

#### **MATHS**

# NCERT - NCERT MATHS (KANNADA ENGLISH)

# **TRIANGLES**

**Examples** 

**1.** In the given Figure AB and CD are intersecting at 'O', OA = OB and OD = OC. Show

that (i)  $\Delta AOD\cong \Delta BOC$  and (ii)

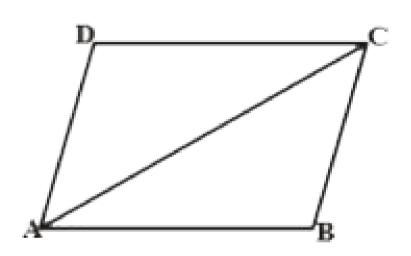
 $AD \mid BC$ .



**2.** AB is a line segment and line I is its perpendicular bisector. If a point P lies on I, show that P is equidistant from A and B.

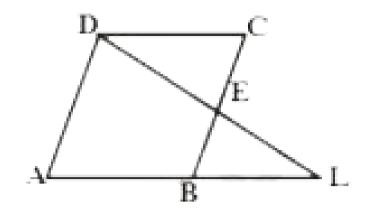


**3.** In the given figure, AB||DC| and AD||BC| show that  $\Delta ABC\cong \Delta CDA$ .



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**4.** In the given figure, AL || DC, E is mid point of BC. Show that  $\Delta EBL\cong\Delta ECD$ .



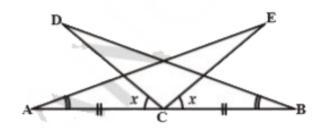


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**5.** Use the information given in the adjoining figure, to prove :

$$(i)\Delta DBC\cong\Delta EAC$$

(ii)DC = EC.



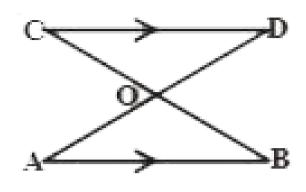


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**6.** Line-segment AB is parallel to another line-segment CD. O is the mid-point of AD.

Show that (i)  $\Delta AOB\cong \Delta DOC$  (ii) O is also

the mid-point of BC.

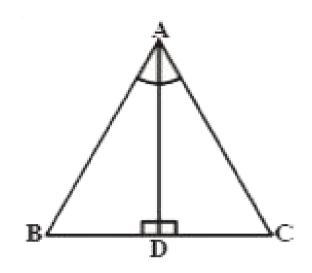




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**7.** In  $\Delta ABC$ , the bisector AD of A is perpendicular to side BC Show that AB = AC

and  $\Delta ABC$  is isosceles.

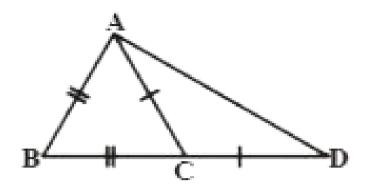




8. In the adjacent figure,

 $AB = BC \ \mathrm{and} \ AC = CD$ . Prove that :

 $\angle BAD$ :  $\angle ADB = 3:1$ .

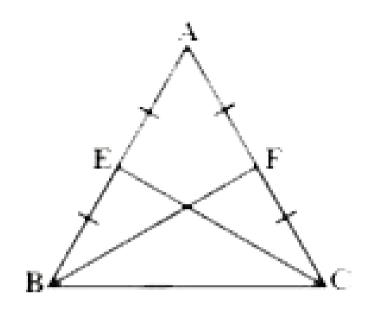




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**9.** E and F are respectively the mid-points of equal sides AB and AC of  $\Delta ABC$  (see figure)

Show that BF = CE.





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**10.** In an isosceles triangle ABC with AB = AC, D and E are points on BC such that BE = CD (see

figure) Show that AD = AE



that

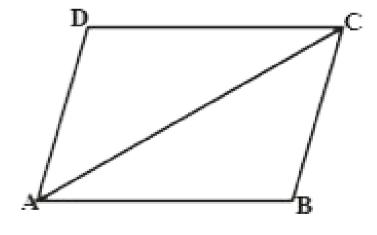
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**11.** In quadrilateral ABCD, AB = CD, BC=AD show

 $\Delta ABC\cong \Delta CDA$ 

Consider

 $\Delta ABC$  and  $\Delta CDA$ 





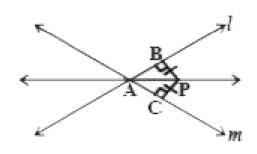
**12.** AB is a line - segment. P and Q are points on either side of AB such that each of them is equidistant from the points A and B (See Fig ). Show that the line PQ is the perpendicular bisector of AB.



