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## MATHS

## BOOKS - PSEB

## STRAIGHT LINES

Exercise

1. Draw a quadrilateral in the Cartesian plane,
whose vertices are (-4,5), (0, 7), (5,-5) and (-4,
-2). Also, find the area.
2. The base of an equilateral triangle with side

2a lies along the $y$-axis such that the mid-point of the base is at the origin. Find vertices of the triangle.

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3. Find the distance between $\mathrm{P}\left(x_{1}, y_{1}\right)$ and Q
$\left(x_{2}, y_{2}\right)$ when : (i) PQ is parallel to the y -axis,
(ii) $P Q$ is parallel to the $x$-axis.

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4. Find $a$ point on the $x$-axis, which is equidistant from the points $(7,6)$ and $(3,4)$.

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5. Find the slope of a line, which passes
through the origin, and the mid-point of the
line segment joining the points $P(0,-4)$ and $B$ $(8,0)$.

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6. Without using the Pythagoras theorem, show that the points $(4,4),(3,5)$ and $(-1,1)$ are the vertices of a right angled triangle.

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7. Find the slope of the line, which makes an angle of $30^{\circ}$ with the positive direction of $y$ axis measured anticlockwise.

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8. Find the value of x for which the points ( x ,
$-1),(2,1)$ and $(4,5)$ are collinear.

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9. Without using distance formula, show that
points $(-2,-1),(4,0),(3,3)$ and $(-3,2)$ are the vertices of a parallelogram.

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10. Find the angle between the $x$-axis and the
line joining the points ( $3,-1$ ) and (4,-2).

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11. The slope of a line is double of the slope of another line. If tangent of the angle between
them is $\frac{1}{3}$, find the slopes of the lines.

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12. A line passes through $\left(x_{1}, y_{1}\right)$ and ( $\mathrm{h}, \mathrm{k}$ ). If
slope of line is $m$, show that
$k-y_{1}=m\left(h-x_{1}\right)$.
13. If three points $(h, 0),(a, b)$ and $(0, k)$ lies on
a line, show that $\frac{a}{h}+\frac{b}{k}=1$

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14. In the following, find the equation of the line which satisfy the given conditions: Passing
through the point $(-4,3)$ with slope $\frac{1}{2}$.

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15. In the following, find the equation of the
line which satisfy the given conditions: Passing through $(0,0)$ with slope $m$.

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16. In the following, find the equation of the
line which satisfy the given conditions: Passing through $(2,2 \sqrt{3})$ and inclined with the x-axis at an angle of $75^{\circ}$.
17. In the following, find the equation of the line which satisfy the given conditions: Intersecting the $x$-axis at a distance of 3 units to the left of origin with slope -2 .

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18. In the following, find the equation of the line which satisfy the given conditions: Intersecting the $y$-axis at a distance of 2 units
above the origin and making an angle of $30^{\circ}$ with positive direction of the $x$-axis.

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19. In the following, find the equation of the line which satisfy the given conditions: Passing through the points ( $-1,1$ ) and ( $2,-4$ ).

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20. In the following, find the equation of the line which satisfy the given conditions:

Perpendicular distance from the origin is 5 units and the angle made by the perpendicular with the positive $x$-axis is $30^{\circ}$.

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21. The vertices of $\triangle P Q R$ are $\mathrm{P}(2,1), \mathrm{Q}(-2,3)$
and $R(4,5)$. Find equation of the median through the vertex R .
22. Find the equation of the line passing through $(-3,5)$ and perpendicular to the line through the points $(2,5)$ and $(-3,6)$.

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23. A line perpendicular to the line segment joining the points $(1,0)$ and $(2,3)$ divides it in the ratio $1: n$. Find the equation of the line.
24. Find the equation of a line that cuts off equal intercepts on the coordinate axis and passes through the point $(2,3)$.

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25. Find equation of line passing through the point $(2,2)$ and cutting off intercepts on the axes whose sum is 9 .
26. Find equation of the line through the point
$(0,2)$ making an angle $\frac{2 \pi}{3}$ with the positive $x$ axis. Also, find the equation of line parallel to it and crossing the $y$-axis at a distance of 2 units below the origin.

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27. The perpendicular from the origin to a line meets it at the point $(-2,9)$, find the equation of the line.

