



MATHS

BOOKS - PRADEEP PUBLICATION

CONTINUITY AND DIFFERENTIABILITY

EXAMPLE

1. The function f defined as
$$f(x)=egin{cases} rac{\sin x^2}{x} & x
eq 0 \\ 0 & 0 \end{cases}$$
 is :

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2. Discuss the continuity of the function $f(x) = egin{cases} x^2 & x \leq 0 \ 1-x & x > 0 \end{bmatrix} atx = 0$

3. Find the value of
$$f\left(\frac{\pi}{4}\right)$$
 so that the function $f(x) = \frac{\sqrt{2}\cos x - 1}{\cot x - 1}, x \neq \frac{\pi}{4}$, becomes continuous at $x = \frac{\pi}{4}$
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4. Find the relationship between a and b so that the function f defined by:

 $f(x) = egin{cases} ax+1 & ext{if} \quad x\leq 3 \ bx+3 & ext{if} \quad x>3 \end{cases}$ is continuous at x=3

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5. Find the relationship between a and b so that the function f defined by:

$$f(x) = egin{cases} ax+1 & ext{if} \quad x \leq 3 \ bx+3 & ext{if} \quad x > 3 \end{cases}$$
 is continuous at $x=3$

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6. Discuss the continuity of the function :

$$f(x) = egin{cases} rac{ert x-aert}{x-a} & whenx
eq a \ 1 & whenx = a \end{cases}$$
 at x = a

7. Let
$$f(x) = \begin{cases} rac{\sin x}{x} + \cos x & when x
eq 0 \\ 2 & when x = 0 \end{cases}$$
 show that f (x) is continouous

at x = 0.

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8. Let 'f' be the function defined by $f(x) = rac{\sqrt{4+x}-2}{x}, x
eq 0.$ What

choice, if any, of f (0) will make it continuous at x = 0?

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9. If
$$f(x)=egin{cases} rac{x^3+x^2-16x+20}{\left(x-2
ight)^2} & x
eq 2\ k & x=2 \end{cases}$$
 is continuous at x =2, find the value

of 'k'.



10. If the function $f(x) = egin{cases} 3ax+b & ext{if} \quad x>1 \ 11 & ext{if} \quad x=1 \ 1x = 1 \ 5ax-2b & ext{if} \quad x<1 \end{cases}$

1, find the values of a,b.

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11. Find a,b so that the function $f(x) = egin{cases} 1 & x \leq 3 \\ ax+b & 3 < x < 5 \\ 7 & x \geq 5 \end{cases}$ may be

continuous at x = 3 and x = 5

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12. Let
$$f(X) = \begin{cases} (x-1)\tan\left(\frac{\pi}{2}x\right) & x \neq 1 \\ k & x = 1 \end{cases}$$
. Find k if f is continuous at x = 1.

13. Find a for which the function f defined as
$$\left(f(x) = \left\{ \left[\left(a \sin\left(\frac{\pi}{2}\right)(x+1) \text{ if } x \le 0\right], \left[\left(\frac{\tan x - \sin x}{x^3}\right) \text{ if } x > 0\right] \right\} \right\}$$
is continuous at $(x = 0)$.

nuous at (x= 0).

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that the function is continuous at x = 0, is.....

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15. Determine the value of the constant k so that the function

$$f(x)=\left\{egin{array}{ccc} rac{\sin 2x}{5x} & ext{if} & x
eq 0\ k & ext{if} & x=0 \end{array}
ight.$$
 is continuous at x = 0

16. Examine
 for
 continuity,
 the
 function

$$f(x) = \begin{cases} |x - a| \sin\left(\frac{1}{x - a}\right) & \text{if } x \neq a \\ 0 & \text{if } x = a \end{cases}$$
 Image: the second sec

17. Let
$$f(x)= egin{cases} rac{1-\cos 2x}{2x^2} & x<0\ k & x=0$$
 . Find k if f is continous at x =0 $rac{x}{|x|} & x>0 \end{cases}$

18. Examine for continuity, the function 'f' defined by $f(x) = \begin{cases} e^{1/x} & x \neq 0 \\ 0 & x = 0 \end{cases} \text{ at } x = 0$ Watch Video Solution

19. Discuss the continuity of fx) at x =0, when:

$$f(x) = \left\{egin{array}{c} rac{e^{1/x}-1}{e^{1/x}+1} & x
eq 0\ 0 & x=0 \end{array}
ight.$$

20. The function
$$f(x) = rac{\log(1+ax) - \log(1-bx)}{x}$$
 is not defined at x =

0. Find the value of f(0) so that f is continuous at x = 0

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21. Let f(x) = [x] + [-x] for $x \neq 0$ and $f(0) = \lambda$. For what value of λ , if any, is f

continuous at x = 0?

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22. Examine for cotinuity the function $f(x) = \begin{cases} 2+x & ext{if } x < 0 \\ -x+2 & ext{if } x > 0 \end{cases}$

23. Prove that the function
$$f(x)= egin{cases} rac{\sin x}{x} & x < 0 \ x^2+1 & x \geq 0 \end{cases}$$
 is continuous.



26. Show that the function $f(x) = \begin{cases} x+\lambda & x<1\\ \lambda x^2+1 & x\geq 1 \end{cases}$ is a continous

function. Regardless of the choice of $\lambda \in R.$

27. Find all the points of discontinuity of the function f defined by

$$f(x) = egin{cases} x &+ & 2 & ext{ if } x < 1 \ 0 & ext{ if } x = 1 \ x &- & 2 & ext{ if } x > 1 \end{cases}$$

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28. Locate the points of discontinuity of the function
$$f(x) = \begin{cases} (|x|+3) & \text{if } x \leq -3 \\ -2x & \text{if } -3 < x < 3 \\ 6x+2 & \text{if } x \geq 3 \end{cases}$$

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29. Let
$$f(x)= egin{cases} 1&x\leq -1\\ \lambda x+\mu &-1< x<3 ext{ find }\lambda ext{ and }\mu ext{ if f is a continuous}\\ 5&x\geq 3 \end{bmatrix}$$

function.

30. Prove that the following functions are continuous:



33. Find the domain of the continuity of the following functions:

 $\sin^{-1}x - [x]$



34. Find the domain of the continuity of the following functions:

 $\sin^{-1}x-[x]$

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35. Find the domain of the continuity of the following functions:

$$\frac{\log x}{\sqrt{1-4x^2}}$$

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36. Let
$$f(x) = (x-a) \cos \left(rac{1}{x-a}
ight) f$$
 or $x
eq a$ and le f (a) = 0. Show

that f is continuous at x = a but not derivable thereat.

37. Show that the function $f(x) = \begin{cases} x^n \sin\left(rac{1}{x}\right) & x
eq 0 \\ 0 & x = 0 \end{cases}$ is continuous

but not differentiable at x= 0.

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38. Show that the function
$$f(x) = \begin{cases} x^n \sin\left(rac{1}{x}\right) & x \neq 0 \\ 0 & x = 0 \end{cases}$$
 is continuous

but not differentiable at x= 0.

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39. Show that the function
$$f(x) = \begin{cases} x^n \sin\left(rac{1}{x}\right) & x
eq 0 \\ 0 & x = 0 \end{cases}$$
 is continuous

but not differentiable at x= 0.

40. Let f(x) = x|x| for all $x \in R$. Discuss continuity and derivability of f(X) at

x = 0



41. Show that f(x) = |x - 5| is continuous but not differentiable at x = 5.

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42. Show that the function $f(x) = |x-1| + 1 \mid f ext{ or } all x \in R$, is not

differentiable at x = -1 and x =1

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43. Let $f(x) = egin{cases} x+a & x\leq 1 \\ ax^2+1 & x>1 \end{bmatrix}$. Show that f is continuous at 1. Find 'a'

so that it is derivable at 1.

44. For what values of 'a' and 'b' the function:

$$f(x) = egin{cases} x^2 & x \leq c \ ax+b & x > c \end{cases}$$
 is differentiable at x =c.

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45. Show that the function defined by:

$$f(x) : egin{cases} 3-2x & ext{if} \quad x < 2 \ 3x-7 & ext{if} \quad x \geq 2 \end{cases}$$
 is not derivable at x =2.

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46. find derivative, find f' (2) when $f(x) = 5^{3x}$

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47. Let $f(x) = \log x$, Evaluate f' (e).



52. Find
$$rac{dy}{dx}$$
 when $y=e^x\log x$



53. Find
$$rac{dy}{dx}$$
 when $y=rac{e^x-1}{e^x+1}$

54. Find
$$rac{dy}{dx}$$
 when $y=rac{1-\log x}{1+\log x}$

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55. Find
$$\displaystyle rac{dy}{dx}$$
 when $\displaystyle y=a^{x}x^{a}, a>0$

56. Find
$$rac{dy}{dx}$$
 when $y=rac{e^x}{1+\sin x}$



61. Find
$$\left(rac{dy}{dx}
ight)$$
 when $y=2u^3+1\,\, ext{and}\,\,u=rac{1}{x^{2/3}}$

C

62. Differentiate
$$\left|2x^2-1\right|$$
 w.r.t.x.

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63. Differentiate
$$f(x) = \left(x+2
ight)^{2/3}\!\left(1-x
ight)^1/3
ight)w.\,r.\,t.\,x$$

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64. If
$$y = \log\left\{\left(e^x rac{\left(rac{x-2}{x+2}
ight)^3}{4}
ight)
ight\}$$
, show that $rac{dy}{dx} = rac{x^2-1}{x^2-4}$

65. Find the derivative of the function $\sqrt{a+\sqrt{a+x}}$ w.r.t.x

66. if
$$y=\sqrt{rac{1-x}{1+x}}$$
, prove that $:(1-x)^2igg(rac{dy}{dx}igg)+y=0$

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67. Find the derivatives of following w.r.t.x

$$\sqrt{3x-2}, x>rac{2}{3}$$

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68. Find the derivatives of following w.r.t.x

$$\left(4x^3-5x^2+1
ight)^4$$

69. Use Chain Rule to find the derivatives of the following:

$$f(x) = ig(2x^2+3ig)^{rac{5}{3}}(x+5)^{-rac{1}{3}}$$



70. Differentiate the following w.r.t. x:

$$\sqrt{3x+2}+rac{1}{\sqrt{2x^2+4}}$$

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71. Find
$$rac{dy}{dx}$$
 when $y=rac{\sqrt{x+a}-\sqrt{x-a}}{\sqrt{x-a}+\sqrt{x+a}}$, where x > a > 0

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72. Differentiate the following w.r.t.x: $\sin x^3$



77. Differentiate the followig w.r.t.x:



81. Differentiate the following w.r.t.x.

$$\log \sqrt{rac{1-\cos x}{1+\cos x}}$$

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82. Differentiate the following functions w.r.t.x

 $\log_7(\log x)$

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83. Find the derivative of
$$\cosig(\sin x^2ig) atx = \sqrt{ig(rac{\pi}{2}ig)}$$

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84. Differentiate the following functions w.r.t.x.

 $e^{\sin\sqrt{x}}$

85. Differentiate the following functions w.r.t.x.

$$\log\Bigl\{ an\Bigl(rac{\pi}{4}+rac{x}{2}\Bigr) \Bigr\}$$

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$$\log\!\left(rac{x+\sqrt{x^2-a^2}}{x-\sqrt{x^2-a^2}}
ight)$$

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87. If
$$y = f\left(rac{2x-1}{x^2+1}
ight)$$
 and $f'(x) = \sin x^2$, then find $rac{dy}{dx}$.

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88. Find
$$rac{dy}{dx}$$
 when $y=\sqrt{a+\sqrt{a}+\sqrt{a}+x^2}\Big)\Big)$, 'a' being constant.

89.
$$y=rac{\cos x+\sin x}{\cos x-\sin x}, provet^{-}$$
dy/dx = $\mathrm{sec}^{2}\Big(rac{\pi}{4}+x\Big)$

90. If
$$y = rac{e^x - e^{-x}}{e^x + e^{-x}}.$$
 Prove that $rac{dy}{dx} = 1 - y^2$

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91. If
$$y=\sqrt{rac{1+e^x}{1-e^x}}, ext{ show that } rac{dy}{dx}=rac{e^x}{(1-e^x)\sqrt{1-e^2x}}, x<0$$

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92. If
$$y = \log \left| rac{a - b \cos x}{a + b \cos x} \right|$$
, then show that $rac{dy}{dy} = rac{2ab \sin x}{a^2 - b^2 \cos^2 x}$

93. If
$$y=e^{3\log x+2x}$$
 , prove that $rac{dy}{dx}=x^2(2x+3)e^{2x}$

94. If
$$y=rac{\log \left(x+\sqrt{x^2+1}
ight)}{\sqrt{x^2+1}}$$
 , prove that $ig(x^2+1)rac{dy}{dx}+xy=1$

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95. If
$$x=rac{1-t^2}{1+t^2}\,\, ext{and}\,\,y=rac{2t}{1+t^2}$$
 , then show that $\left(rac{dy}{dx}
ight)+rac{x}{y}=0$

96. For a positive constant a find
$$\frac{dy}{dx}$$
, where $y = a^{t + \left(\frac{1}{t}\right)}$, and $x = \left(t + \frac{1}{t}\right)^a$
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97. If
$$x = a(\sin \theta - \theta \cos \theta)$$
 and $y = a(\cos \theta + \theta \sin \theta)$ find dy/dx at $\theta = \frac{\pi}{4}$



98. Differntiate
$$\sin^2 ig(heta^2 + 1 ig) w. \, r. \, t heta$$

99. Differenitiate $\sin^2 x$ w.r.t. $e^{\cos x}$

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100. Find
$$\frac{dy}{dx}$$
, when $x = a\left(\cos t + \log\left|\frac{\tan t}{2}\right|\right)$ and $y = a\sin t, 0 < t < \frac{\pi}{2}$

101. If
$$x = e^{\cos 2t}$$
 and $y = e^{\sin 2t}$, then prove that $\frac{dy}{dx} = \frac{-y \log x}{x \log y}$.
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102. If $x = \sqrt{a^{\sin^{-1}t}}$, $y = \sqrt{a^{\cos^{-1}t}}$, show that $\frac{dy}{dx} = -\frac{y}{x}$, $a > 0$
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103. Find $\frac{dy}{dx}$ at $t = \frac{\pi}{4}$ when $xe^{-t}(\sin t + \cos t)$ and $y = e^{-t}(\sin t - \cos t)$
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104. If $x = a \sin 2 t(1+\cos 2t)$ and $y = b \cos 2t(1-\cos 2t)$, find: the value of

$$rac{dy}{dx}att=rac{\pi}{4} ext{ and } t=rac{\pi}{3}$$

105. if $x = \sec \theta - \cos \theta$ and $y = \sec^n \theta - \cos^n \theta$, then show that $(x^2 + 4) \left(\frac{dy}{dx}\right)^2 = n^2 (y^2 + 4)$

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106. Find
$$\frac{dy}{dx}$$
 when $y = \sin^{-1}\left(\frac{\sqrt{x}-1}{\sqrt{x}+1}\right) + \sec^{-1}\left(\frac{\sqrt{x}+1}{\sqrt{x}-1}\right)$, x > 1`

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107. Differentiate the following functions w.r.t.x

$$\sqrt{\sin^{-1}\sqrt{x}}$$



108. Differentiate the following functions w.r.t.x

$$\cot^{-1}\left(rac{1+x}{1-x}
ight)$$

109. Differentiate the following functions w.r.t.x

$$\sin^{-1} igg(rac{2^{x+1}}{1+4^x} igg)$$



110. Differntiate the following functions w.r.t.x

 $x^2 \cot^{-1} \sqrt{x}$

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111. Differentiate the following functions w.r.t. $tan^{-1}(sin x + cos x)$







