



## MATHS

### BOOKS - VIKRAM PUBLICATION ( ANDHRA PUBLICATION)

### DIFFERENTIATION

#### Solved Problems

1. Show that  $f(x) = x^2$  is differentiable  $\forall x \in R$ . Hence find the derived function.



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2. Check whether the function  $f(x) = \begin{cases} 3 + x & \text{if } x \geq 0 \\ 3 - x & \text{if } x < 0 \end{cases}$  is differentiable at  $x = 0$ .

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3. If  $f(x) = (ax + b)^n$ ,  $\left(x > -\frac{b}{a}\right)$  then find  $f'(x)$ .

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4. Find the derivative of  $f(x) = e^x(x^2 + 1)$ .

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5. If  $y = \frac{a - x}{a + x}$ ,  $(x \neq -a)$  then find  $\frac{dy}{dx}$

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6. If  $f(x) = e^{2x} \cdot \log x$ , ( $x > 0$ ) then find  $f'(x)$ .

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7. If  $f(x) = \sqrt{\frac{1+x^2}{1-x^2}}$  ( $|x| < 1$ ) then find  $f'(x)$ .

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8. If  $f(x) = x^2 \cdot 2^x \log x$  ( $x > 0$ ), find  $f'(x)$ .

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9. If  $y = \left| \frac{f(x)g(x)}{\phi(x)\Psi(x)} \right|$  then show that

$$\frac{dy}{dx} = \left| \frac{f(x)g(x)}{\phi(x)\Psi(x)} \right| + \left| \frac{f(x)g'(x)}{\phi(x)\Psi(x)} \right|$$

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10. Find  $f(x) = 7^{3+3x}$  ( $x > 0$ ), then find  $f'(x)$ .

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11. If  $f(x) = xe^x \sin x$  then find  $f'(x)$ .

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12. If  $f(x) = \sin(\log x)$ , ( $x > 0$ ) then find  $f'(x)$ .

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13. If  $f(x) = (x^3 + 6x^2 + 12x - 15)^{100}$ , find  $f'(x)$ .

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14. Find the derivative of  $f(x) = \frac{x \cos x}{\sqrt{1 + x^2}}$

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15. If  $f(x) = \log(\sec x + \tan x)$ , find  $f'(x)$ .

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16. If  $y = \sin^{-1} \sqrt{x}$ , then find  $\frac{dy}{dx}$ .

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17. If  $y = \sec(\sqrt{\tan x})$ , find  $\frac{dy}{dx}$ .

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18. Find  $\int \frac{x \sin^{-1} x}{\sqrt{1-x^2}} dx$

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19. If  $y = \log(\cosh 2x)$  then find  $\frac{dy}{dx}$

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20. If  $y = \log(\sin(\log x))$ , find  $\frac{dy}{dx}$ .

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21. If  $y = (\cot^{-1} x^3)^2$  then find  $\frac{dy}{dx}$ .

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22. If  $y = \cos e c^{-1}(e^{2x+1})$ , find  $\frac{dy}{dx}$

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23. If  $y = \tan^{-1}(\cos \sqrt{x})$  then find  $\frac{dy}{dx}$

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24. If  $y = \tan^{-1} \left( \frac{\sqrt{1+x^2} + \sqrt{1-x^2}}{\sqrt{1+x^2} - \sqrt{1-x^2}} \right)$  then find  $\frac{dy}{dx}$ .

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25. If  $y = x^2 e^x \sin x$ , then find  $\frac{dy}{dx}$

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26. If  $y = (\tan x)^{\sin x}$  then find  $\frac{dy}{dx}$

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27. If  $x = a \left[ \cos t + \log \tan \left( \frac{t}{2} \right) \right]$ ,  $y = a \sin t$  then find  $\frac{dy}{dx}$ .

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28. If  $x^y = e^{x-y}$ , then show that  $\frac{dy}{dx} = \frac{\log x}{(1 + \log x)^2}$

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29. if  $\sin y = x \sin(a + y)$  then show that  $\frac{dy}{dx} = \frac{\sin^2(a + y)}{\sin a}$ .

