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## MATHS

## BOOKS - ARIHANT MATHS

## PROPERTIES AND SOLUTION OF TRIANGLES

## Examples

1. Find the angles of the triangle whose sides are $3+\sqrt{3}, 2 \sqrt{3}$ and $\sqrt{6}$.

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2. The sides of a triangle are $8 \mathrm{~cm}, 10 \mathrm{~cm}$ and 12 cm . Prove that the greatest angle is double of the smallest angle.
3. With usual notations, if in a triangle $A B C \frac{b+c}{11}=\frac{c+a}{12}=\frac{a+b}{13}$, then prove that: $\frac{\cos A}{7}=\frac{\cos B}{19}=\frac{\cos C}{25}$

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4. The sides of a triangle are three consecutive natural numbers and its largest angle is twice the smalles one. Determine the sides of the triangle.

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5. In the triangle ABC , lines $O A, O B$ and $O C$ are drawn so that angles $O A B$, $O B C$ and OCA are each equal to $\omega$, prove that $\cot \omega=\cot A+\cot B+\cot C$

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6. Solve
$b \cos ^{2} \frac{C}{2}+c \cos ^{2} \frac{B}{2}$ in terms of k , where k is permeter of the $\triangle A B C$.

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7. In a $\triangle A B C, c \cos ^{2} \frac{A}{2}+a \cos ^{2} \frac{C}{2}=\frac{3 b}{2}$, then $a, b, c$ are in

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8. In a $\triangle A B C, a=2 b$ and $|A-B|=\frac{\pi}{3}$. Determine the $\angle C$.

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9. In a $\triangle A B C$, the tangent of half the difference of two angle is onethird the tangent of half the sum of the angle. Determine the ratio of the sides opposite to the angles.
10. If the angles of a triangle are $30^{\circ}$ and $45^{\circ}$, andFind the third angle.

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11. Consider the following statements concerning a $\triangle A B C$
(i) The sides $\mathrm{a}, \mathrm{b}, \mathrm{c}$ and area of triangle are rational.
(ii) $a, \tan \frac{B}{2}, \tan \frac{C}{2}$
(iii) $a, \sin A \sin B, \sin C$ are rational .

Prove that $(i) \Rightarrow(i i) \Rightarrow(i i i) \Rightarrow(i)$

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12. Prove that $\frac{r_{1}-r}{a}+\frac{r_{2}-r}{b}=\frac{c}{r_{3}}$

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13. If in a triangle $r_{1}=r_{2}+r_{3}+r$, prove that the triangle is right angled

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14. In any $\triangle A B C$, prove the following : $r_{1}=r \cot \left(\frac{B}{2}\right) \cot \left(\frac{C}{2}\right)$

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15. In a right angles triangle, prove that $r+2 R=s$.

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16. The exradii $r_{1}, r_{2}$ and $r_{3}$ of $\triangle A B C$ are in H.P. Show that its sides $a, b a n d c$ are in $A \dot{P}$.

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17. If $A, B, C$ are the angles of a triangle then prove that $\cos A+\cos B-\cos C=-1+4 \cos \left(\frac{A}{2}\right) \cos \left(\frac{B}{2}\right) \sin \left(\frac{C}{2}\right)$

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18. Find the ratio of the circum-radius and the inradius of $\triangle A B C$, whose sides are in the ratio $4: 5: 6$.

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19. Find the ratio of $I A: I B: I C$, where l is the incentre of $\triangle A B C$.

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20. If the sides of a triangle are in GP and its largest angle is twice tha smallset then the common ratio $r$ satisfies the inequality
21. The equation $a x^{2}+b x+c=0$, where $\mathrm{a}, \mathrm{b}, \mathrm{c}$ are the side of a $\Delta A B C$, and the equation $x^{2}+\sqrt{2} x+1=0$ have a common root. Find measure for $\angle C$.

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22. In triangle $A B C$, if $\cot A, \cot B, \cot C$ are in $A \dot{P}$; then $a^{2}, b^{2}, c^{2}$ are in $\qquad$ progression.

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23. Find the Side of pedal triangle and Circum-Radius of pedal Triangle ?

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24. Find the ratio of the circum-radius and the inradius of $\triangle A B C$, whose sides are in the ratio $4: 5: 6$.

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25. In a triangle ABC $I_{1}, I_{2}, I_{3}$ are excentre of triangle then show that $I I_{1} . I I_{2} . I I_{3}=16 R^{2} r$.

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26. Prove that the locus of a point that is equidistant from both axis is $y=x$.

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27. If $\mathrm{g}, \mathrm{h}, \mathrm{k}$ denotes the side of a pedal triangle, then prove that $\frac{g}{a^{2}}+\frac{h}{b^{2}}+\frac{k}{c^{2}}=\frac{a^{2}+b^{2}+c^{2}}{2 a b c}$
28. If $x, y, z$ are respectively perpendiculars from the circumcentre on the sides of the $\triangle A B C$, the value of $\frac{a}{x}+\frac{b}{y}+\frac{c}{z}-\frac{a b c}{4 x y z}=$

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29. If $\mathrm{O}, \mathrm{H}$ and G represents circum centre, orthocentre and centroid respectively, then show 'HG:GO=

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30. In $\triangle A B C$ it is given distance between the circumcentre ( O ) and orthocentre (H) is $R \sqrt{1-8 \cos A \cos B \cos C}$. If Q is the midopoint of $O H$, then $A Q$ is
31. Find the distance between the circumcentre and the incentre of the $\triangle A B C$.

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32. Differentiate the following w.r.t x
$2^{\sin x}$

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33. If the area of circle is $A_{1}$ and area of regular pentagon inscibed in the circle is $A_{2}$, then find the ratio of area of two.

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34. The area of a cyclic quadrilateral $A B C D$ is $\frac{(3 \sqrt{3})}{4}$. The radius of the circle circumscribing cyclic quadrilateral is 1.If $A B=1, B D=\sqrt{3}$, then
find BC. CD.

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35. A regular pentagon and a regular decagon have the same perimeter, prove that their areas are as $2: \sqrt{5}$.

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36. If the sides of a cyclic quadrilateral are $3,3,4,4$, show that a circle be inscribed in it.

