



## MATHS

# NCERT - NCERT MATHEMATICS(TAMIL ENGLISH)

## TRIANGLES

### Examples

1. In the given Figure AB and CD are intersecting at 'O',  
 $OA = OB$  and  $OD = OC$ . Show that (i)  $\triangle AOD \cong \triangle BOC$   
and (ii)  $AD \parallel BC$ .



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2. AB is a line segment and line l is its perpendicular bisector. If a point P lies on l, show that P is equidistant from A and B.



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3. In the given figure,  $AB \parallel DC$  and  $AD \parallel BC$  show that  $\triangle ABC \cong \triangle CDA$ .



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4. In the given figure,  $AL \parallel DC$ , E is mid point of BC. Show that  $\triangle EBL \cong \triangle ECD$ .



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5. Use the information given in the adjoining figure, to prove :

(i)  $\triangle DBC \cong \triangle EAC$

(ii)  $DC = EC$ .



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6. Line-segment  $AB$  is parallel to another line-segment  $CD$ .  $O$  is the mid-point of  $AD$ .

Show that (i)  $\triangle AOB \cong \triangle DOC$  (ii)  $O$  is also the mid-point of  $BC$ .



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7. In  $\triangle ABC$ , the bisector  $AD$  of  $A$  is perpendicular to side  $BC$ . Show that  $AB = AC$  and  $\triangle ABC$  is isosceles.



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8. In the adjacent figure,  $AB = BC$  and  $AC = CD$ .

Prove that :  $\angle BAD : \angle ADB = 3 : 1$ .



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9. In the given figure, AD is perpendicular to BC and  $EF \parallel BC$ , if  $\angle EAB = \angle FAC$ , show that triangles ABD and ACD are congruent.

Also, find the values of  $x$  and  $y$  if

$AB = 2x + 3$ ,  $AC = 3y + 1$ ,  $BD = x$  and  $DC = y + 1$ .



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**10.** E and F are respectively the mid-points of equal sides AB and AC of  $\triangle ABC$  (see figure)

Show that  $BF = CE$ .



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**11.** In an isosceles triangle ABC with  $AB = AC$ , D and E are points on BC such that  $BE = CD$  (see figure) Show that

$AD = AE$



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12. In quadrilateral ABCD,  $AB = CD$ ,  $BC=AD$  show that  $\triangle ABC \cong \triangle CDA$  Consider  $\triangle ABC$  and  $\triangle CDA$



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13. AB is a line - segment. P and Q are points on either side of AB such that each of them is equidistant from the points A and B (See Fig ). Show that the line PQ is the perpendicular bisector of AB.



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14. P is a point equidistant from two lines  $l$  and  $m$  intersecting at point A (see figure). Show that the line AP bisects the angle between them.



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15. D is a point on side BC  $\triangle ABC$  such that  $AD = AC$  (see figure). Show that  $AB > AD$ .



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1. There are some statements given below. Write whether they are true or false :

Two circle are always congruent.



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2. There are some statements given below. Write whether they are true or false :

Two line segments of same length are always congruent.



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3. There are some statements given below. Write whether they are true or false :

Two right angle triangles are sometimes congruent.



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4. There are some statements given below. Write whether they are true or false :

Two equilateral triangles with their sides equal are always congruent.



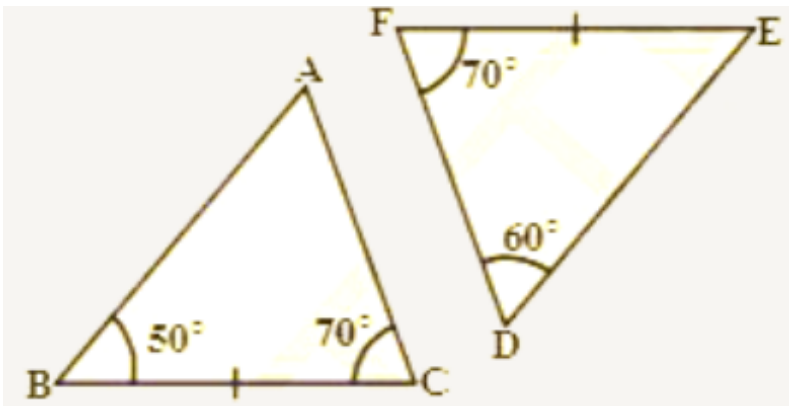
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5. Which minimum measurements do you require to check if the given figures are congruent:

- i. Two rectangles      ii. Two rhombuses.

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6. State whether the following triangles are congruent or not? Give reasons for your answer.



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7. State whether the following triangles are congruent or not? Give reasons for your answer.



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8. In the given figure, the point P bisects AB and DC.

Prove that

$$\triangle APC \cong \triangle BPD$$

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9. In the adjacent figure  $\triangle ABC$  and  $\triangle DBC$  are two triangles such that  $\overline{AB} = \overline{BD}$  and  $\overline{AC} = \overline{CD}$ . Show that  $\triangle ABC \cong \triangle DBC$ .



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10. Now draw a triangle  $ABC$  and measure its sides. Find the sum of the sides  $AB + BC$ ,  $BC + AC$  and  $AC + AB$ , compare it with the length of the third side. What do you observe?

You will observe that  $AB + BC > AC$ ,  $BC + AC > AB$  and  $AC + AB > BC$ .

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## Exercise 7 1

1. In quadrilateral  $ACBD$ ,  $AC = AD$  and  $AB$  bisects  $\angle A$  Show that  $\triangle ABC \cong \triangle ABD$ .

What can you say about  $BC$  and  $BD$ ?



