

MATHS

BOOKS - ARIHANT MATHS

DIFFERENTIATION

Examples

1. Differentiate the following functions w.r.t x using first principle.

$$f(x) = \tan x$$



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2. Differentiate the following functions w.r.t x using first principle.

$$e^{x^2}$$



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3. Differentiate the following functions w.r.t x using first principle.

$$\sqrt{\sin x}$$



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4. If $y = \sin x + e^x$, Then find $\frac{dy}{dx}$.



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5. If $y = x^2 + \sin^{-1} x + \log_e x$, then find $\frac{dy}{dx}$



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6. If $y = \log_{10} x + \log_e x + \log_{10} 10$, then find $\frac{dy}{dx}$



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7. If $y = x^{-1/2} + \log_5 x + \frac{\sin x}{\cos x} + 2^x$, then find $\frac{dy}{dx}$



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8. If $y = m^2 \sec^{-1} x$, then find $\frac{dy}{dx}$.



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9. If $y = \log_e x^3 + 3 \sin^{-1} x + kx^2$, then find $\frac{dy}{dx}$



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10. If $y = e^x \sin x$, then find $\frac{dy}{dx}$



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11. If $y = e^x \tan x + x \cdot \log_e x$, then find $\frac{dy}{dx}$



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12. Let f, g and h be differentiable function. If $f(0) = 1, g(0) = 2, h(0) = 3$ and the derivatives of their pair wise products at $x = 0$ are $(fg)'(0) = 6, (gh)'(0) = 4$ and $(hf)'(0) = 5$ then the value of $\frac{(fg)'(0)}{2}$ is



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13. If $y = (1 + x)(1 + x^2)(1 + x^4)(1 + x^{2n})$, then find $\frac{dy}{dx}$ at $x = 0$.



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14. If $y = \frac{x}{x^2 + 1}$, then find $\frac{dy}{dx}$



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15. If $y = \frac{x \sin x}{\log_e x}$, then find $\frac{dy}{dx}$



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16. If $y = \frac{3a^2x - x^3}{a^3 - 3ax^2}$ then find $\frac{dy}{dx}$



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17. If $y = \frac{e^x - \tan x}{x^n + \cot x}$, then find $\frac{dy}{dx}$



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18. If $y = \frac{\log_e x}{x} + e^x \sin x + \log_5 x$ then find $\frac{dy}{dx}$.



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19. If $y = \frac{x^4 + x^2 + 1}{x^2 + x + 1}$ then $\frac{dy}{dx} = ax + b$, find a and b



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20. Let $y = \frac{\sec x + \tan x - 1}{\tan x - \sec x + 1}$. If $\left(\frac{dy}{dx}\right)_{x=\frac{\pi}{4}} = a + \sqrt{b}$, then value of $a + b$ is equal to



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21. If $y = \frac{\tan^{-1} x - \cot^{-1} x}{\tan^{-1} x + \cot^{-1} x}$, find $\left(\frac{dy}{dx}\right)_{x=-1}$ 0 (b) 1 (c) $2/\pi$ (d) -1



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22. If $y = e^{(\tan^{-1} x)}$ then find $\frac{dy}{dx}$



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23. $y = \log_e \left(\tan^{-1} \sqrt{1+x^2} \right)$ then $\frac{dy}{dx}$ is



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24. Find $\frac{dy}{dx}$, when $y = e^{ax} \cos(bx + c)$



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25. Differentiate the following w. r. t. x. (i) $\sqrt{\log\left\{\sin\left(\frac{x^2}{3} - 1\right)\right\}}$ (ii)
 $\log_e\left(\frac{x + \sqrt{x^2 - a^2}}{x - \sqrt{x^2 - a^2}}\right)$



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26. If $y = x \cos y + y \cos x$, then find $\frac{dy}{dx}$



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27. If $y\sqrt{1 - x^2} + x\sqrt{1 - y^2} = 1$, then $\frac{dy}{dx} =$



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28. If $\sqrt{1 - x^6} + \sqrt{1 - y^6} = a^3(x^3 - y^3)$ prove that
$$\frac{dy}{dx} = \frac{x^2\sqrt{1 - y^6}}{y^2\sqrt{1 - x^6}}$$

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29. Let $y = \sqrt{x + \sqrt{x + \sqrt{x + \dots \infty}}}$, then $\frac{dy}{dx}$ is equal to

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30. If $y = \sec^{-1}\left(\sqrt{1 + x^2}\right)$, when $-1 < x < 1$, then find $\frac{dy}{dx}$

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31. $y = \tan^{-1}\sqrt{\frac{1-x}{1+x}}$ find $\frac{dy}{dx}$

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32. Prove that $\tan^{-1}\left(\sqrt{\frac{1-\cos x}{1+\cos x}}\right) = \frac{x}{2}$, $x < \pi$.



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33. If $y = \tan^{-1}\left(\frac{\sqrt{1+x^2}-1}{x}\right)$, then find $\frac{dy}{dx}$.



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34. Differentiate the following functions with respect to x :

(i) $\tan^{-1}\left(\frac{a+x}{1-ax}\right)$ (ii) $\tan^{-1}\left(\frac{a \cos x - b \sin x}{b \cos x + a \sin x}\right)$



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35. if $y = \sin^{-1}\left(\frac{5x+12\sqrt{1-x^2}}{13}\right)$ then find $\frac{dy}{dx}$



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36. Find $\frac{dy}{dx}$ for $y = \tan^{-1} \sqrt{\frac{a-x}{a+x}}$, $-a < x < a$



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37. Sketch the graph for $y = \sin^{-1}(\sin x)$.



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38. Sketch the graph for $y = \cos^{-1}(\cos x)$.



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39. Sketch the graphs for $y = \sin(\sin^{-1} x)$



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40. Sketch the graphs for $y = \cos(\cos^{-1} x)$



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41. Sketch the graphs for $y = \tan(\tan^{-1} x)$



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42. Draw the graph of $y = \operatorname{cosec}(\operatorname{cosec}^{-1} x)$ or $y = \sec(\sec^{-1} x)$.



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43. Sketch the graphs for $y = \sec(\sec^{-1} x)$



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44. Sketch the graphs for $y = \cot(\cot^{-1} x)$ and hence find $\frac{dy}{dx}$



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45. If $x = e^{-t^2}$, $y = \tan^{-1}(2t + 1)$, then $\frac{dy}{dx} =$



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46. Find $\frac{dy}{dx}$ if $x = a(\theta - \sin \theta)$ and $y = a(1 - \cos \theta)$.



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47. Find $\frac{dy}{dx} = -\frac{y}{x}$ if $x = \sqrt{a^{\sin^{-1} t}}$, $y = \sqrt{a^{\cos^{-1} t}}$



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48. If $x = a \left(\cos t + \frac{1}{2} \log \tan^2 t \right)$ and $y = a \sin t$ then find $\frac{dy}{dx}$ at $t = \frac{\pi}{4}$



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49. If $y = x^{\sin x}$, then find $\frac{dy}{dx}$



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50. $x^y \cdot y^x = 1$. Find $\frac{dy}{dx}$



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51. If $(\tan^{-1} x)^y + y^{\cot x} = 1$, then find $\frac{dy}{dx}$.



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52. If $f(x) = \prod_{n=1}^{100} (x - n)^{n(101-n)}$ then find $\frac{f(101)}{f, (101)}$



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53. If $y = \sqrt{\log x + \sqrt{\log x + \sqrt{\log x + \dots \infty}}}$, then $\frac{dy}{dx}$ is



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54. Differentiate $\sin^{-1}\left(\frac{2x}{1+x^2}\right)$



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55. Differentiate $\tan^{-1}\left(\frac{\sqrt{1-x^2}}{x}\right)$ w.r.t. $\cos^{-1}\left(2x\sqrt{1-x^2}\right)$



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56. Find the derivative of $\sec^{-1}\left(\frac{1}{2x^2-1}\right)$ w.r.t. $\sqrt{1-x^2}$ at $x = \frac{1}{2}$.



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57. If $y = f(x^3)$, $z = g(x^5)$, $f'(x) = \tan x$, and $g'(x) = \sec x$, then find the value of

$$\lim_{x \rightarrow 0} \frac{(dy/dz)}{x}$$



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58. Find the derivative of $f(\tan x)$ w.r.t. $g(\sec x)$ at $x = \frac{\pi}{4}$, where $f'(1)=2$ and $g'(\sqrt{2}) = 4$.



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59. If $y = x^3 \log_e x$, then find y'' and y''' .



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60. If $y = \sin(\sin x)$, prove that $\frac{d^2y}{dx^2} + \tan x \frac{dy}{dx} + y \cos^2 x = 0$.



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61. If $x = a(t - \sin t)$ and $y = (1 - \cos t)$, then find $\frac{d^2y}{dx^2}$.



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62. If $f(x) = \begin{bmatrix} x & x^2 & x^3 \\ 1 & 2x & 3x^2 \\ 0 & 2 & 6x \end{bmatrix}$ find $f'(x)$



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63. $\begin{vmatrix} x^2 + a^2 & ab & ac \\ ab & x^2 + b^2 & bc \\ ac & bc & x^2 + c^2 \end{vmatrix} =$



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64. Let $f(x) = \begin{vmatrix} x^3 & \sin x & \cos x \\ 6 & -1 & 0 \\ p & p^2 & p^3 \end{vmatrix}$ where p is a constant. Then $\frac{d^3}{dx^3}\{f(x)\}$ at

$x=0$ is



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65. If $y = \sin mx$ the value of the determinant

$$\begin{vmatrix} y & y_1 & y_2 \\ y_3 & y_4 & y_5 \\ y_6 & y_7 & y_{98} \end{vmatrix} \quad \text{where}$$

$y_n = \frac{d^n y}{dx^n}$ is



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66. If $f(x) = \begin{vmatrix} (1+x)^a & (1+2x)^b & 1 \\ 1 & (1+x)^a & (1+2x)^b \\ (1+2x)^b & 1 & (1+x)^a \end{vmatrix}$ then find constant term and coefficient of x



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67. Find the solution of differential Equation

$$2xy \frac{dy}{dx} = x^2 + 3y^2$$



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68. If $y = f(x) = x^3 + x^5$ and g is the inverse of f find $g'(2)$



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69. Let $f(x) = \exp(x^3 + x^2 + x)$ for any real number and let $g(x)$ be the inverse function of $f(x)$ then $g'(e^3)$

A. $\frac{1}{6e^3}$

B. $\frac{1}{6}$

C. $\frac{1}{34e^{19}}$

D. 6

Answer:



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70. Let f be twice differentiable function, such that $f'(x) = -f(x)$ and $f'(x) = g(x)$, $h(x) = [f(x)]^2 + [g(x)]^2$. Find

$h(10)$, if $h(5) = 11$

- A. 0
- B. 9
- C. 11
- D. None of these

Answer:



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71. if $y = \frac{(a-x)\sqrt{a-x} - (b-x)\sqrt{x-b}}{\sqrt{a-x} + \sqrt{x-b}}$, then $\frac{dy}{dx}$ wherever it

is defined is

- A. $\frac{x - (a - b)}{\sqrt{(a - x)(x - b)}}$
- B. $\frac{2x + (a + b)}{\sqrt{(a - x)(x - b)}}$
- C. $\frac{2x - (a + b)}{2} \left(\sqrt{(a - x)(x - b)} \right)$
- D. None of these

Answer:



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72. If $x^2 + y^2 = R^2$ (where $R > 0$) and $k = \frac{y''}{(1+y^2)^3}$ then find k in terms of R alone.

A. $\frac{1}{R}$

B. $-\frac{1}{R}$

C. R

D. $\frac{1}{2R}$

Answer:



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73. Let $f(x) = x + \sin x$. Suppose g denotes the inverse function of f .