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37. The two adjacent sides of a cyclic quadrilateral are $2 a n d 5$ and the angle between them is $60^{\circ}$. If the area of the quadrilateral is $4 \sqrt{3}$, find the remaining two sides.
38. If $a, b, c, d$ are the side of a quadrilateral, then find the the minimum value of $\frac{a^{2}+b^{2}+c^{2}}{d^{2}}$

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39. In any triangle $A B C$, the sides are $6 \mathrm{~cm}, 10 \mathrm{~cm}$ and 14 cm . Then the triangle is obtuse angled with the obtuse angle equal to

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40. If $\mathrm{a}, \mathrm{b}$ and A are given in a triangle and $c_{1}, c_{2}$ are possible values of the third side, then prove that $c_{1}^{2}+c_{2}^{2}-2 c_{1} c_{2} \cos 2 A=4 a^{2} \cos ^{2} A$

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41. Differentiate the following w.r.t x $x^{\log x}$

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42. Two hagstaffs stand on a horizontal plane. $A$ and $B$ are two points on the line joining their feet and between them. The angles of elevation of the tops of the flagstaffs as seen from $A$ are $30^{\circ}$ and $60^{\circ}$ and as seen from $B$ are $60^{\circ}$ and $45^{\circ}$. If $A B$ is 30 m , then the distance between the flagstaffs is
A. $30+15 \sqrt{3}$
B. $45+15 \sqrt{3}$
C. $60-15 \sqrt{3}$
D. $60+15 \sqrt{3}$

## Answer: A:C

43. In a cubicul hall $A B C D P Q R S$ with each side $10 m, G$ is the centre of the walls $B C R Q$ and $T$ is the midpoint of the side $A B$, the angle of elevation of $G$ at the Point $T$ is
A. $\sin ^{-1}\left(\frac{1}{\sqrt{3}}\right)$
B. $\cos ^{-1}\left(\frac{1}{\sqrt{3}}\right)$
C. $\tan ^{-1}\left(\frac{1}{\sqrt{3}}\right)$
D. $\cot ^{-1}\left(\frac{1}{\sqrt{3}}\right)$

## Answer: A: C

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44. Each side of an equilateral triangle subtends an angle of $60^{\circ}$ at the top of $a$ tower $h \mathrm{~m}$ high located at the centre of the triangle. If a is the length of each side of the triangle, then
A. $3 a^{2}=2 h^{2}$
B. $2 a^{2}=2 h^{2}$
C. $a^{2}=3 h^{2}$
D. $3 a^{2}=h^{2}$

## Answer: A::B::C

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45. A vertical tower $P Q$ subtends th same angle $30^{\circ}$ at each of two place
$A$ and $B, 60 \mathrm{~m}$ apart on the ground, $A B$ subtends an angle $120^{\circ}$ at the foot of the tower. If h is the height of the tower, then $9 h^{2}+h+1$ is equal to
A. 3121
B. 2136
C. 3600
D. None of these

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46. If $\frac{\tan ^{2}(\pi-A)}{4}+\frac{\tan ^{2}(\pi-B)}{4}+\frac{\tan ^{2}(\pi-C)}{4}=1$, then $A B C$ is equilateral (b) isosceles (c) scalene (d) none of these
A. equilateral
B. isosceles
C. scalene
D. None of these

## Answer: A::B::C

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47. In $\triangle A B C, a^{2}+c^{2}=2002 b^{2}$ then $\frac{\cot A+\cot C}{\cot B}$ is equal to
A. $\frac{1}{2001}$
B. $\frac{2}{2001}$
C. $\frac{3}{2001}$
D. $\frac{4}{2001}$

## Answer: B

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48. A triangle has vertices $A, B$ and $C$, and the respective opposite sides have lengths $a, b$ and $c$. This triangle is inscribed in a circle of radius R. If $b=c=1$ and the altitude from A to side BC has length $\sqrt{\frac{2}{3}}$, then R equals:
A. $\frac{1}{\sqrt{3}}$
B. $\frac{2}{\sqrt{3}}$
C. $\frac{\sqrt{3}}{2}$
D. $\frac{\sqrt{3}}{2 \sqrt{2}}$

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49. In $\triangle A B C$, if $A C=8, B C=7$ and D lies between A and B such that $A D=2, B D=4$, then the length $C D$ equals
A. $\sqrt{46}$
B. $\sqrt{48}$
C. $\sqrt{51}$
D. $\sqrt{75}$

## Answer: A

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50. 

In
a
triangle
ABC,
if
$(a+b+c)(a+b-c)(b+c-a)(c+a-b)=\frac{8 a^{2} b^{2} c^{2}}{a^{2}+b^{2}+c^{2}}$ then the
triangle is
(a)isosceles
(b)right angled
(c)equilateral
(d)obtuse angled
A. isosceles
B. right angled
C. equilateral
D. obtuse angled

## Answer: A::B::C::D

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51. Consider a $\triangle A B C$ and let $\mathrm{a}, \mathrm{b}$ and c denote the lengths of the sides opposite to vertices A, B and C, repectively. if $a=1, b=3$ and $C=60^{\circ}$, then $\sin ^{2} \mathrm{~B}$ is equal to
A. $\frac{27}{28}$
B. $\frac{3}{28}$
C. $\frac{81}{28}$
D. $\frac{1}{3}$

## Answer: B

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52. In $\triangle A B C$, if $\cos A+\sin A-\frac{2}{\cos B+\sin B}=0$, then $\frac{a+b}{c}$ is equal to
A. $\sqrt{2}$
B. 1
C. $\frac{1}{\sqrt{2}}$
D. $2 \sqrt{2}$

## Answer: A

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53. In a triangle $A B C$, if $\angle A=30^{\circ}, b=10$ and $a=x$, then the values of $x$ for which there are 2 possible triangles is given by(All symbols used have usual meaning in a triangle.)
(a) $5<x<10$
(b) $x<\frac{5}{2}$
(c) $\frac{5}{3}<x<10$
(d) $\frac{5}{2}<x<10$
A. (a) $5<x<10$
B. (b) $x<\frac{5}{2}$
C. (c) $\frac{5}{3}<x<10$
D. (d) $\frac{5}{2}<x<10$

## Answer: A:B

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54. In a $\triangle A B C, A B=A C, P$ and $Q$ are points on AC and AB respectively such that $C B=B P=P Q=Q A$. if $\angle A Q P=\theta$, then $\tan ^{2} \theta$ is a root of the equation
A. $y^{3}+21 y^{2}-35 y-12=0$
B. $y^{3}-21 y^{2}+35 y-12=0$
C. $y^{3}-21 y^{2}+35 y-7=0$
D. $12 y^{3}-35 y^{2}+35 y-12=0$

## Answer: A::B::C

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55. The angle of elevation of the top of a tower a point $A$ due south of it is $30^{\circ}$ and from a point B due west of it is $45^{\circ}$.If the height of the tower is 100 meters ,then find the distance $A B$.
(a) 150 m
(b) 200 m
(c) 173.2 m
(d) 141.4 m
A. 150 m
B. 200 m
C. 173.2 m
D. 141.4 m

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56. An aeroplane flying horizontally 1 km above the ground is observed at an elevation of 60 o . After 10 seconds, its elevation is observed to be 30 o .