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**13.** P is a point equidistant from two lines I and m intersecting at point A (see figure). Show

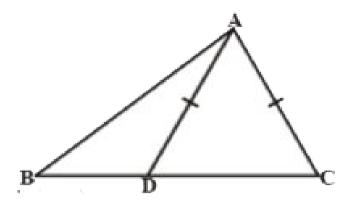
that the line AP bisects the angle between them.





**14.** D is a point on side BC  $\triangle$ ABC such that AD =

AC (see figure). Show that AB > AD.





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Do This

1. There are some statements given below.

Write whether they are true or false:

Two circle are always congruent.



2. There are some statements given below.

Write whether they are true or false:

Two right angle triangles are sometimes congruent.



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**3.** Find the component statements of the following compound statements and check

whether they are true or false.

Number 3 is prime or it is odd.



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4. There are some statements given below.

Write whether they are true or false:

Two equilateral triangles with their sides equal are always congruent.



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**5.** Which minimum measurements do you require to check if the given figures are congruent:

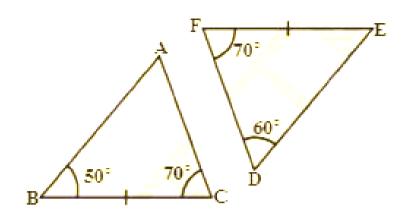
i. Two rectangles ii. Two rhombuses.



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**6.** State whether the following triangles are congruent or not? Give reasons for your

answer.

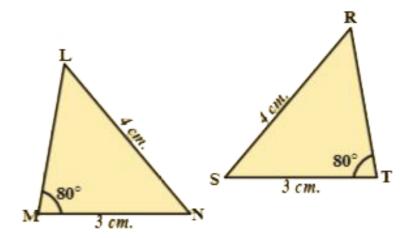




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**7.** State whether the following triangles are congruent or not? Give reasons for your

answer.





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**8.** In the given figure, the point P bisects AB and DC. Prove that

$$\Delta APC \cong \Delta BPD$$

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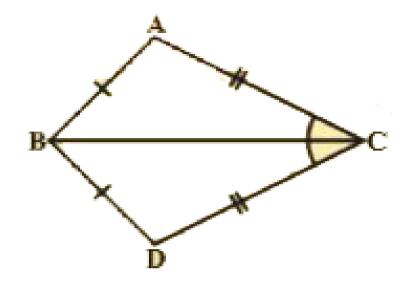
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**9.** In the adjacent figure  $\Delta ABC$  and  $\Delta DBC$ are two triangles such that  $\overline{AB}=\overline{BD}$  and

 $\overline{AC}=\overline{CD}$  . Show that  $\Delta ABC\cong\Delta DBC$  .





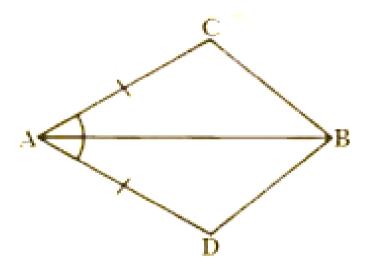
Exercise 7 1

**1.** In quadrilateral

ACBD, AC = AD and AB bisects  $\angle A$ 

Show that  $\Delta ABC\cong\Delta ABD$ .

What can you say about BC and BD?