The value of $g' \left(\frac{\pi}{4} + \frac{1}{\sqrt{2}} \right)$ has the value equal to

A. (a) $2 + \sqrt{2}$

B. (b) $\sqrt{2} - 2$

C. (c) $2 - \sqrt{2}$

D. (d) $2\sqrt{2}$

Answer:



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74. If $e^{f(x)} = \log x$ and $g(x)$ is the inverse function of $f(x)$, then $g'(x)$ is

A. e^{e^x}

B. e^x

C. $e^{e^x + x}$

D. None of these

Answer:



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75. Given: $f(x) = 4x^3 - 6x^2 \cos 2a + 3x \sin 2a \sin 6a + \sqrt{\ln(2a - a^2)}$

then

A. $af' \left(\frac{1}{2} \right) < 0$

B. $af' \left(\frac{1}{2} \right) \leq 0$

C. $af' \left(\frac{1}{2} \right) > 0$

D. None of these

Answer:



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76. Suppose $f(x) = e^{ax} + e^{bx}$, where $a \neq b$, and that $f''(x)$

$-2f'(x) - 15f(x) = 0$ for all x . Then the product ab is

A. 15

B. -15

C. 10

D. 16

Answer:



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77. Which of the following is not true $\log(1 + x) < x$ for $x > 0$

A. $e^y = xy' + 1$

B. $y' = -\frac{1}{(x-1)}$

C. $y' + e^y = 0$

D. $y' = e^y$

Answer:



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78. If $x^p y^q = (x + y)^{(p+q)}$ then $\frac{dy}{dx} = ?$

- A. independent of p
- B. independent of q
- C. dependent both p and q
- D. $\frac{y}{x}$

Answer:



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79. Two functions f & g have first & second derivatives at $x=0$ & satisfy the relations,

$$f(0) = \frac{2}{g(0)}, f'(0) = 2g'(0) = 4g(0), g(0)=5 \text{ } f(0) = 6 \text{ } f(0) = 3 \text{ then-}$$

A. If $h(x) = \frac{f(x)}{g(x)}$, then $h'(0) = 15$

B. If $k(x) = f(x) \cdot g(x) \cdot \sin x$ then $k'(0)d = 2$

C. $\lim_{x \rightarrow 0} \frac{g'(x)}{f'(x)} = \frac{1}{2}$

D. None of above

Answer:



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80. $f(x) = |x^2 - 3x|x| + 2|$. Then which of the following is/are true ?

A. $f'(x) = 2x - 3$ for $x \in (0, 1) \cup (2, \infty)$

B. $f'(x) = 2x + 3$ for $x \in (-\infty, -2) \cup (-10)$

C. $f'(x) = -2x - 3$ for $x \in (-2, -1)$

D. None of the above

Answer:



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81. Consider $f(x) = \frac{x}{x^2 - 1}$ and $g(x) = f''(x)$ Statement I Graph of $g(x)$ is concave up for $x > 1$. Statement II

$$\frac{d^n}{dx^n} f(x) = \frac{(-1)^n n!}{2} \left\{ \frac{1}{(x-1)^{n+1}} + \frac{1}{(x+1)^{n+1}} \right\} n \in N$$

- A. Both statement I and Statement II are correct and Statement II is the correct explanation of Statement I
- B. Both Statement I and Statement II are correct but Statement II is not the correct explanation of Statement I
- C. Statement I is correct but Statement II is incorrect
- D. Statement II is correct but Statement I is correct.

Answer:



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82. Statement 1: If differentiable function $f(x)$ satisfies the relation

$$f(x) + f(x - 2) = 0 \quad \forall x \in R, \quad \text{and} \quad \text{if}$$

$$\left(\frac{d}{dx} f(x) \right)_{x=a} = b, \text{ then } \left(\frac{d}{dx} f(x) \right)_{x=a+4000} = b. \text{ Statement 2: } f(x) \text{ is}$$

a periodic function with period 4.

A. Both statement I and Statement II are correct and Statement II is

the correct explanation of Statement I

B. Both Statement I and Statement II are correct but Statement II is

not the correct explanation of Statement I

C. Statement I is correct but Statement II is incorrect

D. Statement II is correct but Statement I is correct.

Answer:



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83. Let $f(x) = x[x]$, where $[*]$ denotes the greatest integer function, when x is not an integer then find the value of $f'(x)$



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84. $f(x)$ is a polynomial of degree

A. 2

B. 3

C. 4

D. 5

Answer:



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85. The moment when A is at $(0, 0)$ and B is at $(1, 2)$. The derivative $\frac{dy}{dx}$ of line AB is

A. $\frac{1}{9}$

B. $\frac{1}{7}$

C. $\frac{1}{5}$

D. None of these

Answer:



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86. The moment when A is at $(1, 2)$ and B is at $(0, 0)$. The derivative $\frac{dx_B}{dx_A}$, is

A. 16

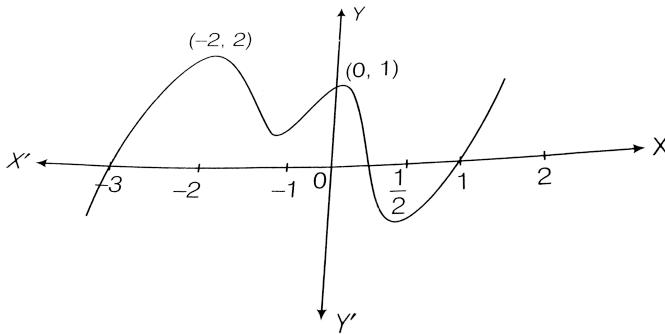
B. 8

C. 9

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87. In the given figure graph of

$y = P(x) = ax^5 + bx^4 + cx^3 + dx^2 + ex + f$, is given.



If $P''(x)$ has real roots α, β, γ , then $[\alpha] + [\beta] + [\gamma]$, is

A. -2

B. -3

C. -1

D. 0

Answer: -2



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88. Match the Column I with Column II and mark the correct option from the given below.

| | Column I | Column II |
|-------|--|------------------|
| | If $f'(x) = \sqrt{3x^2 + 6}$ and $y = f(x^3)$ then at | p. - 2 |
| (i) | $x = 1$, $\frac{dy}{dx}$ is | |
| (ii) | If f is a differentiable function such that $f(xy) = f(x) + f(y)$: $x, y \in R$, then $f(e) + f(1/e)$ is | q. - 1 |
| (iii) | If f is a twice differentiable function such that $f''(x) = -f(x)$ and $f'(x) = g(x)$. If $h(x) = [f(x)]^2 + [g(x)]^2$ and $h(5) = 9$, then $h(10)$ is | r. 0 |
| | $y = \tan^{-1}(\cot x) + \cot^{-1}(\tan x)$, | s. 9 |
| (iv) | $\frac{\pi}{2} < x < \pi$, then $\frac{dy}{dx}$ is | |

- A. i ii iii iv
s r s p
- B. i ii iii iv
p q r s
- C. i ii iii iv
() q p r r
- D. i ii iii iv
s p q q

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89. Match the Column I with Column II and mark the correct option from the given below.

| | Column I | Column II |
|-------|--|------------------|
| (i) | If $y = \cos^{-1}(\cos x)$, then y' at $x = 5$ is equal to | p. -1 |
| (ii) | For the function $f(x) = \log_e \tan\left(\frac{\pi}{4} + \frac{x}{2}\right)$, if $\frac{dy}{dx} = \sec x + p$, then p is equal to | q. 0 |
| (iii) | The derivative of $\tan^{-1}\left(\frac{1+x}{1-x}\right)$ at $x = -1$ is | r. $1/2$ |
| (iv) | The derivative of $\frac{\log x }{x}$ at $x = -1$ is | s. 1 |

- A. i ii iii iv
p q r s
- B. i ii iii iv
q p r s
- C. i ii iii iv
s r q p
- D. i ii iii iv
r s p q

Answer:



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90. If $y = \sqrt{(x - \sin x) + \sqrt{x - \sin x} + \dots}$, then
 $\left| \frac{dx}{dy} \right|_{x=\frac{\pi}{2}}^2 - 2\pi = \dots \dots \dots$



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91. Let $f(x) = \int_{-2}^x e^{(1+t)^2} dt$ and $g(x) = f(h(x))$, where $h(x)$ is defined for all $x \in R$. If $g'(2) = e^4$ and $h'(2) = 1$ then absolute value of sum of all possible values of $h(2)$ is ___



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92. If $f(x) = \cos \left\{ \frac{\pi}{2}[x] - x^3 \right\}$, $1 < x < 2$ and $[x] =$ the greatest integer $\leq x$, then find $f' \left(\sqrt[3]{\frac{\pi}{2}} \right)$



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93. If $u = f(x^3)$, $v = g(x^2)$, $f'(x) = \cos x$, and $g'(x) = \sin x$, then $\frac{du}{dv}$ is (a) $\frac{3}{2}x\cos x^3 \cos ex^2$ (b) $\frac{2}{3}\sin x^3 \sec x^2$ (c) $\tan x$ (d) none of these



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94.

$$f: R \rightarrow R, f(x) = x^3 + x^2 f'(1) + x f''(2) + f'''(3) \text{ for all } x \in R.$$

The value of $f(1)$ is



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95.

Let

$$f(x) = x^2 + x g'(1) + g''(2) \text{ and } g(x) = x^2 + x f'(2) + f''(3).$$

Then

a. $f'(1) = 4 + f'(2)$

b. $g'(2) = 8 + g'(1)$

c. $g''(2) + f''(3) = 4$

d. all of these



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96. If $y = \frac{\sin x}{1 + \frac{\cos x}{1 + \frac{\sin x}{1 + \frac{\cos x}{\ddots}}}}$, prove that $\frac{dy}{dx} = \frac{(1+y)\cos x + y\sin x}{1 + 2y + \cos x - \sin x}$



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97. If $\sqrt[3]{3\left(\sqrt[3]{x} - \frac{1}{\sqrt[3]{x}}\right)} = 2$, then $\sqrt[3]{x} - \frac{1}{\sqrt[3]{x}}$



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98.

If
 $y = \tan^{-1}\left(\frac{1}{x^2 + x + 1}\right) + \tan^{-1}\left(\frac{1}{x^2 + 3x + 3}\right) + \tan^{-1}\left(\frac{1}{x^2 + 5x + 7}\right) + \dots$. to n terms, show that $\frac{dy}{dx} = \frac{1}{(x+n)^2 + 1} - \frac{1}{x^2 + 1}$



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99. if $f(\theta) = \cos \theta_1 \cdot \cos \theta_2 \cdot \cos \theta_3 \dots \cos \theta_n$, show that
 $\{\tan \theta_1 + \tan \theta_2 + \tan \theta_3 + \dots + \tan \theta_n\} = - \left\{ \frac{f'(\theta)}{f(\theta)} \right\}$,

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100. Find the sum of $\sin x + 3 \sin 3x + 5 \sin 5x + \dots + (2k-1)\sin(2k-1)x$.

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101. Find the sum of the series $\sum_{r=1}^n rx^{r-1}$ using calculus .

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102. Show that

$$\frac{1}{x+1} + \frac{2}{x^2+1} + \frac{4}{x^4+1} + \dots + \frac{2^n}{x^{2n+1}} = \frac{1}{x-1} - \frac{2^{n+1}}{x^{2^{n+1}}-1}$$



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103.

$f_n(x) = e^{f_{n-1}(x)}$ for all $n \in N$ and $f_0(x) = x$, then $\frac{d}{dx}\{f_n(x)\}$ is



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104. If $y^3 - y = 2x$, prove that $\frac{d^2y}{dx^2} = -\frac{24y}{(3y^2-1)^3}$.



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105. If $2x = y^{\frac{1}{5}} + y^{-\frac{1}{5}}$ then $(x^2 - 1) \frac{d^2y}{dx^2} + x \frac{dy}{dx} = ky$, then find the value of k.



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106.

Let

$$y = 1 + \frac{a_1}{x - a_1} + \frac{a_2 x}{(x - a_1)(x - a_2)} + \frac{a_3 x^2}{(x - a_1)(x - a_2)(x - a_3)} + \dots$$

Find $\frac{dy}{dx}$



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107. If $y = f\left(\frac{2x - 1}{x^2 + 1}\right)$ and $f'(x) = \sin x^2$, then find $\frac{dy}{dx}$



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108. let $f(x)$ be a polynomial function of second degree. If $f(1) = f(-1)$ and a_1, a_2, a_3 are in AP, then show that $f'(a_1), f'(a_2), f'(a_3)$ are in AP.