Find the speed of the aeroplane in $\mathrm{km} / \mathrm{hr}$.
A. 240
B. $240 \sqrt{3}$
C. $60 \sqrt{3}$
D. None of these

## Answer: A::B::C::D

57. In $\triangle A B C$, the ratio $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$ is not always equal to
(All symbols used have usual meaning in a triangle.)
a. $2 R$, where $R$ is the circumradius
b. $\frac{a b c}{2 \Delta}$, where $\Delta$ is the area of the triangle
c. $\frac{2}{3}\left(a^{2}+b^{2}+c^{2}\right)^{\frac{1}{2}}$
d. $\frac{(a b c)^{\frac{2}{3}}}{\left(h_{1} h_{2} h_{3}\right)^{\frac{1}{3}}}$
A. $2 R$, where $R$ is the circumradius
B. $\frac{a b c}{2 \Delta}$, where $\Delta$ is the area of the triangle
C. $\frac{2}{3}\left(a^{2}+b^{2}+c^{2}\right)^{\frac{1}{2}}$
D. $\frac{(a b c)^{\frac{2}{3}}}{\left(h_{1} h_{2} h_{3}\right)^{\frac{1}{3}}}$

## Answer: A::B::C::D

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58. Let $A B C D$ be a cyclic quadrilateral such that $A B=2, B C=3, \angle B=120^{\circ}$ and area of quadrilateral $=4 \sqrt{3}$. Which of the following is/are correct ?
A. The value of $(A C)^{2}$ is equal to 19
B. The sum of all positive value of product AC. BD I is equal to 35
C. The sum of all posible value of $(A D)^{2}$ is equal to 29
D. The value of $(C D)^{2}$ can be 4

## Answer: B

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59. In a triangle $A B C$, which of the following quantities denote the area of the triangles $\frac{a^{2}-b^{2}}{2} \frac{\sin A \sin B}{\sin (A-B)}$

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60. Consider the system of equations
$\sin x \cos 2 y=\left(a^{2}-1\right)^{2}+1, \cos x \sin 2 y=a+1$
The number of values of $x \in[0,2 \pi]$, when the system has solution for permissible values of $a$, is/are

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61. In a triangle ABC , let $2 a^{2}+4 b^{2}+c^{2}=2 a(2 b+c)$, then which of the following holds good?
A. $\cos B=\frac{-7}{8}$
B. $\sin (A-C)=0$
C. $\frac{r}{r_{1}}=\frac{1}{5}$
D. $\sin A: \sin B: \sin C=1: 2: 1$

## Answer: A::B::C

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62. In $A A B C$, angle $A, B$ and $C$ are in the ratio $1: 2: 3$, then which of the following is (are) correct? (All symbol used have usual meaning in a triangle.)
A. Circum-radius of $\triangle A B C=c$
B. $a: b: c=1: \sqrt{3}: 2$
C. Permimeter of $\triangle A B C=3+\sqrt{3}$
D. Area of $\triangle A B C=\frac{\sqrt{3}}{8} c^{2}$

## Answer: A::B::C

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63. If the length of tangents from $A, B, C$ to the incircle of $\triangle A B C$ are $4,6,8$ then which of the following is(are) correct? (All symbols used have usual meaning in a triangle.
A. Area of $\triangle A B C i s 12 \sqrt{6}$
B. $r_{1}, r_{2}, r_{3}$ are in HP
C. a,b,c are in AP
D. $r=\frac{4 \sqrt{6}}{3}$

## Answer: B

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64. In a right angle triangle $A B C$, let $b=10, c=10 \sqrt{2}$ find $a$.
A. Area of triangle $A B C$ is 50 .
B. Distance between orthocentre and circumcetre iss $5 \sqrt{2}$.
C. Sum of circum-radius and in-radius of $\triangle A B C$ is equal to 10 .
D. Length of internal angle bisector of $\angle A B C$ of $\triangle A B C$ is $\frac{5}{2 \sqrt{2}}$.

## Answer: A::B::C

65. Let ' $I$ ' is the length of median from the vertex $A$ to the side $B C$ of a $\triangle A B C$. Then
A. $4 l^{2}=2 b^{2}+2 c^{2}-a^{2}$
B. $4 l^{2}=b^{2}+x^{2}+2 b c \cos A$
C. $4 l^{2}=a^{2}+4 b \mathrm{o} s A$
D. $4 l^{2}=(2 s-a)^{2}-4 b c \sin ^{2} \frac{A}{2}$

## Answer: A::B::C::D

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66. If a right angled $\triangle A B C$ of maximum area is inscribled within a circle of radius R , then $\left(\delta\right.$ representes area of $\triangle A B C$ and $r, r_{1}, r_{2}, r_{3}$ represent in-radius and ex-radii, and s is the semi-perimeter of $\triangle A B C$, then
A. $\Delta=R^{2}$
B. $\frac{1}{r_{1}}+\frac{1}{r_{2}}+\frac{1}{r_{3}}=\frac{\sqrt{2}+1}{R}$
C. $r=(\sqrt{2}-1) R$
D. $s=(1+\sqrt{2}) R$

## Answer: A,B,C,D

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67. Statement I In a $\triangle A B C$, if $a<b<c$ and r is inradius and $r_{1}, r_{2}, r_{3}$ are the exradii opposite to angle A,B,C respectively, then $r<r_{1}<r_{2}<r_{3}$.

Statement II For, $\Delta A B C r_{1} r_{2}+r_{2} r_{3}+r_{3} r_{1}=\frac{r_{1} r_{2} r_{3}}{r}$
A. Statement I is True, Statement II is True, Statement II is a correct explanation for Statement I.
B. Statement I is True, Statement II is True, Statement II is NOT a correct explanation for Statement I.
C. Statement I is True, Statement II is False.
D. Statement I is False, Statement II is True.

## Answer: A::B::C::D

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68. Solve the given quadratic equation
$-2 x^{2}+4 x+1=0$

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69. Statement I In $a \Delta A B C, \sum \frac{\cos ^{2} \frac{A}{2}}{a}$ has the value equal to $\frac{s^{2}}{a b c}$.

