



# MATHS

# **BOOKS - ARIHANT MATHS**

# ELLIPSE

#### Examples

1. If PSQ is a focal chord of the ellipse  $16x^2 + 25y^2 = 400$  such that SP = 8, then find the length of SQ is (a) 2 (b) 1 (c)  $\frac{8}{9}$  (d)  $\frac{16}{9}$ 



**3.** If the distance between the directrices is thrice

the distance between the foci, then find eccentricity of the ellipse.









**6.** An ellipse having foci at (3, 3) and (-4, 4) and

passing through the origin has eccentricity equal

to (a)
$$rac{3}{7}$$
 (b)  $rac{2}{7}$  (c)  $rac{5}{7}$  (d)  $rac{3}{5}$ 

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7. Find the lengths of major and minor axes, the coordinate of foci, vertices and the eccentricity of the ellipse  $3x^2 + 2y^2 = 6$ . Also the equation of the directries.



8. Find the equation of the ellipse whose focus is (1, -1), the corresponding directrix is x - y - 3 = 0, and eccentricity is  $\frac{1}{2}$ .

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9. If the line lx + my + n = 0 cuts the ellipse  $\left(\frac{x^2}{a^2}\right) + \left(\frac{y^2}{b^2}\right) = 1$  at points whose eccentric angles differ by  $\frac{\pi}{2}$ , then find the value of  $\frac{a^2l^2 + b^2m^2}{n^2}$ .

10. If the chord, joining two points whose eccentric angles are  $\alpha$  and  $\beta$ , cuts the major axis of the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  at a distance c from the centre, then  $\tan \alpha / 2$ .  $\tan \beta / 2$  is equal to



# 11. If the angle between the straight lines joining foci and the ends of minor axis of the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ is $\frac{\pi}{2}$ then the eccentricity is



12. Find the equation of the ellipse refer to its

centre whose minor axis is equal to

distance between the foci and latus rectum is 10.

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**13.** The ratio of any triangle PQR inscribed in an ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  and that of triangle formed by the corresponding points on the auxilliary circle is  $\frac{b}{a}$ .

**14.** If the extremities of a line segment of length I moves in two fixed perpendicular straight lines, then the locus of the point which divides this line segment in the ratio 1:2 is-



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15. Find the lengths of and the equations to the focal radii drawn to the point  $(4\sqrt{3}, 5)$  of the ellipse  $25x^2 + 16y^2 = 1600$ 

16. Find the position of the point (4,-3) relative to

the ellipse  $5x^2 + 7y^2 = 140$ .



18. If straight line lx + my + n = 0 is a tangent

of the ellipse  $rac{x^2}{a^2}+rac{y^2}{b^2}=1,$  then prove that  $a^2l^2+b^2m^2=n^2.$ 

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19. If the straight line  $x\cos\alpha + y\sin\alpha = p$ touches the curve  $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ , then prove that  $a^2\cos^2\alpha - b^2\sin^2\alpha = p^2$ .

20. The values of  $\lambda$  for which the line y=x+ $\lambda$  touches the ellipse  $9x^2+16y^2=144$  , are

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**21.** If the line  $3x + 4y = \sqrt{7}$  touches the ellipse

 $3x^2+4y^2=1,\,$  then the point of contact is

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22. Find the equations of the tangents to the ellipse  $3x^2 + 4y^2 = 12$  which are perpendicular

to the line 
$$y + 2x = 4$$
.  
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23. Find the locus of the foot of the perpendicular  
drawn from the center upon any tangent to the  
ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ .  
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24. Find the point on the ellipse  $16x^2 + 11y^2 = 256$  where the common tangent to it and the circle  $x^2 + y^2 - 2x = 15$  touch.







**26.** Find the slope of a common tangent to the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  and a concentric circle of radius  $r_{\cdot}$ 

**27.** Prove that the product of the perpendicular from the foci on any tangent to an ellipse is equal

to the square of the semi-minor axis.



28. The locus of the middle point of the portion of a tangent to the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  included between axes is

**29.** Show that the tangents at the extremities of the latus rectum of an ellipse intersect on the corresponding directrix.



**30.** The normal at an end of a latus rectum of the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  passes through an end of the minor axis if (A)  $e^4 + e^2 = 1$  (B)  $e^3 + e^2 = 1$  (C)  $e^2 + e = 1$  (D)  $e^3 + e = 1$ 

**31.** The line lx + my + n = 0 is a normal to the

ellipse  $rac{x^2}{a^2}+rac{y^2}{b^2}=1$  . then prove that  $rac{a^2}{l^2}+rac{b^2}{m^2}=rac{\left(a^2-b^2
ight)^2}{n^2}$ 



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**32.** A normal inclined at  $45^{\circ}$  to the axis of the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  is drawn. It meets the x-axis & the y-axis in P & Q respectively. If C is the centre of the ellipse, show that the area of triangle CPQ is  $\frac{(a^2 - b^2)^2}{2(a^2 + b^2)}$ 

#### sq units



**33.** Any ordinate MP of an ellipse meets the auxillary circle in Q. Ptove that the locus of the point of intersection of the normals at P and Q is the circle  $x^2 + y^2 = (a + b)^2$ .

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**34.** Prove that the chord of contact of tangents drawn from the point (h,k) to the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  will subtend a right angle at the

centre, if

$$rac{h^2}{a^4} + rac{k^2}{b^4} = rac{1}{a^2} + rac{1}{b^2}$$



**35.** Show that the locus of the middle points of chord of an ellipse which paas through a fixed

point, is another ellipse



**36.** Show that the tangents at the ends of conjugate diameters of the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  intersect on the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 2$ .

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**37.** Tangents at right angle are drawn to the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ . Show that the focus of the

middle points of the chord of contact is the curve

$$\left(rac{x^2}{a^2}+rac{y^2}{b^2}
ight)^2=rac{x^2+y^2}{a^2+b^2},$$

**38.** A ray emanating from the point (-3,0) is incindent on the ellipse  $16x^2 + 25y^2 = 400$  at the point p with ordinate 4. Find the equation of the reflected ray after first reflection.







**40.** Point 'O' is the centre of the ellipse with major axis AB & minor axis CD. Point F is one focus of the ellipse. If OF = 6 & the diameter of the inscribed circle of triangle OCF is 2, then find the product (AB). (CD)

A. 52

B. 65

C. 78

D. None of these

Answer: A::B::C



**41.** Let  $P_i$  and  $P_i$ ' be the feet of the perpendiculars drawn from the foci SandS' on a tangent  $T_i$  to an ellipse whose length of semimajor axis is 20. If  $\sum_{i=0}^{10} (SP_i)(S'\Pi') = 2560$ , then the value of eccentricity is (a)  $\frac{1}{5}$  (b)  $\frac{2}{5}$  (c)  $\frac{3}{5}$  (d)  $\frac{4}{5}$ 

A. 
$$\frac{1}{5}$$
  
B.  $\frac{2}{5}$   
C.  $\frac{3}{5}$ 

#### Answer: B::C



42. The coordinates of the vertices BandC of a triangle ABC are (2, 0) and (8, 0), respectively. Vertex A is moving in such a way that  $4\frac{\tan B}{2}\frac{\tan C}{2} = 1$ . Then find the locus of AA.  $\frac{x-5^2}{25} + \frac{y^2}{16} = 1$ B.  $\frac{(x-5)^2}{16} + \frac{y^2}{9} = 1$ 

C. 
$$rac{{{\left( {x - 5} 
ight)}^2 }}{{25}} + rac{{{y^2}}}{9} = 1$$
  
D.  $rac{{{\left( {x - 5} 
ight)}^2 }}{{16}} + rac{{{y^2}}}{{25}} = 1$ 

#### Answer: A::B



**43.** A ray emanating from the point (0,6) is incident on the ellipse  $25x^2 + 16y^2 = 1600$  at the point P with ordinate S. After reflection, ray cuts the Y-axis at B. The length of PB is

B. 7

C. 12

D. 13

Answer: A::B::C::D

44. If the ellipse 
$$rac{x^2}{4}+y^2=1$$
 meets the ellipse  $x^2+rac{y^2}{a^2}=1$  at four distinct points and  $a=b^2-5b+7,$  then  $b$  does not lie in

(a) [4, 5] (b)  $(-\infty, 2) \cup (3, \infty)$  (c)  $(-\infty, 0)$  (d) [2, 3]A. (1,4)B.  $(-\infty, 2) \cup (3, \infty)$ C. (2, 3)D. None of these