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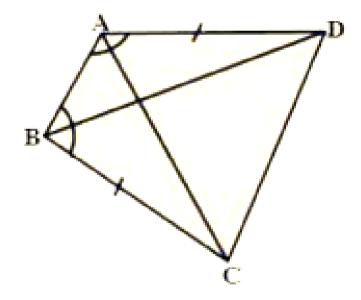
#### 2. ABCD is a quadrilateral in which AD = BC and

$$\angle DAB = \angle CBA$$
 Prove that

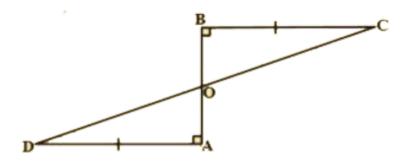
$$(i)\Delta ABD\cong\Delta BAC$$

(ii) 
$$BD = AC$$

(iii)
$$\angle ABD = \angle BAC$$



**3.** AD and BC are equal and perpendiculars to a line segment AB. Show that CD bisects AB.

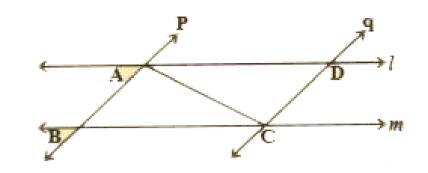




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**4.** I and m are two parallel lines intersected by another pair of parallel lines p and q . Show

that  $\Delta ABC\cong \Delta CDA$ .

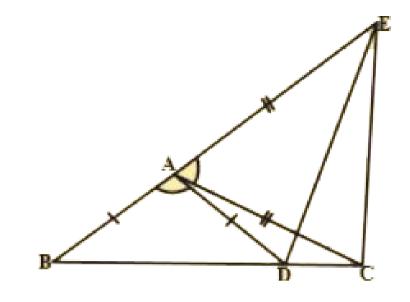




**5.** 

**5.** In the adjacent figure, 
$$AC = AE, AB = AD \text{ and } \angle BAD = \angle EAC$$

. Show that BC = DE.





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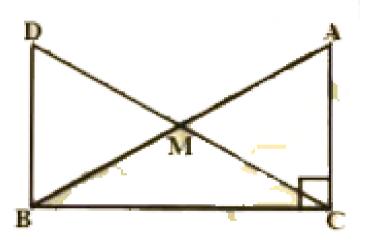
6. In right triangle ABC, right angle is at C, M is the mid-point of hypotenuse AB. C is joined toM and produced to a point D such that DM =CM. Point D is joined to point B (see figure).

Show that:

$$(i)\Delta AMC\cong\Delta BMD$$

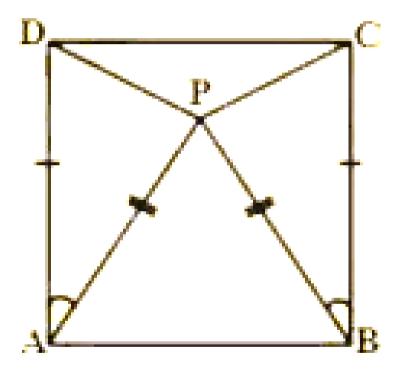
 $(ii) \angle DBC$  is a right angle

$$(iii)\Delta DBC\cong \Delta ACB$$
 (iv) $CM=rac{1}{2}AB.$ 



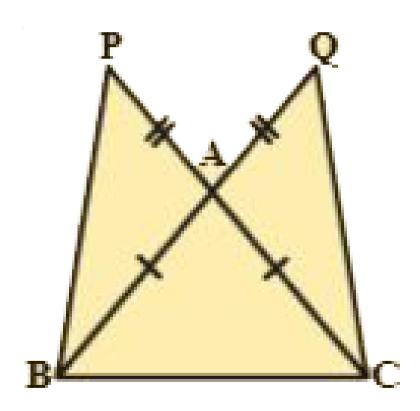


**7.** In the adjacent figure ABCD is a square and  $\Delta APB$  is an equilateral triangle. Prove that  $\Delta APD\cong\Delta BPC.$ 

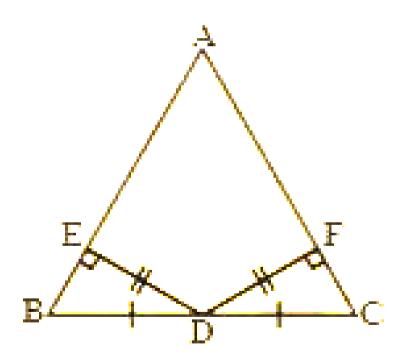




**8.** In the adjacent figure  $\Delta ABC$  is isosceles as  $\overline{AB}=\overline{AC}, \overline{BA} \text{ and } \overline{CA}$  are produced to Q and P such that  $\overline{AQ}=\overline{AP}.$  . Show that  $\overline{PB}=\overline{QC}.$ 