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2.  $ABCD$  is a quadrilateral in which  $AD = BC$  and  $\angle DAB = \angle CBA$  Prove that

(i)  $\triangle ABD \cong \triangle BAC$

(ii)  $BD = AC$

(iii)  $\angle ABD = \angle BAC$



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3. AD and BC are equal and perpendiculars to a line segment AB. Show that CD bisects AB.



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4. l and m are two parallel lines intersected by another pair of parallel lines p and q . Show that

$$\triangle ABC \cong \triangle CDA.$$



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5. In the adjacent figure,  $AC = AE$ ,  $AB = AD$  and  $\angle BAD = \angle EAC$ . Show that  $BC = DE$ .



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6. In right triangle  $ABC$ , right angle is at  $C$ ,  $M$  is the midpoint of hypotenuse  $AB$ .  $C$  is joined to  $M$  and produced



to a point D such that  $DM = CM$ . Point D is joined to point B (see figure). Show that :

(i)  $\triangle AMC \cong \triangle BMD$

(ii)  $\angle DBC$  is a right angle

(iii)  $\triangle DBC \cong \triangle ACB$  (iv)  $CM = \frac{1}{2}AB$ .



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7. In the adjacent figure ABCD is a square and  $\triangle APB$  is an equilateral triangle. Prove that  $\triangle APD \cong \triangle BPC$ .



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8. In the adjacent figure  $\triangle ABC$  is isosceles as  $\overline{AB} = \overline{AC}$ ,  $\overline{BA}$  and  $\overline{CA}$  are produced to Q and P such that  $\overline{AQ} = \overline{AP}$ . Show that  $\overline{PB} = \overline{QC}$ .



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9. In the adjacent figure  $\triangle ABC$ ,  $D$  is the midpoint of  $BC$ .  $DE \perp AB$ ,  $DF \perp AC$  and  $DE = DF$ . Show that  $\triangle BED \cong \triangle CFD$ .



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10. If the bisector of an angle of a triangle also bisects the opposite side, prove that the triangle is isosceles.



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11. In the given figure ABC is a right triangle and right angled at B such that  $\angle BCA = 2\angle BAC$ .

Show that hypotenuse  $AC = 2BC$ .



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1. In an isosceles triangle  $ABC$ , with  $AB = AC$ , the bisectors of  $\angle B$  and  $\angle C$  intersect each other at  $O$ . Join  $A$  to  $O$ . Show that :

(i)  $OB = OC$  (ii)  $AO$  bisects  $\angle A$



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2. In  $\triangle ABC$ , the bisector  $AD$  of  $A$  is perpendicular to side  $BC$ . Show that  $AB = AC$  and  $\triangle ABC$  is isosceles.



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3. ABC is an isosceles triangle in which altitudes BD and CE are drawn to equal sides AC and AB respectively (see figure) Show that these altitudes are equal.



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4. ABC is a triangle in which altitudes BD and CE to sides AC and AB are equal (see figure) . Show that

(i)  $\triangle ABD \cong \triangle ACE$

(ii)  $AB = AC$  i.e., ABC is an isosceles triangle.



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5.  $\triangle ABC$  and  $\triangle DBC$  are two isosceles triangles on the same base  $BC$  (see figure). Show that  $\angle ABD = \angle ACD$ .



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### Exercise 7 3

1.  $AD$  is an altitude of an isosceles triangle  $ABC$  in which  $AB = AC$ . Show that, (i)  $AD$  bisects  $BC$  (ii)  $AD$  bisects  $\angle A$ .

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2. Two sides AB, BC and median AM of one triangle ABC are respectively equal to sides PQ and QR and median PN of  $\triangle PQR$  (See figure). Show that:

(i)  $\triangle ABM \cong \triangle PQN$

(ii)  $\triangle ABC \cong \triangle PQR$



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3. BE and CF are two equal altitudes of a triangle ABC. Using RHS congruence rule, prove that the triangle ABC is isosceles.



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4.  $\triangle ABC$  is an isosceles triangle in which  $AB = AC$ .

Show that  $\angle B = \angle C$ .



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5.  $\triangle ABC$  is an isosceles triangle in which  $AB = AC$ . Side  $BA$  is produced to  $D$  such that  $AD = AB$  (see figure). Show that  $\angle BCD$  is a right angle.



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6. ABC is a right angled triangle in which  $\angle A = 90^\circ$  and  $AB = AC$ . Show that  $\angle B = \angle C$ .



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7. Show that the angles of an equilateral triangle are  $60^\circ$  each.



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Exercise 7 4

1. Show that in a right angled triangle, the hypotenuse is the longest side.



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2. In adjacent figure, sides  $AB$  and  $AC$  of  $\triangle ABC$  are extended to points  $P$  and  $Q$  respectively. Also,  $\angle PBC < \angle QCB$ . Show that  $AC > AB$ .



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3. In adjacent figure,  $\angle B < \angle A$  and  $\angle C < \angle D$  Show that  $AD < BC$ .



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4. AB and CD are respectively the smallest and longest sides of quadrilateral ABCD (see adjacent figure). Show that  $\angle A > \angle C$  and  $\angle B > \angle D$ .



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5. In adjacent figure,  $PR > PQ$  and  $PS$  bisects  $\angle QPR$ .

Prove that  $\angle PSR > \angle PSQ$ .



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6. If two sides of a triangle measure 4 cm and 6 cm find all possible measurements (positive Integers) of the third side. How many distinct triangles can be obtained?



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7. Try to construct a triangle with 5 cm, 8 cm and 1 cm. Is it possible or not ? Why ? Give your justification?



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