



India's Number 1 Education App

## MATHS

### BOOKS - UNITED BOOK HOUSE

### MODEL QUESTION PAPERS-SET 11

Exercise

1. Which is null set?

A. a) $\{0\}$

B. b) $\{\emptyset\}$

C. c)  $\{x : x \in I \text{ and } 4 \leq x \leq 5\}$

D. d)  $\{x : x \in R \text{ and } x^2 + 9 = 0\}$

**Answer:**



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2.  $z$  is a complex number. The minimum value of  $|z| + |z - 2|$  is

A. a) 0

B. b) 1

C. c) 2

D. d)3

**Answer:**



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3. The value of  $m$ , satisfy the equation

$$|m - 2|^2 + |m - 2| - 6 = 0$$

A. a)1

B. b)2

C. c)3

D. d)4

**Answer:**



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4. In an AP, if the  $m$ th and  $(m + n)$ th terms are  $n$  and  $0$  respectively then  $n$ th term will be

A. a) $m$

B. b) $-m$

C. c) $m+n$

D. d) $m-n$

**Answer:**



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5. x axis divides the line segment containing two endpoints  $(3, 6)$  and  $(2, -5)$  in the ratio is

A. a)-6:5

B. b)6:5

C. c)5:6

D. d)-5:6

**Answer:**



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6. The radius of the circle

$$(p - 1)x^2 + y^2 - x - py = 0 \text{ is}$$

A. a)  $\frac{\sqrt{5}}{2} \text{ unit}$

B. b)  $\frac{\sqrt{3}}{2} \text{ unit}$

C. c)  $\sqrt{3} \text{ unit}$

D. d) 1 unit

**Answer:**



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7. The value of  $\lim_{x \rightarrow 16} \frac{x^{1/4} - 16^{1/4}}{x - 16}$  is

A. a)16

B. b)1/16

C. c)32

D. d)1/32

**Answer:**



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8. If  $y = \frac{1+x^2}{1+x}$ , then  $\frac{dy}{dx}$  at  $x=0$  is

A. a)1/2

B. b)-1/2

C. c)-1/4

D. d)-1

**Answer:**



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**9.** A bag contains 5 red caps and 4 blue caps. The probability that two drawn caps are on same colour is

A. a)1/3

B. b)1/9

C. c)2/9

D. d)None of these.

**Answer:**



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**10.** The median of 1st 67 natural number is

A. a)34

B. b) $2^{67}$

C. c) $\frac{67 \times 68}{2}$

D. d) $67^2$

**Answer:**



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11. If  $A = \{x : -1 \leq x \leq 2\}, B = \{x : 0 \leq x \leq 4\}$

Find A-B.



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12. If  $f: fR \rightarrow R^+$  defined as  $f(x) = x^2$ , show that f is surjective.



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13. If  $\cot \alpha \cot \beta = 3$ , show that  $\frac{\cos(\alpha - \beta)}{\cos(\alpha + \beta)} = 2$



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14. In  $\triangle ABC$  if  $\frac{1}{a+c} + \frac{1}{b+c} = \frac{3}{a+b+c}$ , show that  $\angle C = \frac{\pi}{3}$



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15. Express  $\frac{\sqrt{3} - i}{1 - \sqrt{3}i}$  in modulus amplitude form



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16. show that  ${}^nC_r + {}^{(n-1)}C_{r-1} + {}^{(n-1)}C_{r-2} = {}^{(n+1)}C_r$



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17. Find the middle term of the expansion of

$$\left(P^2 - \frac{1}{P}\right)^9$$



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18. Show that the sum of  $4 + 12 + 20 + 28 + \dots$  up to n

the term is a square of even number



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**19.** If the distance from- origin to- the straight line  $3x + 5y + a = 0$  is  $3\sqrt{17}$  units,then find the value of 'a'



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**20.** Find the co-ordinate of the image of  $(3, 2, -4)$  on xy plane.



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**21.** If  $f(x)=x^5 + x^3 - 2x + 3$ ,Prove that  $f'(1)+f'(-1)=4f(0)$ .