**9.** In the adjacent figure  $\Delta ABC,D$  is the midpoint of BC.  $DE\perp AB,DF\perp AC$  and DE=DF. Show that  $\Delta BED\cong \Delta CFD.$ 





**10.** If the bisector of an angle of a triangle also bisects the opposite side, prove that the triangle is isosceles.

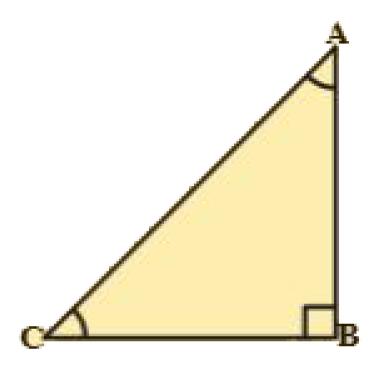


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**11.** In the given figure ABC is a right triangle and right angled at B such that

$$\angle BCA = 2\angle BAC$$
.

Show that hypotenuse AC = 2BC.



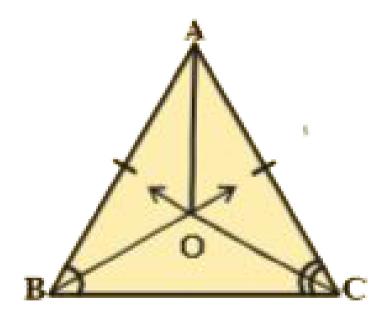


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Exercise 7 2

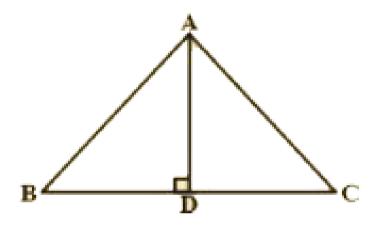
**1.** In an isosceles triangle ABC, with AB = AC, the bisectors of  $\angle B$  and  $\angle C$  intersect each other at O. Join A to O. Show that :

(i) OB = OC (ii) AO bisects 
$$\angle A$$





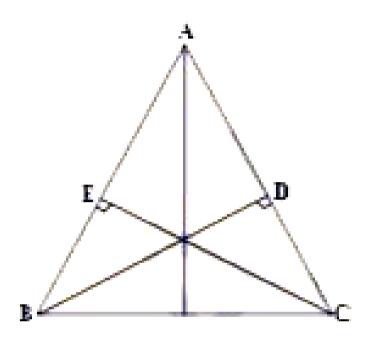
**2.** In  $\Delta ABC$ , AD is the perpendicular bisector of BC (See adjacent figure). Show that  $\Delta ABC$  is an isosceles triangle in which AB = AC.





**3.** ABC is an isosceles triangle in which altitudes BD and CE are drawn to equal sides

AC and AB respectively (see figure) Show that these altitudes are equal.

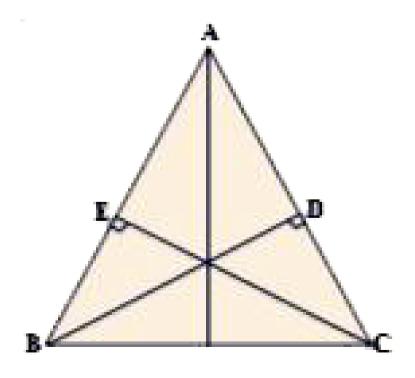




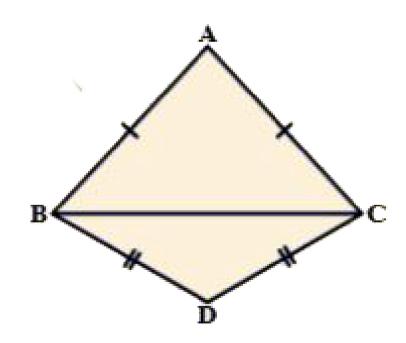
**4.** ABC is a triangle in which altitudes BD and CE to sides AC and AB are equal (see figure) . Show that

$$(i)\Delta ABD\cong\Delta ACE$$

(ii)AB=AC i.e., ABC is an isosceles triangle.



