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## MATHS

## NCERT - NCERT MATHS (KANNADA

## ENGLISH)

## TRIANGLES

Examples

1. In the given Figure $A B$ and $C D$ are
intersecting at ' $O$ ', $O A=O B$ and $O D=O C$. Show
that $\quad$ (i) $\quad \triangle A O D \cong \triangle B O C \quad$ and
$A D|\mid B C$.

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2. $A B$ is a line segment and line $I$ is its perpendicular bisector. If a point $P$ lies on $I$, show that $P$ is equidistant from $A$ and $B$.

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3. In the given figure, $A B \| D C$ and $A D \| B C$ show that $\triangle A B C \cong \triangle C D A$.


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4. In the given figure, $A L \| D C, E$ is mid point of BC . Show that $\triangle E B L \cong \triangle E C D$.


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5. Use the information given in the adjoining
figure, to prove :
(i) $\Delta D B C \cong \triangle E A C$
(ii) $D C=E C$.


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6. Line-segment $A B$ is parallel to another linesegment CD. O is the mid-point of AD.

Show that (i) $\triangle A O B \cong \triangle D O C$ (ii) O is also
the mid-point of $B C$.


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7. In $\triangle A B C$, the bisector AD of A is perpendicular to side $B C$ Show that $A B=A C$
and $\Delta A B C$ is isosceles.


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8. 

In
the
adjacent
figure,
$A B=B C$ and $A C=C D$. Prove that
$\angle B A D: \angle A D B=3: 1$.


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9. $E$ and $F$ are respectively the mid-points of equal sides AB and AC of $\triangle A B C$ (see figure)

Show that $B F=C E$.


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10. In an isosceles triangle $A B C$ with $A B=A C, D$ and $E$ are points on $B C$ such that $B E=C D$ (see
figure) Show that AD $=A E$

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11. In quadrilateral $A B C D, A B=C D, B C=A D$ show that $\Delta A B C \cong \triangle C D A$

Consider
$\triangle A B C$ and $\triangle C D A$

12. $A B$ is a line - segment. $P$ and $Q$ are points on either side of $A B$ such that each of them is equidistant from the points $A$ and $B$ (See Fig ).

Show that the line $P Q$ is the perpendicular bisector of $A B$.

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13. $P$ is a point equidistant from two lines I and
m intersecting at point A (see figure). Show
that the line AP bisects the angle between
them.

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14. $D$ is a point on side $B C \triangle A B C$ such that $A D=$
$A C$ (see figure). Show that $A B>A D$.


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## Do This

1. There are some statements given below.

Write whether they are true or false :

Two circle are always congruent.

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2. There are some statements given below. Write whether they are true or false :

Two right angle triangles are sometimes congruent.

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3. Find the component statements of the following compound statements and check
whether they are true or false.

Number 3 is prime or it is odd.

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4. There are some statements given below.

Write whether they are true or false :

Two equilateral triangles with their sides equal are always congruent.
5. Which minimum measurements do you
require to check if the given figures are congruent:
i. Two rectangles ii. Two rhombuses.

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6. State whether the following triangles are congruent or not? Give reasons for your
answer.


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7. State whether the following triangles are congruent or not? Give reasons for your
answer.


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8. In the given figure, the point $P$ bisects $A B$ and DC. Prove that
$\triangle A P C \cong \triangle B P D$
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9. In the adjacent figure $\triangle A B C$ and $\triangle D B C$ are two triangles such that $\overline{A B}=\overline{B D}$ and

## $\overline{A C}=\overline{C D}$. Show that $\triangle A B C \cong \triangle D B C$.



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Exercise 71
1.
In
quadrilateral
$A C B D, A C=A D$ and $A B$ bisects $\angle A$

Show that $\triangle A B C \cong \triangle A B D$.

What can you say about BC and BD?


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2. $A B C D$ is a quadrilateral in which $A D=B C$ and
$\angle D A B=\angle C B A$ Prove that
(i) $\triangle A B D \cong \triangle B A C$
(ii) $B D=A C$
(iii) $\angle A B D=\angle B A C$


## 3. $A D$ and $B C$ are equal and perpendiculars to $a$

 line segment $A B$. Show that $C D$ bisects $A B$.

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4. I and m are two parallel lines intersected by another pair of parallel lines $p$ and q. Show
that $\triangle A B C \cong \triangle C D A$.


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5. 

In
the
adjacent
figure,
$A C=A E, A B=A D$ and $\angle B A D=\angle E A C$
. Show that BC = DE.


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6. In right triangle $A B C$, right angle is at $C, M$ is
the mid-point of hypotenuse $A B . C$ is joined to
$M$ and produced to a point $D$ such that $D M=$
$C M$. Point $D$ is joined to point $B$ (see figure).

