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## MATHS

### NCERT - NCERT Maths(KANNADA)

#### TRIGONOMETRY

##### Example

1. If  $\tan A = \frac{3}{4}$ , then find the other trigonometric ratio of angle A.



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2. If  $\angle A$  and  $\angle P$  are acute angles such that  $\sin A = \sin P$  then prove that  $\angle A = \angle P$



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3. Consider a triangle PQR ,right at R ,in which  $PQ = 29$  units , $QR = 21$  units and  $\angle PQR = \theta$ , then find the values of

(i)  $\cos^2 \theta + \sin^2 \theta$  and (ii)  $\cos^2 \theta - \sin^2 \theta$



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4. In  $\Delta ABC$  , right angle is at B, $AB = 5\text{cm}$  and  $\angle ACB = 30^\circ$

Determine the lengths of the sides BC and AC.



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5. A chord of a circle of radius 6cm is making an angle  $60^\circ$  at the centre.Find the length of the chord.



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6. In  $\Delta PQR$ , right angle is at Q, PQ = 3cm and PR = 6cm Determine  $\angle QPR$  and  $\angle PRQ$



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7. If  $\sin(A - B) = \frac{1}{2}$ ,  $\cos(A + B) = \frac{1}{2}$ , where  $0^\circ < A + B \leq 90^\circ$  and  $A > B$  find A and B



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8. Evaluate  $\frac{\sec 35^\circ}{\cos ec 55^\circ}$



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9. If  $\cos 7A = \sin(A - 6^\circ)$ , where  $7A$  is an acute angle ,find the value of A .



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10. If  $\sin A = \cos B$ , then prove that  $A+B = 90^\circ$

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11. Express  $\sin 81^\circ + \tan 81^\circ$  in terms of trigonometric ratio of angles between  $0^\circ$  and  $45^\circ$

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12. If A, B and C are interior angled of a triangle ABC, then show that

$$\sin\left(\frac{B+C}{2}\right) = \cos \frac{A}{2}$$

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13. Show that  $\cot \theta + \tan \theta = \sec \theta \cos e c \theta$



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14. Show that  $\tan^2 \theta + \tan^4 \theta = \sec^4 \theta - \sec^2 \theta$



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15. Prove that  $\sqrt{\frac{1 - \cos \theta}{1 + \cos \theta}} = \cos ec\theta - \cot \theta, 0 \leq \theta \leq 90^\circ$



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Do This

1. Identify "Hypotenuse", "Opposite side " and "Adjacent side " for given triangle.



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2. In triangle XYZ,  $\angle Y$  is right angle , XZ =17m and YZ =15 cm then find

(1)  $\sin X$  (ii)  $\cos Z$  (iii)  $\tan X$



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3. In a triangle PQR with right angle at Q , the value of  $\angle P$  is  $x$ ,  $PQ = 7\text{cm}$  and  $QR = 24\text{cm}$ , then find  $\sin x$  and  $\cos x$



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4. Find the values of  $\operatorname{cosec} 60^\circ$  ,  $\sec 60^\circ$  and  $\cot 60^\circ$



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5. If  $\sin C = \frac{15}{17}$ , then find  $\cos C$ ,



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6. If  $\tan x = \frac{5}{12}$ , then find  $\sec x$ .



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7. If  $\cos ec\theta = \frac{25}{7}$ , then find  $\cot \theta$



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**Try This**

1. In a right angle triangle ABC, right angle is at C,  $BC+CA = 23$  cm and

$BC-CA = 7$  cm ,then find  $\sin A \tan B$



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2. Express  $\sec A$  and  $\cos A$  in terms of sides of right angle triangle



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3. Find the values of

$$\sin 30^\circ + \cos 30^\circ + \tan 30^\circ + \cot 30^\circ + \sec 30^\circ + \csc 30^\circ.$$



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4. Find the values for  $\tan 90^\circ$ ,  $\csc 90^\circ$ ,  $\sec 90^\circ$  and  $\cot 90^\circ$



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5. Evaluate the following and justify your answer.

$$(i) \frac{\sin^2 15^\circ + \sin^2 75^\circ}{\cos^2 36^\circ + \cos^2 54^\circ}$$



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**6.** Evaluate the following and justify your answer.

$$\sin 5^\circ \cos 85^\circ + \cos 5^\circ \sin 85^\circ$$



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**7.** Evaluate the following and justify your answer.

$$\sec 16^\circ \cos ec 74^\circ - \cot 74^\circ \tan 16^\circ$$



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### Think And Discuss

**1.** Discuss among your friends

Does  $\sin x = \frac{4}{3}$  exists for some value of angle?



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**2.** Discuss among your friends

The value of  $\sin A$  and  $\cos A$  is always less than 1, Why?