**5.**  $\Delta ABC$  and  $\Delta DBC$  are two isosceles triangles on the same base BC (see figure). Show that  $\angle ABD = \angle ACD$ .



# Exercise 7 3

**1.** AD is an altitude of an isosceles triangle ABC in which AB = AC. Show that, (i) AD bisects BC (ii) AD bisects  $\angle A$ .



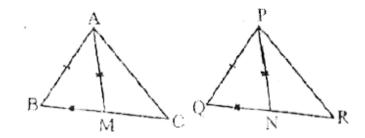
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**2.** Two sides AB and BC and median AM of one triangle ABC are respectively equal to sides PQ

and QR and median PN of  $\Delta$  PQR. Show that

$$\Delta ABM\cong \Delta PQN$$

(ii)  $\Delta ABC\cong\Delta PQR$ 





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**3.** BE and CF are two equal altitudes of a triangle ABC. Using RHS congruence rule, prove that the triangle ABC is isosceles.

**4.**  $\triangle ABC$  is an isosceles triangle in which AB =

AC. Show that  $\angle B = \angle C$ .

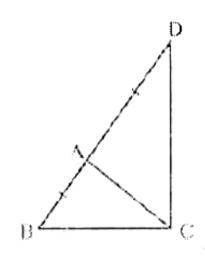


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**5.**  $\Delta ABC$  is an isosceles triangle in which AB =

AC. Side BA is produced to D such that AD = AB.

Show that BCD is a right angle.





6. ABC is a right angled triangle in which

$$ngle A=90^\circ$$
 and  $AB=AC$ . Show that

$$\angle B = \angle C$$
.



**7.** Show that the angles of an equilateral triangle are  $60^{\circ}$  each.



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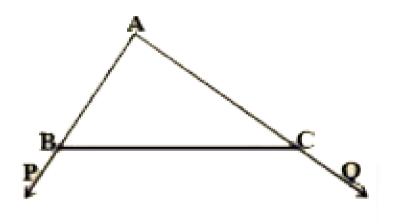
Exercise 7 4

**1.** Show that in a right angled triangle, the hypotenuse is the longest side.



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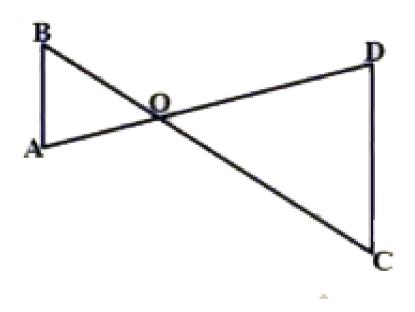
**2.** In adjacent figure, sides AB and AC of  $\triangle ABC$  are extended to points P and Q respectively. Also,  $\angle PBC < \angle QCB$ . Show that AC > AB.





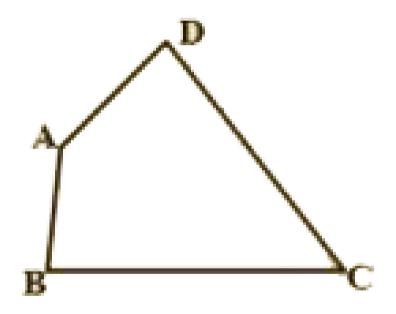
3. In adjacent figure,

 $\angle B < \angle A$  and  $\angle C < \angle D$  Show that AD < BC.

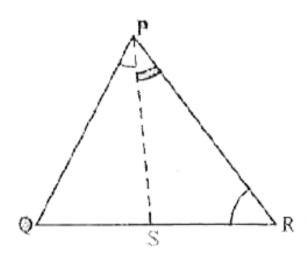




**4.** AB and CD are respectively the smallest and longest sides of aquadrilateral ABCD (see adjacent figure). Show that  $\angle A > \angle C$  and  $\angle B > \angle D$ .



**5.** In Pr  $\,>\,$  PQ and PS bisects  $\angle QPR$ . Prove that  $\angle PSR > \angle PSQ$ 





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**6.** If two sides of a triangle measure 4 cm and 6 cm find all possible measurements (positive Integers) of the third side. How many distinct triangles can be obtained?



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**7.** Try to construct a triangle with 5 cm, 8 cm and 1 cm. Is it possible or not? Why? Give your justification?



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