# ©゙doubtnut 

India's Number 1 Education App

## MATHS

## BOOKS - ML KHANNA

## PROBABILITY

## Problem Set 1 Multiple Choice Questions

1. The probability of getting head in both trials, when a balanced coin is tossed twice, will be
A. $\frac{1}{4}$
B. $\frac{1}{2}$
C. 1
D. $\frac{3}{4}$
2. Two cards are drawn at random from a pack of 52 cards. The probability of these two being aces is
A. $\frac{1}{26}$
B. $\frac{1}{221}$
C. $\frac{1}{2}$
D. none

## Answer: B

## - Watch Video Solution

3. From a well shuffled pack of playing cards, two cards are drawn one by one with replacement. The probability that both are aces is
A. $\frac{2}{13}$
B. $\frac{1}{51}$
C. $\frac{1}{221}$
D. none

## Answer: D

## - Watch Video Solution

4. A card is drawn from a pack of 52 cards. Find the probability of getting:
(ii) a king or a diamond
A. $\frac{4}{52}$
B. $\frac{4}{13}$
C. $\frac{1}{52}$
D. $\frac{2}{13}$

## Answer: B

5. A card is drawn at random from apack of cards. The prob. Of this card being a red or queen is
A. $1 / 3$
B. $1 / 26$
C. $1 / 2$
D. $7 / 13$

## Answer: D

## - Watch Video Solution

6. A card is drawn from a well-shuffled pck of cards. The probability of getting a queen of club or a king of heart is
A. $1 / 52$
B. $1 / 26$
C. $1 / 13$
D. none

## Answer: B

## - Watch Video Solution

7. A single letter is selected at random from the word "PROBABILITY" . The probability that it is a vowel is
A. $\frac{3}{11}$
B. $\frac{4}{11}$
C. $\frac{2}{11}$
D. 0

## Answer: B

8. 3 mangoes and 3 apples are in a box. If 2 fruits are chosen at random, the probability that one is a mango and the other is an apple, is
A. $2 / 3$
B. $3 / 5$
C. $1 / 3$
D. none

## Answer: B

## - Watch Video Solution

9. A bag contains 5 brown and 4 white socks. A man pulls out two socks. The probability that these are of the same colour is $\frac{5}{108}$ b. $\frac{18}{108}$ c. $\frac{31}{108}$ d. $\frac{48}{108}$
A. $\frac{5}{108}$
B. $\frac{1}{6}$
C. $\frac{5}{18}$
D. $\frac{4}{9}$

## Answer: D

## - Watch Video Solution

10. A card is drawn at random from a pack of 100 cards numbered 1 to 100. The probability of drawing a number which is a square, is
A. $1 / 5$
B. $2 / 5$
C. $1 / 10$
D. none

## Answer: C

11. Two dice are thrown. The probability that the sum of the points on two dice will be 7 is
A. $\frac{5}{36}$
B. $\frac{6}{36}$
C. $\frac{7}{36}$
D. $\frac{8}{36}$

## Answer: B

## - Watch Video Solution

12. In a throw of a dice the probability of getting one is even number of throws is
A. $\frac{5}{36}$
B. $\frac{5}{11}$
C. $\frac{6}{11}$
D. $\frac{1}{6}$

## Answer: B

## - Watch Video Solution

13. Two dice are thrown simultaneosly. The probability of obtaining a total score of 5 is
A. $\frac{1}{18}$
B. $\frac{1}{12}$
C. $\frac{1}{9}$
D. none

## Answer: C

## - Watch Video Solution

14. Three letters are written to different persons and addressess to three envelopes are also written. Without looking at the addresses, the probability that probability that the letters go into right envelopes, is
A. $\frac{1}{27}$
B. $\frac{1}{6}$
C. $\frac{1}{9}$
D. none

## Answer: B

## - Watch Video Solution

15. There are 4 envelopes corresponding to 4 letters. If the letters are placed in the envelopes at random, probability that all the letters are not placed in the right envelopes is
B. 1
C. $23 / 24$
D. $9 / 2$

## Answer: C

## - Watch Video Solution

16. Three identical dice are rolled. The probability that same number appears on them, is
A. $1 / 6$
B. $1 / 18$
C. $1 / 36$
D. none

## Answer: C

17. One die and one coin are tossed simultaneously. The probability of getting 6 on die and head on coin is
A. $\frac{1}{2}$
B. $\frac{1}{6}$
C. $\frac{1}{12}$
D. none

## Answer: C

## - Watch Video Solution

18. A coin is tossed and a die is rolled. The chance that the coin shows a head and the die shows 3 is
A. $1 / 8$
B. $1 / 12$
C. $1 / 2$
D. 1

## Answer: B

## - Watch Video Solution

19. From a pack of cards two are drawn the first being replaced before the second is drawn Find the probability that the first is a diamond and the second is a king .
A. $13 / 4$
B. $4 / 13$
C. $1 / 52$
D. 52

## Answer: C

20. Seven chits are numbered 1 to 7 . three are drawn one by one with replacements. The probability that the least number on any selected chit is 5 , is
A. $1-(2 / 7)^{4}$
B. 4. $(2 / 7)^{4}$
C. $(3 / 7)^{3}$
D. none

## Answer: C

## - Watch Video Solution

21. Two cards are drawn successively with replacement from a wellshuffled pack of 52 cards. The probability of drawing two aces is

$$
\text { A. } \frac{1}{13} \times \frac{1}{13}
$$

B. $\frac{1}{13} \times \frac{1}{17}$
C. $\frac{1}{52} \times \frac{1}{51}$
D. $\frac{1}{13} \times \frac{4}{51}$

## Answer: A

## - Watch Video Solution

22. Fifteen coupons are numbered $1,2,3, \ldots, 15$ respectively. Seven coupons are selected random one at a time with replacement. The probability that the largest number appearing on the selected coupons is atmost 9 , is :
A. $(1 / 16)^{6}$
B. $(8 / 15)^{7}$
C. $(3 / 5)^{7}$
D. none

## Answer: C

23. There are 20 cards, 10 of these cards have the letter 'I' printed on them and the other 10 have the letter ' $T$ ' printed on them. If three cards are picked up at random and kept in the same order, the probability of making word IIT is
A. $\frac{9}{80}$
B. $\frac{1}{8}$
C. $\frac{4}{27}$
D. $\frac{5}{38}$

## Answer: D

## - Watch Video Solution

24. A' draws two cards with replacement from a pack of 52 cards and ' B ' throws a pair of dice what is the chance that 'A' gets both cards of same
suit and 'B' gets total of 6
A. $1 / 144$
B. $1 / 4$
C. 5/144
D. $7 / 144$

## Answer: C

## - Watch Video Solution

25. In a box containing 100 bulbs, 10 are defective. What is the probability that out of a sample of 5 bulbs, (i) none is defective and (ii) exactly 2 are defective?
A. $10^{-5}$
B. $\left(\frac{1}{2}\right)^{5}$
C. $(9 / 10)^{5}$

## Answer: C

## - Watch Video Solution

26. An unbiased die with faced marked $1,2,3,4,5$, and 6 is rolled four times. Out of four face value obtained, the probability that the minimum face value is not less than 2 and the maximum face value is not greater than five is then $16 / 81$ b. $1 / 81$ c. $80 / 81$ d. $65 / 81$
A. $16 / 81$
B. $1 / 81$
C. $80 / 81$
D. $65 / 81$

## Answer: A

27. A student appears for tests I, II and III. The student is successful if the passes either in tests I and II or tests I and III. The probabilities of the student passing in tests I, II and III are $\mathrm{p}, \mathrm{q}$ and $\frac{1}{2}$, respectively. If the probability that the student is successful, is $\frac{1}{2}$, then
A. $p=q=1$
B. $p=q=\frac{1}{2}$
C. $p=1, q=0$
D. $\mathrm{p}=1, \mathrm{q}=\frac{1}{2}$

## Answer: C

## - Watch Video Solution

28. Two dice are thrown simultaneously, the probability of obtaining total score of 7 is $1 / 6$ b. $7 / 36$ c. $4 / 9$ d. $11 / 36$
A. $\frac{1}{6}$
B. $\frac{7}{36}$
C. $\frac{1}{4}$
D. none

## Answer: A

## - Watch Video Solution

29. It is given that the events $A$ and $B$ are such that $P(A)=\frac{1}{4}, P\left(\frac{A}{B}\right)=\frac{1}{2}$ and $P\left(\frac{B}{A}\right)=\frac{2}{3}$. Then $P(B)$ is
A. $\frac{1}{6}$
B. $\frac{1}{3}$
C. $\frac{2}{3}$
D. $\frac{1}{2}$

## Answer: B

30. $A$ die is thrown. Let $A$ be the event that the number obtained is greater than 3. Let B be the event that the number obtained is less than
31. Then $P(A \cup B)$ is (1) $\frac{3}{5}$ (2) 0 (3) 1 (4) $\frac{2}{5}$
A. $\frac{3}{5}$
B. 0
C. 1
D. $\frac{2}{5}$

## Answer: C

## D Watch Video Solution

31. Of cigarette smoking population $70 \%$ are men and $30 \%$ are women, $10 \%$ of these men and $20 \%$ of these women smoke wills. Probability that a person seen smoking a Wills to be a man is
A. $1 / 5$
B. $7 / 13$
C. $5 / 13$
D. $7 / 10$

## Answer: B

## - Watch Video Solution

32. Two numbers are chosen at random from $\{1,2,3,4,5,6\}$ at a time. The probability that the smaller of the two is less than 4 , is
A. $4 / 5$
B. $1 / 15$
C. $1 / 5$
D. $14 / 15$
33. The chance of throwing an ace first only of two successive throws with an ordinary die is
A. $\frac{1}{36}$
B. $\frac{5}{36}$
C. $\frac{25}{36}$
D. $\frac{1}{6}$

## Answer: B

## - Watch Video Solution

34. Words from the letters of the work PROBABILITY are formed by taking al at a time. The probability that both B's are together and both l's are together is
A. $\frac{1}{55}$
B. $\frac{2}{55}$
C. $\frac{4}{165}$
D. none

## Answer: B

## - Watch Video Solution

35. One of the two events must occur. If the chance of one is $2 / 3$ of the other, then odds in favour of the other are a. 1:3 b. 3:1 c. 2:3 d. 3:2
A. $1: 3$
B. 3: 1
C. 2: 3
D. none
36. A number is chosen at random among the first 120 natural numbers. The probability of the number chosen being a multiple of 5 or 15 is
A. $\frac{1}{5}$
B. $\frac{1}{8}$
C. $\frac{1}{6}$
D. none

## Answer: A

## - Watch Video Solution

37. If 3 distinct numbers are chosen randomly from $\{1,2, \ldots 100\}$, then probability that all are divisible by both 2 and 3 is

$$
\text { A. } 4 / 25
$$

B. $4 / 35$
C. $4 / 33$
D. $4 / 1155$

## Answer: D

## - Watch Video Solution

38. There are 3 works. One is of 3 volumes, one is of 4 volumes and one is of only one and they are placed a random in at shelf. What is the chance that volume of the same work is placed together
A. $1 / 40$
B. $3 / 140$
C. $9 / 70$
D. none

## Answer: B

39. From a pack of 52 cards, the cards are drawn till an ace appears .

Probability that an ace does not come in first 26 cards is,
A. $46 / 153$
B. $23 / 27$
C. 109 / 153
D. none

## Answer: D

## - Watch Video Solution

40. The probability of India winning a test match against West Indies is
$1 / 2$. Assuming independence from match to match, find the probability that in a match series Indias second win occurs at the third test.
A. $1 / 8$
B. $1 / 4$
C. $1 / 2$
D. $2 / 3$

## Answer: B

## - Watch Video Solution

41. If 10 biscuits be distributed at random among 20 beggars, what is the chance that a particular beggar receives 3 biscuits ?

