

#### **MATHS**

**BOOKS - PSEB** 

#### **LIMITS AND DERIVATIVES**

Exercise

**1.** Evaluate the following limits:-  $\lim_{x o 3} x + 3$ 



**2.** Evaluate the following limits:- 
$$\lim_{x o \pi} \left( x - rac{22}{7} 
ight)$$



**3.** Evaluate the following limits:-  $\lim_{r o 1} \, \pi r^2$ 



**4.** Evaluate the following limits:-  $\lim_{x o 4} rac{4x+3}{x-2}$ 



5. Evaluate the following limits:-

$$\lim_{x
ightarrow-1} \, rac{x^{10}+x^5+1}{x-1}$$



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6. Evaluate the following limits:-

$$\lim_{x
ightarrow 0} rac{\left(x+1
ight)^5-1}{x}$$



$$\lim_{x \to 2} \frac{3x^2 - x - 10}{x^2 - 4}$$



7. Evaluate the following limits:-

8. Evaluate the following limits:-

 $\lim_{x o 3} \ rac{x^4 - 81}{2x^2 - 5x - 3}$ 



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**9.** Evaluate the following limits:-  $\lim_{x o 0} \ \frac{ax+b}{cx+1}$ 

10. Evaluate the following limits:- 
$$\lim_{z \to 1} \frac{z^{\frac{1}{3}} - 1}{z^{\frac{1}{6}} - 1}$$



11. Evaluate the following limits:-

$$\lim_{x o 1} rac{ax^2+bx+c}{cx^2+bx+a}, a+b+c
eq 0$$



$$\lim_{x o -2} rac{rac{1}{x}+rac{1}{2}}{x+2}$$



- **13.** Evaluate the following limits:-  $\lim_{x \to 0} \frac{\sin ax}{bx}$ 
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14. Evaluate the following limits:- 
$$\lim_{x o 0} \frac{\sin ax}{\sin bx}, \, a, \, b 
eq 0$$

**15.** Evaluate the following limits:-

$$\lim_{x o\pi} \ rac{\sin(\pi-x)}{\pi(\pi-x)}$$



**16.** Evaluate the following limits:  $\lim_{x\to 0} \frac{\cos x}{\pi - x}$ 



17. Evaluate the following limits:- 
$$\lim_{x \to 0} \frac{\cos 2x - 1}{\cos x - 1}$$



**18.** Evaluate the following limits: $ax + x \cos x$  $b\sin x$  $x \rightarrow 0$ 



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**19.** Evaluate the following limits:-  $\lim_{x \to \infty} x \sec x$  $x \rightarrow 0$ 

$$\lim_{x o 0} \ rac{\sin ax + bx}{ax + \sin bx} a, b, a+b 
eq 0$$



# **21.** Evaluate the following limits:-

$$\lim_{x \to 0} (\cos ecx - \cot x)$$



$$\lim_{x o rac{\pi}{2}} \; rac{ an 2x}{x - rac{\pi}{2}}$$



**23.** Find  $\lim_{x o 0} f(x)$  and  $\lim_{x o 1} f(x)$ , where  $f(x) = \left\{ egin{array}{ll} 2x+3 & x \leq 0 \\ 3(x+1) & x > 0 \end{array} 
ight.$ 

$$f(x) = \left\{egin{array}{ll} 2x+3 & x \leq 0 \ 3(x+1) & x > 0 \end{array}
ight.$$



**24.** Find 
$$\lim_{x \to 1} f(x)$$

$$\lim_{x \to 1}$$

where

$$f(x) = \left\{ egin{array}{ll} x^2 - 1 & x \leq 1 \ -x^2 - 1 & x > 1 \end{array} 
ight.$$



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# **25.** Evaluate $\lim_{x \to 0} f(x)$ ,

where

$$f(x) = \left\{ egin{array}{ll} rac{|x|}{x} & x 
eq 0 \ 0 & x = 0 \end{array} 
ight.$$



26. Find 
$$\lim_{x\to 0} f(x)$$
,

where

$$f(x) = \left\{ egin{array}{ll} rac{x}{|x|} & x 
eq 0 \ 0 & x = 0 \end{array} 
ight.$$



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# **27.** Find $\lim_{x o 5} f(x)$ , where f(x) = |x| - 5



**28.** Suppose 
$$f(x)=\left\{egin{array}{ll} a+bx & x<1 \ 4 & x=1 \ b-ax & x>1 \end{array}
ight.$$

 $\lim_{x o 1} \, f(x) = f(1)$  what are possible values of a and b?



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**29.** Let  $a_1, a_2 \dots a_n$  be fixed real numbers and function define a  $f(x) = (x - a_1)(x - a_2)...(x - a_n).$  What is  $\lim_{x o a_1} f(x)$ ? For some  $a 
eq a_1, a_2, .... a_n$ , compute  $\lim_{x \to a} f(x)$ .

**30.** If 
$$f(x)=\left\{egin{array}{ll} |x|+1 & x<0 \ 0 & x=0 \ |x|-1 & x>0 \end{array}
ight.$$

value (s) of a does  $\lim_{x \to a} f(x)$  exists?



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**31.** If the function f(x) satisfies  $\lim_{x o 1} rac{f(x)-2}{x^2-1} = \pi$ , evaluate  $\lim_{x o 1} f(x)$ .



**32.** If 
$$f(x)=egin{cases} mx^2+n & x<0 \ nx+m & 0\leq x\leq 1 \ nx^3+m & x>1 \end{cases}$$
 . For

what integers m and n does both  $\lim_{x o 0} f(x)$ 

and  $\lim_{x \to 1} f(x)$  exist?



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**33.** Find the derivative of  $x^2 - 2$  at x = 10.



