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## PHYSICS

## BOOKS - HC VERMA

## ALTERNATING CURRENT

## Examples

1. The peak value of an alternating current is 5 A and
its frequency is 60 Hz . Find its rms value. How long will
the cukrgrenQt current IS 5 A and its frequency is 60
Hz . Find its runs value.
2. Find the reactance of a capacitor $(C=200 \mu F)$ when it is connected to (a) a10HzACsource, (b) $a 50 H z A C$ source and (c) $a 500 H z A C$ source.

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3. An inductor $(L=200 \mathrm{mH})$ is connected to an $A C$ source of peak emf 210 V and frequency 50 Hz .

Calculate the peak current. What is the instantaneous
voltage of the source when the current is at its peak value?
4. An LCR series circuit with
$L=100 \mathrm{mH}, C=100 \mu F, R=120 \Omega$ is connected
to an $A C$ source of emf $\varepsilon=(30 V) \sin \left(100 s^{-1}\right) t$.
Find the impedance, the peak current and the resonant frequency of the circuit.

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5. A radio set operates at $6 V D C$. A transformer with

18 turns in the secondary coil is used to step down the input $220 V A C e m f \rightarrow 6 V A C e m f$. This $A C e m f$
is then rectified by another circuit to give $6 V D C$
which is fed to the radio. Find the number of turns in the primary.

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## Worked Out Examples

1. A resistance of $20 \Omega$ is connected to a source of alternating current rated $110 \mathrm{~V}, 50 \mathrm{~Hz}$. Find (a) the $r m s$ current, (b) the maxium instantaneous current in the resistor and (c) the time taken by the current to change from its maximum value to the rms value.
2. The current in a discharging $L R$ circuit is given by $I=i_{0} e^{-\frac{t}{\tau}}$ where $\tau$ is the time constant of the circuit. Calculate the rms current for the period $t=0$ to $t=\tau$.

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3. A coil having a resistance of $50.0 \Omega$ and an inductance of 0.500 henryisco $\cap$ ected $\rightarrow$ anAC sourceof 110 volts, $50.0^{\text {© cycle//s. Find the rms value }}$ of the current in the circuit.
4. A capacitor of capacitance $100 \mu F$ and a coil of resistance $50 \Omega$ and inductance 0.5 H are connected in series with $a 110 \mathrm{~V}, 50 \mathrm{HzAC}$ source. Find the rms value of the current.

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5. A capacitor of capacitance $12.0 \mu F$ is joined to an
$A C$ source of frequency 200 Hz . The rms current in the circuit is $2.00 A$. (a) Find the rms voltage across the capacitor. (b) Find the average energy stored in the electric field between the plates of the capacitor.
6. A series AC circuit contains an inductor $(20 \mathrm{mH})$, a capacitor $(100 \mu F)$, a resistor ( $50 \Omega$ ) and an AC source of $12 \mathrm{~V}, 50 \mathrm{~Hz}$. Find the energy dissipated in the circuit in $1000 s$.

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7. An inductor of inductance 100 mH is connected in series with a resistance, a variable capacitance and an
$A C$ source of frequency 2.0 kHz . What should be the
value of the capacitance so that maximum current may be drawn into the circuit?
8. An inductor coil joined to a $6 V$ battery draws a steady current of $12 A$. This coil is connected to a capacitor and an $A C$ source of rms voltage 6 V in series. If the current in the circuit is in phase with the emf, find the rms current.

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## Short Answer

## 1. What is the reactance of a capacitor connected to a

 constant $D C$ source?
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2. The voltage and current in a series AC circuit are given by
$V=V_{0} \cos \omega t$ and $I=i_{0} \sin \omega t$.
What is the power dissipated in the circuit?

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3. Two alternating currents are given by
$i_{1}=i_{0} \sin \omega t$ and $\left.i_{2}=i_{0} \sin \left(\omega t+\frac{\pi}{3}\right)\right)$.
Will the rms values of the currents be equal or different?

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4. Can the peak voltage across the inductor be greater than the peak voltage of the source in an LCR

## circuit?

5. In a circuit containing a capacitor and an AC source, the current is zero at the instant the source voltage is maximum. Is it consistent with Ohm's law?

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6. An AC source is connected to a capacitor. Will the rms current increase, decrease or remain constnat if a dielectric slab is inserted into the capacitor?
7. When the frequency of the AC source in an LCR circuit equals the resonant frequency, the reactance of the circuit is zero. Does it mean that there is no current through the inductor or the capacitor?

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8. When an AC source is connected to a capacitor there is a steady-state current in the circuit. Does it mean that the charges jump from one plate to the other to complete the circuit?
9. A current $i_{1}=i_{10} \sin \omega t$ passes through a resistor of resistance $R$. How much thermal energy is produced in one time period? A current
$i_{2}=-i_{0} \sin \omega t$ passes through the resistor. How much thermal energy is produced in one time period?

If $i_{1}$ and $i_{2}$ both pass through the resistor simultaneously, how much thermal energy is produced? Is the principle of superposition obeyed in this case?
10. Is energy produced when a transformer steps up the voltage?