Statement II in $a \Delta A B C, \cos \frac{A}{2}=\sqrt{\frac{(s-b)(s-c)}{b c}}$
$\cos \frac{\beta}{2}=\sqrt{\frac{(s-a)(s-c)}{a c}}, \cos \frac{c}{2}=\sqrt{\frac{(s-a)(s-b)}{a b}}$
A. Statement I is True, Statement II is True, Statement II is a correct explanation for Statement I.
B. Statement I is True, Statement II is True, Statement II is NOT a correct explanation for Statement I.
C. Statement I is True, Statement II is False.
D. Statement I is False, Statement II is True.

## Answer: C

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70. If $\operatorname{side}(a)=4$ then area of the equilateral triangle $\triangle A B C$ is equal to
A. а) $\frac{3 \sqrt{2}}{2}$
B. b) 3
C. c) $4 \sqrt{3}$
D. d) $3 \sqrt{2}$

## Answer: A::B::C::D

71. In triangle $A B C$ let $\tan A=1, \tan B=2, \tan C=3$ and $c=3$, The radius of the circle circumscribing the triangle $A B C$, is equal to
A. $\frac{\sqrt{10}}{2}$
B. $\sqrt{5}$
C. $\sqrt{10}$
D. $\frac{\sqrt{5}}{2}$
A. $\frac{\sqrt{10}}{2}$
B. $\sqrt{5}$
C. $\sqrt{10}$
D. $\frac{\sqrt{5}}{2}$

## Answer: A::B::C::D

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72. Let $\Delta$ denote the area of the $\Delta A B C$ and $\Delta p$ be the area of its pedal triangle. If $\Delta=k \Delta p$, then k is equal to

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73. If $\sin x=1$, then $x$ is equal to
A. $\frac{\pi}{9}$
B. $\frac{2 \pi}{9}$
C. $\frac{\pi}{3}$
D. None of these

## Answer: B

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74. If the sum of squares of two sides is equal to square of third side then
A. Equilateral
B. Isosceless
C. Scalene
D. Right angled

## Answer: D

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75. Consider the differential equation $y^{2} d x+\left(x-\frac{1}{y}\right) d y=0$. If $\mathrm{y}(1)=1$, then x is given by:

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76. If $\mathrm{I}, \mathrm{m}, \mathrm{n}$ denote the side of a pedal triangle, then $\frac{l}{a^{2}}+\frac{m}{b^{2}}+\frac{n}{c^{2}}$ is equal to

$$
\text { A. (a) } \frac{a^{2}+b^{2}+c^{2}}{a^{3}+b^{3}+c^{2}}
$$

B. (b) $\frac{a^{2}+b^{2}+c^{2}}{2 a b c}$
C. (c) $\frac{a^{3}+b^{3}+c^{3}}{a b c(a+b+c)}$
D. (d) $\frac{1}{a}+\frac{1}{b}+\frac{1}{c}$

## Answer: B

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77. If R be circum-radius of $\triangle A B C$, then circum-radius of a pedal $\Delta$ is
A. R
B. $\frac{2 R}{3}$
C. $\frac{R}{3}$
D. $\frac{R}{2}$

## Answer: D

78. The in-radius of pedal $\Delta$ of a $\Delta A B C$ is
A. $\frac{R}{2}$
B. $R \sin A \sin B \sin C$
C. $2 R \cos A \cos B \cos C$
D. $4 R \sin \frac{A}{2} \sin \frac{b}{2} \sin \frac{C}{2}$

## Answer: A::B::C::D

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79. In a triangle ABC, if $r_{1}+r_{3}+r=r_{2}$, then find the value of $\left(\sec ^{2} A+\cos ^{2} B-\cot ^{2} C\right)$,

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80. In $\triangle A B C$, let $b=6, c=10$ and $r_{1}=r_{2}+r_{3}+r$ then find area of $\triangle A B C$.

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81. Consider on obtuse angle triangles with side $8 \mathrm{~cm}, 15 \mathrm{~cm}$ and $\times \mathrm{cm}$ (largest side being 15 cm ). If $\times$ is an integer, then find the number of possible triangels.

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82. let $A B C$ be a right angled triangle at $C$. If the inscribed circle touches the side $A B$ at $D$ and $(A D)(B D)=11$, then find the area of triangle $A B C$.

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83. Consider a $\triangle A B C$ and let $\mathrm{a}, \mathrm{b}$, and c denote the leghts of the sides opposite to vertices $\mathrm{A}, \mathrm{B}$ and C , respectively. Suppose $a=2, b=3, c=4$ and H be the orthocentre. Find $15(H A)^{2}$.
84. In a triangle $A B C$, the internal angle bisector of $\angle A B C$ meets $A C$ at $K$. If $B C=2, C K=1$ and $B K=\frac{3 \sqrt{2}}{2}$, then find the length of side AB.

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85. Triangle $A B C$ has $A C=13, A B=15$ and $B C=14$. Let ' $O$ ' be the circumcentre of the $\triangle A B C$. If the length of perpendicular from the point ' $O$ ' on $B C$ can be expressed as a rational $\frac{m}{n}$ in the lowest form then find $(m+n)$.

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86. Two sides of a triangle are given by the roots of the equation $x^{2}-2 \sqrt{3} x+2=0$. The angle between the sides is $\frac{\pi}{3}$. Find the perimeter of $\Delta$.
87. If in $\triangle A B C, \angle A=90^{\circ}$ and $\mathrm{c}, \sin \mathrm{B} \cos \mathrm{B}$ are rational numbers, then show a and b are rational .

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88. If the sides of a $\triangle A B C$ are in AP and a is the smallest side, then $\cos \mathrm{A}$ equals

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89. If $\mathrm{A}, \mathrm{B}$ and C are angles of a triangle such that $\angle A$ is obtuse, then show $\tan \mathrm{B} \tan C<1$.

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90. If $A$ is the area and $2 s$ is the sum of the sides of a triangle, then (a) $A \leq \frac{s^{2}}{4}$ (b) $A \leq \frac{s^{2}}{3 \sqrt{3}}$ (c) $2 R \sin A \sin B \sin C$ (d) none of these

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91. In a triangle, if $r_{1}>r_{2}>r_{3}$, then show $a>b>c$.