Answer: B



**45.** The normal at a variable point P on the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  of eccentricity e meets the axes of the ellipse at QandR. Then the locus of the midpoint of QR is a conic with eccentricity e' such that (a)e' is independent of e (b) e' = 1 (c) e' = e (d)  $e' = \frac{1}{e}$ 

A. e' is indipendant of e

B. e'=1

C. e'=e

D. e'=1/e

#### Answer:



**46.** If the curves  $\frac{x^2}{4} + y^2 = 1$  and  $\frac{x^2}{a^2} + y^2 = 1$ for a suitable value of a cut on four concyclic points, the equation of the circle passing through these four points is

A. 
$$x^2 + y^2 = 8$$

$$\mathsf{B.}\,x^2+y^2=4$$

$$\mathsf{C}.\,x^2=y^2=2$$

D. 
$$x^2+y^2=1$$

Answer: A::B



**47.** If P is the length of perpendicluar drawn from the origin to any normal to the ellipse  $\frac{x^2}{25} + \frac{y^2}{16} = 1$ , then the maximum value of p is

A. 5

B. 4

D. 1

#### Answer: D



**48.** Consider the ellipse  $\frac{x^2}{f(k^2+2k+5)} + \frac{y^2}{f(k+11)} = 1$ . If f(x) is a positive decr4easing function, then the set of values of k for which the major axis is the x-axis is (-3, 2). the set of values of k for which the major axis is the y-axis is  $(-\infty, 2)$ . the set of values of k for which the major axis is the y-axis is  $(-\infty, 2)$ .



Answer: B::C

**49.** If a tangent of slope 2 of the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  is normal to the circle  $x^2 + y^2 + 4x + 1 = 0$ , then the maximum value of ab is 4 (b) 2 (c) 1 (d) none of these

A. 1

B. 2

C. 4

D. 8

#### Answer: D



50. Extremities of the latus rectum of the ellipses

 $rac{x^2}{a^2}+rac{y^2}{b^2}=1(a>b)$  having a major axis 2a lies on

a.  $x^2 = a(a-y)$ b. x = a(a + y)c.  $y^2 = a(a + x)$ d.  $y^2 = a(a - x)$ A.  $x^2 = a(a - y)$ B. x=a(a+y)C.  $y^2 = a(a + x)$ 

Answer: A::B

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51. The locus of the image of the focus of the ellipse  $\frac{x^2}{25} + \frac{y^2}{9} - 1$ , (a > b), with respect to any of the tangents to the ellipse is  $(x + 4)^2 + y^2 = 100$  (b)  $(x + 2)^2 + y^2 = 50$  $(x - 4)^2 + y^2 = 100$  (d)  $(x + 2)^2 + y^2 = 50$ 

A.  $(x+4)^2 + y^2 = 100$ 

C. 
$$(x-4)^2 + y^2 = 100$$

D. 
$$\left(x-20^2+y^2=50
ight)$$

Answer: A::B::D

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52. A tangent to the ellipse  $4x^2 + 9y^2 = 36$  is cut by the tangent at the extremities of the major axis at T and  $T^1$ , the circle on  $TT^1$  as diameter passes through the point

A. 
$$(-\sqrt{5}, 0)$$
  
B.  $(\sqrt{5}, 0)$   
C.  $(\sqrt{3}, 0)$   
D.  $(-\sqrt{3}, 0)$ 

#### Answer: A::B::D

**53.** Consider the ellipse 
$$\frac{x^2}{\tan^2 \alpha} + \frac{y^2}{\sec^2 \alpha} = 1$$
  
where  $\alpha \in \left(0, \frac{\pi}{2}\right)$ . Which of the following quantities would vary as  $\alpha$  varies?
- A. (a)degree of flatness
- B. (b)ordinate of the vertex
- C. (c)coordinate of the foci
- D. (d)length of latusrectum

# Answer: A::C::D

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**54.** Let  $A(\alpha)$  and  $B(\beta)$  be the extremities of a chord of an emplise. If the slope of AB is equal to

the slope of the tangent at a point  $C(\theta)$  on the

ellipse, then alpha is equal to

A. 
$$\displaystyle rac{lpha+eta}{2}$$
  
B.  $\displaystyle rac{lpha-eta}{2}$   
C.  $\displaystyle rac{lpha+eta}{2}+\pi$   
D.  $\displaystyle \displaystyle rac{lpha-eta}{2}-\pi$ 

Answer: A::C



**55.** A series of concentric ellipses  $E_1, E_2, E_3..., E_n$  are drawn such that E touches the extremities of the major axis of  $E_{n-1}$ , and the foci of  $E_n$  coincide with the extremities of minor axis of  $E_{n-1}$  If the eccentricity of the ellipses is independent of n, then the value of the eccentricity, is

A. (a) 
$$\frac{3-\sqrt{5}}{2}$$
  
B. (b)  $\frac{\sqrt{5}-1}{2}$   
C. (c)  $\frac{2-\sqrt{3}}{2}$   
D. (d)  $\frac{\sqrt{3}-1}{2}$ 

Answer: A::B



# 56. If eccentricity of curve is 1 then the curve is

A. a parabola

B. an ellipse

C. a hyperbola

D. a rectangular hyperbola

Answer: A::B::C

....

**57.** A series of concentric ellipse  $E_1, E_2, E_3, \ldots, E_n$  is constructed as follows: Ellipse  $E_n$  touches the extremities of the major axis of  $E_{n-1}$  and have its focii at the extremities of the minor axis of  $E_{n-1}$  If equation of ellipse  $E_1$  is  $\frac{x^2}{9} + \frac{y^2}{16} = 1$ , then equation pf ellipse  $E_3$  is

A. 
$$rac{x^2}{9}+rac{y^2}{16}=1$$
  
B.  $x^2+y^{49}=1$   
C.  $rac{x^2}{25}+rac{y^2}{41}=1$ 

D. 
$$rac{x^2}{16} + rac{y^2}{25} = 1$$

Answer: A::B::D

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**58.** Consider an ellipse  $E, \frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ , centered at point Oand having AB and CD as its major and minor axes, respectively. If  $S_1$  is one of the focus of the ellipse, the radius of the incircle of triangle  $OCS_1$  is 1 unit, and  $OS_1 = 6$  units, then the value of  $\displaystyle \frac{a-b}{2}$  is\_\_\_\_\_



**59.** An ellipse E,  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ , centred at point O has AB and CD as its major and minor axes, respectively. Let  $S_1$  be one of the foci of the ellipse, the radius of the incircle of traingle  $OCS_1$ be 1 unit, adn  $OS_1 = 6$  units

The perimeter of  $\Delta OCS_1$  is

A. (a)10

B. (b)15

C. (c)20

D. (d)25

Answer: A::B::C

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60. Find the derivative of cosecx cotx .



**61.** If the normals at the four points  $(x_1, y_1), (x_2, y_2), (x_3, y_3)$  and  $(x_4, y_4)$  on the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  are concurrent, then the value of  $\left(\sum_{i=1}^4 x_i\right) \left(\sum_{i=1}^4 \frac{1}{x_i}\right)$ 

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AA7 4 8

62. If 
$$x, y \in R$$
, satisfies the equation  $\frac{(x-4)^2}{4} + \frac{y^2}{9} = 1$  , then the difference between the largest and the smallest value of the expression  $\frac{x^2}{4} + \frac{y^2}{9}$  is\_\_\_\_\_

**63.** Statement 1 Feet of prependiculars drawn from foci of an ellipse  $4x^2 + y^2 = 16$  on the line  $2\sqrt{3}x + y = 8$  lie on the circle  $x^2 + y^2 = 16$ Statement 2 If prependiculars are from foci of an ellipse to its any tangent, the feet of these perpendicular lie on director circle of the ellipse.



**64.** The line lx+my=n is a normal to the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ 





**66.** The line lx+my=n is a normal to the ellipse  $rac{x^2}{a^2} + rac{y^2}{b^2} = 1$ 

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**67.** An ellipse slides between two perpendicular straight lines.

Then identify the locus of its center.

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**68.** Triangles are formed by pairs of tangent drawn

from any point on the ellipse  $a^2x^2+b^2y^2=\left(a^2+b^2
ight)$  to the ellipse  $rac{x^2}{a^2}+rac{y^2}{b^2}=1$  and the chord of contact. Show that the

orthocentre of each such triangles lies triangle

lies on the ellipse.





