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India's Number 1 Education App

## MATHS

## NCERT - NCERT Maths(KANNADA)

## PROGRESSIONS

## Examples

1. For ths A.P. $\frac{1}{4},-\frac{1}{4},-\frac{3}{4},-\frac{5}{4} \ldots \ldots . . . .$. ,
write the first term a and the common
difference d. And find the 7th term.

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2. Which of the following forms an AP? If they form an AP, then write the next two items?
(i) $4,10,16,22, \ldots .$. , (ii) $1,-1,-3,-5$,
$-2,2,-2,2,-2$,......... (iv) $1,1,1,2,2,2,3,3,3, \ldots . .$.
(v) $x, 2 x, 3 x, 4 x, \ldots . . . . . .$.

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3. find the 10th term of the AP : 5,1,-3,7,.....

# 4. Which term of the AP: $21,18,15, \ldots . . . .$. Is -81 ? 

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5. Determine the AP whose 3rd term is 5 and
the 7 th term is 9.
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6. Check whether 301 is a term of the list of
numbers, 5,11,17,23,.....

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7. How many two-digit numbers are divisible by
$3 ?$
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8. Find the 11th term from the last of the AP series given below:

AP: 10,7,4,...., -62

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9. A sum of 1000 is invested at $8 \%$ simple interest per year. Calculate the interest at the end of each year. Do these interests form an
$A P$ ? If so, find the interest at the end of 30 years.
10. In a flower bed, there are 23 rose plants in the first row, 21 in the second, 19 in the third, and so on. There are 5 rose plants in the last row. How many rows are there in the flower bed?

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11. If the sum of the first 14 terms of an AP is

1050 and its first term is 10 , find the 20th term.
12. How many terms of the AP $24,21,18, \ldots .$. Must be taken so that their sum is 78 ?

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13. Find the sum of:
(i) the first 1000 natural numbers, (ii) the first n natural numbers.

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14. Find the sum of first 24 terms of the list of numbers whose nth term is given by $a_{n}=3+2 n$

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15. A manufacturer of TV sets produced 600 sets in the third year and 700 sets in the seventh year. Assuming that the production increases uniformly by a fixed number every year, find:
(i) the production in the 1st yea
(ii) the production in the 10th year
(iii) the total production in first 7 years Solution:

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16. Write the GP if the first term $a=3$, and the common ratio $r=2$.

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17. Write GP. If $\mathrm{a}=256, r=-\frac{1}{2}$

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18. Find the common ratio of the GP 25,
$-5,1,-\frac{1}{5}, \ldots \ldots .$.

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19. Which of the following lists of numbers

## form GP?

(i) $3,6,12, \ldots . . . .$.
(ii) $64,-32,16$,
(iii) $\frac{1}{64}, \frac{1}{32}, \frac{1}{8}, \ldots \ldots \ldots$.

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20. Find the 20th and $n$th term of the GP.
$5 \quad 5 \quad 5$
$\overline{2}, \overline{4}, \overline{8} \ldots \ldots .$.

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21. Which terms of the GP: $2,2 \sqrt{2}, 4, \ldots . . . . .$. Is 128
?

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22. In a GP the 3 rd term is 24 and 6 th term is
23. Find the 10th term.

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Try This

1. Which of these are Arithmetic Progressions and why?
(a) $2,3,5,7,8,10,15, \ldots . . .$.
(ii) $2,5,7,10,12,15, \ldots . . .$.
(c) $-1,-3,-5,-7, \ldots \ldots .$.

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2. Write 3 more Arithemic Progressions.

# 1. Write three examples for finite AP and three 

 for infinite AP.- Watch Video Solution

2. Add a fixed number to each and every term of AP. Write the resulting numbers as a list.

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3. Similarly subtract a fixed number from each and every term ofAP. Write the resulting numbers as a list.