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92. D is midpoint of BC in $\triangle A B C$ such that AD and AC are perpendicular, Show that $\cos A \cos C=\frac{2\left(c^{2}-a^{2}\right)}{3 a c}$

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93. In any $\triangle A B C$, prove that
$a^{3} \cos (B-C)+b^{3} \cos (C-A)+c^{3} \cos (A-B)=3 a b c$
94. If in a triangle of base ' $a$ ', the ratio of the other two sides is $r$ ( $<1)$.Show that the altitude of the triangle is less than or equal to $\frac{a r}{1-r^{2}}$

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95. $\left(x^{2}+y^{2}\right) d y=x y d x$. If $y\left(x_{0}\right)=e, \mathrm{y}(1)=1$, then the value of $x_{0}=$
$\qquad$

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96. The internal bisectors of the angles of a $\triangle A B C$ meet the sides BC ,
$\mathrm{CA}, \mathrm{AB}$ in $\mathrm{D}, \mathrm{E}$ and F , respectively. Show that the area of the $\triangle D E F$ is equal to,

$$
\frac{2 \Delta a b c}{(b+c)(c+a)(a+b)}
$$

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97. Prove m:n theorem in a $\triangle A B C$, a point D is taken on side BC such that $\mathrm{BD}: \mathrm{DC}$ is $\mathrm{m}: \mathrm{n}$. Then prove that $(1)(m+n) \cot \theta=m \cot \alpha-n \cot \beta$
(2) $(m+n) \cot \theta=n \cot B-m \cot C$

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98. The base of a triangle is divided into three equal parts. If $t_{1}, t_{2}, t_{3}$ are the tangents of the angles subtended by these parts at the opposite vertex, prove that $\left.\left(\frac{1}{t_{1}}+\frac{1}{t_{2}}\right)\left(\frac{1}{t_{2}}+\frac{1}{t_{3}}\right)=4\left(1+\frac{1}{\left(t_{2}\right)^{2}}\right)\right)$.

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99. Prove that the triangle $A B C$ is equilateral if $\cot A+\cot B+\cot C=\sqrt{3}$

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100. In any triangle. if $\frac{a^{2}-b^{2}}{a^{2}+b^{2}}=\frac{\sin (A-B)}{\sin (A+B)}$, then prove that the triangle is either right angled or isosceles.

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101. The sides of a triangle are in AP. If the angles $A$ and $C$ are the greatest and smallest angle respectively, then $4(1-\cos A)(1-\cos C)$ is equal to

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102. perpendiculars are drawn from the angles $A, B a n d C$ of an acuteangled triangle on the opposite sides, and produced to meet the circumscribing circle. If these produced parts are $\alpha, \beta, \gamma$, respectively, then show that $\frac{a}{\alpha}+\frac{b}{\beta}+\frac{c}{\gamma}=2(\tan A+\tan B+\tan C)$.

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103. If $a=\cos \theta+i \sin \theta, b=\cos \phi+i \sin \phi, c=\cos \psi+i \sin \psi$ and $\frac{a}{b}+\frac{b}{c}+\frac{c}{a}=2$ then $\sin (\theta-\phi)+\sin (\phi-\psi)+\sin (\psi-\theta)$ equals

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104. If $p$ is the produce of the since of angles of a triange, and $q$ the product of their consines then tangents of the angles are roots of the equation

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105. Given the base of a triangle, the opposite angle A , and the product $k^{2}$ of the other two sides, show that it is not possible for $a$ to be less than $2 k \frac{\sin A}{2}$

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106. If in a triangle $A B C, \angle C=60^{\circ}$, then prove that $\frac{1}{a+c}+\frac{1}{b+c}=\frac{3}{a+b+c}$.

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107. Let $1<m<3$. In a triangle $A B C$, if $2 b=(m+1)$ a \& $\cos A=\frac{1}{2} \sqrt{\frac{(m-1)(m+3)}{m}}$ prove that the are two values to the third side, one of which is $m$ times the other.

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108. In any $\triangle A B C$, if D be any points of the base BC such that $\frac{B D}{D C}=\frac{m}{n}$ and $\angle A B D=\alpha, \angle D A C=\beta, \angle C D A=\theta$ and $A D=x$ then prove that
$(m+n)^{2} \cdot x=(m+n)\left(m b^{2}+n c^{2}\right)-m n a^{2}$
109. ABCD is a trapezium such that $A B|\mid C D a n d C B$ is perpendicular to them. If $\angle A D B=\theta, B C=p, \operatorname{andCD}=q \quad$, show that $A B=\frac{\left(p^{2}+q^{2}\right) \sin \theta}{p \cos \theta+q \sin \theta}$

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110. 

In a triangle
ABC,
prove
that $\frac{\cot \left(\frac{A}{2}\right)+\cot \left(\frac{B}{2}\right)+\cot \left(\frac{C}{2}\right)}{\cot A+\cot B+\cot (C)}=\frac{(a+b+c)^{2}}{a^{2}+b^{2}+c^{2}}$

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111. If the sides of a triangle are in A.P., and its greatest angle exceeds the least angle by $\alpha$, show that the sides are in the ratio $1+x: 1: 1-x$, , where $x=\sqrt{\frac{1-\cos \alpha}{7-\cos \alpha}}$

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112. In a $A B C$, if $\frac{\tan A}{2}, \frac{\tan B}{2}, \frac{\tan C}{2}$ are $\in A \dot{P}$; then show that $\cos A, \cos B, \cos C$ are in $A P$.

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113. If a,b,c are in HP, then prove that $\sin ^{2} \frac{A}{2}, \sin ^{2} \frac{B}{2}, \sin ^{2} \frac{C}{2}$ are also in HP.

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114. If $r_{1}, r_{2}, r_{3}$ are the ex-radii of $\triangle A B C$, then prove that
$\frac{b c}{r_{1}}+\frac{c a}{r_{2}}+\frac{a b}{r_{3}}=2 R\left[\left(\frac{a}{b}+\frac{b}{a}\right)+\left(\frac{b}{c}+\frac{c}{b}\right)+\left(\frac{c}{a}+\frac{a}{c}\right)-3\right]$

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115. If r and R are radii of the incircle and circum-circle of $\triangle A B C$, then prove that :

## $8 r R\left\{\cos ^{2} A / 2+\cos ^{2} B / 2+\cos ^{2} C / 2\right\}$

$=2 b c+2 c a+2 a b-a^{2}-b^{2}-c^{2}$.

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116. Prove that
$r_{1}^{2}+r_{2}^{2}+r_{3}^{3}+r^{2}=16 R^{2}-a^{2}-b^{2}-c^{2}$.
where $\mathrm{r}=$ in radius, $\mathrm{R}=$ circumradius,, $r_{1}, r_{2}, r_{3}$ are ex-radii.

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117. Tangent are parallel to the three sides are drawn to the in-circle. If $x, y, z$ are the lengths of parts of the tangents with in triangle, then prove that $\frac{x}{a}+\frac{y}{b}+\frac{z}{c}=1$.

