



# PHYSICS

## BOOKS - HC VERMA

# BOHR'S MODEL AND PHYSICS OF THE ATOM

### Example

1. Calculate the energy of a  $He^{+}$  ion in its first excited state solution



[Watch Video Solution](#)

2. Calculate the wavelength of radiation emitted when  $He^+$  makes a transition from the state  $n = 3$  to the state  $n = 2$



[Watch Video Solution](#)

3. The excitation energy of a hydrogen-like ion in its first excited state is  $40.8\text{eV}$  Find the

energy needed to remove the electron from the ion



[Watch Video Solution](#)

## Worked Out Example

1. Find the radius of  $Li^{++}$  ions in its ground state assuming Bohr's model to be valid



[Watch Video Solution](#)

2. A particular hydrogen like radiation of frequency  $2.467 \times 10^{15} \text{ Hz}$  when it makes transition from  $n = 2 \rightarrow n = 1$ , What will be the frequency of the radiation emitted in a transition from  $n = 3 \rightarrow n = 1$ ?



**Watch Video Solution**

3. Calculate the two highest wavelength of the radiation emitted when hydrogen atoms make transition from higher state to  $n = 2$





Watch Video Solution

4. What is the wavelength of the radiation emitted when the electron in a hydrogen atom jumps from  $n = \text{infinity} \rightarrow n = 2$ ?



Watch Video Solution

5. (a) Find the wavelength of the radiation required to excite the electron in  $\text{Li}^{++}$  from the first to the third Bohr orbit (b) How many

spectral lines are observed in the emission spectrum of the above excited system?



**Watch Video Solution**

6. Find the wavelength present in the radiation emitted when hydrogen atoms emitted to  $n = 3$  states return to their ground state.



**Watch Video Solution**

7. How many different wavelengths may be observed in the spectrum from a hydrogen sample if the atoms excited to states with principal quantum number  $n$ ?



**Watch Video Solution**

8. Monochromatic radiation of wavelength  $\lambda$  is incident on a hydrogen sample in ground state hydrogen atoms absorb a fraction of

light and subsequently emit radiation of six different wavelength .Find the value of  $\lambda$



**Watch Video Solution**

9. The energy needed to detach the electron of a hydrogen like ion in ground state is a 4 Rydberg. (a) what is the wavelength of the radiation emitted when the electron jumps from the first excited state to the ground state? (b) What is the radius of the orbit for this atom?





**Watch Video Solution**

**10.** A hydrogen sample is prepared in a particular state A. A photon of energy  $2.55\text{eV}$  is observed to excite some of the electrons in the sample to take some of the electrons in a farther excited state B. Find the quantum numbers of the state A and B.



**Watch Video Solution**

**11. (a)** Find the maximum wavelength  $\lambda_{90}$  of light which can ionize a hydrogen atom in its

ground (b) light of wavelength  $\lambda_0$  is inclined on a hydrogen atom which is in its first excited state find the kinetic energy of the electron coming out



**Watch Video Solution**

**12.** Derive an expression for the magnetic field at the site of the nucleus in a hydrogen atom due to the circular motion of the electron. Assume that the atom is in its ground state.

and the answer in terms of fundamental constants



**Watch Video Solution**

**13.** A lithium atom has three electrons. Assume the following simple picture of the atom. Two electrons move close to the nucleus making up a spherical cloud, and the third moves outside the cloud in a circular orbit. Bohr's model can be used for the motion of this third electron but  $n = 1$  states are not available to it.

Calculate the ionization energy of lithium in ground state using the above picture.



**Watch Video Solution**

**14.** A particle known as mu meson has a charge equal to that of an electron and mass 208 times the mass of the electron. It moves in a circular orbit around a nucleus of charge  $+3e$ . Take the mass of the nucleus to be infinite. Assuming that the Bohr's model is applicable to this system (a) derive an expression for the

radius of the  $n$ th Bohr orbit (b) find the value of  $a$  for which the radius of the orbit is approximately the same as that at the first Bohr orbit for a hydrogen atom (c) find the wavelength of the radiation emitted when the electron makes a jump from the orbit to the first orbit



**Watch Video Solution**

**15.** Find the wavelength in a hydrogen spectrum between the range  $500\text{nm} \rightarrow 700\text{nm}$



Watch Video Solution

16. A beam of ultraviolet radiation having wavelength between  $100\text{nm}$  and  $200\text{nm}$  is incident on a sample of atomic hydrogen gas. Assuming that the atoms are in ground state, which wavelength will have low intensity in the transmitted beam? If the energy of a photon is equal to the ground state, it has a large probability of being absorbed by an atom in the ground state.



