



MATHS

BOOKS - ARIHANT MATHS

ESSENTIAL MATHEMATICAL TOOLS

Examples

1. Solve $2x + 1 > 3$.



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2. solve $-2 < 2x - 1 < 2$.



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3. Solve the inequalities given below for real x

$$\therefore \frac{3(x - 2)}{5} \leq \frac{5(2 - x)}{3}$$



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4. solve for X. $\frac{4}{x + 1} \leq 3 \leq \frac{6}{x + 1}, (x > 0)$



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5. Explain the following : (i) $|x| = 5$ (ii)
 $|x| = -5$ (iii) $|x| < 5$ (iv) $|x| < -5$ (v)
 $|x| > -5$ (vi) $|x| < 5$



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6. solve for , x where $f(x) = |x| \geq 0$



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7. solve $|x - 3| < 5$.



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8. solve $|x - 1| \leq 2$.



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9. Solve the following systems of linear inequations:

$$1 \leq |x - 2| \leq 3$$



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10. solve $1 \leq |x - 1| \leq 3$,



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11. solve $\left| \frac{2}{x - 4} \right| > 1, x \neq 4$.



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12. Solve $|x - 1| + |x - 2| \geq 4$



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13. Find the interval in which $f(x)$ is positive or negative : $f(x) = (x-1)(x-2)(x-3)$



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14. solve $f(x) = \frac{(x-1)(2-x)}{(x-3)} \geq 0.$



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15. find the value of x for which

$$f(x) = \frac{(2x - 1)(x - 1)^2(x - 2)^2}{(x - 4)^2} \geq 0.$$



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16. Find the value of x for which

$$f(x) = \frac{(x - 2)^2(1 - x)(x - 3)^2(x - 4)^2}{(x - 1)} \leq 0.$$



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17. Solve : $\frac{|x| - 1}{|x| - 2} \geq 0, x \neq \pm 2$



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18.

Solve:

$$\frac{-1}{|x| - 2} \geq 1, \text{ where } x \in R, x \neq \pm 2.$$



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19. solve $\frac{|x + 3| + x}{x + 2} > 1$



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20.

If

$$f(x) = \frac{(x-1)^3(x+2)^4(x-3)^5(x+6)}{x^2(x-7)^3},$$

Solve the following inequality $f \geq 0$



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21. For what values of x , the numbers $\frac{3}{8}, x, \frac{8}{3}$ are in G.P?



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22. Find the sum of the series – $1 + 5 + 11 + \dots$ to n terms.



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23. find a for which $3x^2 + ax + 3 > 0, \forall x \in R.$



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24. find a for which

$$ax^2 + x - 1 < 0, \forall x \in R?$$



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25. Solve $(x + 1)^2 + (x^2 + 3x + 2)^2 = 0$.



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26. Solve $|x + 1| + \sqrt{x} - 1 = 0$.



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Example

1. Solve

$$|x^2 - 1| + (x - 1)^2 + (\sqrt{x})^2 - 3x + 2 = 0.$$



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2. Let $f(x) = x$ and $g(x) = |x|$ be two real-valued functions, check whether the functions are one-one.



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Exercise For Session 1

1. All the rational numbers are irrational also.



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2. All the integers are irrational also.



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3. Irrational numbers are real numbers also.



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4. Zero is a natural number.



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5. Sum of two natural numbers is a rational number.



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6. A positive integer is a natural number also.



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7. sum of two rational numbers is

A. rational

B. irrational

C. Both (a) and (b)

D. None of these

Answer: A



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8. Which one of the following statement is true?

- (i) The sum of two irrational numbers is always an irrational number.
- (ii) The sum of two irrational numbers is always a rational number.
- (iii) The sum of two irrational numbers may be a rational number or irrational number.

(iv) The sum of two irrational numbers is always an integer.



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9. Product of two rational numbers is

A. always rational

B. rational or irrational

C. always irrational

D. None of these

Answer: A



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10. If a is an irrational number which is divisible by b , then the number b
- A. must be rational
 - B. must be irrational
 - C. may be rational or irrational
 - D. None of these

Answer: C



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Exercise For Session 2

1. solve for x, $|x - 1| < 2$



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2. solve for x, $|x - 3| > 2$



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3. Solve: $0 < |x - 1| < 3$



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4. solve for x, $(x - 1) + (2x - 3) = (3x - 4)$



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5. $\left| \frac{x - 3}{x^2 - 4} \right| \leq 1.$





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Exercise For Session 3

1. Solve $\frac{x - 2}{x + 2} > \frac{2x - 3}{4x - 1}$



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2. $\frac{2x - 1}{2x^3 + 3x^2 + x} > 0.$