## - Watch Video Solution

42. A six-faced dice is so biased that it is twice as likely to show an even number as an odd number when thrown. It is thrown twice, the probability that the sum of two numbers thrown is even is $1 / 12 \mathrm{~b} .1 / 6 \mathrm{c}$. $1 / 3$ d. $5 / 9$
43. Three of the six vertices of a regular hexagon are chosen at random. The probability that the triangle with these three vertices is equilateral equals :
A. $1 / 2$
B. $1 / 5$
C. $1 / 10$
D. $1 / 20$

## Answer: C

## - Watch Video Solution

44. Three tangents are drawn at random to a given circle. Show that the odds are 3:1 against the circle being inscribed in the triangle formed by the tangents.
45. In shuffling a pack of cards three are accidentally dropped. The probability that the missing cards are of distinct colours is
A. $169 / 425$
B. $261 / 425$
C. $104 / 425$
D. none

## Answer: A

## - Watch Video Solution

46. A person draws . two cards with replacement from a pack of 52 cards .

What is the chance that he gets both cards of the same suit?
A. $1 / 4$
B. $3 / 13$
C. $1 / 16$
D. none

## Answer: A

## - Watch Video Solution

47. Find the probability that a leap year selected at random will contain 53 sundays.
A. $7 / 366$
B. $26 / 183$
C. $1 / 7$
D. $2 / 7$

## Answer: D

48. Find the probability of getting more than 7 when two dice are rolled.
A. $7 / 36$
B. $7 / 12$
C. $5 / 12$
D. none

## Answer: C

## Watch Video Solution

49. The probability that in the toss of two dice we obtain an even sum or a sum less than 5 is
A. $\frac{1}{2}$
B. $\frac{1}{6}$
C. $\frac{2}{3}$
D. $\frac{5}{9}$

## Answer: D

## - Watch Video Solution

50. In throwing of two dice, the probability of getting a multiple of 4 is
A. $\frac{1}{9}$
B. $\frac{1}{3}$
C. $\frac{1}{4}$
D. none

## Answer: C

## - Watch Video Solution

51. An arbitrary cube has four blank faces, one face marked 2 and another marked 3. Then the probability of obtaining a total of exactly 12 in 5 throws is
A. $\frac{5}{1296}$
B. $\frac{5}{1944}$
C. $\frac{5}{2592}$
D. none

## Answer: C

## - Watch Video Solution

52. From 4 children, 2 women and 4 men, 4 are selected. Probability that there are exactly 2 children among the selected is
A. $11 / 21$
B. $9 / 21$
C. $10 / 21$
D. none

## Answer: B

## - Watch Video Solution

53. What is the chance of getting multiple of 2 on one and multiple of 3 one the other in a single throw of two dice
A. $1 / 3$
B. $7 / 36$
C. $11 / 36$
D. none

## Answer: C

54. A five digit number if formed by the digits $1,2,3,4,5,6$ and 8 . The probability that the number has even digit at both ends is
A. $2 / 7$
B. $3 / 7$
C. $4 / 7$
D. none

## Answer: A

## - Watch Video Solution

55. A pack of cards contains 4 aces, 4 kings, 4 queens and 4 jacks. Two cards are drawn $t$ random. the probability that at least one of them is an ace is a. $1 / 5$ b. $3 / 16$ c. $9 / 20$ d. $1 / 9$
A. $\frac{1}{5}$
B. $\frac{3}{16}$
C. $\frac{9}{20}$
D. $\frac{1}{9}$

## Answer: C

## - Watch Video Solution

56. The probability that an event A happens in one trial of an experiment is 0.7 . Three independent rials of the experiment are performed. The probability that the event A happens at least once is
A. 657
B. 973
C. $\cdot 027$
D. $\cdot 343$

## Answer: B

57. If two dice are thrown find probability of getting an odd number one and multiple of 3 on other is
A. $1 / 3$
B. $1 / 4$
C. $11 / 36$
D. $\frac{13}{36}$

## Answer: C

## - Watch Video Solution

58. In solving any problem, odds against A are 4 to 3 and in favour of Bin solving the same is 7 to 5 . The probability that problem will be solved is
A. $5 / 21$
B. $16 / 21$
C. $15 / 84$
D. $69 / 84$

## Answer: B

## - Watch Video Solution

59. The probability that a person will hit a target in shooting practice is 0.3 . If he shoots 10 times, the probability that he hits the target is
A. 1
B. $1-(0 \cdot 7)^{10}$
C. $(0 \cdot 7)^{10}$
D. $(0 \cdot 3)^{10}$

## Answer: B

## - Watch Video Solution

60. The probability that a man aged 50 years will die in a year is $p$. The probability that out of n men $A_{1}, A_{2}, A_{3}, \ldots . ., A_{n}$ each aged 50 year, $A_{1}$ will die and first to die is
A. $1-(1-p)^{n}$
B. $\left[1-(1-p)^{n}\right] / n^{2}$
C. $\left[1-(1-p)^{n}\right] / n$
D. none

## Answer: C

## - Watch Video Solution

61. If the probability that $A$ and $B$ will die within a year are $p$ and $q$ respectively, then the probability that only one of them will be alive at the end of the year, is

$$
\text { A. } p+q
$$

B. $p+q-2 p q$
C. $p+q-p q$
D. $p+q+p q$

## Answer: B

## - Watch Video Solution

62. The probability that Krishna will be alive 10 years hence is $7 / 15$ and that Hari will be alive is $7 / 10$. What is t he probability that both Krishna and Hari will be dead 10 years hence?
A. $\frac{21}{150}$
B. $\frac{24}{150}$
C. $\frac{49}{150}$
D. $\frac{56}{150}$

Answer: B
63. Fifteen coupons are numbered $1,2,3, \ldots, 15$ respectively. Seven coupons are selected random one at a time with replacement. The probability that the largest number appearing on the selected coupons is atmost 9 , is :
A. $\left(\frac{9}{10}\right)^{6}$
B. $\left(\frac{8}{15}\right)^{7}$
C. $\left(\frac{3}{5}\right)^{7}$
D. none

## Answer: C

## - Watch Video Solution

64. Two numbers are chosen at random from $\{1,2,3,4,5,6\}$ at a time. The probability that the smaller of the two is less than 4 , is
A. $4 / 5$
B. $1 / 15$
C. $1 / 5$
D. $14 / 15$

## Answer: A

## - Watch Video Solution

65. The probability that a certain beginner at golf gets a good shot if he uses the correct club is $\frac{1}{3}$, and the probability of a good shot with an incorrect club is $\frac{1}{4}$. In his bag are 5 different clubs, only one of which is correct for the shot is question. if he chooses a club at random and takes a stroke, the probabilitiy that he gets a good shot is
A. $\frac{1}{3}$
B. $\frac{1}{12}$
C. $\frac{4}{15}$
D. $\frac{7}{12}$

## Answer: C

## - Watch Video Solution

66. Two bags contain 3 white, 2 black and 2 white, 4 black balls respectively. A ball is chosen at random then the probability of its being black is
A. $\frac{8}{15}$
B. $\frac{2}{3}$
C. $\frac{6}{4}$
D. none

## Answer: A

## - Watch Video Solution

67. A purse contains 4 copper coins, 3 silver coins, the second purse contains 6 copper coins and 2 silver coins. A coin is taken out of any purse, the probability that it is a copper coin is
A. $\frac{4}{7}$
B. $\frac{3}{4}$
C. $\frac{3}{7}$
D. $\frac{37}{56}$

## Answer: D

## - Watch Video Solution

68. A cricket club has 15 members, of them of whom only 5 can bowl. If the names of 15 members are put into a box and 11 are drawn at random, then the probability of getting an eleven containing at least 3 bowlers is $7 / 13$ b. $6 / 13$ c. $11 / 158$ d. $12 / 13$
A. $\frac{7}{13}$
B. $\frac{11}{15}$
C. $\frac{12}{13}$
D. none

## Answer: C

## - Watch Video Solution

69. On a toss of two dice, A throws a total of 5, then the probability that he will throw another 5 before the throws 7 , is
A. $\frac{1}{9}$
B. $\frac{1}{6}$
C. $\frac{2}{5}$
D. $\frac{5}{36}$

## Answer: C

70. $A, B, C$ in order toss a coin. A start $s$ to toss the first one to throw a head wins. Assuming the game continues indefinite their respective chances of winning the game are
A. $\frac{4}{7}, \frac{2}{7}, \frac{1}{7}$
B. $\frac{1}{7}, \frac{4}{7}, \frac{2}{7}$
C. $\frac{2}{7}, \frac{4}{7}, \frac{1}{7}$
D. none

## Answer: A

## Watch Video Solution

71. Find the mean number of heads in three tosses of a fair coin.
A. $\frac{3}{2}$
B. $\frac{5}{2}$
C. $\frac{1}{2}$
D. $\frac{1}{8}$

## Answer: A

## - Watch Video Solution

72. Two persons each make a single throw with a die. The probability they get equal value is $P_{1}$. Four persons each make a single throw and probability of three being equal is $P_{2}$. Then
A. $P_{1}=P_{2}$
B. $P_{1}<P_{2}$
C. $P_{1}>P_{2}$
D. none

## Answer: C

73. A bag has 13 red, 14 green and 15 black balls, The probability of getting exactly 2 black on pulling out 4 balls is $P_{1}$. Now the number of each colour ball is doubled and 8 balls are pulled out. The probability of getting exactly 4 blacks is $P_{2}$ then.
A. $P_{1}=P_{2}$
B. $P_{1}>P_{2}$
C. $P_{1}<P_{2}$
D. none

## Answer: B

## - Watch Video Solution

74. Ina certain town, $40 \%$ of the people have brown hair, $25 \%$ have brown eyes, and $15 \%$ have both brown hair and brown eyes. If a person selected
at random from the town has brown hair, the probability that he also has brown eyes is $1 / 5$ b. $3 / 8 \mathrm{c} .1 / 3 \mathrm{~d} .2 / 3$
A. $1 / 5$
B. $3 / 8$
C. $1 / 3$
D. $2 / 3$

## Answer: B

## - Watch Video Solution

75. Two persons, $A$ and $B$, have respectively $n+1$ and $n$ coins, which they toss simultaneously. Then the probability that A will have more heads that $B$ is
A. $\frac{1}{2}$
B. $>\frac{1}{2}$
C. $<\frac{1}{2}$
D. none

## Answer: A

## - Watch Video Solution

76. If the letters of the word REGULATION be arranged at random, the probability that there will be exactly four letters between $R$ and $E$ is
A. $1 / 5$
B. $1 / 2$
C. $1 / 9$
D. $1 / 10$

## Answer: C

## - Watch Video Solution

77. A biased die is tossed and the respective probabilities for various faces to turn up are

| Face | $:$ | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Probability | $:$ | 0.1 | 0.24 | 0.19 | 0.18 | 0.15 | 0.14 |

If an even face has turned up, then the probability that it is face 2 or face 4, is
A. $0 \cdot 25$
B. $0 \cdot 42$
C. $0 \cdot 75$
D. $0 \cdot 9$

## Answer: C

## - Watch Video Solution

78. In a purse there are 9 five paisa coins and one rupee coin. In another purse there are all 10 five paisa coins. 9 coins are taken from the former and put into the second and then 9 coins are taken from the latter and
put into the first. What is the chance that rupee coin is still in the first purse
A. $1 / 9$
B. $10 / 19$
C. $5 / 19$
D. none

## Answer: B

## - Watch Video Solution

79. $A$ and $B$ throw alternately with a pair of dice. $A$ wins if he throws 6 before $B$ throws 7 , and $B$ if he throws 7 before $A$ throws 6 . If $A$ begins, find his chance of winning.
80. Ten pairs of shoes are in a closet. Four shoes are selected at random. Find the probability that there is at least one pair among the four selected.