Watch Video Solution

17. A neutron moving with a speed  $v$  makes a head-on collision with a hydrogen atom in ground state kept at rest. Find the Minimum Kinetic Energy of Neutron for which inelastic collision will be take place is (assume that mass of h-atom is nearly equal to the mass of neutron)



**Watch Video Solution**

**18.** Light corresponding to the transition  $n = 4 \rightarrow n = 2$  in hydrogen atom falls on cesium metal (work function  $= 1.9eV$ ) Find the maximum kinetic energy of the photoelectrons emitted



**Watch Video Solution**

**19.** A small particle of mass  $m$  move in such a way the potential energy  $U = \frac{1}{2}m^2\omega^2r^2$  where  $\omega$  is a constant and  $r$  is the



distance of the particle from the origin.  
Assuming Bohr's model of quantization of angular momentum and circular orbits , show that radius of the  $n$ th allowed orbit is proportional to  $\sqrt{n}$



**Watch Video Solution**

## Short Answer

1. How many wavelength are emitted by atomic hydrogen in visible range ( $380nm - 780nm$ )

? In the range  $50\text{nm} \rightarrow 100\text{nm}$ ?



**Watch Video Solution**

2. The first excited energy of a  $He^+$  ion is the same as the ground state energy of hydrogen is it always true that one of the energies of any hydrogen like ion will be the same as the ground state energy of a hydrogen atom?



**Watch Video Solution**

3. Which wavelength will be emitting by a sample of atomic hydrogen gas (in ground state) if electron of energy  $12.2\text{eV}$  collide with the atoms of the gas?



**Watch Video Solution**

4. When white radiation is passed through a sample of hydrogen gas at room temperature , absorption lines are observed in lyman series only Explain





[Watch Video Solution](#)

5. Balmer series was observed and analysed before the other series .Can you suggest a reason for such an order?



[Watch Video Solution](#)

6. What will be the energy corresponding to the first excited state of a hydrogen atom if the potential energy of the atom is taken to be  $10eV$  when the electron is widely

separated from the proton ? Can be still write

$$E_n = E_1 / n^2, \text{ or } , r_n = a_0 n^2?$$



**Watch Video Solution**

7. The difference in the frequency of series limit of lyman series and balmer series is equal to the frequency of the first line of the lyman series Explain



**Watch Video Solution**

8. The numerical value of ionization in eV equals the ionization potential in volts. Does the equality hold if these quantities are measured in some other units?



**Watch Video Solution**

9. We have stimulated and spontaneous emission. Do we also have stimulated absorption and spontaneous absorption?



**Watch Video Solution**

**10.** An atom is in its excited state ,Does the probability of its coming to ground state depend on whether the radiation is already present or not? If you does it also depends on the wavelength of the radiation present?



**Watch Video Solution**

**Objective - I**

1. The minimum orbital angular momentum of the electron in a hydrogen atom is

A. a)  $h$

B. b)  $h / 2$

C. c)  $h / 2\pi$

D. d)  $h / \lambda$

**Answer: C**



**Watch Video Solution**



2. Three photons coming from excited atoms hydrogen sample are picked up. Their energies are  $12.1\text{eV}$ ,  $10.2\text{eV}$  and  $1.9\text{eV}$  these photons must come from

A. a simple atom

B. two atoms

C. three atoms

D. either two atoms or three atoms

**Answer: D**



**Watch Video Solution**

3. Suppose the electron in a hydrogen atom makes transition from  $n = 3 \rightarrow n = 2$  in  $10^{-8}s$  The order of the torque acting on the electron in this period, using the relation between torque and angular momentum as discussed in the chapter on rotational mechanics is

