



MATHS

BOOKS - ARIHANT MATHS

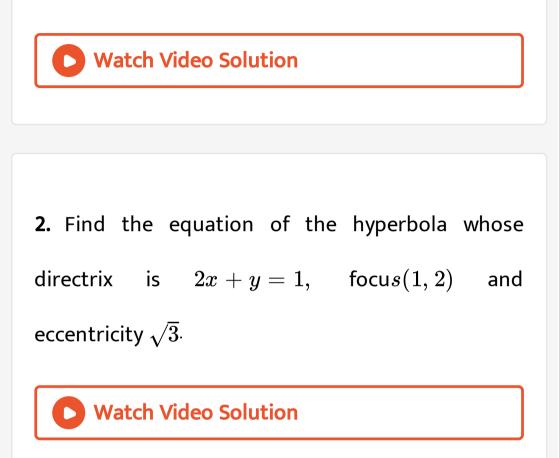
HYPERBOLA



1. To find the equation of the hyperbola from the definition that hyperbola is the locus of a point which moves such that the difference of its

distances from two fixed points is constant with

the fixed point as foci



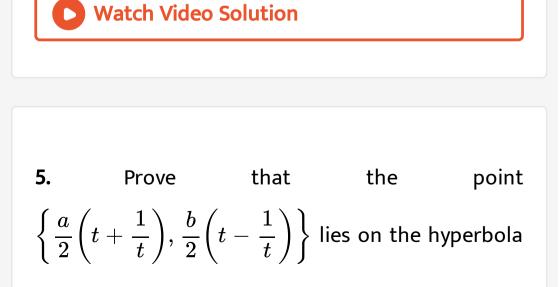
3. Find the lengths of the transvers and the conjugate axis, eccentricity, the coordinates of foci,

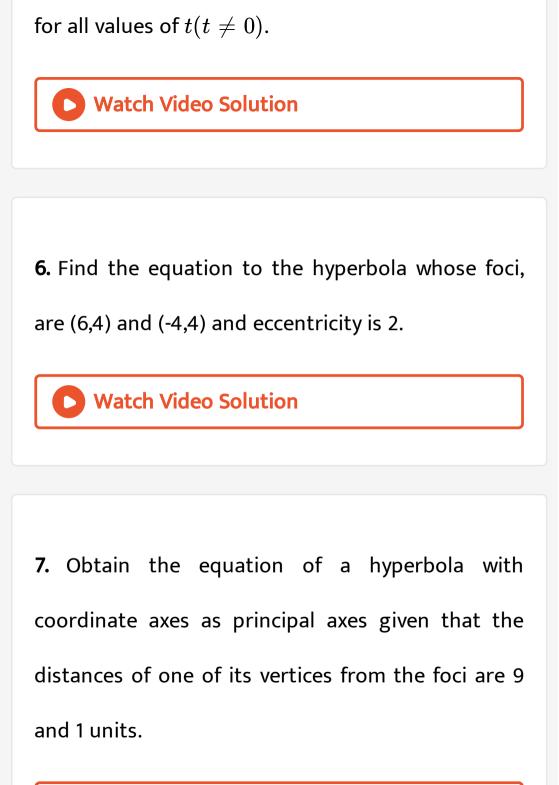
vertices, the lengths of latus racta, and the equations of the directrices of the following hyperbola: $16x^2 - 9y^2 = -144$.

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4. Write the eccentricity of the hyperbola whose

latus rectum is half of its transverse axis.





8. The foci of a hyperbola coincide with the foci of the ellipse $\frac{x^2}{25} + \frac{y^2}{9} = 1$, find the equation of hyperbola if ecentricity is 2.

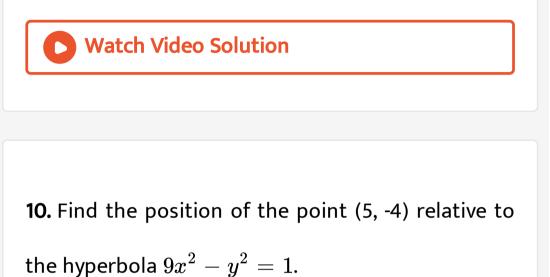
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9. Let two points P and Q lie on the hyperbola ${x^2\over a^2}-{y^2\over b^2}=1,$

whose centre C be such that CP is perpendicular to

CQ,

a lt b. Then the value of
$$\displaystyle rac{1}{CP^2} + \displaystyle rac{1}{CQ^2}$$
 is



A. inside

B. outside

C. on the hyperbola

D. none of the above

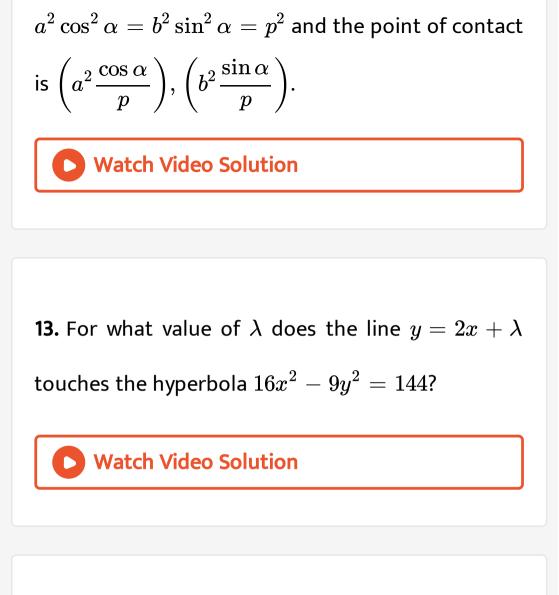
Answer:



11. If the line
$$lx+my+n=0$$
 touches the hyperbola $rac{x^2}{a^2}-rac{y^2}{b^2}=1.$ Then show $a^2l^2-b^2m^2=n^2$

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12. Show that the line $x \cos \alpha + y \sin \alpha + p$ touches the ellipse $rac{x^2}{a^2} + rac{y^2}{b^2} = 1$ if



14. If it is possible to draw the tangent to the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ having slope 2, then find its range of eccentricity.



15. Find the equation of the tangent to the hyperbola $x^2 - 4y^2 = 36$ which is perpendicular to the line x - y + 4 = 0.

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16. Find the equations to the common tangents to

the two hyperbolas
$$rac{x^2}{a^2}-rac{y^2}{b^2}=1$$
 and $rac{y^2}{a^2}-rac{x^2}{b^2}=1$

17. PQ is a chord joining the points ϕ_1 and ϕ_2 on the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$. If ϕ_1 and $\phi_2 = 2\alpha$, where *alha* is constant, prove that PQ touches the hyperbola $\frac{x^2}{a^2}\cos^2\alpha - \frac{y^2}{b^2} = 1$ Watch Video Solution

18. If the line $y = mx + \sqrt{a^2m^2 - b^2}$ touches the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ at the point $(a \sec \phi, b \tan \phi)$, show that $\phi = \sin^{-1}\left(\frac{b}{a}m\right)$.

19. A normal to the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ meets the axes at MandN and lines MP and NP are drawn perpendicular to the axes meeting at P. Prove that the locus of P is the hyperbola $a^2x^2 - b^2y^2 = (a^2 + b^2)^2$.

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20. Prove that the straight line lx + my + n = 0 is

a normal to the ellipse $rac{x^2}{a^2}+rac{y^2}{b^2}=1$ if $rac{a^2}{l^2}+rac{b^2}{m^2}=rac{\left(a^2-b^2
ight)^2}{n^2}.$

21. If the normal at $P(\theta)$ on the hyperbola $rac{x^2}{a^2} - rac{y^2}{2a^2} = 1$ meets the transvers axis at G, then prove that $AG\dot{A}'G = a^2(e^4\sec^2\theta - 1)$,

where AandA' are the vertices of the hyperbola.

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22. Find the locus of the foot of perpendicular from

the centre upon any normal to line hyperbola $rac{x^2}{a^2} - rac{y^2}{b^2} = 1.$

23. The locus of the poles of the chords of the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ which subtend a right angle at its centre is

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24. From the points on the circle $x^2 + y^2 = a^2$, tangents are drawn to the hyperbola $x^2 - y^2 = a^2$: prove that the locus of the middle-points $(x^2 - y^2)^2 = a^2(x^2 + y^2)$

25. Prove that the locus of the middle-points of the

chords of the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ which pass through a fixed point (α, β) is a hyperbola whose centre is $\left(\frac{\alpha}{2}, \frac{\beta}{2}\right)$.

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26. If the pair of straight lines
$$Ax^2 + 2Hxy + By^2 = 0$$
 be conjugate diameters of the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$, then prove that $Aa^2 = Bb^2$.

27. Find the asymptotes of the curve xy - 3y - 2x = 0.

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28. The asymptotes of a hyperbola are parallel to lines 2x + 3y = 0 and 3x + 2y = 0. The hyperbola has its centre at (1, 2) and it passes through (5, 3). Find its equation.

29. If the normal to the rectangular hyperbola $xy=c^2$ at the point 't' meets the curve again at t_1 then t^3t_1 , has the value equal to

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30. A triangle has its vertices on a rectangular hyperbola. Prove that the orthocentre of the triangle also lies on the same hyperbola.

31. A ray emerging from the point (5, 0) is incident on the hyperbola $9x^2 - 16y^2 = 144$ at the point Pwith abscissa 8. Find the equation of the reflected ray after the first reflection if point P lies in the first quadrant.

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32. The equation of the transverse and conugate axes of a hyperbola are respectively 3x + 4y - 7 = 0 and 4x - 3y + 8 = 0 and their respective lengths are 4 and 6. Find the equation of the hyperbola.



33. If the eccentricity of the hyperbola $x^2 - y^2(\sec)^2 \alpha = 5$ is $\sqrt{3}$ times the eccentricity of the ellipse $x^2(\sec)^2 \alpha + y^2 = 25$, then a value of α is : (a) $\frac{\pi}{6}$ (b) $\frac{\pi}{4}$ (c) $\frac{\pi}{3}$ (d) $\frac{\pi}{2}$

A.
$$\frac{\pi}{6}$$

B. $\frac{\pi}{4}$
C. $\frac{\pi}{3}$
D. $\frac{\pi}{2}$

Answer: B



34. Find the area of the triangle formed by any tangent to the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ with its asymptotes.

