



MATHS

BOOKS - UNITED BOOK HOUSE

MODEL QUESTION PAPERS-SET 4

Exercise

1. Null set is

A. a) $\{x : x^2 = 1 \text{ or } x = 2\}$

B. b) $\{0\}$

C. c) $\{x : x^2 + 1 = 0\}$

D. d) $\{x : x > 0 \text{ or } x < 0\}$

Answer:



Watch Video Solution

2. The number of real solution of $x^2 - 3|x| + 2 = 0$ are

A. a)4

B. b)3

C. c)2

D. d)1

Answer:





Watch Video Solution

3. z is a complex number and $z\bar{z} = 0$, it is true only when

A. a) $\operatorname{Re}(z)=0$

B. b) $\operatorname{Im}(z)=0$

C. c) $\operatorname{Re}(z)+\operatorname{Im}(z)=0$

D. d) z is not equal to 0

Answer:



Watch Video Solution

4. If 4th, 7th and 10th term of G.P are x , y and z , then

A. y, x, z are in G.P.

B. z, y, x are in GP

C. x, y, z are in GP

D. x, y, z are in AP.

Answer:



Watch Video Solution

5. The co-ordinate of the foot of the perpendicular from the point $(4, 3, 5)$ to z axis is

A. a)(0,0, 5)

B. b)) (0, 3, 0)

C. c)(0, 0, 4)

D. d)(4, 0, 0)

Answer:



Watch Video Solution

6. The equation of the circle passes through the point (0, 4), (0, 0) and (3, 0) is

A. a) $x^2 + y^2 - 4x - 3y = 0$

B. b) $x^2 + y^2 - 3x - 4y = 0$

C. $x^2 + y^2 - 4x + 3y = 0$

D. $x^2 + y^2 + 4x - 3y = 0$

Answer:



Watch Video Solution

7. The value of $\lim_{x \rightarrow 0} \frac{1 - \cos 4x}{x^2}$ is

A. a)-6

B. b)6

C. c)8

D. d)2

Answer:



Watch Video Solution

8. If $f(2) = 2$, and $f'(2) = 1$, then the value of

$$\lim_{x \rightarrow 2} \frac{xf(2) - 2f(x)}{x - 2}$$

A. a)0

B. b)1

C. c)-1

D. d)2

Answer:



Watch Video Solution

9. Three unbiased dice are thrown at a time. The probability of getting three distinct numbers in three dice is

A. a) $\frac{1}{9}$

B. b) $\frac{1}{36}$

C. c) $\frac{5}{9}$

D. d) $\frac{3}{2^3}$

Answer:



Watch Video Solution

10. If the variance of a distribution is 4 coefficient of variation is 5%, then mean of the distribution is ___

A. a)20

B. b)25

C. c)40

D. d)80

Answer:



[Watch Video Solution](#)

11. If $n(X) = 4$ and $n(Y) = 8$. Find the maximum and minimum numbers of elements of $X \cup Y$

 [Watch Video Solution](#)

12. If $A = \{(a, b) : a + 3b = 12, a, b \in \mathbb{N}\}$, find the range of A.

 [Watch Video Solution](#)

13. Show that $\cos^6 \theta + \sin^6 \theta = \frac{1}{8} (5 + 3 \cos 4\theta)$

 [Watch Video Solution](#)

14. If n be an integer, then find the value of $\tan \left\{ \frac{n\pi}{2} + (-1)^n \cdot \frac{\pi}{4} \right\}$.

 [Watch Video Solution](#)

 [Watch Video Solution](#)

15. If $(1 + i) (2 + i) (3 + i) \dots (n + i) = a + ib$, show that $2.5.10 \dots$

$$(n^2 + 1) = a^2 + b^2$$



[Watch Video Solution](#)

16. If n is an even number, find the sum of the series up to

n terms $1^2 - 2^2 + 3^2 - 4^2 + 5^2 - \dots$



[Watch Video Solution](#)

17. How many 5 digits telephone numbers can be formed from the digits from 0 to 9 when every number starts

with 23 (no digit being repeated in any number)



[Watch Video Solution](#)

18. Find the value of $\frac{3^2}{3} \cdot \frac{3^2}{9} \cdot \frac{3^2}{27} \dots$



[Watch Video Solution](#)

19. If the gradient of the line joining the points $(2a, -2)$ and $(1, -a)$ is -2 . Find the value of a .



[Watch Video Solution](#)

20. Find the ratio in which the plane $2x+3y+5z=1$ divides the line segment joining the points $(1,0,-3)$ and $(1,-5,7)$.