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28. The length $L$ (in centimetre) of a copper rod is a linear function of its Celsius temperature C . In an experiment, if $\mathrm{L}=124.942$ when $\mathrm{C}=20$ and $\mathrm{L}=125.134$ when $\mathrm{C}=110$, express L in terms of C .
29. The owner of a milk store finds that, he can sell 980 litres of milk each week at Rs $14 /$ litre and 1220 litres of milk each week at Rs $16 /$ litre.

Assuming a linear relationship between selling price and demand, how many litres could he sell weekly at Rs 17/litre?

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30. $P(a, b)$ is the mid-point of a line segment between axis. Show' that equation of the line
is $\frac{x}{a}+\frac{y}{b}=2$.

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31. Point $R$ (h, k) divides a line segment between the axes in the ratio 1:2. Find equation of the line.

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32. By using the concept of equation of a line,
prove that the three points $(3,0),(-2,-2)$ and
$(8,2)$ are collinear.

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33. Reduce the following equation into slope intercept form and find their slopes and the $y$ -intercepts.:- $x+7 y=0$

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34. Reduce the following equation into slope intercept form and find their slopes and the $y$ -
intercepts.:- $6 x+3 y-5=0$

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35. Reduce the following equation into slope intercept form and find their slopes and the $y$ -intercepts.:- $y=0$.

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36. Reduce the following equation into
intercept form and find their intercepts on the
axes.:- $3 x+2 y-12=0$

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37. Reduce the following equation into intercept form and find their intercepts on the axes.:- $4 x-3 y=6$

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38. Reduce the following equation into
intercept form and find their intercepts on the
axes.:- $3 y+2=0$.

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39. Reduce the following equation into normal
form. Find their perpendicular distances from
the origin and angle between perpendicular and the positive x -axis.:- $x-\sqrt{3} y+8=0$

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40. Reduce the following equation into normal
form. Find their perpendicular distances from
the origin and angle between perpendicular and the positive $x$-axis.:- $y-2=0$,

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41. Reduce the following equation into normal
form. Find their perpendicular distances from
the origin and angle between perpendicular and the positive $x$-axis.:- $x-y=4$.
42. Find the distance of the point $(-1,1)$ from the line $12(x+6)=5(y-2)$.

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43. Find the points on the $x$-axis, whose distances from the line $\frac{x}{3}+\frac{y}{4}=1$ are 4 units.
44. Find the distance between parallel lines:$15 x+8 y-34=0$ and $15 x+8 y+31=0$

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45. Find the distance between parallel lines:-
$l(x+y)+p=0$ and $l(x+y)-r=0$.

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46. Find equation of the line parallel to the
line $3 x-4 y+2=0$ and passing through the point ( $-2,3$ ).

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47. Find equation of the line perpendicular to
the line $x-7 y+5=0$ and having x intercept 3.

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48. Find angles between the lines $\sqrt{3} x+y=1$ and $x+\sqrt{3} y=1$.

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49. The line through the points (h,3) and (4, 1)
intersects the line $7 x-9 y-19=0$ at right angle. Find the value of $h$.

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50. Prove that the line through the point
$\left(x_{1}, y_{1}\right)$ and parallel to the line
$A x+B y+C=0$
$A\left(x-x_{1}\right)+B\left(y-y_{1}\right)=0$.

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51. Two lines passing through the point $(2,3)$ intersects each other at an angle of $60^{\circ}$. If slope of one line is 2 , find equation of the other line.
52. Find the equation of the right bisector of the line segment joining the points $(3,4)$ and $(-1,2)$.

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53. Find the coordinates of the foot of perpendicular from the point $(-1,3)$ to the line $3 x-4 y-16=0$.
54. The perpendicular from the origin to the line $y=m x+c$ meets it at the point $(-1,2)$.

Find the values of $m$ and $c$.

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55. If $p$ and $q$ are the lengths of perpendiculars
from the origin to the lines
$x \cos \theta-y \sin \theta=k \cos 2 \theta$
$x \sec \theta+y \cos e c \theta=k, \quad$ respectively, prove
that $p^{2}+4 q^{2}=k^{2}$.

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56. In the triangle $A B C$ with vertices $A(2,3), B$
$(4,-1)$ and $C(1,2)$, find the equation and length of altitude from the vertex $A$.

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57. If $p$ is the length of perpendicular from the origin to the line whose intercepts on the axes are a and b , then show that $\frac{1}{p^{2}}=\frac{1}{a^{2}}+\frac{1}{b^{2}}$.

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58. Find the values of $k$ for which the line
$(k-3) x-\left(4-k^{2}\right) y+k^{2}-7 k+6=0 \quad$ is
Parallel to the $x$-axis.