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109. If $5f(x) + 3f\left(\frac{1}{x}\right) = x + 2$ and $y = xf(x)$, then find $\frac{dy}{dx}$ at $x = 1$



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Example

1. Differentiate the following functions w.r.t x using first principle.

$$f(x) = e^{2x}$$



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2. If $(a + bx)e^{\frac{y}{x}} = x$, Prove that $x^3 \frac{d^2y}{dx^2} = \left(x \frac{dy}{dx} - y \right)^2$



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3. Show that the function $y = f(x)$ defined by the parametric equations

$x = e^t \sin(t)$, $y = e^t \cdot \cos(t)$, satisfies the relation

$$y''(x + y)^2 = 2(xy' - y)$$



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Solved Examples

1. Let $f(x)$ be a real valued function not identically zero, which satisfied the following conditions

I. $f(x + y^{2n+1}) = f(x) + (f(y))^{2n+1}$, $n \in N$, x, y are any real numbers.

II. $f'(0) \geq 0$

The value of $f'(10)$, is

A. 3, 2

B. 0, 1

C. 1, 5

D. 5, 1

Answer:



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2. Let $f\left(\frac{x+y}{2}\right) = \frac{f(x) + f(y)}{2}$ and $f(0) = b$. Find $f''(x)$ (where y is independent of x), when $f(x)$ is differentiable.

A. 0

B. 1

C. a

D. None of these

Answer:



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3. The functions $u = e^x \cdot \sin x$ and $v = e^x \cdot \cos x$ satisfy the equation

A. a) $v \frac{du}{dx} - u \frac{dv}{dx} = u^2 + v^2$

B. b) $v \frac{du}{dx} + u \frac{dv}{dx} = u^2 + v^2$

C. c) $\frac{du}{dx} + \frac{dv}{dx} = 2v$

D. d) $\frac{du}{dx} + \frac{dv}{dx} = 2u$

Answer:



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4. The leading coefficient of $f(x)$, is,



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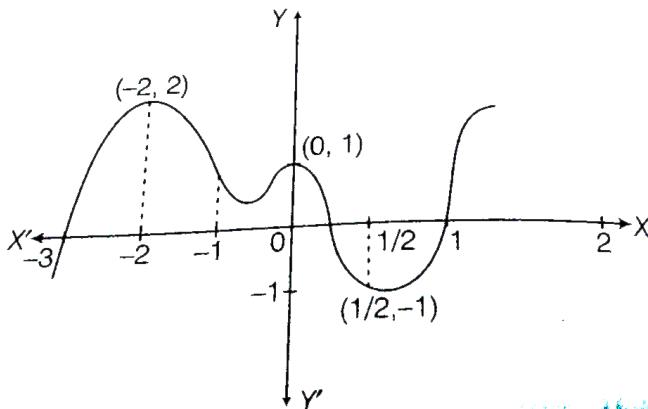
5. If $f(x) = 18x + 11$ then find the value of $f''(x)$, is



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6. The minimum number of real roots of equation

$$(p''(x))^2 + p'(x) \cdot p'''(x) = 0$$



A. 5

B. 7

C. 6

D. 4

Answer:



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7. Find a, b, c, and d, where

$f(x) = (ax + b)\cos x + (cx + d)\sin x$ and $f'(x) = x \cos x$ is identity in x.



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8. If for all x, y the function f is defined by $f(x) + f(y) + f(xy)$. $f(y) = 1$ and $f(x) > 0$. Then show $f'(x) = 0$



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Exercise More Than One Correct Option Type Questions

1. If $y = \frac{\sec x - \tan x}{\sec x + \tan x}$, then $\frac{dy}{dx}$ equals.

A. $2 \sec x(\sec x - \tan x)$

B. $-2 \sec x(\sec x - \tan x)^2$

C. $2 \sec x (\sec x - \tan x)^2$

D. $-2 \sec x (\sec x + \tan x)^2$

Answer: B



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2. If $y = \frac{x^4 + x^2 + 1}{x^2 + x + 1}$ then $\frac{dy}{dx} = ax + b$, find a and b

A. $a = 2, b = 1$

B. $a = -2, b = 1$

C. $a = 2, b = -1$

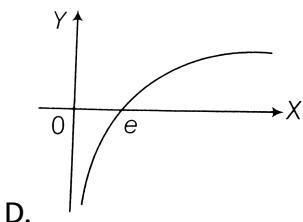
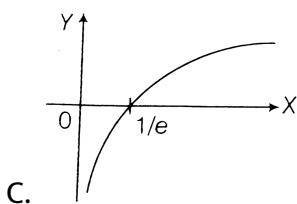
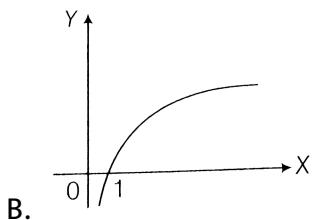
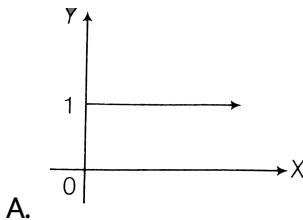
D. $a = -2, b = -1$

Answer: C



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3. Which of the following could be the sketch graph of $y = \frac{d(x \ln x)}{dx}$



Answer: C



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4. Let $f(x) = x + 3\ln(x - 2)$ & $g(x) = x + 5\ln(x - 1)$, then the set of x satisfying the inequality $f'(x) < g'(x)$ is

- A. $\left(2, \frac{7}{2}\right)$
- B. $(1, 2) \cup \left(\frac{7}{2}, \infty\right)$
- C. $(2, \infty)$
- D. $\left(\frac{7}{2}, \infty\right)$

Answer: D



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5. If $\cos^{-1} \left(\frac{x^2 - y^2}{x^2 + y^2} \right) = a$, then $\frac{dy}{dx} =$

- A. $-\frac{x}{y}$
- B. $-\frac{y}{x}$
- C. $\frac{y}{x}$
- D. $\frac{x}{y}$

Answer: C



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6. If $f(x) = |x|^{\sin x}$, then $f' \left(\frac{\pi}{4} \right)$ equals

- A. $\left(\frac{\pi}{4} \right)^{1\sqrt{2}} \cdot \left(\frac{\sqrt{2}}{2} \log \frac{4}{\pi} - \frac{2\sqrt{2}}{\pi} \right)$
- B. $\left(\frac{\pi}{4} \right)^{1\sqrt{2}} \cdot \left(\frac{\sqrt{2}}{2} \log \frac{4}{\pi} + \frac{2\sqrt{2}}{\pi} \right)$
- C. $\left(\frac{\pi}{4} \right)^{1\sqrt{2}} \cdot \left(\frac{\sqrt{2}}{2} \log \frac{4}{\pi} - \frac{2\sqrt{2}}{\pi} \right)$
- D. $\left(\frac{\pi}{4} \right)^{1\sqrt{2}} \cdot \left(\frac{\sqrt{2}}{2} \log \frac{4}{\pi} + \frac{2\sqrt{2}}{\pi} \right)$

Answer: A



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7. $y = \frac{x}{a + \frac{x}{b + \frac{x}{a + \frac{x}{b + \dots \infty}}}}, \frac{dy}{dx} = \frac{b}{a(b + 2y)}$

A. $\frac{a}{ab + 2ay}$

B. $\frac{b}{ab + 2ay}$

C. $\frac{a}{ab + 2by}$

D. $\frac{b}{ab + 2ay}$

Answer: D



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8. If $y = x^{x^2}$, then $\frac{dy}{dx}$ equals

A. $2 \log x \cdot x^2$

B. $x(2 \log x + 1) \cdot x^{x^2}$

C. $(2 \log x + 1) \cdot x^{x^2} + 1$

D. $x^{x^2+1} \cdot (\log(ex^2))$

Answer: D



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9. If $x\sqrt{1+y} + y\sqrt{1+x} = 0$, prove that $\frac{dy}{dx} = -\frac{1}{(x+1)^2}$.

A. $\frac{1}{(1+x)^2}$

B. $\frac{-1}{(1+x)^2}$

C. $\frac{-1}{(1+x)} + \frac{1}{(1+x)^2}$

D. None of these

Answer: B



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10. If $x^2e^y + 2xye^x + 13 = 0$ then $\frac{dy}{dx} =$

A. $\frac{-2xe^{y-x} + 2y(x-1)}{x(xe^{y-x} + 2)}$

B. $\left[\frac{2xe^{y-x} + 2y(x-1)}{x(xe^{y-x} + 2)} \right]$

C. $\frac{2xe^{y-x} + 2y(x-1)}{x(xe^{y-x} + 2)}$

D. None of these

Answer: B



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11. If $x = e^{y+e^{y+e^{y+\dots^{\infty}}}}$, $x > 0$, then $\frac{dy}{dx}$ is equal to

A. $\frac{x}{1+x}$

B. $\frac{1+x}{x}$

C. $\frac{1-x}{x}$

D. $\frac{1}{x}$

Answer: C



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12. Let g be the inverse function of f and $f'(x) = \frac{x^{10}}{1+x^2}$. If $g(2) = a$ then $g'(2)$ is equal to

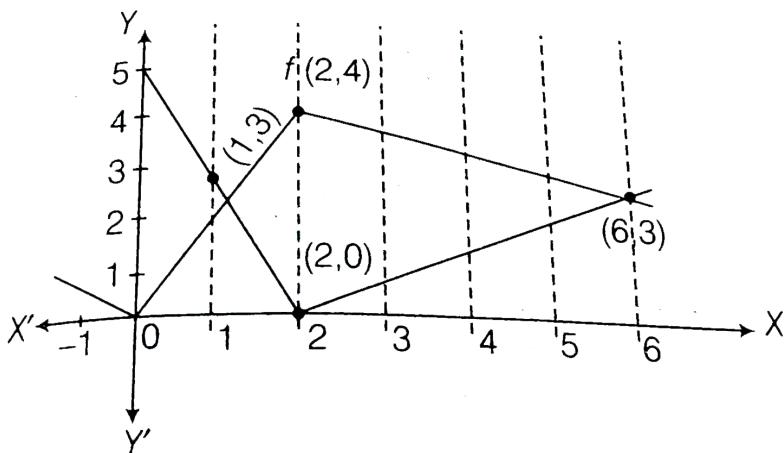
- A. $\frac{5}{2^{10}}$
- B. $\frac{1+a^2}{a^{10}}$
- C. $\frac{a^{10}}{1+a^2}$
- D. $\frac{1+a^{10}}{a^2}$

Answer: B



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13. If f and g are the functions whose graphs are as shown, let $u(x) = f(g(x))$, $w(x) = g(g(x))$



Then the

value of $u'(1) + w'(1)$ is

- A. $-\frac{1}{2}$
- B. $-\frac{3}{2}$
- C. $-\frac{5}{4}$
- D. does not exist

Answer: B



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14. $f'(x) = g(x)$ and $g'(x) = -f(x)$ for all real x and

$f(5) = 2 = f'(5)$ then $f^2(10) + g^2(10)$ is

A. 2

B. 4

C. 8

D. None of these

Answer: C



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15.

if

$$f(x) = x + \frac{x^2}{1}! + \frac{x^3}{2}! \pm \dots + \frac{x^n}{n-1}! \text{ then } f(0) + f'(0) + f''(0)$$

is equal to

A. $\frac{n(n+1)}{2}$

B. $\frac{(n^2+1)}{2}$

C. $\left(\frac{n(n+1)}{2}\right)^2$

D. $\frac{n(n+1)(2n+1)}{6}$

Answer: A



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16. If $y = (f_0 f_0 f)(x)$ and $f(0) = 0, f'(0) = 2$ then $y'(0)$ is equal to

A. 6

B. 7

C. 8

D. 9

Answer: C



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17. If $y^2 = P(x)$ is a polynomial of degree 3, then $2\left(\frac{d}{dx}\right)\left(y^2 \frac{d^2y}{dx^2}\right)$ is equal to $P^x + P'(x)$ (b) $P^x \dot{P}^x$ (c) $P(x) \dot{P}^x$ (d) a constant

A. $p'''(x) \cdot p'(x)$

B. $p''(x) \cdot p'''(x)$

C. $p(x) \cdot p'''(x)$

D. None of these

Answer: C



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18. If $y = f(x)$ and $x = g(y)$ are inverse functions of each other, then