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$$3. \frac{4x}{x^2 + 3} \geq 1.$$



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$$4. \frac{(x - 1)(x + 1)(x + 4)(x + 6)}{7x^2 + 8x + 4} > 0$$



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$$5. \frac{x}{x^2 - 5x + 9} \leq 1.$$



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6. Solution of inequality $|x - 1| < 0$ is



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7. Solution of inequailty $x^2 + x + |x| + 1 \leq 0$

is

A. (1,2)

B. (0,1)

C. No solution

D. None of these

Answer: C



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8. Solution of inequality $x^2 + x + |x| + 1 \leq 0$

is

A. $\left(-\frac{2}{3}, 4 \right)$

B. $(4, \infty)$

C. $\left(-\frac{2}{3}, 1 \right)$

D. None of these

Answer: D



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9. Solve $\frac{x+2}{6} - \left(\frac{11-x}{3} - \frac{1}{4} \right) = \frac{3x-4}{12}$



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10. For what value of x , the numbers
 $-\frac{5}{9}, x, \frac{9}{5}$ are in G.P?



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11. The solution of $||x| - 1| < |1 - x|$, $x \in R$

is

- A. $(-1, 1)$
- B. $(0, \infty)$
- C. $(-1, \infty)$
- D. None of these

Answer: D



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12. The solution of $2^x + 2^{|x|} \geq 2\sqrt{2}$ is

A. $(-\infty, \log_2(\sqrt{2} + 1))$

B. $(0, \infty)$

C. $\left(\frac{1}{2}, \log_2(\sqrt{2} - 1)\right)$

D. $(-\infty, \log_2(\sqrt{2} - 1)] \cup \left[\frac{1}{2}, \infty\right)$

Answer: D



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Exercise For Session 4

1. Find all values of 'm' which
 $(2m - 3)x^2 + 2mx + 4 < 0$ for all real x.



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2. If $ax^2 - bx + 5 = 0$ does not have two distinct real roots, then find the minimum value of $5a+b$.



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3. $a, b, c \in R$, $a \neq 0$ and the quadratic equation $ax^2 + bx + c = 0$ has no real roots, then



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4. If $x, y \in [0, 10]$, then find the number of solutions (x, y) of the inequation

$$3(\sec^2 x - 1) \sqrt{9y^2 - 6y + 2} \leq 1$$



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Exercise Single Option Correct Type Questions

1. For a $a \leq 0$, determine all real roots of the equation $x^2 - 2a|x - a| - 3a^2 = 0$.



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2. Solve $|x^2 + 4x + 3| + 2x + 5 = 0$.



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$$3. \text{ Solve } |x^2 - 3x - 4| = 9 - |x^2 - 1|$$



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$$4. \text{ Solve the equation}$$

$$2^{|x+1|} - 2^x = |2^x - 1| + 1$$



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$$5. \text{ Solve } -\frac{3x - 2}{4} + \frac{2x + 3}{3} = x - \frac{2}{3}$$



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6. Solve $(x + 3)^2 - (x - 1)^2 \geq 244$.



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7. Solve $|x - 2 - 1| \geq 3$.



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8. Solve $1 \leq \frac{3x^2 - 7x + 8}{x^2 + 1} \leq 2$.



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9. Let $f(x) = \frac{2x}{2x^2 + 5x + 2}$, find the interval for which $f(x) > 0$.



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10. Draw the graph of $|x|$ and check its injectivity.



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11. Solve the inequality

$$|x - 1| + |2 - x| > 3 + x.$$



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12. Solve the equation

$$\sqrt{x^2 + 12y} + \sqrt{y^2 + 12x} = 33, x + y = 23.$$



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13. Solve the equation

$$\sqrt{2x - 1} + \sqrt{3x - 2} = \sqrt{4x - 3} + \sqrt{5x - 4}.$$



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14. If x, y and z are real such that

$x + y + z = 4$, $x^2 + y^2 + z^2 = 6$, x belongs to



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15. If $f(x) = 3x + 2$ & $g(x) = -3x - 1$. Find $f(g(-3))$



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16. Given $f(x) = 3x - 1$. Find: (i) $f(-2)$ (ii) $f(5)$



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17.