**74.** Two concentric ellipses are such that the foci of one are on the other and their major axes are equal. Let *eande'* be their eccentricities. Then. the quadrilateral formed by joining the foci of the two ellipses is a parallelogram the angle  $\theta$ between their axes is given by  $heta = \cos^{-1} \sqrt{rac{1}{e^2} + rac{1}{e^{\,'2}}} = rac{1}{e^{2}e^{\,'2}}$ lf  $e^2 + e^{'2} = 1$ , then the angle between the axes of the two ellipses is  $90^0$  none of these

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**75.** Find the derivative of  $(x^2+1)\cos x$ 



an angle theta.

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$$\frac{\sec x - 1}{\sec x + 1}$$

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**Exercise For Session 1** 

**1.** If the length of the major axis of an ellipse in 3 times the length of minor axis , then its eccentricity is

A. 
$$\frac{1}{\sqrt{2}}$$
  
B. 
$$\frac{1}{\sqrt{3}}$$
  
C. 
$$\frac{2\sqrt{2}}{3}$$

D.  $\frac{2\sqrt{2}}{5}$ 

### Answer: C







represents an ellipse, if

A. a < 4

 ${\sf B.}\,a>4$ 

 ${\sf C.4} < a < 10$ 

D. a > 10

# Answer: A



**3.** Find the eccentricity of an ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  whose latus rectum is half of its major axis.

A. 1/sqrt3

B. 1/sqrt2

C. sqrt3/2

D. 
$$\sqrt{\left(\frac{2}{3}\right)}$$







**5.** If the distance between the foci of an ellipse is equal to length of minor axis, then its eccentricity .

is

A. 
$$\frac{1}{2}$$
  
B.  $\frac{1}{\sqrt{2}}$   
C.  $\frac{1}{3}$   
D.  $\frac{1}{\sqrt{3}}$ 

## Answer: B



6. The eccentric angle of a point on the ellipse  $rac{x^2}{6}+rac{y^2}{2}=1$  whose distance from the centre of

the ellipse is 2, is

A. 
$$-\frac{\pi}{4}$$
  
B.  $\frac{\pi}{4}$   
C.  $\frac{3\pi}{2}$   
D.  $\frac{5\pi}{3}$ 

#### Answer: A::B



7. If  $\tan \theta_1 \cdot \tan \theta_2 = -\frac{a^2}{b^2}$  then the chord Joining two points  $\theta_1$  and  $\theta_2$  on the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  will subtend a right angle at (A) focus (B) centre (C) end of the major axis (D) end of the major axis

A. focus

B. center

C. end of major axis

D. end of minor axis

#### Answer: B

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# 8. If the eccentricities of the two ellipse $\frac{x^2}{169} + \frac{y^2}{25} = 1$ and $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ and equal , then the value $\frac{a}{b}$ , is

A. 
$$\frac{3}{13}$$
  
B.  $\frac{6}{13}$ 

C. 
$$\frac{13}{5}$$
  
D.  $\frac{13}{6}$ 

#### Answer: C



**9.** The ratio of the area of triangle inscribed in ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  to that of triangle formed by the corresponding points on the auxiliary circle is 0.5. Then, find the eccentricity of the ellipse.

A. 
$$\frac{1}{2}$$
  
B. 
$$\frac{\sqrt{3}}{2}$$
  
C. 
$$\frac{1}{\sqrt{2}}$$
  
D. 
$$\frac{1}{\sqrt{3}}$$

#### **Answer: B**



A. 
$$\frac{2}{9}$$
  
B.  $\frac{4}{9}$   
C.  $\frac{8}{9}$   
D.  $\frac{16}{9}$ 

# Answer: D

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11. Let P be a variable point on the ellipse 
$$\frac{x^2}{25} + \frac{y^2}{16} = 1$$
 with foci at S and S'. If A be the

area of triangle PSS' then the maximum value of

A, is

A. 12 sq units

B. 24 sq units

C. 36 sq units

D. 48 sq units

Answer: A



**12.**  $S_1 and S_2$  are the foci of an ellipse of major axis of length 10 units, and P is any point on the ellipse such that the perimeter of triangle  $PS_1$  is 15. Then the eccentricity of the ellipse is 0.5 (b) 0.25 (c) 0.28 (d) 0.75

A. 
$$\frac{1}{2}$$
  
B.  $\frac{1}{4}$   
C.  $\frac{7}{25}$   
D.  $\frac{3}{4}$ 

#### Answer: A



**13.** Find the latus rectum, eccentricity, coordinates of the foci and the length of axes of the ellipse

$$4x^2 + 9y^2 - 8x - 36y + 4 = 0.$$

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**14.** The distance between the foci of an ellipse is 10 and its latus rectum is 15, find its equation referred to its axes as axes of coordinates.



15. Find the equation of the ellipse whose axes are parallel to the coordinate axes having its centre at the point (2, -3) one focus at (3, -3) and vertex at (4, -3).

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16. Find the equation of the ellipse whose foci are

 $(2,3),(\,-2,3)$  and whose semi-minor axes is  $\sqrt{5}$ 



17. Show that the equation  $(10x - 5)^2 + (10y - 5)^2 = (3x + 4y - 1)^2$  represents an ellipse, find the eccentricity of the ellipse.



**Answer: B** 



18. The locus of the latusrectum of the family of

ellipse  $b^2 + y^2 = a^2 b^2$  is

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**Exercise For Session 2** 

1. The number of values of c such that the straight line y = 4x + c touches the curve  $\frac{x^2}{4} + \frac{y^2}{1} = 1$  is (a) 0 (b) 1 (c) 2 (d) infinite

A. 0

B. 1

C. 2

D. infinite

Answer: C

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**2.** If any tangent to the ellipse 
$$rac{x^2}{a^2}+rac{y^2}{b^2}=1$$
 cuts

off intercepts of length h and k on the axes, then

 $rac{a^2}{h^2}+rac{b^2}{k^2}=~$  (A) 0 (B) 1 (C) -1 (D) Non of these

A. -1

B. 0

C. 1

D. None of these

Answer: C

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**3.** The equations of the tangents to the ellipse  $3x^2 + y^2 = 3$  making equal intercepts on the axes are

A. 
$$y=\pm x\pm 2$$
$\texttt{B.}\, y=~\pm~x~\pm~4$ 

C. 
$$y=\pm x\pm \sqrt{30}$$

D. 
$$y=~\pm x\pm \sqrt{35}$$

### **Answer: A**



4. If 
$$\frac{x}{a} + \frac{y}{b} = \sqrt{2}$$
 touches the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ , then find the eccentric angle  $\theta$  of

point of contact.

B.  $45^{\circ}$ 

 $\mathsf{C.}\,60^{\,\circ}$ 

D.  $90^{\circ}$ 

Answer: B

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5. The number of values of  $\phi \in [0, 2\pi]$  for which the line  $2x \cos \phi + 3y \sin \phi = 6$  touches the ellipse  $4x^2 + 9y^2 = 36$  is a) four b) two c)one d) infinite A. 1

B. 2

C. 4

D. infinite

### **Answer: D**



A. x+y+4=0

B. x-y+7=0

C. 2x+3y+8=0

D. None of these

Answer: D

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7. If the normal at any point P on the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  meets the axes at G and g respectively, then find the ratio PG: Pg.