**34.** Find the derivative of 99x at x = 100.



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35. Find the derivative of x at x = 1.



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36. Find the derivative of the following function from first principle:-  $x^3-27$ 



**37.** Find the derivative of the following function from first principle:- (x-1)(x-2)



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**38.** Find the derivative of the following function from first principle:-  $\frac{1}{x^2}$ 



**39.** Find the derivative of the following function from first principle:-  $\frac{x+1}{x-1}$ 



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**40.** For the function

$$f(x) = rac{x^{100}}{100} + rac{x^{99}}{99} + ... + rac{x^2}{2} + x + 1.$$

Prove that f'(1) = 100f'(0).



**41.** Find the derivative of

$$x^{n} + ax^{n-1} + a^{2}x^{n-2} + \ldots + a^{n-1}x + a^{n}$$

for some fixed real number a.



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**42.** For some constants a and b, find the derivative of (x-a)(x-b)



**43.** For some constants a and b, find the derivative of  $\left(ax^2+b\right)^2$ 



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44. For some constants a and b, find the derivative of  $\frac{x-a}{x-b}$ 



**45.** Find the derivative of  $\frac{x^n - a^n}{x - a}$  for some constant a.

**47.** Find the derivative of:-



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**46.** Find the derivative of:-  $2x-\frac{3}{4}$ 



$$\big(5x^3+3x-1\big)(x-1)$$



**48.** Find the derivative of:- 
$$x^{-3}(5+3x)$$

**49.** Find the derivative of:-  $x^5(3-6x^{-9})$ 

**50.** Find the derivative of:-  $x^{-4}(3-4x^{-5})$ 





**51.** Find the derivative of:- 
$$\dfrac{2}{x+1}-\dfrac{x^2}{3x-1}$$



**52.** Find the derivative of cos x from first principle.



**53.** Find the derivative of the following function:  $\sin x \cos x$ 



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**54.** Find the derivative of the following function:  $5 \sec x + 4 \cos x$ 



**55.** Find the derivative of the following



function:  $\cos ecx$ 

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**56.** Find the derivative of the following function:  $3 \cot x + 5 \cos ecx$ 



**57.** Find the derivative of the following

function:  $5\sin x - 6\cos x + 7$ 



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**58.** Find the derivative of the following function:  $2 \tan x - 7 \sec x$ 



**59.** Find the derivative of the following function from first principle: -x



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**60.** Find the derivative of the following function from first principle:  $(-x)^{-1}$ 



**61.** Find the derivative of the following function from first principle:  $\sin(x+1)$ 



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**62.** Find the derivative of the following function from first principle:  $\cos\left(x-\frac{\pi}{8}\right)$ 



**63.** Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers): (x + a)



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**64.** Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers):  $(px + q)\left(\frac{r}{x} + s\right)$ 

**65.** Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers):  $(ax + b)(cx + d)^2$ 



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**66.** Find the derivative of the following function (it is to be understood that a, b, c,

d,p, q, r and s are fixed non-zero constants and m and n are integers):  $\dfrac{ax+b}{cx+d}$ 



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**67.** Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers):  $\frac{1+\frac{1}{x}}{1-\frac{1}{x}}$ 



**68.** Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers):  $\frac{1}{ax^2 + bx + c}$ 



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**69.** Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers):  $\frac{ax+b}{px^2+qx+r}$ 

**70.** Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers):  $\frac{px^2+qx+r}{ax+b}$ 



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**71.** Find the derivative of the following function (it is to be understood that a, b, c,

d,p, q, r and s are fixed non-zero constants and m and n are integers):  $\frac{a}{x^4} - \frac{b}{x^2} + \cos x$ 



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72. Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers):  $4\sqrt{x}-2$ 



**73.** Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers):  $(ax + b)^n$ 



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**74.** Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers):  $(ax + b)^n (cx + d)^m$ 

**75.** Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers):  $\sin(x + a)$ 



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**76.** Find the derivative of the following function (it is to be understood that a, b, c,

d,p, q, r and s are fixed non-zero constants and m and n are integers):  $\cos ecx \cot x$ 



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77. Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers):  $\frac{\cos x}{1+\sin x}$ 



**78.** Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers):  $\frac{\sin x + \cos x}{\sin x - \cos x}$ 



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**79.** Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers):  $\frac{\sec x - 1}{\sec x + 1}$ 

**80.** Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers):  $\sin^n x$ 



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**81.** Find the derivative of the following function (it is to be understood that a, b, c,

d,p, q, r and s are fixed non-zero constants and m and n are integers):  $\frac{a + b \sin x}{c + d \cos x}$ 



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82. Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers):  $\frac{\sin(x+a)}{a}$ 



**83.** Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers):  $x^4(5\sin x - 3\cos x)$ 



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**84.** Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers):  $(x^2 + 1)\cos x$ 

**85.** Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers):  $(ax^2 + \sin x)(p + q\cos x)$ 



**86.** Find the derivative of the following function (it is to be understood that a, b, c,

d,p, q, r and s are fixed non-zero constants and m and n are integers):  $(x + \cos x)(x - \tan x)$ 



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87. Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers):  $\frac{4x + 5\sin x}{3x + 7\cos x}$ 



88. Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers):  $\frac{x^2\cos\left(\frac{\pi}{4}\right)}{\sin x}$ 



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89. Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers):  $\frac{x}{1+\tan x}$ 

**90.** Find the derivative of the following function (it is to be understood that a, b, c, d,p, q, r and s are fixed non-zero constants and m and n are integers):  $(x + \sec x)(x - \tan x)$ 



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**91.** Find the derivative of the following function (it is to be understood that a, b, c,

d,p, q, r and s are fixed non-zero constants and

m and n are integers):  $\frac{x}{\sin^n x}$ 