A. $g''(y) = \frac{1}{f''(x)}$

B. $g''(y) = \frac{f''(x)}{(f''(x))^3}$

C. $g''(y) = \frac{f'(x)}{(f'(x))^3}$

D. None of these

Answer: B



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19. If y is a function of x then $\frac{d^2y}{dx^2} + y \frac{dy}{dx} = 0$. If x is a function of y then the equation becomes

- A. $\frac{d^2x}{dy^2} - x \frac{dx}{dy} = 0$
- B. $\frac{d^2x}{dy^2} + y \left(\frac{dx}{dy} \right)^2 = 0$
- C. $\frac{d^2x}{dy^2} - y \left(\frac{dx}{dy} \right)^2 = 0$
- D. $\frac{d^2x}{dy^2} - x \left(\frac{dx}{dy} \right)^2 = 0$

Answer: C



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20. Let $g(x) = \log f(x)$, where $f(x)$ is a twice differentiable positive function on $(0, \infty)$ such that $f(x+1) = xf(x)$. Then, for $N = 1, 2, 3, \dots$, $g''\left(N + \frac{1}{2}\right) - g''\left(\frac{1}{2}\right)$ is equal to

- A. $-4 \left\{ 1 + \frac{1}{9} + \frac{1}{25} + \dots + \frac{1}{(2N-1)^2} \right\}$

- B. $4 \left\{ 1 + \frac{1}{9} + \frac{1}{25} + \dots + \frac{1}{(2N-1)^2} \right\}$
- C. $-4 \left\{ 1 + \frac{1}{9} + \frac{1}{25} + \dots + \frac{1}{(2N+1)^2} \right\}$
- D. $4 \left\{ 1 + \frac{1}{9} + \frac{1}{25} + \dots + \frac{1}{(2N+1)^2} \right\}$

Answer: A



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21. If the functions $f(x) = x^3 + e^{x/2}$ and $g(x) = f^{-1}(x)$, the value of $g'(1)$ is



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22. Let $f(\theta) = \sin \left(\tan^{-1} \left(\frac{\sin \theta}{\sqrt{\cos 2\theta}} \right) \right)$, where $-\frac{\pi}{4} < \theta < \frac{\pi}{4}$ then the value of $\frac{d}{d(\tan \theta)} f(\theta)$ is

A. 1

B. 2

C. 3

D. 4

Answer: A



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23. If $y = \log_{\sin x}(\tan x)$, then $\frac{dy}{dx}$ at $x = \frac{\pi}{4}$ is equal to

A. $\frac{4}{\log 2}$

B. $-4 \log 2$

C. $\frac{-4}{\log 2}$

D. None of these

Answer: C



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24. If $y = \sum_{r=1}^x \tan^{-1} \left(\frac{1}{1+r+r^2} \right)$, then $\frac{dy}{dx}$ is equal to

- A. $\frac{1}{1+x^2}$
- B. $\frac{1}{1+(1+x)^2}$
- C. 0
- D. None of these

Answer: B



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25. If $f(x) = \cot^{-1} \left(\frac{x^x - x^{-x}}{2} \right)$ then $f'(1)$ equals

- A. -1
- B. 1
- C. $\log_e 2$
- D. $-\log_e 2$

Answer: A



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26. The function $f(x) = e^x + x$, being differentiable and one-to-one, has a differentiable inverse $f^{-1}(x)$. The value of $\frac{d}{dx}(f^{-1})$ at the point $f(\log 2)$ is $\frac{1}{1n2}$ (b) $\frac{1}{3}$ (c) $\frac{1}{4}$ (d) none of these

A. $\frac{1}{1n2}$

B. $\frac{1}{3}$

C. $\frac{1}{4}$

D. None of these

Answer: B



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27. If $f''(x) = -f(x)$ and $g(x) = f'(x)$ and
 $F(x) = \left(f\left(\frac{x}{2}\right)\right)^2 + \left(g\left(\frac{x}{2}\right)\right)^2$ and given that $F(5) = 5$, then $F(10)$
is (a) 5 (b) 10 (c) 0 (d) 15

A. 5

B. 10

C. 0

D. 15

Answer: A



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28. Write the subsets of $\{1,2\}$.



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29. If $x = f(t)\cos t - f'(t)\sin t$ and $y = f(t)\sin t + f'(t)\cos t$, then

$$\left(\frac{dx}{dt}\right)^2 + \left(\frac{dy}{dt}\right)^2 = f(t) - f(t)$$

(b) $\{f(t) - f(t)\}^2$ (c) $\{f(t) + f(t)\}^2$

(d) none of these

A. $f(t) - f''(t)$

B. $[f(t) - f''(t)]^2$

C. $[f(t) + f''(t)]^2$

D. None of these

Answer: C



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30. If $y = at^2 + 2bt - c$ and $t = ax^2 + 2bx + c$, then $\frac{d^3y}{dx^3}$ equals

A. $24a^2(at + b)$

B. $24a(ax + b)^2$

C. $24a(at + b)^2$

D. $24a^2(ax + b)$

Answer: D



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31. Differential coefficient of

$\left(x^{\frac{l+m}{m-n}}\right)^{1/(n-l)} \cdot \left(x^{\frac{m+n}{n-l}}\right)^{1/(l-m)} \cdot \left(x^{\frac{n+l}{l-m}}\right)^{1/(m-n)}$ wrt x is

A. 1

B. 0

C. -1

D. x^{lmn}

Answer: B



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32. if $y = (A + Bx)e^{mx} + (m - 1)^{-1}e^x$ then $\frac{d^2y}{dx^2} - 2m\frac{dy}{dx} + m^2y$ is equal to:

- A. e^x
- B. e^{mx}
- C. e^{-mx}
- D. $e^{(1-m)x}$

Answer: A



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33. If $f(x) = -\frac{x^3}{3} + x^2 \sin a \cdot \sin 2a - 5 \sin^{-1}(a^2 - 8a + 17)$, then

- A. $f(x)$ is not defined at $x = \sin 8$
- B. $f'(\sin 8) > 0$
- C. $f'(x)$ is not defined at $x = \sin 8$
- D. $f'(\sin 8) < 0$

Answer: D



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34. Let f and g be differentiable functions satisfying $g(a) = b$, $g'(a) = 2$ and $f \circ g = I$ (identity function). Then $f'(b)$ is equal to

A. $2/3$

B. 1

C. 0

D. $1/2$

Answer: D



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35. If $f(x) = \frac{\cos^{-1} 1}{\sqrt{13}}(2 \cos x - 3 \sin x) + \frac{\sin^{-1} 1}{\sqrt{13}} \cdot (2 \cos x + 3 \sin x)$ wrt $\sqrt{1+x^2}$, then find $\frac{df(x)}{dx}$ at $x = \frac{3}{4}$.

A. $\frac{3}{2}$

B. $\frac{5}{2}$

C. $\frac{10}{3}$

D. 0

Answer: C



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36. If $f(x) = \sqrt{x + 2\sqrt{2x - 4}} + \sqrt{x - 2\sqrt{2x - 4}}$ then the value of $10f'(102^+)$, is

A. -1

B. 0

C. 1

D. does not exist

Answer: C



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37. Let $y = \ln(1 + \cos x)^2$. Then the value of $\frac{d^2y}{dx^2} + \frac{2}{e^{\frac{y}{2}}}$ equal (b)
 $\frac{2}{1 + \cos x}$ $\frac{4}{1 + \cos x}$ (d) $\frac{-4}{(1 + \cos x)^2}$

A. 0

B. $\frac{2}{1 + \cos x}$

C. $\frac{4}{(1 + \cos x)}$

D. $\frac{-4}{(1 + \cos x)^2}$

Answer: A



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38. If $f(x) = \frac{a + \sqrt{a^2 - x^2} + x}{\sqrt{a^2 - x^2} + a - x}$ where $a > 0$ then $f'(0)$ has the value
equal to

A. \sqrt{a}

B. a

- C. $\frac{1}{\sqrt{a}}$
- D. $\frac{1}{a}$

Answer: D



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39. Let $u(x)$ and $v(x)$ be differentiable functions such that $\frac{u(x)}{v(x)} = 7$ If

$\frac{u'(x)}{v'(x)} = p$ and $\left(\frac{u(x)}{v(x)}\right)' = q$, then $\frac{p+q}{p-q}$ has the value

- (a) 1 (b) 0 (c) 7 (d) -7

A. 1

B. 0

C. 7

D. -7

Answer: A



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40. If $f(x) = |\log_e|x||$, then $f'(x)$ equals

A. $\frac{1}{|x|}, x \neq 0$

B. $\frac{1}{x}$ for $|x| > 1$ and $-\frac{1}{x}$ for $|x| < 1$

C. $-\frac{1}{x}$ for $|x| > 1$ and $-\frac{1}{x}$ for $|x| < 1$

D. $\frac{1}{x}$ for $x > 0$ and $-\frac{1}{x}$ for $x < 0$

Answer: B



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41. If $f(x)$ is given by

$$f(x) =$$

$$(\cos x + i \sin x)(\cos 3x + i \sin 3x) \dots \dots [\cos(2n-1)x + i \sin(2n-1)x]$$

then $f''(x)$ is equal to

a. $n^3 f(x)$

b. $-n^4 f(x)$

c. $-n^2 f(x)$

d. $n^4 f(x)$

A. $n^3 f(x)$

B. $-n^4 f(x)$

C. $-n^2 f(x)$

D. $n^4 f(x)$

Answer: B



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42. Let $f(x) = x^n$, n being a non-negative integer, The value of n for which the equality $f'(x + y) = f'(x) + f'(y)$ is valid for all $x, y > 0$, is

A. 0,1

B. 2

C. 2,4

D. None of these

Answer: B



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43. If $f(x) = \sin\left\{\frac{\pi}{3}[x] - x^2\right\}$ for $2 < x < 3$ and $[x]$ denotes the greatest integer less than or equal to x , then $f'(\sqrt{\pi/3})$ is equal to

A. $\sqrt{\pi/3}$

B. $-\sqrt{\pi/3}$

C. $-\sqrt{\pi}$

D. None of these

Answer: B



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44. The functions $u = e^x \cdot \sin x$ and $v = e^x \cdot \cos x$ satisfy the equation

A. $v \frac{du}{dx} - u \frac{dv}{dx} = u^2 + v^2$

B. $v \frac{d^2u}{dx^2} = 2v$

C. $\frac{d^2v}{dx^2} = -2u$

D. All of these

Answer: D



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45. If $f(x) = \log_{x^2}(\log x)$, then $f'(x)$ at $x = e$ is

A. e

B. $-e$

C. e^2

D. e^{-1}

Answer: D



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46. Let f be a differentiable function satisfying

$$[f(x)]^n = f(nx) \text{ for all } x \in R.$$

Then, $f'(x)f(nx)$

- a. $f(x)$
- b. 0
- c. $f(x)f'(nx)$
- d. none of these

A. $f(x)$

B. 0

C. $f(x)f'(nx)$

D. None of these

Answer: C



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47. If $y = f(x)$ is an odd differentiable function defined on $(-\infty, \infty)$ such that $f'(3) = -2$, then $|f'(-3)|$ equals _____.

A. 4

B. 2

C. -2

D. 0

Answer: C



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48.

If $y = \sqrt{x + \sqrt{y + \sqrt{x + \sqrt{y + \dots \infty}}}}$, then prove that $\frac{dy}{dx} = \frac{y^2 - 2x}{2y^3 - 2y}$

A. $\frac{y+x}{y^2 - 2x}$

B. $\frac{y^3 - x}{2y^2 - 2xy - 1}$

C. $\frac{y^3 + x}{2y^2 - x}$

D. None of these

Answer: D



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49. If $f(x) = |\cos x - \sin x|$, then $f' \left(\frac{\pi}{4} \right)$ is equal to

A. $\sqrt{2}$

B. $-\sqrt{2}$

C. 0

D. None of these

Answer: D



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50.

Let

$f(x) = x^2 + xg'(1) + g''(2)$ and $g(x) = f(1) \cdot x^2 + xf'(x) + f''(x)$,
then find $f(x)$ and $g(x)$.