## - Watch Video Solution

81. A person throws two dice, on the common cube, and the other regular tetrahedron, the number in the lowest face being taken in the case of a tetrahedron. What is the chance that the sum of the numbers thrown is not less than 5 ?

## - Watch Video Solution

82. Out of 21 tickets consecutively numbered, three are drawn at random.

Find the chance that the numbers on them are in A.P.

## - Watch Video Solution

83. Cards are dealt one by one from a well shuffled pack until an ace appears. Find the chance that exactly n cards are dealt before the first ace.

## - Watch Video Solution

84. An urn contains 4 white and 5 black balls, a second urn contains 5 white and 4 black balls. One ball is transferred from the first to second urn, then a ball is drawn from the second urn, what is the probability that it is white ?

## - Watch Video Solution

85. In a group of equal number of men and women $10 \%$ men and $45 \%$ women are unemployed. What is the probability that a person selected at random is employed ?
86. A bag contains 3 black and 4 red balls. Two balls are drawn at random one at a time without replacement. What is the probability that the first ball selected is black, if the second ball is known to be red ?

## - Watch Video Solution

87. If $P(A)=0.3, P(B)=0.2$ and $P(C)=0.1$ and $A, B, C$ are independent events, find the probability of occurrence of at least one of the three events $A, B$ and C.

## - Watch Video Solution

88. Find the probability of getting at least one head in three throws of a coin.
A. $7 / 8$
B. $3 / 8$
C. $1 / 8$
D. none

## Answer: A

## - Watch Video Solution

89. The probability of solving a problem by three students $X, Y$ and $Z$ is $\frac{1}{2}, \frac{1}{3}$ and $\frac{1}{4}$ respectively. the probability that the problem will be solved is :
A. $1 / 4$
B. $1 / 2$
C. $3 / 4$
D. $1 / 3$

## Answer: C

## D Watch Video Solution

90. The probability of a problem being solved by two students are $1 / 2,1 / 3$. the proba-bility of the problem being solved is
A. $2 / 3$
B. $4 / 3$
C. $1 / 3$
D. 1

## Answer: A

## - Watch Video Solution

91. Find the probability of getting at least one tail in 4 tosses of a coin.
A. $15 / 16$
B. $1 / 16$
C. $1 / 4$
D. 1

## - Watch Video Solution

92. The probability that a marksman will hit a target is given as $\frac{1}{5}$. Then, the probabiltiy that atleast one hit in 10 shots is
A. $1-\left(\frac{4}{5}\right)^{10}$
B. $\frac{1}{5^{10}}$
C. $1-\frac{1}{5^{10}}$
D. none

## Answer: A

## - Watch Video Solution

93. The probability that a man can hit a target is $3 / 4$. He tries 5 times. The probability that he will hit the target at least three times is
A. $\frac{291}{364}$
B. $\frac{371}{464}$
C. $\frac{471}{502}$
D. $\frac{459}{512}$

## Answer: D

## - Watch Video Solution

94. A coin is tossed 3 times. The probability of obtaining at least two heads will be
A. $3 / 8$
B. $1 / 2$
C. 1
D. 2

## Answer: B

95.8 coins are tossed simultaneously. The probability of getting at least 6 heads is
A. $57 / 64$
B. $229 / 256$
C. $7 / 64$
D. $37 / 256$

## Answer: D

## - Watch Video Solution

96. From a group of 4 boys and 3 girls, candidates are arranged at random, one after the other, for an interview. The probability that the boys and girls alternate, is
A. $1 / 34$
B. $1 / 35$
C. $1 / 33$
D. $1 / 32$

## Answer: B

## - Watch Video Solution

97. Out of 13 applicants for a job, there are 5 women and 8 men It is desired to select 2 persons for the job. The probability that atleast one of the selected persons will be a woman is.
A. $\frac{25}{39}$
B. $\frac{14}{39}$
C. $\frac{5}{13}$
D. $\frac{10}{13}$

## D Watch Video Solution

98. The probability that an event $A$ happens in one trial of an experiment, is 0.4 There independent trials of the experiments are performed. The probability that the event $A$ happens atleast once, is
A. $0 \cdot 936$
B. $0 \cdot 784$
C. $0 \cdot 904$
D. none

## Answer: B

99. The probability that a man will live 10 more years is $\frac{1}{4}$ and the probability that his wife will live 10 more years is $\frac{1}{3}$. Then the probability that neither will be alive in 10 years is
A. $5 / 12$
B. $1 / 2$
C. $7 / 12$
D. $11 / 12$

## Answer: B

## - Watch Video Solution

100. Odds 8 to 5 against a person who is 40 years old living till he is 70 year and 4 to 3 against another person now 50 years till he will be living 80 years. Probability that one of them will be alive next 30 years
A. $59 / 91$
B. $44 / 91$
C. $51 / 91$
D. $32 / 91$

## Answer: B

## - Watch Video Solution

101. The probability that a student is not a swimmer is $\frac{1}{5}$. What is the probability that out of 5 students, 4 are swimmers?
A. ${ }^{5} C_{4}\left(\frac{4}{5}\right)^{4} \frac{1}{5}$
B. $\left(\frac{4}{5}\right)^{4} \frac{1}{5}$
C. ${ }^{5} C_{1} \frac{1}{5}\left(\frac{4}{5}\right)^{4}$
D. none

## Answer: A

102. A die is thrown thrice. A success is or 6 in a throw. Find the mean and variance of the number of successes.
A. $\mu=1, \sigma^{2}=2 / 3$
B. $\mu=2 / 3, \sigma^{2}=1$
C. $\mu=2, \sigma^{2}=2 / 3$
D. none

## Answer: A

Watch Video Solution
103. The Binomial distribution whose mean is 3 and whose standard deviation is $3 / 2$ is
A. $(1 / 2+1 / 2)^{12}$
B. $(1 / 4+3 / 4)^{12}$
C. $(3 / 4+1 / 4)^{12}$
D. none

## Answer: C

## - Watch Video Solution

104. India plays two matches each with West Indies and Australia. In any match the probabilities of India getting points 0,1 and 2 are $0.45,0.05$ and 0.50 respectively. Assuming that the outcomes are independent, the probability of India getting at least 7 points is
A. $0 \cdot 8750$
B. 0875
C. $0 \cdot 0625$
D. $0 \cdot 0250$

## Answer: B

105. The value of $P(2)$ in a Binomial distribution when $\mathrm{p}=1 / 6$ and $\mathrm{n}=5$ is
A. $\frac{3125}{7776}$
B. $\frac{250}{7776}$
C. $\frac{1250}{7776}$
D. $\frac{25}{7776}$

## Answer: C

## - Watch Video Solution

106. One hundred identical coins, each with probability ' p ' of showing heads are tossed once. If $0<p<1$ and the probability of heads showing on 50 coins is equal to that of heads showing on 51 coins, then the value of $p$ is
A. $\frac{1}{2}$
B. $\frac{49}{101}$
C. $\frac{50}{101}$
D. $\frac{51}{101}$

## Answer: D

## - Watch Video Solution

107. A class consists of 80 students 25 of them are girls and 55 boys. If 10 of them are rich and the remaining poor and also 20 of them are intelligent them the probability of selecting an intelligent rich girl is
A. $5 / 128$
B. $25 / 128$
C. 5/512
D. none

## Answer: C

108. v37
A. $1 / 2$
B. $1 / 8$
C. $3 / 8$
D. none

## Answer: A

## - Watch Video Solution

109. A coin and a die are thrown simultaneously. The probability that a head appears on coin and ' 3 ' on the die is
A. $1 / 8$
B. $1 / 12$
C. $1 / 2$
D. 1

## Answer: B

## - Watch Video Solution

110. $A a n d B$ are two independent events. The probability that both AandB occur is $1 / 6$ and the probability that neither of them occurs is $1 / 3$. Find the probability of the occurrence of $A$.
A. $1 / 2$
B. $1 / 3$
C. 0
D. 1

## Answer: A: B

111. If on an average, 1 ship in every 10 is sunk, find the chance that out of 5 ships expected 4 at least will arrive safely.

## - Watch Video Solution

112. Of three independent events the prob. that the first only should happen is $\frac{1}{4}$, the prob. that the second only should happen is $\frac{1}{8}$ and the probability that the third only should happen is $\frac{1}{12}$. Obtain the unconditional probabilities of the three events.

## - View Text Solution

113. Two sets of candidates are competing for the position on the board of directors of a company. The probabilities that the first and second sets will win are 0.6 and 0.4 respectively. If the first set wins, the probability of introducing a new product is 0.8 and the corresponding probability if the
second set wins is 0.3 . What is the probability that the new product will be introduced ?

## - Watch Video Solution

114. In a bolt factory machines $A, B, C$ manufacture respectively 25,35 and 40 percent of the total. Out of their output 5,4 and 2 percent are defective bolts. A bolt is drawn from the produce and is found defective.

What is the probability that it was manufactured by A?

## - Watch Video Solution

115. A manufacturing firm produces steel pipes in three plants with daily production volumes of 500, 1000, and 2000 units respectively. According to past experience it is known that fractions of defective outputs produced by the three plants are respectively $0.005,0.008$ and 0.010 . if a pipe is selected from day's total production and found to be defective, what is the probability that it came from the first plant?
116. If the events A and B are independent, then $P(A \cap B)$ is equal to
A. $P(A)+P(B)$
B. $P(A) P(B)$
C. $P(A / B)$
D. $P(B / A)$

## Answer: B

## - Watch Video Solution

117. If A and B are mutually exclusive events, then $P(A \cap B)$ equals
A. 0
B. $\frac{1}{2}$
C. 1
D. $\frac{1}{4}$

## Answer: A

## - Watch Video Solution

118. If $A$ and $B$ are arbitrary events, then
A. $P(A \cap B) \geq P(A)+P(B)-1$
B. $P(A \cap B) \leq P(A)+P(B)-1$
C. $P(A \cap B)=P(A)+P(B)-1$
D. none

Answer: A

## - Watch Video Solution

119. If A and B are arbitrary events, then a) $P(A \cap B) \geq P(A)+P(B)$ (b) $P(A \cup B) \leq P(A)+P(B)$ (c) $P(A \cap B)=P(A)+P(B)$ (d)None of these
A. $P(A \cap B) \geq P(A)+P(B)$
B. $P(A \cap B) \leq P(A)+P(B)$
C. $P(A \cap B)=P(A)+P(B)$
D. none

## Answer: B

## - Watch Video Solution

120. The happening of any one of the two mutually exclusive events $A$ and $B$ is
A. $P[A] . P[B]$
B. $P(A)+P(B)-P(A \cap B)$
C. $P[A]+P[B]$
D. none

Answer: C

## - Watch Video Solution

121. For any two independent events $E_{1}$ and $E_{2}$, $P\left\{E_{1} \cup\left(E_{2}\right) \cap\left(\overline{E_{1}}\right) \cap\left(\overline{E_{2}}\right)\right\}$ is
A. $\leq 1 / 4$
B. $>1 / 4$
C. $\geq 1 / 2$
D. none

## Answer: A

122. If A and B are two events such that $P(A)>0$ and $P(B) \neq 1$, then $P\left(\frac{\bar{A}}{B}\right)$ is equal to
A. $1-P(A / B)$
B. $1-P(\bar{A} / B)$
C. $\frac{1-P(A \cup B)}{P(\bar{B})}$
D. $\frac{P(\bar{A})}{P(\bar{B})}$