Show that :
$(i) \Delta A M C \cong \Delta B M D$
(ii) $\angle D B C$ is a right angle
$(i i i) \Delta D B C \cong \triangle A C B($ iv $) C M=\frac{1}{2} A B$.

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7. In the adjacent figure $A B C D$ is a square and
$\triangle A P B$ is an equilateral triangle. Prove that
$\triangle A P D \cong \triangle B P C$.


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8. In the adjacent figure $\Delta A B C$ is isosceles as
$\overline{A B}=\overline{A C}, \overline{B A}$ and $\overline{C A}$ are produced to Q and P such that $\overline{A Q}=\overline{A P}$. . Show that $\overline{P B}=\overline{Q C}$.


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9. In the adjacent figure $\triangle A B C, D$ is the midpoint of BC. $D E \perp A B, D F \perp A C$ and $D E=D F$. Show that $\triangle B E D \cong \Delta C F D$.


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10. If the bisector of an angle of a triangle also
bisects the opposite side, prove that the triangle is isosceles.

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11. In the given figure $A B C$ is a right triangle and right angled at $B$ such that
$\angle B C A=2 \angle B A C$.

Show that hypotenuse $A C=2 B C$.


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1. In an isosceles triangle $A B C$, with $A B=A C$,
the bisectors of $\angle B$ and $\angle C$ intersect each other at O. Join A to O. Show that :
(i) $\mathrm{OB}=\mathrm{OC}$ (ii) AO bisects $\angle A$


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2. In $\triangle A B C$, AD is the perpendicular bisector of BC (See adjacent figure). Show that $\triangle A B C$ is an isosceles triangle in which $A B=A C$.


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3. $A B C$ is an isosceles triangle in which altitudes $B D$ and CE are drawn to equal sides
$A C$ and $A B$ respectively (see figure) Show that these altitudes are equal.

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4. $A B C$ is a triangle in which altitudes $B D$ and
$C E$ to sides $A C$ and $A B$ are equal (see figure).

Show that
(i) $\triangle A B D \cong \triangle A C E$
(ii) $A B=A C$ i.e., ABC is an isosceles triangle.

5. $\triangle A B C$ and $\triangle D B C$ are two isosceles triangles on thesame base $B C$ (see figure).

Show that $\angle A B D=\angle A C D$.


## Exercise 73

1. $A D$ is an altitude of an isosceles triangle $A B C$
in which $A B=A C$. Show that, (i) $A D$ bisects $B C$
(ii) AD bisects $\angle A$.

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2. Two sides $A B$ and $B C$ and median $A M$ of one
triangle $A B C$ are respectively equal to sides $P Q$
and QR and median PN of $\Delta \mathrm{PQR}$. Show that $\Delta A B M \cong \triangle P Q N$
(ii) $\triangle A B C \cong \triangle P Q R$


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3. $B E$ and CF are two equal altitudes of a triangle $A B C$. Using RHS congruence rule, prove that the triangle $A B C$ is isosceles.
4. $\triangle A B C$ is an isosceles triangle in which $\mathrm{AB}=$ AC . Show that $\angle B=\angle C$.

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5. $\triangle A B C$ is an isosceles triangle in which $\mathrm{AB}=$
$A C$. Side $B A$ is produced to $D$ such that $A D=A B$.

Show that BCD is a right angle.


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6. $A B C$ is a right angled triangle in which
$\angle A=90^{\circ}$ and $A B=A C$. Show that
$\angle B=\angle C$.

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7. Show that the angles of an equilateral triangle are $60^{\circ}$ each.

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Exercise 74

1. Show that in a right angled triangle, the
hypotenuse is the longest side.

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2. In adjacent figure, sides $A B$ and $A C$ of
$\triangle A B C$ are extended to points P and Q respectively. Also, $\angle P B C<\angle Q C B$. Show that $A C>A B$.

3. In adjacent figure,
$\angle B<\angle A$ and $\angle C<\angle D$ Show that $\mathrm{AD}<$ BC.


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4. $A B$ and $C D$ are respectively the smallest and
longest sides of aquadrilateral ABCD (see adjacent figure).

Show
that
$\angle A>\angle C$ and $\angle B>\angle D$.

5. In $\operatorname{Pr}>\mathrm{PQ}$ and PS bisects $\angle Q P R$. Prove
that $\angle P S R>\angle P S Q$


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6. If two sides of a triangle measure 4 cm and

6 cm find all possible measurements (positive Integers) of the third side. How many distinct triangles can be obtained?

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7. Try to construct a triangle with $5 \mathrm{~cm}, 8 \mathrm{~cm}$
and 1 cm . Is it possible or not ? Why ? Give your justification?