## - Watch Video Solution

4. Multiply or divide each term of AP by a fixed number and write the resulting numbers as a list.

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5. Find the sum of indicated number of terms
in each of the following Aps
(i) $16,11,6, \ldots . ., 23$ terms
(ii) $-0.5,-1.0,-1.5, \ldots . . . . . ., 10$ terms
(iii) $-1, \frac{1}{4}, \frac{3}{2}, \ldots . . .10$ terms

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6. Find which of the following are not GPs

6,12,24,48,.....
7. Find which of the following are not GPs

1,4,9,16,......

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8. Find which of the following are not GPs
$1,-1,1,-1, . . . . . .$.
(D) Watch Video Solution
9. Find which of the following are not GPs
$-4,-20,-100,-500$,

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Exercise 61

1. In which of the following situations, does
the list of numbers involved form an arithmetic progression, and why?
(i)The taxi fare after each km when the fare is

Rs 15 for the first km and Rs 8 for additional km.
(ii) The amount of air present in a cylinder when a vacuum pump removes $\left(\frac{1}{4}\right)^{t h}$ of the air remaining in the cylinder at a time.
(iii) The cost of digging a well, after every metre of digging, when it costs 150 for the first metre and rises by 50 for each subsequent metre.
(iv) The amount of money in the account every
year, when 10000 is deposited at compound interest at 8 \% per annum.
2. Write first four terms of the AP, when the first term a and the common difference $d$ are given as follows:
(i) $a=10, d=10$
(ii) $a=-2, d=0$
(iii) $\mathrm{a}=4, \mathrm{~d}=-3$
(iv) $a=-1, d=\frac{1}{2}$
(v) $a=-1.25, d=-0.25$

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3. For the following Aps, write the first term and the common difference:
(i) $3,1,-1,-3, \ldots$
(ii) $-5,-1,3,7$,
(iii) $\frac{1}{3}, \frac{5}{3}, \frac{9}{3}, \frac{13}{3}, \ldots \ldots \ldots$
(iv) $0.6,1.7,2.8,3.9$,

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4. Which of the following are Aps? If they form
an AP, find the common difference $d$ and write
the next three terms.
(i) $2,4,8,16, . . .$.
(ii) $2, \frac{5}{2}, 3, \frac{7}{2}, \ldots \ldots$
(iii) $-1.2,-3.2,-5.2,-7.2, . . . . . .$.
(iv) $-10,-6,-2,2, \ldots . . . . . .$.
(v) $3,3+\sqrt{2}, 3+2 \sqrt{2}, 3+3 \sqrt{2}$.
(vi) $0.2,0.22,0.222,0.2222, . . .$.
(vii) $0,-4,-8,-12$,.........
(viii) $-\frac{1}{2},-\frac{1}{2},-\frac{1}{2},-\frac{1}{2}$,
(ix) $1,3,9,27, \ldots . . .$.
(x) a,2a, Ba, 4a,.......
(xi) $a, a^{2}, a^{3}, a^{4}, \ldots . . . .$.
(xii) $\sqrt{2}, \sqrt{8}, \sqrt{18}, \sqrt{32}, \ldots .$.
(xiii) $\sqrt{3}, \sqrt{6}, \sqrt{9}, \sqrt{12}, \ldots . . . . . . . . . .$.

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## Exercise 62

## 1. Find the

(i) 30th term of the AP 10,7,4,....
(ii) 11th term fo the AP: $-3,-\frac{1}{2}, 2 \ldots . . .$.

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2. Find the respective terms for the following

Aps:
(i) $a_{1}=2, a_{3}=26$ find $a_{2}$
(ii) $a_{2}=13, a_{4}=3$ find $a_{1}, a_{3}$
(iii) $a_{1}=5, a_{4}=-22$ find $a_{1}, a_{3}, a_{4}, a_{5}$

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3. Which term of the AP: $3,8,13,18, \ldots . . .$. . Is 78 ?
4. Find the number of terms in each of the following Aps,
(i) $7,13,19, . . . . . . .205$
(ii) $18,15\left(\frac{1}{2}\right), 13, \ldots \ldots-47$.

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5. Check whether, -150 is a term fo the AP:

11,8,5,2,.....
6. Find the 31th term of an AP whose 11th term is 38 and the 16 th term is 73 .