A.  $10^{-34}Nm$

B.  $10^{-24}Nm$

C.  $10^{-42}Nm$

D.  $10^{-8}Nm$

**Answer: B**



**Watch Video Solution**

**4.** In which of the following transition will the wavelength be minimum ?

A.  $n = 5 \rightarrow n = 4$

B.  $n = 4 \rightarrow n = 3$

C.  $n = 3 \rightarrow n = 2$

D.  $n = 2 \rightarrow n = 1$

**Answer: D**



**Watch Video Solution**

5. In which of the following system will the radius of the first orbit( $n = 1$ ) be minimum?

A. a) Hydrogen atom

B. b) Deuterium atom

C. c) Single ionized helium

D. d) Doubly ionized lithium

**Answer: D**



**Watch Video Solution**

6. In which of the following system will the wavelength corresponding to  $n = 2 \rightarrow n = 1$  be minimum ?

A. a) Hydrogen atom

B. b) Deuterium atom

C. c) Single ionized helium

D. d) Doubly ionized lithium

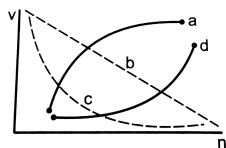
**Answer: D**



**Watch Video Solution**

7. Which of the following curve may represent the speed of the electron in a hydrogen atom as a function of the principal

quantum number  $n$ ?



A.



B.



C.



D.



**Answer: C**



**Watch Video Solution**

8. As one considers orbits with higher value of  $n$  in a hydrogen atom, the electron potential energy of the atom

- A. a) decreases
- B. b) increases
- C. c) remain the same
- D. d) does not increases

**Answer: B**



**Watch Video Solution**



9. The energy of an atom (or ion) in the ground state is  $-54.4\text{eV}$ . It may be?

A. a) Hydrogen

B. b) Deuterium

C. c)  $\text{He}^+$

D. d)  $\text{Li}^{++}$

**Answer: C**



**Watch Video Solution**

10. The radius of the shortest orbit in a one electron system is 18pm it may be

A. Hydrogen

B. deuterium

C.  $He^+$

D.  $Li^{++}$

**Answer: D**



**Watch Video Solution**

11. A hydrogen atom in ground state absorbs  $10.2\text{eV}$  of energy .The orbital angular momentum of the electron is increases by

A.  $1.05 \times 10^{-34} Js$

B.  $2.11 \times 10^{-34} Js$

C.  $3.16 \times 10^{-34} Js$

D.  $4.22 \times 10^{-34} Js$

**Answer: A**



**Watch Video Solution**

**12.** Which of the following parameters are the same for all hydrogen like atoms and ions in their ground state?

A. Radius of the orbit

B. Speed of the electron

C. Energy of the atom

D. Orbital angular momentum of the electron

**Answer: D**



**Watch Video Solution**

**13.** In a laser tube all the photons

- A. have same wavelength
- B. have same energy
- C. move in same direction
- D. move with same speed

**Answer: D**



**Watch Video Solution**

## Objective - II

1. In a laboratory experiment on emission from atomic hydrogen in a discharge tube only a small number of lines are observed whereas a large number of lines are present in the hydrogen spectrum of a star. This is because in a laboratory

A. the amount of hydrogen taken is smaller than that present in the star

B. the temperature of hydrogen is much smaller than that of the star

C. the pressure of hydrogen is much smaller than that of the star

D. the gravitational pull is much smaller than that of the star

**Answer: B**



**Watch Video Solution**

2. An electron with kinetic energy  $5eV$  is incident on a hydrogen atom in its ground state. The collision

- A. must be elastic
- B. may be partially elastic
- C. must be completely inelastic
- D. may be completely inelastic

**Answer: A**



**Watch Video Solution**



3. Which of the following products in a hydrogen atom are independent of the principal quantum number  $n$ ? The symbols have their usual meanings

A.  $u_n$

B.  $E_n$

C.  $E_{p_i}$

D.  $u_r$

**Answer: A::B**



**Watch Video Solution**

4. Let  $A_0$  be the area enclosed by the orbit in a hydrogen atom. The graph of  $\ln(A_0 / A_1)$  against  $\ln(n)$

- A. will pass through the origin
- B. will be a straight line with slope 4
- C. will be a monotonically increasing nonlinear curve
- D. will be a circle