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30. If  $y = x^4 + \tan x$  then find  $y''$ .

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31. If  $f(x) = \sin x, \sin 2x \sin 3x$ , find  $f'(x)$ .

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32. Show that  $y = x + \tan x$  satisfies the equation

$$\cos^2 x \frac{dy^2}{dx^2} + 2x = 2y.$$

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33. If  $x = a(t - \sin t), y = a(1 + \cos t)$  find  $\frac{d^2y}{dx^2}$ .

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34. Find the second order derivative of  $y = \tan^{-1}\left(\frac{2x}{1-x^2}\right)$

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35. If  $y = \sin(\sin x)$  then show that  $y'' + (\tan x)y' + y \cos^2 x = 0$ .

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36. If  $y = \tan^{-1} \sqrt{\frac{1-x}{1+x}}$  then  $\frac{dy}{dx}$  at

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37. If  $y = \tan^{-1}\left[\frac{2x}{1-x^2}\right]$  ( $|x| < 1$ ) then we shall  $\frac{dy}{dx}$ .

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38. Find  $\frac{dy}{dx}$  if  $x = a \cos^3 t$ ,  $y = a \sin^3 t$ .

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39. If  $y = e^t + \cos t$ ,  $x = \log t + \sin t$  then find  $\frac{dy}{dx}$ .

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40. To find the derivative of  $f(x) = x^{\sin \frac{1}{x}}$  with respect to  $g(x) = \sin^{-1} x$ , we have to compute  $\frac{df}{dg}$

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41. If  $x^3 + y^3 = 3axy$  then  $\frac{dy}{dx} =$

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42. If  $2x^2 - 3xy + y^2 + x + 2y - 8 = 0$ , then  $\frac{dy}{dx}$  is equal to

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43. If  $y = x^x$  ( $x > 0$ ), find  $\frac{dy}{dx}$

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44. If  $y = (\tan x)^{\sin x}$  then find  $\frac{dy}{dx}$

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## Exercise 9 A

1. Find the derivatives of the following functions  $f(x)$ .

$$\sqrt{x} + 2x^{\frac{3}{4}} + 3x^{\frac{5}{6}} \quad (x > 0)$$

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2. Find the derivatives of the following functions  $f(x)$ .

$$\sqrt{2x - 3} + \sqrt{7 - 3x}$$

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3. Find the derivatives of the following functions  $f(x)$ .

$$(x^2 - 3)(4x^3 + 1)$$

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4. Find the derivatives of the following functions  $f(x)$ .

$$(\sqrt{x} - 3x) \left( x + \frac{1}{x} \right)$$

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5. Find the derivatives of the following functions  $f(x)$ .

$$\left(\sqrt{x+l}\right)(x^2 - 4x + 2)(x > 0)$$

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6. Find the derivative of the following functions (it is to be understood that  $a, b, c, d, p, q, r$  and  $s$  are fixed non-zero constants and  $m$  and  $n$  are integers):

$$(ax + b)^n(cx + d)^m$$

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7. Find the derivatives of the following functions  $f(x)$ .

$$5 \sin x + e^x \log x$$

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8. Find the derivatives of the following functions  $f(x)$ .

$$5^x + \log x + x^3 e^x$$



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9. Find the derivatives of the following functions  $f(x)$ .

$$e^x + \sin x \cos x$$



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10. Find the derivative of w.r.to x

$$\frac{1}{ax^2 + bx + c} \text{ (whre } |a| + |b| + |c| \neq 0)$$



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11. Find the derivatives of the following functions  $f(x)$ .

$$\log_7(\log x) (x > 0)$$

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12. Find the derivative of w.r.to x

$$\frac{1}{ax^2 + bx + c} \text{ (whre } |a| + |b| + |c| \neq 0)$$

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13. Find the derivatives of the following functions  $f(x)$ .

$$e^{2x} \log(3x + 4) \left( x > \frac{-4}{3} \right)$$

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14. Find the derivatives of the following functions  $f(x)$ .

$$(4 + x^2)e^2xy$$



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15. Find the derivatives of the following functions  $f(x)$ .

$$\frac{ax + b}{ax + d} [|c| + |d| \neq 0]$$



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16. Find the derivatives of the following functions  $f(x)$ .

$$a^x \cdot e^{x^2}$$



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17. If  $f(x) = 1 + x + x^2 + \dots + x^{100}$ , then find  $f'(1)$ .