A. $\sec\lambda$

B. $\cos ec\lambda$

 $\mathsf{C.sec}^2 \lambda$

D. $\cos ec^2 \lambda$

Answer: A

35. The equation to the chord joining two points (x_1, y_1) and (x_2, y_2) on the rectangular hyperbola

$$egin{aligned} &xy=c^2 & ext{is:} &rac{x}{x_1+x_2}+rac{y}{y_1+y_2}=1\ &rac{x}{x_1-x_2}+rac{y}{y_1-y_2}=1\ rac{x}{y_1+y_2}+rac{y}{x_1+x_2}=1\ & ext{(d)}\ &rac{x}{y_1-y_2}+rac{y}{x_1-x_2}=1 \end{aligned}$$

A.
$$rac{x}{x_1+x_2}+rac{y}{y_1+y_2}=1$$

B. $rac{x}{x_1-x_2}+rac{y}{y_1-y_2}=1$

C.
$$\displaystyle rac{x}{y_1+y_2}+rac{y}{x_1+x_2}=1$$

D.
$$rac{x}{y_1-y_2} + rac{y}{x_1-x_2} = 1$$

Answer: A



36. Area of the quadrilateral formed with the foci of the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ and $\frac{x^2}{a^2} - \frac{y^2}{b^2} = -1$ (a) $4(a^2 + b^2)$ (b) $2(a^2 + b^2)$ (c) $(a^2 + b^2)$ (d) $\frac{1}{2}(a^2 + b^2)$

A.
$$4(a^2+b^2)$$

$$\mathsf{B.}\,2\big(a^2+b^2\big)$$

D.
$$rac{1}{2}ig(a^2+b^2ig)$$

Answer: B

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37. Let $P(a \sec \theta, b \tan \theta)$ and $A(a \sec \phi, b \tan \phi)$, where $\theta + \phi = \frac{\pi}{2}$, be two points on the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$. If (h, k) is the point of intersection of normals at P and Q. then k is equal to

A.
$$\left(rac{a^2+b^2}{a}
ight)$$

B. $-\left(rac{a^2+b^2}{a}
ight)$

$$\begin{array}{l} \mathsf{C}.\left(\frac{a^2+b^2}{b}\right)\\ \mathsf{D}.-\left(\frac{a^2+b^2}{b}\right) \end{array}$$

Answer: D



38. Let the major axis of a standard ellipse equals the transverse axis of a standard hyperbola and their director circles have radius equal to 2R and R respectively. If e_1 and e_2 , are the eccentricities of the ellipse and hyperbola then the correct relation

A. (a)
$$4e_1^2 - e_2^2 = 6$$

B. (b)
$$e_1^2 - 4e_2^2 = 2$$

C. (c)
$$4e_2^2 - e_1^2 = 6$$

D. (d)
$$e_2^2 - 4 e_1^2 = 2$$

Answer: C



39. The tangent to the hyperbola $xy = c^2$ at the point P intersects the x-axis at T and y- axis at T'.The normal to the hyperbola at P intersects the x-axis at N and the y-axis at N'. The areas of the triangles

PNT and PN'T' are Δ and Δ' respectively, then $\frac{1}{\Delta} + \frac{1}{\Delta}$ ' is

A. (a)equal to 1

B. (b)depends on t

C. (c)depends on c

D. (d)equal to 2

Answer: C



40. Let any double ordinate PNP^1 of the hyperbol $rac{x^2}{9}-rac{y^2}{4}=1$ be produced both sides to meet the asymptotes in Q and Q', then PQ. P'Q is equal to A. 9 **B**. 4 C. 25

Answer: B

D. 41



41. The coordinates of a point on the hyperbola $\frac{x^2}{24} - \frac{y^2}{18} = 1$ which is nearest to the line 3x + 2y + 1 = 0 are (6, 3) (b) (-6, -3) (6, -3) (d) (-6, 3)

A. (6, 3)

- B. (-6, -3)
- C. (6, -3)

D.
$$(-6, 3)$$

Answer: D

42. For each positive integer consider the point P with abscissa n on the curve $y^2 - x^2 = 1$. If d_n represents the shortest distance from the point P to the line y = x then $\lim_{n \to \infty} (nd_n)$ has the value equal to:

A. (a)
$$\frac{1}{2\sqrt{2}}$$

B. (b) $\frac{1}{2}$
C. (c) $\frac{1}{\sqrt{2}}$
D. (d) 0

Answer: A

43. If two tangents can be drawn the different branches of hyperbola $rac{x^2}{1}-rac{y^2}{4}=1$ from $(lpha,lpha^2)$, then

A.
$$lpha\in(-\infty,\ -2)$$

B. $lpha\in(-2,0)$
C. $lpha\in(0,2)$
D. $lpha\in(2,\infty)$

Answer: A::D



44. If the ellipse $x^2 + \lambda^2 y^2 = \lambda^2 a^2$, $\lambda^2 > 1$ is confocal with the hyperbola $x^2 - y^2 = a^2$, then a. ratio of eccentricities of ellipse and hyperbola is $1:\sqrt{3}$

b. ratio of major axis of ellipse and transverse axis of hyperbola is $\sqrt{3}$: 1

c. The ellipse and hyperbola cuts each other orthogonally

d. ratio of length of latusrectumof ellipse and hyperbola is 1:3

A. ratio of eccentricities of ellipse and hyperbola

is $1:\sqrt{3}$

B. ratio of major axis of ellipse and transverse

axis of hyperbola is $\sqrt{3}$: 1

C. The ellipse and hyperbola cuts each other

orthogonally

D. ratio of length of latusrectumof ellipse and

hyperbola is 1:3

Answer: A::B::C



45. If the circle $x^2 + y^2 = a^2$ intersects the hyperbola $xy = C^2$ at four points $P(x_1, y_1), Q(x_2, y_2), R(x_3, y_3),$ and $S(x_4, y_4),$ then proove $x_1 + x_2 + x_3 + x_4 = 0,$ $y_1 + y_2 + y_3 + y_4 = 0, x_1x_2x_3x_4 = C^4, y_1y_2y_3y_4 =$ C^4



46. A straight line touches the rectangular hyperbola $9x^2 - 9y^2 = 8$ and the parabola $y^2 = 32x$. An equation of the line is

A. $9x + 3y - 8 = \infty$

B.
$$9x - 3y + 8 = 0$$

C.
$$9x+3y+8=0$$

D.
$$9x - 3y - 8 = 0$$

Answer: B::C



47. The differential equation $\frac{dx}{dy} = \frac{3y}{2x}$ represents a family of hyperbolas (except when it represents a pair of lines) with eccentricity.

A.
$$\sqrt{\frac{7}{3}}$$

B. $\sqrt{\frac{5}{3}}$
C. $\sqrt{\frac{3}{2}}$
D. $\sqrt{\frac{5}{2}}$

Answer: B::D



48. A conic C satisfies the differential equation $(1 + y^2)dx - xydy = 0$ and passes through the point (1, 0). An ellipse E which is confocal with C



Q. find the length of the latus rectum of the conic C

A. 1

 $\mathsf{B.}\,2$

C. 3

 $\mathsf{D.}\,4$

Answer: B



49. A conic C satisfies the differential equation, $(1 + y^2)dx - xydy = 0$ and passes through the point (1, 0).An ellipse E which is confocal with C having its eccentricity equal to $\sqrt{\frac{2}{3}}$. find the equation of the ellipse E

A.
$$rac{x^2}{3} + rac{y^2}{1} = 1$$

B. $rac{x^2}{1} + rac{y^2}{3} = 1$
C. $rac{x^2}{4} + rac{y^2}{9} = 1$
D. $rac{x^2}{9} + rac{y^2}{4} = 1$

Answer: A

50. A conic C satisfies the differential equation $(1 + y^2)dx - xydy = 0$ and passes through the point (1, 0). An ellipse E which is confocal with C having its eccentricity equal to $\sqrt{\frac{2}{3}}$ Q. find the locus of the point of intersection of the

perpendicular tangents to the ellipse E

A.
$$x^2+y^2=4$$

$$\mathsf{B.}\,x^2+y^2=8$$

C.
$$x^2+y^2=10$$

D. $x^2+y^2=13$

Answer: A



51. For the hyperbola $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$, the normal at point P meets the transverse axis AA' in G and the connjugate axis BB' in g and CF be perpendicular to the normal from the centre. Q. The value $\frac{PF \cdot PG}{(CB^2)}$ is equal to

A. (a)4

B. (b)3

C. (c)2

D. (d)1

Answer: D

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52. For the hyperbola $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$, the normal at point P meets the transverse axis AA' in G and the connjugate axis BB' in g and CF be perpendicular to the normal from the centre. Q. The value $PF \cdot Pg$ is equal to

A.
$$\left(CA
ight)^2$$

 $\mathsf{B.}\left(CF\right) ^{2}$

$\mathsf{C.}\left(CB\right)^2$

$\mathsf{D.}\, CA\cdot CB$

Answer: A

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53. For the hyperbola $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$, the normal at point P meets the transverse axis AA' in G and the connjugate axis BB' in g and CF be perpendicular to the normal from the centre. Q. Locus of middle-point of G and g is a hyperbola of eccentricity

A.
$$\frac{1}{\sqrt{e^2-1}}$$

B.
$$\frac{e}{\sqrt{e^2-1}}$$

C. $2\left(\sqrt{e^2-1}\right)$
D. $\frac{e}{2}$

Answer: B



54. The equation of transverse axis of hyperbola (passing through origin) having asymptotes 3x - 4y = 1 and 4x - 3y = 6 is $ax + by - c = 0, a, b \in N$ and gcd(a, b, c) = 1 then the value of a + b + c is ____



55. If a variable line has its intercepts on the coordinate axes eande', where $\frac{e}{2}$ and $\frac{e}{2}$ are the eccentricities of a hyperbola and its conjugate hyperbola, then the line always touches the circle $x^2 + y^2 = r^2$, where r = 1 (b) 2 (c) 3 (d) cannot be decided



56. Statement-I Director circle of hypebola $rac{x^2}{a^2}-rac{y^2}{b^2}+1=0$ is defined only when $b\geq a.$

Statement-II Director circle of hyperbola $rac{x^2}{25}-rac{y^2}{9}=1$ is $x^2+y^2=16.$

A. Statement-I is true, Statement-II is also true, Statement-II is the correct explanation of Statement-I.

B. Statement-I is true, Statement-II is also true, Statement-II is not the correct explanation of Statement-I.

C. Statement-I is true, Statement-II is false.

D. Statement-I is false, Statement-II is true

Answer: B

57. Statement 1 : If a circle S = 0 intersects a hyperbola xy = 4 at four points, three of them being (2, 2), (4, 1) and $\left(6, \frac{2}{3}\right)$, then the coordinates of the fourth point are $\left(\frac{1}{4}, 16\right)$. Statement 2 : If a circle S = 0 intersects a hyperbola $xy = c^2$ at t_1, t_2, t_3 , and t_4 then $t_1t_2t_3t_4 = 1$

A. Statement-I is true, Statement-II is also true,

Statement-II is the correct explanation of

Statement-I.