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11. A transformer is designed to convert an AC voltage of 110 V to an $A C$ voltage of 12 V . If the input terminals are connected to a $D C$ voltage of 110 V , the transformer usually burns. Explain.
12. Can you have an $A C$ series circuit in which there is a phase difference of (a) $180^{\circ}$ (b) $120^{\circ}$ between the emf and the current?

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13. A resistance is connected to an $A C$ source. If a
capacitor is included in the series circuit, will the average power absorbed by the resistance increase or decrease? If an inductor of small inductance is also included in the series circuit, will the average power absorbed increase or decrease further?
14. Can a hot-wire ammeter be used to measure a direct current having a constant value? Do we have to change the graduation?

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## Objective 1

1. A capacitor acts as an infinite resistance for
A. DC
B. $A C$
C. DC as well as AC
D. Neither AC nor DC

## Answer: A

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2. An AC source producing emf

$$
\varepsilon=\varepsilon_{0}\left[\cos \left(100 \pi s^{-1}\right) t+\cos \left(500 \pi s^{-1}\right) t\right]
$$

is connected in series with a capacitor and a resistor.
The steady-state current in the circuit is found to be

$$
I=i_{1} \cos \left[\left(100 \pi s^{-1} t+\varphi_{1}\right]+i_{2} \cos \left[\left(500 \pi s^{-1}\right) t+\phi_{2}\right]\right.
$$

A. $i_{1}>i_{2}$
B. $i_{1}=i_{2}$
C. $i_{1}<i_{2}$
D. The information is insufficient to find the relation between $i_{1}$ and $i_{2}$.

## Answer: C

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3. The peak voltage in a $220 \mathrm{~V} A C$ source is
A. 220 V
B. about 160 V

## C. about 310 V

## D. 440 V

## Answer: C

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4. An AC source is rated $220 \mathrm{~V}, 50 \mathrm{~Hz}$. The average voltage is calculated in a time interval of 0.01 s . It
A. must be zero
B. may be zero
C. is never zero
D. is $\left(\frac{220}{\sqrt{2}}\right) V$

Answer: B

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5. The magnetic field energy in an inductor changes
from maximum value to minimum value in 5.0 ms
when connected to an AC source. The frequency of
the source is
A. 20 Hz
B. 50 Hz

## C. 200 Hz

D. 500 Hz .

## Answer: B

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6. Which of the following plots may represent the reactance of a series $L C$ combination?

7. A series $A C$ circuit has a resistance of $4 \Omega$ and a reactance of $3 \Omega$. The impedance of the circuit is
A. $5 \Omega$
B. $7 \Omega$
C. $\frac{12}{7} \Omega$
D. $\frac{7}{12} \Omega$

Answer: A

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8. Transformer are used in
A. in DC circuits only
B. in AC circuits only
C. in both DC and AC circuits

## D. neither in $D C$ nor in $A C$ circuits

## Answer: B

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9. An alternating current is given by the equation
$i=\left(i_{1} \cos \omega t+i_{2} \sin \omega t\right)$. The rms current is given by

$$
\text { A. } \frac{i_{1}+i_{2}}{\sqrt{2}}
$$

B. $\frac{\left|i_{1}+i_{2}\right|}{\sqrt{2}}$
C. $\sqrt{\frac{i_{1}^{2}+i_{2}^{2}}{2}}$
D. $\sqrt{\frac{i_{1}^{2}+i_{2}^{2}}{\sqrt{2}}}$

## Answer: C

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10. An alternating current having peak value $14 A$ is used to heat a metal wire. To produce the same heating effect, a constant current $i$ can be used where $i$ is
A. $14 A$
B. about $20 A$
C. $7 A$
D. about $10 A$

## Answer: D

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11. A constant current of $2.8 A$ exists in a resistor. The rms current is
A. $2.8 A$
B. about $20 A$
C. $1.4 A$
D. undefined for a direct current

## Answer: A

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Objective 2

1. An inductor, a resistor and a capacitor are joined in series with an AC source. As the frequency of the source is slightly increased from a very low value, the reactance
A. of the inductor increases
B. of the resistor increases
C. of the capacitor increases
D. of the circuit increases

## Answer: A

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2. The reactance of a circuit is zero. It is possible that the circuit contains
A. an inductor and a capacitor
B. an inductor but no capacitor

## C. a capacitor but no inductor

D. None of the Above

## Answer: A

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3. In an AC series circuit, the instanctaneous current is zero when the instantaneous voltage is xamimum.