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**3.** Discuss among your friends

$\tan A$  is product of  $\tan$  and  $A$



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**4.** Is  $\frac{\sin A}{\cos A}$  equal to  $\tan A$  ?



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**5.** Discuss with your friends about the following conditions:

What can you say about  $\cos ec 0^\circ = \frac{1}{\sin 0^\circ}$ ? Is it defined? Why?



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**6.** Discuss with your friends about the following conditions:

What can you say about  $\cot 0^\circ = \frac{1}{\tan 0^\circ}$ ? Is it defined? Why?



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**7.** Discuss with your friends about the following conditions:

$\sec 0^\circ = 1$  Why?



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**8.** Observe the above table

What can you say about the values of  $\sin A$  and  $\cos A$ , as the value of angle  $A$  increases from  $0^\circ$  to  $90^\circ$ ?

If  $A \geq B$  then  $\sin A \geq \sin B$ , Is it true?

If  $A \geq B$ , then  $\cos A \geq \cos B$ , Is it true? Discuss.



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**9.** If one of the sides and any other part (either an acute angle or any side) of a right angle triangle is known, the remaining sides and angles of the triangle can be determined. Do you agree? Explain with an example.



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**10.** For which value of an acute angle  $\theta$ , (i)  $\frac{\cos \theta}{1 - \sin \theta} + \frac{\cos \theta}{1 + \sin \theta} = 4$  is true ?

For which value of  $0^\circ \leq \theta \leq 90^\circ$ , above equation is not defined?



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**11.** Are these identities true only for  $0^\circ \leq A \leq 90^\circ$ ? If not ,for which other values of A they are true ?

$$\sec^2 A - \tan^2 A = 1$$

$$\cos ec^2 A - \cot^2 A = 1$$



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## Exercise 11 1

1. In right angle triangle ABC, 8cm ,15 cm and 17 cm are the length of AB,BC and CA respectively , Then find  $\sin A$ ,  $\cos A$  and  $\tan A$ .



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2. The sides of a right angle triangle PQR are  $PQ = 7\text{cm}$  ,  $PR = 25\text{ cm}$  and  $\angle Q = 90^\circ$  respectively , Then find  $\tan P$  - $\tan R$



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3. In a right angle triangle ABC with right angle at B , in which  $a= 24$  units ,  $b = 25$  units and  $\angle BAC = \theta$ , then find  $\cos A$   $\tan A$  ( $A < 90^\circ$ )



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4. If  $\cos A = \frac{12}{13}$ , then find  $\sin A$  and  $\tan A$  ( $A < 90^\circ$ )



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5. If  $3 \tan A = 4$ , then find  $\sin A$  and  $\cos A$



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6. In  $\Delta ABC$  and  $\Delta XYZ$ , if  $\angle A$  and  $\angle X$  are acute angles such that  $\cos A = \cos X$  then show that  $\angle A = \angle X$



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7. Given  $\cot \theta = \frac{7}{8}$ , then evaluate (i)  
$$\frac{(1 + \sin \theta)(1 - \sin \theta)}{(1 + \cos \theta)(1 - \cos \theta)}$$
 (ii)  $\cot^2 \theta$



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8. In a right angle triangle ABC, right angle is at B ,If  $\tan A = \frac{1}{\sqrt{3}}$  ,  
then find the value of

(i)

$$\sin A \cos C + \cos A \sin C$$

$$(ii) \cos A \cos C - \sin A \sin C$$



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## Exercise 11 2

1. Evaluate the following

$$\sin 45^\circ + \cos 45^\circ$$



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**2. Evaluate the following**

$$\frac{\cos 45^\circ}{\sec 30^\circ + \cos ec 60^\circ}$$



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**3. Evaluate the following**

$$\frac{\sin 30^\circ + \tan 45^\circ - \cos ec 60^\circ}{\sec 30^\circ + \cos 60^\circ + \cot 45^\circ}$$



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**4.  $2\tan^2 45^\circ + \cos^2 30^\circ - \sin^2 60^\circ = ?$**



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**5. Evaluate the following**

$$\frac{\sec^2 60^\circ - \tan^2 60^\circ}{\sin^2 30^\circ + \cos^2 30^\circ}$$



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$$6. \frac{2\tan 30^\circ}{1 + \tan^2 45^\circ} =$$



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$$7. \frac{1 - \tan^2 45^\circ}{1 + \tan^2 45^\circ} = ?$$

A.  $\tan 90^\circ$

B. 1

C.  $\sin 45^\circ$

D. 0

Answer: d



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$$8. \frac{2\tan 30^\circ}{1 - \tan^2 30^\circ}$$

A.  $\cos 60^\circ$

B.  $\sin 60^\circ$

C.  $\tan 60^\circ$

D.  $\sin 30^\circ$

**Answer: c**



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$$9. \sin 60^\circ \cos 30^\circ + \sin 30^\circ \cos 60^\circ = ?$$



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10. Is it right to say that

$$\cos(60^\circ + 30^\circ) = \cos 60^\circ \cos 30^\circ - \sin 60^\circ \sin 30^\circ$$



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11. In right angle triangle  $\Delta PQR$ , right angle at Q,  $PQ = 6\text{cm}$  and  $\angle RPQ = 60^\circ$ . Determine the lengths of QR and PR.



