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India's Number 1 Education App

## MATHS

## BOOKS - UNITED BOOK HOUSE

## KALIDHAN INSTITUTION

## Exercise

1. If $\sin \theta+\sin \phi=2$, then what is the value of
$\cos (\theta+\phi) ?$
A. a) 0
B. b)1
C. c) -1
D. d)2

Answer:

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2. If $z$ and $w$ are two non-zero complex numbes
such that $|z|=|w| a n d$ argz+arg.w $=\pi$, then the
value of $z$ is
A. a) $\bar{w}$
B. b) $-\bar{w}$
C. c)w

D. d)-w

Answer:

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3. Suppose $a, b, c$ are in A.P and $a^{2}, b^{2}, c^{2}$ are in
G.P if a
A. a) $\frac{1}{2 \sqrt{2}}$
B. b) $\frac{1}{2 \sqrt{3}}$
C. c) $\frac{1}{2}-\frac{1}{\sqrt{3}}$
D. d) $\frac{1}{2}-\frac{1}{\sqrt{2}}$

## Answer:

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4. The number of terms in the expansion of
$(a+b+c)^{10}$ is
A. a) 55
B. b) 66
C. c) 33
D. d) 44

## Answer:

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5. The equation of a line which makes an angle $45^{\circ}$ with $x$-axis and cuts the $y=a x i s$ is at $(0,3)$ is
A. a) $y=x+3$
B. b) $y=3$
C. c) $x=3$
D. d)None of these

## Answer:

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6. The point $P$ divides the line-segment joining
the points $A(1,5)$ and $B(-4,7)$ internally in the
ratio 2:3.State which of the following is

## abscissa of $P$ ?

A. a)-1
B. b) 11
C. c) 1
D. $d)-11$

Answer:

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## 7. The digit in the unit's place of the number

 $\left[(183)!+3^{183}\right]$ is-A. a) 4
B. b)2
C. c)3
D. d) 7

Answer:

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## 8. The maximum value of $\sin \theta \cos \theta$ is

A. a) $1 / 2$
B. b)1
C. c) 2
D. d) $\infty$

Answer:

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9. There are two children in a family.One of
them is a girl child .What is probability that the other one is also a girl child?
A. a) 0
B. b) $1 / 2$
C. c) 1
D. d)cant be determined.

Answer:

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10. The probability that in a family of 5 members, exactly 2 members have birthday on

Sunday is -

$$
\begin{aligned}
& \text { A. a) } \frac{12 \times 5^{3}}{7^{5}} \\
& \text { B. b) } \frac{10 \times 6^{2}}{7^{5}} \\
& \text { C. c) } 2 / 3 \\
& \text { D. d) } \frac{10 \times 6^{3}}{7^{5}}
\end{aligned}
$$

## Answer:

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11. The angles of a triangle are in the ration

5:4:3 .Find the circular measure of the greatest angle.

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12. Prove that, $\sqrt{\frac{\sec \theta-1}{\sec \theta+1}}=\operatorname{cosec} \theta-\cot \theta$
13. If $A, B, C$ are positive acute angles and $\tan A=\frac{4}{7}$ and $\tan \mathrm{B}=1 / 7, \tan \mathrm{C}=1 / 8$ prove that $A+B+C=45^{\circ}$

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14. Find the value of $\frac{1}{2} \sec 80^{\circ}-2 \cos 20^{\circ}$

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15. Find out the three cube-roots of 8 .

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16. In how many ways can the results of the three football matches be predicted?

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17. State the binomial theorem for a positve integral index.
18. Is 600 a terms of the A.P\{ $7,11,15,19, . .$.$\} .Give$ reason for your answer.

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19. Find the equation of the line which passes
through the point $(4,-6)$ and mkes intercepts
on the axes equal in magnitude.but opposite in sign.
20. The co-ordinates of a moving point $P$ are.

$$
\left[\frac{a}{2}(\operatorname{cosec} \theta+\sin \theta) \frac{b}{2}(\operatorname{cosec} \theta-\sin \theta)\right]
$$

where $\theta$ is a variable parameter.Show that,the
equation to the locus of $P$ is
$b^{2} x^{2}-a^{2} y^{2}=a^{2} b^{2}$

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21. Find the value of $p$ so that the roots of the equation $\quad 3 x^{2}-2(7+9 p) x+(8-5 p)=0$ are reciprocal to one another.
22. Do you think 4 as a complex number?if so why?

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23. Two unbaised dice are rolled together.Find
the probability getting 2 digits, the sum of which is 7.

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24. What is the chance that a leap year selected at random will contain 53 sundays?

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25. $\sin \alpha+\sin \beta=a$ and $\cos \alpha+\cos \beta=b$ prove that
$\tan \left(\frac{\alpha-\beta}{2}\right)= \pm \sqrt{\frac{4-a^{2}-b^{2}}{a^{2}+b^{2}}}$

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26. $\sin \theta=k \sin (\theta+\phi)$.show that
$\tan (\theta+\phi)=\frac{\sin \phi}{\cos \phi-K}$

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27. Prove by the principle of mathematical induction that. $4^{n}+15 n-1$ is a mulitple of 9 for all $n \in N$.