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**18.** Find the derivatives of the following functions from the first principles.

$$x^3$$

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**19.** Find the derivatives of the following functions from the first principles.

$$x^4 + 4$$

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**20.** Find the derivatives of the following functions from the first principles.

$$ax^2 + bx + c$$

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21. Find the derivatives of the following functions from the first principles.

$$\sqrt{x+l}$$

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22. Find the derivatives of the following functions from the first principles.

$$\sin 2x$$

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23. Find the derivatives of the following functions from the first principles.

$$\cos ax$$



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24. Find the derivatives of the following functions from the first principles.

$$\tan 2x$$



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25. Find the derivatives of the following functions from the first principles.

$$\cot x$$



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26. Find the derivatives of the following functions from the first principles.

$$\sec 3x$$



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27. Find the derivativ of the function from first principles :

$$x \sin x$$



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28. Find the derivativ of the function from first principles :

$$\cos^2 x$$



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29. Find the derivative of  $\frac{1 - x\sqrt{x}}{1 + x\sqrt{x}}$ , ( $x > 0$ )



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30. Find the derivative of  $x^n n^x \log(nx)$ , ( $x > 0, n \in \mathbb{N}$ ).

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31. Find the derivative of the w.r.t.x

$$ax^{2n} \log x + bx^n e^{-x}$$

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32. Find the derivatives of the following function.

$$\left(\frac{1}{x} - x\right)^3 e^x$$

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33. Is the following function  $f$  derivable at 2 ? Justify .

$$f(x) \begin{cases} x & \text{if } 0 \leq x \leq 2 \\ 2 & \text{if } x \geq 2 \end{cases}$$

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## Exercise 9 B

1. Find the derivative of w.r.to x

$$(\cot x)^n$$

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2. Find the derivative of w.r.to x

$$\cos ec^4 x$$

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3. Find the derivatives of the following function.

$$\tan(e^x)$$

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4. Evaluate the following integrals

$$\int \frac{1 - \cos 2x}{1 + \cos 2x} dx$$

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5. Find the derivatives of the following function.

$$\sin^m x \cos^n x$$

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6. Find the derivatives of the following function.

$$\sin mx \cdot \cos nx$$

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7. Find the derivatives of the function

$$x \tan^{-1} x$$

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8. Find the derivatives of the function

$$\sin^{-1}(\cos x)$$

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9. Find the derivatives of the following function.

$$\log(\tan 5x)$$

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10. Find the derivatives of the following function.

$$\sinh^{-1}\left(\frac{3x}{4}\right)$$

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11. Find the derivatives of the function

$$\tan^{-1}(\log x)$$

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12. Find the derivative of  $\log\left(\frac{x^2 + x + 2}{x^2 - x + 2}\right)$  w.r.to  $x$ .

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13. Find the derivatives of the following function.

$$\log(\sin^{-1}(e^x))$$

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14. Find the derivative of the function

$$\sin^2 x (\sin^{-1} x)^2$$

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15. Find the derivative of  $y = \frac{\cos x}{\sin x + \cos x}$ .