B. Statement-I is true, Statement-II is also true,

Statement-II is not the correct explanation of

Statement-I.

C. Statement-I is true, Statement-II is false.

D. Statement-I is false, Statement-II is true

Answer: D

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58. Prove that the perpendicular focal chords of a

rectangular hyperbola are equal.

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59. The normal at three points P, Q, R on a rectangular hyperbola intersect at a point T on the curve. Prove that the centre of the hyperbola is the centroid of the triangle PQR.

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60. Find the equation of the hyperbola, whose asymptotes are the straight lines (x + 2y + 3) = 0, (3x + 4y + 5) = 0 and which passes through the point (1-1).



61. Evaluate
$$\frac{4!-2!}{2}$$

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62. A circle with centre $(3\alpha, 3\beta)$ and of variable radius cuts the rectangular hyperbola $x^2 - y^2 = 9a^2$ at the points P, Q, S, R. Prove that the locus of the centroid of triangle PQR is $(x - 2\alpha)^2 - (y - 2\beta)^2 = a^2$.

1. Show that the equation $7x^2 - 9y^2 + 54x - 28y - 116 = 0$ represent a hyperbola. Find the coordinate of the centre, lenghts of transverse and conjugate axes, eccentricity, latusrectum, coordinates of foci and vertices of the hyperbola.

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2. If SY and S'Y' be drawn perpendiculars from foci to any tangent to a hyperbola. Prove that y and Y'

lie on the auxiliary circle and that product of these

perpendicular is constant.



3. IF=f the diameter through any point any point P of a parabola meets any chord in A and the tangent at the end of the chord meets the diameter in B and C. then prove that $PA^2 = PB$. PC.



4. For the hyperbola $x^2 - y^2 = a^2$, prove that the triangle CPD is isosceles and has constant area, where CP and CD are a pair of its conjugate diameter.

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5. If the lines lx + my + n = 0 passes through the

extremities of a pair of conjugate diameters of the

hyperbola
$$rac{x^2}{a^2}-rac{y^2}{b^2}=1,$$
 show that $a^2l^2-b^2m^2=0.$

6. If any tangent to the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ with centre C, meets its director circle in P and Q, show that CP and CQ are conjugate semi-diameters of the hyperbola.



7. Show that the tangent at any point of a hyperbola cuts off a triangle of constant area from the asymptotes and that the portion of it intercepted between the asymptotes is bisected at the point of contact.



Jee Type Solved Examples Matching Type Questions

1. Find the 8^{th} term of the G.P ,whose 4^{th} term is 32

and the common ratio is 3.

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Jee Type Solved Examples Subjective Type Questions

1. Consider hyperbola xy = 22 to find the equation of

tangent at point (2, 11).



2. The tangent at the point P of a rectangular hyperbola meets the asymptotes at L and M and C is the centre of the hyperbola. Prove that PL = PM = PC

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3. Evaluate (2! + 3!)

4. The vertex of the parabola $y^2 = 4ax$ is



5. If the normals at four points $P(x_iy_i), i=1,2,3,4$ on the rectangular hyperbola $xy=c^2$, meet at the point Q(h, k), then prove that $x_1+x_2+x_3+x_4=h$

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6. Find the first five terms of the following sequence

and obtain the corresponding series :

$$a_1=a_2=3, a_n=a_{n-2}+1, n\geq 3$$

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Exercise For Session 1

1. The eccentricity of the conic represented by $x^2-y^2-4x+4y+16=0$ is 1 (b) $\sqrt{2}$ (c) 2 (d) $rac{1}{2}$

- A. 1
- $\mathsf{B}.\,\frac{1}{2}$
- C. -1

D.
$$\sqrt{2}$$

Answer: D



2. If e_1 and e_2 represent the eccentricity of the curves $6x^2 - 9y^2 = 144$ and $9x^2 - 16y^2 = 144$ respectively. Then $\frac{1}{e_1^2} + \frac{1}{e_2^2}$ is equal to

A.
$$e_1^2 - e_2^2 = 1$$

- B. $e_1^2 e_2^2 < 3$
- ${\sf C}.\, e_1^2 e_2^2 = 3$

D.
$$e_1^2 - e_2^2 > 3$$

Answer: B



3. The transverse axis of a hyperbola is of length 2a and a vertex divides the segment of the axis between the centre and the corresponding focus in the ratio 2:1. The equation of the hyperbola is

A.
$$4x^2-5y^2=4a^2$$

B.
$$4x^2 - 5y^2 = 5a^2$$

C.
$$5x^2-4y^2=4a^2$$

D.
$$5x^2 - 4y^2 = 5a^2$$

Answer: D



4. The eccentricity of the hyperbola whose latusrectum is 8 and length of the conjugate axis is equal to half the distance between the foci, is

A.
$$\frac{2}{\sqrt{3}}$$

B.
$$\frac{3}{\sqrt{3}}$$

C.
$$\frac{4}{\sqrt{3}}$$

D.
$$\frac{5}{\sqrt{3}}$$

Answer: A

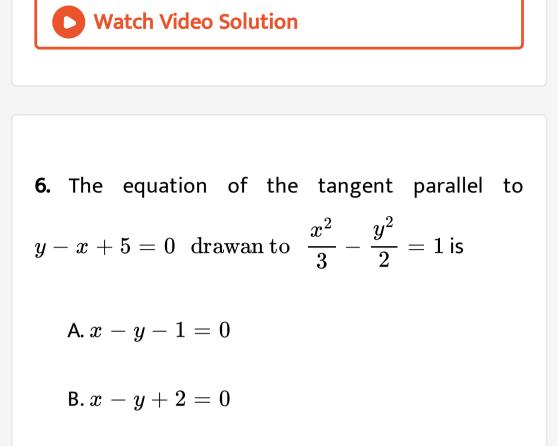


5. The straight line $x+y=\sqrt{2}P$ will touch the hyperbola $4x^2-9y^2=36$ if

A.
$$p^2=2$$

B. $p^2=5$
C. $p^2=rac{2}{5}$
D. $p^2=rac{2}{5}$

Answer: D



- C. x + y 1 = 0
- D. x+y+2=0`

Answer: A

7. If e and e' are the eccentricities of the hyperbola

$$rac{x^2}{a^2}-rac{y^2}{b^2}=1$$
 and $rac{y^2}{b^2}-rac{x^2}{a^2}=1$, then the point $\left(rac{1}{e},rac{1}{e'}
ight)$ lies on the circle:

A.
$$x^2+y^2=1$$

$$\mathsf{B.}\,x^2+y^2=2$$

$$\mathsf{C.}\,x^2+y^2=3$$

D.
$$x^2 + y^2 = 4$$

Answer: A



8. If e and e' are the eccentricities of the ellipse $5x^2+9y^2=45$ and the hyperbola $5x^2-4y^2=45$ respectively , then ee' is equal to

A. -1

B. 1

C.-4

D. 9

Answer: B



9. The equation $rac{x^2}{10-\lambda}+rac{y^2}{6-\lambda}=1$ represents

A. a hyperbola if $\lambda < 6$

B. an ellipse if $\lambda > 6$

C. a hyperbola if $6 < \lambda < 10$

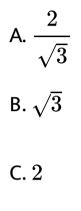
D. an ellipse if $0 < \lambda < 6$

Answer: C::D



10. Find the centre, eccentricity, foci and directrices

of the hyperbola : $x^2 - 3y^2 - 2x = 8$.



D. $\sqrt{2}$

Answer: (c)



11. For hyperbola $x^2 \sec^2 lpha - y \cos ec^2 lpha = 1$, which of the following remains constant with change in 'lpha'

A. abscissae of vertices

B. abscissae of foci

C. eccentricity

D. directrix

Answer: B

12. If the foci of the ellipse $rac{x^2}{16}+rac{y^2}{b^2}=1$ and the hyperbola $rac{x^2}{144}-rac{y^2}{81}=rac{1}{25}$ coincide, then find the value b^2

A. `1

B. 5

C. 7

D. 9

Answer: (c)

13. Find the standard equation of hyperbola in each

of the following cases:

(i) Distance between the foci of hyperbola is 16 and its eccentricity is $\sqrt{2}$.

(ii) Vertices of hyperbola are $(\pm 4, 0)$ and foci of hyperbola are $(\pm 6, 0)$.

(iii) Foci of hyperbola are $\left(0, \ \pm \sqrt{10}
ight)$ and it passes

through the point (2,3).

(iv) Distance of one of the vertices of hyperbola from the foci are 3 and 1.

14. Find the equation of the hyperbola whose foaci

are (0, 5) and (-2, 5) and eccentricity 3.



15. Prove that the straight lines
$$\frac{x}{a} - \frac{y}{b} = m$$
 and $\frac{x}{a} + \frac{y}{b} = \frac{1}{m}$, where *a* and *b* are given positive real numbers and '*m*' is a parameter, always meet on a hyperbola.

16. Find the centre, eccentricity and length of axes

of the hyperbola $3x^2 - 5y^2 - 6x + 20y - 32 = 0$.

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17. The eccentricity of the conjugate hyperbola of the hyperbola $x^2-3y^2=1$ is (a) 2 (b) $2\sqrt{3}$ (c) 4 (d) $\frac{4}{5}$



18. If the line $y=3x+\lambda$ touches the hyperbola $9x^2-5y^2=45$, then λ =

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19. Find the equation of tangents to the curve

 $4x^2 - 9y^2 = 1$ which are parallel to 4y = 5x + 7.

