



MATHS

NCERT - FULL MARKS MATHEMATICS(TAMIL)

SETS, RELATIONS AND FUNCTIONS

Example

1. Find the number of subsets of A if

$$A = \{(x : x = 4n + 1, 2 \leq n \leq 5, n \in \mathbb{N})\}.$$

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2. In a survey of 5000 persons in a town, it was found that 45% of the persons know language A, 25% know language B, 10% know Language C, 5% know Language A and B, 4% know Languages Band C, and 4% now

Languages A and C. If 3% of the persons know all the three Languages

find the number of persons who knows only Language A.

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3. Prove that

$$((A \cup B' \cup C) \cap (A \cap B' \cap C')) \cup ((A \cup B \cup C') \cap (B' \cap C'')) = B'$$

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4. If $X = \{1, 2, 3, \dots, 10\}$ and $A = \{1, 2, 3, 4, 5\}$ find the number of sets $B \subseteq X$ such that $A - B = \{4\}$.

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5. If A and B are two sets so that $n(B - A) = 2n(A - B) = 4n(A \cap B)$ and if $n(A \cup B) = 14$, then find $n(\mathcal{P}(A))$.

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6. Two sets have m and k elements. If the total number of subsets of the first set is 112 more than that of the second set, find the values of m and k .

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7. If $n(A) = 10$ and $n(A \cap B) = 3$ find $n((A \cap B)' \cap A)$

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8. If $A = \{1, 2, 3, 4\}$ and $B = \{3, 4, 5, 6\}$ find $n((A \cup B) \times (A \cap B) \times (A \Delta B))$.

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9. If $\mathcal{P}(A)$ denotes the power set of A then find $n(\mathcal{P}(\mathcal{P}(\mathcal{P}(\emptyset))))$.

10. Check the relation $R = \{(1, 1), (2, 2), (3, 3), \dots, (n, n)\}$ defined on the set $S = \{1, 2, 3, \dots, n\}$ for the three basic relations.

11. Let $S = \{1, 2, 3\}$ and $\rho = \{(1, 1), (1, 2), (2, 2), (1, 3), (3, 1)\}$.

(i) Is ρ reflexive? If not, state the reason and write the minimum set of ordered pairs to be included to ρ so as to make it reflexive.

(ii) Is ρ symmetric? If not, state the reason, write minimum number of ordered pairs to be included to ρ so as to make it symmetric and write minimum number of ordered pairs to be deleted from ρ so as to make it symmetric.

(iii) Is ρ transitive? If not, state the reason, write minimum number of ordered pairs to be included to ρ so as to make it transitive and write minimum number of ordered pairs to be deleted from ρ so as to make it transitive.

(iv) Is ρ an equivalence relation? If not, write the minimum ordered pairs to be included to ρ so as to make it an equivalence relation.

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12. Let $A = \{0, 1, 2, 3\}$. Construct relations on A of the following types:
not reflexive, not symmetric, not transitive

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13. Let $A = \{0, 1, 2, 3\}$. Construct relations on A of the following types:
not reflexive, not symmetric, transitive

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14. Let $A = \{0, 1, 2, 3\}$. Construct relations on A of the following types:
not reflexive, symmetric, not transitive

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15. Let $A = \{0, 1, 2, 3\}$. Construct relations on A of the following types:
not reflexive, symmetric, transitive



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16. Let $A = \{0, 1, 2, 3\}$. Construct relations on A of the following types:
reflexive, not symmetric, not transitive



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17. Let $A = \{0, 1, 2, 3\}$. Construct relations on A of the following types:
reflexive, not symmetric, transitive



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18. Let $A = \{0, 1, 2, 3\}$. Construct relations on A of the following types:
reflexive, symmetric, non transitive

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19. In the set \mathbb{Z} of integers, define $m R n$ if $m-n$ is multiple of 12. Prove that R is an equivalence relation.

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20. Check whether of the following functions are one to one and onto.

(i) $f: \mathbb{N} \rightarrow \mathbb{N}$ defined $f(n) = n + 2$

(ii) $f: \mathbb{N} \cup \{-1, 0\} \rightarrow \mathbb{N}$ defined by $f(n) = n + 2$.