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16. Find the derivatives of the following function.

$$\frac{x(l + x^2)}{\sqrt{l - x^2}}$$

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17. Differentiate the following w.r.t.  $x$  :

$$e^{\sin^{-1} x}$$



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18. Find the derivatives of the following function.

$$y = \cos(\log x + e^x)$$



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19. Find the derivatives of the following function.

$$y = \frac{\sin(x + a)}{\cos x}$$



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20. Find the derivatives of the function

$$\cot^{-1}(\cos ec3x)$$

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21. Find the derivatives of the following functions.

$$x = \sinh^2 y$$

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22. Find the derivatives of the following functions.

$$x = \tanh^2 y$$

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23. Find the derivatives of the following functions.

$$x = e^{\sinh y}$$

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24. Find the derivatives of the following functions.

$$x = \tan(e^{-y})$$

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25. Find the derivatives of the function

If  $x = \log(1 + \sin^2 y)$  show that  $\frac{dy}{dx} = \frac{e^x}{\sin 2y}$ .

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26. Find the derivatives of the function

If  $x = \log(1 + \sqrt{y})$ , then show that  $\frac{dy}{dx} = 2\sqrt{y}e^x$

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27. Find the derivative of  $v = \cos[\log(\cot x)]$

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28. Find derivative  $y = \sinh^{-1}\left(\frac{1-x}{1+x}\right)$ .

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29. Find the derivative of w.r.to x

$\log(\cot(1 - x^2))$

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**30.** Find the derivatives of the following functions.

$$y = \sin[\cos(x^2)]$$

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**31.** Find the derivative of the function wrt  $x$ .

$$\sin(\tan^{-1}(e^{-x}))$$

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**32.** Integrate the functions

$$\sin(ax + b)\cos(ax + b)$$

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33. Find the derivatives of the following functions.

$$y = \tan^{-1}\left(\tanh. \frac{x}{2}\right)$$

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34. Find the derivative of the function

$$\sin x (\tan^{-1} x)^2$$

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35. Find the derivative of  $\sin^{-1}\left(\frac{b + a \sin x}{a + b \sin x}\right)$  w.r. to  $x$ .

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36. Find the derivatives of the function

$$\cos^{-1}\left(\frac{b + a \cos x}{a + b \cos x}\right), (a > 0, b > 0)$$

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37. Find the derivatives of the following functions.

$$\tan^{-1} \left[ \frac{\cos x}{1 + \cos x} \right]$$

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### Exercise 9 C

1. Find the derivative of  $\sin^{-1}(3x - 4x^3)$  with respect of 'x'.

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2.  $\frac{d}{dx} [\cos^{-1}(4x^3 - 3x)] =$

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3. Integrate the functions

$$\sin^{-1}\left(\frac{2x}{1+x^2}\right)$$

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4. Find the derivative of  $\tan^{-1}\left(\frac{a-x}{1+ax}\right)$

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5. Integrate the following functions with respect to x.

$$\tan^{-1}\sqrt{\frac{1-\cos 2x}{1+\cos 2x}}$$

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6. Find the derivatives of the following functions.

$$y = \sin[\cos(x^2)]$$

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7. Find the derivatives of the following functions.

$$\sec^{-1}\left(\frac{l}{2x^2 - l}\right) \left(0 < x < \frac{l}{\sqrt{2}}\right)$$

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8. Find the derivative of the function wrt x.

$$\sin(\tan^{-1}(e^{-x}))$$

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9. Differentiate  $f(x) = e^x$  wr.to  $g(x) = \sqrt{x}$ .

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10. Differentiate  $f(x) = e^{\sin x}$  w.r.to  $g(x) = \sin x$ .

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11. Find the derivative of

$$f(x) = \tan^{-1}\left(\frac{2x}{1-x^2}\right) \text{ w. r. to } g(x) = \sin^{-1}\left(\frac{2x}{1+x^2}\right).$$

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12. If  $y = e^{a \sin^{-1} x}$  then prove that  $\frac{dy}{dx} = \frac{ay}{\sqrt{1-x^2}}$ .

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13. Find the derivative of  $\tan^{-1}\left(\frac{3a^2x - x^3}{a(a^2 - 3x^2)}\right)$ .