A. $f'(1) = 4 + f'(2)$

B. $g'(2) = 8 + g'(10)$

C. $g''(2) + f''(3) = 4$

D. All of the above

Answer: D



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51. if $f(x) = x^n$ then the value of
 $f(1) - \frac{f'(1)}{1!} + \frac{f''(1)}{2!} + \dots + \frac{(-1)^n f^{(n)}(1)}{n!}$

A. 1

B. 2^n

C. 2^{n-1}

D. 0

Answer: D



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52. If $y + \log(1 + x) = 0$ which of the following is true?

A. $e^y = xy' - 1$

B. $y' = -\frac{1}{(x+1)}$

C. $y' + e^y = 0$

D. $y' = e^y$

Answer: B::C



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53. If $y = 2^{3^x}$, then y' equals

A. $3^x \cdot \log 3 \cdot \log 2$

B. $y \cdot (\log 2y) \cdot \log 3 \cdot \log 2$

C. $2^{3^x} \cdot 3^x \cdot \log 6$

D. $2^{3^x} \cdot 3^x \cdot \log 3 \cdot \log 2$

Answer: B::D



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54. If g is the inverse of f and $f(x) = x^2 + 3x - 3$, ($x > 0$). then $g'(1)$ equals



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55. If $x^3 - 2x^2y^2 + 5x + y - 5 = 0$ and $y(1) = 1$, then

a. $y'(1) = \frac{4}{3}$

b. $y''(1) = -\frac{1}{3}$

c. $y''(1) = -8\frac{22}{27}$

d. $y'(1) = \frac{2}{3}$

A. $y'(1) = \frac{4}{3}$

B. $y''(1) = -\frac{1}{3}$

C. $y''(1) = -8\frac{22}{27}$

D. $y'(1) = \frac{2}{3}$

Answer: A::C



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56. Let $y = \sqrt{x + \sqrt{x + \sqrt{x + \infty}}}$, $\frac{dy}{dx}$ is equal to

A. $\frac{1}{2y - 1}$

B. $\frac{x}{x + 2y}$

C. $\frac{1}{\sqrt{1 - 4x}}$

D. $\frac{y}{2x + y}$

Answer: A::D



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57. If $y = x^{(\ln x)^{\ln(\ln x)}}$, then $\frac{dy}{dx}$ is equal to

A. $\frac{y}{x} \left(\ln x^{\ln x - 1} + 2 \ln + (\ln x) \right)$

B. $\frac{y}{x} (\ln x)^{\ln(\ln x)} (\ln(\ln x) + 1)$

C. $\frac{y}{x \ln x} \left((nx)^2 + 2 \ln x (\ln x) \right)$

D. $\frac{y}{x} \cdot \frac{\ln y}{\ln x} (2 \ln(\ln x) + 1)$

Answer: D



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58. Which of the following functions are not derivable at $x = 0$?

A. $f(x) = \sin^{-1} 2x\sqrt{1 - x^2}$

B. $g(x) = \sin^{-1}\left(\frac{2^x + 1}{1 + 4^x}\right)$

C. $h(x) = \sin^{-1}\left(\frac{1 - x^2}{1 + x^2}\right)$

D. $k(x) = \sin^{-1}(\cos x)$

Answer: B::C::D



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59. If $2^x + 2^y = 2^{x+y}$ then $\frac{dy}{dx}$ is equal to

A. $-\frac{2^y}{2^x}$

B. $\frac{1}{1 - 2^x}$

C. $1 - 2^y$

D. $\frac{2^x(1 - 2^y)}{2^y(2^x - 1)}$

Answer: A::B::C::D



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60. For the function $y = f(x) = (x^2 + bx + c)e^x$, which of the following holds?

- A. If $f(x) > 0$ for all real $x \cancel{\Rightarrow} f'(x) > 0$
- B. If $f(x) > 0$ for all real $x \Rightarrow f'(x) > 0$
- C. If $f'(x) > 0$ for all real $x \Rightarrow f(x) > 0$
- D. If $f'(x) > 0$ for all real $x \cancel{\Rightarrow} f(x) > 0$

Answer: A::C



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61. If $\sqrt{y+x} + \sqrt{y-x} = c$, where $c \neq 0$, then $\frac{dy}{dx}$ has the value equal to

A. $\frac{2x}{e^2}$

B. $\frac{x}{y + \sqrt{y^2 - x^2}}$

C. $\frac{y - \sqrt{y^2 - x^2}}{x}$

D. $\frac{c^2}{2y}$

Answer: C



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62. If $y = \tan x \tan 2x \tan 3x$, ($\sin 12x \neq 0$) then $\frac{dy}{dx}$ has the value equal to

A.

$3 \sec^2 3x \tan x \tan 2x + \sec^2 x \tan 2x \tan 3x + 2 \sec^2 2x \tan 3x \tan x$

B. $2y(\cos ec 2x + 2 \cos ec 4x + 3 \cos ec 6x)$

C. $3 \sec^2 3x - 2 \sec^2 2x - \sec^2 x$

D. $\sec^2 x + 2 \sec^2 2x + 3 \sec^2 3x$

Answer: A::B::C



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Exercise Statement I And II Type Questions

1. Consider $f(x) = \frac{x}{x^2 - 1}$

Statement I Graph of $f(x)$ is concave up for $x > 1$.

Statement II If $f(x)$ is concave up then $f''(x) > 0$

- A. Both statement I and Statement II are correct and Statement II is the correct explanation of Statement I
- B. Both Statement I and Statement II are correct but Statement II is not the correct explanation of Statement I
- C. Statement I is correct but Statement II is incorrect
- D. Statement II is correct but Statement I is incorrect.

Answer: A



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2. If $f(x) = \sin^{-1}\left(\frac{2x}{1+x^2}\right)$, then

Statement I The value of $f(2) = \sin^{-1}\left(\frac{4}{5}\right)$.

Statement II $f(x) = \sin^{-1}\left(\frac{2x}{1+x^2}\right) = -2$, for $x < 1$

- A. Both statement I and Statement II are correct and Statement II is the correct explanation of Statement I
- B. Both Statement I and Statement II are correct but Statement II is not the correct explanation of Statement I
- C. Statement I is correct but Statement II is incorrect
- D. Statement II is correct but Statement I is incorrect.

Answer: C



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3. Let f and g be real valued functions defined on interval $(-1, 1)$ such that

$g''(x)$

is

continuous,

$g(0) \neq 0, g'(0) = 0, g''(0) \neq 0$, and $f(x) = g(x)\sin x$.

Statement I $\lim_{x \rightarrow 0} [g(x)\cos x - g(0)\cosec x] = f''(0)$. and

Statement II $f'(0) = g(0)$.

For the following questions, choose the correct answer from the codes

(a), (b), (c) and (d) defined as follows.

A. Both statement I and Statement II are correct and Statement II is

the correct explanation of Statement I

B. Both Statement I and Statement II are correct but Statement II is

not the correct explanation of Statement I

C. Statement I is correct but Statement II is incorrect

D. Statement II is correct but Statement I is incorrect.

Answer: B



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4. Statement I If $y = \sin^{-1}(3x - 4x^3)$, then $\frac{dy}{dx} = \frac{3}{\sqrt{1-x^2}}$ only when $\frac{-1}{2} \leq x < \frac{1}{2}$.

Statement

II

$$\sin^{-1}(3x - 4x^3)$$

$$= \begin{cases} -\pi - 3\sin^{-1}x & -1 \leq x \leq -\frac{1}{2} \\ 3\sin^{-1}x & -\frac{1}{2} \leq x \leq \frac{1}{2} \\ \pi - 3\sin^{-1}x & \frac{1}{2} \leq x \leq 1 \end{cases}$$

- A. Both statement I and Statement II are correct and Statement II is the correct explanation of Statement I
- B. Both Statement I and Statement II are correct but Statement II is not the correct explanation of Statement I
- C. Statement I is correct but Statement II is incorrect
- D. Statement II is correct but Statement I is incorrect.

Answer: A



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5. If $y = \cos^{-1}\left(\frac{1-x^2}{1+x^2}\right)$, then

Statement I $\frac{dy}{dx} = \frac{2}{1+x^2}$ for $x \in R$

Statement II $\cos^{-1}\left(\frac{1-x^2}{1+x^2}\right) = \begin{cases} 2\tan^{-1}x & x \geq 0 \\ -2\tan^{-1}x & x < 0 \end{cases}$

- A. Both statement I and Statement II are correct and Statement II is the correct explanation of Statement I
- B. Both Statement I and Statement II are correct but Statement II is not the correct explanation of Statement I
- C. Statement I is correct but Statement II is incorrect
- D. Statement II is correct but Statement I is incorrect.

Answer: D



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6. Statement I If $f(x)$ is a continuous function defined from R to Q and $f(5) = 3$, then differential coefficient of $f(x)$ w. r. t. x will be 0

Statement II Differentiation of constant functions is always zero.

- A. Both statement I and Statement II are correct and Statement II is the correct explanation of Statement I

B. Both Statement I and Statement II are correct but Statement II is

not the correct explanation of Statement I

C. Statement I is correct but Statement II is incorrect

D. Statement II is correct but Statement I is incorrect.

Answer: A



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7. Statement I Derivative of $\sin^{-1}\left(\frac{2x}{1+x^2}\right)$ w. r. t. $\cos^{-1}\left(\frac{1-x^2}{1+x^2}\right)$ is 1

for $0 < x < 1$.

Statement 2 $\sin^{-1}\left(\frac{2x}{1+x^2}\right) = \cos^{-1}\left(\frac{1-x^2}{1+x^2}\right)$ for $-1 \leq x \leq 1$

A. Both statement I and Statement II are correct and Statement II is

the correct explanation of Statement I

B. Both Statement I and Statement II are correct but Statement II is

not the correct explanation of Statement I

C. Statement I is correct but Statement II is incorrect

D. Statement II is correct but Statement I is incorrect.

Answer: C



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8. Suppose the function $f(x)$ satisfies the relation $f(x + y^3) = f(x) + f(y^3) \forall x, y \in R$ and is differentiable for all x . Statement 1: If $f'(2) = a$, then $f'(-2) = a$ Statement 2: $f(x)$ is an odd function.

A. Both statement I and Statement II are correct and Statement II is

the correct explanation of Statement I

B. Both Statement I and Statement II are correct but Statement II is

not the correct explanation of Statement I

C. Statement I is correct but Statement II is incorrect

D. Statement II is correct but Statement I is incorrect.

Answer: A



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Exercise Passage Based Questions

1. Let $\frac{f(x+y) - f(x)}{2} = \frac{f(y) - 1}{2} + xy$, for all $x, y \in R$, $f(x)$ is differentiable and $f'(0) = 1$. Domain of $\log(f(x))$, is

A. R^+

B. $R - \{0\}$

C. R

D. R^-

Answer: C



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2. Let $\frac{f(x+y) - f(x)}{2} = \frac{f(y) - 1}{2} + xy$, for all $x, y \in R$, $f(x)$ is differentiable and $f'(0) = 1$.

Range of $y = \log_{3/4}(f(x))$ is

A. $(-\infty, 1)$

B. $[3/4, \infty$

C. $(-\infty, \infty)$

D. R

Answer: A



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3. Let $\frac{f(x+y) - f(x)}{2} = \frac{f(y) - 1}{2} + xy$, for all $x, y \in R$, $f(x)$ is differentiable and $f'(0) = 1$. Let $g(x)$ be a derivable function at $x = 0$ and follows the function rule $g\left(\frac{x+y}{k}\right) = \frac{g(x) + g(y)}{k}$, $k \in R$, $k \neq 0, 2$ and $g'(0) = \lambda$ If the

graphs of $y = f(x)$ and $y = g(x)$ intersect in coincident points then λ can take values

A. -3

B. 1

C. -1

D. 4

Answer: C



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4. Find the derivative of $\log(\sin(\log x))$.