121. Differntiate the following functions w.r.t.x
$$\cos(2\sin - 1x) + \sin(2\sin^{-1}x)$$

122. Find
$$rac{dy}{dx}$$
 when: $y=\sin^{-1}igg(rac{2x}{1+x^2}igg)$

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123. Find
$$rac{dy}{dx}$$
 when y = $\cos^{-1}\left(rac{3\cos x - 4\sin x}{5}
ight)$

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124. Find
$$rac{dy}{dx}$$
 if $y=\sin^{-1}\left[rac{6x-4\sqrt{1-4x^2}}{5}
ight]$

125. If
$$y= an^{-1}igg(2rac{x}{1-x^2}igg)+\cos^{-1}igg(rac{1-x^2}{1+x^2}igg), f\in d$$
dy/dx $when$ x in

126. If
$$y = an^{-1} \left(2 rac{x}{1-x^2}
ight) + \cos^{-1} \left(rac{1-x^2}{1+x^2}
ight), f \in d ext{dy/dx} when x$$
 in (0,1)`

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127. If
$$y= an^{-1}igg(rac{2x}{1-x^2}igg)+\cos^{-1}igg(rac{1-x^2}{1+x^2}igg), f\in d$$
dy/dx $when$ x in (1,

infty)`

128. If
$$y= an^{-1}igg(2rac{x}{1-x^2}igg)+\cos^{-1}igg(rac{1-x^2}{1+x^2}igg), f\in d$$
dy/dx $when$ x in

129. If
$$y= an^{-1}\left(rac{2x}{1-x^2}
ight)+\cos^{-1}\left(rac{1-x^2}{1+x^2}
ight)$$
, find $rac{dy}{dx}$ when $x\in(-\infty,\ -1)$

130. Find the derivative of
$$\sec^{-1}\left(\frac{1}{2x^2-1}\right)$$
 w.r.t. $\sqrt{1-x^2}$ at $x=\frac{1}{2}$.
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131. Differentiate
$$\sec^{-1}\left(rac{1}{2x^2-1}
ight)w.\ r.\ t\sin^{-1}ig(3x-4x^3ig)$$

132. Differentiate
$$an^{-1}\left(rac{\sqrt{1+x^2}-1}{x}
ight)$$
 w.r.t. $\sin^{-1}\left(rac{2x}{1+x^2}
ight)$.

133. Differentiate
$$an^{-1} \left(rac{\sqrt{1-x^2}}{x}
ight)$$
 w.r.t. $\cos^{-1} \left(2x \sqrt{1-x^2}
ight)$

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134. If
$$y=\sin^{-1}\Big[x\sqrt{1-x}-\sqrt{x}\Big(\sqrt{1-x^2}\Big)\Big]$$
 find $rac{dy}{dx}$

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135. If
$$y=\sin^{-1}igg(rac{\sinlpha\sin x}{1-\coslpha\sin x}igg)$$
 , find y'(0)
136. Find
$$\displaystyle rac{dy}{dx}$$
 in the following : $ax^2+2hxy+by^2+2gx+2+y+c=0$

137. Find
$$\displaystyle rac{dy}{dx}$$
 if $\displaystyle x^{rac{2}{3}}+y^{rac{2}{3}}=a^{rac{2}{3}}$

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138. Find
$$rac{dy}{dx}$$
 if $\sin(x-y)=3x$

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139. Find
$$rac{dy}{dx}$$
 where $e^x \log y = \sin^{-1} x + \sin^{-1} y$

140. If y = x sin y, prove that
$$x \frac{dy}{dx} = \frac{y}{1 - x \cos y}$$



141. If
$$\sin y = x \sin(a+y)$$
, prove that $\displaystyle rac{dy}{dx} = \displaystyle rac{\sin^2(a+y)}{\sin a}$

142. If
$$y = b an^{-1} \Big\{ rac{x}{a} + an^{-1} \Big(rac{y}{x} \Big) \Big\}, ext{ find } rac{dy}{dx}$$

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143. If
$$\log \left(x^2+y^2
ight)=2 an^{-1}\Big(rac{y}{x}\Big),\,$$
 then show that $rac{dy}{dx}=rac{x+y}{x-y}.$

144. If
$$\tan^{-1}\left(\frac{x^2 - y^2}{x^2 + y^2}\right) = a$$
, provet $\frac{\widehat{dy}}{dx} = x \frac{1 - \tan a}{y(1 + \tan a)}$
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145. If $\sqrt{y + x} + \sqrt{y - x} = a$, then show that $\frac{dy}{dx} = 2\frac{x}{a^2}$
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146. If $x\sqrt{1 + y} + y\sqrt{1 + x} = 0$ show that $\frac{dy}{dx} = -\frac{1}{(1 + x)^2}$
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147. If
$$y\sqrt{1-x^2}+x\sqrt{1-y^2}=1$$
 , then prove that $\displaystyle rac{dy}{dx}=-\sqrt{rac{1-y^2}{1-x^2}}$

148. Differentiate the following functions w.r.t. x

$$\frac{e^{x^2}\tan^{-1}x}{\sqrt{1+x^2}}, x>0$$

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149. Differentiate the following functions w.r.t. x

$$igg(xrac{\sqrt{x^2+4}}{(3x+2)^{2/3}},x>0igg)$$

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150. Find
$$rac{dy}{dx}$$
 when $y=x^{\log x}+\left(\log x
ight)^x, x>1$

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151. If
$$x^y = e^{x-y}$$
, prove that $\displaystyle rac{dy}{dx} = \displaystyle rac{\log x}{\left\{ \log(xe)
ight\}^2}$



156. Differentiate the following functions w.r.t.x

 $(\log x)^x + x^{\log x}$

157. Find
$$\displaystyle rac{dy}{dx}$$
 if $x^y+y^x=a^b$

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158. Find
$$\frac{dy}{dx}$$
 when $(\cos x)^y = (\cos y)^x$

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159. Find
$$\displaystyle rac{dy}{dx}$$
 when $\displaystyle y = 10^{10^x} + 10^{x^x} + 10^{x^{10}}$

160. Find
$$rac{dy}{dx}$$
 when $x^y=y^x$

161. Find
$$\displaystyle rac{dy}{dx}$$
 when $\displaystyle y=10^{x^{10^x}}$

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162. If
$$y = (\log_{\cos x} \sin x) (\log_{\sin x} \cos x)^{-1} + \sin^{-1} \left(\frac{2x}{1+x^2} \right)$$
, find $\frac{dy}{dx} atx = \frac{\pi}{4}$

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163. Verify Rolle's Theorem for the function $f(x) = x^2 + x - 6$ in the interval [-3,2]

164. Verify Rolle's theorem for the function $f(x)=x^3-9x^2+26x-24$

in the interval [2,4]



166. Verify Rolle's Theorem for the function $f(x) = \cos\left\{2\left(x - \frac{\pi}{4}\right)\right\}$ in the interval $\left[0, \frac{\pi}{2}\right]$

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167. Verify Rolle's theorem for function $f(x) = e^x \cos x$ in the interval

$$\Big[-\frac{\pi}{2},\frac{\pi}{2}\Big].$$



168. Differentiate the following

 $\log(\tan x)$

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169. Find the derivative of $an 5x + \sin 4x$

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170. Verify Lagrange's Mean value Theorem (LMV.) for the function f(x) =

x(2-x) in [0,1]`



171. Verify lagrange mean value theorem for the function $f(x) = 2x^2 - 10x + 29$ in the interval [2,7]



173. Verify Lagrange's Mean Value Theorem for the function f defined by

 $f(x)=x^3+x^2-6x$ in the interval [-1,4]



174. Find 'c' of Lagrange's Mean Value Theorem for the functions:

 $f(x)=e^x$ in the interval [0,1]

175. Find 'c' of Lagrange's Mean Value Theorem for the functions:

 $f(x) = \log x$ in the interval [1,e]



176. Find a point on the parabola $y = (x - 3)^2$, where the tangent s parallel to the chord joining (3,0) and (4,1)

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177. Does Lagrange's mean value theorem apply to $f(x) = x^{1/3}, \ -1 \le x \le 1.$ What conclusions can be drawn?

178. Let
$$f(x)$$
 $\begin{cases} 2+x^3f ext{ or } x\leq 1\\ 3xf ext{ or } x>1 \end{cases}$ Verify Lagrange's mean value theorem for the function `f(x) on [-1,2]



EXERCISE

1. Examine the continuity of
$$f(x)=\left\{egin{array}{c} rac{x^2-9}{x-3} & x
eq 3\ 6 & x=3 \end{array}
ight.$$
 at x = 3`

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2. If
$$f(X) = rac{x^2-1}{x-1}$$
 for $x
eq 1$ and f(x) = 2 when x = 1. Show that the

function f(X) is continuous at x = 1.

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3. The value of the constant k so that the function
$$f(x) = \begin{cases} rac{x^2 - 3x + 2}{x - 1} &, ext{ if } x
eq 1 \\ k &, ext{ if } x = 1 \end{cases}$$
 is continuous at x = 1 is

4. The constant k, so that the $f(x)= egin{cases} rac{x^2-2x-3}{x+1} & ext{if} \quad x
eq -1 \ k & ext{if} \quad x=-1 \end{cases}$ is

continuous at x = -1 is

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5. Examine the function
$$f(X) = \begin{cases} rac{1-\cos 3x}{x} & x \neq 0 \\ 0 & x = 0 \end{cases}$$
 for continuity at x =

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6. For what value of k, function f(x) is continuous at x = 0 where

$$f(x)=\left\{ egin{array}{c} rac{1-\cos4x}{8x^2}, \, ig(egin{array}{c} x
eq 0\ x=0 \end{array}
ight)$$

7. A function f(x) is defined as $f(x) = \left\{egin{array}{cc} rac{x^2-x-6}{x-3} & x
eq 3 \ 5 & x=3 \end{array}
ight.$ show that f(X)

is continous at x = 3.

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8. Discuss the continuity of the function f(x), where $f(x) = \begin{cases} 2-x & x < 0 \\ 2+x & x \ge 0 \end{cases}$, at x = 2,0 and -2.

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9. Discuss the continuity of the function f(x)atx=0 , where

$$f(x) = egin{cases} \left(egin{array}{c} |x| \ x \end{pmatrix} & x
eq 0 \ 0 & x = 0 \end{array}
ight.$$

10. Discuss the continuity of the function f(x) at x = 2, where $f(x)=egin{cases} 3x+5 & ext{if} & x\geq 2\ x^2 & ext{if} & x<2 \end{cases}$

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11. Discuss continuity of
$$f(X) = egin{cases} -1 & x < 0 \ 2 - x & x \ge 0 \end{bmatrix}$$
 at x = 0

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12. Examine the following functions for continuity:

$$f(x) = \left\{egin{array}{cc} rac{2x^2-3x-2}{x-2} & x
eq 2\ 3 & x=2 \end{array}
ight.$$

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13. Examine the following functions for continuity:

$$f(x) = egin{cases} x+a & x < 1 \ ax^2+1 & x \geq 1 \end{cases}$$
 at x = 1

 14. Examine the following functions for continuity:

$$f(x) = egin{cases} rac{|x-3|}{2(x-3)} & ext{if} \ x
eq 3 \ 0 & ext{if} \ x = 3 \end{cases}$$
 at x = 3

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15. Examine the following functions for continuity:

$$f(x)=\left\{egin{array}{cc} rac{x-ert xert}{x} & x
eq 0\ 2 & x=0 \end{array}
ight.$$
at x = 0

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16. Examine the following functions for continuity:

$$f(x) = \left\{egin{array}{cc} \left(rac{x^2}{2}
ight) & ext{if} & 0 \leq x \leq 1 \ 2x^2 - 3x + rac{3}{2} & ext{if} & 1 < x \leq 2 \end{array}
ight.$$
at x = 1

17. Examine the following functions for continuity:

$$f(x) = \left|x\right| + \left|x - 1\right|$$

at x = 1

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18. Examine the continuity of the function
$$f(x) = \begin{cases} 3x - 2 & x \le 0 \\ x + 1 & x > 0 \end{cases} atx = 0$$
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19. Is the function
$$f(X) = \begin{cases} rac{1-x^n}{1-x} & x
eq 1 \\ n-1 & x = 1 \end{cases}$$
, $\mathsf{n} \in \mathsf{N}$ continuous at x =1?

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20. If
$$f(x)= egin{cases} rac{x}{|x|+2x^2}, & x
eq 0 \ k, & x=0 \end{cases}$$

Prove that f(x) remain discontinous at x = 0 for any real value of k.

21. Determine the value of the constant k so that the function

$$f(x)= egin{cases} rac{\sin 2x}{5x} & ext{ if } x
eq 0 \ k & ext{ if } x=0 \end{cases}$$
 is continuous at x = 0

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22. Determine the value of the constant k so that the function

$$f(x) = egin{cases} rac{\sin kx}{x} & x
eq 0 \ 4+x & x=0 \end{cases}$$
 is continuous at 0.

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23. Determine the value of the constant k so that the function $f(x) = \begin{cases} 3x - 8 & \text{if } x \leq 5 \\ 2k & \text{if } x > 5 \end{cases}$ is continuous at x = 5

24. Determine the value of the constant k so that the function (1 + 1)

$$f(x) = egin{cases} \kappa x + 1 & ext{if } x \leq \pi \ \cos x & ext{if } x > \pi \end{cases}$$
 is continuous at $\mathsf{x} = \pi.$

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25. Determine the value of the constant k so that the function

 $f(x) = egin{cases} kx+1 & ext{if} \ x\leq 5\ 3x-5 & ext{if} \ x>5 \end{cases}$ is continuous at x = 5.

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26. Determine the value of the constant k so that the function

$$f(x)=egin{cases} kig(x^2+2ig) & ext{if} \ \ x\leq 0\ 3x+1 & ext{if} \ \ x>0 \end{cases}$$
 is continuous at x = 0

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27. Determine the value of the constant k so that the function $f(x) = \begin{cases} 2x^2 + k & ext{if } x \ge 0 \\ -2x^2 + 4 & ext{if } x < 0 \end{cases}$ is continuous at x = 0

28. Find the values of a so that the function f defined by $f(X) = \begin{cases} \frac{\sin^2 ax}{x^2} & x \neq 0\\ 1 & x = 0 \end{cases}$ may be continuous at x = 0. Watch Video Solution

29. Find the value of a if the function f defined by $f(x) = \begin{cases} 2x - 1 & x < 2 \\ a & x = 2 \\ x + 1 & x > 2 \end{cases}$ is continuous at x = 2.

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30. Show that the function f(x) = |x + 1| + |x - 1| is continuous at x = -1, x = 1

31. Consider the functions defined as follows, for $x \neq 0$. In each case, what choice (if any) of f(0) will make it continuous at x = 0? $f(x)=rac{3x+4 an x}{x}$

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32. Consider the functions defined as follows, for $x \neq 0$. In each case, what choice (if any) of f(0) will make it continuous at x = 0?

 $f(x)=rac{3x+4 an x}{x}$

A. Consider the functions defined as follows, for $x \neq 0$. In each case,

what choice (if any) of f(0) will make it continuous at x = 0?

$$f(x)=rac{3x+4 an x}{x}$$

Β.

C.

D.

33. Find a
$$\in$$
 R so that $f(x) = egin{cases} x^2 & x \geq 0 \\ ax & x < 0 \end{bmatrix}$ is continuous at 0.

34. Find
$$k\in R$$
 if $f(x)= egin{cases} rac{\cos^2x-\sin^2x-1}{\sqrt{x^2+1}-1} & x
eq 0 \\ k & x=0 \end{cases}$ is continuous at 0.

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35. Let
$$f(x) = \begin{cases} rac{1-\cos ax}{x\sin x} & x
eq 0 \\ rac{1}{2} & ext{if } x = 0 \end{cases}$$
 If f is continuous at x=0, find a.