A. a:b

B.  $a^2: b^2$ 

 $\mathsf{C}.\,b\!:\!a$ 

 $\mathsf{D}.\,b^2 \colon a^2$ 

Answer: D

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**8.** The number of distinct normal lines that can be drawn to the ellipse  $rac{x^2}{169}+rac{y^2}{25}=1$  from the point P(0,6) is

B. two

C. three

D. four

Answer: C

9. If a tangent of slope 2 of the ellipse 
$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$
 is normal to the circle  $x^2 + y^2 + 4x + 1 = 0$ , then the maximum value of  $ab$  is

A. 4

B. 2

C. 1

D. none of these

### **Answer: A**





11. The line  $5x - 3y = 8\sqrt{2}$  is a normal to the ellipse  $\frac{x^2}{25} + \frac{y^2}{9} = 1$ , If 'theta' be eccentric angle of the foot of this normal then 'theta' is equal to

A. 
$$\frac{\pi}{6}$$
  
B.  $\frac{\pi}{4}$   
C.  $\frac{\pi}{3}$   
D.  $\frac{\pi}{2}$ 

### Answer: B



12. Find the derivative of  $(x + \cos x)(x - \tan x)$ 

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**13.** If the normal at any point P on the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  cuts the major and minor axes in L and M respectively and if C is the centre of the ellipse, then  $a^2 CL^2 + b^2 CM^2$  is equal to (A) (a - b) (B)  $(a^2 - b^2)^2$  (C) (a + b) (D)  $(a^2 + b^2)$ 



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15. The tangent and normal at any point P of an ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  cut its major axis in point Q and R respectively. If QR=a prove that the eccentric angle of the point P is given by  $e^2 \cos^2 \theta + \cos \theta - 1 = 0$ 

**1.** Find the angle between the pair of tangents from the point (1,2) to the ellipse  $3x^2 + 2y^2 = 5$ .

A. 
$$\tan^{-1}\left(\frac{12}{5}\right)$$
  
B.  $\tan^{-1}\left(\frac{6}{\sqrt{5}}\right)$   
C.  $\tan^{-1}\left(\frac{12}{\sqrt{5}}\right)$   
D.  $\tan^{-1}\left(\sqrt{5}\right)$ 

# ( •

## Answer: C

2. If the chords of contact of tangents from two

poinst  $(x_1, y_1)$  and  $(x_2, y_2)$  to the ellipse  $rac{x^2}{a^2} + rac{y^2}{b^2} = 1$  are at right angles, then find the value of  $rac{x_1 x_2}{y_1 y_2}$ .



### Answer: C

3. If the tangents from the point  $(\lambda,3)$  to the ellipse  $\frac{x^2}{9} + \frac{y^2}{4} = 1$  are at right angles then  $\lambda$  is

- A.  $\pm 1$
- $\mathsf{B.}\pm2$
- $\mathsf{C}.\pm 3$
- $\mathsf{D}.\pm4$

### Answer: B



4. The eccentric angle of one end of a diameter of  $x^2 + 3y^2 = 3$  is  $\frac{\pi}{6}$ , then the eccentric angle of the other end will be



### Answer: B





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D. (1,1)

## Answer: D



7. The locus of the point of intersection of two prependicular tangents of the ellipse  $rac{x^2}{9}+rac{y^2}{4}=1$  is A.  $x^2 + y^2 = 4$ B.  $x^2 + y^2 = 9$ C.  $x^2 + y^2 = 13$ D.  $x^2 + y^2 = 5$ 



**10.** Find the derivative of  $(x + \sec x)$ 

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11. The locus of the mid-points of the chords of the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  which pass through the positive end of major axis, is.

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12. If chord of contact of the tangents drawn from the point (lpha,eta) to the ellipse  $rac{x^2}{a^2}+rac{y^2}{b^2}=1$ 



incident on the ellipse  $9x^2 + 4y^2 = 36$  at the point P with abscissa 2. find the equation of the reflected ray after first reflection.

## Exercise Single Option Correct Type Questions

**1.** Given f is increasing, the equation 
$$\frac{x^2}{f(2a)} + \frac{y^2}{f(a^2-3)} = 1$$
 represents an ellipse with X-axis as major axis if

A. [-1,3]

B. [1,3]

C. (-1,3)

D. (0,5)

## Answer: C



2. If 
$$\frac{x^2}{f(4a)} + \frac{y^2}{f(a^2-5)}$$
=1 represents an ellipse with major axis as Y-axis and f is a decreasing function,then

A.  $lpha\in(1\infty,1)$ 

B.  $lpha\in(5,\infty)$ 

 $\mathsf{C}.\,\alpha \in (1,\,4)$ 

D.  $lpha\in(\,-1,\,5)$ 

### Answer: D



- 3. The curve represents by the equation  $rac{x^2}{\sin\sqrt{2}-\cos\sqrt{3}}+rac{y^2}{\sin\sqrt{3}-\cos\sqrt{2}}=1$  is
  - A. (a) an ellipse with foci on X-axis
  - B. (b) an ellipse on focii Y-axis
  - C. (c) a hyperbola with foci on X-axis
  - D. (d) an hyperbola with foci on Y-axis

## Answer: A



4. The maximum distance of the centre of the ellipse  $\frac{x^2}{16} + \frac{y^2}{9} = 1$  from the chord of contact of mutually perpendicular tangents of the ellipse is

A. (a) 144/5

B. (b) 16/5

C. (c) 
$$\frac{9}{5}$$





7. C is the centre of the ellipse  $rac{x^2}{16}+rac{y^2}{9}=1$  and A and B are two points on the ellipse such that  $\angle ACB=90^\circ$ , then  $rac{1}{\left(CA\right)^2}+rac{1}{\left(CB\right)^2}=$ 

A. (a) 
$$\frac{7}{12}$$
  
B. (b)  $\frac{12}{7}$   
C. (c)  $\frac{25}{144}$   
D. (d)  $\frac{144}{25}$ 

#### Answer: C



8. Let (lpha,eta) be a point from which two perpendicular tangents can be drawn to the ellipse  $4x^2 + 5y^2 = 20$ . If F = 4lpha + 3eta, then

A. (a) 
$$-15 \leq F \leq 15$$

B. (b)  $F \geq 0$ 

C. (c)  $-5 \leq F \leq 20$ 

D. (d)  $F \leq -5\sqrt{5} \, \, {
m or} \, \, F \geq 5\sqrt{5}$ 

#### Answer: A



9. If  $a = [t^2 - 3t + 4]$  and b = [3 + 5t], where [.] donates the greatest integer function, then the latusrectum of the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  at  $t = \frac{3}{2}$  is

A. 20

B. 10

C. 
$$\frac{1}{5}$$
  
D.  $\frac{1}{10}$ 

## Answer: C



10. If the line x + 2y + 4 = 0 cutting the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  in points whose eccentric angles are  $30^{\circ}$  and  $60^{\circ}$  subtends right angle at the origin then its equation is

A. 
$$rac{x^2}{8}+rac{y^2}{4}=1$$
  
B.  $rac{x^2}{16}+rac{y^2}{4}=1$   
C.  $rac{x^2}{4}+rac{y^2}{16}=1$ 

D. None of the above

## Answer: B

11. Find the perimeter of the parallelogram whose

adjacent sides are 3 and 7.

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12. Write the equation of tangent to the ellipse

$$rac{x^2}{25}+rac{y^2}{16}=1$$
 at any point  $P.$ 

13. Write the parametric form of equation of tangents drawn from any point on the circle  $x^2 + y^2 = 25$ 

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14. the equation of the chord of contact of the pair of tangents drawn to the ellipse  $4x^2 + 9y^2 = 36$  from the point (m, n) where  $m\dot{n} = m + n, m, n$  being nonzero positive integers, is

A. 2x + 9y = 18

B. 2x + 2y = 1

C. 
$$4x + 9y = 18$$

D. none of these

## Answer: C



**15.** 
$$x - 2y + 4 = 0$$
 is a common tangent to  $y^2 = 4x$  and  $\frac{x^4}{4} + \frac{y^2}{b^2} = 1$ . Then the value of b and the other common tangent are given by

A. 
$$b=\sqrt{3}, x+2y+4=0$$

B. 
$$b = 3, x + 2y + 4 = 0$$

C. 
$$b=\sqrt{3}, x+2y-4=0$$

D. 
$$b=\sqrt{3}, x-2y-4=0$$

Answer: A



16. Find the derivative of 
$$\displaystyle rac{x^2}{2} + x + 1$$

17. Find the derivative of secx + cosecx



ellipse. Then the eccentricity of the ellipse for which the length of latus-rectum of the ellipse and the parabola are same is

A. 
$$\sqrt{2}-1$$

- $\mathsf{B.}\,\sqrt{3}-1$
- C.  $2\sqrt{2}-2$
- D.  $3\sqrt{3}-5$

### Answer: A



#### Answer: B

21. The length of the common chord of the ellipse  $rac{\left(x-1
ight)^2}{9}+rac{\left(y-2
ight)^2}{4}=1$  and the circle  $\left(x-1
ight)^2+\left(y-2
ight)^2=1$  is (A) 2 (B)  $\sqrt{3}$  (C) 4 (D)

none of these

A. zero

B. one

C. three

D. eight

#### **Answer: A**


22. The eccentricity of ellipse $ax^2+by^2+2gx+2fy+c=0$  if its axis is

parallel to x-axis is

A. (a) 
$$\sqrt{\left(\frac{b-a}{b}\right)}$$
  
B. (b)  $\sqrt{\left(\frac{a+b}{b}\right)}$   
C. (c)  $\sqrt{\left(\frac{a+b}{a}\right)}$ 

D. (d)None of these

#### **Answer: A**



**23.** A circle has the same center as an ellipse and passes through the foci  $F_1andF_2$  of the ellipse, such that the two curves intersect at four points. Let P be any one of their point of intersection. If the major axis of the ellipse is 17 and the area of triangle  $PF_1F_2$  is 30, then the distance between the foci is