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7. If the $3^{\text {rd }}$ and the $9^{\text {th }}$ terms of an AP are 4 and -8 respectively, which term of this AP is zero ?
(D) Watch Video Solution
8. The 17 th term of an AP exceeds its 10th term by 7. Find the common difference.

## D Watch Video Solution

9. Two APs have the same common difference.

The difference between their 100th terms is
100. What is the difference between their 1000th terms?

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10. How many 3-digit numbers are divisible by

## $7 ?$

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11. How many multiples of 4 lie between 10 and $250 ?$
12. For what value of $n$, are the $n$th terms of two APs: $63,65,67, \ldots$ and $3,10,17, \ldots$ equal?

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13. Determine the AP whose third term is 16 and the 7th term exceeds the 5th term by 12.
14. Find the 20th term from the end of the AP:3, 8, 13, ..., 253.

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15. The sum of the 4 th and 8 th terms of an AP is 24 and the sum of the 6th and 10th terms is
16. Find the first three terms of the AP.

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16. Subba Rao started work in 1995 at an annual salary of Rs. 5000 and received an increment of Rs. 200 cash year. In which year did this income reach Rs. 7000 ?

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Exercise 63

1. Find the sum of the following Aps,
(i) $2,7,12$,.....to 10 terms.
(ii) $-37,-33,-29$, to 12 terms
(iii) $0.6,1.7,2.8, . . . .$. to 100 terms
(iv) $\frac{1}{15}, \frac{1}{12}, \frac{1}{10}, \ldots \ldots . . . . . .$. To 11 terms.

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2. Find the sums given below:
(i) $7+10 \frac{1}{2}+14+\ldots \ldots \ldots+84$
(ii) $34+32+30+\ldots .+10$
(iii)
$-5+(-8)+(-11)+\ldots \ldots \ldots+(-230)$

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## 3. In an AP:

(i) Given $\mathrm{a}=5, \mathrm{~d}=3, a_{n}=50$, find n and $S_{n}$
(ii) given a=7, $a_{13}=35$, find d and $S_{13}$.
(iii) given $a_{12}=37, d=3$, find a and $S_{12}$
(iv) given $a_{3}=15, S_{10}=125$, find d and $a_{10}$
(v) given $\mathrm{a}=2, \mathrm{~d}=8, S_{n}=90$, find n and $a_{n}$
(vi) given $a_{n}=4, d=2, S_{n}=-14$, find n and a .
(vii) given $\mathrm{I}=28, \mathrm{~S}=144$, and there are total 9 terms, find a.
4. The first and the last terms of an AP are 17 and 350 respectively. If the common difference is 9 , how many terms are there and what is their sum?

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5. Find the sum of first 51 terms of an AP whose second and third terms are 14 and 18 respectively.
6. If the sum of first 7 terms of an AP is 49 and
that of 17 terms is 289 , find the sum of first $n$ terms.

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7. Show that $a_{1}, a_{2}, \ldots, a_{n}, \ldots$ form an A.P
where an is defined as below : (i) $a_{n}=3+4 n$
(ii) $a_{n}=9-5 n$.

Also find the sum of the first 15 terms in each case.

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8. If the sum of the first $n$ terms of an $A P$ is
$4 n-n^{2}$, what is the first term (note that the
first term is $S_{1}$ )? What is the sum of first two
terms? What is the second term? Similarly, find the 3rd, the 10th and the nth terms

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9. Find the sum ofthe first 40 positive integers divisible by 6.

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10. A sum of Rs. 700 to be used to give seven
cash prizes to students of a school for thir overall academic performance. If each prize is

Rs. 20 less than its preceding prize, find the value of each of the prizes.
11. In a scholl students thought of planting trees in and around the school to reduce air pollution. It was decided that the number of tress, that each section of each class will plant,
will be the same as the class, in which they are
studying, e.g., a section of Class I with plant I tree, a section of Class II will plant 2 trees and so on till Class XII. Three are three sections of each class. How many tress will be planted by the students ?