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5. Left hand derivative and right hand derivative of a function $f(x)$ at a point $x = a$ are defined as

$$\begin{aligned}
 f'(a^-) &= \lim_{h \rightarrow 0^+} \frac{f(a) - f(a-h)}{h} \\
 &= \lim_{h \rightarrow 0^+} \frac{f(a+h) - f(a)}{h} \\
 \text{and } f'(a^+) &= \lim_{h \rightarrow 0^+} \frac{f(a+h) - f(a)}{h} \\
 &= \lim_{h \rightarrow 0^+} \frac{f(a) - f(a+h)}{h} \\
 &= \lim_{h \rightarrow 0^+} \frac{f(a) - f(x)}{a-x} \text{ respectively.}
 \end{aligned}$$

Let f be a twice differentiable function. We also know that derivative of an even function is odd function and derivative of an odd function is even function.

If f is even function, which of the following is right hand derivative of f' at $x = a$?

- A. (a) $\lim_{h \rightarrow 0^-} \frac{f'(a) + f'(-a+h)}{-h}$
- B. (b) $\lim_{h \rightarrow 0^-} \frac{f'(a) + f'(-a-h)}{h}$
- C. (c) $\lim_{h \rightarrow 0^-} \frac{-f'(-a) + f'(-a-h)}{-h}$
- D. (d) $\lim_{h \rightarrow 0^+} \frac{f'(a) + f'(-a+h)}{-h}$

Answer: A



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6. Find $\frac{dy}{dx}$ if $ax + by + c = 0$



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7. If $f(x) = \sin^{-1}(3x - 4x^3)$. Then answer the following

The value of $f'(0)$, is

A. -3

B. 3

C. $\sqrt{2}$

D. $-\sqrt{2}$

Answer: B



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8. If $f(x) = \sin^{-1}(3x - 4x^3)$. Then answer the following

The value of $f' \left(\frac{1}{\sqrt{2}} \right)$, is

A. -3

B. 3

C. $-3\sqrt{2}$

D. $3\sqrt{2}$

Answer: C



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9. Let the derivative of $f(x)$ be defined as

$$D^* f(x) = \lim_{h \rightarrow 0} \frac{f^2(x+h) - f^2(x)}{h}, \text{ where } f^2(x) = \{f(x)\}^2.$$

If $u = f(x)$, $v = g(x)$, then the value of $D^*(u \cdot v)$ is

A. (a) $(D^* u)v + (D^* v)u$

B. (b) $u^2(D^* v) + v^2(D^* u)$

C. (c) $D^* u + D^* v$

D. (d) $uvD^*(u + v)$

Answer: B



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10. Let the derivative of $f(x)$ be defined as

$$D^* f(x) = \lim_{h \rightarrow 0} \frac{f^2x + h - f^2(x)}{h}, \text{ where } f^2(x) = \{f(x)\}^2.$$

If $u = f(x)$, $v = g(x)$, then the value of $D^* \left(\frac{u}{v} \right)$ is.

A. $\frac{u^2(D^* v) - v^2(D^* u)}{v^4}$

B. $\frac{u(D^* v) - v(D^* u)}{v^2}$

C. $\frac{v^2(D^* u) - u^2(D^* v)}{v^4}$

D. $\frac{v(D^* u) - u(D^* v)}{v^2}$

Answer: C



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11. A curve is represented parametrically by the equations $x = e^t \cos t$ and $y = e^t \sin t$ where t is a parameter. Then The relation between the parameter 't' and the angle α between the tangent to the given curve and the x-axis is given by, 't' equals

A. $\frac{\pi}{2} - \alpha$

B. $\frac{\pi}{4} + \alpha$

C. $\alpha - \frac{\pi}{4}$

D. $\frac{\pi}{4} - \alpha$

Answer: C



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12. A curve is represented parametrically by the equations $x = e^t \cos t$ and $y = e^t \sin t$ where t is a parameter. Then

The value of $\frac{d^2y}{dx^2}$ at the point where $t = 0$ is

A. 1

B. 2

C. -2

D. 3

Answer: B



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13. A curve is represented parametrically by the equations

$x = e^t \cos t$ and $y = e^t \sin t$, where t is a parameter. Then, If

$F(t) = \int(x + y)dt$, then the value of $F\left(\frac{\pi}{2}\right) - F(0)$ is

A. 1

B. -1

C. $e^{\pi/2}$

D. 0

Answer: C



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14.

Equation

$x^n - 1 = 0, n > 1, n \in N$, has roots $1, a_1, a_2, \dots, a_{n-1}$.

The value of $(1 - a_1)(1 - a_2) \dots (1 - a_{n-1})$ is

A. $\frac{n^2}{2}$

B. n

C. $(-1)^n n$

D. None of the above

Answer: B



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15. Equation $x^n - 1 = 0$, $n > 1$, $n \in N$, has roots $1, a_1, a_2, \dots, a_n$. The

value of $\sum_{r=2}^n \frac{1}{2 - a_r}$, is

A. $\frac{2^{n-1}(n-2) + 1}{2^n - 1}$

B. $\frac{2^n(n-2) + 1}{2^n - 1}$

C. $\frac{2^{n-1}(n-1) - 1}{2^n - 1}$

D. None of the above

Answer: A



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16. Equation $x^n - 1 = 0$, $n > 1$, $n \in N$, has roots $1, a_1, a_2, \dots, a_n$.

The value of $\sum_{r=2}^n \frac{1}{2 - a_r}$, is

A. $\frac{n}{4}$

B. $\frac{n(n-1)}{2}$

$$\text{C. } \frac{n - 1}{2}$$

D. None of these

Answer: D



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Differentiation Exercise 5

1. Match the entries between the following two columns.

| Column I | Column II |
|--|------------------|
| (A) $y = f(x)$ be given by $x = t^5 - 5t^3 - 20t + 7$ and $y = 4t^3 - 3t^2 - 18t + 3$, then $-5 \times \frac{dy}{dx} \quad t = 1$ | (p) 0 |
| (B) $P(x)$ be a polynomial of degree 4 with $P(2) = -1, P'(2) = 0, P''(2) = 2,$ $P'''(2) = -12$ and $P''''(2) = 24$, then $P''(3)$ is equal to | (q) -2 |
| (C) $y = \frac{1}{x}$, then $\frac{\frac{dy}{dx}}{\sqrt{1+x^4}}$ | (r) 2 |
| (D) $f\left(\frac{2x+3y}{5}\right) = \frac{2f(x)+3f(y)}{5}$ and $f'(0) = p$ and $f(0) = q$, then $f''(0)$ | (s) -1 |



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2. If $A = \{5, 7, 9, 11\}$, $B = \{7, 9, 11, 13\}$, $C = \{11, 13\}$. Find $A \cap (B \cup C)$.



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Exercise Subjective Type Questions

1. If $f(x) = x^3 + x^2 f'(1) + x f''(2) + x f''(2) + f'''(3)$ for all $x \in R$. then find $f(x)$ independent of $f'(1)$, $f''(2)$ and $f'''(3)$.



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2. $\int \sin^{-1} \left(\frac{2x+2}{\sqrt{4x^2+8x+13}} \right) dx$ is,



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3.

If

$$f(x) = \begin{vmatrix} (x-a)^4 & (x-a)^3 & 1 \\ (x-b)^4 & (x-b)^3 & 1 \\ (x-c)^4 & (x-c)^3 & 1 \end{vmatrix} \text{ then } f'(x) = \lambda \cdot \begin{vmatrix} (x-a)^4 & (x-a)^2 \\ (x-b)^4 & (x-b)^2 \\ (x-c)^4 & (x-c)^2 \end{vmatrix}$$

. The value of λ is



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4. Let $p(x)$ be a polynomial of degree 4 such that $P(1) = P(3) = P(5) = P'(7) = 0$. If the real number $a \neq 1, 3, 5$ is such that $P(a) = 0$ can be expressed as $a = \frac{p}{q}$, where p and q are relatively prime, then $(p - 8q)$ is.....



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5. If $x^2 + y^2 = t - \frac{1}{t}$ and $x^4 + y^4 = t^2 + \frac{1}{t^2}$, then $\left(\frac{dy}{dx}\right)_{(1,1)}$ is.....



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6. If $x^2 + y^2 + z^2 - 2xyz = 1$, then the value of $\frac{dx}{\sqrt{1-x^2}} + \frac{dy}{\sqrt{1-y^2}} + \frac{dz}{\sqrt{1-z^2}}$ is equal to.....



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7. If y is twice differentiable function of x , then the expression $(1 - x^2) \cdot \frac{d^2y}{dx^2} - x \frac{dy}{dx} + y$ by means of the transformation $x = \sin t$ in terms of t is $\frac{d^2y}{dt^2} + \lambda y$. Thus λ is....



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8. The derivative of $f(x) = \cos^{-1}\left(\frac{1}{\sqrt{3}}(2\cos x - 3\sin x)\right) + \left\{\sin^{-1}\left(\frac{1}{\sqrt{3}}(2\cos x + 3\sin x)\right)\right.$ w.r.t. $\sqrt{1+x^2}$ at $x = \frac{1}{\sqrt{3}}$ is.....



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9. Suppose $f(x) = e^{ax} + e^{bx}$, where $a \neq b$ and $f''(x) - 2f'(x) - 15f(x) = 0$ for all x , then the value of $|a+b|$ is equal to.....



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10. Suppose $A = \frac{dy}{dx}$ of $x^2 + y^2 = 4$ at $(\sqrt{2}, \sqrt{2})$, $B = \frac{dy}{dx}$ of $\sin y + \sin x = \sin x \cdot \sin y$ at (π, π) and $C = \frac{dy}{dx}$ of $2e^{xy} + e^x \cdot e^y - e^x - e^y = e^{xy+1}$ at $(1, 1)$, then $(A - B - C)$ has the value equal to.....



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11. A function is represented parametrically by the equations $x = \frac{1+t}{t^3}; y = \frac{3}{2t^2} + \frac{2}{t}$ then the value of $\frac{f(dy)}{dx} - x \left(\frac{dy}{dx} \right)^3$ is _____



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12. Suppose the function $f(x) - f(2x)$ has the derivative 5 at $x = 1$ and derivative 7 at $x = 2$. The derivative of the function $f(x) - f(4x)$ at $x=1$ has the value equal to (a) 19 (b) 9 (c) 17 (d) 14



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13. If $x + y = 3e^2$ then $D(x^y)$ vanishes when x equals to



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14. Let $h(x)$ be differentiable for all x and let $f(x) = (kx + e^x)h(x)$, where k is some constant. If $h(0) = 5$, $h'(0) = -2$, and $f'(0) = 18$, then the value of k is



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Exercise Questions Asked In Previous 13 Years Exam

1. For $x \in R$, $f(x) = |\log 2 - \sin x|$ and $g(x) = f(f(x))$, then

A. g is not differentiable at $x = 0$

B. $g'(0) = \cos(\log 2)$

C. $g'(0) = -\cos(\log 2)$

D. g is differentiable at $x = 0$ and $g'(0) = -\sin(\log 2)$

Answer: b



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2. Let $f: R \rightarrow R$ and $h: R \rightarrow R$ be differentiable functions such that

$f(x) = x^3 + 3x + 2$, $g(f(x)) = x$ and $h(g(x)) = x$ for all $x \in R$.

Then, $h'(1)$ equals.

A. $g'(2) = \frac{1}{15}$

B. $h'(1) = 666$

C. $h(0) = 16$

D. $h(g(3)) = 36$

Answer: b,c



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3.