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Exercise For Session 2

1. Find the equation of tangent to the hyperbola $16x^2 - 25y^2 = 400$ perpendicular to the line x - 3y = 4.

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2. If
$$4x^2 + py^2 = 45$$
 and $x^2 - 4y^2 = 5$ cut

orthogonally, then the value of p is

A.
$$\frac{1}{9}$$

B. $\frac{1}{3}$

C. 9

D. 18

Answer: C

3. If the tangent at the point
$$(2 \sec \theta, 3 \tan \theta)$$
 to
the hyperbola $\frac{x^2}{4} - \frac{y^2}{9} = 1$ is parallel to
 $3x - 4y + 4 = 0$, then the value of θ , is

A.
$$\frac{\pi}{6}$$

B. $\frac{\pi}{4}$
C. $\frac{\pi}{3}$

Answer: A

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4. If the line $2x + \sqrt{6}y = 2$ touches the hyperbola $x^2 - 2y^2 = 4$, then the point of contact is $(-2, \sqrt{6})$ (b) $(-5, 2\sqrt{6})$ $\left(\frac{1}{2}, \frac{1}{\sqrt{6}}\right)$ (d) $(4, -\sqrt{6})$ B. $(-5, 2\sqrt{6})$

$$\mathsf{C}.\left(\frac{1}{2},\frac{1}{\sqrt{6}}\right.$$
$$\mathsf{D}.\left(4,\ -\sqrt{6}\right)$$

Answer: D



5. Find the equation of the chord of the hyperbola $25x^2 - 16y^2 = 400$ which is bisected at the point (5, 3).

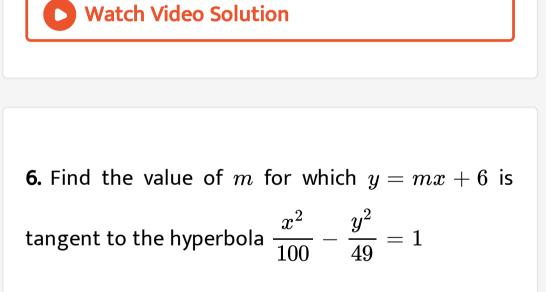
A.
$$115x - 47y = 434$$

B.
$$125x - 48y = 481$$

C.127x - 49y = 488

D.
$$155x - 67y = 574$$

Answer: B



A.
$$\sqrt{\frac{17}{20}}$$

B. $-\sqrt{\frac{17}{21}}$
C. $\sqrt{\frac{20}{17}}$

$$\mathsf{D.}-\sqrt{\frac{21}{17}}$$

Answer: A

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7. P is a point on the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$, and N is the foot of the perpendicular from P on the transverse axis. The tantent to the hyperbola at P meets the transverse axis at T. If O is the centre of the hyperbola, then OT.ON is equal to

A.
$$a^2$$

 $\mathsf{B.}\,b^2$

 $\mathsf{C}. e^2$

D. `b^(2)la

Answer: A



8. Find the first five terms of the following sequence

$$a_1=a_2=1, a_n=a_{n-1}+a_{n-2}, n\geq 3$$

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9. Find the first five terms of the following sequence

whose n^{th} term is $a_n = 5n+3$

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10. The tangent at a point P on the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ passes through the point (0, -b) and the normal at P passes through the point $(2a\sqrt{2}, 0)$. Then the eccentricity of the hyperbola is

A.
$$\frac{5}{4}$$

B. $\frac{3}{2}$

C. $\sqrt{2}$

D. $2\sqrt{2}$

Answer: C

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11. A tangent to the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ cuts the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ at PandQ. Show that the locus of the midpoint of PQ is $\left(\frac{x^2}{a^2} + \frac{y^2}{b^2}\right)^2 = \frac{x^2}{a^2} - \frac{y^2}{b^2}$.

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12. A line through the origin meets the circle $x^2 + y^2 = a^2$ at P and the hyperbola $x^2 - y^2 = a^2$ at Q. Prove that the locus of the point of intersection of tangent at P to the circle with the tangent at Q to the hyperbola is a straight line.

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13. Find the 6^{th} term of the following sequence whose n^{th} term is $a_n = 4n^2 + 7$

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14. Chords of the hyperbola, $x^2 - y^2 = a^2$ touch the parabola, $y^2 = 4ax$. Prove that the locus of their middlepoints is the curve, $y^2(x-a) = x^3$.

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Exercise For Session 3

1. The diameter of $16x^2 - 9y^2 = 144$ which is conjugate to x = 2y is

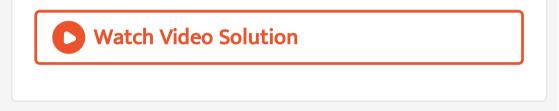
A.
$$y=rac{16}{9}x$$

B. $y=rac{32}{9}x$

C.
$$x=rac{16}{9}y$$

D. $x=rac{32}{9}y$

Answer: B



2. Tangents drawn from a point on the circle $x^2+y^2=9$ to the hyperbola $rac{x^2}{25}-rac{y^2}{16}=1,$

then tangents are at angle

A. (a)
$$\frac{\pi}{6}$$

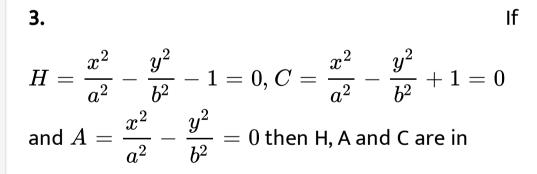
B. (b) $\frac{\pi}{4}$

C. (c)
$$\frac{\pi}{3}$$

D. (d) $\frac{\pi}{2}$

Answer: D





B. (b) GP

C. (c) HP

D. (d) AGP

Answer: A

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4. Find the angle between the asymptotes of the

hyperbola
$$rac{x^2}{16} - rac{y^2}{9} = 1.$$

A. $an^{-1} igg(rac{2}{3} igg)$
B. $an^{-1} igg(rac{3}{2} igg)$
C. $2 an^{-1} igg(rac{2}{3} igg)$

$$\mathsf{D}.\,2\tan^{-1}\!\left(\frac{3}{2}\right)$$

Answer: D

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5. If e and e_1 , are the eccentricities of the hyperbolas $xy=c^2$ and $x^2-y^2=c^2$, then $e^2+e_1^2$ is equal to

A. a) 2

B. b) 4

C. c) 6

D. d) 8

Answer: D



6. Find the product of the length of perpendiculars drawn from any point on the hyperbola $x^2 - 2y^2 - 2 = 0$ to its asymptotes.

A.
$$\frac{1}{2}$$

B. 2

 $-\frac{1}{3}$

Answer: C

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7. The number of points on the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 3$ from which mutually perpendicular tangents can be drawn to the circle $x^2 + y^2 = a^2$ is/are (a)0 (b) 2 (c) 3 (d) 4

A. 0

C. 3

D. 4

Answer: A

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8. If the sum of the slopes of the normal from a point P to the hyperbola $xy=c^2$ is equal to $\lambda(\lambda\in R^+)$, then the locus of point P is (a) $x^2=\lambda c^2$ (b) $y^2=\lambda c^2$ (c) $xy=\lambda c^2$ (d) none of these

A.
$$x^2=\lambda c^2$$

B.
$$y^2=\lambda c^2ig)$$

C.
$$xy = \lambda c^2$$

D. None of these

Answer: A



9. If S=0 is the equation of the hyperbola $x^2+4xy+3y^2-4x+2y+1=0$, then the value of K for which S+K=0 represents its asymptotes is (a)20 (b) -16 (c) -22 (d) 18

A. 20

 $B.\,18$

C. -16

D. - 22

Answer: D

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10. A ray emanating from the point $(\sqrt{41}, 0)$ is incident on the hyperbola $16x^2 - 25y^2 = 400$ at the point P with abscissa10.Find the equation of a reflected ray after first reflection and point P lies in 2nd quadrant is

A.
$$4\sqrt{3} - (10 - \sqrt{41})y + 4\sqrt{123} = 0$$

B. $4\sqrt{3} + (10 - \sqrt{41})y - 4\sqrt{123} = 0$
C. $4\sqrt{3} + (10 - \sqrt{41})y + 4\sqrt{123} = 0$
D. $4\sqrt{3} - (10 - \sqrt{41})y - 4\sqrt{123} = 0$

Answer: B



11. If a ray of light incident along the line
$$3x + (5 - 4\sqrt{2})y = 15$$
 gets reflected from the hyperbola $\frac{x^2}{16} - \frac{y^2}{9} = 1$, then its reflected ray goes along the line

A.
$$x\sqrt{2}-y+5=0$$

B.
$$y\sqrt{2}-x+5=0$$

C.
$$y\sqrt{2}-x-5=0$$

D. None of these

Answer: D



12. The equation of the transvers and conjugate axes of a hyperbola are, respectively, x + 2y - 3 = 0 and 2x - y + 4 = 0, and their respective lengths are $\sqrt{2}$ and $\frac{2}{\sqrt{3}}$. The equation

of the hyperbola is

a)
$$\frac{2}{5}(x+2y-3)^2 - \frac{3}{5}(2x-y+4)^2 = 1$$

b) $\frac{2}{5}(x-y-4)^2 - \frac{3}{5}(x+2y-3)^2 = 1$
c) $\frac{2}{5}(2x-y+4)^2 - \frac{3}{5}(x+2y-3)^2 = 1$
d) $2(x+2y-3)^2 - 3(2x-y+4)^2 = 1$

A.
$$2{(x+2y-3)}^2-3{(2x-y+4)}^2=5$$

B.
$$2(2x - y + 4)^2 - 3(x + 2y - 3)^2 = 5$$

 $\mathsf{C.} \ 2{(x+2y-3)}^2 - 3{(2x-y+4)}^2 = 1$

D.
$$2(2x - y + 4)^2 - 3(x + 2y - 3)^2 = 1$$

Answer: B



13. Find the equation of that diameter which bisects the chord 7x + y - 2 = 0 of the hyperbola $\frac{x^2}{3} - \frac{y^2}{7} = 1.$



14. Find the equation of the hyperbola which has 3x - 4y + 7 = 0 and 4x + 3y + 1 = 0 as its asymptotes and which passes through the origin.

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15. The asymptotes of the hyperbola centre of the point (1, 2) are parallel to the lines 2x + 3y = 0 and 3x + 2y = 0. If the hyperbola passes through the points (5, 3), show that its equation is (2x + 3y - 8)(3x + 2y + 7) = 154

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16. If the pair of straight lines
$$Ax^2 + 2Hxy + By^2 = 0$$
 be conjugate diameters of the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$, then prove that $Aa^2 = Bb^2$.