## Answer: C

## - Watch Video Solution

123. If there are n independent trials, p and q are the probability of success and failure respectively, then probability of exactly $r$ success
A. $q^{n}$
B. ${ }^{n} C_{r} q^{n} p^{r}$
C. ${ }^{n} C_{r} q^{n-r} p^{r}$
D. ${ }^{n} C_{r} p^{n-r} q^{r}$

## Answer: C

## - Watch Video Solution

124. If A and B ar two events such that $P(A \cup B)=\frac{5}{6}, P(A \cap B)=\frac{1}{3}$ and $P\left(\bar{B}=\frac{1}{2}\right)$ then the events A and B are
A. dependent
B. independent
C. mutually exclusive
D. none

## Answer: B

## - Watch Video Solution

125. If $P(A)=0 \cdot 65, P(B)=0 \cdot 15, P(\bar{A})+P(\bar{B})=$
A. 1 - 5
B. $1 \cdot 2$
C. $0 \cdot 8$
D. none

## Answer: B

## - Watch Video Solution

126. Two events $\operatorname{Aand} B$ have probabilities 0.25 and 0050 , respectively. The probability that both $\operatorname{AandB}$ occur simultaneously is 0.14 . then the probability that neither $A$ nor $B$ occurs is a. 0.39 b .0 .25 c .0 .11 d . none of these
A. 75
B. 61
C. 39
D. none

## Answer: C

## - Watch Video Solution

127. The probability of an event $A$ occurring is 0.5 and of $B$ occuring is 0.3 . If $A$ and $B$ are mutually exclusive events, then the probability of neither $A$ nor B occurring is
A. $0 \cdot 6$
B. $0 \cdot 5$
C. $0 \cdot 7$
D. none

## Answer: D

128. The simulataneous occurrence of two dependent events $A$ and $B$ is
A. $P(A) \cdot P(B / A)$
B. $P(A)+P(B)-2 P(A \cap B)$
C. $P(A) \cdot P(B)$
D. none

## Answer: A

## - Watch Video Solution

129. Two independent events $A$ and $B$ will happen simultaneously, the probability is
A. $P(A)+P(B)$
B. $P(\bar{A}) \cdot P(\bar{B})$
C. $P(A) \cdot P(B)$
D. $P(A)-P(B)$

## Answer: C

## - Watch Video Solution

130. If $A$ and $B$ are two independent events in a sample space then $P(\bar{A} / \bar{B})$ equals
A. $1-P(A / B)$
B. $1-P(\bar{A} / B)$
C. $1-P(B)$
D. $1-P(A)$

## Answer: D

## - Watch Video Solution

131. The probability that at least one of the event $A$ and $B$ occurs is 0.6 . If

A and B occur simultaneously with probability 0.2 , then find $P(A)+P(B)$.
A. $0 \cdot 4$
B. $0 \cdot 8$
C. $1 \cdot 2$
D. $1 \cdot 4$

## Answer: C

## - Watch Video Solution

132. If $0<P(A)<1,0<P(B)<1$
$P(A \cup B)=P(A)+P(B)-P(A) P(B)$, then
A. $P(B / A)=P(B)-P(A)$
B. $P\left(A^{C}-B^{C}\right)=P\left(A^{C}\right)-P\left(B^{C}\right)$
C. $P(A \cup B)^{C}=P\left(A^{C}\right) \cdot P\left(B^{C}\right)$
D. $P(A / B)=P(A)$

## Answer: C::D

## - Watch Video Solution

133. If $E$ and $F$ are independent events such that $0<P(E)<1$ and $0<P(F)<1$, then
A. E and F are mutually exclusive
B. E and $F^{C}$ (complement of the event F ) are independent
C. $E^{C}$ and $F^{C}$ are independent
D. $P(E / F)+P\left(E^{C} / F\right)=1$

## Answer: B::C::D

134. If $A$ and $B$ are any two events, the probability that exactly one of them occurs is
A. $P(A)+P(B)-2 P(A \cap B)$
B. $P(\bar{A})+P(\bar{B})-2 P(\bar{A} \cap \bar{B})$
C. $P(A \cup B)+P(A \cap B)$
D. $P(A)-P(B)+2 P(\bar{A} \cap B)$

## Answer: A:B::C:D

## - Watch Video Solution

135. If $P(B)=\frac{3}{4}, P(A \cap B \cap \bar{C})=\frac{1}{3}$ and $P(\bar{A} \cap B \cap \bar{C})=\frac{1}{3}$, then $P(B \cap C)$
A. $1 / 12$
B. $3 / 4$
C. $5 / 12$

## Answer: A

## - Watch Video Solution

136. Let E and F be two independent events. The probability that both E and $F$ happen is $\frac{1}{12}$ and the probability that neither $E$ nor $F$ happens is $\frac{1}{2}$, then a value of $\frac{P(E)}{P(F)}$ is
A. $P(E)=\frac{1}{3}, P(F)=\frac{1}{4}$
B. $P(E)=\frac{1}{2}, P(F)=\frac{1}{6}$
C. $P(E)=\frac{1}{6}, P(F)=\frac{1}{2}$
D. $P(E)=\frac{1}{4}, P(F)=\frac{1}{3}$

## Answer: A:D

## - Watch Video Solution

137. $A$ and $B$ are two independent events. The probability that both $A$ and B occur is $1 / 6$ and the probability that neither of them occurs is $1 / 3$. the probability of $A$ is
A. $P(A)=1 / 2, P(B)=1 / 3$
B. $P(A)=1 / 2, P(B)=1 / 6$
C. $P(A)=1 / 3, P(B)=1 / 2$
D. none

## Answer: A::C

## - View Text Solution

138. For any two events $A$ and $B$ in a sample space
A. $P(A / B) \geq \frac{P(A)+P(B)-1}{P(B)}, P(B) \neq 0$ is always true.
B. $P(A \cap \bar{B})=P(A)-P(A \cap B)$ does not hold
C. $P(A \cup B)=1-P(\bar{A}) P(\bar{B})$, if A and B are independent
D. $P(A \cup B)=1-P(\bar{A}) P(\bar{B})$, if A and B are disjoint

## Answer: A: C

## - Watch Video Solution

139. If $A$ and $B$ are two events, the probability that exactly one of them occurs is given by
A. $P(M)+P(N)-2 P(M \cap N)$
B. $P(M)+P(N)-P(M \cap N)$
C. $P\left(M^{C}\right)+P\left(N^{C}\right)-2 P\left(M^{C} \cap N^{C}\right)$
D. $P\left(M \cap N^{C}\right)+P\left(M^{C} \cap N\right)$

## Answer: A::C::D

## - Watch Video Solution

140. For two given event A and $\mathrm{B}, P(A \cap B)$ is
A. not less than $P(A)+P(B)-1$
B. not greater than $P(A)+P(B)$
C. equal to $P(A)+P(B)-P(A \cup B)$
D. equal to $P(A)+P(B)+P(A \cup B)$

## Answer: A::C

## - Watch Video Solution

141. If $A$ and $B$ are arbitrary events then
A. $P(A \cap B) \leq P(A)+P(B)$
B. $P(A \cup B) \leq P(A)+P(B)$
C. $P(A \cup B)=P(A)+P(B)$
D. $P(A \cup B) \geq P(A)+P(B)$

## D Watch Video Solution

142. There are 3 bags each containing 5 white balls and 2 black balls, and 2 bags each containing 1 white ball and 4 black balls, a black ball having been drawn, find the chance that it came from the first group.

## - Watch Video Solution

143. A fair die is tossed repeatedly until a 6 is obtained. Let $X$ denote the number of tosses required.

The probability that $X=3$ equals
A. $\frac{25}{216}$
B. $\frac{25}{36}$
C. $\frac{5}{36}$
D. $\frac{125}{216}$

## D Watch Video Solution

144. A fair die is tossed repeatedly until a 6 is obtained. Let $X$ denote the number of tosses rerquired.

The probability that $\geq 3$ equals
A. $\frac{125}{216}$
B. $\frac{25}{36}$
C. $\frac{5}{36}$
D. $\frac{25}{216}$

## Answer: B

145. A fair die is tossed repeatedly until a six obtained. Let $X$ denote the number of tosses required.

The conditional probability that $X \geq 6$ given $X>3$ equals
A. $\frac{125}{216}$
B. $\frac{25}{216}$
C. $\frac{5}{36}$
D. $\frac{25}{36}$

## Answer: D

## - Watch Video Solution

146. A pair of fair dice is thrown independently three times. The probability of getting a score of exactly 9 twice is (1) 1/729 (2) 8/9 (3) 8/729 (4) 8/243
A. $\frac{1}{729}$
B. $\frac{8}{9}$
C. $\frac{8}{729}$
D. $\frac{8}{243}$

## Answer: D

## - Watch Video Solution

147. An experiment has 10 equally likely outcomes. Let $A$ and $B$ be two non-empty events of the experiment. If a consists of 4 outcomes, the number of outcomes that B must have so that A and B are independent, is
A. 2,4 or 8
B. 3,6 or 9
C. 4 or 8
D. 5 or 10

## Answer: D

## - Watch Video Solution

148. There are $n$ urns numbered 1 to $n$. The ith urn contains $i$ white contains $i$ white and $(n+1-i)$ black balls. Let $E_{i}$ denote the even of selecting ith urn at random and let $W$ denote the event that the ball drawn from the selected urn is white. If $P\left(E_{i}\right) \propto i$ for $i=1,2 \ldots \ldots \ldots, n$ then $\lim _{n \rightarrow \infty} P(W)$ is
A. $2 / 3$
B. $1 / 3$
C. $1 / 2$
D. $3 / 4$

## Answer: A

149. There are n urns each continuous ( $\mathrm{n}+1$ ) balls such that the ithurn contains 'I' white balls and ( $\mathrm{n}+1-\mathrm{i}$ ) red balls. Let $u_{1}$ be the event of selecting ith urn, $i=1,2,3 . \ldots . . . . . n$ and $W$ denotes the event of getting a white balls.

If n is even and E dentes the event of choosing even numbered urn $\left[P\left(u_{i}\right)=\frac{1}{n}\right]$, then the value of $P(W / E)$ is
A. $\frac{1}{2}$
B. $\frac{n}{n+1}$
C. $\frac{n+2}{2(n+1)}$
D. $\left(\frac{n+1}{n+2}\right)$

## Answer: C

## - Watch Video Solution

150. There are n urns $U_{i},(i=1, \ldots, n)$ which contains $i$ white and ( $\mathrm{n}+1-\mathrm{i}$ ) black balls. $U_{i}$ is even of selecting the $j$ th urn, W event of getting
white ball from the selected urn, E is event of getting even number of balls from selected urn.
Q. $P\left(U_{i}\right)=\frac{1}{n}$, and one urn is selected at random, then $\mathrm{P}(\mathrm{W})$ is:
A. $\frac{1}{2}$
B. $\frac{1}{n}$
C. $\frac{n}{n+1}$
D. $\frac{n+1}{n+2}$

## Answer: A

## D Watch Video Solution

151. Let $H_{1}, H_{2}, \ldots, H_{n}$ be mutually exclusive and exhaustive events with
$P\left(H_{i}\right)>0, i=1,2, \ldots n$. Let E be any other event with $0<P(E)<1$.
STATEMENT-1: $P\left(H_{i} \mid E\right)>P\left(E \mid H_{1}\right) \cdot P\left(H_{i}\right)$ for $i=1,2, \ldots, n$
because
STATEMENT-2: $\sum_{i=1}^{n} P\left(H_{i}\right)=1$
A. (a)Statement -1 is true , Statement -2 is true, Statement -2 is a correct explanation for Statement -1
B. (b)Statement -1 is true, Statement -2 is true, Statement -2 is not a correct explanation for Statement -1
C. (c)Statement -1 is true, Statement -2 is false
D. (d)Statement-1 is false, Statement- 2 is true

## Answer: B

## D Watch Video Solution

## Problem Set 1 True And False

1. $A$ and $B$ throw a pair of dice. If $A$ throws 9 , find Bs chance of throwing a higher number.
2. If $A$ and $B$ are mutually exclusive events, then they will be independent also.

