



MATHS

BOOKS - UNITED BOOK HOUSE

MODEL QUESTION PAPERS-SET 12

Exercise

1. Which of the following sets have only one subset

A. a){0}

B. b){ ϕ , 0}

C. c){ ϕ }

D. d){1}

Answer:



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2. The value of $1 + i^2 + i^4 + i^6 + \dots + i^{16}$ is

A. a)-1

B. b)1

C. c)0

D. d)2

Answer:



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3. No of diagonals of a 12 sided polygon are

A. a)12

B. b)49

C. c)54

D. d)62

Answer:



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4. If the sum of three consecutive numbers of an AP is 45, then the middle number will be

A. a)19

B. b)15

C. c)20

D. d)22.5

Answer:



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5. The acute angle between the two lines' $7x - 4y = 0$ and $3x - 11y = 2$ will be

A. a) $\frac{\pi}{3}$

B. b) $\frac{\pi}{4}$

C. c) $\frac{\pi}{6}$

D. d) $\frac{2\pi}{6}$

Answer:



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6. The circle $x^2 + y^2 - 2x - 2y + k = 0$

represents a point circle when $k =$

A. a) 0

B. b) -1

C. c)1

D. d)2

Answer:



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7. The value of $\lim_{x \rightarrow 3} \frac{\sqrt{x+3} + \sqrt{x-3}}{x}$ is

A. a) $\frac{\sqrt{6}}{3}$

B. b) $-\frac{\sqrt{6}}{3}$

C. c)3

D. d)0

Answer:



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8. If $f(x) = 2x^3 - 3x^2 + 4x - 2$, then the value of $f'(3)$ is

A. a)0

B. b)30

C. c)40

D. d)50

Answer:



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9. Two dice are thrown at a time. The probability that the sum of two numbers is equal to 5 is

A. a) $\frac{1}{5}$

B. b) $\frac{1}{9}$

C. c) $2/5$

D. d) $2/9$

Answer:



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10. The median of 1st 2013 natural number is

A. a) 1007

B. b) 1090

C. c) 1008

D. d)None of these.

Answer:



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11. For any two sets A and B , if $A \cup B = A \cap B$, then show that $A = B$.



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12. $A = \{1, 2, 3, 4, 5\}$, $B = \{1, 3, 4\}$ and the relation R from set A to set B where $(x, y) \in R$ implies $x > y$. Find the ordered pairs of R^{-1}



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13. Show that

$$\tan 67^\circ - \tan 22^\circ - \tan 67^\circ \tan 22^\circ = 1$$


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14. In $\triangle ABC$, if $\angle C = 90^\circ$, then find the value of $\tan A + \tan B$.



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15. If ${}^n P_r = 120 {}^n C_{(n-r)}$, find the value of r .



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16. x and y are real and if $x + iy = \frac{5}{-3 + 4i}$, find the value of x and y .



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17. Find the constant term of the expansion of

$$\left(a^3 - \frac{1}{a^2}\right)^{15}$$



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18. If the P th term of an AP is $(3P - 5)$, then find the common difference and 15th term of this AP.



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19. Find the equation of a straight line passes through the middle of the straight lines $2x - 3y + 1 = 0$ and $2x - 7 = 3y$.



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20. Find the ratio in which the plane xy divides the join of $A(2, 3, 5)$ and $B(-2, -5, -3)$.



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21. If $y = xe^x$, show that $xy/dx=(1+x)y$.



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22. $f(x) = x^2 + ax$, when $0 \leq x \leq 1$ and

$f(x) = 3 - bx^2$, when $1 \leq x \leq 2$ if

$\lim_{x \rightarrow 1} f(x) = 4$, then find the value of a and b .



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23. A unbiased coin tossed three times. Find the probability of getting 1 head



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24. If the variance of a distribution is 4 coefficient of variation is 5%,then mean of the distribution is ___



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25. For any two sets, show that

$$(A \cap B) \cup (A - B) = A.$$



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26. If $\tan^2 \alpha = 1 + 2 \tan^2 \beta$, show that $\cos 2\beta = 1 + 2 \cos 2\alpha$.