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17. A circle cuts the rectangular hyperbola xy=1

in the points $(x_r,y_r), r=1,2,3,4.$

Prove that $x_1x_2x_3x_4=y_1y_2y_3y_4=1$



1. P is any point on the hyperbola $x^2 - y^2 = a^2$. If F_1 and F_2 are the foci of the hyperbola and $PF_1 \cdot PF_2 = \lambda (OP)^2$. Where O is the origin, then λ is equal to

A. 1

 $\mathrm{B.}\,\sqrt{2}$

 $\mathsf{C.}\,2$

 $\mathsf{D.3}$

Answer: A



2. If the sum of the slopes of the normal from a point P to the hyperbola $xy=c^2$ is equal to $\lambda(\lambda\in R),$ then the locus of point P is

A.
$$x^2-y^2=\lambda c^2$$

B.
$$y^2=\lambda c^2ig)$$

C.
$$xy=\lambda c^2$$

D.
$$x^2=\lambda c^2$$

Answer: D

3. If $xy = \lambda^2 - 9$ be a rectangular hyperbola whose branches lie only in the second and fourth quadrant, then

A. $|\lambda| \geq 3$

B. $|\lambda| < 3$

 $\mathsf{C}.\,\lambda\in R-\{\,-\,3,\,3\}$

D. None of these

Answer: B



4. If there are two points A and B on rectangular hyperbola $xy=c^2$ such that abscissa of A=ordinate of B, then locusof point of intersection of tangents at A and B is (a) $y^2 - x^2 = 2c^2$ (b) $y^2-x^2=rac{c^2}{2}$ (c) y=x (d) non of these A. $y^2 = x^2 + 2c^2$ B. $y^2 = x^2 + \frac{c^2}{2}$ $\mathsf{C}. y = x$ D. y = 3x

Answer: C

5. A series of hyperbola are drawn having a common transverse axis of length 2a. Prove that the locus of point P on each hyperbola, such that its distance from the transverse axis is equal to its distance from an asymptote, is the curve $\left(x^2-y^2
ight)^2=\lambda x^2(x^2-a^2), ext{ then }\lambda ext{ equals}$ A. $(x^2 - y^2)^2 = 4x^2(x^2 - a^2)$ B. $(x^2 - y^2)^2 = x^2(x^2 - a^2)$ C. $(x^2 - y^2)^2 = 4y^2(x^2 - a^2)$ D. $(x^2 - y^2)^2 = y^2(x^2 - a^2)$

Answer: A



6. If a rectangular hyperbola (x-1)(y-2) = 4cuts a circle $x^2 + y^2 + 2gx + 2fy + c = 0$ at points (3, 4), (5, 3), (2, 6) and (-1, 0), then the value of (g + f) is equal to

 $\mathsf{A.\,a)}-3$

B.b) -9

C. c) 8

D. d) 9

Answer: A



7. If p, q, r, s ae rational numbers and the roots of f(x) = 0 are eccentricities of a parabola and a rectangular hyperbola, where $f(x0 = px^3 + qx^2 + rx + s, thenp + q + r + s = p$ b. -p c. 2p d. 0

A. - 1

B. 0

C. 1

D. data inadequate

Answer: B



8. From a point on the line y = x + c, c(parameter), tangents are drawn to the hyperbola $\frac{x^2}{2} - \frac{y^2}{1} = 1$ such that chords of contact pass through a fixed point (x_1, y_1) . Then, $\frac{x_1}{y_1}$ is equal to

A. 2

C.4

D. None of these

Answer: A

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9. Find the 11^{th} term of the following sequence whose n^{th} term is $a_n = (-1)^{n+1}(5n-10)$

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10. The number of points outside the hyperbola $\frac{x^2}{9} - \frac{y^2}{16} = 1$ from where two perpendicular tangents can be drawn to the hyperbola are:

A. 0

B. 1

 $\mathsf{C.}\,2$

D. None of these

Answer: A



11. Let A = (-3, 4) and B = (2, -1) be two fixed points. A point C moves such that $\tan\left(\frac{1}{2}\angle ABC\right): \tan\left(\frac{1}{2}\angle BAC\right) = 3:1$ Thus, locus of C is a hyperbola, distance between

whose foci is

 $\mathsf{A.}\,5$

B. $5\sqrt{2}$ C. $\frac{5}{2}$ D. $\frac{5}{\sqrt{2}}$

Answer: B

12. A point P is taken on the right half of the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ having its foci as S_1 and S_2 . If the internal angle bisector of the angle $\angle S_1 P S_2$ cuts the x-axis at poin $Q(\alpha, 0)$ then range of α is

A. a. [-a, a]B. b. [0, a]C. c. (0, a]D. d. [-a, 0]

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Answer: C

13. If the angle between the asymptotes of hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ is 120^0 and the product of perpendiculars drawn from the foci upon its any tangent is 9, then the locus of the point of intersection of perpendicular tangents of the hyperbola can be $x^2 + y^2 = 6$ (b) $x^2 + y^2 = 9$ $x^2 + y^2 = 3$ (d) $x^2 + y^2 = 18$

A.
$$x^2+y^2=3$$

$$\mathsf{B.}\,x^2+y^2=6$$

C.
$$x^2+y^2=9$$

D.
$$x^2+y^2=18$$

Answer: D

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14. If $\alpha + \beta = 3\pi$, then the chord joining the points α and β for the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ passes through which of the following points? Focus (b) Center One of the endpoints of the transverse exis. One of the endpoints of the conjugate exis.

B. centre

C. one of the end point of the transverse axis

D. one of the end of the conjugate axis

Answer: B



15. If
$$rac{x^2}{a^2} + rac{y^2}{b^2} = 1 (a > b)$$
 and $x^2 - y^2 = c^2$ cut

at right angles, then:

A.
$$a^2+b^2=2c^2$$

$$\mathsf{B}.\,b^2-a^2=2c^2$$

C.
$$a^2-b^2=2c^2$$

D.
$$a^2b^2=2c^2$$

Answer: C



16. Find the 15^{th} term of the following sequence whose n^{th} term is $a_n = (-1)^{n+1}(2n-5)$

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17. An ellipse has eccentricity $\frac{1}{2}$ and one focus at the point P $\left(\frac{1}{2},1\right)$. Its one directrix is the common tangent nearer to the point P, to the circle $x^2 + y^2 = 1$ and the hyperbola $x^2 - y^2 = 1$. The equation of the ellipse is standard form is

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18. The equation of the line passing through the centre of a rectangular hyperbola is x - y - 1 = 0. If one of its asymptotoes is 3x - 4y - 6 = 0, the equation of the other asymptote is A. 4x - 3y + 8 = 0

B.
$$4x + 3y + 17 = 0$$

C. 3x - 2y + 15 = 0

D. 4x+3y-17=0

Answer: B

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19. The condition that a straight line with slope m will be normal to parabola $y^2 = 4ax$ as well as a tangent to rectangular hyperbola $x^2 - y^2 = a^2$ is

A. a)
$$m^6 - 4m^2 + 2m - 6y = 0$$

B. b)
$$m^4 + 3m^3 + 2m + 1 = 0$$

C. c)
$$m^6-2m=0$$

D. d)
$$m^6 + 4m^4 + 3m^2 + 1 = 0$$

Answer: D

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20. Find the locus of the midpoints of chords of hyperbola $3x^2 - 2y^2 + 4x - 6y = 0$ parallel to y = 2x.

A.
$$3x-4y=4$$

B.
$$3y - 4x + 4 = 0$$

$$\mathsf{C.}\,4x-4y=3$$

D.
$$3x - 4y = 2$$

Answer: A



21. The co-ordinates of the centre of the hyperbola,

$$x^2 + 3xy + 3y^2 + 2x + 3y + 2 = 0$$
 is

A.
$$(\,-1,0)$$

B.(1,0)

$$\mathsf{C.}~(-1,1)$$

D.
$$(1, -1)$$

Answer: A



22. Find the
$$5^{th}$$
 term of the G.P , $\frac{1}{2}, \frac{1}{4}, \frac{1}{8}$

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23. Locus of the point of intersection of the tangents at the points with eccentric angles $\phi \,\, {
m and} \,\, {\pi \over 2} - \phi \, {
m on} \, {
m the} \, {
m hyperbola} \, {x^2 \over a^2} - {y^2 \over b^2} = 1 \, {
m is}$ A. x = a $\mathsf{B}.\, y = b$ $\mathsf{C}. x = ab$ D. y = abAnswer: B



24. Latusrectum of the conic satisfying the differential equation xdy + ydx = 0 and passing through the point (2, 8) is

A. $4\sqrt{2}$

B. 8

C. $8\sqrt{2}$

D. 16

Answer: C



25. The point of intersection of the curve whose parametrix equations are $x = t^2 + 1, y = 2t$ and $x = 2s, y = \frac{2}{s}$, is given by

- A. (1, -3)
- B.(2,2)
- C. (-2, 4)
- D.(1, 2)

Answer: B



26. If the tangent and normal to a rectangular hyperbola cut off intercepts a_1 and a_2 on one axis and b_1 and b_2 on the other, then

A.
$$a_1b_1+a_2b_2=0$$

B.
$$a_1b_2+a_2b_1=0$$

C.
$$a_1 a_2 + b_1 b_2 = 0$$

D. None of these

Answer: C

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27. The focus of rectangular hyperbola
$$(x-a)\cdot(y-b)=c^2$$
 is
A. (a) $(h-p,k-p)$
B. (b) $(h-p,k+p)$
C. (c) $(h+p,k-p)$

D. (d) None of these

Answer: A



28. The equation of a hyperbola conjugate to the hyperbola $x^2 + 3xy + 2y^2 + 2x + 3y = 0$ is A. $x^2 + 3xy + 2y^2 + 2x + 3y + 1 = 0$ B. $x^2 + 3xy + 2y^2 + 2x + 3y + 2 = 0$ C. $x^2 + 3xy + 2y^2 + 2x + 3y + 3 = 0$ D. $x^2 + 3xy + 2y^2 + 2x + 3y + 4 = 0$

Answer: B

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29. If the values of m for which the line $y=mx+2\sqrt{5}$ touches the hyperbola $16x^2-9y^2=144$ are the roots of the equation $x^2-(a+b)x-4=0$, then the value of a+b is

- $\mathsf{A}.-2$
- **B**. 0
- $\mathsf{C.}\,2$
- $\mathsf{D.}\,4$

Answer: B



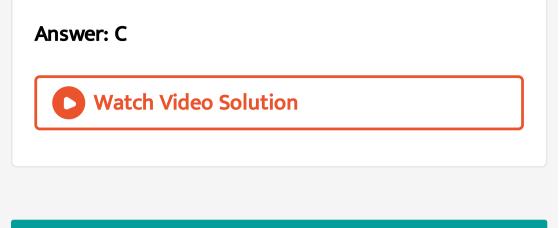
30. Let *C* be a curve which is the locus of the point of intersection of lines x = 2 + m and my = 4 - m. A circle $s \equiv (x - 2)^2 + (y + 1)^2 = 25$ intersects the curve *C* at four points: *P*, *Q*, *R*, and*S*. If *O* is center of the curve *C*, then $OP^2 + OQ^2 + OR^2 + OS^2$ is (a) 25 (b) 50 (c) 100 (d) 200

A. 25

B. 50

C. 100

D. 200



Exercise More Than One Correct Option Type Questions

1. The equation of common tangent to the parabola

$$y^2=8x$$
 and hyperbola $3x^2-y^2=3$ is

A.
$$2x - y + 1 = 0$$

$$\mathsf{B}.\,2x-y-1=0$$

C.
$$2x + y + 1 = 0$$

D.
$$2x + y - 1 = 0$$

Answer: A::C

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2. If the length of minor axis of the ellipse $\frac{x^2}{k^2a^2} + \frac{y^2}{b^2} = 1$ is equal to the length of transverse axis of hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$, and the equation of ellipse is confocal with hyperbola then the value k is equal to

A.
$$-\sqrt{2}$$

 $\mathsf{B.}\,\sqrt{2}$

 $\mathsf{C}.-\sqrt{3}$

D. $\left(\sqrt{3}\right)$

Answer: C::D

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3. If $(a \sec \theta, b \tan \theta)$ and $(a \sec \phi, b \tan \phi)$ are the ends of a focal chord of $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$, then prove that $\tan \frac{\theta}{2} \tan \frac{\phi}{2} = \frac{1-e}{1+e}$.