Let

$$f(x) = \frac{x^2 - 2x + 1}{x + 3}, \text{ find } x : (i) f(x) > 0$$

$$(ii) f(x) < 0$$



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18. Solve the inequation:

$$\left| 1 - \left(\frac{|x|}{1 + |x|} \right) \right| \geq \frac{1}{2}$$



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Exercise More Than One Correct Option Type Questions

1. If $\cos x - y^2 - \sqrt{y - x^2 - 1} \geq 0$, then

A. $y \geq 1$

B. $x \in R$

C. $y=1$

D. $x=0$

Answer: C::D



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2. If $(\sin \alpha)x^2 - 2x + b \geq 2$, for all real values of $x \leq 1$ and $\alpha \in \left(0, \frac{\pi}{2}\right) \cup (\pi/2, \pi)$, then possible real value of b is /are a. 2 b. 3 c. 4 d. 5

A. 2

B. 3

C. 4

D. 5

Answer: A::C



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3. If $|ax^2 + bx + c| \leq 1$ for all x in $[0, 1]$ then

A. $|a| \leq 8$

B. $|b| \leq 8$

C. $|c| \leq 1$

D. $|a| + |b|_{|c|} \leq 17$

Answer: A::B::D



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Exercise Passage Based Questions

1. If $f(x) = 5x + 3$, $x \in \mathbb{R}$. If $f(x) = 13$, find the value of x .

A. 1

B. 0

C. 2

D. 3

Answer: A



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2. Let $f(x) = ax^2 + bx + C$, $a, b, c \in R$. It is given $|f(x)| \leq 1$, $|x| \leq 1$. The possible value of $|a + c|$, if $\frac{8}{3}a^2 + 2b^2$ is maximum, is given by

A. 1

B. 0

C. 2

D. 3

Answer: A



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3. Let $f(x) = ax^2 + bx + c, ab, c \in R$. It is given $|f(x)| \leq 1, |x| \leq 1$

The possible value of $|a + c|$, if $\frac{8}{3}a^2 + 2ab^2$ is maximum is given by

A. 32

B. $\frac{32}{3}$

C. $\frac{2}{3}$

D. $\frac{16}{3}$

Answer: B



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4. Consider the equation

$|2x| - |x - 4| = x + 4$ The least integer

satisfying the equation is

A. -4

B. 4

C. 5

D. -5

Answer: A



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5. solve $\frac{3x + 5}{2} = 7$



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6. Solve $\frac{2x - 3}{3x + 2} = -\frac{2}{3}$



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7. Consider a number $N=21\text{P}53\text{Q}4$.

The number of ordered pairs (P,Q) so that the number' N' is divisible by 9, is

A. 11

B. 12

C. 10

D. 8

Answer: A



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8. Consider a number $n=21\ P\ 5\ 3\ Q\ 4$.

The number of values of Q so that the number ' N ' is divisible by 8, is

A. 4

B. 3

C. 2

D. 6

Answer: B



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9. Consider a number $N = 2 \ 1 \ P \ 5 \ 3 \ Q \ 4$. The number of ordered pairs (P,Q) so that the number 'N' is divisible by 44, is

A. 2

B. 3

C. 4

D. 5

Answer: C



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10. Consider the nine digit number $n = 7\ 3\ \alpha\ 4\ 9\ 6\ 1\ \beta\ 0$. If p is the number of all possible distinct values of $(\alpha - \beta)$, then P is equal to

A. 17

B. 18

C. 19

D. 20

Answer: C



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11. Consider the nine digit number $n = 73\alpha 4961\beta 0$. If q is the number of all possible values of β for which the given number is divisible by 8, then q is equal to

A. 2

B. 3

C. 4

D. 5

Answer: A



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12. Consider the nine digit number $n = 73\alpha 4961\beta 0$. The number of ordered pairs (α, β) for which the given number is divisible by 88, is

A. 1

B. 2

C. 3

D. 4

Answer: B



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13. Consider the nine digit number $n = 7\ 3\ \alpha\ 4\ 9\ 6\ 1\ \beta\ 0$. The number of possible values of $(\alpha + \beta)$ for which the given number is divisible by 6, is

A. 3

B. 4

C. 6

D. 7

Answer: D



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14. Consider the nine digit number $n = 7 \ 3 \ \alpha \ 4 \ 9 \ 6 \ 1 \ \beta \ 0$. The number of possible values of β for which $i^N = 1$ (where $i = \sqrt{-1}$),

A. 2

B. 3

C. 4

D. 5

Answer: D



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$$15. \text{ Solve } 3x - \frac{2}{3}(x - 2) = 3 - x - \frac{1}{3}$$



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16. Solve $\frac{2x - 3}{3x - 2} = \frac{x + 4}{3x - 8}$



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17. Solve $\frac{x}{x - 1} - \frac{1}{x + 2} = \frac{1}{x + 2}$



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Exercise Single Integer Answer Type Questions

1. The number of solutions of the equation

$$|x - 1| - |2x - 5| = 2x$$



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2. The number of integral solution of the

equation $|x^2 - 7| \leq 9$ are



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3. Find the number of solution of the system
of equation $x+2y=6$ and $|x-3|=y$



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