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118. If in a triangle $A B C, \cos A+2 \cos B+\cos C=2$ prove that the sides of the triangle are in $A P$

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119. In a cyclic quadrilateral $A B C D$, prove that $\tan ^{2} \frac{B}{2}=\frac{(s-a)(s-b)}{(s-c)(s-d)}, a, b, c$, and $d$ being the lengths of sides $A B C, C D$ and DA respectively and $s$ is semi-perimeter of quadrilateral.

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120. If $x, y, z$ are perpendicular from circum centre of the sides of the $\triangle A B C$ respectively. Prove that $\frac{a}{z}+\frac{b}{y}+\frac{c}{z}=\frac{a b c}{4 x y z}$

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121. If $\mathrm{x}=\mathrm{a} \cos \theta+\mathrm{b} \sin \theta$ and $\mathrm{y}=\mathrm{a} \sin \theta-\mathrm{b} \cos \theta$, then prove that $y^{2} \frac{d^{2} y}{d x^{2}}-x \frac{d y}{d x}+y=0$

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122. The circle inscribed in the triangle $A B C$ touches the side $B C, C A$ and AB in the point $A_{1} B_{1}$ and $C_{1}$ respectively. Similarly the circle inscribed in the $\Delta A_{1} B_{1} C_{1}$ touches the sieds in $A_{2}, B_{2}, C_{2}$ respectively and so on. If $A_{n} B_{n} C_{n}$ be the nth $\Delta$ so formed, prove that its angle are $\frac{\pi}{3}-(2)^{-n}\left(A-\frac{\pi}{3}\right), \frac{\pi}{3}-(2)^{-n}\left(B-\frac{\pi}{3}\right), \frac{\pi}{3}-(2)^{-n}\left(C-\frac{\pi}{3}\right)$.

Hence prove that the triangle so formed is ultimately equilateral.

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123. In a $\triangle A B C$, prove that:
$2 r \leq \frac{a \cot A+b \cot B+c \cot C}{3} \leq R$
124. If $\Delta$ is the area of a triangle with side lengths $a, b$, and $c$, then show that $\Delta \leq \frac{1}{4} \sqrt{(a+b+c) a b c}$. Also show that equality occurs in the above inequality if and only if $a=b=c$

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## SOLVED EXAMPLES

1. Match the statements of Column I with values of Column II.

## Column I

## Column II

(A) $\lim _{x \rightarrow \frac{\pi^{+}}{2}} \tan ^{-1}(\tan x)$
(p) 0
(B) $\lim _{n \rightarrow \infty}\left[\sum_{r=1}^{n} \frac{1}{2^{r}}\right]([\cdot]$ denotes the
(q) Doesn't exist greatest integer function)
(C) $\lim _{x \rightarrow \infty} \sec ^{-1}\left(\frac{x}{x+1}\right)$
(r) $-\frac{\pi}{2}$
(D) $\lim _{x \rightarrow \frac{\pi}{2}} \frac{\cos x}{(1-\sin x)^{2 / 3}}$
(s)
$\frac{\pi}{2}$

1. In the given figure,if $A B=A C, \angle B A D=30^{\circ}$ and $A E=A D$, then $x$ is equal to

A. $15^{\circ}$
B. $10^{\circ}$
C. $12 \frac{1}{2}$
D. $7 \frac{1}{2}$
2. In $\triangle A B C, a=4, b=12$ and $B=60^{\circ}$, thn the vlaue of $\sin \mathrm{A}$ is
A. $\frac{1}{2 \sqrt{3}}$
B. $\frac{1}{3 \sqrt{2}}$
C. $\frac{2}{\sqrt{3}}$
D. $\frac{\sqrt{3}}{2}$

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3. Let ABC be a triangle such that $\angle A=45^{\circ}, \angle B=75^{\circ}$, then $a+c \sqrt{2}$ is equal to
A. (a) 0
B. (b) $b$
C. (c) $2 b$
D. (d) $-b$

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4. If the angles $\mathrm{A}, \mathrm{B}, \mathrm{C}$ of $\triangle A B C$ are in A.P. and $b: c=\sqrt{3}: \sqrt{2}$, show that $A=75^{\circ}$.
A. $\frac{\pi}{6}$
B. $\frac{\pi}{4}$
C. $\frac{5 \pi}{12}$
D. $\frac{\pi}{2}$

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5. If $\cot \frac{A}{2}=\frac{b+c}{a}$, then $\triangle A B C$ is
A. (a) Isosceles
B. (b) Equilateral
C. (c) Right angled
D. (d) None of these

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6. In any triangle. if $\frac{a^{2}-b^{2}}{a^{2}+b^{2}}=\frac{\sin (A-B)}{\sin (A+B)}$, then prove that the triangle is either right angled or isosceles.
A. Right angled or isosceles
B. Right angled and isosceles
C. Equiliateral
D. None of these

$$
\frac{a^{2} \sin (B-C)}{\sin B+\sin C}+\frac{b^{2} \sin (C-A)}{\sin C+\sin A}+\frac{c^{2} \sin (A-B)}{\sin A+\sin B}=0
$$

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8. In any $\Delta A B C$, is $2 \cos B=\frac{a}{c}$, then the triangle is
A. right angled
B. equilateral
C. isosceles
D. None of these

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9. Prove that
$\sin ^{2}\left(\frac{\pi}{4}\right)+\cos ^{2}\left(\frac{\pi}{6}\right)-\tan ^{2}\left(\frac{\pi}{4}\right)=\frac{1}{4}$
10. If a $\cos A=b \cos B$, then the triange is
A. Isosceles
B. Right angled
C. Isosceles or right angled
D. Right angled isosceles

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11. In $\triangle A B C,(a+b+c)(b+c-a)=k b c$ if
A. $\lambda<0$
B. $\lambda>0$
C. $0<\lambda<4$
D. $\lambda<4$

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12. If : $a=9, b=8$ and $c=x$ satisfies $3 \cos \mathrm{C}=2$, then $: \mathrm{x}=$
A. $x=5$
B. $x=6$
C. $x=4$
D. $x=7$

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13. In $\triangle A B C, \quad$ if $\sin ^{2} A+\sin ^{2} B=\sin ^{2} C$, then the triangle is
A. equilateral
B. isosceles
C. right angled
D. None of these