A.
$$\frac{e-1}{e+1}$$

$$B. \frac{1-e}{1+e}$$

$$C. \frac{1+e}{1-e}$$

$$D. \frac{e+1}{e-1}$$

Answer: B::C

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4. If foci of
$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$
 coincide with the foci of $\frac{x^2}{25} + \frac{y^2}{16} = 1$ and eccentricity of the hyperbola is 3. then

A.
$$a^2 + b^2 = 9$$

B. there is no directrix circle to the hyperbola

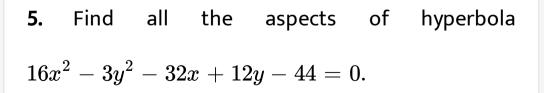
C. centre of the directrix circle is (0, 0)

D. Length of the latusrecum of the hyperbola

=16

Answer: A::B::D

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A. length of the transverse axis= $2\sqrt{3}$

B. length of the conjugate axis =8

C. centre at
$$(1,\ -2)$$

D. eccentricity
$$=\sqrt{19}$$

Answer: A::B::C

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6. If the line ax+by+c=0 is a normal to the curve xy=1, then a>0, b>0 a>0, b<0 a>0, b<0 a<0, b<0 (d) a<0, b<0 none of these

A.
$$a>0, b\geq 0$$

$$\mathsf{B.}\,a>0,b<0$$

$$\mathsf{C}.\,a<0,b>0$$

D. a < 0, b < 0

Answer: B::C



7. The sum of 3 numbers of an arithmetic progression is 24 and their product is 44. Find the three numbers.



8. The line y = x + 5 touches

A. the parabola $y^2=20x$

B. the ellipse $9x^2 + 16y^2 = 144$

C. the hyperbola $rac{x^2}{29} - rac{y^2}{4} = 1$

D. the circle $x^2+y^2=25$

Answer: A::B::C



9. The coordinates of a point common to a directrix and an asymptote of the hyperbola $rac{x^2}{25} - rac{y^2}{16} = 1$

are

$$A.\left(\frac{25}{\sqrt{41}}, \frac{20}{\sqrt{41}}\right)$$
$$B.\left(\frac{-25}{\sqrt{41}}, \frac{-20}{\sqrt{41}}\right)$$
$$C.\left(\frac{25}{3}, \frac{20}{3}\right)$$
$$D.\left(\frac{-25}{3}, \frac{-20}{3}\right)$$

Answer: A::B



10. If (5,12) and (24,7) are the foci of a conic passing

through the origin, then the eccentricity of conic is

A.
$$e = \frac{\sqrt{386}}{12}$$

B. $e = \frac{\sqrt{386}}{13}$
C. latusrectum $= \frac{121}{3}$
D. latusrectum $= \frac{121}{6}$

Answer: A::D



11. For the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$, let n be the number of points on the plane through which perpendicular tangents are drawn.

A. If n=1, then $e=\sqrt{2}$

B. if n>1, then $0 < e < \sqrt{2}$

C. if n=0, then $e > \sqrt{2}$

D. None of these

Answer: A::B::C

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12. Find the n^{th} term of the G.P , $\frac{1}{3}, \frac{1}{6}, \frac{1}{12}$



13. Length of common tangents to the hyperbolas $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1 \text{ and } \frac{y^2}{a^2} - \frac{x^2}{b^2} = 1 \text{ is}$ A. $y = x + \sqrt{a^2 - b^2}$ B. $y = x - \sqrt{a^2 - b^2}$ C. $y = -x + \sqrt{a^2 - b^2}$ D. $y = -x - \sqrt{a^2 - b^2}$

Answer: A::B::C::D



14. Given ellipse $rac{x^2}{16}+rac{y^2}{17}=1$ and the hyperbola $rac{x^2}{144}-rac{y^2}{81}=rac{1}{25}$, if the ordinate of one of the points of intersection is produced to cut asymptote at P, then which of the following is true? A. They have the same foci B. Square of the ordinate of point of intersection is $\frac{63}{25}$

C. Sum of the squares of coordinate of P is 16

D. P lies on the auxiliary circle formed by ellipse

Answer: A::B::C::D



- 15. Solutions of the differential equation $ig(1-x^2ig)rac{dy}{dx}+xy=ax$ where $\mathsf{a}\in\mathsf{R}$ is
 - A. a conic which is an ellipse
 - B. centre of the conic is (0, a)
 - C. length of one of the principal axes is 1
 - D. length of one of the principal axes is equal to

Answer: A::B::D



Exercise Passage Based Questions

1. The graph of the conic $x^2 - (y-1)^2 = 1$ has one tangent line with positive slope that passes through the origin . The point of the tangency being (a, b) then find the value of $\sin^{-1}\left(\frac{a}{b}\right)$

A.
$$\frac{5\pi}{12}$$

B. $\frac{\pi}{6}$

C.
$$\frac{\pi}{4}$$

D. $\frac{\pi}{3}$

Answer: C



2. The graph of the conic $x^2 - (y-1)^2 = 1$ has one tangent line with positive slope that passes through the origin. The point of tangency being (a, b).

Length of the latusrectum of the conic is

(a) 1 (b) $\sqrt{2}$ (c) 2 (d) 4

A. 1

 $\mathsf{B.}\,\sqrt{2}$

 $\mathsf{C}.2$

 $\mathsf{D.}\,4$

Answer: C

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3. The graph of the conic $x^2 - (y-1)^2 = 1$ has one tangent line with positive slope that passes through the origin. The point of tangency being (a, b). Q. If e be the eccentricity of the conic, then the value of $\left(1+e^2+e^4
ight)$ is

A. 3

 $\mathsf{B.7}$

$$\mathsf{C}.\,\frac{7}{4}$$

 $\mathsf{D}.\,21$

Answer: B



4. A point P moves such that the sum of the slopes of the normals drawn from it to the hyperbola xy = 16 is equal to the sum of ordinates of feet of normals . The locus of P is a curve C.

the equation of the curve C is

A.
$$x^2=2y$$

B. $x^2=4y$
C. $x^2=6y$
D. $x^2=8y$

Answer: B

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5. Find the 8^{th} term of the G.P , $\frac{7}{2}, \frac{7}{4}, \frac{7}{8}$

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6. A point P moves such that the sum of the slopes of the normals drawn from it to the hyperbola xy = 4 is equal to the sum of the ordinates of feet of normals. The locus of P is a curve C. Q. The area of the equilateral triangle inscribed in the curve C having one vertex as the vertex of curve C is A. (a) $8\sqrt{3}$ sq. units

B. (b) $12\sqrt{3}$ sq. units

C. (c) $27\sqrt{3}$ sq. units

D. (d) $16\sqrt{3}$ sq. units

Answer: D

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7. Let P(x, y) be a variable point such that

$$\left| \sqrt{\left(x-1
ight)^2 + \left(y-2
ight)^2} - \sqrt{\left(x-5
ight)^2 + \left(y-5
ight)^2}
ight| = 3$$

which represents a hyperbola.

The locus of the intersection of two perpendicular

tangents to the hyperbola is

A.
$$\frac{5}{4}$$

B. $\frac{4}{3}$
C. $\frac{5}{3}$
D. $\frac{3}{2}$

Answer: C



8. Let P(x, y) be a variable point such that $\left|\sqrt{(x-1)^2 + (y-2)^2} - \sqrt{(x-5)^2 + (y-5)^2} \right| = 4$ which represents a hyperbola. Q. Locus of point of intersection of two

perpendicular tangents to the hyperbola is

A.
$$(x-3)^2 + \left(y - \frac{7}{2}\right)^2 = \frac{1}{4}$$

B. $(x-3)^2 + \left(y - \frac{7}{2}\right)^2 = \frac{3}{4}$
C. $(x-3)^2 + \left(y - \frac{7}{2}\right)^2 = \frac{5}{4}$
D. $(x-3)^2 + \left(y - \frac{7}{2}\right)^2 = \frac{7}{4}$

Answer: D

9. Let P(x, y) be a variable point such that $\left|\sqrt{\left(x-1
ight)^2+\left(y-2
ight)^2}-\sqrt{\left(x-5
ight)^2+\left(y-5
ight)^2}=4
ight.$

which represents a hyperbola.

Q. If origin is shifted to point $\left(3, \frac{7}{2}\right)$ and axes are rotated in anticlockwise through an angle θ , so that the equation of hyperbola reduces to its standard form $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$, then θ equals

A.
$$\tan^{-1}\left(\frac{4}{3}\right)$$

B. $\tan^{-1}\left(\frac{3}{4}\right)$
C. $\tan^{-1}\left(\frac{5}{4}\right)$

$$\mathsf{D}.\tan^{-1}\left(\frac{4}{5}\right)$$

Answer: B

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10. Let $P(\theta_1)$ and $Q(\theta_2)$ are the extremities of any focal chord of the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ whose eccentricity is e. Let θ be the angle between its asymptotes. Tangents are drawn to the hyperbola at some arbitrary points R. These tangent meet the coordinate axes at the points A and B respectively. The rectangle OABC (O being the origin) is completedm, then

Q.Locus of point C is

A.
$$rac{b^2}{x^2} - rac{a^2}{y^2} = 1$$

B. $rac{b^2}{x^2} + rac{a^2}{y^2} = 1$
C. $rac{a^2}{x^2} - rac{b^2}{y^2} = 1$
D. $rac{a^2}{x^2} + rac{b^2}{y^2} = 1$

Answer: D



11. Let $P(\theta_1)$ and $Q(\theta_2)$ are the extremities of any focal chord of the hyperbola $rac{x^2}{a^2} - rac{y^2}{b^2} = 1$ whose eccentricity is e. Let θ be the angle between its asymptotes. Tangents are drawn to the hyperbola at some arbitrary points R. These tangent meet the coordinate axes at the points A and B respectively. The rectangle OABC (O being the origin) is completedm, then

