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## MATHS

## BOOKS - UNITED BOOK HOUSE

## MODEL QUESTION PAPERS-SET 6

Exercise

1. Which is nul set
A. a) $\{x: x$ is an integer,\& '-8 lt $x$ lt 9 ' $\}$
B. b) $\{0\}$
C. c) $\{m\}$
D. $d)\{x: x$ is an irrationat no. \& $1 \mathrm{lt} x \mathrm{lt}\}$

## Answer:

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2. $\sqrt{4 i}=$
A. a) $\pm \sqrt{2}(1-i)$
B. b) $\pm(1+i)$

$$
\text { C. c) } \pm(1-i)
$$

D. d$) \pm \sqrt{2}(1+i)$

## Answer:

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3. In the expansion of $\left(1+2 x+x^{2}\right)^{20}$, the no of-terms will be
A. a) 20
B. b) 40
C. c) 41
D. d) 60

## Answer:

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4. If an A.P., the sum of 1 st n terms is $2 n^{2}+3 n$,
then the common difference will
A. a)3
B. b) 4
C. c) 5
D. d) 6

## Answer:

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5. $\frac{x^{2}}{1-\lambda}+\frac{y^{2}}{1-\lambda}+1=0$,the equation
represent an ellipse if
A. a) $\lambda>1$
B. b) $\lambda>3$
C. c) $\lambda<3$
D. d) $1<\lambda<3$

## Answer:

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6. If the straight lines $2 x-3 y+5=0$ and $a x+2 y$.
$=6$ are parallel, then the value of $a$ is
A. a)-3/4
B. b) $-4 / 3$
C. c) $3 / 4$
D. d) $4 / 3$

## Answer:

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7. The value of $\lim _{x \rightarrow 4} \frac{x^{5 / 2}-4^{5 / 2}}{x-4}$ is
A. a) 14

B. b) 16

C. c) 18
D. d) 20

## Answer:

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8. For all values ofx and $y, f f(x+y)=f(x) \cdot f(y)$,
$f(5)=2$ and $f^{\prime}(0)=3$, the value of $f^{\prime}(5)$ is
A. a) 5
B. b) 6
C. c) 2
D. d) 0

## Answer:

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9. Two imbaised coins are tossed at a time.

What is the probability of getting at least one tail?
A. a)3/4
B. b) $1 / 4$

## C. c) $1 / 2$

$$
\text { D. d) } 1 / 3
$$

## Answer:

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10. If the variance of a distribution is 4 coefficient of variation is $5 \%$,then mean of the distribution is
A. a) 20
B. b) 40
C. c) 60
D. d) 70

Answer:

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11. Find the power set of $A=\{\{a\},\{b, c\}\}$
12. If $P=\{4.5\}, ' Q=\{7\}$. find the defined relations

## from P to Q .

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13. 

Find
the
value
of
$\cos 10^{\circ}+\cos 110^{\circ}+\cos 130^{\circ}$

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14. In $\triangle A B C$, if $(\mathrm{c}+\mathrm{a}+\mathrm{b})(\mathrm{a}+\mathrm{b}-\mathrm{c})=\mathrm{ab}$,
find the-value of $\angle C$.

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15. If $\alpha, \beta$ be the imaginary cube root of unity,
then show that $\alpha^{4}+\beta^{4}+\alpha^{-1} \beta^{-1}=0$

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16. Find the number of diagonals of a polygon having sides 10.

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17. Show.that there will be-no term containing
$P^{6}$ in the expansion of $\left(2 P^{2}-\frac{3}{p}\right)^{11}$

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18. Which term of this-progression $0.004,0.02$,
$0.1 . . .$. is 12.5 ?

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19. Find the gradient of a straight line which is passes through the point $(-3,6)$ and the mid point of (4, -5) and ( $-2,9$ )

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20. Show that the points $A(1,2,3), B(-1,-2,-1)$
,$C(2,3,2)$ and $D(4,7,6)$ are the vertices of a parallelogram ABCD but it is not a rectangle

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21. If $2 f(x)+3 f(-x)=x^{2}-x+1$, find the value of $f(1)$.