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27. Solve : $\sin x + 4 \cos x = \sin 2x + 4 \cos 2x$.



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28. Prove by mathematical induction,

$$1 + \frac{1}{4} + \frac{1}{9} + \dots + \frac{1}{n^2} < 2 - \frac{1}{n} \text{ when } n \geq 2,$$

is a integer.



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29. If $\arg \left(\frac{z-1}{z+1} \right) = \frac{\pi}{4}$, then show that in

complex plane, the locus of z is a cricle.



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30. Find the term independent of x of the

expansion of $(1 + x)^3 \left(x - \frac{1}{x}\right)^6$



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31. If p th, q th and r th terms of an AP are a , b and c , then show that $a(q - r) + b(r - p) + c(p - q) = 0$.



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32. A straight line forms a right-angled triangle with the axes. If the length of the hypotenuse and the area of this triangle are 13 units and 30 sq units, find the equation of this straight line.



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33. If the coordinates of the vertices of a triangle are $(10, 4)$, $(-4, 9)$ and $(-2, -1)$. Find the coordinates of its orthocenter.



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34. Find the co-ordinate of a point on the circle $x^2 + y^2 - 4x + 2y - 20 = 0$ nearest to $\left(2, \frac{3}{2}\right)$.



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35. The co-ordinate of the vertices of a triangle are $A(0, 2, -3)$, $B(-2, 0, -4)$ and $C(3, 6, -3)$. Find the ratio in which the bisector of $\angle BAC$ divides BC and also find the co-ordinate of that point



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36. Differentiate $x + \frac{1}{x}$ ($x \neq 0$) at $x = 1$, with respect to x , with the help of 1st principle



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37. Evaluate : $\lim_{x \rightarrow 0} \frac{\sin(x^2 + 4x)}{x^3 - 5x^2 + 2x}$



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38. 'If p and q are rational numbers, then pq is also rational' convert this compound statement into a simple statement and check whether the statement is true or false.



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39. 'Square of a whole number is positive or negative'-find the validity of this compound statement.



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40. If two numbers a and b are chosen at random from the 1st 30 natural numbers, find the probability that the expression $(a^2 - b^2)$ is divisible by 3.



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41. Find A.M. and SD of the following distribution table :

Class interval	0-10	10-20	20-30	30-40	40-50
frequency	5	8	15	16	6



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42. Using vector method in a triangle , prove that,

$$(i) \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C} \text{ and}$$



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43. If α, β positive acute angles and $\sec(\alpha + \beta) - \sec(\alpha - \beta) = 2 \operatorname{cosec} \alpha$ show

$$\text{that } \sin \alpha = \cos \left(\frac{\beta}{2} \right) - \sin \left(\frac{\beta}{2} \right)$$



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44. Draw the graph and find the common region of the system of following inequations :

$$x + y \leq 5, 2x - 3y \geq 6, x \geq 2.$$



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45. if $z_1 = 1 + i\sqrt{3}, z_2 = \sqrt{3} - i$ show that

(a) $\arg(z_1 z_2) = \arg(z_1) + \arg(z_2)$ and (b)

$$\arg(z_1 / z_2) = \arg(z_1) - \arg(z_2)$$



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46. Find the value of $47C_4 + \sum_{r=0}^3 (50 - r C_3)$



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47. Find the length of the normal chord of a parabola $y^2 = 4x$, which makes an angle 45° with its axes.



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48. If θ and ϕ are the eccentric angles of the end points of a chord which passes through the focus of an ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$. Show that $\tan(\theta/2)\tan(\phi/2) = \left(\frac{e-1}{e+1}\right)$, where e is the eccentricity of the ellipse.



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49. Find the equation of a hyperbola, having foci $(\pm 7, 0)$ and its eccentricity is $4/3$.



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