Q. If
$$\cos^2\!\left(rac{ heta_1+ heta_2}{2}
ight)=\lambda\cos^2\!\left(rac{ heta_1- heta_2}{2}
ight)$$
, then λ

is equal to

A.
$$rac{a^2+b^2}{a^2}$$

B. $rac{a^2+b^2}{b^2}$

C.
$$rac{a^2+b^2}{ab}$$

D. $rac{a^2+b^2}{2ab}$

Answer: A

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12. If e is the eccentricity of the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ and θ is the angle between the asymptotes, then $\cos \frac{\theta}{2}$ is equal to

A.
$$\frac{1}{2e}$$

B. $\frac{1}{e}$

C.
$$\frac{1}{e^2}$$

D. $\frac{1}{2e^2}$

Answer: B



13. The vertices of $\triangle ABC$ lie on a rectangular hyperbola such that the orhtocentre of the triangle is (2, 3) and the asymptotes of the rectangular hyperbola are parallel to the coordinate axes. The two perpendicular tangents of the hyperbola intersect at the point (1, 1). Q. The equation of the

asymptotes is

A.
$$xy-1=y-x$$

$$\mathsf{B.}\, xy + 1 = x + y$$

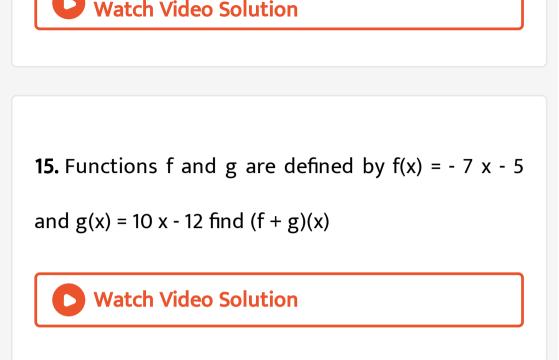
C.
$$xy - 1 = x - y$$

D.
$$xy+1=\ -x-y$$

Answer: B



14. Function f is defined by f(x) = 6 x - 3 find f(-2).



Exercise Single Integer Answer Type Questions

1. The ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ and the hyperbola $\frac{x^2}{A^2} - \frac{y^2}{B^2} = 1$ are given to be confocal and length of mirror axis of the ellipse is same as the conjugate axis of the hyperbola. If e_1 and e_2

represents the eccentricities of ellipse and hyperbola respectively, then the value of $e_1^{-2} + e_1^{-2}$ is

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2. If abscissa of orthocentre of a triangle inscribed in a rectangular hyperbola xy = 4 is $\frac{1}{2}$, then the ordinate of orthocentre of triangle is

3. Normals drawn to the hyperbola xy = 2 at the point $P(t_1)$ meets the hyperbola again at $Q(t_2)$, then minimum distance between the point P and Q

is



- **4.** The normal at P to a hyperbola of eccentricity $\frac{3}{2\sqrt{2}}$ intersects the transverse and conjugate axes
- at M and N respectively. The locus of mid-point of

MN is a hyperbola, then its eccentricity.



5. If radii of director circle of the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ and hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ are in the ratio 1:3 and $4e_1^2 - e_2^2 = \lambda$, where e_1 and e_2 are the eccetricities of ellipse and hyperbola respectively, then the value of λ is

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6. The shortest distance between the curves $rac{x^2}{a^2}-rac{y^2}{b^2}=1 ext{ and } 4x^2+4y^2=a^2(b>a)$ is

7. ABC is a triangle such that $\angle ABC = 2 \angle BAC$. If

AB is fixed and locus of C is a hyperbola, then the

eccentricity of the hyperbola is

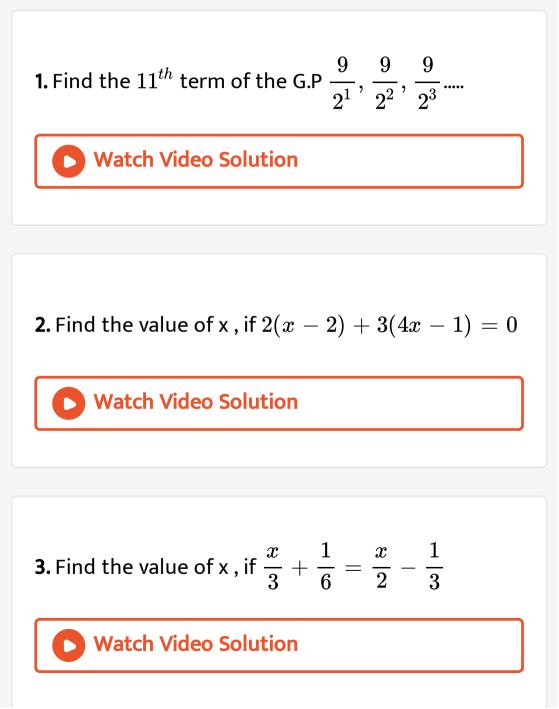
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8. Point P lie on hyperbola 2xy = 1. A triangle is contructed by P, S and S' (where S and S' are foci). The locus of ex-centre opposite S (S and P lie in first quandrant) is $(x + py)^2 = (\sqrt{2} - 1)^2(x - y)^2 + q$, then the value of p + q is

9. Chords of the circle $x^2 + y^2 = 4$, touch the hyperbola $\frac{x^2}{4} - \frac{y^2}{16} = 1$. The locus of their middle-points is the curve $(x^2 + y^2)^2 = \lambda x^2 - 16y^2$, then the value of λ is

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10. Tangents are drawn from the point (α, β) to the hyperbola $3x^2 - 2y^2 = 6$ and are inclined at angle θ and ϕ to the x-axis. If $\tan \theta \cdot \tan \phi = 2$, then the value $2\alpha^2 - \beta^2$ is _____.



1. Statement-I $\frac{5}{3}$ and $\frac{5}{4}$ are the eccentricities of two conjugate hyperbolas. Statement-II If e_1 and e_2 are the eccentricities of two conjugate hyperbolas, then $e_1e_2 > 1$.

A. Statement-I is true, Statement-II is also true,

Statement-II is the correct explanation of

Statement-I.

B. Statement-I is true, Statement-II is also true,

Statement-II is not the correct explanation of

Statement-I.

C. Statement-I is true, Statement-II is false.

D. Statement-I is false, Statement-II is true

Answer: B

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2. Statement-I A hyperbola and its conjugate hyperbola have the same asymptotes.

Statement-II The difference between the second

degree curve and pair of asymptotes is constant.

A. Statement-I is true, Statement-II is also true,

Statement-II is the correct explanation of Statement-I.

- B. Statement-I is true, Statement-II is also true, Statement-II is not the correct explanation of Statement-I.
- C. Statement-I is true, Statement-II is false.
- D. Statement-I is false, Statement-II is true

Answer: A



3. Statement-I The equation of the directrix circle to the hyperbola $5x^2 - 4y^2 = 20$ is $x^2 + y^2 = 1$. Statement-II Directrix circle is the locus of the point of intersection of perpendicular tangents.

A. Statement-I is true, Statement-II is also true,

Statement-II is the correct explanation of Statement-I.

B. Statement-I is true, Statement-II is also true,

Statement-II is not the correct explanation of

Statement-I.

C. Statement-I is true, Statement-II is false.

D. Statement-I is false, Statement-II is true

Answer: D

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4. Statement-I Two tangents are drawn from a point

on the circle $x^2 + y^2 = 9$ to the hyperbola $rac{x^2}{25} - rac{y^2}{16} = 1$, then the angle between tangnets is $rac{\pi}{2}.$

Statement-II $x^2 + y^2 = 9$ is the directrix circle of $rac{x^2}{25} - rac{y^2}{16} = 1.$

A. Statement-I is true, Statement-II is also true,

Statement-II is the correct explanation of Statement-I.

- B. Statement-I is true, Statement-II is also true, Statement-II is not the correct explanation of Statement-I.
- C. Statement-I is true, Statement-II is false.
- D. Statement-I is false, Statement-II is true

Answer: A



5. Statement-I If eccentricity of a hyperbola is 2, then eccentricity of its conjugate hyperbola is $\frac{2}{\sqrt{3}}$. Statement-II if e and e_1 are the eccentricities of two conjugate hyperbolas, then $ee_1 > 1$.

A. Statement-I is true, Statement-II is also true,

Statement-II is the correct explanation of

Statement-I.

B. Statement-I is true, Statement-II is also true,

Statement-II is not the correct explanation of

Statement-I.

C. Statement-I is true, Statement-II is false.

D. Statement-I is false, Statement-II is true

Answer: B

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6. Statement-I The line 4x - 5y = 0 will not meet the hyperbola $16x^2 - 25y^2 = 400$. Statement-II The line 4x - 5y = 0 is an asymptote ot the hyperbola.

A. Statement-I is true, Statement-II is also true,

Statement-II is the correct explanation of

Statement-I.

B. Statement-I is true, Statement-II is also true,

Statement-II is not the correct explanation of

Statement-I.

C. Statement-I is true, Statement-II is false.

D. Statement-I is false, Statement-II is true

Answer: A



7. Statement-I The point (5, -3) inside the hyperbola $3x^2-5y^2+1=0.$

Statement-II The point (x_1,y_1) inside the hyperbola $rac{x^2}{a^2}-rac{y^2}{b^2}=1$, then $rac{x_1^2}{a^2}+rac{y_1^2}{b^2}-1<0.$

A. a) Statement-I is true, Statement-II is also true, Statement-II is the correct explanation of Statement-I.

B. b) Statement-I is true, Statement-II is also

true, Statement-II is not the correct explanation of Statement-I.

C. c) Statement-I is true, Statement-II is false.

D. d) Statement-I is false, Statement-II is true

Answer: C



8. Statement-I A hyperbola whose asymptotes include $\frac{\pi}{3}$ is said to be equilateral hyperbola. Statement-II The eccentricity of an equilateral hyperbola is $\sqrt{2}$.

A. Statement-I is true, Statement-II is also true,

Statement-II is the correct explanation of

Statement-I.

B. Statement-I is true, Statement-II is also true,

Statement-II is not the correct explanation of

Statement-I.