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36. Find the value of the constant k so that function

$$f(x)= egin{cases} rac{k\cos x}{\pi-2\pi} & ext{if} x
eq rac{\pi}{2} \ 3 & ext{if} \ x=rac{\pi}{2} \end{cases}$$
 is continuous at $x=rac{\pi}{2}$

37. Examine the following functions for continuity:

$$f(x)= egin{cases} x^nrac{\sin 1}{x} & x
eq 0\ - & x=0 \end{cases}$$
 at x = 0, where n $\ \geq \ 1.$

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38. Examine the following functions for continuity:

$$f(x) = egin{cases} x\cos\left(rac{1}{x}
ight) & x
eq 0 \ 0 & x = 0 \end{cases}$$
 at x = 0

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39. Examine the following functions for continuity:

$$f(x)=egin{cases} (x-a) \cos \Bigl(rac{1}{x-a}\Bigr) & x
eq a\ 0 & x=a \end{cases}$$
at x = a

40. Examine the following functions for continuity:

$$f(x)=\left\{egin{array}{cc} e^{1/x} & x
eq 0\ 1 & x=0 \end{array}
ight.$$
at x = 0

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41. If
$$f(x)= \left\{ egin{array}{ccc} rac{x^2-(a+2)\,x+a}{x-2} & x
eq 2 \\ 2 & x=2 \end{array}
ight.$$
 is continuous at x =2, then the

value of a is

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42. Find f(0) if the function defined as
$$f(x) = \begin{cases} \frac{\log(1 + \frac{x}{a}) - \log(1 - \frac{x}{b})}{x} (f \text{ or } x \neq 0), \text{ is continuous at } x = \\ 0. \text{ ab } \neq 0 \end{cases}$$

43. For what value of λ is the function defined by $f(x) = \{\lambda(x^2 - 2x), \text{ if } x \leq 0, 4x + 1, \text{ if } x > 0\}$ continuous at x = 0? What about continuity at x = 1?

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44. Show that the function defined by g(x) = x - [x] is discontinuous at all integral points. Here [x] denotes the greatest integer less than or equal to x.

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45. Show that the function $f(x) = |\sin x + \cos x|$ is continuous at $x = \pi$.



46. Extend the defination of the function
$$f(x) = rac{1-\cos[7(x-\pi)]}{5(x-\pi)^2}, x
eq \pi$$
 by continuity at $x=\pi$

47. Let
$$f(x) = \begin{cases} 4x - 3 & ext{if} \quad x < 0 \\ 4x + 3 & ext{if} \quad x \ge 0 \end{cases}$$
. Is it a continuous function? Justify

your answer.

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48. Prove that the following functions are continuous at all points of their

domains: $f(x) = \cos x$



49. Prove that the following functions are continuous:

cot x



53. Prove that the following functions are continuous:

|x + 1| + |x| Solution

54. Prove that the following functions are continuous:

sin |x|

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55. Prove that the following functions are continuous:

|sin x|

Watch Video Solution

56. Prove that the following functions are continuous:

|cos x|





57. Prove that the following functions are continuous:

 $\cos x^2$

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58. Show that the following functions are continuous:

$$f(x) = \sin \left(x^2
ight)$$

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59. Prove that the following functions are continuous:

 $e^{\cos x}$

60. Prove that the following functions are continuous:

$$e^x(\tan x)$$

61. Prove that the following functions are continuous:

$$\frac{x^2+x+1}{(x-1)(x-2)}$$

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62. If
$$f(x) = rac{|x-4|}{4-x}, x
eq 4, f(4) = 0$$
, show that f is continuous every

where except at x = 4.

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63. Examine for continuity the following functions:

$$f(x)= egin{array}{ccc} x & ext{ if } & x
eq 0 \ 1 & ext{ if } & x=0 \end{array}$$

64. Examine for continuity the following functions:

$$f(x)= egin{array}{cc} rac{x}{|x|} & x
eq 0 \ 0 & x=0 \end{array}$$

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65. Examine for continuity the following functions:

$$f(x) = egin{array}{ccc} x^2 & ext{if} & x \geq 1 \ x & ext{if} & x < 1 \end{array}$$

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66. Examine for continuity the following functions:

$$f(x)= egin{array}{ccc} 2x-1 & ext{ if } & x<2\ rac{3}{2}x & ext{ if } & x\geq 2 \end{array}$$

67. Examine for continuity the following functions:

$$f(x) = egin{cases} \sin x & ext{ if } x < 0 \ x & ext{ if } x \geq 0 \end{cases}$$

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68. Examine for continuity the following functions:

$$f(x) = egin{cases} x^2 & ext{if} \;\; x \leq 1 \ x-2 & ext{if} \;\; x > 1 \end{cases}$$

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69. Examine for continuity the following functions:

$$f(x) = egin{cases} -2 & ext{if} \;\; x \leq \, -1 \ 2x & ext{if} \;\; -1 < x \leq 1 \ 2 & ext{if} \;\; x > 1 \end{cases}$$

70. Locate the points of discontinuity of the function:

$$f(x) = egin{cases} rac{x^4 - 16}{x - 2} & ext{ if } x
eq 2 \ 16 & ext{ if } x = 2 \end{cases}$$

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71. Locate the points of discontinuity of the following functions:

$$f(x) = egin{cases} \left(egin{array}{ccc} x^3 - x^2 + 2x - 2 & x
eq 1 \ 4 & x = 1 \end{array}
ight.$$

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72. Determine the constant k(if it exists), so that the following functions

may be continuous:

$$f(x)=egin{cases} kx^2 & x\leq 2\ 3 & x>2 \end{cases}$$

73. Determine the constant k(if it exists), so that the following functions

may be continuous:

$$f(x) = egin{cases} kig(x^2-2xig) & x < 0 \ \cos x & x \ge 0 \end{cases}$$

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74. For what choice of a and b are the following functions continuous?

$$f(x) = \left\{egin{array}{ccc} ax^2+b & x>2\ 2 & x=2\ 2ax-b & x<2 \end{array}
ight.$$

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75. Find the values of a and b so that the following function is continuous

at x = 3 and x=5:

$$f(x) = egin{cases} 1 & ext{if} \;\; x \leq 3 \ ax + b & ext{if} \;\; 3 < x < 5 \ 7 & ext{if} \;\; 5 \leq x \end{cases}$$

76. For what choice of a and b are the following functions continuous?

$$f(x) = egin{cases} x^2 & x \leq 0 \ ax+b & x > 0 \end{cases}$$

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77. Examine for continuity the function $: f(x) = egin{cases} \sin^{-1}|x| & x
eq 0 \\ 0 & x = 0 \end{bmatrix}$ at x =

0



78. Let
$$f(x) = \begin{cases} 1 & x \leq -1 \\ \lambda x + \mu & -1 < x < 3 \text{ find } \lambda \text{ and } \mu \text{ if f is a continuous} \\ 5 & x > 3 \end{cases}$$

function.

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79. Examine the function [1-x]+[x-1] for continuity at x = 1.



80. Find the domain of continuity of the following functions:

$$f(x)=rac{\sin^{-1}x}{[x]}$$

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81. Find the domain of the following functions:

$$f(x)=\log(1-x)+\sqrt{x^2-1}$$

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82. Find the domain of continuity of the following functions:

$$f(f(x)), where f(x) = rac{1}{x-1}$$
83. Find the domain of continuity of the following functions:

$$f(x) = |2 - 3x + |x||.$$

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84. Given the function $f(x)=rac{1}{x+2}.$ Find the points of discontinuity of te composite function y=f(f(x))

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85. Find all the points of discontinuity of the function
$$f(t) = \left(\frac{1}{t^2 + t - 2}\right)$$
, where t $= \frac{1}{x - 1}$

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86. Examine the following functions for continuity:

$$f(x) = egin{cases} x\cos\left(rac{1}{x}
ight) & x
eq 0 \ 0 & x = 0 \end{cases}$$
at x = 0

87. Examine for continuity and differentiability, each of the following

functions:

$$f(x) = egin{cases} x^2 \sin \left(rac{1}{x}
ight) & x
eq 0 \ 0 & x = 0 \end{cases} atx = 0$$

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88. Examine for continuity, each of the following functions:

$$f(x)=egin{cases} (x-a){
m sin}igg(rac{1}{x-a}igg) & x
eq a\ 0 & x=a \end{cases}$$
at x = a

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89. Examine for continuity and differentiability, each of the following

functions:

$$f(x)=egin{cases} x^2\sin\Bigl(rac{1}{x}\Bigr) & x
eq 0\ 0 & x=0 \end{smallmatrix}$$
 at $x=0$

90. Examine for continuity and differntiability, each of the following

functions:

$$f(x)=egin{cases} 1+x & x\leq 0\ 1-x & x>0 \end{pmatrix} atx=0$$

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91. Examine for continuity the following functions:

$$f(x) = egin{array}{ccc} x^2 & ext{ if } & x \geq 1 \ x & ext{ if } & x < 1 \end{array}$$

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92. Let f(x) = x + |x|. Show that f is continuous but not derivable at x = 0

93. Show that the function $f(x) = egin{cases} -x^2 & x \leq 0 \ x^2 & x > 0 \end{bmatrix}$ is continuous at

x=0. Also show that f is differentiable at x=0.



 $f(x)=egin{cases} x^2+3x+a & ext{ if } x\leq 1\ bx+2 & ext{ if } x>1 \end{cases}$ is derivable for every x, Find the

values of 'a' and 'b'.

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95. Find a
$$\in$$
 R so that $f(x) = egin{cases} x^2 & x \geq 0 \ ax & x < 0 \end{bmatrix}$ is continuous at 0.

96. Examine the differentiability of the function 'f' defined by:

$$f(x) = egin{cases} 2x+3 & ext{if} & -3 \leq x < -2 \ x+1 & ext{if} & -2 \leq x < 0 \ x+2 & ext{if} & 0 \leq x \leq 1 \end{cases}$$

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97. Show that the function 'f' defined as follows, is continuous at x = 2, but

not differentiable there at:

$$f(x) = \left\{egin{array}{ccc} 3x-2 & 0 < x \leq 1 \ 2x^2-x & 1 < x \leq 2 \ 5x-4 & x > 2 \end{array}
ight.$$

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98. If $f(x) = e^x$, find f' (3) starting from defination

99. If
$$f(x) = e^{\sqrt{x}}$$
 find f' (x).

100. A function $f: R \to R$ satisfies the equation f(x + y) = f(x). f(y) for all x, y in R and $f(x) \neq 0$ for any x in R. Let the function be differentiable at x = 0 and f'(0) = 2 Show that f'(x) = 2 f(x) for all x in R. Hence, determine f(x).

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101. If $f(x) = \log (2x-1)$, find f'(c).

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102. If
$$f(x) = \begin{cases} x \left(rac{e^{1/x} - e^{-1/x}}{e^{1/x} + e^{-1/x}}
ight), & x
eq 0 \\ 0, & x = 0 \end{cases}$$
, then at x = 0 f(x) is

103. Find f'(X) using first prinicples when $f(x)=e^{3x-2}$



106. Find derivative of each of the following functions:

 $x^2 \log x$

107. Find derivative of each of the following functions:







111. Find derivative of each of the following functions:

$$\frac{e^x(x-1)}{x+1}$$

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112. Find derivative of each of the following functions:

 $\frac{e^x + \sin x}{1 + \log x}$



113. Find derivative of each of the following functions:

 $xe^x \sin x$

114. Find derivative of each of the following functions:

$$x^2 \log x \cos x$$

115. Find
$$rac{dy}{dx}$$
 when $y=\sin u, u=e^{\sqrt{t}}$ and $t=\log x$

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116. Find the derivatives of the following functions at any point of their

domains:

 $\sec(3x+3)$



117. Find the derivatives of the following functions at any point of their

 $\sin 2x + (2x+5)^2$

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118. Find the derivatives of the following functions at any point of their domains:

uomains

 $\cos x^2$

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119. Find the derivatives of the following functions at any point of their

domains:

 $\cos(\log x)$



120. Find the derivatives of the following functions at any point of their

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121. Find the derivatives of the following functions at any point of their
domains:
e^{x^2}

domains:

 $\log |\sin x|$



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123. Find the derivatives of the following functions at any point of their



domains:

 $\cosig(1-x^2ig)^2$

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125. Find the derivatives of the following functions at any point of their

domains:

$$\sqrt{rac{1+x}{1-x}}$$



126. Find the derivatives of the following functions at any point of their





domains:

 $\sin^2(ax^2+bx+c), n\neq -1$

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128. Find the derivatives of the following functions at any point of their

domains:

 $2^{\cos^2 x}$



129. Find the derivatives of the following functions at any point of their

$$\sin\sqrt{x} + \cos^2\sqrt{x}$$



domains:

 $\sec(\tan\sqrt{x})$

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131. Differentiate the following functions w.r.t.x :

$$\frac{x^3-8}{\left(x+2\right)^3}$$



132. Differentiate the following functions w.r.t.x :

$\sin 2x \cos 3x$

$$\frac{\sin^2 x}{1 + \cos^2 x}$$



134. Differentiate the following functions w.r.t.x :

 $\frac{1}{\log(\cos x)}$



135. Differentiate the following functions w.r.t.x :

 $\sin 2x$

 e^x

 $\frac{x}{\sin 3x}$



137. Differentiate the following functions w.r.t.x :

 $e^x + \log x$

 $\sin 3x$

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138. Differentiate the following functions w.r.t.x :

 $\frac{\sin x + x^2}{\cot 2x}$



139. Differentiate the following functions w.r.t.x.

- $1 \cos x$
- $1 + \cos x$





 $\sin x$

 $\sqrt{\cos x}$





144. Differentiate the following functions w.r.t.x :

 $\sin\left(\sqrt{\sin x + \cos x}\right)$

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145. Differentiate the following functions w.r.t.x :

$$\sqrt{\cosig(1+x^2ig)}$$

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146. Differentiate the following functions w.r.t.x :

$$\tan^2\Bigl(\sqrt{x^4+3}\Bigr)$$



$$\cos\left(\frac{x}{x+1}\right)$$

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148. Differentiate the following functions w.r.t.x :

$$\sqrt{\left(\log\!\left(\sin\!\left(rac{x^2}{3}-1
ight)
ight)
ight)}$$

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149. Differentiate the following functions w.r.t.x :

$$\log\sqrt{rac{1-\sin x}{1+\sin x}}$$



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153. Differentiate the following functions w.r.t.x :

 $2\sqrt{\cot x}(x^2)$



 $\sin^P x \cos^q x$

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155. Differentiate the following functions w.r.t.x :

 $e^{ax}\cos(bx+c)$

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156. Differentiate the following functions w.r.t.x :

 $\frac{e^{2x}-1}{e^{2x}+1}$

 $\frac{e^{2x}-e^{-2x}}{e^{2x}+e^{-2x}}$



158. Differentiate the following functions w.r.t.x :

$$\left(\frac{2x^3+1}{3x^2+1}\right)^2$$

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159. Differentiate the following functions w.r.t.x :

$$\frac{x}{a-\sqrt{a^2-x^2}}$$



160. Differentiate the following functions w.r.t.x :

$$\frac{\left(x^{5}-2x-1\right)^{3\,/\,2}}{x^{2}}$$



 $\sin(e^x \log x)$

 $x \log x + \log(\log x)$



165. Differentiate the following functions w.r.t.x :

$$x\sqrt{1+x^2} + \log\Bigl(x+\sqrt{x^2+1}\Bigr)$$

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166. Differentiate the following functions w.r.t.x :

 $\frac{\log(1+x)}{1-x}$



167. Differentiate the following functions w.r.t.x :

$$\log\Bigl(x+\Bigl(\sqrt{x^2+a^2}\Bigr)$$



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169. Differentiate the following functions w.r.t.x :

 $\frac{e^{ax}}{\sin(bx+c)}$



170. Differentiate the following functions w.r.t.x :

$$e^{\,-\,ax^2}\log(\sin x)$$

$$\log\Bigl(x+e^{\sqrt{x}}\Bigr)$$

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172. Differentiate the following functions w.r.t.x :

 $(\log x)e^{ an x+x^2}$

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173. Differentiate the following functions w.r.t.x :

 $e^{\sin x} \sin(e^x)$



174. Differentiate the following functions w.r.t.x :

$$\sqrt{rac{1+e^x}{1-e^x}}$$

 $\cos(\tan\sqrt{x})$

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176. Differentiate the following functions w.r.t.x :

 $\sin x^2 + \sin^2 x + \sin^2 x^2$

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177. Differentiate the following functions w.r.t.x.