A. (a)13

B. (b)11

D. (d)7

#### **Answer: A**



24. The area of the rectangle formed by the perpendiculars from the centre of the standard ellipse to the tangent and normal at its point whose eccentric angles  $\frac{\pi}{4}$  is

A. 
$$rac{ig(a^2-b^2ig)ab}{a^2+b^2}$$
B.  $ig(rac{a^2-b^2}{a^2+b^2}ig)$ 

C. 
$$rac{ig(a^2+b^2ig)ab}{(a^2-b^2)}$$
  
D.  $rac{ig(a^2+b^2ig)}{(a^2-b^2)}$ 

### Answer: A



**25.** An ellipse is inscribed in a circle and a point within the circle is chosen at random. If the probability that this point lies outside the ellipse is  $\frac{2}{3}$  then the eccentricity of the ellipse is: (A)  $\frac{2\sqrt{2}}{3}$  (B)  $\frac{\sqrt{5}}{3}$  (C)  $\frac{8}{9}$  (D)  $\frac{2}{3}$ 



# Answer: A



**26.** An ellipse slides between two perpendicular straight lines. Then identify the locus of its center.

A. parabola

B. ellipse

C. hyperbola

D. circle

### Answer: D

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D. None of the above

## Answer: D



**28.** The equation of the locus of the middle point

of the portion of the tangent to the ellipse

 $rac{x^2}{16}+rac{y^2}{9}=1$  included between the co-ordinate

axes is the curve

A. 
$$9x^2 + 16y^2 = 4x^2y^2$$

B. 
$$16x^2 + 9y^2 = 4x^2y^2$$

C. 
$$3x^2 + 4y^2 = 4x^2y^2$$

D. 
$$9x^2 + 16y^2 = x^2y^2$$

#### Answer: A



**29.** The tangent at a point  $P(a \cos \varphi, b \sin \varphi)$  of the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  meets its auxiliary circle at two points, the chord joining which subtends a right angle at the center. Find the eccentricity of the ellipse.

A. 
$$e^2ig(1+\cos^2 hetaig)=1$$
  
B.  $e^2ig(\cos ec^2 heta+1ig)=1$   
C.  $e^2ig(1+\sin^2 hetaig)=1$   
D.  $e^2ig(1+\tan^2 hetaig)=1$ 

#### Answer: C



Exercise More Than One Correct Option Type Questions

1. The locus of extremities of the latus rectum of the family of ellipse  $b^2x^2 + a^2y^2 = a^2b^2$  is

A. 
$$x^2 - ay = a^2$$

B. 
$$x^2 - ay = b^2$$

C. 
$$x^2 + ay = a^2$$

D. 
$$x^2 + ay = b^2$$

# Answer: A::C



2. The distance of a point on the ellipse  $rac{x^2}{6}+rac{y^2}{2}=1$  from the center is 2. Then the

eccentric angle of the point is

A. 
$$\frac{\pi}{4}$$
  
B.  $\frac{3\pi}{4}$   
C.  $\frac{5\pi}{4}$   
D.  $\frac{7\pi}{4}$ 

## Answer: A::B::C::D



**3.** If the equation of family of ellipse is  $x^2 \sec^2 \theta + y^2 \cos ec^2 \theta = 1$ ,  $where \frac{\pi}{4} < \theta < \frac{\pi}{2}$ , then the locus of extremities of the latusrectum is

A. 
$$2y^2ig(1+x^2ig) = ig(1-x^2ig)^2$$
  
B.  $2x^2ig(1+y^2=ig(1-y^2ig)^2$   
C.  $2yig(1-x^2ig) = 1+x^2$ 

D. 
$$2y^2ig(1+x^2ig) = 1+x^4-2x^2$$

Answer: B::D

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**4.** Let  $F1, F_2$  be two focii of the ellipse and PT and PN be the tangent and the normal respectively to the ellipse at ponit P.then

A. (a)PN bisects  $\angle F_1PF_2$ 

B. (b)PT bisects  $\angle F_1 PF_2$ 

C. (c)PT bisects  $\angle(180^\circ-\angle F_1PF_2)$ 

# D. (d)None of above

# Answer: A::C



5. 
$$\displaystyle rac{x^2}{r^2-r-6}+rac{y^2}{r^2-6r+5}=1$$
 will represent

ellipse if r lies in the interval

A. 
$$(-\infty, -2)$$

 $\mathsf{B.}\left(1,\infty\right)$ 

 $\mathsf{C}.\left(3,\infty
ight)$ 

D.  $(5,\infty)$ 

# Answer: A::D



- 6. A laturectum of an ellipse is a line
  - A. passing through a focus
  - B. passing through the major axis
  - C. perpendicular to the major axis
  - D. parallel to the major axis

## Answer: A::B::C

7. An ellipse passes through the point (4, -1)and touches the line x + 4y - 10 = 0. Find its equation if its axes coincide with the coordinate axes.

A. 
$$x^2 + 64y^2 = 80$$
  
B.  $x^2 + 4y^2 = 20$   
C.  $x^2 + 20y^2 = 100$   
D.  $x^2 + 8y^2 = 40$ 

## Answer: A::B



8. If P is any point lying on the ellipse  $rac{x^2}{a^2}+rac{y^2}{b^2}=1$  , whose foci are S and S'. Let A. SP + S'P = 2a, if a > b $\mathsf{B}.\,SP+S'P=2b,\quad \mathrm{if}\ b>a$  $\operatorname{C.tan}\left(rac{ heta}{2}
ight) \operatorname{tan}\left(rac{\phi}{2}
ight) = rac{1-e}{e+1}$ D.

Answer: A::B::C



**9.** If (5, 12) and (24, 7) are the foci of an ellipse passing through the origin, then find the eccentricity of the ellipse.



## Answer: A::B



**10.** Find the  $4^{th}$  term in the following sequence

whose  $n^{th}$  term is  $a_n=n^2+3$ 

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A. foci are at (3, 1), (3, 9)

$$\mathsf{B.}\,e=\frac{4}{5}$$

C. center is (5, 3)

D. major axis axis is 6

Answer: A::B

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12. If the tangent to the ellipse  $x^2+4y^2=16$  at the point heta normal to the circle  $x^2+y^2-8x-4y=0$  then heta is equal to

A.  $\frac{\pi}{2}$ B.  $\frac{\pi}{4}$ 

C. 0

# Answer: A::C

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**13.** The product of eccentricities of two conics is unity, one of them can be a/an

A. parabola

B. ellipse

C. hyperbola

D. circle

## Answer: A::B::C



14. The parametric  $\angle \alpha$  where  $-\pi < \alpha \leq \pi$  of the point on the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  at which the tangent drawn cuts the intercept of minimum length on the coordinates axes, is/are

A. 
$$\tan - \sqrt{\frac{b}{a}}$$
  
B.  $-\tan(-1)\sqrt{\frac{b}{a}}$   
C.  $\pi - \tan^{-1}\sqrt{\frac{b}{a}}$ 

D. 
$$\pi + an^{-1} \sqrt{rac{b}{a}}$$

# Answer: A::B::C





A. 
$$\frac{\pi}{12}$$
  
B.  $\frac{\pi}{6}$   
C.  $\frac{5\pi}{12}$ 

# Answer: A::C

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Exercise Passage Based Questions

1. A conic is represented by  $C\equiv 9x^2+4xy+6y^2-22x-16y+9=0$  Q.

The centre of conic C is

A. (0,0)

B. (1,0)

C. (0,1)

D. (1,1)

Answer: D

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3. A conic is represented by  $C\equiv 9x^2+4xy+6y^2-22x-16y+9=0$  Q.