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28. If $w$ be a imaginary cube root of uniyt and
$a+b+c=0$
then
show
that
$\left(a+b w+c w^{2}\right)^{3}+\left(a+b w^{2}+c w\right)^{3}=27 a b c$

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29. In a machine,there is a password of five characters of which the first three letters and
the last two are digits.How many passwords can be formed?
30. If the term independetn of $x$ in the expansion of $\left(\frac{k}{3} x^{2}-\frac{3}{2 x}\right)^{9}$ be 2268 ,find the value of $K$.

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31. Find the sum $: 3.1^{2}+4.2^{2}+5.3^{2}+\ldots$.
upto n terms.
32. A straight line passes through the point
$(2,3)$ and is such that the portion of intercepted between the axes is divided internally at that point in the ration 4:3.Find the equaiton of the straight line.

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33. Find the image of the point $(3,8)$ with respect to the line $x+3 y=7$ assuming the line to be a plane mirror.
34. The sum of the distances of a moving point
from the points $(c, 0)$ and $(-c, 0)$ is always 2 a unit (a>c).Find the equation to the locus of the moving point.

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35. If the sum of first $n$ terms of a G.P is $p$ and
the sum of the first $2 n$ terms is $3 p$,show that the sum of first $3 n$ terms is $7 p$.
36. The roots of the equation
$x^{2}+3 x+4=0$ are $\quad \alpha$ and $\quad \beta$.Form the equations whose roots are $(\alpha+\beta)^{2}$ and $(\alpha-\beta)^{2}$

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37. Foe any two events $A$ and $B$ prove that,
$P(A) \geq P(A \cap B) \geq P(A)+P(B)-1$
38. Two fair dice are thrown simultaneously
.The two scores are then multiplied together.Calculate the probability that the prodcut is $A$ ) 12 and $B$ )even.

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39. Find the maximum and minimum values of
$3 \sin \theta+4 \cos \theta+5$
40. Find the locus of a point which forms a triangle of area 21 square unit with the points
$(2,-7)$ and (-4,3).

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41. 

Show
that
$\sin 16^{\circ}+\cos 16^{\circ}=\frac{1}{\sqrt{2}}\left(\sqrt{3} \cos 1^{\circ}+\sin 1^{\circ}\right)$

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42. $\sin A=m$ sin $B$,show that
$\tan \left(\frac{A-B}{2}\right)=\frac{m-1}{m+1} \tan \left(\frac{A+B}{2}\right)$

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43. Exhibit graphically the solution sets of the following system of linear inequations. $x-2 y \leq 3,3 x+4 y \geq 12, x \geq 0, y \geq 0$
44. State the fundamental theorem of algebra.solve the following in the complex space: $6 x^{2}-(18+5 i) x+18+i=0$

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45. How many 4 digit numbers can be formed
form the digits,1,1,2,2,3,3,4,4,5,5?

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# 46. Find the sum upto $n$ 

 terms:0.7+0.77+0.777+...
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47. The co-ordinates of $A, B, C$ are (6,3),(-3,5) and
$(4,-2)$ respectively and $P$ is the point $(x, y)$ show
that , $\frac{\text { areaofthe } \triangle P B C}{\text { areaofthe } \triangle A B C}=\left|\frac{x+y-2}{7}\right|$

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48. The equations of two sides of a square are
$5 x+12 y-10=0$ and $5 x+12 y+29=0$ and the third
side passes through (3,5):find equations of all other possible sides of the square.

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49. Find the equations of the lines passing thorugh the point (4,5)making equal angles with the lines $3 x=4 y+7$ and $5 y=12 x+6$.
50. Write the two meanings of statistics.

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51. Define attribute with examples.

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52. Distinguish between discrete and continuous variable.
53. Define primary data with examples.

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54. Define time-series data with examples.

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55. Define Pilot survey.
56. Define tabulation.
( Watch Video Solution
57. Write two uses of ogive.

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58. If $\omega$ is the imaginary cube root of unity and

$$
\begin{aligned}
& \text { a+b+c=0 then show that } \\
& \left(a+b \omega+c \omega^{2}\right)^{3}+\left(a+b \omega^{2}+c \omega\right)^{3}=27 a b c
\end{aligned}
$$

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59. Define impossible event with examples.

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60. Describe the different parts of a table.

## - Watch Video Solution

61. Describe the different parts of a table.

- Watch Video Solution

62. Distinguish between Histogram and Bar diagram.

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63. Write the uses of Geometric mean.

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64. Show that $\sum_{i=1}^{n}\left(x_{i}-A\right)^{2}$ is minimum when $A=\bar{x}$.
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65. Prove that $\bar{x}_{1}<\bar{x}<\bar{x}_{2}$ where the symbols have their usual meanings.
66. If $y=a+b x$, then show that $M e(y)=a+b$
$\mathrm{Me}(\mathrm{x})$.

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67. Show it with an experiment that different materials have different ability to conduct heat through them.

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68. Write the classical definition of probability and state its limitations.

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69. For any two events $A$ and $B$, show that,
$P(A \cup B)=P(A)+P(B)-P(A \cap B)$.

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70. How would you construct a frequency distribution of a continuous variable?

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71. A variable takes values, $\mathrm{a}, \mathrm{ar}, a r^{2}$, $a r^{n-1}$ with equal frequencies. Find $\mathrm{AM}, \mathrm{GM}$ and HM and hence show that
$(G M)^{2}=A . M . \times H . M$.
72. State and prove Cauchy-Schwartz inequality.

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