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12. In  $\Delta XYZ$ , right angle is at Y,  $YZ = x$ , and  $XZ = 2x$ . Then determine  $\angle YXZ$  and  $\angle YZX$ .



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13. Is it right to say that  $\sin(A + B) = \sin A + \sin B$ ? Justify your answer.



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## Exercise 11.3

1. Evaluate

$$\frac{\tan 36^\circ}{\cot 54^\circ}$$



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2. Evaluate

$$\cos 12^\circ - \sin 78^\circ$$



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3.  $\cos ec 31^\circ - \sec 59^\circ = ?$



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#### 4. Evaluate

$$\sin 15^\circ \sec 75^\circ$$



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#### 5. Evaluate

$$\tan 26^\circ \tan 64^\circ$$



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#### 6. Show that

$$\tan 48^\circ \tan 16^\circ \tan 42^\circ \tan 74^\circ = 1$$



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#### 7. Show that

$$\cos 36^\circ \cos 54^\circ - \sin 36^\circ \sin 54^\circ = 0$$



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8. If  $\tan 2A = \cot(A - 18^\circ)$  where  $2A$  is an acute angle, find the value of  $A$ .



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9. If  $\tan A = \cot B$ , prove that  $A + B = 90^\circ$



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10. If  $A$ ,  $B$  and  $C$  are interior angles of a triangle  $ABC$ , then show that

$$\tan\left(\frac{A+B}{2}\right) = \frac{\cot C}{2}$$



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**11.** Expression  $\sin 75^\circ + \cos 65^\circ$  in terms of trigonometric ratios of angles between  $0^\circ$  and  $45^\circ$



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#### **Exercise 11 4**

**1.** Evaluate the following

$$(1 + \tan \theta + \sec \theta)(1 + \cos \theta - \cos e\theta)$$



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**2.** Evaluate the following

$$(\sin \theta + \cos \theta)^2 + (\sin \theta - \cos \theta)^2$$



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**3. Evaluate the following**

$$(\sec^2 \theta - 1)(\cos ec^2 \theta - 1)$$



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**4. Show that**  $(\cos ec\theta - \cot\theta)^2 = \frac{1 - \cos\theta}{1 + \cos\theta}$



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**5. Show that**  $\sqrt{\frac{1 + \sin A}{1 - \sin A}} = \sec A + \tan A$



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**6. Show that**  $\frac{1 - \tan^2 A}{\cot^2 A - 1} = \tan^2 A$



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7. Show that  $\frac{1}{\cos \theta} - \cos \theta = \tan \theta \cdot \sin \theta$



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8. Simplify  $\sec A (1 - \sin A)(\sec A + \tan A)$



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9. Prove that

$$(\sin A + \cos eCA)^2 + (\cos A + \sec A)^2 = 7 + \tan^2 A + \cot^2 A$$



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10. Simplify  $(1 - \cos \theta)(1 + \cos \theta)(1 + \cot^2 \theta)$ .



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11. If  $\sec \theta + \tan \theta = p$ , then find the value of  $\sec \theta - \tan \theta$



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12. If  $\cos ec\theta + \cot \theta = k$ , then prove that  $\cos \theta = \frac{k^2 - 1}{k^2 + 1}$



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### Optional Exercise

1. Prove that  $\frac{\cot \theta - \cos \theta}{\cot \theta + \cos \theta} = \frac{\cos ec\theta - 1}{\cos ec\theta + 1}$



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2. Prove that  $\frac{\sin \theta - \cos \theta + 1}{\sin \theta + \cos \theta - 1} = \frac{1}{\sec \theta - \tan \theta}$  [use the identity  $\sec^2 \theta = 1 + \tan^2 \theta$ ]



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3. Prove that  $(\cos ec A - \sin A)(\sec A - \cos A) = \frac{1}{\tan A + \cot A}$



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4. Prove that  $\frac{1 + \sec A}{\sec A} = \frac{\sin^2 A}{1 - \cos A}$



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5. Show that  $\left( \frac{1 + \tan^2 A}{1 + \cot^2 A} \right) = \left( \frac{1 - \tan A}{1 - \cot A} \right)^2 = \tan^2 A$



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6. Prove that  $\frac{(\sec A - 1)}{(\sec A + 1)} = \left( \frac{1 - \cos A}{(1 + \cos A)} \right)$



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