 $\sqrt{\sec^2 x + \cos e c^2 x}$

 $2^{x}e^{2(x+3)}$

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179. Differentiate the following functions w.r.t.x :

 $2^{5x^2} imes 3^{-4x}$

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180. Differentiate the following functions w.r.t.x :

 $\log \left| rac{a+b\sin x}{a-b\sin x}
ight|$



181. Differentiate the following functions w.r.t.x :

 $(5x)^{3\cos^2x}$



182. If
$$y = \sin (\cos \sqrt{a}x + b), ext{ find } rac{dy}{dx}$$

183. If
$$y=\sqrt{rac{1+x}{1-x}}$$
, prove that $\left(1-x^2
ight)rac{dy}{dx}-y=0$

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184. If
$$y=\sqrt{rac{1-\sin 2x}{1+\sin 2x}}$$
, prove that

$$rac{dy}{dx} + \mathrm{sec}^2 \Big(rac{\pi}{4} - x \Big) = 0, 0 \leq x \leq rac{\pi}{4}$$

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185. If
$$y=e^{x+3\log x}$$
 prove that $\displaystyle rac{dy}{dx}=x^2(x+3)e^x$

186. If
$$y=rac{e^x+e^{-x}}{e^x-e^{-x}}$$
 , then show that $\left(rac{dy}{dx}
ight)=1-y^2$

187. Find the derivatives of the following functions at the indicated points.

$$\cos\Bigl(2x+rac{\pi}{2}\Bigr)atx=rac{\pi}{3}$$

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188. Find the derivatives of the following functions at the indicated

points.

 $\frac{1+\sin x}{1+\cos x}atx=\frac{\pi}{2}$

189. Find the derivatives of the following functions at the indicated

points.

 $\cot x + \sec^2 x - 5atx = rac{\pi}{6}$

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190. Find the derivatives of the following functions at the indicated points.

 $9\sin x + sin3x$

at $x=rac{\pi}{3}$

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191. Find the derivatives of the following functions at the indicated points.

$$\left(\cos ec^2x + \tan x + \cot x
ight)^7 atx = rac{\pi}{4}$$

192. Find the derivatives of the following functions at the indicated points.

$$\sqrt{\sin^4 x^2 + \cos^4 x^2}$$
 at $x = \left(\sqrt{rac{\pi}{2}}
ight)$

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193. Find
$$\displaystyle rac{dy}{dx}$$
 when $x=t+\displaystyle rac{1}{t}, y=t-\displaystyle rac{1}{t}$

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194. Find
$$\frac{dy}{dx}$$
, when: $x = e^{ heta} \left(heta + rac{1}{ heta}
ight)$ and $y = e^{- heta} \left(heta - rac{1}{ heta}
ight)$

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195. Find
$$rac{dy}{dx}$$
 when $x=a\sin^2 t, y=b\cos^2 t$

196. Find
$$rac{dy}{dx}$$
 when $x=e^{t-\sin t}, y=e^{t+\cos t}$

197. Find
$$rac{dy}{dx}$$
 when $x=a\cos^3 t, y=b\sin^3 t$

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198. Find
$$rac{dy}{dx}$$
 when $x=e^t(\sin t+\cos t), y=e^t(\sin t-\cos t)$

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199. Find
$$rac{dy}{dx}$$
 when $x=\cos heta+\cos2 heta,y=\sin heta+\sin2 heta)$

200. Find
$$rac{dy}{dx}$$
 when $x=a(heta+\sin heta), y=a(1+\cos heta)$

201. Find
$$rac{dy}{dx}$$
 when $x=a(heta+\sin heta), y=a(1+\cos heta)$

202. Find
$$\frac{dy}{dx}att = \frac{\pi}{4}$$
, when $x = 2\cos 2t$ and $y = 2\sin t - \sin 2t$

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203. If
$$x=a\sec^3 heta and y=a\tan^3 heta,\,f\in drac{dy}{dx} heta=rac{\pi}{3}.$$

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204. Find
$$rac{dy}{dx}$$
at t = 2 when $x=rac{2bt}{1+t^2}$ and $y=rac{aig(1-t^2ig)}{1+t^2}$

205. Find
$$\frac{dy}{dx}$$
 when x = 2t/(1+ t^2) and y = (1- t^2)/(1+ t^2)`

206. Differentiate the following functions:

 $\sin x^3 w. r. t. x^3$

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207. Differentiate the following functions:

 $\frac{\sin x}{1+\cos x}$ w.r.t. $\frac{x}{2}$



208. Differentiate the following functions:

 $\sin x^2$ w.r.t x^2


209. Differentiate the following functions:

$$rac{x^2}{x^2+1}$$
 w.r.t. x^2

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210. Differentiate the following functions:

$$\cot^3(2x+1)w.\ r.\ t.\ x^2+1$$

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211. Differentiate the following functions:

```
\frac{x}{\sin x} w.r.t \sin x.
```

212. If
$$x = \frac{1 + \log t}{t^2}$$
, $y = \frac{3 + 2\log t}{t}$, $t > 0$, prove that $y\left(\frac{dy}{dx}\right) - 2x\left(\frac{dy}{dx}\right)^2 = 1$

213. If
$$x = 3\cos t - 2\cos^3 t$$
 and $y = 3\sin t - 2\sin^3 t$, show that $\frac{dy}{dx} = \cot t$

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214. Find
$$rac{dy}{dx}$$
 if $x=rac{\sin^3 t}{\sqrt{\cos 2t}}, y=rac{\cos^3 t}{\sqrt{\cos 2t}}$

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215. Find
$$rac{dy}{dx}$$
 if $3y = \sqrt{\sec^2 x - 1}$



220. Differentiate the following functions w.r.t. $\sin(an^{-1}x)$







233. Differentiate the following functions w.r.t.x

$$\sec^{-1}\left(\frac{x+1}{x-1}\right) + \sin^{-1}\left(\frac{x-1}{x+1}\right)$$

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234. Differentiate the following functions w.r.t.x
 $\cos^{-1}\left(\frac{\sin x + \cos x}{\sqrt{2}}\right), \frac{\pi}{4} < x < \frac{\pi}{4}$
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235. Prove that $\cos^{-1}x = \frac{\pi}{2} - \sin^{-1}x$ for $-1 \le x \le 1$ and use this
result to find $\frac{d}{dx}(\cos^{-1}x)$
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236. Prove that $\sec^{-1}x = \cos^{-1}\left(\frac{1}{x}\right)$ and use this to find $\frac{d}{dx}(\sec^{-1}x)$

237. Prove that $\cot^{-1}x = \frac{\pi}{2} - \tan^{-1}x$ and use this to find the derivative of $\cot^{-1}x$.

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238. Prove that

$$anig(\sin^{-1}xig) = igg(rac{x}{\sqrt{1-x^2}}igg), 1x1 < 1$$

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239. Find
$$rac{dy}{dx}$$
 if $y = \sin^{-1}x + \sin^{-1}\sqrt{1-x^2}, 0 < x < 1$

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240. Differentiate the following functions w.r.t.x

$$x\sin^{-1}x + \sqrt{1-x^2}$$



241. Differentiate the following functions w.r.t.x

$$\cot^{-1} \left(rac{1 + \cos x}{\sin x}
ight)$$

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242. Differentiate the following functions w.r.t.x L

$$an^{-1} \left(rac{\cos x}{1 + \sin x}
ight)$$

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243. Differentiate the following functions w.r.t.x:

$$\cot^{-1}(\cos ecx + \cot x)$$

244. Differentiate the following functions w.r.t.x L

$$4 an^{-1}igg(\sqrt{rac{1+\cos 2x}{1-\cos 2x}}igg)$$

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245. Differentiate the following functions w.r.t.x

$$\sin^{-1}\Bigl(2x\sqrt{1-x^2}\Bigr), |x|<rac{1}{\sqrt{2}}$$

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246. Differentiate the following functions w.r.t.x L

$${
m sec}^{-1}igg(rac{1}{2x^2-1}igg) 0 < x < rac{1}{\sqrt{2}}$$

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247. Differentiate the following functions w.r.t.x L

$$\sinigg(2 an^{-1}\sqrt{rac{1-x}{1+x}}igg), \ -1\leq x<1$$

248. Differentiate the following functions w.r.t.x

$$x \left(\sin^{-1}x
ight)^2 + 2 \sqrt{1-x^2} \sin^{-1}x - 2x$$

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249. Differentiative the following (by suitable substitutions, if valid), w.r.t.x

$$an^{-1} igg(2 rac{x}{1-x^2} igg)$$

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250. Differentiative the following (by suitable substitutions, if valid), w.r.t.x

$$\cos^{-1}igg(rac{1-x^2}{1+x^2}igg)$$

$$\sin^{-1}\bigl(3x-4x^3\bigr)$$

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252. Differentiative the following (by suitable substitutions, if valid), w.r.t.x

 $\cos^{-1}ig(4x^3-3xig)$

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253. Differentiative the following (by suitable substitutions, if valid), w.r.t.x

 $\cos^{-1}ig(1-2x^2ig)$

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254. Differentiative the following (by suitable substitutions, if valid), w.r.t.x

$$\sin^{-1} \Big(2x \sqrt{1-x^2} \Big)$$

$$\cos ec^{-1}\left(rac{1+x^2}{2x}
ight)$$

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256. Differentiative the following (by suitable substitutions, if valid), w.r.t.x

$$an^{-1}igg(rac{3x-x^3}{1-3x^2}igg)$$

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257. Differentiative the following (by suitable substitutions, if valid), w.r.t.x

$$an^{-1} \Big(\sqrt{1+x^2} - x \Big)$$

$$\tan^{-1}\left(\frac{x}{1+\sqrt{1-x^2}}\right)$$
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259. Differentiative the following (by suitable substitutions, if valid), w.r.t.x

$$\cot^{-1}\Bigl(\sqrt{1+x^2}+x\Bigr)$$

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260. Differentiate the following w.r.t.x.

$$an^{-1}igg(rac{x}{\sqrt{a^2-x^2}}igg)$$

$$\sin^{-1} \Biggl(rac{1}{\sqrt{1+x^2}} \Biggr)$$

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262. Differentiate the following (by suitable substitutions, if valid), w.r.t.x

$$\sin^{-1}\left(rac{2x}{1+x^2}
ight)$$

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263. Differentiative the following (by suitable substitutions, if valid), w.r.t.x

$$an^{-1} igg(rac{\sqrt{1+x^2}+1}{x} igg)$$

$${
m sec}^{-1}igg(rac{1}{4x^3-3x}igg), rac{1}{2} \leq x < 1$$

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265. Differentiate the following w.r.t. as indicated:

$$an^{-1} igg(rac{\sqrt{1+x^2}-1}{x} igg) w. r. t. an^{-1} x$$

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266. Differentiate the following w.r.t. as indicated:

$$an^{-1} igg(rac{\sqrt{1+a^2x^2}-1}{ax} igg) w. r. t. an^{-1} ax$$

267. Prove that derivative of $an^{-1} igg(rac{x}{1+\sqrt{1-x^2}} igg)$ w.r.t \sin^{-1} x is

independent of x.

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268. Find
$$rac{dy}{dx}$$
 when $y= an^{-1}iggl(rac{4\sqrt{x}}{1-4 imes}iggr)$

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269. Find
$$rac{dy}{dx}$$
 when $y= an^{-1}igg(rac{\sqrt{x}-\sqrt{a}}{1+\sqrt{a}x}igg)$

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270. Find
$$rac{dy}{dx}$$
 when $an^{-1} igg(rac{\sqrt{x}(3-x)}{1-3x} igg)$

271. Find
$$\displaystyle rac{dy}{dx}$$
, if $\displaystyle y= an^{-1}igg(\displaystyle rac{x^{rac{1}{3}}+a^{rac{1}{3}}}{1-x^{rac{1}{3}}a^{rac{1}{3}}}igg)$

272. Find
$$rac{dy}{dx}$$
 when $y=\cos^{-1}(2x)+2\cos^{-1}\sqrt{1-4x^2}$

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273. Differentiate the following functions w.r.t.x :

$$an^{-1}igg(rac{a+bx}{b-ax}igg), rac{bx}{a} > -1$$

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274. Differentiate the following functions w.r.t.x :

$$an^{-1}igg(rac{3-2x}{1+6x}igg)$$

275. Differentiate the following functions w.r.t.x :

$$\cot^{-1}igg(rac{3-2 an x}{2+3 an x}igg), 0< an x<rac{2}{3}$$

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276. Differentiate the following functions w.r.t.x :

$$an^{-1}igg(rac{5ax}{a^2-6x^2}igg), a>06x^2< a^2$$

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277. If
$$y = \sin^{-1}\left(\frac{2x}{1+x^2}\right) + \sec^{-1}\left(\frac{1+x^2}{1-x^2}\right)$$
 , prove that $\frac{dy}{dx} = \frac{4}{1+x^2}$, $0 < x < 1$

278. If
$$y= an^{-1}igg(rac{2x}{1-x^2}igg)+ ext{sec}^{-1}igg(rac{1+x^2}{1+x^2}igg)$$
, find $rac{dy}{dx}$

279. Find
$$\frac{dy}{dx}$$
 when $y=\sin^{-1}\left(\frac{2x}{1+x^2}\right)+\cos^{-1}\left(\frac{1-x^2}{1+x^2}\right)$ when $x\in(0,1)$

280. Find
$$\frac{dy}{dx}$$
 when $y = \sin^{-1}\left(\frac{2x}{1+x^2}\right) + \cos^{-1}\left(\frac{1-x^2}{1+x^2}\right)$ when $x \in (0,1)$

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281. Find
$$\frac{dy}{dx}$$
 when $y = \sin^{-1}\left(\frac{2x}{1+x^2}\right) + \cos^{-1}\left(\frac{1-x^2}{1+x^2}\right)$ when $x \in (0,1)$

282. Find
$$\frac{dy}{dx}$$
 when $y=\sin^{-1}\left(\frac{2x}{1+x^2}\right)+\cos^{-1}\left(\frac{1-x^2}{1+x^2}\right)$ when $x\in(0,1)$

283. If
$$y = 2 \tan^{-1} \left(\sqrt{\frac{x-a}{b-x}} \right)$$
 and a < x < b, then show that $\left(\frac{dy}{dx} \right)^2 + \frac{1}{(x-a)(x-b)} = 0$

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284. Differentiate
$$\cos^{-1}\left(rac{1}{\sqrt{1+t^2}}
ight)$$
 w.r.t $\sin^{-1}\left(rac{t}{\sqrt{1+t^2}}
ight)$

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285. Differentiate
$$\sin^{-1}\left(\frac{2x}{1+x^2}\right) w. r. t. \cos^{-1}\left(\frac{1-x^2}{1+x^2}\right)$$

286. Differentiate
$$\sin^{-1}\left(\frac{2x}{1+x^2}\right)$$
 w.r.t. $\tan^{-1}x, -x < x < 1$.
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287. Differentiate $\tan^{-1}\left(\frac{\sqrt{1+x^2}-1}{x}\right)w.r.t\tan^{-1}\left(\frac{x}{\sqrt{1-x^2}}\right)$
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288. Differentiate $\tan^{-1}\left(\frac{x}{\sqrt{1-x^2}}\right)$ w.r.t. $\sin^{-1}\left(2x\sqrt{1-x^2}\right)$.
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289. Find
$$\frac{dy}{dx}$$
 when $y = \sin^{-1}\left(\frac{1}{\sqrt{1+x^2}}\right) + \frac{\tan^{-1}\left(\sqrt{1+x^2}-1\right)}{x}$, $x > 0$