If for $x \in \left(0, \frac{1}{4}\right)$, the derivative of $\tan^{-1}\left(\frac{6x\sqrt{x}}{1-9x^3}\right)$ is $\sqrt{x} \cdot g(x)$,

then $g(x)$ equals

A. $\frac{3}{1+9x^3}$

B. $\frac{9}{1+9x^3}$

C. $\frac{3x\sqrt{x}}{1-9x^3}$

D. $\frac{3x}{1-9x^3}$

Answer: c



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4. Let $g(x) = \log f(x)$, where $f(x)$ is a twice differentiable positive function

on $(0, \infty)$ such that $f(x+1) = xf(x)$. Then, for

$N = 1, 2, 3, \dots, g''\left(N + \frac{1}{2}\right) - g''\left(\frac{1}{2}\right)$ is equal to

A. $-4\left\{1 + \frac{1}{9} + \frac{1}{25} + \dots + \frac{1}{(2N-1)^2}\right\}$

- B. $4 \left\{ 1 + \frac{1}{9} + \frac{1}{25} + \dots + \frac{1}{(2N-1)^2} \right\}$
- C. $-4 \left\{ 1 + \frac{1}{9} + \frac{1}{25} + \dots + \frac{1}{(2N+1)^2} \right\}$
- D. $4 \left\{ 1 + \frac{1}{9} + \frac{1}{25} + \dots + \frac{1}{(2N+1)^2} \right\}$

Answer: a



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5. $\frac{d^2x}{dy^2}$ equals

- a. $\left(\frac{d^2y}{dx^2} \right)^{-1}$
- b. $- \left(\frac{d^2y}{dx^2} \right)^{-1} \left(\frac{dy}{dx} \right)^{-3}$
- c. $\left(\frac{d^2y}{dx^2} \right) \left(\frac{dy}{dx} \right)^{-2}$
- d. $- \left(\frac{d^2y}{dx^2} \right) \left(\frac{dy}{dx} \right)^{-3}$

A. $\left(\frac{d^2y}{dx^2} \right)^{-1}$

B. $- \left(\frac{d^2y}{dx^2} \right)^{-1} \left(\frac{dy}{dx} \right)^{-3}$

C. $\left(\frac{d^2y}{dx^2} \right) \left(\frac{dy}{dx} \right)^{-2}$

$$\text{D. } - \left(\frac{d^2y}{dx^2} \right) \left(\frac{dy}{dx} \right)^{-3}$$

Answer: d



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6. If $f''(x) = -f(x)$, $g(x) = f'(x)$

$F(x) = f\left(\frac{x}{2}\right)^2 + g\left(\frac{x}{2}\right)^2$ and $F(5) = 5$, then $F(10)$ is equal to

A. 0

B. 5

C. 10

D. 25

Answer: b



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7. If y is a function of x and $\log(x + y) - 2xy = 0$, then the value of $y'(0)$ is

- (a) 1 (b) -1 (c) 2 (d) 0

A. 1

B. -1

C. 2

D. 0

Answer: a



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8. If $x^2 + y^2 = t - \frac{1}{t}$ and $x^4 + y^4 = t^2 + \frac{1}{t^2}$, then prove that
 $\frac{dy}{dx} = \frac{1}{x^3y}$



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Exercise For Session 1

1. Differentiate the following with respect of x : $e^{a \log a} + e^{a \log x} + e^{a \log a}$



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2. Evaluate: (i) $\int \sin^{-1}(\cos x) dx, \quad 0 \leq x \leq \pi$

(ii) $\int \tan^{-1} \left\{ \sqrt{\left(\frac{1 - \cos 2x}{1 + \cos 2x} \right)} \right\} dx, \quad 0 \leq x \leq \pi/2$



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3. Differentiate the following with respect of x : $(\log)_3 x + 3(\log)_e x + 2 \tan x$



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4. Differentiate $|x| + a_0 x^n + a_1 x^{n-1} + a_2 x^{n-2} + \dots + a_{n-1} x + a_n$



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$$5. y = \sec^{-1} \left(\frac{x+1}{x-1} \right) + \sin^{-1} \left(\frac{x-1}{x+1} \right), x > 0. \text{ Find } dy/dx$$



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$$6. \text{ Differentiate w.r.t } x : x^n \log_a x e^x$$



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$$7. \text{ Differentiate: } \frac{2^x \cot x}{\sqrt{x}}$$



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$$8. \text{ Differentiate } \frac{\sin x - x \cos x}{x \sin x + \cos x} \text{ with respect to } x.$$



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9. If $y = 1 + \frac{x}{1!} + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$, then $\frac{dy}{dx} = \dots \dots \dots \dots$



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10. Find the values of 'x' for which the rate of change of $\frac{x^4}{4} + \frac{x^3}{3} - x$ is more than $\frac{x^4}{4}$



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Exercise For Session 2

1. Differentiate the following w.r.t.x. $(x^2 + x + 1)^4$



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2. Differentiate the following w.r.t.x. $\sqrt{x^2 + x + 1}$



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3. Differentiate the following w.r.t.x. $\sin^3 x$



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4. Differentiate the following w.r.t.x. $\frac{1}{\sqrt{a^2 - x^2}}$



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5. Differentiate the following w.r.t.x. $e^x \sin x$



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6. Differentiate the following w.r.t.x. $\sin^{-1} \left(\frac{a + b \cos x}{b + a \cos x} \right)$, $b > a > 1$



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7. Differentiate the following w.r.t.x. e^{e^x}



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8. Differentiate the following w.r.t.x. $\log\left(x + \sqrt{a^2 + x^2}\right)$



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9. Differentiate w.r.t. 'x' : $f(x) = \log\left(\frac{a + b \sin x}{a - b \sin x}\right)$



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10. Differentiate the following w.r.t.x. $\log \sqrt{\frac{1 + \sin x}{1 - \sin x}}$



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11. Differentiate the following w.r.t.x. $\frac{e^x + \log x}{\sin 3x}$



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12. Differentiate the following w.r.t.x. $\sin(m \sin^{-1} x)$, $|x| < 1$



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13. Differentiate the following w.r.t.x. $a^{(\sin^{-1} x)^2}$, $|x| < 1$



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14. Differentiate the following w.r.t.x. $e^{\cos^{-1}(\sqrt{1-x^2})}$, $|x| < 1$



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15. Differentiate the following w.r.t.x. $\frac{x \sin^{-1} x}{\sqrt{1-x^2}} + \log \sqrt{1-x^2}$, $|x| < 1$



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16. Differentiate the following w.r.t.x. $\log_{10} x + \log_x 10 + \log_x x + \log_{10} 10$



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17. Differentiate the following w.r.t.x. $5^{3-x^2} + (3 - x^2)^5$



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18. Differentiate the following w.r.t.x. $\frac{\sqrt{a^2 + x^2} + \sqrt{a^2 - x^2}}{\sqrt{a^2 - x^2} - \sqrt{a^2 + x^2}}$



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19. Differentiate the following w.r.t.x. $\sqrt{4 + \sqrt{4 + \sqrt{4 + x^2}}}$



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20. Differentiate the following w.r.t.x. The differentiation cooeffiecent of

$f(\log_e x)$ w. r. t. x, where $f(x) = \log_e x$, is

A. $\frac{x}{\log_e x}$

B. $\frac{1}{x} \log_e x$

C. $\frac{1}{x \log_e x}$

D. None of these

Answer: C



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21. If $f(x) = |\log_e|x||$, then $f'(x)$ equals

A. $\frac{1}{|x|}$

B. $\frac{1}{x}$

C. $-\frac{1}{x}$

D. None of these

Answer: B



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22. If $f(x) = \sin x$, $g(x) = x^2$ and $h(x) = \log x$. IF

$F(x) = h(f(g(x)))$, then $F'(x)$ is

A. $2x \cot x^2$

B. $2 \cos e c^3 x$

C. $-2 \cos e c^2 x$

D. None of these

Answer: A



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23. If $f(x) = \cos x \cos 2x \cos 4x \cos 8x \cos 16x$ then find $f' \left(\frac{\pi}{4} \right)$

A. $\sqrt{2}$

B. $\frac{1}{\sqrt{2}}$

C. 1

D. None of these

Answer: A



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24. If $y = f\left(\frac{3x + 4}{5x + 6}\right)$ and $f'(x) = \tan x^2$, then $\frac{dy}{dx}$ is equal to

A. $-2\tan\left(\frac{3x + 4}{5x + 6}\right)^2 \cdot \frac{1}{(5x + 6)^2}$

B. $f\left(\frac{3\tan x^2 + 3}{5\tan x^2 + 6}\right)\tan x^2$

C. $2x \tan\left(\frac{3x - 4}{5x - 6}\right)$

D. $\tan x^2$

Answer: A



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25. If $y = |\cos x| + |\sin x|$, then $\frac{dy}{dx}$ at $x = \frac{2\pi}{3}$ is

A. $\frac{1}{2}(\sqrt{3} + 1)$

B. $2(\sqrt{3} - 1)$

C. $\frac{1}{2}(\sqrt{3} - 1)$

D. None of these

Answer: C



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26. If $f'(x) = \sin x + \sin 4x \cdot \cos x$, then $f'(2x^2)$ is

A. $4x \{ \cos(2x^2) - \sin 8x^2 \cdot \sin 2x^2 \}$

B. $4x \{ \cos(2x^2) + \sin 8x^2 \cdot \cos 2x^2 \}$

C. $\{ \cos(2x^2) - \sin 8x^2 \cdot \sin 2x^2 \}$

D. None of these

Answer: D



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27. If $f'(x) = \sqrt{2x^2 - 1}$ and $y = f(x^2)$, then $\frac{dy}{dx}$ at $x = 1$ is

A. 1

B. -1

C. -2

D. 2

Answer: D



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Exercise For Session 3

1. If $\log(x^2 + y^2) = 2\tan^{-1}\left(\frac{y}{x}\right)$, then show that $\frac{dy}{dx} = \frac{x+y}{x-y}$



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2. If $\cos^{-1}\left(\frac{x^2 - y^2}{x^2 + y^2}\right) = \tan^{-1} a$, prove that $\frac{dy}{dx} = \frac{y}{x}$.



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3. If $\sin y = x \sin(a + y)$, prove that $\frac{dy}{dx} = \frac{\sin^2(a + y)}{\sin a}$



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4. If $x^2 + y^2 = 1$, then



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5. If $\sin(xy) + \cos(xy) = 0$, then $\frac{dy}{dx}$ is

A. $\frac{y}{x}$

B. $-\frac{y}{x}$

C. $-\frac{x}{y}$

D. $\frac{x}{y}$

Answer: B



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6. If $ax^2 + 2hxy + by^2 = 0$ then $\frac{dy}{dx}$ is

A. $\frac{y}{x}$

B. $\frac{x}{y}$

C. $-\frac{x}{x}$

D. None of these

Answer: A



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7. If $x^2e^y + 2xye^x + 13 = 0$, then $\frac{dy}{dx}$ equals

A. $\frac{-2xe^{y-x} - 2y(x-1)}{x(xe^{y-x} + 2)}$

B. $\frac{2xe^{x-y} - 2y(x-1)}{x(xe^{y-x} + 2)}$

C. $\frac{2xe^{x-y} + 2y(x-1)}{x(xe^{y-x} + 2)}$

D. None of these

Answer: A



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8. If $\log(x + y) = 2xy$, then $y'(0)$ is

A. 1

B. -1

C. 2

D. 0

Answer: A



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9. If $x \log_e y + y \log_e x = 5$, then $\frac{dy}{dx}$ is

A. $-\frac{y}{x} \left(\frac{x \log y + y}{x + y \log x} \right)$

B. $-\frac{x}{y} \left(\frac{x \log y + y}{x + y \log x} \right)$

C. $-\frac{y}{x} \left(\frac{x \log y - y}{x + y \log x} \right)$

D. None of these

Answer: A



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Exercise For Session 3

1. If $x\sqrt{1+y} + y\sqrt{1+x} = 0$ then $\frac{dy}{dx}$ equals.



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Exercise For Session 4

1. If $y = \tan^{-1}\left(\frac{1 - \cos x}{\sin x}\right)$, then $\frac{dy}{dx}$ is



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2. If $y = \cos^{-1}\left(\frac{x - x^{-1}}{x + x^{-1}}\right)$, then $\frac{dy}{dx}$ is

A. $-\frac{2}{1+x^2}$

B. $\frac{2}{1+x^2}$

C. $\frac{1}{1+x^2}$

D. $-\frac{1}{1+x^2}$

Answer: C



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3. If $y = \tan^{-1} \frac{(\sqrt{1 + \sin x} + \sqrt{1 - \sin x})}{(\sqrt{1 + \sin x} - \sqrt{1 - \sin x})}$, find $\frac{dy}{dx}$.