## - Watch Video Solution

3. Two independent events are always mutually exclusive.

## ( Watch Video Solution

4. If the probabilities for $A$ to fail in an examination is 0.2 and that for $B$ is 0.3 , then the probability that either $A$ or $B$ fails is

## - Watch Video Solution

5. The odds in favour of $A$ winning a game of chess against $B$ are 5:2. if three games are to be played, then the odds in favour of A's winning at least one game are 355:8.
6. If $\left(A_{1} \cup A_{2}\right)=1-P\left(A_{1}^{c}\right) P\left(A_{2}^{c}\right)$ where C is the complementary then $A_{1}$ and $A_{2}$ are independent.

## Watch Video Solution

7. $A$ and $B$ each throw a die. Then it is $7: 5$ that $A$ 's throw is not greater than B's.

## - Watch Video Solution

8. A biased die is tossed and the respective probabilities for various faces to turn up are

| Face | $:$ | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Probability | $:$ | 0.1 | 0.24 | 0.19 | 0.18 | 0.15 | 0.14 |

If an even face has turned up, then the probability that it is face 2 or face 4, is
9. The probabilities of three mutually exclusive events $A, B$ and $C$ are given by $2 / 3,1 / 4$ and $1 / 6$ respectively. The statement. a. is true $b$. is false $c$. nothing can be said d. could be either

## - Watch Video Solution

10. Ten students are seated at random in a row. The probability that two particular students are not seated side by side is $4 / 5$.

## - Watch Video Solution

11. Two persons $A$ and $B$ throw a coin alternatively till one of them gets head and wins the game. Find their respective probabilities of winning.

## - Watch Video Solution

1. A pair of unbiased dice are rolled together till a sum of either 5 or 7 is obtained. Then find the probability that 5 comes before 7 .

## Watch Video Solution

2. The probability that a bomb dropped from a plane strikes the target is $1 / 5$. the probability that out of six bombs dropped, at least two bombs strike the target is $\qquad$

## - Watch Video Solution

3. A pair of dice is thrown 4 times. If getting a doublet is considered a success, find the probability of two successes.

## - Watch Video Solution

4. A determinant is chosen at random from the set of all determinants of order two with elements 0 or 1 only. Probability that the determinant chosen has positive value is

## - Watch Video Solution

5. For a biased die, the probabilities for the different faces to turn up are given by the table

| Face | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Probability | 0.1 | 0.32 | 0.21 | 0.15 | 0.05 | 0.17 |

The die is thrown and you are told that either the face 1 or the face 2 has turned up, then the probability that it is face 1 , is

## - Watch Video Solution

6. The probability of getting a number between 1 and 100 which is divisible by 1 and itself only is $\qquad$
7. A box contains 100 tickets numbered $1,2,3, \ldots, 100$. Two tickets are chosen at random. It is given that the maximum number on the two chosen tickets is not more than 10 . the minimum number on them is 2 with probability $\qquad$ .

## - Watch Video Solution

8. $P(A$ cup $B)=P(A \text { cap } B)^{\prime}$ if and only if the relation between $P(A)$ and $P(B)$ is

## - Watch Video Solution

9. If $A$ and $B$ be two events such that $P(A)=0 \cdot 3$ and $P(A \cup \bar{B})=0 \cdot 8$. If A and B are independent events, then $\mathrm{P}(\mathrm{B})=$ $\qquad$
10. If $E_{1}$ and $E_{2}$ are exclusive events then $P\left(E_{1} \cap E_{2}\right)=$ $\qquad$

## - Watch Video Solution

11. If $\frac{1+3 p}{3}, \frac{1-p}{4}$ and $\frac{1-2 p}{2}$ are the probabilities of three mutually exclusive events, then the set of all values of $p$ is $\qquad$ .

## - Watch Video Solution

12. If $\frac{(1-3 p)}{2}, \frac{(1+4 p)}{3}, \frac{(1+p)}{6}$ are the probabilities of three mutually excusing and exhaustive events, then the set of all values of $p$ is
a. $(0,1)$ b. $(-1 / 4,1 / 3)$ c. $(0,1 / 3)$ d.
A. $(0,1)$
B. $\left(-\frac{1}{4}, \frac{1}{3}\right)$
C. $\left(0, \frac{1}{3}\right)$
D. $(0, \infty)$

## - Watch Video Solution

13. If $E_{1}$ and $E_{2}$ are two events and $E_{2}$ is a subset of $E_{1}$ then $P\left(E_{1} / E_{2}\right)$
$=$ $\qquad$

## D Watch Video Solution

14. If two events $A$ and $B$ are such that $P(\bar{A})=0.3, P(B)=0.4$ and $P(A \cap \bar{B})=0.5$, then $P\left(\frac{B}{A \cup \bar{B}}\right)$ is equal to

## - Watch Video Solution

15. If $P(A \cup B)=0 \cdot 9, P(B)=0 \cdot 4$ when A and B are independent events then $P(A)=$ $\qquad$
16. Urn A contains 6 red and 4 black balls and urn B contains 4 red and 6 black balls, one ball is drawn at random from urn $A$ and placed in urn $B$. then one ball drawn at random from urn $B$ and placed in urn $A$. if one ball is now drawn from urn $A$, the probability that it is found to be red is $\qquad$

## ( Watch Video Solution

17. The probability that India wins a cricket test match against England is $1 / 3$. if india and england play three test matches, the probability that India will win at least one test match is $\qquad$

## ( Watch Video Solution

## Self Assessment Test

1. The probability of getting heads in both trials, when a balanced coin is tossed twice, will be
A. $1 / 4$
B. $1 / 2$
C. 1
D. $3 / 4$

## Answer: A

## - Watch Video Solution

2. Two cards are drawn at random from a pack of 52 cards. The probability of these two being aces is
A. $\frac{1}{26}$
B. $\frac{1}{221}$
C. $\frac{1}{2}$

## D. none

## Answer: B

## - Watch Video Solution

3. An almirah stores 5 black and 4 white socks well mixed. A boy pulls out 2 socks at random. The probability that 2 are of the same colour is
A. $\frac{5}{108}$
B. $\frac{1}{6}$
C. $\frac{5}{18}$
D. $\frac{4}{9}$

Answer: D

## - Watch Video Solution

4. $A$ and $B$ throw a pair of dice. If $A$ throws 9 , find Bs chance of throwing a higher number.
A. 1
B.
C. both
D. none

## Answer: A

## - Watch Video Solution

5. Two cards are drawn successively with replacement from a well-shuffled pack of 52 cards. The probability of drawing two aces is
A. $\frac{1}{13} \times \frac{1}{13}$
B. $\frac{1}{13} \times \frac{1}{17}$
C. $\frac{1}{52} \times \frac{1}{51}$
D. $\frac{1}{13} \times \frac{4}{51}$

## Answer: A

## - Watch Video Solution

6. A pack of cards contains 4 aces, 4 kings, 4 queens and 4 jacks. Two cards are drawn at random. The probability that at least one of them is an ace is
A. $\frac{9}{20}$
B. $\frac{3}{16}$
C. $\frac{1}{6}$
D. $\frac{1}{9}$

## Answer: A

## - Watch Video Solution

7. Three urns contain respectively 3 white and 1 black balls, 2 white and 2 black, 1 white and 3 black. One ball is selected at random from each urn. Find the chance that the three selected comprise 1 white and 2 black balls.

## - Watch Video Solution

8. Two dice are thrown. What is the probability of scoring either a double, or a sum greater than 9 ?

## - Watch Video Solution

9. An integer is chosen at random from the first two hundred digits. What is the probability that the integer chosen is divisible by 6 or 8 ?

## - Watch Video Solution

10. A person draws a card from a pack of playing cards, replaces it and shuffles the pack. He continues doing this until he shows a spade. The chance that he will fail the first two times is
A. $\frac{9}{64}$
B. $\frac{1}{64}$
C. $\frac{1}{16}$
D. $\frac{9}{16}$

## Answer: A

## - Watch Video Solution

11. If $A$ and $B$ are mutually exclusive events, then they will be independent also.
A. 1
B.
C. both
D. none

## Answer: B

## - Watch Video Solution

12. Two independent events are always mutually exclusive.
A. 1
B.
C. both
D. none

## Answer: B

## - Watch Video Solution

13. Three letters are written to different persons and addressess to three envelopes are also written. Without looking at the addresses, the probability that probability that the letters go into right envelopes, is
A. $\frac{1}{27}$
B. $\frac{1}{6}$
C. $\frac{1}{9}$
D. none

## Answer: B

## - Watch Video Solution

14. The probability that a student is not a swimmer is $\frac{1}{5}$. What is the probability that out of 5 students, 4 are swimmers?

> A. ${ }^{5} C_{4}\left(\frac{4}{5}\right)^{4} \frac{1}{5}$
> B. $\left(\frac{4}{5}\right)^{4} \frac{1}{5}$
C. ${ }^{5} C_{1} \frac{1}{5}\left(\frac{4}{5}\right)^{4}$
D. none

## Answer: A

## - Watch Video Solution

15. Probability of throwing a 5 only on the first of two successive throws of an ordinary die is
A. $\frac{1}{36}$
B. $\frac{5}{36}$
C. $\frac{25}{36}$
D. $\frac{1}{6}$

## Answer: B

16. A fair coin is tossed repeatedly. If tail appears on first four tosses, them the probability of head appearing that 2 white and 1 black balls will be drawn, is
A. $\frac{1}{2}$
B. $\frac{1}{32}$
C. $\frac{31}{32}$
D. $\frac{1}{5}$

## Answer: A

## Watch Video Solution

17. There are three works, one consisting of 3 volumes, one of 4 , and the other of 1 volume. They are placed on a shelf at random. Find the chance that volumes of the same works are all together.
18. A bag contains 4 white, 5 red and 6 black balls. Three are drawn at random. Find the probability that (i) no ball drawn is black, (ii) exactly 2 are black (iii) all are of the same colour.

## - Watch Video Solution

19. An urn contains 11 balls numbered from 1 to 11 . if a ball is selected at random, what is the probability of having a ball with a number which is multiple of either 2 or 3 ?

## - Watch Video Solution

20. The probability that a certain beginner at golf gets a good shot if he uses the correct club is $\frac{1}{3}$, and the probability of a good shot with an incorrect club is $\frac{1}{4}$. In his bag are 5 different clubs, only one of which is correct for the shot is question. if he chooses a club at random and takes a stroke, the probability that he gets a good shot is
A. $\frac{1}{3}$
B. $\frac{1}{12}$
C. $\frac{4}{15}$
D. $\frac{7}{12}$

## Answer: C

## - Watch Video Solution

21. The probability that in the toss of two dice we obtain the sum 7 or 11 is
A. $\frac{1}{6}$
B. $\frac{1}{18}$
C. $\frac{2}{9}$
D. $\frac{23}{108}$

## Answer: C

22. Two dice are thrown. The probability that the sum of the points on two dice will be 7 is
A. $\frac{5}{36}$
B. $\frac{6}{36}$
C. $\frac{7}{36}$
D. $\frac{8}{36}$

## Answer: B

## - Watch Video Solution

23. Two dice are thrown simultaneosly. The probability of obtaining a total score of 5 is
A. $\frac{1}{18}$
B. $\frac{1}{12}$
C. $\frac{1}{9}$
D. none

## Answer: C

## - Watch Video Solution

24. A can solve $75 \%$ of the problems of Mathematics and $B$ can solve $70 \%$. What is the probability that either $A$ or $B$ can solve a problem chosen at random?