290. If
$$y = \sin^{-1} x^2 \sqrt{1 - x^2} + x \sqrt{1 - x^4}$$
, show that $\frac{dy}{dx} - \frac{2x}{\sqrt{1 - x^4}} = \frac{1}{\sqrt{1 - x^2}}$

291. If
$$y=\sin^{-1}\Bigl[x\sqrt{1-x}-\sqrt{x}\Bigl(\sqrt{1-x^2}\Bigr)\Bigr]$$
 find $\displaystyle rac{dy}{dx}$

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292. If
$$y = \frac{2}{\sqrt{a^2 - b^2}} \tan^{-1} \left(\sqrt{\frac{a+b}{a-b}} \tan \frac{x}{2} \right)$$
, prove that $\frac{dy}{dx} = \frac{1}{a-b\cos x}$

293. Find
$$\displaystyle rac{dy}{dx}$$
 when $xy=c^2$

294. Find
$$rac{dy}{dx}$$
 when $x^2+y^2=a^2$

295. Find
$$rac{dy}{dx}$$
 when $rac{x^2}{a^2}-rac{y^2}{b^2}=1$

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296. Find
$$\displaystyle rac{dy}{dx}$$
 when $\displaystyle 2x^2 - 3xy + 4y^2 = 5$

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297. Find
$$\displaystyle rac{dy}{dx}$$
 when $xy^2-x^2y=4$

298. Find
$$\displaystyle rac{dy}{dx}$$
 when $xy^3-x^3y=y$

299. Find
$$rac{dy}{dx}$$
 when $ig(x^2+y^2ig)ig)^2=xy$

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300. Find
$$rac{dy}{dx}$$
 when $\sin(x+y)=rac{1}{2}$

301. Find
$$rac{dy}{dx}$$
 when $ax^2+2hxy+by^2=c^2$

302. Find
$$rac{dy}{dx}$$
 when $xy^3 - x^3y = x$

303. Find
$$\displaystyle rac{dy}{dx}$$
 if $x^3+x^2y+xy^2+y^3=81$

304. If
$$x^{2/3}+y^{2/3}=2$$
, find $\displaystyle rac{dy}{dx}$ at (1,1)

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305. Use implicit differentation to verify that
$$\frac{dy}{dx} \cdot \frac{dx}{dy} = 1$$
 when $y^2 = 4ax$

306. Use implicit differentation to verify that $\frac{dy}{dx} \cdot \frac{dx}{dy} = 1$ when $x^3 + y^3 = 3axy.$

307. Find
$$rac{dy}{dx}$$
 when $\cos(x+y)=y\sin x$

308. Find
$$rac{dy}{dx}$$
 when $x \sin 2y = y \cos 2x$

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309. Find
$$\frac{dy}{dx}$$
 in the following :

 $y \sec x + \tan x + x^2 y = 0$

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310. Find
$$rac{dy}{dx}$$
 when $y^2 \sin x + y \tan x + ig(1+x^2) \cos x = 0$

311. Find
$$rac{dy}{dx}$$
 when $ye^{x^2} + an x + \log(\sin x) = 0$

312. Find
$$rac{dy}{dx}$$
 when $x \sin y + x^3 = an^{-1} y$

313. Find
$$rac{dy}{dx}$$
 when $\sin y = \log_{\sin x} (\cos x)$

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314. Find
$$rac{dy}{dx}$$
 when $an(x+y)+ an(x-y)=1$

315. Find
$$rac{dy}{dx}$$
 when $\cot(y)+xy=y$



316. Find
$$rac{dy}{dx}$$
, if $\sin^2 x + \cos^2 y = 1$

317. Find
$$rac{dy}{dx}$$
 when $\operatorname{sec}(x+y) = xy$

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318. Find
$$rac{dy}{dx}$$
 when $an^{-1}ig(x^2+y^2ig)=a$

319. If
$$y=\sqrt{1+\sqrt{1+x^4}}$$
, prove $ext{that} y ig(y^2-1ig) rac{dy}{dx}=x^3$



321. If
$$e^x + e^y = e^{x+y}$$
, prove that $\displaystyle rac{dy}{dx} = -e^{y-x}$

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322. If
$$\cos^{-1}\left(rac{x^2-y^2}{x^2-y^2}
ight)= an^{-1}a, ext{ then prove that } rac{dy}{dx}=rac{y}{x}.$$

323. If
$$x^2+y^2=t+rac{1}{t}$$
 and $x^4+y^4=t^2+rac{1}{t^2}$, then show that $rac{dy}{dx}=-rac{1}{x^3y}$

324. If
$$\log \sqrt{x^2+y^2} = an^{-1}(y/x)$$
 , then show that $rac{dy}{dx} = rac{x+y}{x-y}$

C

325. If
$$\sqrt{x^2+1}y=\log\Bigl(\sqrt{x^2+1}-x\Bigr)$$
, then show that $(x^2+1)\dfrac{dy}{dx}+xy+1=0$

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326. If
$$\sqrt{1-x^2}+\sqrt{1-y^2}=a(x-y), ext{ show that } rac{dy}{dx}=\sqrt{rac{1-y^2}{1-x^2}}$$

327. If
$$\sqrt{1-x^6} + \sqrt{1-y^6} = a^3(x^3-y^3)$$
, prove that : $\frac{dy}{dx} = \frac{x^2}{y^2}\sqrt{\frac{1-y^6}{1-x^6}}.$

328. If
$$y=\sqrt{x+\sqrt{x+\sqrt{x+\dots\infty}}}$$
, show that $(2y-1)rac{dy}{dx}=1$

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329.
$$y = \sqrt{\tan x + \sqrt{\tan x + \sqrt{\tan x + \dots \cos x}}}$$
 prove that $(2y-1)\frac{dy}{dx} = \sec^2 x$.

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330. Differentiate the following functions w.r.t.x :
$$(x+1)^2(x+2)^3(x+3)^4$$



335. Differentiate the following functions w.r.t.x : $e^x \cos^3 x \sin^4 x$



338. Find
$$rac{dy}{dx}$$
 when $x^y+y^x=a^t$

339. Find
$$rac{dy}{dx}$$
 when $x^y=1$

340. Find
$$rac{dy}{dx}$$
 when $xy=e^{x-y}$

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341. Differentiate the following functions w.r.t.x :

 x^x



342. Differentiate the following functions w.r.t.x :

 $(\sin x)^x$

343. Differentiate the following functions w.r.t.x :

$$(2x+3)^{x-5}$$



344. Differentiate the following functions w.r.t.x :

 $x^{\sin^{-1}x}$

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345. Differentiate the following functions w.r.t.x :

 $x^{\sin x} + \sin x^{\cos x}$


346. Differentiate the following functions w.r.t.x :



349. Differentiate the following functions w.r.t.x :

$$x^{ an x}+\sqrt{rac{x^2+1}{2}}$$

350. Differentiate the following functions w.r.t.x :

$$\left(\cos x
ight)^{x}+\left(\sin x
ight)^{1/x}$$

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351. If
$$x=e^{x\,/\,y},$$
 prove that $\displaystyle rac{dy}{dx}=\displaystyle rac{x-y}{x\log x}$

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352. Differentiate the following w.r.t.x.

If
$$y^x = e^{y-x}$$
, prove that $\displaystyle rac{dy}{dx} = \displaystyle rac{\left(1 + \log y
ight)^2}{\log y}$

353. If
$$x^p. \ y^q = \left(x+y
ight)^{p+q}$$
 , show that $\displaystyle rac{dy}{dx} = \displaystyle rac{y}{x};$





362. Differentiate the following functions w.r.t.x $\left(x\cos x
ight)^x + \left(x\sin x
ight)^{rac{1}{x}}$



363. Differentiate
$$(x^x)^x$$
 w.r.t.x .

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364. Find
$$rac{dy}{dx} wheny = 10x^x + x^{x^x} + \left(x^{10}
ight)$$

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365. Find
$$\displaystyle rac{dy}{dx} wheny = e^{e^{e^x}} + e^{x^{e^x}} + e^{e^{x^x}}$$

366. Find
$$\frac{dy}{dx}$$
 when $(\sin x)^y = (\sin y)^x$

367. Find
$$\displaystyle rac{d^2 y}{dx^2}$$
 when $\displaystyle y=2x^3+3x^2+6$

368. Find
$$rac{d^2 y}{dx^2}$$
 when $y=rac{\log x}{x}$

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369. Find
$$rac{d^2y}{dx^2}$$
 when $y=x^x$

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370. Find
$$\displaystyle rac{d^2 y}{dx^2}$$
 when $\displaystyle y=e^x \sin x$

371. Find
$$rac{d^2 y}{dx^2}$$
 when $y=x^2+ an x$



372. Find
$$\displaystyle rac{d^2 y}{dx^2}$$
 when $\displaystyle y=x^3+ an x$

373. Find the second derivative of $\log x + \cos x$.



375. If
$$y=\log\Bigl(x+\sqrt{x^2+1}\Bigr), provet \widehat{:} \, \bigl(x^2+1\bigr) d^2 rac{y}{dx^2}+xrac{dy}{dx}=0.$$

376. Find the second order derivative of $e^{x \tan x}$

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377. If
$$y = an^{-1} x$$
, find $rac{d^2 y}{dx^2}$ in terms of y alone.

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378. If $y = A \sin x + B \cos x$ then prove that $d^2 rac{y}{dx^2} + y = 0$

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379. If $y=3\cos(\log x)+4\sin(\log x)$ show that $x^2y_2+xy_1+y=0$

380. If
$$y = Ae^{mx} + Be^{nx}$$
, Show that

$$\left(rac{d^2}{dx^2}y
ight)-(m+n)rac{dy}{dx}+mny=0 \; ,$$

381. If
$$y=e^{ax}\cos bx$$
, then prove that $rac{d^2y}{dx^2}-2arac{dy}{dx}+ig(a^2+b^2ig)y=0.$

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382. If
$$y=\left(\sqrt{x+1}-\sqrt{x-1}
ight)$$
, then prove that $ig(x^2-1ig)y_2+xy_1=rac{1}{4}y$

383.
$$y=e^{m\sin^{-1}x}, ext{ prove that } ig(1-x^2ig)y_2-xy_1=m^2y$$

384. If
$$rac{x^2}{a^2}-rac{y^2}{b^2}=1$$
, prove that $\left(rac{d^2y}{dx^2}
ight)=rac{-b^4}{a^2y^3}$

385. If
$$(x-a)^2 + (y-b)^2 = c^2$$
, for some $c > 0$, prove that
$$\frac{\left[1 + \left(\frac{dy}{dx}\right)^2\right]^{\frac{3}{2}}}{\frac{d^2y}{dx^2}}$$
is a constant independent of a and b.

386. Find
$$rac{d^2y}{dx^2}$$
, if $x=a(heta-\sin heta), y=a(1+\cos heta)$

387. If
$$x = 2\cos\theta - \cos 2\theta, y = 2\sin\theta - \sin 2\theta$$
, find $\frac{dy}{dx}at\theta = \frac{\pi}{2}$

388. If
$$x = a \left\{ \cos t + \log \left| rac{ an t}{2}
ight|
ight\}$$
 and y = a sin t, $0 < t < rac{\pi}{2}$, find $rac{d^2 y}{dx^2}$

389. If
$$x = a\cos\theta + b\sin\theta$$
 and $y = a\sin\theta - b\cos\theta$, then prove that
$$y^2 \frac{d^2y}{dx^2} - \frac{dy}{dx} + y = 0$$

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390. If
$$y = x \log \left(rac{x}{a+bx}
ight)$$
, prove that $x^3 y_2 = \left(x y_1 - y
ight)^2$

391. If
$$x = g(t)$$
 and $y = f(t)$, find $\frac{d^2y}{dx^2}$ as a function of t.







x sin x



sin 3 x sin 6 x



400. Find the second derivative of the following functions:

$$\frac{x}{x^2-3x+2}$$

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401. If
$$y = \sin^{-1} x$$
, then prove that

$$rac{d^2y}{dx^2} = rac{x}{(1-x^2)^{rac{3}{2}}}$$

402. If
$$y=\sin^{-1}x$$
, then show that $ig(1-x^2ig)rac{d^2y}{dx^2}-xrac{dy}{dx}=0$

403. If
$$y=\sin^{-1}x$$
, prove that $ig(1-x^2ig)y_2-xy_1=0$

If
$$y=x+ an x$$
, prove that $\cos^2 x.~rac{d^2y}{dx^2}-2y+2x=0$

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405. Find the second order derivative of the following functions

If
$$y=ae^{mx}+be^{-mx}$$
 , prove that $\displaystyle rac{d^2y}{dx^2}-m^2y=0$

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406. If
$$y=3e^{2x}+2e^{3x}$$
, prove that $d^2\displaystyle\frac{y}{dx^2}-5\displaystyle\frac{dy}{dx}+6y=0.$

If $y=a\cos(\log x)+b\sin(\log x), ext{ prove that } x^2y_2+xy_1+y=0.$

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408. If x cos (a+y) = cos y, then prove that
$$\frac{dy}{dx} = \frac{\cos^2(a+y)}{\sin a}$$
 Hence,
show that $\sin a \frac{d^2y}{dx^2} + \sin 2(a+y) \frac{dy}{dx} = 0$
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409. If y = 2 sin x + 3 cos x, prove that
$$y + rac{d^2y}{dx^2} = 0$$

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410. If $y=a\cos mx+b\sin mx$, prove that $y_2+m^2y=0$

If
$$y=\log\Bigl[x+\sqrt{x^2+a^2}\Bigr]$$
 , show that $\bigl(x^2+a^2\bigr)rac{d^2y}{dx^2}+xrac{dy}{dx}=0$

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412. If
$$y = \left[\log\left(x + \sqrt{x^2 + 1}
ight)
ight]^2$$
 then show that $\left(x^2 + 1
ight)y_2 + xy_1 = 0$

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413. Find the second order derivative of the following functions

If
$$y=rac{\sin^{-1}x}{\sqrt{1-x^2}}$$
 , prove that $ig(1-x^2ig)y_2-3xy_1-y=0$

414. If
$$x = \tan\left(\frac{1}{a}\log y\right)$$
, then show that $(1 + X^2)\frac{d^2y}{dx^2} + (2x - a)\frac{dy}{dx} = 0$
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415. If $y = x^x$, prove that $y_2 - y^{-1}(y_1)^2 - yx^{-1} = 0$
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416. If
$$y = \left(\tan^{-1}x\right)^2$$
, then prove that $\left(1+x^2\right)^2 \frac{d^2y}{dx^2} + 2x\left(1+x^2\right)\frac{dy}{dx} - 2 = 0$

417. If $y=\left[\sin^{-1}x
ight]^2$, then prove that $:\left(1-x^2
ight)y_2-xy_1-2=0.$

If
$$y = \cos^{-1} x$$
, find $\frac{d^2 y}{dx^2}$ in terms of y alone.