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22. Evaluate: $\lim _{x \rightarrow 0} \frac{e^{x^{2}}-\cos x}{x^{2}}$

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23. Three Coins are tossed: What is the probability of getting at least one tail?
24. If mean $=10$, coefficient of variation $=50 \%$, find the standard deviation.

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25. In three sets, $\mathrm{A}, \mathrm{B}, \mathrm{C}$, show that $(A \cap B)^{\prime}=$
$A^{\prime} \cup B^{\prime}$.

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26. If $\tan \theta=\frac{\tan \alpha+\tan \beta}{1+\tan \alpha \tan \beta}$, then show that $\sin 2 \theta=\frac{\sin 2 \alpha+\sin 2 \beta}{1+\sin 2 \alpha \sin 2 \beta}$

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27. In any $\triangle A B C$, show that ' $\mathrm{c} \sin$
$\frac{A-B}{2}=(a-b) \cos \left(\frac{C}{2}\right)$

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28. Show that by mathematical induction,
$3.5^{2 n+1}+2^{3 n+1}$ is divisible by 17 , when
$n>=0$ is an integer.

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29. If $x+i y=\frac{3}{2+\cos \theta+i \sin \theta}$ then show that $x^{2}+y^{2}=4 x-3$.

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30. The sum of an infinite G.P series is 15 and
the sum of the squares of these terms is 45 ,

Find the G.P
31. How many different arrangements be' possible in'EXAMINATION where two A's will be together?

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32. A ray of light comming from $(1,2)$ to the $x$ axis at $A$ and reflecting with the point $(5,3)$.

Find the co-ordinate of A .

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33. The co-ordinate of the two verties of a trainge are $(15,0)$ and ( 0,10 ): If the co-ordinate of the ortho centre of this triangle is (6, 9),find the co-ordinate of the third vertex of the triangle.

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34. Find the equation of the concentric- cricle of the circle $x^{2}+y^{2}-5 x+4 y=1$, which
touches the straight line $4 x-3 y=6$.

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35. The distance between the point on $x$ axis and $(3,2,-4)$ is $m$ unit.Find the co-ordinate of that point which lies on $x$ axis

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36. 

Prove
that,
$\lim _{n \rightarrow \infty} \frac{1^{3}+2^{3}+3^{3}+\ldots+n^{3}}{n^{4}}=\frac{1}{4}$

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37. If $y=\frac{x \sin x+\cos x}{x \cos x-\sin x}$, then show that
$\frac{d y}{d x}=\frac{x^{2}}{(x \cos x-\sin x)^{2}}$

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38. If $n$ is a such real number that $n>3$ then
$n^{2}>9$ prove it by the method of contradiction.
39. The mean and SD of 20 items were found to be 12.5 and 2.1 resp.After that,one item of 23 being added: find the AM and SD of 21 items

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40. Out of 15 articles in a box, three of. them
are defective. If 5 articles of them are drawn at
random, what is the probability that at least one article are defective.
41. In $\triangle A B C$, if
$\left(a^{2}+b^{2}\right) \sin (A-B)=\left(a^{2}-b^{2}\right) \sin (A+B)$
,show that the triangle is either isosceles or right angled.

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42. State the fundamental theorem of algebra

Solve : $i x^{2}-x+12 i=0$
43. If $S$ be the sum. $P$ be the product,and $R$ the sum of the reciprocals of n terms in a G.P.,

Prove that $P^{2}=\left(\frac{S}{R}\right)^{n}$

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44. Exhibit graphically the solution region of the following system of 'inequations :

$$
2 x+y \geq 4, x+y \leq 3,2 x-3 y \leq 6, x>0, y>0
$$

45. In quadrilateral PQRS, there are 3, 4, 5, 6 points are taken on $\mathrm{PQ} . \mathrm{QR}$. RS,SP respectively:How many triangles are formed from those points?

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46. If the extremitied of a focal chord of the parabola $\quad y^{2}=4 a x$ be $\quad\left(a t_{1}^{2}, 2 a t_{1}\right)$ and
$\left(a t_{2}^{2}, 2 a t_{2}\right)$,show that $t_{1} t_{2}=-1$
47. Find the equation of an ellipse which passes through the point $(-2,2),(3,-1)$ and the major and minor axes as the axes of co ordinate. Find its eccentricity.
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