## - Watch Video Solution

25. A room has three lamp sockets. From a collection of 10 light bulbs of which only six ar good, three bulbs are selected at random and placed in the sockets. What is the probability that there will be light in the room?
26. One of the two events must occur. If the chance of one is $2 / 3$ of the other, then odds in favour of the other are a. 1:3 b. 3:1 c. 2:3 d. 3:2
A. 1:3
B. 3: 1
C. 2:3
D. none

## Answer: D

## - Watch Video Solution

27. An arbitrary cube has four blank faces, one face marked 2 and another marked 3 . Then the probability of obtaining a total of exactly 12 in 5 throws is
A. $\frac{5}{1296}$
B. $\frac{5}{1944}$
C. $\frac{5}{2592}$
D. none

## Answer: C

## - Watch Video Solution

28. An experiment succeeds twice as often as it fails. Find the probability that in the next six trials, there will be atleast 4 successes.

## - Watch Video Solution

29. The probability that a marksman will hit a target is given as $\frac{1}{5}$. Then, the probabiltiy that atleast one hit in 10 shots is
A. $1-\left(\frac{4}{5}\right) s$
B. $\frac{1}{5}$ s
C. $1-\frac{1}{5} s$
D. none

## Answer: A

## - Watch Video Solution

30. The probability that a man can hit a target is $3 / 4$. He tries 5 times. The probability that he will hit the target at least three times is
A. $\frac{291}{364}$
B. $\frac{371}{464}$
C. $\frac{471}{502}$
D. $\frac{459}{512}$

## Answer: D

## - Watch Video Solution

31. The probability of ' n ' independent events are $P_{1}, P_{2}, P_{3} \ldots \ldots, P_{n}$. Find an expression for probability that at least one of the events will happen.

## - Watch Video Solution

32. A's skill is to $B$ as $1: 3$, to $C$ 's as $3: 2$ and to $D$ 's as $4: 3$, find the chance that A in three trials, one with each person, will succeed twice at least.

## - Watch Video Solution

33. Five person $A, B, C, D, E$ throw a dice in the order specified until one of them throws an ace, find their relative chances of winning, supposing the throws to continue till an ace appears.

## - Watch Video Solution

34. Three urns contain respectively 1 white, 2 black balls, 2 W and 1 B balls, 2 W and 2 B balls. One ball is transferred from the first urn into the second, then one from the letter is transferred into the third. Finally one ball is drawn from the third urn. what is the probability of its being white ?

## - Watch Video Solution

35. $A$ is a set containing $n$ elements. $A$ subset $P$ of $A$ is chosen at random.

The set A is reconstructed by replacing the elements of P. A subset $Q$ is again chosen at random. The probability that $P$ and $Q$ are disjoint sets, is

## - Watch Video Solution

36. The odds in favour of A winning a game of chess against B are 5:2. if three games are to be played, then the odds in favour of A's winning at least one game are 355:8 .If this is true give answer 1 else 0 .
A. 1
B. 0
C. both
D. none

## Answer: A

## - Watch Video Solution

37. A number is chosen at random among the first 120 natural numbers.

The probability of the number chosen being a multiple of 5 or 15 is
A. $1 / 5$
B. $1 / 8$
C. $1 / 6$
D. none
38. The probability of an event $A$ occurring is 0.5 and of $B$ occuring is 0.3 .

If $A$ and $B$ are mutually exclusive events, then the probability of neither $A$ nor B occurring is
A. $0 \cdot 6$
B. $0 \cdot 5$
C. $0 \cdot 7$
D. none

## Answer: D

## - Watch Video Solution

39. The probability that an event A happens in one trial of an experiment, is 0.4 There independent trials of the experiments are performed. The probability that the event A happens atleast once, is
A. $0 \cdot 936$
B. $0 \cdot 784$
C. $0 \cdot 904$
D. none

## Answer: B

## - Watch Video Solution

40. A single letter is selected at random from the word "PROBABILITY" .

The probability that it is a vowel is
A. $3 / 11$
B. $4 / 11$
C. $2 / 11$
D. 0
41. In a box containing 100 bulbs, 10 are defective. What is the probability that out of a sample of 5 bulbs, (i) none is defective and (ii) exactly 2 are defective?
A. $10^{-5}$
B. $(1 / 2)^{5}$
C. $(9 / 10)^{5}$
D. $9 / 10$

## Answer: C

## - Watch Video Solution

42. If the probabilities for $A$ to fail in an examination is 0.2 and that for $B$ is 0.3 , then the probability that either $A$ or $B$ fails is
A. 1
B. 0.44
C. both
D. none

## Answer: B

## - Watch Video Solution

43. A multiple choice examination has 5 questions. Each question has three alternative answers of which exactly one is correct. The probability that a student will get 4 or more correct answers just guessing is
A. $\frac{17}{3^{5}}$
B. $\frac{13}{3^{5}}$
C. $\frac{11}{3^{5}}$
D. $\frac{10}{3^{5}}$

## Answer: C

## D Watch Video Solution

44. The probability of having at least one tail 4 throws with a coin is
A. $15 / 16$
B. $1 / 16$
C. $1 / 4$
D. 1

## Answer: A

## Watch Video Solution

45. From a pack of cards two are drawn the first being replaced before the second is drawn Find the probability that the first is a diamond and the second is a king .
A. $13 / 4$
B. $4 / 13$
C. $1 / 52$
D. 52

## Answer: C

## - Watch Video Solution

46. Two cards are drawn at random from a pack of playing cards. Find the probability that one card is a heart and the other is an ace.

## - View Text Solution

47. Two uniform dice marked 1 to 6 are tossed together. The probability of the total 7 in a single throw is
B. $5 / 12$
C. $2 / 31$
D. $1 / 6$

## Answer: D

## - Watch Video Solution

48. The probability of India winning a test match against west Indies is
$1 / 2$. assuming independence from match to match, the probability that in a 5 match series India's second win occurs at third test is
A. $1 / 8$
B. $1 / 4$
C. $1 / 2$
D. $2 / 3$

## Answer: B

49. A coin is tossed $(m+n)$ times $(m>n)$. Find the probability of at least m consecutive heads.

## - Watch Video Solution

50. Each coefficient in the equation $a x^{2}+b x+c=0$ is determined by throwing ordinary six faced die. Find the probability that the equation will have real roots.

## - Watch Video Solution

51. Three persons A, B and C, in order, cut a pack of cards replacing them after each cut on the condition that the first who cuts a spade shall win the prize. Find their respective chances.
52. One bag contains 5 white and 3 red balls, and a second bag contains 4 white and 5 red balls. From one of them chosen at random two balls are drawn, find the chance that they are of different colours.

## - Watch Video Solution

53. Supposing that it is 9 to 7 against a person $A$ who is now 35 years of age living till he is 65 , and 3 to 2 against a person $B$ now 45 till he is 75 , find the chance that one at least of these persons will be alive 30 years hence.

## - Watch Video Solution

54. In shuffling a pack of 52 playing cards, four are accidently dropped; find the chance that the missing cards should be one from each suit.

## - Watch Video Solution

55. The probability that Krishna will be alive 10 years hence is $7 / 15$ and that Hari will be alive is $7 / 10$. What is t he probability that both Krishna and Hari will be dead 10 years hence?
A. $\frac{21}{150}$
B. $\frac{24}{150}$
C. $\frac{49}{150}$
D. $\frac{56}{150}$

## Answer: B

## - Watch Video Solution

56. A bag has 13 red, 14 green and 15 black balls, The probability of getting exactly 2 black on pulling out 4 balls is $P_{1}$. Now the number of each colour ball is doubled and 8 balls are pulled out. The probability of getting exactly 4 blacks is $P_{2}$ then.

$$
\text { A. } P_{1}=P_{2}
$$

B. $P_{1}>P_{2}$
C. $P_{1}<P_{2}$
D. none

## Answer: B

## - Watch Video Solution

57. A purse contains 4 copper coins, 3 silver coins, the second purse contains 6 copper coins and 2 silver coins. A coin is taken out of any purse, the probability that it is a copper coin is
A. $\frac{4}{7}$
B. $\frac{3}{4}$
C. $\frac{3}{7}$
D. $\frac{37}{56}$

## Answer: D

58. Two persons, $A$ and $B$, have respectively $n+1$ and $n$ coins, which they toss simultaneously. Then the probability that A will have more heads that $B$ is
A. $\frac{1}{2}$
B. $>\frac{1}{2}$
C. $<\frac{1}{2}$
D. none

## Answer: A

## - Watch Video Solution

59. Fifteen coupons are numbered $1,2, \ldots, 15$ respectively. Seven coupons are selected at random one at a time with replacement. The probability that the largest number appearing on a selected coupon is 9 , is
A. $\left(\frac{9}{10}\right)^{6}$
B. $\left(\frac{8}{15}\right)^{7}$
C. $\left(\frac{3}{5}\right)^{7}$
D. none

## Answer: C

## - Watch Video Solution

60. An unbiased die with faced marked $1,2,3,4,5$, and 6 is rolled four times. Out of four face value obtained, the probability that the minimum face value is not less than 2 and the maximum face value is not greater than five is then $16 / 81$ b. $1 / 81 \mathrm{c} .80 / 81 \mathrm{~d} .65 / 81$
A. $16 / 81$
B. $1 / 81$
C. $80 / 81$
D. $65 / 81$

## Answer: A

## - Watch Video Solution

61. A box contains 100 tickets, numbered $1,2,3, \ldots$. 100 . two tickets are chosen at random. It is given that the maximum number on the two chosen tickets is not more than 10 . The minimum number of them is 2 with probability. ....

## - View Text Solution

62. A student appears for tests I, II and III. The student is successful if the passes either in tests I and II or tests I and III. The probabilities of the student passing in tests I, II and III are $\mathrm{p}, \mathrm{q}$ and $\frac{1}{2}$, respectively. If the probability that the student is successful, is $\frac{1}{2}$, then
A. $p=q=1$
B. $\mathrm{p}=\mathrm{q}=\frac{1}{2}$
C. $p=1, q=0$
D. $p=1, q=\frac{1}{2}$

## Answer: C

## - Watch Video Solution

63. If $\frac{1+3 p}{3}, \frac{1-p}{4}$ and $\frac{1-2 p}{2}$ are the probabilities of three mutually exclusive events, then the set of all values of $p$ is $\qquad$ .

## - Watch Video Solution

64. If $\frac{1-3 p}{2}, \frac{1+4 p}{3}$ and $\frac{1+p}{6}$ are the probabilities of three mutually exclusive events, then the set of all values of $p$ is $\qquad$
A. $(0,1)$
B. $\left(-\frac{1}{4}, \frac{1}{3}\right)$
C. $\left(0, \frac{1}{3}\right)$

## D. $(0, \infty)$

## Answer: B

## - Watch Video Solution

65. Urn A contains 6 red and 4 black balls and urn B contains 4 red and 6 black balls. One ball is drawn at random from urn A and placed in urn B. Then, one ball is drawn at random from urn B and placed in urn A. If one ball is drawn at random from urn A, the probability that it is found to be red, is....

## - Watch Video Solution

66. One hundred identical coins, each with probability $p$, of showing up heads are tossed once. If `o
A. $\frac{1}{2}$
B. $\frac{49}{101}$
C. $\frac{50}{101}$
D. $\frac{51}{101}$

## Answer: D

## - Watch Video Solution

67. India plays two matches each with West Indies and Australia. In any match the probabilities of India getting points 0,1 and 2 are $0.45,0.05$ and 0.50 respectively. Assuming that the outcomes are independent, the probability of India getting at least 7 points is (a) 0.8750 (b) 0.0875 (c) 0.0625 (d) 0.0250
A. $0 \cdot 8750$
B. 0875
C. $0 \cdot 0625$
D. $0 \cdot 0250$

## Answer: B

## (D) Watch Video Solution

68. There are 3 bags each containing 5 white balls and 2 black balls, and 2 bags each containing 1 white ball and 4 black balls, a black ball having been drawn, find the chance that it came from the first group.