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419. If
$$y = \cos ec^{-1}x$$
, $x > 1$, then show that :
 $x(x^2-1)\frac{d^2y}{dx^2} + (2x^2-1)\frac{dy}{dx} = 0$
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420. If
$$y = x^x$$
, prove that $y_2 - y^{-1}(y_1)^2 - yx^{-1} = 0$

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421. If $y=e^{-ax}\cos(bx+c)$, show that $rac{d^2y}{dx^2}+2arac{dy}{dx}+ig(a^2+b^2ig)y=0$

422. If
$$y^2 = ax^2 + b$$
, prove that $\displaystyle rac{d^2y}{dx^2} = a \displaystyle rac{b}{y^3}$



423. If
$$x^2+y^2=a^2$$
, prove that $\displaystyle rac{d^2y}{dx^2}=~-rac{a^2}{y^3}$

424. If
$$x^my^n=(x+y)^{m+n}$$
, prove that $\displaystyle rac{dy}{dx}=\displaystyle rac{y}{x} \; ext{and} \; \displaystyle rac{d^2y}{dx^2}=0$

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425. If
$$rac{x^2}{a^2}+rac{y^2}{b^2}=1$$
, prove that `(d^2y)/(dx^2) = -(b^4)/(a^2y^3)~

426. If
$$\sqrt{x} + \sqrt{y} = \sqrt{x}$$
, find $\displaystyle rac{d^2y}{dx^2} atx = a$

427. Find
$$\displaystyle rac{d^2 y}{dx^2}$$
 if $x=at^2 ig)$, y = 2 a t.

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428. Find
$$rac{d^2y}{dx^2}$$
 if $x=\cos heta, y=a\sin heta)$

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429. If
$$x=a\sin^3 heta, y=a\cos^3 heta$$
 , find $rac{d^2y}{dx^2}at heta=rac{\pi}{4}$

430. If x=a (cos t + t sin t) and y = a (sin t - t cos t), $f \in d(d^2x)/(dt^2)$,

 $(d^2y)/(dt^2)$ and $(d^2y)/(dx^2)$. Also mention the domain of validity.

431. Find
$$rac{d^2y}{dx^2}$$
 in the following
 If $x=a(heta+\sin heta), y=a(1-\cos heta)$, find $rac{d^2y}{dx^2}$ at $heta=rac{\pi}{2}$

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432. If
$$x=rac{1-t^2}{1+t^2}, y=rac{2t}{1+t^2}$$
, find $rac{dy}{dx}$ at x=2.

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$$f(x)=\logig(x^2+2ig)-\log 3{
m in}[\,-1,1]$$



438. Verify the conditions of Rolle's Theorem in the followin problems. In eah case, find a point in the interval where the derivative vanishes: e^{1-x^2} on [-1,1]

439. Verify Rolle's theorem for the following functions in the given intervals and find a point in the interval where the derivative vanishes : $f(x) = \sin x + \cos x in \left[0, \frac{\pi}{3}\right]$

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$$f(x) = \sin x + \cos x - \ln \left[0, rac{\pi}{2}
ight]$$



441. Verify Rolle's theorem for the following functions in the given intervals and find a point in the interval where the derivative vanishes : $f(x) = \sin 3x \ln[0, \pi]$



442. Verify Rolle's theorem for the following functions in the given intervals and find a point in the interval where the derivative vanishes : $f(x) = \sin x - 1 \ln[0, 2\pi]$

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444. Verify Rolle's theorem for the following functions in the given intervals and find a point in the interval where the derivative vanishes : $f(x) = \sin 2x \ln \left[0, \frac{\pi}{2}\right]$

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445. Verify Rolle's theorem for the following functions in the given intervals and find a point in the interval where the derivative vanishes : $f(x) = (x^2 + 2)in[-2, 2]$

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447. Verify Rolle's theorem for the following functions in the given intervals and find a point (or point) in the interval where the derivative vanishes : f(x) = (x - 1)(x - 2)(x - 3)in[1, 3]



448. Verify Rolle's theorem for the following functions in the given intervals and find a point (or point) in the interval where the derivative vanishes : $f(x) = (x^2 - 1)(x - 2)in[-1, 2]$

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vanishes : $f(x) = x(x-1)^2$ in[0,1]



450. Verify Rolle's theorem for the following functions in the given intervals and find a point (or point) in the interval where the derivative vanishes : $f(x) = \sqrt{4 - x^2}$ in[-2, 2]

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451. Verify Rolle's theorem for the following functions in the given intervals and find a point (or point) in the interval where the derivative vanishes : $f(x) = \log\left(\frac{x^2 + ab}{(a+b)x}\right)$ in [a,b], a>0

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vanishes : $f(x)=x(x+3)e^{-rac{x}{2}}$ in[-3,0]



453. Verify Rolle's theorem for the following functions in the given intervals and find a point (or point) in the interval where the derivative vanishes : $f(x) = (x - 2)^2 (x - 3)^3 in[2,3]$

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454. Verify Rolle's theorem for the following functions in the given intervals and find a point (or point) in the interval where the derivative vanishes : $f(x) = e^x(\sin x - \cos x)$ in $\left[\frac{\pi}{4}, \frac{5\pi}{4}\right]$

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vanishes : $f(x) = \log \left(x^2 + 2
ight) - \log (x+2)$ in[0,1]`



456. Verify Rolle's theorem for the following functions in the given intervals and find a point (or point) where the derivative vanishes : $f(x) = e^x \cos x \ln \left[-\frac{\pi}{2}, \frac{\pi}{2} \right]$

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457. Verify Rolle's theorem for the following functions in the given intervals and find a point (or point) where the derivative vanishes : $f(x) = \frac{\sin x}{e^x} in[0, \pi]$

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459. Verify Rolle's theorem for the following functions in the given intervals and find a point (or point) where the derivative vanishes : $f(x) = e^{-\frac{x}{2}}(x^2 + 3x)$ on [-3,0]

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460. Verify Rolle's theorem for the following functions in the given intervals and find a point (or point) where the derivative vanishes : $f(x) = \sin^4 x + \cos^4 x \ln \left[0, \frac{\pi}{2}\right]$

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461. Discuss the applicablity of Rolle's theorem for the following functions

in the indicated intervals:





462. Discuss the applicablity of Rolle's theorem for the following functions in the indicated intervals:

f(x) = |x| in [-1,1]



463. Discuss the applicablity of Rolle's theorem for the following functions in the indicated intervals:

 $f(x) = 3 + (x-2)^{2/3}$ in [1,3]



464. Discuss the applicablity of Rolle's theorem for the following functions in the indicated intervals:





f(x) = (x-1)(2x-3) in [1,3]

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466. Discuss the applicability of Rolle's theorem for the following

functions

 $f(x) = |x-1|, x \in [0,2]$

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467. Discuss the applicablity of Rolle's theorem for the following functions in the indicated intervals:





468. Discuss the applicablity of Rolle's theorem for the following functions in the indicated intervals:

f(x) = x in [1,2]

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469. Apply Rolle's theorem to find point (or points) on the following curves where the tangent is parallel to x -axis. $y = x^2$ in[-2.2]

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470. Apply Rolle's theorem to find point (or points) on the following curves where the tangent is parallel to x -axis. $y = -1 + \cos x in [0, 2\pi]$

471. Apply Rolle's theorem to find oint (or points) on the following curves

where the tangent is parallel to x -axis. $y = 16 - x^2, x$ in[-1, 1]



curves where the tangent is parallel to x -axis. $y = (x - 4)x \ln[0, 4]$

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473. It is given that for the function 'f' given by :
$$f(x)=x^3+bx^2+ax, x\in [1,3]$$
 Rolle's Theorem holds with $c=2+rac{1}{\sqrt{3}}.$ Find the values of 'a' and 'b'.

474. Discuss the applicability of Rolle's Theorem for the function :

$$f(x) egin{cases} \left\{ egin{array}{cc} (x^2+1) & whe0 \leq x \leq 1 \ 3-x & when1 < x \leq 2 \end{array}
ight.$$

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475. If f and g are differentiable functions for $0 \le x \le 1$ such that f(0) = 2, g(0), f(1) = 6, g(1) = 2, then show that there exists c satisying 0 < c < 1 and f' (c) = 2g' (c)

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476. Verify Lagrange's mean value theorem for the function f(x) in the

interval [3,5] where f(x) =(x-3)(x-6)(x-9)
477. Verify Lagrange's mean value theorem for the following functions in the given interval and also find 'c' of this theorem:

 $f(x)=2x-x^2$ on [0,1]

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478. Verify Lagrange's mean value theorem for the following functions in the given interval and also find 'c' of this theorem:

$$f(x)=x(x-3)$$
in [2,4]

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479. Verify Lagrange's mean value theorem for the following functions

$$f(x)=x^3-2x^2-x+3$$
 in the interval $[0,1]$

480. Verify Lagrange's mean value theorem for the following functions in

the given interval and also find 'c' of this theorem:

$$f(x)=(x)(x-1)(x-2)\mathsf{in}iggl[0,rac{1}{2}iggr]$$

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481. Verify Lagrange's mean value theorem for the following functions in the given interval and also find 'c' of this theorem:

$$f(x) = \log x$$
 in [1,2]

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482. Verify Lagrange's mean value theorem for the following functions in

the given interval and also find 'c' of this theorem:

$$f(x)=\sin x-\sin 2x$$
in $[0,\pi]$

483. Verify Lagrange's mean value theorem for the following functions in

the given interval and also find 'c' of this theorem:

$$f(x) = (x-1)(x-2)(x-3){
m in}[0,4]$$

484. Verify Lagrange's mean value theorem for the following functions in the given interval and also find 'c' of this theorem:

$$f(x)=\sqrt{x^2-4}$$
in [2,4]

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485. Verify Lagrange's mean value theorem for the following functions in the given interval and also find 'c' of this theorem:

$$f(x)=\sqrt{25-x^2}$$
in[1,5]

486. Differentiate the function $f(x) = \sqrt{x-2}$



487. Verify Lagrange's mean value theorem for the following functions in

the given interval and also find 'c' of this theorem:

 $f(x)=x^{2\,/\,3}$ in [0,1]

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488. Verify Lagrange's mean value theorem for the following functions in

the given interval and also find 'c' of this theorem:

 $f(x)= an^{-1}$ in [0,1]

489. Verify Lagrange's mean value theorem for the following functions in

the given interval and also find 'c' of this theorem:

$$f(x)=rac{1}{4x-1}$$
in [1,4]

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490. Show that Lagrange's theorem is not applicable to the function $f(x) = rac{1}{x}$ in [-1,1]

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491. Discuss applicability of Lagrange's mean value theorem to the

function $f(x) = (x-1)^{2/3}$ in [1,2]

492. Verify the Lagrange's Mean Value Theorem for the functions:

f(x) = ert x ert in the interval [-1,1]



493. Find a point on the curve $y=x^2$ where the tangent is parallel to the

chord joining (0,0) and (1,1)

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494. Find a point on the curve $y = x^3$ where the tangent is parallel to the

chord joining (1,1) and (3,27)

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495. Lagrange's Theorem to determine a point P on the curve $f(x) = \sqrt{x-2}$ defined in the interval [2,3], where the tangent is parallel





496. Using Mean value Theorem, prove that there is a point on the curve

 $y=2x^2-5x+3$ between the point A(1,0) and B(2,1). Where the tangent

is parallel to the chord AB. Also find that point.





 $\cot 7x + 3x^5 + \sin 3x$

503. Let $f(x)=rac{e^{1/x}}{1+e^{1/x}}$ for x
eq 0. Find f (0) if f is left continuous at x =

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504. Show that the function
$$f(x) = \begin{cases} x^n \sin\left(rac{1}{x}\right) & x
eq 0 \\ 0 & x = 0 \end{cases}$$
 is continuous

but not differentiable at x= 0.

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505. Find a \in R so that $f(x) = egin{cases} x^2 & x \geq 0 \\ ax & x < 0 \end{bmatrix}$ is continuous at 0.

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506. Let $f(x) = rac{2^{rac{1}{x}}}{1+2^{rac{1}{x}}}$ for x
eq 0. Find f(0) if f is right continuous at x = 0

507. Let
$$f(x) = [\sin x]$$
, is f continuous at $x = rac{\pi}{2}$

508. Let
$$f(x) = \begin{cases} 2x-5 & ext{if} \quad x \geq 2 \\ x^2 & ext{if} \quad x < 2 \end{cases}$$
. Is f continuous at x = 2?

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509. Determine the value of the constant k so that the function $f(x) = \begin{cases} 3x - 8 & \text{if } x \leq 5\\ 2k & \text{if } x > 5 \end{cases}$ is continuous at x = 5
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510. Given
$$f(x) = \frac{1}{x+2}$$
. Write down the set of points of discontinuity of f(f(x))

511. Write down the domain of continuity of the function f(x) = x|x|

512. Let f(x) =
$$|x|\cos\left(\frac{1}{x}\right)$$
 for $x \neq 0$. Write the down the value of (f) (0) if f

is continuous at x = 0

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513. Write down the domain of continuity of $f(x) = e^{|x|}$



514. Let f(x) = x[x]. Is f continuous on left of x = 2.

515. Find the value of 'k', such that the function :

$$f(x)=iggl\{rac{2x^{x+2}-16}{4^x-16}, ext{ if } x
eq 2iggr), (k, ext{ if } x=2) ext{ is continuous at x}$$
=2

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516. Find
$$rac{d}{dx} igg(rac{1}{\sqrt{1-x^2}}$$

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517. Compute
$$rac{d}{dx}(x|x|)whenx < 0$$

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518. Find
$$rac{dy}{dx}$$
 when $xy=1$

519. Write down the value of $rac{dy}{dx}$ at x=e when $y=\log_a x$

520. Compute
$$rac{d}{dx}ig(\sin^{-1}(\sin x)ig)$$
 when $rac{\pi}{2}\leq x\leq rac{3\pi}{2}$

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521. Find
$$rac{d}{dx}ig(\cos^{-1}(\cos x)ig)$$
 when $\pi\leq x\leq 2\pi$

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522. Find
$$rac{d}{dx}ig(an^{-1}(an x)ig)when -rac{\pi}{2} < x < rac{\pi}{2}$$

523. Compute $\lim_{h o 0} \left(rac{\sin(x+h) - \sin x}{h}
ight)$

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524. Compute
$$rac{d}{dx}(\log_e |\sin x|), \ -rac{\pi}{2} < x < rac{\pi}{2}$$

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525. Find the value of $\sin^{-1}(\cos(\sin^{-1}x)) + \cos^{-1}(\sin(\cos^{-1}x))$

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526. If f(x) is an even function, state whether f'(x) is an odd function or an

even function.

527. Find
$$rac{dy}{dx} when y = x^x, x > 0$$



528. Compute
$$\frac{d}{dx}\left(\frac{\log x}{x}\right)$$

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529. If x = sin t, y = cos t, find
$$\frac{dy}{dx}$$

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530. Find the differential coefficient of $\sqrt{1+x^2}$ w.r.t $1+x^2$

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531. If $f(x) = \log_x (\log x)$ then the value of f'(e) is



535. If $y = x^2$, write the value of $(d^3y)/(d(x)^3)$ at x = 0

536. What is the value of the $\underset{h
ightarrow 0}{L} t igg(rac{\log(e+h) - \log e}{h} ?$

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537. If
$$y = \sin^{-1} igg(rac{2x}{1+x^2} igg)$$
 and -1 < x < 1, $f \in d$ dy/dx

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538. Find
$$rac{d}{dx}(\sin(\cos x)+\cos(\sin x))$$

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539. Find
$$rac{d}{dx} \Big(e^{\sqrt{1+x^2}} \Big)$$

540. Find
$$rac{d}{dx} \Big(2^{\cos^2 x} \Big)$$

541. Compute
$$rac{d}{dx}ig(\sin^nig(ax^2+bx+cig)ig), n\in N.$$

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542. If
$$f(x) = \sin^{-1}x + \cos^{-1}x$$
, find f' (x)

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543. Find
$$\displaystyle rac{d}{dx} igg(\displaystyle rac{8^x}{x^8} igg)$$

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544. Compute
$$\frac{d}{dx} \left\{ \sin^{-1} \left(\frac{1}{\sqrt{x+1}} \right) \right\}$$

545. Evaluate $\frac{d}{dx}(\sin^m x \cos^n x)$, where m,n inN`.



546. If
$$y = (\sin x)^{\cos x}$$
, find $\frac{dy}{dx}$

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547. Differentiate
$$\frac{x}{\sin x} w. r. t \sin x$$

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548. If
$$y = an^{-1} x$$
, find $rac{d^2 y}{dx^2}$ in terms of y alone.