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14. Simplify each of the following:

$$\tan^{-1}(\sec x + \tan x)$$

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15. Write the following function in the simplest form :

$$\tan^{-1} \frac{\sqrt{1+x^2} - 1}{x}, x \neq 0$$

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16. Find the derivatives of the following function.

$$(\log x)^{\tan x}$$

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17. Find the derivatives of the following function.

$$(x^x)^x = x^{x^2}$$

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18. Find the derivative of  $20^{\log(\tan x)}$ .

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19. Find the derivative of the w.r.to x.

$$x^x + e^{e^x}$$

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20. Find the derivatives of the following function.

$$x \cdot \log x \cdot \log(\log x)$$



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21. Find the derivative of

$$e^{-ax^2} \cdot \sin(x \log x) \text{ w.r.t. } x$$

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22.  $\sin^{-1} \left( \frac{2^{x+1}}{1+4^x} \right)$  (put  $2^x = \tan \theta$ )

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23. Find  $\frac{dy}{dx}$  for the following functions.

$$x = 3 \cos t - 2 \cos^3 t,$$

$$y = 3 \sin t - 2 \sin^3 t$$

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24. If  $x = \frac{3at}{1+t^3}$ ,  $y = \frac{3at^2}{1+t^3}$  then find  $\frac{dy}{dx}$ .

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25. Find  $\frac{dy}{dx}$  if

$$x = a(\cos t + t \sin t), y = a(\sin t - t \cos t).$$

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26. If  $x = a \left[ \frac{1-t^2}{1+t^2} \right]$ ,  $y = \frac{2bt}{1+t^2}$  then find  $\frac{dy}{dx}$ .

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27. Differentiate  $f(x) = \log_a x$  with respect to  $g(x) = a^x$ .

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28. Differentiate  $f(x)$  with respect to  $g(x)$  for the following .

$$f(x) = \sec^{-1}\left(\frac{1}{2x^2 - 1}\right), g(x) = \sqrt{l - x^2}$$



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29. Find the derivative of  $f(x)$  w.r.t.  $g(x)$  for the

$$f(x) = \tan^{-1}\left(\frac{\sqrt{1 + x^2} - 1}{x}\right), g(x) = \tan^{-1} x$$



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30. Find the derivative of  $x^4 + y^4 - a^2xy = 0$ .



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31. Find the derivative of  $y = x^y$ .



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32. Find the derivative of the function  $y$  defined implicitly by each of the following equations.

$$y^x = x^{\sin y}$$

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33. If  $\sqrt{1-x^2} + \sqrt{1-y^2} = a(x-y)$  then prove that

$$\frac{dy}{dx} = \frac{\sqrt{1-y^2}}{\sqrt{1-x^2}}.$$

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34. If  $y = x\sqrt{a^2+x^2} + a^2 \log(x + \sqrt{a^2+x^2})$ , then show that

$$\frac{dy}{dx} = 2\sqrt{a^2+x^2}.$$

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35. If  $x^{\log y} = \log x$  then find  $\frac{dy}{dx}$ .

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36. If  $y = \tan^{-1}\left(\frac{3x - x^3}{1 - 3x^2}\right) + \tan^{-1}\left(\frac{4x - 4x^3}{1 - 6x^2 + 4x^4}\right)$  then  $\frac{dy}{dx} =$

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37. If  $x^y = y^x$  then show that  $\frac{dy}{dx} = \frac{y(x \log y - y)}{x(y \log x - x)}$ .

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38. If  $x^3 + y^3 = 3axy$  then  $\frac{dy}{dx} =$

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39. Find the derivative  $\frac{dy}{dx}$  of the function

$$y = \frac{(1 - 2x)^{2/3}(1 + 3x)^{-3/4}}{(1 - 6x)^{5/6}(1 + 7x)^{-6/7}}.$$

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40. Find the derivative  $\frac{dy}{dx}$  of each of the following functions.

$$\begin{aligned} y &= \frac{x^4 \cdot \sqrt[3]{x^2 + 4}}{\sqrt{4x^2 - 7}} \\ &= \frac{x^4(x^2 + 4)^{1/3}}{(4x^2 - 7)^{1/2}} \end{aligned}$$