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21. Check the following functions for one to oneness and onto ness and ontoneess.

(i) $f: \mathbb{N} \rightarrow \mathbb{N}$ defined by $f(n) = n^2$

(ii) $f: \mathbb{R} \rightarrow \mathbb{R}$ defined by $f(n) = n^2$

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22. Check whether the following for one to one ness and ontoneess.

(i) $f: \mathbb{R} \rightarrow \mathbb{R}$ defined by $f(x) = \frac{1}{x}$

(ii) $f: \mathbb{R} - \{0\} \rightarrow \mathbb{R}$ defined by $f(x) = \frac{1}{x}$

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23. If $f: \mathbb{R} - \{-1, 1\} \rightarrow \mathbb{R}$ is defined by $f(x) = \frac{x}{x^2 - 1}$, verify whether f is one to one or nto.

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24. If $f: R \rightarrow R$ is defined as $f(x) = 2x^2 - 1$ find the pre images of 17,4 and -2.



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25. If $f: [-2, 2] \rightarrow B$ is given by $f(x) = 2x^3$ then find B so that f is onto.



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26. Check whether the function $f(x) = x|x|$ defined on $[-2, 2]$ is one to one or not. If it is one to one find a suitable co domain so that the function becomes a bijection.



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27. Find the largest possible domain for the real valued function f defined by $f(x) = \sqrt{x^2 - 5x + 6}$



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28. Find the domain of $f(x) = \frac{1}{1 - 2 \cos x}$



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29. Find the range of the function $f(x) = \frac{1}{1 - 3 \cos x}$



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30. Find the largest possible domain for the real valued function given by

$$f(x) = \frac{\sqrt{9 - x^2}}{\sqrt{x^2 - 1}}$$



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31. Let $f = \{(1, 2), (3, 4), (2, 2)\}$ and $g = \{(2, 1), (3, 1), (4, 2)\}$ Find $g \circ f$ and $f \circ g$.



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32. Let $f = \{(1, 4), (2, 5), (3, 5)\}$ and $g = \{(4, 1), (5, 2), (6, 4)\}$. Find $g \circ f$. Can you find $f \circ g$?



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33. Let f and g be the two functions from \mathbb{R} to \mathbb{R} defined by $f(x) = 3x - 4$ and $g(x) = x^2 + 3$. Find $g \circ f$ and $f \circ g$



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34. Show that the statement.

if f and g of are one to one then $g \circ f$ is one to one is not true.



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35. Let $f, g: \mathbb{R} \rightarrow \mathbb{R}$ be defined as $f(x) = 2x - |x|$ and $g(x) = 2x + |x|$.

Find $f \circ g$.

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36. If $f: \mathbb{R} \rightarrow \mathbb{R}$ is defined by $f(x) = 2x - 3$ prove that f is a bijection and find its inverse.

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Exercise 1 1

1. Write the following in roster form.

$$\{x \in \mathbb{N} : x^2 < 121 \text{ and } x \text{ is a prime}\}$$

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2. Write the following in roster form.

the set of all positive roots of the equation $(x - 1)(x + 1)(x^2 - 1) = 0$



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3. Write the following in roster form.

$$\{x \in \mathbb{N} : 4 \times 9 < 53\}$$



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4. Write the following in roster form.

$$\left\{ x : \frac{x - 4}{x + 2} = 3, x \in \mathbb{R} - \{-2\} \right\}$$



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5. Write the set $\{-1,1\}$ in set builder form.



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6. State whether the following sets are finite or infinite.

$\{x \in \mathbb{N} : x \text{ is an even prime number}\}$



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7. State whether the following sets are finite or infinite.

$\{x \in \mathbb{N} : x \text{ is an odd prime number}\}$



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8. State whether the following sets are finite or infinite.

$\{x \in \mathbb{Z} : x \text{ is even and less than } 10\}$



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9. State whether the following sets are finite or infinite.

$\{x \in \mathbb{R} : x \text{ is rational number}\}$

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10. State whether the following sets are finite or infinite.