C. Statement-I is true, Statement-II is false.

D. Statement-I is false, Statement-II is true

Answer: D



Exercise Subjective Type Questions

1. Given the base of a triangle and the ratio of the tangent of half the base angles .Show that the vertex moves on a hyperbola whose foci are the extremities of a diameter



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2. A, B, C are three points on the rectangular hyperbola $xy = c^2$, The area of the triangle formed

by the points A, B and C is

3. If a hyperbola be rectangular, and its equation be $xy=c^2,\,$ prove that the locus of the middle points of chords of constant length 2d is $\left(x^2+y^2
ight)\left(xy-c^2
ight)=d^2xy.$

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4. If four points be taken on a rectangular hyperbola such that the chord joining any two is perpendicular to the chord joining the other two,

and if $\alpha, \beta, \gamma, \delta$ be the inclinations to either asymptotes

of the straight lines joining these points to the

centre, then

 $an \alpha an \beta an \gamma an \delta$ is equal to

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5. A circle cuts two perpendicular lines so that each intercept is of given length. The locus of the centre

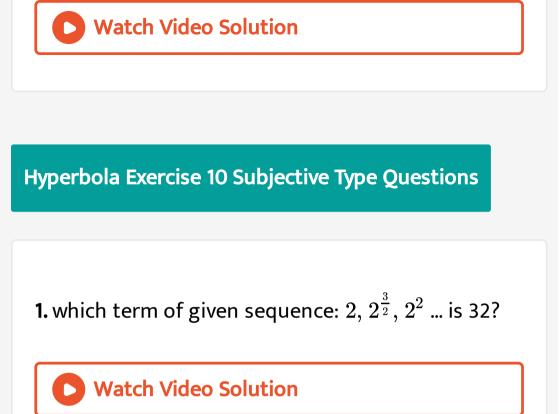
of the circle is conic whose eccentricity is



6. Let the tangent at a point P on the ellipse meet the major axis at B and the ordinate from it meet the major axis at A. If Q is a point on the AP such that AQ = AB, prove that the locus of Q is a hyperbola. Find the asymptotes of this hyperbola.

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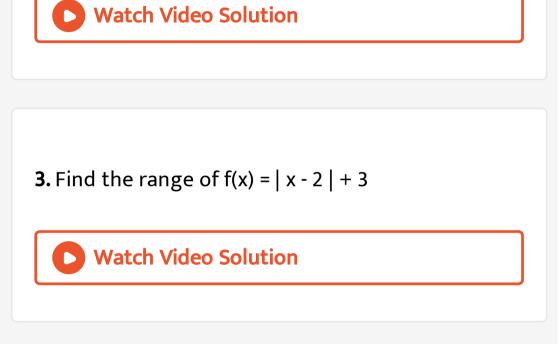
7. A series of hyperbola is drawn having a common transverse axis of length 2a. Then the locus of a point P on each hyperbola, such that its distance from the transverse axis is equal to its distance from an asymptotes, is



2. (a) Prove that any line parallel to either of the asymptotes of a hyperbola shall meet it in one point at infinity.

(b) Prove that the asymptotes of a hyperbola are

the diagonals of the rectangle formed by the lines drawn parallel to the axes at the vertices of the hyperbola [i.e., at ($\pm a, 0$) and $(0, \pm b)$].



4. A carpenter was hired to build 192 window frames. The first day he made five frames and each day, thereafter he made two more frames than he

made the day before. How many days did it take

him to finish the job?



Exercise Questions Asked In Previous 13 Years Exam

1. Find the locus of a point P(lpha, eta) moving under the condition that the line y = ax + eta is a tangent

to the hyperbola
$$rac{x^2}{a^2}-rac{y^2}{b^2}=1.$$

A. an ellipse

B. a circle

C. a parabola

D. a hyperbola

Answer: D

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2. Let a hyperbola passes through the focus of the ellipse $\frac{x^2}{25} + \frac{y^2}{16} = 1$. The transverse and conjugate axes of this hyperbola coincide with the major and minor axis of the given ellipse. Also, the product of the eccentricities of the given ellipse and hyperbola is 1. Then, A. the equation of hyperbola is $rac{x^2}{9} - rac{y^2}{16} = 1$ B. the equation of hyperbola is $rac{x^2}{9} - rac{y^2}{25} = 1$

C. focus of hyperbola is (5,0)

D. vertex of hyperbola is $\left(5\sqrt{3},0
ight)$

Answer: A::C

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3. A hyperbola having the transverse axis of length 2 sin θ is confocal with the ellipse $3x^2 + 4y^2 = 12$. Then its equation is

A.
$$x^2 \cos ec^2 heta - y^2 \sec^2 heta = 1$$

B.
$$x^2 \sec^2 \theta - y^2 \cos ec^2 \theta = 1$$

C.
$$x^2 \sin^2 heta - y^2 \cos^2 heta = 1$$

D.
$$x^2 \sin^2 heta - y^2 \cos^2 heta = 1$$

Answer: A



4. Two branches of a hyperbola

A. a) have a common tangent

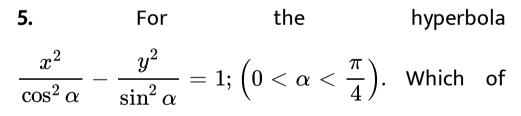
B. b) have a common normal

C. c) do not have a common tangent

D. d) do not have a common normal

Answer: B::C

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the following remains constant when alpha varies?

A. abscissae of vertices

B. abscissae of foci

C. eccentricity

D. directrix

Answer: B

6. If
$$f(x) = \prod_{n=1}^{100} (x-n)^{n(101-n)}$$
 then find
 $\frac{f(101)}{f, (101)}$
A. $1 - \sqrt{\frac{2}{3}}$
B. $\sqrt{\frac{3}{2}} - 1$
C. $1 + \sqrt{\frac{2}{3}}$

D.
$$\sqrt{rac{3}{2}}+1$$

Answer: B

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7. An ellipse intersects the hyperbola $2x^2 - 2y = 1$ orthogonally. The eccentricity of the ellipse is reciprocal to that of the hyperbola. If the axes of the ellipse are along the coordinate axes, then (a) the foci of ellipse are $(\pm 1, 0)$ (b) equation of ellipse is $x^2 + 2y^2 = 2$ (c) the foci of ellipse are (t2, 0) (d) equation of ellipse is (x^22y) A. equation of ellipse $x^2 + 2y^2 = 2$

B. the foci of the ellipse are $(~\pm~1,~0)$

C. equation of ellipse is $x^2+2y^2=4$

D. the foci of ellipse are $ig(\pm\sqrt{2},0ig)$

Answer: A::B

8. The circle
$$x^2 + y^2 - 8x = 0$$
 and hyperbola
 $\frac{x^2}{9} - \frac{y^2}{4} = 1$ intersect at points A and B.
The equation of a common tangent with positive
slope to the circle as well as to the hperbola is

A.
$$2x-\sqrt{5}y-20=0$$

$$\mathsf{B.}\,2x-\sqrt{5}y+4=0$$

C.
$$3x-4y+8=0$$

D.
$$4x - 3y + 4 = 0$$

Answer: B

9. The circle
$$x^2 + y^2 - 8x = 0$$
 and hyperbola $\frac{x^2}{9} - \frac{y^2}{4} = 1$ intersect at the points A and B. Then the equation of the circle with AB as its diameter is

A.
$$x^2 + y^2 - 12x + 24 = 0$$

B.
$$x^2 + y^2 + 12x + 24 = 0$$

C.
$$x^2 + y^2 + 24x - 12 = 0$$

D.
$$x^2 + y^2 - 24x - 12 = 0$$

Answer: A

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10. If
$$f(x) = \prod_{n=1}^{100} (x-n)^{n(101-n)}$$
 then find $\frac{f(101)}{f,(101)}$

11. Let P(6,3) be a point on the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$. If the normal at point P intersects the x-axis at (9, 0), then find the eccentricity of the hyperbola.

A.
$$\sqrt{\frac{5}{2}}$$

B. $\sqrt{\frac{3}{2}}$
C. $\sqrt{2}$
D. $\sqrt{3}$

Answer: B



12. If
$$f(x) = \prod_{n=1}^{100} (x-n)^{n(101-n)}$$
 then find $\frac{f(101)}{f,(101)}$

A. the equation of hyperbola is $\displaystyle rac{x^2}{3} - \displaystyle rac{y^2}{2} = 1$

B. a focus of the hyperbola is (2,0)

C. the eccentricity of the hyperbola is $\sqrt{rac{5}{2}}$

D. the equation of the hyperbola is

$$x^2 - 3y^2 = 3$$

Answer: B::D

13. Tangents are drawn to the hyperbola $\frac{x^2}{9} - \frac{y^2}{4} = 1$ parallet to the sraight line 2x - y = 1. The points of contact of the tangents on the hyperbola are (A) $\left(\frac{9}{2\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$ (B) $\left(-\frac{9}{2\sqrt{2}}, -\frac{1}{\sqrt{2}}\right)$ (C) $\left(3\sqrt{3}, -2\sqrt{2}\right)$ (D) $\left(-3\sqrt{3}, 2\sqrt{2}\right)$

A.
$$\left(\frac{9}{2\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$$

B. $\left(\frac{-9}{2\sqrt{2}}, \frac{-1}{\sqrt{2}}\right)$
C. $\left(3\sqrt{3}, -2\sqrt{2}\right)$
D. $\left(-3\sqrt{3}, 2\sqrt{2}\right)$

Answer: A::B



14. The eccentricity of the hyperbola whose latusrectum is 8 and conjugate axis is equal to half of the distance between the foci, is

A.
$$\frac{2}{\sqrt{3}}$$

B. $\sqrt{3}$
C. $\frac{4}{3}$
D. $\frac{4}{\sqrt{3}}$

Answer: A



15. A hyperbola passes through the point $P(\sqrt{2}, \sqrt{3})$ and has foci at $(\pm 2, 0)$. Then the tangent to this hyperbola at P also passes through the point

A.
$$(-\sqrt{2}, -\sqrt{3})$$

B. $(3\sqrt{2}, 2\sqrt{3})$
C. $(2\sqrt{2}, 3\sqrt{3})$
D. $(\sqrt{3}, \sqrt{2})$

Answer: C



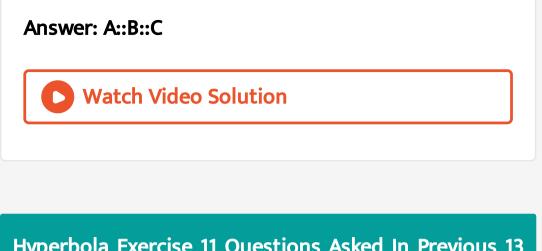
16. If 2x - y + 1 = 0 is a tangent to the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{16} = 1$ then which of the following CANNOT be sides of a right angled triangle?

A. 2a, 8, 1

B. *a*, 4, 1

C. a, 4, 2

D. 2*a*, 4, 1



Hyperbola Exercise 11 Questions Asked In Previous 13 Years Exams

1. which term of the following sequence $: 3^{\frac{1}{2}}, 3, 3^{\frac{3}{2}}$

.....is 81?

2. Find two positive numbers m and n whose AM

and GM are 34 and 16 respectively.