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41. Find  $\frac{dy}{dx}$  for the function (using logarithms).

$$y = \frac{(a - x)^2(b - x)^2}{(c - 2x)^3}$$

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42. Find  $\frac{dy}{dx}$  for the function (using logarithms).

$$y = \frac{x^3 \sqrt{2 + 3x}}{(1 - x)(2 + x)}$$

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43. Differentiate  $\sqrt{\frac{(x - 3)(x^2 + 4)}{(3x^2 + 4x + 5)}}$ .

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44. Find the derivative of  $(\sin x)^{\log x} + x^{\sin x}$ .

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45. Find the derivatives of the following functions.

$$x^{x^x}$$

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46. Find the derivative of (ii)  $(\sin x)^x + x^{\sin x}$  w.r.to x.

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47. Find the derivatives of the following functions.

$$x^3 + (\cot x)^x$$

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48. If  $x^y + y^x = a^b$  then prove that  $\frac{dy}{dx} = - \left[ \frac{yx^{y-1} + y^x \log y}{x^y \log x + xy^{x-1}} \right]$ .

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49. If  $f(x) = \sin^{-1} \sqrt{\frac{x-\beta}{\alpha-\beta}}$ ,  $g(x) = \tan^{-1} \sqrt{\frac{x-\beta}{\alpha-x}}$  then prove that  $f'(x) = g'(x)$

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50. If

$$f(x) = (a^2 - b^2)^{-1/2} \cdot \cos^{-1} \left( \frac{a \cos x + b}{a + b \cos x} \right) \quad a > b > 0 \text{ and } 0 < x < \pi$$

, then S.T  $f'(x) = (a + b \cos x)^{-1}$ .

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51. Differentiate  $(x^2 - 5x + 8)(x^3 + 7x + 9)$  by

Using product rule

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52. Differentiate  $(x^2 - 5x + 8)(x^3 + 7x + 9)$  by

Using product rule

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53. Differentiate  $(x^2 - 5x + 8)(x^3 + 7x + 9)$  by

Using product rule

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### Exercise 9 D

1. If  $y = \frac{2x + 3}{4x + 5}$  then find  $y''$ .

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2. If  $y = ae^{nx} + be^{-nx}$ , then prove that  $y'' = n^2y$ .

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3. Find the second order derivatives of the following functions of  $f(x)$

$$y = \cos^3 x$$



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4. Find the second order derivatives of the following functions of  $f(x)$

$$y = \sin^4 x$$



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5. Find the second order derivatives of the following functions of  $f(x)$

$$\log(4x^2 - 9)$$



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6. Find the second order derivatives of the following functions of  $f(x)$

$$y = e^{-2x} \sin^3 x$$



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7. Find the second order derivatives of the following functions of  $f(x)$

$$e^x \sin x \cos 2x$$



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8. Find the second order derivatives of the following functions of  $f(x)$

$$\tan^{-1} \left[ \frac{l+x}{l-x} \right]$$



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9.  $\tan^{-1} \left( \frac{3x - x^3}{1 - 3x^2} \right) =$

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10. If  $y = ax^{n+1} + bx^{-n}$  then show that  $x^2y'' = n(n+1)y$ .

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11. If  $y = a \cos x + (b + 2x)\sin x$ , then show that  $y'' + y = 4 \cos x$ .

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12. If  $ay^4 = (x + b)^5$  then show that  $5yy'' = (y')^2$ .

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13. If  $y = a \cos(\sin x) + b \sin(\sin x)$  then prove that  $y'' + (\tan x)y' + y \cos^2 x = 0$ .



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14. If  $y = 128 \sin^3 x \cos^4 x$ , then find  $\frac{d^2y}{dx^2}$

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15. If  $y = e^{-kx/2}(a \cos nx + b \sin nx)$  then  
 $y_2 + ky_1 + (n^2 + k^2/4)y =$

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