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## MATHS

### BOOKS - VGS PUBLICATION-BRILLIANT

### MATHEMATICS -I(A) MODEL PAPER 4

#### Section A

1. Find the domain of the real function  $f(x) = \sqrt{x^2 - 25}$



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2. If  $f: R \rightarrow R$ ,  $g: R \rightarrow R$  are defined by  $f(x) = 3x - 1$  and  $g(x) = x^2 + 1$ , then find  $(f \circ g)(2)$



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3. Define a symmetric matrix. Give one example of order  $3 \times 3$



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4. Find the inverse of the matrix  $\begin{bmatrix} 1 & 2 \\ -3 & -5 \end{bmatrix}$ .



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5. If vectors  $-3\bar{i} + 4\bar{j} + \lambda\bar{k}$ ,  $\mu\bar{i} + 8\bar{j} + 6\bar{k}$  are collinear vectors then find  $\lambda$  &  $\mu$ .



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6. Find the vector equation of plane passing through Points  $(0,0,0)$ ,  $(0,5,0)$  and  $(2,0,1)$



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7. Find the angle between the vectors  $\bar{i} + 2\bar{j} + 3\bar{k}$  and  $3\bar{i} - \bar{j} + 2\bar{k}$ .



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8. Find  $\sin 330^\circ \cdot \cos 120^\circ + \cos 210^\circ \cdot \sin 300^\circ$



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9. Find the extreme values of  $\cos 2x + \cos^2 x$



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## Section B

1. If  $A = \begin{bmatrix} 7 & -2 \\ -1 & 2 \\ 5 & 3 \end{bmatrix}$ ,  $B = \begin{bmatrix} -2 & -1 \\ 4 & 2 \\ -1 & 0 \end{bmatrix}$  then find  $AB'$  and  $BA'$



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2.  $\bar{a}, \bar{b}, \bar{c}$  are non coplanar vectors. Prove that the four points  $-\bar{a} + 4\bar{b} - 3\bar{c}$ ,  $3\bar{a} + 2\bar{b} - 5\bar{c}$ ,  $-3\bar{a} + 8\bar{b} - 5\bar{c}$ ,  $-3\bar{a} + 2\bar{b} + \bar{c}$  are co-planar.



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3. Let  $\bar{a}$  and  $\bar{b}$  be vectors satisfying  $|\bar{a}| = |\bar{b}| = 5$  and  $(\bar{a}, \bar{b}) = 45^\circ$ . Find the area of the triangle having  $\bar{a} - 2\bar{b}$  and  $3\bar{a} + 2\bar{b}$  as two of its sides.



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4. If A is not an integral multiple of  $\frac{\pi}{2}$ , prove that  
(i)  $\tan A + \cot A = 2 \cos ec 2A$

(ii)  $\cot A - \tan A = 2\cot 2A'$



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5. Solve the following equations

$$\sqrt{3}\sin\theta - \cos\theta = \sqrt{2}$$



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6.  $\sin^{-1}\left(\frac{4}{5}\right) + \sin^{-1}\left(\frac{5}{13}\right) + \sin^{-1}\left(\frac{16}{65}\right) =$



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7. If  $a = (b - c)\sec\theta$ , then prove that  $\tan\theta = \frac{2\sqrt{bc}}{b - c} \frac{\sin A}{2}$ .



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## Section C

1. If  $f: A \rightarrow B$ ,  $g: B \rightarrow C$  are two bijective functions then prove that  $gof: A \rightarrow C$  is also a bijective function.



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2.

$$\lim_{n \rightarrow \infty} \left\{ \frac{1}{1.3} + \frac{1}{3.5} + \frac{1}{5.7} + \dots + \frac{1}{(2n-1)(2n+1)} \right\} =$$



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3. Show that

$$\begin{vmatrix} a+b+2c & a & b \\ c & b+c+2a & b \\ c & a & c+a+2b \end{vmatrix} = 2(a+b+c)^3$$



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4. solve the following system of equations by using Matrix inversion method.

$$2x - y + 3z = 9, x + y + z = 6, x - y + z = 2.$$



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5. Show that

i)  $\bar{a} \times (\bar{a} \times (\bar{a} \times \bar{b})) = (\bar{a} \cdot \bar{a})(\bar{b} \times \bar{a})$

ii)  $\{(\bar{a} \times \bar{b}) \times (\bar{a} \times \bar{c})\} \cdot \bar{d} = (\bar{a} \cdot \bar{d}) [\bar{a} \bar{b} \bar{c}]$



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6. If  $A, B, C$  are angles in a triangle , then prove that

$$\cos A + \cos B + \cos C = 1 + 4 \sin \frac{A}{2} \sin \frac{B}{2} \sin \frac{C}{2}$$



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7. Show that  $r + r_3 + r_1 - r_2 = 4R \cos B$ .



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