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59. Find the values of $k$ for which the line
$(k-3) x-\left(4-k^{2}\right) y+k^{2}-7 k+6=0 \quad$ is
Parallel to the $y$-axis.

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60. Find the values of $k$ for which the line
$(k-3) x-\left(4-k^{2}\right) y+k^{2}-7 k+6=0 \quad$ is
Passing through the origin.

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61. Find the values of $\theta$ and $p$, if the equation
$x \cos \theta+y \sin \theta=p$ is the normal form of the line $\sqrt{3} x+y+2=0$.

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62. Find the equations of the lines, which cutoff intercepts on the axes whose sum and product are 1 and -6 , respectively.

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63. What are the points on the $y$-axis whose distance from the line $\frac{x}{3}+\frac{y}{4}=1$ is 4 units.

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64. Find perpendicular distance from the origin to the line joining the points $(\cos \theta, \sin \theta)$ and $(\cos \phi, \sin \phi)$.

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65. Find the equation of the line parallel to $y$ axis and drawn through the point of intersection of the lines $x-7 y+5=0$ and $3 x+y=0$.

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66. Find the equation of a line drawn perpendicular to the line $\frac{x}{4}+\frac{y}{6}=1$ through the point, where it meets the $y$-axis.
67. Find the area of the triangle formed by the
lines $y-x=0, x+y=0$ and $x-k=0$.

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68. Find the value of $p$ so that the three lines
$3 x+y-2=0, p x+2 y-3=0 \quad$ and
$2 x-y-3=0$ may intersect at one point.
69. If three lines whose equations are

$$
y=m_{1} x+c_{1}, \quad y=m_{2} x+c_{2} \quad \text { and }
$$

$y=m_{3} x+c_{3}$ are concurrent, then show that $m_{1}\left(c_{2}-c_{3}\right)+m_{2}\left(c_{3}-c_{1}\right)+m_{3}\left(c_{1}-c_{2}\right)=0$

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70. Find the equation of the lines through the point $(3,2)$ which make an angle of $45^{\circ}$ with the line $x-2 y=3$.
71. Find the equation of the line passing through the point of intersection of the lines
$4 x+7 y-3=0$ and $2 x-3 y+1=0$ that has equal intercepts on the axes.

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72. Show that the equation of the line passing
through the origin and making an angle $\theta$ with
the line $y=m x+c$ is $\frac{y}{x}=\frac{m \pm \tan \theta}{1+m \tan \theta}$.
73. In what ratio, the line joining $(-1,1)$ and ( 5 ,
7) is divided by the line $x+y=4$ ?

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74. Find the distance of the line
$4 x+7 y+5=0$ from the point $(1,2)$ along the line $2 x-y=0$.
75. Find the direction in which a straight line must be drawn through the point $(-1,2)$ so that its point of intersection with the line $x+y=$ 4 may be at a distance of 3 units from this point.

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76. The hypotenuse of a right angled triangle has its ends at the points $(1,3)$ and $(-4,1)$. Find
an equation of the legs (perpendicular sides) of the triangle.

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77. Find the image of the point $(3,8)$ with respect to the line $x+3 y=7$ assuming the line to be a plane mirror.

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78. If the lines $y=3 x+1$ and $2 y=x+3$ are equally inclined to the line $y=m x+4$, find the value of $m$.

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79. If sum of the perpendicular distances of a
variable point $P(x, y)$ from the lines
$x+y-5=0$ and $3 x-2 y+7=0$ is always
80. Show that P must move on a line.
81. Find equation of the line which is equidistant from parallel lines
$9 x+6 y-7=0$ and $3 x+2 y+6=0$.

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81. A ray of light passing through the point (1,
2) reflects on the $x$-axis at point $A$ and the reflected ray passes through the point (5, 3).

Find the coordinates of $A$.
82. Prove that the product of the lengths of the perpendiculars drawn from the points
$\left(\sqrt{a^{2}-b^{2}}, 0\right)$ and $\left(-\sqrt{a^{2}-b^{2}}, 0\right)$ to the
line $\frac{x}{a} \cos \theta+\frac{y}{b} \sin \theta=1$ is $b^{2}$.

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83. A person standing at the junction
(crossing) of two straight paths represented
by the equations $2 x-3 y+4=0$ and
$3 x+4 y-5=0$ wants to reach the path whose equation is $6 x-7 y+8=0$ in the least time. Find equation of the path that he should follow.

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