**Answer: A::B**



**Watch Video Solution**

5. Ionization energy of a hydrogen like A is greater than that of another hydrogen like ion B. Let  $r$ ,  $u$ ,  $E$  and  $L$  represent the radius of the orbit, speed of the electron, energy of the atom, and orbital angular momentum of the electron respectively, in ground state

$$\text{A. } r_A > r_B$$

B.  $u_A > u_B$

C.  $E_A > E_B$

D.  $L_A > l_B$

**Answer: B**



**Watch Video Solution**

6. When a photon stimulates the emission of another photon the two photon have

A. same energy

B. same direction

C. same phase

D. same wavelength

**Answer: A::B::C::D**



**Watch Video Solution**

## Exercises

1. The bohr radius is given by  $a_0 = \frac{\epsilon_0 h^2}{\pi m e^2}$

verify that the RHS has dimesions of length



Watch Video Solution

2. Find the wavelength of the radiation by hydrogen in the transition (a)  $n = 3$  to  $n = 2$ , (b)  $n = 5$  to  $n = 4$  and (c)  $n = 10$  to  $n = 9$



Watch Video Solution

3. Calculate the smaller wavelength of radiation that may be emitted by (a) hydrogen (b)  $He^+$  and (c)  $Li^{++}$



**Watch Video Solution**

4. Evaluate Rydberg constant by putting the value of the fundamental constants in its expression



**Watch Video Solution**

5. Find the binding energy of a hydrogen atom in the state  $n = 2$



**Watch Video Solution**

6. Find the radius and energy of a  $He^{++}$  ion in the states (a)  $n = 1$ , (b)  $n = 4$  and (c)  $n = 10$  is



**Watch Video Solution**

7. A hydrogen atom emits ultraviolet of wavelength  $102.5nm$  what are the quantum number of the state involved in the transition?



**Watch Video Solution**



8. Find the first excitation potential of  $He^+$  ion (a) Find the ionization potential of  $Li^{++}$  ion



Watch Video Solution

9. A group of hydrogen atom are prepared in  $n = 4$  states list the wavelength that are emitted as the atoms make transition and return to  $n = 2$  states



Watch Video Solution

**10.** A positive ion having just one electron ejects it if a photon of wavelength  $228\text{\AA}$  or less is absorbed by it. Identify the ion



**Watch Video Solution**

**11.** Find the maximum coulomb force can act on the electron due to the nucleus in a hydrogen atom.



**Watch Video Solution**

12. A hydrogen atom in a having a binding of  $0.85\text{eV}$  makes transition to a state with excited energy  $10.2\text{eV}$  (a) identify the quantum number  $n$  of the upper and the lower energy state involved in the transition (b) Find the wavelength of the emitted radiation



**Watch Video Solution**

13. Whenever a photon is emitted by hydrogen in balmer series it is followed by another in

lyman series what wavelength does this latter photon correspond to?



**Watch Video Solution**

**14.** A hydrogen atom in state  $n = 6$  makes two successive transition and reaches the ground state in the first transition a photon of  $1.13\text{eV}$  is emitted (a) Find the energy of the photon emitted in the second transition (b) what is the value of  $n$  in the intermediate state?



**Watch Video Solution**

**15.** What is the energy of a hydrogen atom in the first excited state if the potential energy is taken to be zero in the ground state?



**Watch Video Solution**

**16.** A hot gas emits radiation of wavelength  $46.0nm$ ,  $82.8nm$  and  $103.5nm$  only. Assume that the atoms have only two excited states and the difference between consecutive energy levels decreases as energy is increased.

Taking the energy of the highest energy state to be zero find the energies of the ground state and the first excited state



**Watch Video Solution**

**17.** A gas of hydrogen like ions is prepared in a particular excited state A. if emit photons having wavelength equal to the wavelength of the first line of the lyman series together with photons of five other wavelength identify the

gas and find the principal quantum number of the state  $A$



**Watch Video Solution**

**18.** Find the maximum angular speed of the electron of a hydrogen atoms in a stationary orbit



**Watch Video Solution**

**19.** A spectroscopic instrument can resolve two nearly wavelength  $\lambda$  and  $\lambda + \Delta\lambda$  if  $\lambda/\Delta\lambda$  is smaller than 8000 This is used to study the spectral lines of the balmer series of hydrogen  
Approximately how many lines will be resolved by the instrument?