## - Watch Video Solution

69. Consider a family with two children. Assume that each child is as likely to be a boy as it is to be a girl. Find the conditional probability that both children are boys, given that (i) the older child is a boy, (ii) at least one of the children is a boy.

## - Watch Video Solution

70. A coin is tossed 3 times. The probability of obtaining at least two heads will be
A. $3 / 8$
B. $1 / 2$
C. 1
D. 2

## Answer: B

## - Watch Video Solution

71.8 coins are tossed simultaneously. The probability of getting at least 6 heads is
A. $57 / 64$
B. $229 / 256$
C. $7 / 64$
D. $37 / 256$

## Answer: D

72. A sample of size 4 is drawn with replacement (without replacement) from an urn containing 12 balls, of which 8 are white, what is the conditional probability that the ball drawn on the third draw was white, given that the sample contains 3 white balls ?

## D View Text Solution

73. If two events A and B are such that $P\left(A^{C}\right)=0 \cdot 3$
$P(B)=0 \cdot 4$ and $P\left(A B^{C}\right)=0 \cdot 5$ then
$P\left[B /\left(A \cup B^{C}\right)\right]=$

## - Watch Video Solution

74. If $A$ and $B$ are two events such that $P(A \cup B)=5 / 6, P(A \cap B)=1 / 3, P(\bar{B})=1 / 2$, then the events $A$ and $B$ are
A. dependent
B. independent
C. mutually exclusive
D. none

## Answer: B

## - Watch Video Solution

75. $A$ and $B$ each throw a die. Then it is $7: 5$ that $A$ 's throw is not greater than B's.
A. 1
B.
C. both
D. none

## Answer: A

76. Two persons each makes a single throw with a die. The probability they get equal value is $P_{1}$. Four persons each makes a single throw and probability of three being equal is $P_{1}$. Then
A. $P_{1}=P_{2}$
B. $P_{1}<P_{2}$
C. $P_{1}>P_{2}$
D. none

## Answer: C

## - Watch Video Solution

77. A cricket team has 15 members, of whom only 5 can bowl. If the names of the 15 members are put into a hat and 11 drawn random, then the chance of obtaining an eleven containig at least 3 bowlers
A. $\frac{7}{13}$
B. $\frac{11}{15}$
C. $\frac{12}{13}$
D. none

## Answer: C

## - Watch Video Solution

78. On a toss of two dice, A throws a total of 5 , then the probability that he will throw another 5 before the throws 7 , is
A. $\frac{1}{9}$
B. $\frac{1}{6}$
C. $\frac{2}{5}$
D. $\frac{5}{36}$

## Answer: C

79. A pair of unbiased dice are rolled together till a sum of either 5 or 7 is obtained. Then find the probability that 5 comes before 7 .

## - Watch Video Solution

80. For any two events $A$ and $B$, prove that
$P[(A \cap \bar{B}) \cup(B \cap \bar{A})]=P(A)+P(B)-2 P(A \cap B)$.

## - Watch Video Solution

81. If $P(B)=\frac{1}{4}, p(\bar{A} \cap B \cap \bar{C})=\frac{1}{3}, P(A \cap B \cap \bar{C})=\frac{1}{3}$, Then $P(B \cap C)$ is
A. $1 / 12$
B. $3 / 4$
C. $5 / 12$
D. $23 / / 36^{\prime}$

## Answer: A

## - Watch Video Solution

82. If the events A and B are independent, then $P(A \cap B)$ is equal to
A. $P(A)+P(B)$
B. $P(A) P(B)$
C. $P(A / B)$
D. $P(B / A)$

## Answer: B

83. If A and B are mutually exclusive events, then $P(A \cap B)$ equals
A. 0
B. $\frac{1}{2}$
C. 1
D. $\frac{1}{4}$

## Answer: A

## - Watch Video Solution

84. If A and B are suchg that events that $P(A)>0$ and $P(B) \neq 1$, then
$P\left(A^{\prime} / B^{\prime}\right)$ equals to
A. $1-P(A / B)$
B. $1-P(\bar{A} / B)$
c. $\frac{1-P(A \cup B)}{P(\bar{B})}$
D. $\frac{P(\bar{A})}{P(\bar{B})}$

## Answer: C

## - Watch Video Solution

85. $P(A$ cup $B)=P(A \text { cap } B)^{\prime}$ if and only if the relation between $P(A)$ and $P(B)$ is $\qquad$

## - Watch Video Solution

86. If $A$ and $B$ are arbitrary events, then
A. $P(A \cap B) \geq P(A)+P(B)-1$
B. $P(A \cap B) \leq P(A)+P(B)-1$
C. $P(A \cap B)=P(A)+P(B)-1$
D. none

## D Watch Video Solution

87. If A and B are arbitrary events, then a) $P(A \cap B) \geq P(A)+P(B)$ (b) $P(A \cup B) \leq P(A)+P(B)$ (c) $P(A \cap B)=P(A)+P(B)$ (d) None of these
A. $P(A \cap B) \geq P(A)+P(B)$
B. $P(A \cap B) \leq P(A)+P(B)$
C. $P(A \cap B)=P(A)+P(B)$
D. none

## Answer: B

## - Watch Video Solution

88. For two given event A and $\mathrm{B}, P(A \cap B)$ is
A. not less than $P(A)+P(B)-1$
B. not greater than $P(A)+P(B)$
C. equal to $P(A)+P(B)-P(A \cup B)$
D. equal to $P(A)+P(B)+P(A \cup B)$

## Answer: A::B::C

## - Watch Video Solution

89. If $M$ and $N$ are any two events, the probability that the exactly one of them occurs is
A. $P(M)+P(N)-2 P(M \cap N)$
B. $P(M)+P(N)-P(M \cap N)$
C. $P\left(M^{C}\right)+P\left(N^{C}\right)-2 P\left(M^{C} \cap N^{C}\right)$
D. $P\left(M \cap N^{C}\right)+P\left(M^{C} \cap N\right)$
90. If $E$ and $F$ are independent events such that $0<P(E)<1$ and $0<P(F)<1$, then
A. E and F are mutually exclusive
B. E and $F^{C}$ (complement of the event F ) are independent
C. $E^{C}$ and $F^{C}$ are independent
D. $P(E / F)+P\left(E^{C} / F\right)=1$

## Answer: B::C::D

## - Watch Video Solution

91. E and F are two independent events. The probability that both $e$ and $F$ happen is $1 / 12$ and the probability that neither $E$ nor $F$ happens is $1 / 2$. Then
A. $P(E)=\frac{1}{3}, P(F)=\frac{1}{4}$
B. $P(E)=\frac{1}{2}, P(F)=\frac{1}{6}$
C. $P(E)=\frac{1}{6}, P(F)=\frac{1}{2}$
D. $P(E)=\frac{1}{4}, P(F)=\frac{1}{3}$

## Answer: A::D

## - Watch Video Solution

92. If A and B are mutually exclusive events, then $P(A \cup B)=$
A. $P(A)+P(B)$
B. $P(A)-P(B)$
C. $P(A) \cdot P(B)$
D. $P(A) / P(B)$

## Answer: A

93. If $A$ and $B$ are two independent events in a sample space then $P(\bar{A} / \bar{B})$ equals
A. $1-P(A / \bar{B})$
B. $1-P(\bar{A} / B)$
C. $1-P(B)$
D. $1-P(A)$

## Answer: D

## - Watch Video Solution

94. For any two events $A$ and $B$ in a sample space
A. $P(A / B) \geq \frac{P(A)+P(B)-1}{P(B)}, P(B) \neq 0$ is always true.
B. $P(A \cap \bar{B})=P(A)-P(A \cap B)$ does not hold
C. $P(A \cup B)=1-P(\bar{A}) P(\bar{B})$, if A and B are independent
D. $P(A \cup B)=1-P(\bar{A}) P(\bar{B})$, if A and B are disjoint.

## Answer: A:C

## - Watch Video Solution

95. The probabilities of three mutually exclusive events $A, B, C$ are :
$P(A)=2 / 3, P(B)=1 / 4, P(C)=1 / 6$. Is the statement
A. 1
B. wrong
C. could be either
D. do not know

Answer: B

## - Watch Video Solution

96. The probability that at least one of the events $A$ and $B$ occurs is 0.7 and they occur simultaneously with probability 0.2 . Then, $P(\bar{A})+P(\bar{B})=$
A. $0 \cdot 4$
B. $0 \cdot 8$
C. $1 \cdot 2$
D. $1 \cdot 4$

## Answer: C

## - Watch Video Solution

97. If $0<P(A)<1,0<P(B)<1$ and
$P(A \cup B)=P(A)+P(B)-P(A) P(B)$, then
A. $P(B / A)=P(B)-P(A)$
B. $P\left(A^{C}-B^{C}\right)=P\left(A^{C}\right)-P\left(B^{C}\right)$
C. $P(A \cup B)^{C}=P\left(A^{C}\right) \cdot P\left(B^{C}\right)$
D. $P(A / B)=P(A)$

## Answer: C::D

## - Watch Video Solution

98. For the three events
$\mathrm{A}, \mathrm{B}$, andC, $\mathrm{P}(\mathrm{exactl}$ yon eoftheeventsAorBoccurs $)=\mathrm{P}(\mathrm{ex}$ ac $=\mathrm{p}$
and
$P($ allthethreeeventsoccursimultaneously $)=p^{2}$, where 0 Then, find the probability of occurrence of at least one of the three events $A, B$, and $C$.
A. $\frac{3 p+2 p^{2}}{2}$
B. $\frac{p+3 p^{2}}{4}$
c. $\frac{p+3 p^{2}}{2}$
D. $\frac{3 p+2 p^{2}}{4}$

## Answer: A

## - Watch Video Solution

99. For a biased die, the probabilities for the different faces to turn up are given by the table

| Face | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Probability | 0.1 | 0.32 | 0.21 | 0.15 | 0.05 | 0.17 |

The die is thrown and you are told that either the face 1 or the face 2 has turned up, then the probability that it is face 1 , is

## D Watch Video Solution

100. A biased die is tossed and the respective probabilities for various faces to turn up are

| Face | $:$ | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Probability | $:$ | 0.1 | 0.24 | 0.19 | 0.18 | 0.15 | 0.14 |

If an even face has turned up, then the probability that it is face 2 or face

4 , is
A. $0 \cdot 25$
B. $0 \cdot 42$
C. $0 \cdot 75$
D. $0 \cdot 9$

## Answer:

## - Watch Video Solution

101. Three identical dice are rolled. The probability that same number appears on them, is
A. $1 / 6$
B. $1 / 36$
C. $1 / 18$
D. $3 / 28$

## Answer: B

102. A letter is known to have come either from LONDON or CLIFTON, on the postmark only the two consecutive letters ON are eligible. The probability that it come from LONDON is

## - Watch Video Solution

103. A card from a pack 52 cards is lost. From the remaining cards , two cards are drawn and are found to be speades. Find the probability that missing card is also a spade.