$\{x \in \mathbb{N} : x \text{ is rational number}\}$

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11. Justify the trueness of the statement

An element of a set can never be a subset of itself.

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12. If $n(A \cap B) = 3$ and $n(A \cup B) = 10$, then find $n(\mathcal{P}(A \Delta B))$

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13. For a set A , $A \times A$ contains 16 elements and two of its elements are $(1,3)$ and $(0,2)$. Find the element of A .



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14. Let A and B be two such that $n(A) = 3$ and $n(B) = 2$. If $(x, 1)$, $(y, 2)$, $(z, 1)$ are in $A \times B$, find A and B where x, y, z are distinct elements.



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15. If $A \times A$ has 16 elements $A = \{(a, b) \in A \times A : a < b\}$, $(-1, 2)$ and $(0,1)$ are two elements of S , then find the remaining element of S .



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1. Discuss the following relations for reflexivity, symmetricity and transitivity:

The relation R defined on the set of all positive integers by mRn if m divides n .



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2. Discuss the following relations for reflexivity, symmetricity and transitivity:

Let P denote the set of all straight lines in a plane. The relation R defined by lRm if l is perpendicular to m .



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3. Discuss the following relations for reflexivity, symmetricity and transitivity:

let A be the consisting of all the members of a family. The relation R defined by aRb if a is not a sister of b .



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4. Discuss the following relations for reflexivity, symmetricity and transitivity:

Let A be the set consisting of all the female members of a family. The relation R defined by aRb if a is not a sister of b .



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5. Discuss the following relations for reflexivity, symmetricity and transitivity:

On the set of natural numbers the relation R defined by xRy if $x + 2y = 1$.



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6. Let $X = \{a, b, c, d\}$ and $R = \{(a, a), (b, b), (a, c)\}$. Write down the minimum number of ordered pairs to be included to R to make it

(i) reflexive (ii) symmetric (iii) transitive (iv) equivalence



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7. Let $A = \{a, b, c\}$ and $R = \{(a, a), (b, b), (a, c)\}$. Write down the minimum number of ordered pairs to be included to R to make it

(i) reflexive (ii) symmetric (iii) transitive (iv) equivalence



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8. On the set of natural numbers let R be the relation defined by $a R b$ if $2a + 3b = 30$. Write down the relation by listing all the pairs. Check whether it is

(i) reflexive (ii) symmetric (iii) transitive (iv) equivalence



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9. On the set of natural numbers let R be the relation defined by aRb if $a + b \leq 6$. Write down the relation by listing all the pairs. Check whether it is

(i) reflexive (ii) symmetric (iii) transitive (iv) equivalence



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10. Let $A = \{a, b, c\}$. What is the equivalence relation of smallest cardinality of A ? What is the equivalence relation of largest cardinality on A ?



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Exercise 13

1. Suppose that 120 are studying in 4 sections of eleventh standard in a school. Let A denote the set of students and B denote the set of the sections. Define a relation from A to B as x related to y if the student x

belongs to the section y. Is this relation a function? What can you say about the inverse relation. Explain your answer.



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2. Write the values of at -4,1,-2,7,0 if

$$f(x) = \begin{cases} -x + 4 & \text{if } -\infty < x \leq -3 \\ x + 4 & \text{if } -3 < x < -2 \\ x^2 - x & \text{if } -2 \leq x < 1 \\ x - x^2 & \text{if } 1 \leq x < 7 \\ 0 & \text{otherwise} \end{cases}$$



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3. Write the values of f at -3,5,2-1,0 if

$$f(x) = \begin{cases} x^2 + x - 5 & \text{if } x \in (-\infty, 0) \\ x^2 + 3x - 2 & \text{if } x \in (3, \infty) \\ x^2 & \text{if } x \in (0, 2) \\ x^2 - 3 & \text{otherwise} \end{cases}$$



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4. State whether the following relations are functions or not. If it is a function check for one to oneness and onto-ness. If it is not a function, state why?