**Watch Video Solution**

**20.** Suppose in certine condition only those transition are allowed to hydrogen atoms in



which the principal quantum number  $n$  changes by 2 (a) Find the smaller wavelength emitted by hydrogen (b) list the wavelength emitted by hydrogen in the visible range ( $380\text{nm} \rightarrow 780\text{nm}$ )



**Watch Video Solution**

21. According to Maxwell's theory of electrodynamics, an electron going in a circle should emit radiation of frequency equal to the frequency of revolution what should be

the wavelength of the radiation emitted by a hydrogen atom in ground state if this rule is followed?



**Watch Video Solution**

**22.** The average kinetic energy of molecules in a gas at temperature  $T$  is  $1.5KT$  find the temperature at which the average kinetic energy of the molecules of hydrogen equals the binding energy of its atoms will hydrogen

remain in molecules form at this temperature ?

Take  $k = 8.62 \times 10^{-5} \text{ eV K}^{-1}$



**Watch Video Solution**

**23.** Find the temperature at which the average thermal kinetic energy is equal to the energy needed to take a hydrogen atom from its ground state  $n = 1$  state to  $n = 3$  state. Hydrogen can now emit red light of wavelength  $653.1 \text{ nm}$  because of Maxwellian distribution of speeds. A hydrogen sample emits red light at

temperature much lower than that obtained from this problem Assume that hydrogen that hydrogen molecules dissociate into atoms



**Watch Video Solution**

**24.** Average lifetime of a hydrogen atom excited to  $n = 2$  state  $10^{-6}s$  find the number of revolutions made by the electron on the average before it jumps to the ground state



**Watch Video Solution**

**25.** calculate the magnetic dipole moment corresponding to the motion of the electron in the ground state of a hydrogen atom



**Watch Video Solution**

**26.** Show that the ratio of the magnetic dipole moment to the angular momentum( $l = mvr$ ) is a universal constant for hydrogen atom and ions find the value



**Watch Video Solution**

27. A beam of light having wavelength distributed uniformly between  $450\text{nm} \rightarrow 550\text{nm}$  passes through a sample of hydrogen gas which wavelength will have the least intensity in the transition beam?



**Watch Video Solution**

28. Radiation coming from transition  $n = 2 \rightarrow n = 1$  of hydrogen atoms falls on helium in  $n = 1$  and  $n = 2$  state what are

the possible transition of helium ions as they absorb energy from the radiation?



**Watch Video Solution**

**29.** A hydrogen atom in ground state absorbs a photon of ultraviolet radiation of wavelength  $50\text{nm}$ . Assuming that the entire photon energy is taken up by the electron with what kinetic energy will the electron be ejected?



30. A parallel beam of light of wavelength  $100\text{nm}$  passes through a sample of atomic hydrogen gas in ground state (a) Assume that when a photon suppose some of its energy to a hydrogen atom the rest of the energy appears as another photon moving in the same direction as the incident photon Neglecting the light emitted by the excited hydrogen atom in the direction of the incident beam, ? (b) A radiation detector is placed near



the gas to detect radiation coming perpendicular to the incident beam find the wavelength of radiation that may be detected by the detector



**Watch Video Solution**

**31.** A beam of monochromatic light of wavelength  $\lambda$  ejects photoelectrons from a cesium ( $\phi = 1.9\text{eV}$ ) these photoelectrons are made to collide with H-atom in ground state . find the maximum value of  $\lambda$  for which (a)

hydrogen atoms may be ionised (b) hydrogen may get excited from the ground state to the first excited state and (c ) the excited hydrogen atoms may emit visible light



**Watch Video Solution**

**32.** Electron are emitted from an electron gun at almost zero velocity and are accelerated by an electric field  $E$  through a distance of  $1.0m$ . The electron are now scattered by an atomic hydrogen sample in ground state what should

be the minimum value of  $E$  so that red light of wavelength  $656.5\text{nm}$  may be emitted by the hydrogen?