549. Find
$$rac{dy}{dx}$$
 when $an^{-1}ig(x^2+y^2ig)=a^2$

550. If
$$y = t + rac{1}{t}$$
 and $x = t - rac{1}{t}$ find $rac{dy}{dx}$



551. Find
$$rac{dy}{dx} wheny = an(x+y)$$

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552. Find
$$\frac{d}{dx}(\tan\sqrt{x})$$

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553. Find
$$\frac{d}{dx}(\tan\sqrt{x})$$

554. If $f(x) = |\sin x - \cos x|$, find f' $(\pi/6)$



555. If
$$f(x) = |\sin x| + |\cos x|$$
, find $f'\left(rac{3\pi}{4}
ight)$

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556. If
$$y = \sec x + \tan x$$
, then prove that $\displaystyle rac{dy}{dx} = \displaystyle rac{1}{1 - \sin x}$

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557. Can Rolle's Theorem be applied to the function f(x) = |x| in the interval [-2,2]

558. Does there exist a point $c(\ \in\)\Big(0, rac{\pi}{2}\Big)$ such that f' (c)= 0 where f(x) =

sin 2x`?



560. Is Lagrange's Theorem applicable to the function f(x) = |x| on the interval [-1,2]



561. Can we find a point $c^{\in}\left(-\frac{\pi}{2},\frac{\pi}{2}\right)$ such that f'© = 0 where f(x) =

|sinx|



562. Find a point $c^{\,\in}(\,-1,2)$ such that $f' @= rac{f(2)-f(\,-1)}{2-(\,-1)}$ where $f(x)=x^2$

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563. At what point on the curve y = (cos x -1) in $[0, 2\pi]$, is the tangent

parallel to x-axis?



565. Examine the continuity of the function $f(x) = 2x^2 - 1$ at x = 3



569. Examine the following function for continuity: f(x) = |x - 5|



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571. Is the function f defined by $f(x) = \begin{cases} x & \text{if } x \leq 1 \\ 5 & \text{if } x > 1 \end{cases}$

continuous at, x=0?At x=1? At x=2?

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572. Find all the points of discontinuity of f, where f is defined by

$$f(x) = egin{cases} 2x+3, \;\; ext{if} \;\; x \leq 2 \ 2x-3, \;\; ext{if} \;\; x > 2 \end{cases}$$

573. Find all points of discontinuity of f, where f is defined by : `f(x)= $\{(|x|+3,...,if x \le -3), (-2x,...,if -3=3):\}$ `



574. Find all points of discontinuity of f, where f is defined by :

$$f(x) = egin{cases} rac{ert x ert}{x} & ext{if} & x
eq 0 \ 0 & ext{if} & x = 0 \end{cases}$$

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575. Find all points of discontinuity of f, where f is defined by:

$$f(x) = egin{cases} rac{x}{|x|} & ext{if} \;\; x < 0 \ -1 & ext{if} \;\; x \ge 0 \end{cases}$$

576. Find all points of discontinuity of f, where f is defined by

$$f(x) = egin{cases} x+1 & ext{ if } x \geq 1 \ x^2+1 & ext{ if } x < 1 \end{cases}$$

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577. Find all points of discontinuity of f, where f is defined by :

$f(x) = \Big\{$	x^3-3	x	\leq	2
	x^2+1	x	>	2

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578. Find all points of discontinuity of f, where f is defined by :

$$f(x) = egin{cases} x^{10}-1 & x \leq 1 \ x^2 & x > 1 \end{cases}$$

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579. Is the function defined by $f(x)=egin{cases} x+5 & ext{if} \quad x\leq 1 \ x-5 & ext{if} \quad x>1 \ \end{array}$ a

continuous function?

580. Disuss the continuity of the function f where f is defined by

$$f(x) egin{cases} 3 & ext{if} & 0 \leq x \leq 1 \ 4 & ext{if} & 1 < x < 3 \ 5 & ext{if} & 3 \leq x \leq 10 \end{cases}$$

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581. Discuss the continuity of the function f, where f is defined by:

$$f(x) = egin{cases} 2x & ext{if} \;\; x < 0 \ 0 & ext{if} \;\; 0 \leq x \leq 1 \ 4x & ext{if} \;\; x > 1 \end{cases}$$

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582. Discuss the continuity of the function f, where f is defined by:

$$f(x) = egin{cases} -2 & ext{if} \;\; x \leq -1 \ 2x & ext{if} \;\; -1 \leq x \leq 1 \ 2 & ext{if} \;\; x > 1 \end{cases}$$

583. Find the relationship between a and b so that the function f defined

by:
$$f(x)=egin{cases} ax+1 & ext{if} \quad x\leq 3 \ bx+3 & ext{if} \quad x>3 \end{cases}$$
 is continuous at $x=3$

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584. For what value of λ is the function defined by $f(x) = \{\lambda(x^2 - 2x), \text{ if } x \leq 0, 4x + 1, \text{ if } x > 0\}$ continuous at x = 0? What about continuity at x = 1?

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585. Show that the function defined by g(x) = x - [x] is discontinuous at all integral points. Here [x] denotes the greatest integer less than or equal to x.





589. Discuss the continuity of the following function: $f(x) = \sin x \cdot \cos x$



590. Discuss the continuity of the cosine, cosecant, secant and cotangent

functions.



592. Determine if f defined by :
$$f(x) = \begin{cases} x^2 \sin\left(\frac{1}{x}\right) & \text{if } x \neq 0 \\ 0 & \text{if } x = 0 \end{cases}$$
 is

a continuous function?

593. Examine the continuity of f, where f is defined by $f(x) = \begin{cases} \sin x - \cos x & \text{if } x \neq 0 \\ -1 & \text{if } x = 0 \end{cases}$

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594. Find the values of k so that the function f is continuous at the

indicated point : $f(x) = \begin{cases} k rac{\cos x}{\pi - 2x} & ext{if } x
eq rac{\pi}{2} \\ 3 & ext{if } x = rac{\pi}{2} \end{cases}$ at $x = rac{\pi}{2}$

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595. In the following, determine the constant so that given function is

continuous at indicated point:

$$f(x)=egin{cases} kx^2 & ext{ if } & x\leq 2\ 2 & ext{ if } & x>2 \end{cases}$$
 at x =2

596. Determine the value of the constant k so that the function

$$f(x) = egin{cases} kx+1 & ext{if} \quad x \leq 5 \ 3x-5 & ext{if} \quad x > 5 \end{cases}$$
 is continuous at x = 5.

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597. Find the values of a and b such that the function defined by

$$f(x)egin{cases} 5 & ext{if} \quad x\geq 2\ ax+b & ext{if} \quad 2< x < 10 ext{ is continuous.}\ 21 & ext{if} \quad x\geq 10 \end{cases}$$

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598. Show that the function defined by $f(x) = \cos(x^2)$ is a continuous

function.



599. Show that the function defined by $f(x) = |\cos x|$ is a continuous

function.



602. Differentiate the following functions with respect to x. $\sin(x^3 + 5x)$





differentiale at x =1
611. Prove that f(x) = [x], 0 < x < 3 is not differentiable at x = 1 but x = 2.



612. Find
$$\frac{dy}{dx}$$
 in the following:

2x+3y = sinx

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613. Find
$$\frac{dy}{dx}$$
 in the following :

 $2x + 3y = \sin y$ `



614. Find
$$\frac{dy}{dx}$$
 in the following: $ax + by^2 = \cos y$

615. Find
$$\displaystyle rac{dy}{dx}$$
 in the following: $xy+y^2= an x+y$

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616. Find
$$rac{dy}{dx}$$
 in the following: $x^2 + xy + y^2 = 100$

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617. Find
$$rac{dy}{dx}$$
 in the following: $x^3 + x^2y + xy^2 + y^3 = 81$

618. Find
$$rac{dy}{dx}$$
 in the following: $\sin^2 y + \cos xy = \pi$

619. Find
$$rac{dy}{dx}$$
, if $\sin^2 x + \cos^2 y = 1$

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620. Find
$$rac{dy}{dx}$$
 in the following: $y=\sin^{-1}igg(rac{2x}{1+x^2}igg)$

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621. Differentiate the following w.r.t. x:

$$an^{-1}igg(rac{3x-x^3}{1-3x^2}igg), \ -rac{1}{\sqrt{3}} < x < rac{1}{\sqrt{3}}$$

622. Find
$$rac{dy}{dx}$$
 in the following: $y = \cos^{-1} igg(rac{1-x^2}{1+x^2} igg), 0 < x < 1$

623. Find
$$\frac{dy}{dx}$$
 in the following: y=sin^-1((1 - x^2)/(1+x^2), 0)

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624. Differentiate the following w.r.t. x:

$$\cos^{-1} igg(2 rac{x}{1+x^2} igg), \; -1 < x < 1$$

625. Find $rac{dy}{dx}$ in the following: $y=\sin^{-1}\left(2rac{x}{1+x^2}
ight)$

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626. Find
$$rac{dy}{dx}$$
 in the following: $y = \sec^{-1} igg(rac{1}{2x^2 - 1} igg), 0 < x < rac{1}{\sqrt{2}}$

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627. Differentiate the following w.r.t. x :

 e^x

 $\sin x$



628. Differentiate the following w.r.t x

 $e^{\sin^{-1}x}$



633. Differentiate the following w.r.t.x :

$$\sqrt{e^{\sqrt{x}},x>0}$$

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634. Differentiate the following w.r.t.x :

 $\log(\log x), x < 1$

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635. Differentiate the following w.r.tx:

 $rac{\cos x}{\log x}, x > 0$



636. Differentiate the functions :

 $\cos x \cos 2x \cos 3x$







645. Differentiate the function w.r.t. ${ t x}: x^{x\cos x} + rac{x^2+1}{x^2-1}$



646. Differentiate the following w.r.t. x:

$$\left(x\cos x
ight)^{x}+\left(x\sin x
ight)^{1/x}$$

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647. Find
$$\displaystyle rac{dy}{dx}$$
 of the function $: x^y + y^x = 1$

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648. Find
$$rac{dy}{dx}$$
 if $x^y = y^x$.

649. Find
$$\frac{dy}{dx}$$
 of the function $:(\cos x)^y = (\cos y)^x$

650. Find
$$\displaystyle rac{dy}{dx}$$
 of the function ${:}xy=e^{x\,-\,y}$

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652. Differentiate $\left(x^2-5x+8
ight)\left(x^3+7x+9
ight)$ by using product rule.

653. Differentiate $\left(x^2-5x+8
ight)\left(x^3+7x+9
ight)$ by expanding the product

to obtain a single polynomial.



654. Differentiate $(x^2 - 5x + 8)(x^3 + 7x + 9)$ by using product rule.

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655. If u, v and w are functions of x, then show that $d/dx(u \ cdot v \ cdot w) = du/dx (v \ cdotw + u \ cdot \ dv/dx \ cdotw + u \ cdot v \ dw/dx) in two ways - first by repeated application of product rule, second by logarithmic differentiation.$



656. Find $\frac{dy}{dx}$, if x and y are connected parametrically by the equations,

given below without eliminating the parameter.

$$x=2at^2,y=at^4$$

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657. Find $\frac{dy}{dx}$, if x and y are connected parametrically by the equations (without eliminating the parameter).

$$x=a\cos heta,y=b\cos heta$$

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658. Find $\frac{dy}{dx}$, if x and y are connected parametrically by the equations (without eliminating the parameter).

$$x = \sin t, y = \cos 2t$$

659. Find $\frac{dy}{dx}$, if x and y are connected parametrically by the equations,

given below without eliminating the parameter.

$$x=4t,y=rac{4}{t}$$

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660. Find $\frac{dy}{dx}$, if x and y are connected parametrically by the equations, given below without eliminating the parameter. $x \cos \theta - \cos 2\theta, y = \sin \theta - \sin 2\theta$

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661. Find $\frac{dy}{dx}$, if x and y are connected parametrically by the equations, given below without eliminating the parameter. $x = a(\theta - \sin \theta), y = a(1 + \cos \theta)$

662. Find
$$\frac{dy}{dx}$$
 if $x = \frac{\sin^3 t}{\sqrt{\cos 2t}}, y = \frac{\cos^3 t}{\sqrt{\cos 2t}}$

663. Find $\frac{dy}{dx}$, if x and y are connected parametrically by the equations

(without eliminating the parameter).

$$x=aigg(\cos t+\log anigg(rac{t}{2}igg)igg), y=a\sin t.$$

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664. Find $\frac{dy}{dx}$, if x and y are connected parametrically by the equations

(without eliminating the parameter).

 $x = a \sec \theta, y = b \tan \theta.$

665. Find $\frac{dy}{dx}$, if x and y are connected parametrically by the equations

(without eliminating the parameter).

$$x=a(\cos heta+ heta\sin heta),y=a(\sin heta- heta\cos heta)$$

666. If
$$x=\sqrt{a}^{\sin^{-1}t}, y=\sqrt{a^{\cos^{-1}t}}$$
 , show that $rac{dy}{dx}=-rac{y}{x}, a>0$

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667. Find the second order derivatives of the function : $x^2 + 3x + 2$





673. Find the second order derviatives of the functions :





679. If $y=3\cos(\log x)+4\sin(\log x)$ show that $x^2y_2+xy_1+y=0$

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680. Find the second order derivative of the following functions

If
$$y=ae^{mx}+be^{-mx}$$
 , prove that $\displaystyle rac{d^2y}{dx^2}-m^2y=0$

681. If
$$y=500e^7x+600e^{-7}x$$
 show that $\left(d^2rac{y}{dx^2}
ight)=49y$

682. If
$$e^y(x+1)=1$$
 show that $\left(d^2rac{y}{dx^2}
ight)=\left(rac{dy}{dx}
ight)^2$ ਹੈ।

683. If
$$y = [\tan^{-1} x]^2$$
, then prove that :
 $(x^2 + 1)^2 y_2 + 2x(x^2 + 1)y_1 = 2.$
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684. Verify Rolle's theorem for the function
 $f(x) = x^2 + 2x - 8, x \in [-4, 2]$
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685. Examine if Rolle's theorem is applicable to any of the following functions. Can you say some thing about the converse of Rolle's theorem from these example? f(x) = [x] for $x \in [5, 9]$



686. Examine if Rolle's theorem is applicable to any of the following functions. Can you say some thing about the converse of Rolle's theorem from these example? f(x) = [x] for $x \in [-2, 2]$



687. Examine if Rolle's theorem is applicable to any of the following functions. Can you say some thing about the converse of Rolle's theorem from these example? $f(x)=x^2-1$ for $x\in [1,2]$

688. If $f \colon [\,-5,\,5] o R$ is a differentiable function and if f'(x) does not

vanish anywhere, then prove that f(-5)
eq f(5)



689. Verify Mean Value Theorem, if $f(x) = x^2 - 4x - 3$, in the interval [a,

b], where a = 1 and b = 4.

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690. Verify Mean Value Theorem, if $f(x) = x^3 - 5x^2 - 3x$, in the interval

[a, b], where a = 1 and b = 3. Find all $c \in (1, 3)$ for which f'(c) = 0.

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691. Examine the applicability of Mean Value Theorem for all three functions given in the above exercise 2. (i) f(x) = [x] for $x \in [5,9]$ (ii) f(x) = [x] for $x \in [-2,2]$ (iii) f(x) = [xsqrt -1] for $x \in [1,2]$



696. Differentiate w.r.t. x the function $:(\log x)^{\log x}, x>1$



697. Differentiate w.r.t. x the function : $\cos(a\cos x + b\sin x)$, for some

constant a and b.