(i) If $A = \{a, b, c\}$ and $f = \{(a, c), (b, c), (c, b)\}$, $(f: A \rightarrow A)$

(ii) If $X = \{x, y, z\}$ and $f = \{(x, y), (x, z), (z, x)\}$, $(f: X \rightarrow X)$



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5. Let $A = \{1, 2, 3, 4\}$ and $B = \{a, b, c, d\}$. Give a function from $A \rightarrow B$ for each of the following:

(i) neither one to one nor onto



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6. Let $A = \{1, 2, 3, 4\}$ and $B = \{a, b, c, d\}$. Give a function from $A \rightarrow B$ for each of the following:

not one to one but onto.



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7. Let $A = \{1, 2, 3, 4\}$ and $B = \{a, b, c, d\}$. Give a function from $A \rightarrow B$

for each of the following:

one to one but not onto.

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8. Let $A = \{1, 2, 3, 4\}$ and $B = \{a, b, c, d\}$. Give a function from $A \rightarrow B$

for each of the following:

one to one and onto.

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9. Find the domain of $\frac{1}{1 - 2 \sin x}$

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10. Find the largest possible domain of the real valued function

$$f(x) = \frac{\sqrt{4 - x^2}}{\sqrt{x^2 - 9}}$$



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11. Find the range of the function $\frac{1}{2 \cos x - 1}$



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12. Show that the relation $xy = -2$ is a function for a suitable domain.

Find the domain and the range of the function.



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13. If $f, g: R \rightarrow R$ are defined by $f(x) = |x| + x$ and $g(x) = |x| - x$

find $g \circ f$ and $f \circ g$.



[View Text Solution](#)

14. If $f: \mathbb{R} \rightarrow \mathbb{R}$ is defined by $f(x) = 3x - 5$, prove that f is a bijection and find its inverse.



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15. The weight of the muscles of a man is a function of his body weight x and can be expressed as $W(x) = 0.35x$. Determine the domain of this function.



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16. The total cost of airfare on a given route is comprised of the base cost C and the fuel surcharge S in rupee. Both C and S are functions of the mileage m , $C(m) = 0.4m + 5$ and $S(m) = 0.03m$. Determine a function for the total cost of a ticket in terms of the mileage and find the airfare for flying 1600 miles.



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17. A sales person whose annual earnings can be represented by the function $A(x) = 30,000 + 0.4x$, where x is the rupee value of the merchandise he sells. His son is also in sales and his earnings are represented by the function $S(x) = 25,000 + 0.05x$. Find $(A + S)(x)$ and determine the total family income if they each sell Rupees 1,50,00,000 worth of merchandise.

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18. The function for exchanging American dollars for Singapore Dollar on a given day is $f(x) = 1.23x$, where x represents the number of American dollars. On the same day the function for exchanging Singapore Dollar to Indian Rupee is $g(y) = 50.50y$, where y represents the number of Singapore dollars. Write a function which will give exchange rate of American dollars in terms of Indian rupee.

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19. The owner of a small restaurant can prepare a particular meal at a cost of Rupees 100. He estimates that if the menu price of the meal is x rupees, then the number of customers who will order that meal at that price in an evening is given by the function $D(x) = 200 - x$. Express his day revenue, total cost and profit on this meal as functions of x .



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20. The formula for converting from Fahrenheit to Celsius temperature is $y = \frac{5x}{9} - \frac{160}{9}$. Find the inverse of this function and determine whether the inverse is also a function.



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21. A simple cipher takes a number and codes it, using the function $f(x) = 3x - 4$. Find the inverse of this function determine whether the inverse is also a function and verify the symmetrical property about the line $y=x$ (by drawing the lines).



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Exercise 1 5

1. If $A = \{(x, y) : y = e^x, x \in R\}$ and $B = \{(x, y) : y = e^{-x}, x \in R\}$ then $n(A \cap B)$ is

A. Infinity

B. 0

C. 1

D. 2

Answer: C



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2. If $A = \{(x, y) : y = \sin x, x \in R\}$ and $B = \{(x, y) : y = \cos x, x \in R\}$ then $A \cap B$ contains

- A. no element
- B. infinitely many elements
- C. only one element
- D. cannot be determined.