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14. The lengths of the sides of a triangle are $\alpha-\beta, \alpha+\beta$ and
$\sqrt{3 \alpha^{2}+\beta^{2}},(\alpha>\beta>0)$. Its largest angle is
A. (a) $\frac{2 \pi}{3}$
B. (b) $\frac{\pi}{2}$
C. (c) $\frac{3 \pi}{4}$
D. (d) $\frac{5 \pi}{6}$
15. In any triangle $A B C$, prove that: $\frac{1+\cos (A-B) \cos C}{1+\cos (A-C) \cos B}=\frac{a^{2}+b^{2}}{a^{2}+c^{2}}$
A. $\frac{a^{2}+b^{2}}{a^{2}+c^{2}}$
B. $\frac{b^{2}+c^{2}}{b^{2}-c^{2}}$
C. $\frac{c^{2}-a^{2}}{a^{2}+b^{2}}$
D. None of these

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16. If the sides of a triangle $A B C$ are in $A P$ and ' $a$ ' is the smallest side, then express $\cos A$ in term of $b$ and $c$.
A. $\frac{3 c-4 b}{2 c}$
B. $\frac{3 c-4 b}{2 b}$
C. $\frac{4 c-3 b}{2 c}$
D. None of these

## D Watch Video Solution

17. In a $\triangle A B C, a^{2} \cos 2 B+b^{2} \cos 2 \mathrm{~A}+2 \mathrm{ab} \cos (\mathrm{A}-\mathrm{B})$ is equal to?

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18. In any $\Delta A B C, 2[b c \cos A+c a \cos B+a b \cos C]=$
A. $a^{2}+b^{2}+c^{2}$
B. $a^{2}+b^{2}-c^{2}$
C. $a^{2}-b^{2}+c^{2}$
D. $a^{2}-b^{2}+c^{2}$
19. In a $\triangle A B C, \tan \frac{1}{2}(A+B) \cdot \cot \frac{1}{2}(A-B)$ is equal to ?

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20. If in a $\triangle A B C, b=\sqrt{3}, c=1$ and $B-C=90^{\circ}$, then $\angle A$ is
A. $30^{\circ}$
B. $45^{\circ}$
C. $75^{\circ}$
D. $15^{\circ}$

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Exercise For Sesssion 2

1. If in a triangle $A B C,(s-a)(s-b)=s(s-c)$, then angle $C$ is equal to
A. $90^{\circ}$
B. $45^{\circ}$
C. $30^{\circ}$
D. $60^{\circ}$

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2. In any $\triangle A B C$, If $\cot \frac{A}{2}, \cot \frac{B}{2}, \cot \frac{C}{2}$ are in AP, then $a, b, c$ are in
(a) AP
(b) GP
(c) HP
(d) None of these
3. In any $\triangle A B C, \frac{\tan \frac{A}{2}-\tan \frac{B}{2}}{\tan \frac{A}{2}+\tan \frac{B}{2}}$ is equal to:
A. (a) $\frac{a-b}{a+b}$
B. (b) $\frac{a-b}{c}$
C. (c) $\frac{a-b}{a+b+c}$
D. (d) $\frac{c}{a+b}$
4. Prove that $b c \cos ^{2} \cdot \frac{A}{2}+c a \cos ^{2} \cdot \frac{B}{2}+a b \cos ^{2} \cdot \frac{C}{2}=s^{2}$
A. $(s-a)^{2}$
B. $(s-b)^{2}$
C. $(s-c)^{2}$
D. $s^{2}$
5. In a $\triangle A B C$, if $\cos A+\cos B=4 \sin ^{2}\left(\frac{C}{2}\right)$, then a,b,c are in
(a) AP
(b) GP
(c) HP
(d) None of these

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6. In a $\triangle A B C$, if $b^{2}+c^{2}=3 a^{2}$, then $\cot B+\cot C-\cot A$ is equal to
A. 1
B. $\sqrt{3}$
C. 2
D. None of these
7. In
any
$\Delta A B C,\left(\frac{b-c}{a}\right) \cos ^{2}\left(\frac{A}{2}\right)+\left(\frac{c-a}{b}\right) \cos ^{2}\left(\frac{b}{2}\right)+\left(\frac{a-b}{2}\right) \cos ^{2}\left(\frac{C}{2}\right)$ is equal to?

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8. In a $\Delta A B C$, the tangent of half the difference of two angle is onethird the tangent of half the sum of the angle. Determine the ratio of the sides opposite to the angles.
A. 2: 3
B. 1: 3
C. 2: 1
D. 3: 4
9. If in a triangle $a \cos ^{2} \cdot \frac{C}{2}+c \cos ^{2} \cdot \frac{A}{2}=\frac{3 b}{2}$, then find the relation between the sides of the triangles
A. AP
B. GP
C. HP
D. AGP

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10. In the adjacent figure ' P ' is any interior point of the equilateral triangle ABC is side length 2 unit. If $x_{a}, x_{b}$ and $x_{c}$ represent the distance of P from the sides $\mathrm{BC}, \mathrm{CA}$ and AB respectively then $x_{a}+x_{b}+x_{c}$ is equal to
A. 6
B. $\sqrt{3}$
C. $\frac{\sqrt{3}}{2}$
D. $2 \sqrt{3}$
11. If $c^{2}=a^{2}+b^{2}$, then prove that $4 s(s-a)(s-b)(s-c)=a^{2} b^{2}$
A. $s^{4}$
B. $b^{2} c^{2}$
C. $c^{2} a^{2}$
D. $a^{2} b^{2}$
12. The number of possible $\angle A B C$ in which $B C=\sqrt{11} \mathrm{~cm}, C A=\sqrt{13} \mathrm{~cm}$ and $A=60^{\circ}$ is
A. 0
B. 1
C. 2
D. None of these

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13. If two sides $\mathrm{a}, \mathrm{b}$ and the $\angle A$ be such that two triangles are formed then sum of two values of the third side is
A. $b^{2}-a^{2}$
B. $2 b \cos A$
C. $2 b \sin A$
D. $\frac{b-c}{b+c}$

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14. If in a $\triangle A B C, \sin A=\sin ^{2} B$ and $2 \cos ^{2} A=3 \cos ^{2} B$, then the $\triangle A B C$ is
A. right angled
B. obtuse angled
C. isosceles
D. equilateral

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15. If a $\cos A=b \cos B$, then the triange is
A. (a)equliateral
B. (b)right angled
C. (c)isosceles
D. (d)isosceles or right angled

## D Watch Video Solution

16. Point $D, E$ are taken on the side $B C$ of an acute angled triangle $A B C$,, such that

$$
B D=D E=E C
$$

If
$\angle B A D=x, \angle D A E=y$ and $\angle E A C=z \quad$ then the value of $\frac{\sin (x+y) \sin (y+z)}{\sin x \sin z}$ is $\sin x \sin z$
A. 1
B. 2
C. 4
D. None of these