Connected to the source may be a
A. pure inductor
B. pure capacitor

## C. pure resistor

D. combination of an inductor and a capacitor

## Answer: A::B::D

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4. An inductor-coil having some resistance is connected to an AC source. Which of the following quantities have zero average value over a cycle?
A. Current
B. Induced emf in the inductor
C. Joule heat

## D. Magnetic energy stored in the inductor

## Answer: A::B::D

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5. The AC voltage across a resistance can be measured using
A. a potentiometer
B. a hot-wire voltmeter
C. a moving-coil galvanometer
D. a moving magnet galvanometer

Answer: B

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6. To convert mechanical energy into electrical energy,

## one can use

A. DC dynamo
B. AC dynamo
C. motor
D. transformer

Answer: A::B::D
7. An $A C$ source rated $100 \mathrm{~V}(\mathrm{rms})$ supplies a current of $10 A(r m s)$ to a circuit. The average power delivered by the source
A. must be $1000 W$
B. may be 1000 W
C. may be greater than 1000 W
D. may be less than 1000 W

## Answer: B::D

1. Find the time required for a 50 Hz alternating current to become its value from zero to the rms value.

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2. The household supply of electricity is at 220 V (rms
value) and 50 Hz . Find the peak voltage and the least
possible time in which the voltage an change from the rms value to zero.
3. A bulb rated 60 W at 220 V is connected across a household supply of alternating voltage of 220 V .

Calculate the maximum instantaneous current through the filament.

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4. An electric bulb is designed to operate at $12 v \mathrm{DC}$. If this bulb is connected to an AC source and gives normal brightness, what would be the peak voltage of the source?
5. The peak power consumed by a resistive coil when connected to an AC source is 80 W . Find the energy consumed by the coil in 100 seconds which is many times larger than the time period of the source.

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6. The dielectric strength of air is $3.0 \times 10^{6} \frac{\mathrm{~V}}{\mathrm{~m}}$. A parallel-plate air-capacitor has area $20 \mathrm{~cm}^{2}$ and plate separation 0.10 mm . Find the maximum rms voltage of an AC source which can be safely connected to this capacitor.
7. The electric current in a circuit is given by $I=i_{0}\left(\frac{t}{\tau}\right)$ for some time. Calculate the rms current for the period $t=0$ to $t=(\tau)$.

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8. A capacitor of capacitance $10 \mu F$ is connected to an oscillator giving an output voltage $\varepsilon=(10 \mathrm{~V}) \sin \omega t$.

Find the peak currents in the circuit for $\omega=10 s^{-1}, 100 s^{-1}, 500 s^{-1}, 1000 s^{-1}$.
9. A coil of inductance 5.0 mH and negligible resistance is connected to the oscillator of the previous problem. Find the peak currents in the circuit for $\omega=100 s^{-1}, 500 s^{-1}, 1000 s^{-1}$.

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10. A coil has a resistance of $10 \Omega$ and an inductance
of 0.4 henry. It is connected to an AC source of $6.5 \mathrm{~V}, \frac{30}{\pi} \mathrm{~Hz}$. Find the average power consumed in the circuit.
11. A resistor of resistance $100 \Omega$ is connected to an $A C$ source $\varepsilon=(12 V) \sin \left(250 \pi s^{-1}\right) t$. Find the energy dissipated as heat during $t=0$ to $t=1.0 \mathrm{~ms}$.

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12. In a series $R C$ circuit with an AC source,
$R=300 \Omega, C=25 \mu F, \varepsilon_{0} 50 \mathrm{~V}$ and $v=\frac{50}{(\Pi) H z}$. Find
the peak current and the average power dissipated in the circuit.
13. An electric bulb is designed to consume $55 W$ when operated at 110 volts. It is connected to a $220 \mathrm{~V}, 50 \mathrm{~Hz}$ line through a choke coil in series. What should be the inductance of the coil for which the bulb gets correct voltage?

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14. In a series $L C R$ circuit with an AC source,
$R=300 \Omega, C=20 \mu F, L=1.0 h e n r y, \varepsilon_{r m s}=50 \mathrm{~V}$
and $v=\frac{50}{\pi} H z$. Find (a) the rms current in the
circuit and (b) the rms potential differences across
the capacitor, the resistor and the inductor. Note that
the sum of the rms potential differences across the three elements is greater than the rms voltage of the source.

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15. Consider the situation of the previous problem.

Find the average electric field energy stored in the capacitor and the average magnetic field energy stored in the coil.
16. An inductance of $2.0 H$, a capacitance of $18 \mu F$ and a resistance of $10 k \Omega$ are connected to an AC source of 20 V with adjustable frequency. (a) What frequency should be chosen to maximise the current in the circuit? (b) What is the value of this maximum current?

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17. A coil a capacitor and an $A C$ source of rms voltage 24 V are connected in series. By varying the frequency of the source, a maximum rms current of 6

A is observed. If coil is connected is at DC batteryof
emf 12 volt and internal resistance $4 \Omega$, then current through it in steady state is

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18. Figure shows a typical circuit for low-pass filter. An
$A C$ input $V_{i}=10 \mathrm{mV}$ is applied at the left end and the output $V_{0}$ is received at the right end. Find the output voltages for
$v=10 \mathrm{kHz}, 100 \mathrm{kHz}, 1.0 \mathrm{MHz}$ and 10.0 MHz . Note
that as the frequency is increased the output decreases and hence the name low-pass filter.

19. A transformer has 50 turns in the primary and 100 in the secondary. If the primary is connected to a $220 V D C$ supply, what will be the voltage across the secondary?

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