1. Write three terms of the GP when the first term 'a' and the common ratio 'r' are given?
(i) $a=4, r=3$
(ii) $a=\sqrt{5}, r=\frac{1}{5}$
(iii) $a=81, r=-\frac{1}{3}$,
(iv) $a=\frac{1}{64}, r=2$
2. Which of the following are GP? If they are in
G.P. Write next three terms?
(i) $4,8,16$,.....
(ii) $\frac{1}{3},-\frac{1}{6}, \frac{1}{12}, \ldots \ldots$.
(iii) $5,55,555$,.......
(iv) $-2,-6,-18$,.......
(v) $\frac{1}{2}, \frac{1}{4}, \frac{1}{6}, \ldots \ldots \ldots$
(iv) $3,--3^{2}, 3^{3}, \ldots \ldots$.
(vii) $x, 1, \frac{1}{x}, \ldots \ldots \ldots . . .(x \neq 0)$
(viii) $\frac{1}{\sqrt{2}},-2,4 \sqrt{2}$, $\ldots \ldots \ldots$.
(ix) $0.4,0.04,0.004$,........
3. Find $x$ so that $x, x+2, x+6$ are consecutive terms of a geometric progression.

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Exercise 65

1. For each geometric progressions find the
common ratio 'r'. And then find $a_{n}$.
(i) $3, \frac{3}{2}, \frac{3}{4}, \frac{3}{8}, \ldots \ldots$.
(ii) $2,-6,18,-54$
(iii) $-1,-3,-9,-27$,.....
(iv) $5,2, \frac{4}{5}, \frac{8}{25}, \ldots \ldots$

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2. Find the 10th and nth term of GP: 5,25,

125,......

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3. Find the the indicated term of each

Geometric, Progression
(i) $a_{1}=9, r=\frac{1}{3}$, find $a_{7}$,
(ii) $a_{1}=-12, r=\frac{1}{3}$, find $a_{6}$

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4. Which terms of the GP:
(i) $2,8,32, \ldots . .$. is 512 ?
(ii) $\sqrt{3}, 3,3 \sqrt{3}$,.............. is 729 ?
(iii) $\frac{1}{3}, \frac{1}{9}, \frac{1}{27}, \ldots \ldots . . . . . .$. Is $\frac{1}{2187}$ ?
5. Find the 12 th term of a G.P. whose 8 th term
is 192 , and the common ratio is 2 .

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6. The 4th term of a geometic progression is $\frac{2}{3}$ and the seventh term is $\frac{16}{81}$. Find the geometic series.
7. If the geometic progressions $162,54,18, . . .$.

And $\frac{2}{81}, \frac{2}{27}, \frac{2}{9}, \ldots \ldots$. . Have there nth term equal. Find the value of $n$.

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## Optional Exercise For Extensive Learning

1. Which term of the AP: $121,117,113, . . . . . .$. . is the
first negative term?
[Hint:Find n for $a_{n}<0$ ]

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2. The sum of the third and the seventh terms of an A.P. is 6 and the product is 8 . Find the sum of first sixteen terms of the A.P.

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3. The houses of a row are numbered consectively from 1 to 49 . show that there is a value of $x$ such that the sum of the houses preceding the house numbered x is equal to
the sum of the numbers of the houses following it. Find this value of $x$.

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4. 150 workers were engaged to finish a piece of work in a certain number of days. Four workers dropped from the work on the second day. Four workers dropped on third day and so on. It took 8 more days to finish the work. Find
the number of days in which the work was completed. [Let the no.of days to finish the
work is ' $x$ ' then
$150 x=\frac{x+8}{2}[2 \times 150+(x+8-1)(-4)]$

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5. A machine costs $5,00,000$. If its value depreciates $15 \%$ in the first year, $13\left(\frac{1}{2}\right) \%$ in
the second year, $12 \%$ in the third year and so
on. What will be its value at the end of 10
years, when all the percentages will be applied to the original cost?
[Total depression $=15+13\left(\frac{1}{2}\right)+12+$
.10 terms
$S_{n}=\frac{10}{2}[30-13.5]=82.5 \%$
$\therefore$ after 10 years original cost $=100-82.5=$
17.5, i.e. $17.5 \%$ of $5,00,000$.