Watch Video Solution

21. Evaluate: $\lim_{x \rightarrow 0} \frac{\sin x}{x}$



Watch Video Solution

22. Find the condition for the existence of $\lim_{x \rightarrow 0} f(x)$



Watch Video Solution

23. Find the variance of 1, 2, 3, 4.



Watch Video Solution

24. There are four letters and four envelopes with proper address. Find the probability that the letters are not in proper envelopes.



Watch Video Solution

25. For any three sets A, B, C . prove that

$$A \times (B \cup C) = (A \times B) \cup (A \times C)$$


Watch Video Solution

26. If $\cos \alpha = k \cos \beta$ Show that

$$\tan\left(\frac{\alpha + \beta}{2}\right) = \frac{1 - k}{1 + k} \cot\left(\frac{\alpha - \beta}{2}\right)$$



Watch Video Solution

27. Solve : $\sec \theta - 1 = (\sqrt{2} - 1) \tan \theta$



Watch Video Solution

28. Prove by mathematical induction.

$$\frac{1}{1.3} + \frac{1}{3.5} + \frac{1}{5.7} + \dots + \frac{1}{(2n-1)(2n+1)} = \frac{n}{2n+1}$$



Watch Video Solution

29. How many different arrangements of the letters of the word ALGEBRA can be made so that the two 'A' is do not come together.



Watch Video Solution

30. If the sum of the n term of an AP is $n^2 + 2n$. which, term will be 201?



Watch Video Solution

31. If $z=x+iy$ and $\frac{z-i}{z+1}$ is purely imaginary, then show that the point z always lies on a circle.



[Watch Video Solution](#)

32. The equation of the two adjacent sides of a parallelogram are $4x + 5y = 0$ and $7x + 2y = 0$ and equation of one of the diagonal is $11x + 7y = 9$, find the equation of other diagonal.



[Watch Video Solution](#)

33. In a rectangle, the co-ordinates of the end point of a diagonal are $(2, 3)$ and $(8, 11)$ and other diagonal is parallel to y axis. Find the co-ordinate of the end points of other diagonal.



[Watch Video Solution](#)



[Watch Video Solution](#)

34. If the straight line $dx + cy = cd$ is perpendicular to the line joining the points $(4, 5)$ and $(3, -8)$ and also it passes through $(6, 1)$. Find the value of c and d



[Watch Video Solution](#)

35. Find the equation of a circle which passes through $(0, -3)$ and $(3, -4)$ and the centre lies on the straight line $2x - 5y + 12 = 0$.



[Watch Video Solution](#)

36. Evaluate: $\lim_{x \rightarrow 0} \frac{\sqrt{1+x^2} - \sqrt{1+x}}{\sqrt{1+x^3} - \sqrt{1+x}}$

 [Watch Video Solution](#)

37. If $f(x)=x|x|$, prove that $f'(x)=2|x|$.

 [Watch Video Solution](#)

38. 'If x is a whole number and x^2 is even, then x is also an even number'. Find the truth value of this statement by contrapositive method.

 [Watch Video Solution](#)

39. 'If a and b are two odd integer, then $(a + b)$ is an even intege."—examine whether this compound statement is true of false



[Watch Video Solution](#)

40. One card is drawn at random from a pack of 52 cards..Find the probability the card will be either a king or a Hearts or red?



[Watch Video Solution](#)

41. Find the mean and variance for the following frequency distributions in

Classes	0-10	10-20	20-30	30-40	40-50
Frequencies	5	8	15	16	6

 [Watch Video Solution](#)

42. Solve : $2 \cos^2 2\theta \cos 5\theta + 2 = \sin^2 \theta, \theta \in R.$

 [Watch Video Solution](#)

43. If $\frac{1}{{}^5C_r} + \frac{1}{{}^6C_r} + \frac{1}{{}^7C_r} + \dots + \frac{1}{{}^nC_r}$ find the value of r .

 [Watch Video Solution](#)

44. Show that there are 72 ways of selecting 5 letters from the word INDEPENDENT.



Watch Video Solution

45. The co-ordinate of vertex and focus of a parabola $x^2 + by^2 + 2hxy + 2gx + 2fy + c = 0$ are $(2, 4)$ and $(6, 2)$. Find the the value of b, h, g, f, c .



Watch Video Solution

46. Prove that the 4 foci of the two ellipses $25x^2 + 169y^2 = 4225$ and $400x^2 + 256y^2 = 102400$

are concyclics.



[Watch Video Solution](#)

47. Show that the difference of the focal distances of any point on the hyperbola $9x^2 - 4y^2 = 36$ is equal to its transverse axis.



[Watch Video Solution](#)