Answer: B

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3. The relation R defined on a set $A = \{0, -1, 1, 2\}$ by $x R y$ if

$|x^2 + y^2| \leq 2$ then which one of the following is true?

- A. $R = \{(0, 0), (0, -1), (0, 1), (-1, 0), (-1, 1), (1, 2), (1, 0)\}$
- B. $R^{-1} = \{(0, 0), (0, -1), (0, 1), (-1, 0), (1, 0)\}$
- C. Domain of R is $\{0, -1, 1, 2\}$
- D. Range of R is $\{0, -1, 1\}$

Answer: D

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4. If $f(x) = |x - 2| + |x + 2|$, $x \in \mathbb{R}$ then

$$\text{A. } f(x) = \begin{cases} -2x & \text{If } x \in (-\infty, -2] \\ 4 & \text{if } x \in (-2, 2] \\ 2x & \text{if } x \in (2, \infty) \end{cases}$$

$$\text{B. } f(x) = \begin{cases} 2x & \text{If } x \in (-\infty, -2] \\ 4 & \text{if } x \in (-2, 2] \\ -2x & \text{if } x \in (2, \infty) \end{cases}$$

$$\text{C. } f(x) = \begin{cases} -2x & \text{If } x \in (-\infty, -2] \\ -4x & \text{if } x \in (-2, 2] \\ -2x & \text{if } x \in (2, \infty) \end{cases}$$

$$\text{D. } f(x) = \begin{cases} -2x & \text{If } x \in (-\infty, -2] \\ 2x & \text{if } x \in (-2, 2] \\ 2x & \text{if } x \in (2, \infty) \end{cases}$$

Answer: A

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5. Let \mathbb{R} be the set of all real numbers. Consider the following subsets of the plane $\mathbb{R} \times \mathbb{R}$

$$S = \{(x, y) : y = x + 1$$

and

$$0 < x < 2\}$$

and

$$T = \{(x, y) : x - y \text{ is an integer}\}$$

Then which of the following is true?

- A. T is an equivalence relation but S is not an equivalence relation.
- B. Neither S nor T is an equivalence relation
- C. Both S and T are equivalence relation
- D. S is an equivalence relation but T is not an equivalence relation.

Answer: A



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6. Let A and B be subsets of the universal set \mathbb{N} , the set of natural numbers. Then $A' \cup [(A \cap B) \cup B']$ is

- A. A
- B. A'
- C. B

D. N

Answer: D



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7. The number of students who take both the subjects Mathematics and Chemistry is 70. This represents 10% of the enrollment in Mathematics and 14% of the enrollment in Chemistry. The number of student take at least one of these two subjects is

A. 1120

B. 1130

C. 1100

D. insufficient data

Answer: B



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8. If $n((A \times B) \cap (A \times C)) = 8$ and $n(B \cap C) = 2$ then $n(A)$ is

A. 6

B. 4

C. 8

D. 16

Answer: B



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9. If $n(A) = 2$ and $n(B \cup C) = 3$ then $n[(A \times B) \cup (A \times C)]$ is

A. 2^3

B. 3^2

C. 6

D. 5

Answer: C



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10. If two sets A and B have 17 elements in common, then the number of elements common to the set $A \times B$ and $B \times A$ is

A. 2^{17}

B. 17^2

C. 34

D. insufficient data

Answer: B



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11. For non empty set A and B if $A \subset B$ then $(A \times B) \cap (B \times A)$ is equal to

A. $A \cap B$

B. $A \times A$

C. $B \times B$

D. None of these

Answer: B



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12. The number of relations on a set containing 3 elements is

A. 9

B. 81

C. 512

D. 1024

Answer: C



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13. Let R be the universal relation on a set X with more than one element.

Then R is

- A. not reflexive
- B. not symmetric
- C. transitive
- D. None of the above

Answer: C



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14. Let $X = \{1, 2, 3, 4\}$ and

$R = \{(1, 1), (1, 2), (1, 3), (2, 2), (3, 3), (2, 1), (3, 1), (1, 4), (4, 1)\}$.