A.

$$\left\{ \left(\frac{1}{2}, \quad \cos \frac{x}{2} > \sin \frac{x}{2} \right), \left(-\frac{1}{2}, \quad \cos \frac{x}{2} < \sin \frac{x}{2} \right), (\text{doesnotexist}, x = \dots) \right.$$

B.

$$\left\{ \left(-\frac{1}{2}, \quad \cos \frac{x}{2} > \sin \frac{x}{2} \right), \left(\frac{1}{2}, \quad \cos \frac{x}{2} < \sin \frac{x}{2} \right), (\text{doesnotexist}, x = \dots) \right.$$

C. $\left\{ \begin{array}{ll} -\frac{1}{2}, & \cos \frac{x}{2} \geq \sin \frac{x}{2} \\ \frac{1}{2}, & \cos \frac{x}{2} < \sin \frac{x}{2} \end{array} \right.$

D. None of these

Answer: B



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4. If $y = \cot^{-1}(\cot x)$, then $\frac{dy}{dx}$ is

A. $1, x \in R$

B. $1, x \in R - \{n\pi\}$

C. $\{(1, x \in R - \{n\pi\}), (\text{does not exist}, x \in \{n\pi\}, n \in \text{integer})\}$

D. None of these

Answer: C



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5. Sketch for the curve $y = \sin^{-1} \left(\frac{2x}{1+x^2} \right)$



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6. Draw the graph of $y = \cos^{-1} \cdot \frac{1-x^2}{1+x^2}$.



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7. Draw the graph of $y = \tan^{-1}\left(\frac{2x}{1-x^2}\right)$



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8. Draw the graph of $y = \tan^{-1}\left(\frac{3x - x^3}{1 - 3x^2}\right)$.



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9. Define $y = \sin^{-1}(3x - 4x^3)$ in terms of $\sin^{-1} x$ and also draw its graph.



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10. Sketch the graph for $y = \sin^{-1}(3x - 4x^3)$



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Exercise For Session 5

1. If $x = 2 \cos \theta - \cos 2\theta$ and $y = 2 \sin \theta - \sin 2\theta$ Prove that

$$\frac{dy}{dx} = \tan\left(\frac{3\theta}{2}\right).$$



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2. If $x = e^{\cos 2t}$ and $y = e^{\sin 2t}$, then prove that $\frac{dy}{dx} = -\frac{y \log x}{x \log y}$.



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3. If $x = \cos t$ and $y = \sin t$, prove : $\frac{dy}{dx} = \frac{1}{\sqrt{3}}$ at $t = \frac{2\pi}{3}$



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4. if $x = t + \frac{1}{t}$, $y = t - \frac{1}{t}$ find dy/dx



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5. If $x = \sin^{-1}\left(\frac{2t}{1+t^2}\right)$ and $y=\tan^{-1}\left(\frac{2t}{1-t^2}\right)$, $t > 1$. Prove that $\frac{dy}{dx}=-1$



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6. If $x = a \sec^3 \theta$ and $y = a \tan^3 \theta$, $f \in d\frac{dy}{dx} \theta = \frac{\pi}{3}$.



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7. Let $y = x^3 - 8x + 7$ and $x = f(t)$ if $\frac{dy}{dt} = 2$ and $x = 3$ at $t = 0$,
then find the value of $\frac{dx}{dt}$ at $t = 0$.



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Exercise For Session 6

1. Differentiate the following w.r.t.x.

$$x^x$$



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2. Differentiate the following w.r.t.x.

$$x^{\sqrt{x}}$$



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3. Differentiate the following w.r.t.x.

$$x^{x^x}$$



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4. Differentiate the following w.r.t.x.

$$x^{x^2}$$





5. Differentiate the following w.r.t.x.

$$x^x \sqrt{x}$$



6. Differentiate the following w.r.t.x.

$$(\cos x)^x$$



7. Differentiate the following w.r.t.x.

$$(\sin x)^{\cos x}$$



8. Differentiate the following w.r.t.x.

$$x^{\cos^{-1}x}$$



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9. Differentiate the following w.r.t.x.

$$\cos(x^x)$$



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10. Differentiate the following w.r.t.x.

$$\log(x^x + \cos ec^2 x)$$



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11. If $y = (\sin x)^{\tan x} + (\cos x)^{\sec x}$, find $\frac{dy}{dx}$



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12. If $x^y = e^{x-y}$, prove that $\frac{dy}{dx} = \frac{\log x}{(1 + \log x)^2}$.



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13. If $x^y + y^x = 2$, find $\frac{dy}{dx}$.



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14. If $(\cos x)^y = (\sin y)^x$, then find $\frac{dy}{dx}$.



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15. If $\sin y = x \sin(a + y)$, prove that $\frac{dy}{dx} = \frac{\sin^2(a + y)}{\sin a}$



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16. If $y = \sqrt{\cos x + \sqrt{\cos x + \sqrt{\cos x + \dots}}} \rightarrow \infty$, prove that
 $\frac{dy}{dx} = \frac{\sin x}{1 - 2y}$



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17. If $y = (\tan x)^{(\tan x)^{(\tan x) \dots \infty}}$, then find $\frac{dy}{dx}$ at $x = \frac{\pi}{4}$



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18. If $y = e^{x^{e^x}}$, Find dy/dx .



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19. If $y = e^x + x$ find dy/dx .



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Exercise For Session 7

1. Differentiate $\tan^{-1}\left(\frac{2x}{1-x^2}\right)$ w.r.t. $\sin^{-1}\left(\frac{2x}{1+x^2}\right)$



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2. Differentiate $\tan^{-1}\left(\frac{2x}{1-x^2}\right)$ w.r.t. $\sin^{-1}\left(\frac{2x}{1+x^2}\right)$



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3. Differentiate $\tan^{-1}\left(\frac{2x}{1-x^2}\right)$ w.r.t. $\sin^{-1}\left(\frac{2x}{1+x^2}\right)$



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4. Find the differential coefficient of the following functions $x^{\sin^{-1} x}$ w.r.t. $\sin^{-1} x$



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5. Differentiate $\sin^{-1}(2ax\sqrt{1-a^2x^2})$ with respect to $\sqrt{1-a^2x^2}$, if $-\frac{1}{\sqrt{2}} < ax < \frac{1}{\sqrt{2}}$.

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6. Differentiate $\log \sin x$ w.r.t. $\sqrt{\cos x}$

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7. Differentiate $\tan^{-1} \left\{ \frac{\sqrt{1+x^2} + \sqrt{1-x^2}}{\sqrt{1+x^2} - \sqrt{1-x^2}} \right\}$ w.r.t.x

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8. Differnetiate x^x w. r. t. $x \log x$.

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9. Differentiate $\sin^{-1}(4x\sqrt{1-4x^2})$ w. r. t. $\sqrt{1-4x^2}$, if
 $x \in \left(-\frac{1}{2\sqrt{2}}, \frac{1}{2\sqrt{2}}\right)$



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10. Differentiate $\sin^{-1}(4x\sqrt{1-4x^2})$ w. r. t. $\sqrt{1-4x^2}$, if
 $x \in \left(-\frac{1}{2\sqrt{2}}, \frac{1}{2\sqrt{2}}\right)$



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11. Differentiate $\sin^{-1}(4x\sqrt{1-4x^2})$ w. r. t. $\sqrt{1-4x^2}$, if
 $x \in \left(-\frac{1}{2\sqrt{2}}, \frac{1}{2\sqrt{2}}\right)$



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Exercise For Session 8

1. If $y = x^x$, show that $\left[\left(d^2 \frac{y}{dx^2} \right) - \frac{1}{y} \left(\frac{dy}{dx} \right)^2 - \frac{y}{x} = 0 \right]$



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2. If $y = A \cos(\log x) + B \sin(\log x)$ then prove that
 $x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} + y = 0$.



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3. If $y = x \log \left\{ \frac{x}{(a+bx)} \right\}$, then show that $x^3 \frac{d^2y}{dx^2} = \left(x \frac{dy}{dx} - y \right)^2$.



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4. Find the second order derivative of the following functions

If $y = \log \left[x + \sqrt{x^2 + a^2} \right]$, show that $(x^2 + a^2) \frac{d^2y}{dx^2} + x \frac{dy}{dx} = 0$



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5. If $y = \left[\log\left(x + \sqrt{x^2 + 1}\right) \right]^2$ then show that $(x^2 + 1)y_2 + xy_1 = 0$



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6. If $x = at^2$, $y = 2at$, then $\frac{d^2y}{dx^2} = -\frac{1}{t^2}$ (b) $\frac{1}{2at^3}$ (c) $-\frac{1}{t^3}$ (d)
 $-\frac{1}{2at^3}$



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7. $x = a \cos^3 \theta$, $y = a \sin^3 \theta$ then find $\frac{d^2y}{dx^2}$



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8. If $x = \tan\left(\frac{1}{a} \log y\right)$, show that $(1 - x^2) \frac{d^2y}{dx^2} + (2x - a) \frac{dy}{dx} = 0$



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9. If $x = a \cos \theta + b \sin \theta$ and $y = a \sin \theta - b \cos \theta$, then prove that

$$y^2 \frac{d^2y}{dx^2} - x \frac{dy}{dx} + y = 0$$



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10. If $y = \frac{ax + b}{cx + d}$, then prove that $2y_1y_3 = 3(y_2)^2$



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11. If $x = f(t)$ and $y = \phi(t)$, prove that $\frac{d^2y}{dx^2} = \frac{f_1\phi_2 - f_2\phi_1}{f_1^3}$ where

suffixes denote differentiation w. r. t. t.



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12. If $x = \sin t$, $y = \sin Kt$ then show that $(1 - x^2)y_2 - xy_1 + K^2y = 0$



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13. If $x^2 + y^2 = 1$, then

a. $yy'' - 2(y')^2 + 1 = 0$

b. $yy'' + (y')^2 + 1 = 0$

c. $yy'' + (y')^{-2} - 1 = 0$

d. $yy'' + 2(y')^2 + 1 = 0$



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14. Let $f(x)$ be polynomial function of degree 2 such that $f(x) > 0$ for all $x \in R$. If $g(x) = f(x) + f'(x) + f''(x)$ for all x , then



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Exercise For Session 9

1. If $f(x)$ $g(x)$ and $h(x)$ are three polynomials of degree 2 and $\Delta = \begin{vmatrix} f(x) & g(x) & h(x) \\ f'(x) & g'(x) & h'(x) \\ f''(x) & g''(x) & h''(x) \end{vmatrix}$ then $\Delta(x)$ is a polynomial of degree (dashes

denote the differentiation).



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2. If f , g , and h are differentiable functions of x and $(\delta) =$

$$\begin{vmatrix} f & g & h \\ (xf)' & (xg)' & (xh)' \\ (x^2f)'' & (x^2g)'' & (x^2h)'' \end{vmatrix}$$

prove that $\delta' = \begin{vmatrix} f & g & h \\ f' & g' & h \\ (x^3f'')' & (x^3g'')' & (x^3h'')' \end{vmatrix}$



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3. Find $\frac{dy}{dx}$ at $x = -1$, when

$$(\sin y)^{\sin\left(\left(\frac{\pi}{2}\right)x\right)} + \frac{\sqrt{3}}{2}\sec^{-1}(2x) + 2^x \tan(\ln(x+2)) = 0$$



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Exercise For Session 10

1. The functions $f(x) = e^x + x$, being differentiable and one-one, has a differentiable inverse $f^{-1}(x)$. The value of $\frac{d}{dx} f^{-1}$ at the point $f(\log 2)$ is

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2. Let $g(x)$ be the inverse of an invertible function $f(x)$, which is differentiable for all real x . Then $g^{f(x)}$ equals. $-\frac{f^x}{(f'(x))^3}$ (b)
 $\frac{f'(x)f^x - (f'(x))^3}{f'(x)}$ (c) $\frac{f'(x)f^x - (f'(x))^2}{(f'(x))^2}$ (d) none of these

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3. Let $g(x)$ be the inverse of an invertible function $f(x)$ which is differentiable at $x = c$. Then $g'(f(x))$ equal. `

A. $f'(c)$

B. $\frac{1}{f'(c)}$

C. $f(c)$

D. None of these

Answer: B



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4. If $f(x) = x + \tan x$ and f is the inverse of g , then $g'(x)$ equals

A. $\frac{1}{[g(x) - x]^2}$

B. $\frac{1}{2 - [g(x) - x]^2}$

C. $\frac{1}{2 + [g(x) - x]^2}$

D. None of these

Answer: C



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