**Watch Video Solution**

**33.** A neutron having kinetic energy  $12.5\text{eV}$  collides with a hydrogen atom at rest neglect the difference in mass between the neutron and the hydrogen atom and assume that the neutron does not leave its path of motion find the

possible kinetic energy of the neutron after the event



[Watch Video Solution](#)

**34.** A hydrogen atom moving at speed  $v$  collides with another hydrogen atom kept at rest .Find the minimum value of  $u$  for which one of the atoms may get ionized the mass of a hydrogen atom  $= 1.67 \times 10^{-27} kg$



[Watch Video Solution](#)

**35.** A neutron moving with a speed  $u$  strikes a hydrogen atom in ground state in ground toward it with the same speed Find the minimum speed of the neutron for which inelastic (completely or partially) collision may take place .The mass of neutron = mass of hydrogen  $= 1.67 \times 10^{-27} \text{ kg}$



**Watch Video Solution**

**36.** When a photon is emitted by a hydrogen atom , the photon carries a momentum with it

(a) calculate the momentum carried by the photon when a hydrogen atom emits light of wavelength  $656.3\text{nm}$  (b) with what speed does the atoms recoil during this transition? Take the mass of the hydrogen atom  $= 1.67 \times 10^{-27}\text{kg}$  (c) Find the kinetic energy of recoil of the atom



**Watch Video Solution**

**37.** When a photon is emitted from an atom , the atom recoils The kinetic energy of recoils

and the energy of the photon come from the difference in energy between the state involved in the transition suppose a hydrogen atom change its state from  $n = 3 \rightarrow n = 2$  calculate the fractional change in the wavelength of light emitted , due to the recoil



**Watch Video Solution**

**38.** The light emitted in the transition  $n = 3 \rightarrow n = 2$  in hydrogen is called  $H_{\alpha}$  light .Find the maximum work fonction a metel one

have so that  $H_{\alpha}$  light can emit photoelectrons from it



**Watch Video Solution**

**39.** Light from balmer series of hydrogen is able to eject photoelectron from a metal what can be the maximum work function of the metal?



**Watch Video Solution**



**40.** Radiation from hydrogen discharge tube falls on a cesium plate. Find the maximum possible kinetic energy of the photoelectron. work function of cesium is  $1.9\text{ eV}$



**Watch Video Solution**

**41.** A filter transmits only the radiation of wavelength greater than  $440\text{ nm}$ . Radiation from a hydrogen discharge tube goes through such a filter and is incident on a metal of work

function  $2.0\text{eV}$  . Find the stopping potential which can stop the photoelectrons.



**Watch Video Solution**

**42.** The earth revolves round the sun due to gravitational attraction. Suppose that the sun and the earth are point particle with their existing masses and that Bhors quantization rule for angular momentum is valid in the case of gravitation (a) Calculate the minimum radius the earth can have for its orbit. (b)

What is the value of the principle quantum number  $n$  for the present radius ? Mass of the earth =  $6.0 \times 10^{24}$  kg, mass of the sun =  $2.0 \times 10^{30}$  kg, earth-sun distance =  $1.5 \times 10^{11} m$ .



**Watch Video Solution**

**43.** Consider a neutron and an electron bound to each other due to gravitational force. Assuming Bohr's quantization rule angular momentum to be valid in this case, derive an

expression for the energy of the neutron-electron system.



**Watch Video Solution**

**44.** A uniform magnetic field  $B$  exists in a region. An electron projected perpendicular to the field goes in a circle. Assuming Bohr's quantization rule for angular momentum, calculate (a) the smallest possible radius of the electron's (b) the radius of the  $n$ th orbit

and (c) the minimum possible speed of the electron.



**Watch Video Solution**

**45.** Suppose in an imaginary world the angular momentum is quantized to be even integral multiples of  $\hbar/2\pi$ . What is the longest possible wavelength emitted by hydrogen atoms in visible range in such a world according to Bohr's model?



**Watch Video Solution**

**46.** Consider an excited hydrogen atom in state  $n$  moving with a velocity  $v$  ( $v < c$ ). It emits a photon in the direction of its motion and changes its state to a lower state  $m$ . Apply momentum and energy conservation principle to calculate the frequency  $\nu$  of the emitted radiation, compare this with the frequency  $\nu_0$  emitted if the atom were at rest.



**Watch Video Solution**