## - Watch Video Solution

104. The probability that in the toss of two dice we obtain an even sum or a sum less than 5 is
A. $1 / 2$
B. $\frac{1}{6}$
C. $\frac{2}{3}$
D. $\frac{5}{9}$

## Answer: D

## D Watch Video Solution

105. A determinant is chosen at random from the set of all determinants of order two with elements 0 or 1 only. Probability that the determinant chosen has positive value is

## - Watch Video Solution

106. An experiment has 10 equally likely outcomes. Let $A$ and $B$ be two non-empty events of the experiment. If a consists of 4 outcomes, the number of outcomes that $B$ must have so that $A$ and $B$ are independent, is
A. 2,4 or 8
B. 3,6 or 9
C. 4 or 8
D. 5 or 10

## Answer: D

## - Watch Video Solution

107. One ticket is selected at ransom form 50 tickets numbered $00,01,02, \ldots, 49$. Then the probability that the sum of the digits on the selected ticket is 8 , given that the product of these digits is zero, is
A. $\frac{1}{50}$
B. $\frac{1}{14}$
C. $\frac{1}{7}$
D. $\frac{5}{14}$

## - Watch Video Solution

108. In a binomial distribution $B\left(n, p=\frac{1}{4}\right)$, if the probability of at least one success is greater than or equal to $\frac{9}{10}$, then n is greater than
(1) $\frac{1}{(\log )_{10}^{4}-(\log )_{10}^{3}}$
(2)
1
(3)
9
$\overline{(\log )_{10}^{4}-(\log )_{10}^{3}}$
A. $\frac{4}{\log _{10} 4-\log _{10} 3}$
B. $\frac{1}{\log _{10} 4-\log _{10} 3}$
C. $\frac{1}{\log _{10} 4+\log _{10} 3}$
D. $\frac{9}{\log _{10} 4-\log _{10} 3}$

## Answer: B

## - Watch Video Solution

109. Four fair dice $D_{1}, D_{2}, D_{2}$ and $D_{4}$ each having six faces numbered 1, $2,3,4,5$ and 6 are rolled simultaneously. The probability that shows a number appearing on one of $D_{1}, D_{2}$ and $D_{2}$ is:
A. $\frac{91}{216}$
B. $\frac{108}{216}$
C. $\frac{125}{216}$
D. $\frac{127}{216}$

## Answer: A

## - Watch Video Solution

110. An urn contains nine balls of which three are red, four are blue and two are green. Three balls are drawn at random without replacement from the urn. The probability that the three balls have different colour, is
A. $\frac{1}{3}$
B. $\frac{2}{7}$
C. $\frac{1}{21}$
D. $\frac{2}{23}$

## Answer: B

## D Watch Video Solution

111. Three numbers are chosen at random without replacement from $\{1,2$,

3, ...... 8\}. The probability that their minimum is 3 , given that their
maximum is 6 , is (1) $\frac{3}{8}$ (2) $\frac{1}{5}$ (3) $\frac{1}{4}$ (4) $\frac{2}{5}$
A. $\frac{3}{8}$
B. $\frac{1}{5}$
C. $\frac{1}{4}$
D. $\frac{2}{5}$

## Answer: B

112. A single which can can be green or red with probability $\frac{4}{5}$ and $\frac{1}{5}$ respectively, is received by station A and then transmitted to station B. The probability of each station reciving the signal correctly is $\frac{3}{4}$. If the singal received at station $B$ is green, then the probability that original singal was green is
A. $\frac{3}{5}$
B. $\frac{6}{7}$
C. $\frac{20}{23}$
D. $\frac{9}{20}$

## Answer: C

## - Watch Video Solution

113. Consider 5 independent Bernoulli.s trials each with probability of success $p$. If the probability of at least one failure is greater than or equal to $\frac{31}{32}$, then p lies in the interval : (1) $\left(\frac{1}{2}, \frac{3}{4}\right]$ (2) $\left(\frac{3}{4}, \frac{11}{12}\right]$ (3) $\left[0, \frac{1}{2}\right]$
(4) $\left(\frac{11}{12}, 1\right]$
A. $\left(\frac{1}{2}, \frac{3}{4}\right)$
B. $\left(\frac{3}{4}, \frac{11}{12}\right)$
C. $\left(0, \frac{1}{2}\right)$
D. $\left(\frac{11}{12}, 1\right)$

## Answer: C

## - Watch Video Solution

114. Let $\omega$ be a complex cube root unity with $\omega \neq 1$. A fair die is thrown three times. If $r_{1}, r_{2} a n d r_{3}$ are the numbers obtained on the die, then the probability that $\omega^{r 1}+\omega^{r 2}+\omega^{r 3}=0$ is $1 / 18$ b. $1 / 9$ c. $2 / 9$ d. $1 / 36$
A. $\frac{1}{18}$
B. $\frac{1}{9}$
C. $\frac{2}{9}$
D. $\frac{1}{36}$

## Answer: C

## - Watch Video Solution

115. Let E and F be two independent events. The probability that exactly one of them occurs is $11 / 25$ and the probability of none of them occurring is $2 / 25$. If $\mathrm{P}(\mathrm{T})$ denotes the probability of occurrence of the event $T$, then
A. $P(E)=\frac{4}{5}, P(E)=\frac{3}{5}$
B. $P(E)=\frac{1}{5}, P(F)=\frac{2}{5}$
C. $P(E)=\frac{2}{5}, P(F)=\frac{1}{5}$
D. $P(E)=\frac{3}{5}, P(F)=\frac{4}{5}$

## - Watch Video Solution

116. A ship is fitted with three engines $E_{1}, E_{2}$, and $E_{3}$ the engines function independently of each othe with respectively probability $1 / 2,1 / 4$, and $1 / 4$. For the ship to be operational at least two of its engines must function. Let $X$ denote the event that the ship is operational and let $X_{1}, X_{2}$, and $X_{3}$ denote, respectively, the events that the engines $E_{1}, E_{2}$, and $E_{3}$ are functioning. Which of the following is (are) true?
A. $P\left[X_{1}^{C} \mid X\right]=\frac{3}{16}$
B. $P$ [Exactly two engines of the ship are functioning $\mid X]=\frac{7}{8}$
C. $P\left[X \mid X_{2}\right]=\frac{5}{16}$
D. $P\left[X \mid X_{1}\right]=\frac{7}{16}$
117. If X and Y are two events such that $P X / Y)=\frac{1}{2}, P(Y / X)=\frac{1}{3}$ and $P(X \cap Y) \frac{1}{6}$. Then, which of the following is/are correct ?
A. $P(X \cup Y)=\frac{2}{3}$
B. $X$ and $Y$ are independent
C. $X$ and $Y$ are not independent
D. $P\left(X^{\prime} \cap Y\right)=\frac{1}{3}$

## Answer: A: B

## - Watch Video Solution

118. Let $U_{1}$, and $U_{2}$, be two urns such that $U_{1}$, contains 3 white and 2 red balls, and $U_{2}$, contains only 1 white ball. A fair coin is tossed. If head appears then 1 ball is drawn at random from $U_{1}$, and put into $U_{2}$, . However, if tail appears then 2 balls are drawn at random from $U_{1}$, and
put into $U_{2}$. . Now 1 ball is drawn at random from $U_{2}$, .61. The probability of the drawn ball from $U_{2}$, being white is
A. $\frac{13}{30}$
B. $\frac{23}{30}$
C. $\frac{19}{30}$
D. $\frac{11}{30}$

## Answer: B

## - Watch Video Solution

119. Given that the drawn ball from $U 2$ is white, the probability that head appeared on the coin
A. $\frac{17}{23}$
B. $\frac{11}{23}$
C. $\frac{15}{23}$
D. $\frac{12}{23}$

## Answer: D

## - Watch Video Solution

120. A fair die is tossed repeatedly until a 6 is obtained. Let $X$ denote the number of tosses required.

The probability that $X=3$ equals
A. $\frac{25}{216}$
B. $\frac{25}{36}$
C. $\frac{5}{36}$
D. $\frac{125}{216}$

## Answer: A

## - Watch Video Solution

121. A fair die is tossed repeated until a six is obtained. Let $X$ denote the number of tosses required.

The probability that $X \geq 3$ is
A. $\frac{125}{216}$
B. $\frac{25}{36}$
C. $\frac{5}{36}$
D. $\frac{25}{216}$

## Answer: B

## - Watch Video Solution

122. A fair die is tossed repeatedly until a six obtained. Let $X$ denote the number of tosses required.

The conditional probability that $X \geq 6$ given $X>3$ equals
A. $\frac{125}{216}$
B. $\frac{25}{216}$
C. $\frac{5}{36}$
D. $\frac{25}{36}$

## Answer: D

## - Watch Video Solution

## Miscellaneous Exercise Comprehension

1. One Indian and four American men and their wives are to be seated randomly around a circular table. Then, the conditional probability that Indian man is seated adjacent to his wife given that each American man is seated adjacent to his wife, is :
A. $1 / 2$
B. $1 / 3$
C. $2 / 5$
D. $1 / 5$

## Answer: C

## - Watch Video Solution

## Miscellaneous Exercise Assertion Reason

1. Let $H_{1}, H_{2}, \ldots, H_{n}$ be mutually exclusive events with $P\left(H_{i}\right)>0, i=1,2, \ldots \ldots \ldots . n$. Let $E$ be any other event with $0<P(E)$ Statement $\quad$ I $P\left(H_{i} \mid E\right)>P\left(E \mid H_{i} . P\left(H_{i}\right) \quad\right.$ for $\quad i=1,2, \ldots \ldots, n$ statement II $\sum_{i=1}^{n} P\left(H_{i}\right)=1$

## - Watch Video Solution

## Miscellaneous Exercise

1. Let $E^{\circ}$ denotes the complement of an event E . If $\mathrm{E}, \mathrm{F}, \mathrm{G}$ are pairwise independent events with $P(G)>0$ and $P(E \cap F \cap G)=0$. Then, $P\left(E^{\circ} \cap F^{\circ} \mid G\right)$ equals :
A. $P\left(E^{C}\right)+P\left(F^{C}\right)$
B. $P\left(E^{C}\right)-P\left(F^{C}\right)$
C. $P\left(E^{C}\right)-P(F)$
D. $P(E)-P\left(F^{C}\right)$

## Answer: C

## - Watch Video Solution

2. There are n urns each continuous $(\mathrm{n}+1)$ balls such that the ithurn contains 'I' white balls and ( $\mathrm{n}+1-\mathrm{i}$ ) red balls. Let $u_{1}$ be the event of selecting ith urn, $i=1,2,3 . . . . . . . n$ and $W$ denotes the event of getting a white balls.

If n is even and E dentes the event of choosing even numbered urn $\left[P\left(u_{i}\right)=\frac{1}{n}\right]$, then the value of $P(W / E)$ is
3. If $\left.P\left(u_{i}\right)\right) \infty i$, where $i=1,2,3, \ldots, n$ then $\lim _{n \rightarrow w} P(w)$ is equal to
A. $\frac{2}{3}$
B. $\frac{1}{3}$
C. $\frac{1}{2}$
D. $\frac{3}{4}$

## Answer: A

## - Watch Video Solution

4. If $P\left(U_{i}\right)=C$ (constant), then $P\left(\frac{U_{n}}{W}\right)$, where n is even :
A. $\frac{1}{2}$
B. $\frac{n}{n+1}$
C. $\frac{n+2}{2(n+1)}$
D. $\left(\frac{n+1}{n+2}\right)$

## Answer: C

## D View Text Solution

5. $P\left(U_{i}\right)=\frac{1}{n}$, and one urn is selected at random, then $\mathrm{P}(\mathrm{W})$ is:
A. $\frac{1}{2}$
B. $\frac{1}{n}$
C. $\frac{n}{n+1}$
D. $\frac{n+1}{n+2}$

## Answer: A

## - View Text Solution

6. Probabilities of Ramesh using car, scooter, bus and train are 1/7, 2/7, 3/7 and $1 / 7$ respectively. Probabilities of him reaching office late with these
vehicles are $2 / 9,4 / 9,1 / 9$ and $1 / 9$ respectively. If he reaches office on time, find the probability that he went by car.

## - Watch Video Solution