Then R is

- A. reflexive

B. symmetric

C. transitive

D. equivalence

Answer: B



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15. The range of the function $\frac{1}{1 - \sin x}$ is

A. $(-\infty, -1) \cup \left(\frac{1}{3}, \infty\right)$

B. $\left(-1, \frac{1}{3}\right)$

C. $\left[-1, \frac{1}{3}\right]$

D. $(-\infty, -1] \cup \left[\frac{1}{3}, \infty\right)$

Answer: D



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16. The range of the function $f(x) = |(x) - x|, x \in \mathbb{R}$ is

- A. $[0, 1]$
- B. $[0, \infty)$
- C. $[0, 1)$
- D. $(0, 1)$

Answer: C



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17. The rule $f(x) = x^2$ is a bijection if the domain and the co domain are given by

- A. \mathbb{R}, \mathbb{R}
- B. $\mathbb{R}, (0, \infty)$
- C. $(, \infty), \mathbb{R}$
- D. $[0, \infty), [0, \infty)$

Answer: D



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18. The number of constant functions from a set containing m elements to a set containing n elements is

A. mn

B. m

C. n

D. $m+n$

Answer: C



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19. The function $f: [0, 2\pi] \rightarrow [-1, 1]$ defined by $f(x) = \sin x$ is

A. one to one

B. onto

C. bijection

D. cannot be determined.

Answer: B



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20. If the function $f: [-3, 3] \rightarrow S$ defined by $f(x) = x^2$ is onto then S is

A. $[-9, 9]$

B. \mathbb{R}

C. $[-3, 3]$

D. $[0, 9]$

Answer: D



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21. Let $X = \{1, 2, 3, 4\}$, $Y = \{a, b, c, d\}$ and $f = \{(1, a), (4, b), (2, c), (3, d), (2, d)\}$. Then f is

- A. an one to one function
- B. an onto function
- C. a function which is not one to one
- D. not a function

Answer: D



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22. The inverse of $f(x) = \begin{cases} x & \text{if } x < 1 \\ x^2 & \text{if } 1 \leq x \leq 4 \\ 8\sqrt{x} & \text{if } x > 4 \end{cases}$ is

A. $f^{-1}(x) = \begin{cases} x & \text{if } x < 1 \\ \sqrt{x} & \text{if } 1 \leq x \leq 16 \\ \frac{x^2}{64} & \text{if } x > 16 \end{cases}$

$$\text{B. } f^{-1}(x) = \begin{cases} -x & \text{if } x < 1 \\ \sqrt{x} & \text{if } 1 \leq x \leq 16 \\ \frac{x^2}{64} & \text{if } x > 16 \end{cases}$$

$$\text{C. } f^{-1}(x) = \begin{cases} x^2 & \text{if } x < 1 \\ \sqrt{x} & \text{if } 1 \leq x \leq 16 \\ \frac{x^2}{64} & \text{if } x > 16 \end{cases}$$

$$\text{D. } f^{-1}(x) = \begin{cases} 2x & \text{if } x < 1 \\ \sqrt{x} & \text{if } 1 \leq x \leq 16 \\ \frac{x^2}{8} & \text{if } x > 16 \end{cases}$$

Answer: A

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23. Let $f: \mathbb{R} \rightarrow \mathbb{R}$ be defined by $f(x) = 1 - |x|$. Then the range of f is

- A. \mathbb{R}
- B. $(1, \infty)$
- C. $(-1, \infty)$
- D. $(-\infty, 1]$

Answer: D



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24. The function $f: \mathbb{R} \rightarrow \mathbb{R}$ is defined by $f(x) = \sin x + \cos x$ is

- A. an odd function
- B. neither an odd function nor an even function
- C. an even function
- D. both odd function and even function.

Answer: B



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25. The function $f: \mathbb{R} \rightarrow \mathbb{R}$ is defined by

$$f(x) = \frac{(x^2 + \cos x)(1 + x^4)}{(x - \sin x)(2x - x^3)} + e^{-|x|} \text{ is}$$

- A. an odd function
- B. neither an odd function nor an even function

C. an even function

D. both odd function and even function.

Answer: C



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