The centre of conic C is

A. (a) (0, 0)B. (b) (1, 0)C. (c) (0, 1)

D. (d) (1, 1)

Answer: A



**4.** An ellipse E has its center C(3,1), focus at (3,6) and passing through the point P(7,4) Q. If the normal at a variable point on the ellipse (E) meets its exes in Q and R, then the locus of the mispoint of QR is a conic with eccentricity  $(e_1)$ , then

A. 20

B.45

C. 40

D. 90

#### Answer: A

**5.** An ellipse E has its center C(3,1), focus at (3,6) and passing through the point P(7,4) Q. If the normal at a variable point on the ellipse (E) meets its exes in Q and R, then the locus of the mispoint of QR is a conic with eccentricity  $(e_1)$ , then

A. 
$$\left(5, \frac{5}{3}\right)$$
  
B. 3,  $\left(\frac{4}{3}\right)$   
C.  $\left(5, \left(\frac{10}{3}\right)\right)$   
D. 3,  $\left(\frac{8}{3}\right)$ 

## Answer: C



**6.** An ellipse E has its center C(3,1), focus at (3,6) and passing through the point P(7,4) Q. The product of the lengths of the prependicular segrent from the focii on tangent at point P is

A. 
$$e_1=rac{3}{\sqrt{5}}$$
  
B.  $e_1=rac{\sqrt{5}}{3}$   
C.  $e_1=rac{3}{\sqrt{10}}$ 

D. 
$$e_1=rac{\sqrt{10}}{3}$$

## **Answer: B**

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7. 
$$C_1 : x^2 + y^2 = r^2 ext{ and } C_2 : rac{x^2}{16} + rac{y^2}{9} = 1$$

interset at four distinct points A,B,C, and D. Their

common tangents form a peaallelogram A'B'C'D'.

if A'B'C'D' is a square, then r is equal to

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Curves

$$C_1\!:\!x^2+y^2=r^2 \,\, ext{and}\,\, C_2\!:\!rac{x^2}{16}+rac{y^2}{9}=1$$

intersect at four distinct points A,B,C and D. Their common tangents from a parallelogram PQRS. Q. If ABCD is square, then the value of  $25r^2$  is

A. 12

8.

- B. 15
- C. 20

D. 25





- . - . . .

9. Curves  

$$C_1: x^2 + y^2 = r^2$$
 and  $C_2: \frac{x^2}{16} + \frac{y^2}{9} = 1$   
intersect at four distinct points A,B,C and D. Their  
common tangents from a parallelogram PQRS. Q.  
If ABCD is square, then the value of  $25r^2$  is

A. 1:4

B.1:2

**C**. 3:4

D. 9:16

## Answer: B



10. An ellipse whose distance between foci S and S' is 4 units is inscribed in the  $\Delta ABC$ touching thesides AB, AC and BCatP, Q and R. If centre of ellipse is at origin and major axis along x-axis SP + S'P = 6, then

A. 
$$9x^2+5y^2=45$$

B. 
$$4x^2 + 9y^2 = 46$$

C. 
$$5x^2 + 9y^2 = 45$$

D. 
$$9x^2 + 4y^2 = 36$$

#### Answer: C



**11.** An ellipse whose distance between foci S and S' is 4 units is inscribed in the  $\triangle ABC$  touching the sides AB,AC and BC at P,Q and R, respectively. If centre of ellipse is at origin and major axis along X-axis, SP+S'P=6`Q. Equation of the ellipse is

A. 
$$\left(x^2+y^2-14
ight)^2=4ig(5x^2+9y^2-45ig)$$
  
B.  $\left(x^2+y^2-14
ight)^2=4ig(5x^2+9y^2-54ig)$   
C.  $\left(x^2+y^2-14
ight)^2=4ig(9x^2+5y^2-45ig)$   
D.  $\left(x^2+y^2-14
ight)^2=4ig(9x^2+5y^2-54ig)$ 

#### Answer: A



**12.** An ellipse whose distance between foci S and S' is 4 units is inscribed in the  $\triangle ABC$  touching the sides AB,AC and BC at P,Q and R, respectively.

If centre of ellipse is at origin and major axis along X-axis, SP+S'P=6`Q. Equation of the ellipse is

A. 
$$5x^2+9y^2=15$$

B. 
$$5x^2 + 9y^2 = 60$$

C. 
$$9x^2 + 5y^2 = 14$$

D. 
$$9x^2 + 5y^2 = 144$$

#### **Answer: B**


**13.** The line $2px + y\sqrt{1 - p^2} = 1(|p| < 1)$  for different values of p, touches a fixed ellipse whose exes are the coordinate axes. Q. The eccentricity of the ellipse is

A. 
$$\frac{1}{\sqrt{5}}$$
  
B. 
$$\frac{1}{\sqrt{3}}$$
  
C. 
$$\frac{\sqrt{3}}{2}$$
  
D. 
$$\frac{2}{\sqrt{5}}$$

#### Answer: C

**14.** For all real p, the line  $2px + y\sqrt{1 - p^2} = 1$  touches a fixed ellipse whose axex are the coordinate axes

The foci of the ellipse are

A. 
$$\left(\pm \frac{\sqrt{3}}{2}, 0\right)$$
  
B.  $\left(0, \pm \frac{\sqrt{3}}{2}\right)$   
C.  $\left(\pm \sqrt{3}, 0\right)$ 

D. 
$$(0, \pm \sqrt{3})$$

#### Answer: B



**15.** The line  $2px + y\sqrt{1 - p^2} = 1(|p| < 1)$  for different values of p, touches a fixed ellipse whose exes are the coordinate axes. Q. The locus of the point of intersection of prependicular tangents of the ellipse is

A. 
$$x^2+y^2=2$$

B. 
$$x^2+y^2=rac{3}{2}$$
  
C.  $x^2+y^2=rac{5}{4}$   
D.  $x^2+y^2=rac{1}{2}$ 



### **Exercise Single Integer Answer Type Questions**

**1.** Two concentric ellipse be such that the foci of one be on the other and if 3/5 and 4/5 be their eccentricities. If  $\theta$  is the angle between their axes, then the values of  $2(1 + \sin^2 \theta + \sin^4 \theta)$  must be



2. Write the first five terms of the sequence

whose 
$$n^{th}$$
 term is  $a_n=rac{n}{n+2}$ 

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**3.** The number of points on the ellipse 
$$\frac{x^2}{50} + \frac{y^2}{20} = 1$$
 from which a pair of perpendicular tangents is drawn to the ellipse  $\frac{x^2}{16} + \frac{y^2}{9} = 1$  is 0 (b) 2 (c) 1 (d) 4

4. The length of the sides of the square which can

be made by four perpendicular tangents to the

ellipse 
$$\displaystyle rac{x^2}{7} + \displaystyle rac{2y^2}{11} = 1$$
, is

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5. The number of distinct normal lines that can be

drawn to the ellipse  $\displaystyle rac{x^2}{169} + \displaystyle rac{y^2}{25} = 1$  from the

point P(0,6) is

6. Write the first five terms of the sequence whose  $n^{th}$  term is  $a_n = 3^n$ 

7. An ellipse passing through the origin has its foci (3, 4) and (6, 8). The length of its semi-minor axis is *b*. Then the value of  $\frac{b}{\sqrt{2}}$  is\_\_\_\_

8. The maximum value of  $5\lambda$  for which four normals can be drawn to ellipse  $rac{x^2}{25}+rac{y^2}{16}=1$  through a point ( $\lambda$ ,0) is

**9.** Find the first five terms of the sequence whose

$$n^{th}$$
 term is  $a_n=rac{n}{4}$ 

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Ellipse Exercise 5 Matching Type Questions

1. Find the first five terms of the sequence whose

$$n^{th}$$
 term is  $a_n = 2^{n+3}$ 

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2. Find the value of x , if x = 
$$\frac{7}{4} - \frac{17}{8}$$

# Match the f

3.

### following

	Column I		Column II
(A)	The minimum and maximum distances of a point (2,6) from the ellipse $9x^2 + 8y^2 - 36x - 16y - 28 = 0$ are <i>L</i> and <i>G</i> , then	(p)	L + G = [0]
(B)	The minimum and maximum distances of a point (1,2) from the ellipse $4x^2 + 9y^2 + 8x - 36y + 4 = 0$ are <i>L</i> and <i>G</i> , then	(q)	L + G = 6
(C)	The minimum and maximum distances of a point $\left(\frac{9}{5}, \frac{12}{5}\right)$	(r)	$\mathbf{G} - \boldsymbol{L} = 8$
	from the ellipse $4(3x + 4y)^2 + 9(4x - 3y)^2 = 900$ are <i>L</i> and <i>G</i> , then		41
(D)	The minimum and maximum distances of a point (0,4) from the ellipse $25x^2 + 9y^2 = 225$ are L and G, then	(s)	G – L = 6

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### **Exercise Statement I And Ii Type Questions**

1. Find the first five terms of the sequence whose

 $n^{th}$  term is  $a_n = 2n + 1$ 



2. Statement 1 : The area of the ellipse  $2x^2 + 3y^2 = 6$  is more than the area of the circle  $x^2 + y^2 - 2x + 4y + 4 = 0$ . Statement 2 : The length f the semi-major axis of an ellipse is more that the radius of the circle.

