cos 300^\circ = \frac{1}{2}$$

.



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22. How many words, with or without meaning, each of 2 vowels and 3 consonants can be formed from the letters of the word DAUGHTER ?

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**23.** Find the value of  $n$  such that :

$${}^n P_5 = 42^n P_3, n > 4.$$

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**24.** Sum of first  $p, q$  and  $r$  terms of an A.P. are  $a, b, c$  respectively. Prove that

$$\frac{a}{p}(q - r) + \frac{b}{q}(r - p) + \frac{c}{r}(p - q) = 0.$$

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25. If the angle between two lines is  $\frac{\pi}{3}$  and slope of one of the line is  $\frac{1}{4}$ . Find the slope of other line.



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26. If a parabolic reflector is 20 cm in diameter and 50 cm deep. Find the focus.



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27. Evaluate:  $\lim_{x \rightarrow 1} \frac{(x + x^2 + x^3 + \dots \dots \dots x^n) - n}{x - 1}$



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28. If  $y = a \sin x + b \cos x$ , prove that  $y^2 + \left( \frac{dy}{dx} \right)^2 = a^2 + b^2$



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29. A, B and C are three mutually exclusive and exhaustive events associated with a random experiment. Find  $P(A)$  given that  $P(B) = \frac{3}{2}P(A)$  and  $P(C) = \frac{1}{2}P(B)$ .



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30. Find  $\theta$  such that  $\frac{3 + 2i \sin \theta}{1 - 2i \sin \theta}$  is purely real.



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31. If  $a + ib = \frac{(x + i)^2}{2x^2 + 1}$ , prove that

$$a^2 + b^2 = \frac{(x^2 + 1)^2}{(2x^2 + 1)^2}.$$



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32. Solve the following system of inequalities graphically:  $4x + 3y \leq 60$ ,  $y \geq 2x$ ,  $x \geq 3$ ,  $x, y \geq 0$



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33. IQ of a person is given by the formula

$$IQ = \frac{MA}{CA} \times 100$$

, where MA is mental age and CA is



chronological age. If  $80 \leq IQ \leq 140$  for a group of 12 years old children, find the range of their mental age.



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34. Evaluate:  $\lim_{x \rightarrow 0} \frac{\sqrt{1+2x} - \sqrt{1-2x}}{x}$



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35. Find the derivative of  $\cos x$  w.r.t.  $x$



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**36.** Find the mean marks from the following data :

Marks	No. of students
Below 10	3
Below 20	5
Below 30	9
Below 40	15
Below 50	20
Below 60	26
Below 70	34
Below 80	41
Below 90	45
Below 100	47



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**37.** Find the mean deviation from the mean for the following data. 38, 70, 48, 40, 42, 55, 63, 46, 54, 44.



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