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698. Differentiate w.r.t. x the function $: x^x + x^a + a^x + a^a$, for some fixed

```
a>0 and x>0
```

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699. Differentiate w.r.t. x the function : $x^{x^2-3} + (x-3)^{x^2}$, f or x>3

700. Find dy/dx if y =12(1-cost), x =10(t-sint)



701. Find
$$rac{dy}{dx}$$
 if $y = \sin^{-1}x + \sin^{-1}\sqrt{1-x^2}, 0 < x < 1$

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702. If $x\sqrt{1+y} + y\sqrt{1+x} = 0$ for x lies between -1 and 1' prove that dy/dx =-1/(1+x)^2

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703. If
$$\cos y = x \cos(a + y)$$
, with $\cos a \neq \pm 1$, prove that $\frac{dy}{dx} = \frac{\cos^2(a + y)}{\sin a}$

704. If
$$x=a(\cos t+t\sin t)$$
 and $y=a(\sin t-t\cos t)$, find $\displaystyle rac{d^2y}{dx^2}$



705. If $f(x) = |x|^3$ show that f''(x) exists for all real x and find it.



706. Using mathematical induction prove that $d\frac{x^n}{dx} = nx^{n-1}$ for all positive integers n.



707. Using the fact that $\sin(A+B)=\sin A\cos B+\cos A\sin B$ and the

differentiation, obtain the sum formula for cosines.



708. Does there exist a function which is continuous everywhere but not

differentiable at exactly two points? Justify your answer.

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709. If
$$y = \begin{vmatrix} f(x) & g(x) & h(x) \\ 1 & m & n \\ a & b & c \end{vmatrix}$$
, prove that
$$\frac{dy}{dx} = \begin{vmatrix} f'(x) & g'(x) & h'(x) \\ 1 & m & n \\ a & b & c \end{vmatrix}$$

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710. If
$$y = e^{a\cos^{-1}x}, -1 \le x \le 1$$
, show that

$$ig(1-x^2)rac{d^2y}{dx^2}-xigg(rac{dy}{dx}igg)-a^2y=0$$



714. If
$$f(x) = \left\{egin{array}{ccc} ax+1 & ext{if} & x\geq 1 \ x+2 & ext{if} & x<1 \end{array}
ight.$$

is continuous, then 'a' should be

equal to ____

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715. Find a
$$\in$$
 R so that $f(x) = egin{cases} x^2 & x \geq 0 \\ ax & x < 0 \end{bmatrix}$ is continuous at 0.

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716. Fill in the blanks:

For all
$$\mathsf{x} \in (6,7), rac{d}{dx}([x])$$
 =

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717. Fill in the blanks:

Derivative of sin x w.r.t cos x is

Derivative of x^2 wr.t x^3 is



719. Fill in the blanks:

If
$$x \geq 0$$
, then $rac{d}{Dx} iggl\{ \cos^{-1} iggl(rac{1-x^2}{1+x^2} iggr) iggr\}$ is equal to

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720. The derivative of sin x cos x w.r.t. x is



721. Fill in the blanks:

The derivative of $\log_{10} x$ w.r.t x is `..... .

If
$$f(x) = |{
m sin}\,x|$$
, then $f'\Big(rac{\pi}{4}\Big)$ is equal to

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723. Fill in the blanks:

Domain of continuity of the function f(x) = |x-1| is

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724. Fill in the blanks:

An example of a function which is continuous everywhere but fails to be

differentiable exactly at two points 2 and 3 is

For the curve
$$\sqrt{x}+\sqrt{y}=1, rac{dy}{dx}atigg(rac{1}{4},rac{1}{4}igg)$$
 is

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726. Fill in the blanks:

If $f(x) = x^{2/3}$, then f'(0) is

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727. Fill in the blanks:

Rolle's Theorem is not applicable to the function $f(x)=\left(x-1
ight)^{2/3}$ on

[0,2] as f is not derivable at



728. Every continuous function is differentiable.

729. True or False :

$$rac{d}{dx}(\log x)=rac{1}{x}$$
 for all $x
eq 0.$



$$rac{d}{dx}(\log \lvert x
vert) = rac{1}{x}$$
 for all $x
eq 0$

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731. If f is continuous on its domain D, then |f| is also continuous on D.



732. True or False :

Rolle's Theorem is applicable to the function $f(x) = |\sin x| \ln \left[-\frac{\pi}{2}, \frac{\pi}{2} \right]$

733. Verify the truth of Rolle's Theorem for the following functions:

f(X) = |x-1| in [1,2]

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734. True or False :

The function $f(x) = \log x^2$ has only one point of discontinuity.

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735. The composition of two continuous function is a continuous function.

736. true false: $\cos|x|$ is differentiable every where.



737. True or False :

The function $f(x)=egin{cases} x+a & x\geq 1\ ax^2+1 & x<1 \end{cases}$ is continuous at x = 1, whatever

'a' may be.

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738. True or False :

The function $f(x) = |\sin x|$ is differentiable at all $x \in R$.

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739. Find a
$$\in$$
 R so that $f(x) = egin{cases} x^2 & x \geq 0 \\ ax & x < 0 \end{bmatrix}$ is continuous at 0.

740. For continuity, at x=a, each of $\lim_{x o a^+} f(x)$ and $\lim_{x o a^-} f(x)$ is equal

to f(a).



741. True or False :

$$rac{d}{dx}(\log_{10}x)=rac{1}{x}f \,\, ext{or} \,\, allx>0$$

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742. True or False :

If $\underset{x
ightarrow a}{L} tf(x)g(x)$ exists then both $\underset{x
ightarrow a^+}{L} tf(X)$ and $\underset{x
ightarrow a^-}{L} tg(x)$ exist

separately.
743. If $f \cdot g$ is continuous at x=a, then f and g are separately continuous at

x=a.

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744. All trigonometric functions have inverse over their respective domains.

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745. True or False :

An increasing function is always a continuous function.



746. True or False :

The function f(x) = |x-1| is a continuous function.



747. True or False :

Derivative of an even function is always an odd function.



749.
$$\lim_x o 0 rac{e^x-1}{x}$$
 is equal to :

A. 0

B. 1

C. e

D. none of these

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750. If a>0,
$$a
eq 1$$
, then $\log_a(x^n) =$

A. $n \log_a x$

$$\mathsf{B}.\,n + \log_a x$$

C.
$$\frac{1}{n}\log_a x$$

D. none of these

751. Which of the following is not true

A.
$$1 < rac{e^x - 1}{x} < rac{1}{1 - x} f \, \, ext{or} \, \, 0 < x < 1$$

$$\mathsf{B}.\log(1+x) \leq xf \,\, \mathrm{or} \,\, x \geq 0$$

$$\mathsf{C}.\log(1+x) < xf ext{ or } x > 0$$

D.
$$\log(1+X) < xf \, ext{ or } \, x \geq 0)$$

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752.
$$\lim_{x \to 0} \frac{e^x - 1}{x}$$
 is equal to A. 2

B. 0

C. 1

753.
$$\lim_x o 0igg(rac{\log(1+x)}{\sin x}$$
 is equal to :

A. 0

B. 1

C. e

D. none of these

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754.
$$Lt_{x o e} igg(rac{\log x - 1}{x - e} igg)$$
 is equal to

A. 1

B. 0

C. e

D.
$$\frac{1}{e}$$

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755. The function
$$f(x)= egin{cases} rac{\sin x}{x}+\cos x & ext{ if } x
eq 0 \\ k & ext{ if } x=0 \end{cases}$$
 is continuous at

x=0, then then value of ' k ' is

A. 3

B. 2

C. 1



756. If (x) = 2x and $g(x) = \frac{x^2}{2} + 1$, then which of the following can be

a discontinuous function

A. f(x) + g(x)

B. f(x) - g(x)

C. f(x)g(x)

D.
$$\frac{g(x)}{f(x)}$$

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757. Let $f(x)=egin{cases} x+a & x\leq 1\ ax^2+1 & x>1 \end{bmatrix}$. Show that f is continuous at 1. Find 'a'

so that it is derivable at 1.

A. a = 0

B. a = 1

C. all $a \in R$

D. none of these



758. Let
$$f(x)= egin{cases} rac{3x+4 an x}{x} & x
eq 0\ k & x=0 \end{cases}$$
 then f is continuous at x = 0 for

- B. k = 1
- C. no k

D. none of these

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759. Let $f(x) = x igg(rac{2^x - 1}{1 - \cos x} igg)$ for x
eq 0. What choice of f(0), if any, will

make f continous at 0?

B.
$$\frac{1}{2}\log 2$$

C. $\frac{1}{2}\log 2$

D. 2 log 2

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760. If $f(x) = x^2 \sin \frac{1}{x}$, where $x \neq 0$ then the value of the function f at x=0, so that the function is continuous at x=0, is

A. 0

 $\mathsf{B.}-1$

C. 1

761. The value of 'k' which makes the function defined by :

$$f(x) = \begin{cases} \sin\left(\frac{1}{x}\right) & \text{if } x \neq 0 \\ k & \text{if } x = 0 \end{cases}$$
continuous at x =0 is
A. 8
B. 1
C. -1
D. none of these

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762. The function given by f(x)=tax x is discontinuous on the set

A.
$$(n\pi\colon n\in Z)$$

B. $(2n\pi\colon
eq Z)$
C. $\Big\{(2n+1)rac{\pi}{2}, n\in Z\Big)$

D.
$$\left\{rac{n\pi}{2}, n\in Z
ight\}$$



763. The function $f(x) = \cot x$ is discontinuous on the set

A.
$$(x=n\pi\!:\!n\in Z)$$

B.
$$(x=2n\pi, n\in Z)$$

D.
$$\left\{x=rac{n\pi}{2}, n\in Z
ight\}$$

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764. The function f(x) = [x], where [x] denotes the greatest integer function, is continuous at

A. 4	
B2	
C. 1	

D. 1.5

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765. The number of points at which the function $f(x) = rac{1}{x-[x]}$ is not

continuous is

A. 1

B. 2

C. 3

766. The function $f(x)=rac{4-x^2}{4x-x^3}$ is

A. discontinuous at only one point

B. disconitnuous exactly at two points

C. discontinuous exactly at three poins

D. none of these

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767. Let f(x) = x |x|, then f(0) is equal to

A. 1

B. -1

C. 0

768. If f(x) = log |x|, then for $x \neq 0$ f'(x) is equal to



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769. Let $f(x) = |\sin x|$. Then

A. f is everywhere differentiable

B. f is everywhere continuous but not differentiable at x = $n\pi, n \in Z$

$$x=(2n+1)rac{\pi}{2},n\in Z$$

D.

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770. The set of points where the function f given by $f(x) = |2x-1| \sin x$

is differentiable is

A. R

B.
$$R-\left\{rac{1}{2}
ight\}$$
C. $(0,\infty)$



771. Lt f(x) = |cos x|, then

A. f is differentiale at all $x \in R$

B. f is continuous at all ξnR but not differentiable at $x=n\pi, n\in Z$

C.f is continuous every where but not differentiable at

$$x=(2n+1)rac{\pi}{2},n\in Z$$

D. none of these

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772. If
$$u=\sin^{-1}\left(2rac{x}{\left(1+x
ight)^2}
ight)\,\, ext{an}\,\,v= an^{-1}\left(2rac{x}{1-x^2}
ight)$$
, the $drac{u}{d}v$ is

A.
$$\frac{1}{2}$$

B. x

C.
$$rac{1-x^2}{|1-x^2|}$$

D. 1

773. The derivative of
$$\cos^{-1} \left(2x^2 - 1
ight)$$
 w.r.t. $\cos^{-1} x$ is

B.
$$\displaystyle rac{2x}{|x|}$$

C. $\displaystyle 1-x^2$

A. 2

D.
$$rac{-1}{\sqrt{2}(1-x^2)}$$

774. If
$$y=\logigg(rac{1-x^2}{1+x^2}igg)$$
, then $rac{dy}{dx}$ is equal to A. $rac{4x^3}{1-x^4}$ B. $rac{-4x}{1-x^4}$

C.
$$rac{1}{4x-x^4}$$

D. $rac{-4x^3}{1-x^4}$

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775.
$$\frac{d}{dx} \left\{ \log \left(x + \sqrt{x^2} + 1 \right) \right\} is$$
A.
$$\sqrt{X^2 + 1}$$
B.
$$\frac{x}{\sqrt{x^2 + 1}}$$
C.
$$x\sqrt{x^2 + 1}$$
D.
$$\frac{1}{\sqrt{x^2 + 1}}$$

776. If
$$y=rac{e^x-e^{-x}}{e^x+e^{-x}}$$
, then $rac{dy}{dx}$ =

A. $1+y^2$

B.
$$y^2 - 1$$

$$\mathsf{C.}\,1-y^2$$

D. none of these

777. If
$$y=\sqrt{\sin x+y}$$
 , then $\displaystyle rac{dy}{dx}$ is equal to

A.
$$\frac{\cos x}{2y - 1}$$

B.
$$\frac{\cos x}{1 - 2y}$$

C.
$$\frac{\sin x}{1 - 2y}$$

D.
$$\frac{\sin x}{2y - 1}$$

778. If
$$x=t^2, y=t^3,$$
 then $\displaystyle rac{d^2 y}{dx^2}$ is A. $\displaystyle rac{3}{2}$ B. $\displaystyle rac{3}{4t}$ C. $\displaystyle rac{3}{2t}$

D. $\frac{3t}{2}$

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779. If
$$y=ae^{mx}+be^{-\,(\,mx\,)}$$
 , then $\displaystyle rac{d^2y}{dx^2}$ =

A. $m^2 y$ B. $-m^2 y$

C. my

D. - my

780. Lagranges's mean value theorem is not applicable to f(x) in [1,4] where f(X) =

A. $x^2 - 2x$ B. |x-2| C. x|x|

 $\mathsf{D.}\,x^3$

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781. The value of c in Rolle's Theorem for the function $f(x)=e^x\sin x,\,x\in[0,\,\pi]$ is A. $rac{\pi}{6}$

B.
$$\frac{\pi}{4}$$

C.
$$\frac{\pi}{2}$$

D. $\frac{3\pi}{4}$

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782. The value of 'c' in Rolle's Theorem for the function $f(x)=x^3-3x$ in the interval $\left[0,\sqrt{3}
ight]$ is



B. -1

C.
$$\frac{3}{2}$$

D. $\frac{1}{3}$

783. If
$$y = an^{-1}\left(2rac{x}{1-x^2}
ight) + \cos^{-1}\left(rac{1-x^2}{1+x^2}
ight), f \in d ext{dy/dx}$$
 in (0,1)`

A.
$$rac{4}{1+X^2}$$

B. 0

C.
$$rac{2}{1+x^2}$$

D. none of these

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784. If
$$f(x) = x^2 + rac{x^2}{1+x^2} + rac{x^2}{\left(1+x^2
ight)^2} + \dots$$
 up to ∞ , then at x = 0 , f(x)

A. has not limit

B. is continuous but not differentiable

C. is discontinuous

D. is differentiable

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785. For the function $f(x) = x + rac{1}{x}, x \in [1,3]$, the value of c for mean value theorem is

A. 1

B. $\sqrt{3}$

C. 2

D. none of these

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786. The value of 'c' in mean Value Theorem for the function $f(x)=x(x-2)\in [1,2]$ is

A.
$$\frac{3}{2}$$

B. $\frac{2}{3}$
C. $\frac{1}{2}$

D. none of these

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787. Let
$$f(x) = \sqrt{1 - \sqrt{1 - x^2}}$$
 then f(x) is

A. continuous on [-1,1] and differentiable on (-1,1)

B. continuous on [-1,1] and differentiable on $(\,-1,0),\,\,\cup\,(0,1)$

C. continuous and differentiableon (-1,1)

788. Domain of differentiability of the function $f(x) = |x-2| \cos x$ is

A. R

B. R - {2}

 $\mathsf{C}.\left(0,\infty
ight)$

D. none of these