A. Statement I is true, statement II is true:
statement II is a correct explanation for
statement I
B. Statement I is true, statement II is true,

statement II is not a correct explanation for

statement I

C. statement I is true, statement II is false

D. statement I is false, statement II is true

Answer: B

**3.** Statement 1 The equation of the director circle to the ellipse  $4x^2 + 9y^2 = 36isx^2 + y^2 = 13$ Statement 2 The locus of the point of intersection of perpendicular tangents to an ellipse is called the director circle.

A. Statement I is true, statement II is true: statement II is a correct explanation for statement I

B. Statement I is true, statement II is true, statement II is not a correct explanation for

statement I

C. statement I is true, statement II is false

D. statement I is false, statement II is true

Answer: A



4. Statement 1 : In an ellipse, the sum of the distances between foci is always less than the sum of focal distances of any point on it.
Statement 2 : The eccentricity of any ellipse is less than 1.

A. Statement I is true, statement II is true: statement II is a correct explanation for statement I

B. Statement I is true, statement II is true,

statement II is not a correct explanation for

statement I

C. statement I is true, statement II is false

D. statement I is false, statement II is true

Answer: A

5. Statement 1 The sum of the focal distances of a

the point ellipse on  $4x^2 + 5y^2 - 16x - 30y + 41 = 0is2\sqrt{5}.$ The equation Statement 2  $4x^2 + 5y^2 - 16x - 30y + 41 = 0$ be can expressed as  $4(x-2)^2 + 5(y-3)^2 = 20$ . A. Statement I is true, statement II is true: statement II is a correct explanation for statement I B. Statement I is true, statement II is true, statement II is not a correct explanation for statement I

C. statement I is true, statement II is false

D. statement I is false, statement II is true

Answer: B

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6. Statement 1 : The locus of the center of a variable circle touching two circle  $(x-1)^2 + (y-2)^2 = 25$  and  $(x-2)^2 + (y-1)^2 = 16$  is an ellipse. Statement 2 : If a circle  $S_2 = 0$  lies completely inside the circle  $S_1 = 0$  , then the locus of the center of a variable circle S = 0 that touches both the circles is an ellipse.

A. Statement I is true, statement II is true: statement II is a correct explanation for statement I
B. Statement I is true, statement II is true, statement II is not a correct explanation for statement I

C. statement I is true, statement II is false

D. statement I is false, statement II is true





7. Find the equation of a curve passing through the point (1,1), if the tangent drawn at any point P(x,y) on the curve meets the coordinate axes at A and B such that P is the mid point of AB.



8. Find the first five terms of the sequence whose

$$n^{th}$$
 term is  $a_n = n^2 - 1$ 

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**Ellipse Exercise 7 Subjective Type Questions** 

#### 1. Find the first five terms of the sequence whose

 $n^{th}$  term is  $a_n=rac{n-1}{n+1}$ 

2. Find the first five terms of the sequence whose

$$n^{th}$$
 term is  $a_n=(\,-1)^{n+1}2n$ 

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3. Find the 12th term of AP if first term is 5 and

common difference is 7.

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**4.** Find the eccentricity of the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  when a=5 and b=3.



**6.** Find the  $7^{th}$  term of the sequence whose  $n^{th}$ 

term is  $a_n = (\,-1)^n n^2$ 

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7. Find the  $10^{th}$  term of the sequence whose  $n^{th}$ 

term is 
$$a_n = rac{n-5}{n+7}$$

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**8.** Find the  $5^{th}$  term of the sequence whose  $n^{th}$ 

term is 
$$a_n=rac{n^2+5}{4}$$

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9. Find the length of latus rectum of the ellipse

$$rac{x^2}{25} + rac{y^2}{16} = 1$$



**3.** Find the  $24^{th}$  term of the sequence whose  $n^{th}$ 

term is  $a_n = 4n - 3$ 

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**Exercise Questions Asked In Previous 13 Years Exam** 

1. The minimum area of the triangle formed by the tangent to  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  and the coordinate axes is

A. ad sq units

B. 
$$\frac{a^2 + b^2}{2}$$
 sq units  
C.  $\frac{(a+b)^2}{2}$  sq units  
D.  $\frac{a^2 + ab + b^2}{3}$  sq units

#### Answer: A



**2.** Find the  $17^{th}$  term in the following sequence

whose  $n^{th}$  term is  $a_n = 2n-4$ 

**3.** An ellipse has OB as the semi-minor axis, FandF' as its foci, and  $\angle FBF'$  a right angle. Then, find the eccentricity of the ellipse.

A. 
$$\frac{1}{\sqrt{2}}$$
  
B. 
$$\frac{1}{2}$$
  
C. 
$$\frac{1}{4}$$
  
D. 
$$\frac{1}{\sqrt{3}}$$

#### Answer: A

**4.** In an ellipse, the distances between its foci is 6

and minor axis is 8. Then its eccentricity is

A. 
$$\frac{3}{5}$$
  
B.  $\frac{1}{2}$   
C.  $\frac{4}{5}$   
D.  $\frac{1}{\sqrt{5}}$ 

Answer: A



5. Find the 9<sup>th</sup> term in the following sequence whose  $n^{th}$  term is  $a_n = (-1)^n (3n + 2)$ Watch Video Solution

6. A focus of an ellipse is at the origin. The directrix is the line x = 4 and the eccentricity is  $rac{1}{2}$  Then the length of the semi-major axis is

A. 
$$\frac{8}{3}$$
  
B.  $\frac{2}{3}$   
C.  $\frac{4}{3}$ 

#### Answer: A

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7. The 5th, 8th, and 11th terms of a GP are p, q and

s respectively. Find relation between p,q and s.

Calusian



8. Is 309 a term of the AP 11, 17, 23....?

\*I*: \_

**9.** A triangle ABC with fixed base BC, the vertex A moves such that  $\cos B + \cos C = 4 \sin^2 \left(\frac{A}{2}\right)$ . If a, b and c, denote the length of the sides of the triangle opposite to the angles A, B, andC, respectively, then

(a)b + c = 4a

(b) b + c = 2a

(c) the locus of point A is an ellipse

(d) the locus of point A is a pair of straight lines

A. b+c=4a

B. b+c=2a

C. locus of point A is an ellipse

D. locus of point A is a pair od straight lines

Answer: B::C

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10. The conic having parametric representation

$$x = \sqrt{3}igg(1 - rac{t^2}{1 + t^2}igg), y = rac{2t}{1 + t^2}$$
 is

A. an circle

B. a parabola

C. an ellipse

D. a hyperbola

#### Answer: C

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**11.** The ellipse  $x^2 + 4y^2 = 4$  is inscribed in a rectangle aligned with the coordinate axes, which in turn is inscribed in another ellipse that passes through the point (4, 0). Then the equation of the ellipse is (1)  $x^2 + 16y^2 = 16$  (2)  $x^2 + 12y^2 = 16$  (3)  $4x^2 + 48y^2 = 48$  (4)  $4x^2 + 64y^2 = 48$ 

A. 
$$x^2+12y^2=16$$

B. 
$$4x^2 + 48y^2 = 48$$

C. 
$$4x^2 + 64y^2 = 48$$

D. 
$$x^2 + 16y^2 = 16$$

#### Answer: A

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12. Tangents are drawn from the point P(3,4) to the ellipse  $\frac{x^2}{9} + \frac{y^2}{4} = 1$  touching the ellipse at point A and B. Q. The coordinates of A and B are A. (3,0) amd (0,2)

B. 
$$\left(-\frac{8}{5}, \left(2\frac{\sqrt{161}}{15}\right) \text{ and } \left(-\frac{9}{8}, \frac{8}{5}\right)\right)$$
  
C.  $\left(-\frac{8}{5}, \left(2\frac{\sqrt{161}}{15}\right) \text{ and } (0, 2)\right)$   
D.  $(3, 0)$  and  $\left(-\frac{9}{5}, \frac{8}{5}\right)$ 