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**22.** Evaluate :  $\lim_{x \rightarrow \infty} \frac{1 + 2 + 3 + \dots + n}{n^2}$



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**23.** For any three sets  $A, B$  and  $C$ , prove that  
$$A - (B \cup C) = (A - B) \cap (A - C).$$



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**24.** For any two positive acute angles  $\theta$  and  $\phi$  if  
$$\sin(\theta + \phi) = k \sin(\theta - \phi)$$
 and  
$$33(\cos 2\phi - \cos 2\theta) + \cos 2\theta \cos 2\phi = 1$$



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**25.** Solve :  $\sqrt{3} \sin x + \cos x = 2$



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**26.** Prove by mathematical induction.

$1.1! + 2. 2! + 3. 3! + \dots + n. n! = (n + 1)! - 1$ , where

$n \in \mathbb{N}^*$ .



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**27.** If  $z = x + iy$  then  $|z - 8| + |z + 8| = 20$ . represents a  
ellipse



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28. If  $(1 + x)^n = c_0 + c_1x + c_2x^2 + \dots + c_nx^n$ , then

show that  $\frac{c_0}{1} + \frac{c_2}{3} + \frac{c_4}{5} + \dots = \frac{2^n}{n+1}$



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29. If the  $a$ th and  $b$ th term of an AP are  $\frac{1}{b}$  and  $\frac{1}{a}$ , then

show that  $(ab)$ th term is 1 and the sum upto first  $(ab)$

term is  $\frac{1}{2}(ab + 1)$ .



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**30.** In  $\triangle XYZ$  the co-ordinate of Y and Z are  $(-a, 0)$  and  $(a, 0)$ , and  $\angle XZY - \angle XYZ = 2\theta$  (constant). Prove that the locus of the point X is  $x^2 - y^2 + 2xy \cot 2\theta = a^2$



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**31.** If the three straight lines  $ax + 2y + 1 = 0$ ,  $3y + bx + 1 = 0$  and  $cx + 4y + 1 = 0$  are concurrent, then show that- a. b, c are in AP.



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**32.** If the circles  $x^2 + y^2 + 2ax + c^2 = 0$  and  $x^2 + y^2 + 2by + c^2 = 0$  touch each other, prove that

$$\frac{1}{a^2} + \frac{1}{b^2} = \frac{1}{c^2}$$



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**33.** Find the co-ordinate of a point equidistance from the points' (0, 0, 0), (4, 0, 0), (0, -6, 0) and (0, 0, 8).



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**34.** Prove that  $\lim_{x \rightarrow 1} \frac{x^2 - \sqrt{x}}{\sqrt{x} - 1} = 3$



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35. Prove that  $\sqrt{5}$  is irrational, (use the method of contradiction).

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36. In xy plane,  $|x - y| = 1$  represents an equation of a circle and one diagonal divides a quadrilateral into 4 parts" write the negation of the statements and check whether the resulting statements are true or false

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**37.** Find the mean deviation with respect to median of the frequency distribution table :

Daily wages (Rs.)	95- 105	105- 115	115- 125	125- 135	135- 145	145- 150
No. of worker	9	13	16	26	30	12



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**38.** If  $\frac{a \cos \theta \sec \phi - x}{a \sin(\theta + \phi)} = \frac{y - b \sin \theta \sec \phi}{b \cos(\theta + \phi)} = \tan \phi$   
show that  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$



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**39.** If  $\sin \alpha + \sin \beta = \frac{1}{2}$ ,  $\cos \alpha + \cos \beta = \frac{5}{4}$  find the value of  $\tan \alpha + \tan \beta$



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**40.** Solve : $(x+1)(x+2)(x+3)(x+4)=120$



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**41.** In a polygon, the measurement of least internal angle is  $120^\circ$ . If the all internal angles form an AP with common difference  $5^\circ$ , then find number of sides of the polygon



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**42.** Out of 15 boys, 7 are skaut. In how many different ways can 12 boys be selected from them so as to (a) always 6 boys are skaut (b) at least 6 boys are skaut.



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**43.** Draw the graph of the following system of inequation and show the common region.

$$4x + 5y \leq 40, x \geq 2, y \geq 3$$



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**44.** Find the equation of a parabola having the coordinate of vertex is  $(-1, -1)$  and the equation of direction is  $x + y + 4 = 0$ .



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**45.** Find the equation of an ellipse having vertices  $(-1, 2)$ - and  $(9, 2)$  . and the eccentricities is  $4/5$ .



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**46.** In each of the find the equations of the hyperbola satisfying the given conditions.

Foci  $(0, \pm \sqrt{10})$ , passing through  $(2, 3)$



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