#### Answer: D

13. Tangents are drawn from the point P(3,4) to the ellipse 
$$rac{x^2}{9}+rac{y^2}{4}=1$$
 touching the ellipse at

point A and B. Q. The orthocenter of the trianlge

### PAB is

A. 
$$\left(5, \frac{8}{7}\right)$$
  
B.  $\left(\frac{7}{5}, \frac{25}{8}\right)$   
C.  $\left(\frac{11}{5}, \frac{8}{5}\right)$   
D.  $\left(\frac{8}{25}, \frac{7}{5}\right)$ 

#### Answer: C


**14.** Tangents are drawn from the point P(3,4) to the ellipse  $\frac{x^2}{9} + \frac{y^2}{4} = 1$  touching the ellipse at point A and B. Q. The equation of the locus of the points whose distance from the point P and the line AB are equal, is

A. 
$$9x^2 + y^2 - 6xy - 54x - 62y + 241 = 0$$
  
B.  $x^2 + 9y^2 + 6xy - 54x + 62y - 241 = 0$   
C.  $9x^2 + 9y^2 - 6xy - 54x - 62y - 241 = 0$   
D.  $x^2 + y^2 - 2xy + 27x + 31y - 120 = 0$ 

#### Answer: A



**15.** Find the equation of an ellipse whose axes lie along the coordinate axes, which passes through the point (-3,1) and has eccentricity equal to  $\sqrt{2/5}$ .

A. 
$$5x^2 + 3y^2 - 48 = 0$$

B. 
$$3x^2 + 5y^2 - 15 = 0$$

C. 
$$5x^2 + 3y^2 - 32 = 0$$

D. 
$$3x^2 + 5y^2 - 32 = 0$$

#### Answer: D



**16.** The ellipse  $E_1: rac{x^2}{9} + rac{y^2}{4} = 1$  is inscribed in a rectangle R whose sides are parallel to the coordinate axes. Another ellipse  $E_2$  passing through the point (0, 4) circumscribes the rectangle  $R_1$  The eccentricity of the ellipse  $E_2$  is (a)  $\frac{\sqrt{2}}{2}$  (b)  $\frac{\sqrt{3}}{2}$  (c)  $\frac{1}{2}$  (d)  $\frac{3}{4}$ A.  $\frac{\sqrt{2}}{2}$ B.  $\frac{\sqrt{3}}{2}$ 

 $\mathsf{C}.\,\frac{1}{2}$ 

### Answer: C

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17. Statement 1: An equation of a common tangent to the parabola  $y^2 = 16\sqrt{3}x$  and the ellipse  $2x^2 + y^2 = 4$  is  $y = 2x + 2\sqrt{3}$ . Statement 2: If the line  $y = mx + \frac{4\sqrt{3}}{m}$ ,  $(m \neq 0)$  is a common tangent to the parabola  $y^2 = 16\sqrt{3}x$  and the ellipse  $2x^2 + y^2 = 4$ , then m satisfies  $m^4 + 2m^2 = 24$ . A. Statement I is true, statement II is true:

statement II is a correct explanation for

statement I

B. Statement 1 is true,

Statement 2 is true,

Statement 2 is a correct explanation for

statemennt 1

C. Statement 1 is true, statement 2 is true,

Statement 2 is not a correct explanation for

statement 1.

D. Statement 1 is true,

Statement 2 is false.

#### Answer: B



**18.** An ellipse is drawn by taking a diameter of the circle  $(x - 1)^2 + y^2 = 1$  as its semi-minor axis and a diameter of the circle  $x^2 + (y - 2)^2 = 4$  as its semi-major axis. If the centre of the ellipse is the origin and its axes are the coordinate axes, then the equation of the ellipse is (1)

$$4x^2 + y^2 = 4$$
 (2)  $x^2 + 4y^2 = 8$  (3)  $4x^2 + y^2 = 8$   
(4)  $x^2 + 4y^2 = 16$   
A.  $4x^2 + y^2 = 4$   
B.  $x^2 + 4y^2 = 8$   
C.  $4x^2 + y^2 = 8$ 

D. 
$$x^2 + 4y^2 = 16$$

### Answer: D



19. the equation of the circle passing through the

foci of the ellipse  $rac{x^2}{16}+rac{y^2}{9}=1$  and having centre at (0,3) is

A. 
$$x^2 + y^2 - 6y - 7 = 0$$

B. 
$$x^2 + y^2 - 6y + 7 = 0$$

C. 
$$x^2 + y^2 - 6y - 5 = 0$$

D. 
$$x^2 + y^2 - 6y + 5 = 0$$

#### Answer: A



**20.** A vertical line passing through the point (h, 0) intersects the ellipse  $\frac{x^2}{4} + \frac{y^2}{3} = 1$  at the points P and Q.Let the tangents to the ellipse at P and Q meet at R. If  $\Delta(h)$  Area of triangle  $\Delta PQR$ , and  $\Delta_1 = \max_{\substack{\frac{1}{2} \le h \le 1 \\ \frac{1}{2} \le h \le 1}} \Delta(h)$  and  $\Delta_2 = \min_{\substack{\frac{1}{2} \le h \le 1 \\ \frac{1}{2} \le h \le 1}} \Delta(h)$  Then  $\frac{8}{\sqrt{5}} \Delta_1 - 8\Delta_2$ 

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21. The locus of the foot of prependicular drawn from the center of the ellipse  $x^2 + 3y^2 = 6$  on any tangent to it is

A. 
$$\left(x^2+y^2
ight)^2=6x^2+2y^2$$
  
B.  $\left(x^2+y^2
ight)^2=6x^2-2y^2$   
C.  $\left(x^2-y^2
ight)^2=6x^2+2y^2$   
D.  $\left(x^2-y^2
ight)^2=6x^2-2y^2$ 

#### Answer: A



A.  $\frac{27}{2}$ 

B. 27

C. 
$$\frac{27}{4}$$

D. 18

### Answer: B



**23.** Let E1 and E2, be two ellipses whose centers are at the origin.The major axes of E1 and E2, lie along the x-axis and the y-axis, respectively. Let S

be the circle  $x^2 + (y-1)^2 = 2$ . The straight line x+ y =3 touches the curves S, E1 and E2 at P,Q and R, respectively. Suppose that  $PQ = PR = \frac{2\sqrt{2}}{3}$ . If e1 and e2 are the eccentricities of E1 and E2, respectively, then the correct expression(s) is(are):

A. (a)
$$e_1^2 + e_2^2 = \frac{43}{40}$$
  
B. (b) $e_1e_2 = \frac{\sqrt{7}}{2\sqrt{10}}$   
C. (c) $|e|_1^2 - e_2^2| = \frac{5}{8}$   
D. (d) $e_1e^2 = \frac{\sqrt{3}}{4}$ 

#### Answer: A::B



24. Suppose that the foci of the ellipse  $rac{x^2}{0}+rac{y^2}{5}=1$  are  $(f_1,0)and(f_2,0)$  where  $f_1>0 and f_2<0.$  Let  $P_1and P_2$  be two parabolas with a common vertex at (0, 0) and with foci at  $(f_1.0)and$  (2f\_2 , 0), respectively. Let  $T_1$  be a tangent to  $P_1$  which passes through  $(2f_2, 0)$  and  $T_2$  be a tangents to  $P_2$  which passes through  $(f_1, 0)$  . If  $m_1$  is the slope of  $T_1$  and  $m_2$ is the slope of  $T_2$ , then the value of  $\left(rac{1}{m_1^2}+m_2^2
ight)$  is



**25.** If the tangents to the ellipse at M and N meet at R and the normal to the parabola at M meets the x-axis at Q, then the ratio of area of the triangle MQR to area of the quadrilateral MF1NF2 .

is

A. 
$$\left(-\frac{9}{10}, 0\right)$$
  
B.  $\left(\frac{2}{3}, 0\right)$   
C.  $\left(\frac{9}{10}, 0\right)$   
D.  $\left(\frac{2}{3}, \sqrt{6}\right)$ 

### Answer: A



**26.** The eccentricity of an ellipse whose centre is at the origin is  $\frac{1}{2}$ . If one of its directrices is x = - 4, then the equation of the normal to it at (1, 3/2) is

A. 
$$x+2y=4$$

:

B. 
$$2y - x = 2$$

C. 
$$4x - 2y = 1$$

D. 
$$4x + 2y = 7$$

## Answer: C

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