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17. If the base angles of triangle are $22 \frac{1}{2}$ and $112 \frac{1}{2}$, then prove that the altitude of the triangle is equal to $\frac{1}{2}$ of its base.
A. half the base
B. the base
C. twice the base
D. four times the base

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18. In a $\triangle A B C, a=1$ and the perrimeter is six times the AM of the sine of the angles. The measure of $\angle A$ is
A. $\frac{\pi}{3}$
B. $\frac{\pi}{2}$
C. $\frac{\pi}{6}$
D. $\frac{\pi}{4}$
19. In a $\Delta A B C$, if median AD is perpendicular to AB , the $\tan A+2 \tan B$ is equal to
A. (a) 1
B. (b) 3
C. (c) 0
D. (d) $\frac{1}{2}$
20. The product of the sines of the angles of a triangle is $p$ and the product of their cosines is $q$. Show that the tangents of the angles are the roots of the equation $q x^{3}-p x^{2}+(1+q) x-p=0$.
A. $q x^{2}-p x^{2}+(1+q) x-p=0$
B. $p x^{3}-q z^{2}+(1-p) x-q=0$
C. $(1+q) x^{3}-p x^{2}+q x-p=0$
D. None of these

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## Exercise For Sesssion 3

1. The side of a triangle are $22 \mathrm{~cm}, 28 \mathrm{~cm}$, and 36 cm So, find the area of a the circumscribed circle.
2. If the lengths of the side of a triangle are 3,4 and 5 units, then find the circum radius R .

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3. In an equliateral triangle of side $2 \sqrt{3} \mathrm{~cm}$. The find circum-radius.

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4. If $8 R^{2}=a^{2}+b^{2}+c^{2}$. then prove that the $\Delta$ is right angled.

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5. In a $\triangle A B C$, show that $2 R^{2} \sin A \sin B \sin C=\Delta$.

## - Watch Video Solution

6. In a $\triangle A B C$, show that $\frac{a \cos A+b \cos B+c \cos C}{a+b+c}=\frac{r}{R}$

## D Watch Video Solution

7. If the sides of a triangle are in the ratio $3: 7: 8$, then find $R: r$

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8. In an equilateral triangle show that the in-radius and the circum-radius are connected by $r=\frac{R}{2}$.

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9. In any $\triangle A B C$, find $\sin A+\sin B+\sin C$.

## - Watch Video Solution

10. In any $\triangle A B C$, show that $\cos A+\cos B+\cos C=\left(1+\frac{r}{R}\right)$.

## - Watch Video Solution

11. Prove that $\frac{r_{1}-r}{a}+\frac{r_{2}-r}{b}=\frac{c}{r_{3}}$

## - Watch Video Solution

12. Prove that $r_{1} r_{2}+r_{2} r_{3}+r_{3} r_{1}=\frac{1}{4}(a+b+c)^{2}$

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13. In triangle ABC .If $\left(r_{1}+r_{2}\right)\left(r_{2}+r_{3}\right)\left(r_{3}+r_{1}\right)=4 R s^{2}$ Then prove it

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14. If $r_{2}+r_{3}+r=r_{1}$, then show that $\Delta$ is right angled.
15. In an equilateral triangle, the inradius, circumradius, and one of the exradii are in the ratio

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16. Show that $\left(\frac{1}{r_{1}}+\frac{1}{r_{2}}\right)\left(\frac{1}{r_{2}}+\frac{1}{r_{3}}\right)\left(\frac{1}{r_{3}}+\frac{1}{r_{1}}\right)=\frac{64 R^{3}}{a^{2} b^{2} c^{2}}$

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17. The ex-radii $r_{1}, r_{2}, r_{3}$ of a $\triangle A B C$ are in Hp , show that its sides $\mathrm{a}, \mathrm{b}, \mathrm{c}$, are in AP.

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18. In a $\Delta A B C$, show that $r_{1} \cdot r_{2} \cdot r_{3} \cdot r=\Delta^{2}$.
19. If $l_{1}, l_{2}, l_{3}$ are respectively the perpendicular from the vertices of a triangle on the opposite side, then show that $l_{1} l_{2} l_{3}=\frac{a^{2} b^{2} c^{2}}{8 R^{3}}$.

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20. If the angle opf a triangle are in the ratio $1: 2: 3$, then show that the sides opposite to the respective angle are in the ratio $1: \sqrt{3}: 2$.

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21. Show that, $4 R r \cos \frac{A}{2} \cos \frac{B}{2} \cos \frac{C}{2}=\Delta$

## - Watch Video Solution

22. If in $\triangle A B C,(a-b)(s-c)=(b-c)(s-a)$, prove that $r_{1}, r_{2}, r_{3}$ are in A.P.

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23. In a triangle ABC , if $\frac{1}{r_{1}^{2}}+\frac{1}{r_{2}^{2}}+\frac{1}{r_{3}^{2}}+\frac{1}{r^{2}}=$

## - Watch Video Solution

24. Prove that $\left(r_{1}-r\right)\left(r_{2}-r\right)\left(r_{3}-r\right)=4 R r^{2}$

## - Watch Video Solution

25. Show that $\left(\frac{1}{r_{1}}+\frac{1}{r_{2}}\right)\left(\frac{1}{r_{2}}+\frac{1}{r_{3}}\right)\left(\frac{1}{r_{3}}+\frac{1}{r_{1}}\right)=\frac{64 R^{3}}{a^{2} b^{2} c^{2}}$
26. Prove that $(r+r 1) \tan ((B-C) / 2)+(r+r 2) \tan ((C-A) / 2)+(r+r 3) \tan ((A-B) / 2)=0$

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27. Show that $\frac{b-c}{r_{1}}+\frac{c-a}{r_{2}}+\frac{a-b}{r_{3}}=0$

## - Watch Video Solution

28. If the sides be $\mathrm{a}, \mathrm{b}, \mathrm{c}$, than find $\left(r_{1}-r\right)\left(r_{2}+r_{3}\right)$.

## - Watch Video Solution

29. If $a, b, c$ are in AP, then show that $r_{1}, r_{2}, r_{3}$ are in HP.

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30. In $\triangle A B C$ with usual notation $\frac{r_{1}}{b c}+\frac{r_{2}}{c a}+\frac{r_{3}}{a b}$ is

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31. Show that $r_{1}+r_{2}=c \cot \left(\frac{C}{2}\right)$

## - Watch Video Solution

32. Show that $\operatorname{Rr}(\sin A+\sin B+\sin C)=\Delta$

## - Watch Video Solution

33. Show that $16 R^{2} r r_{1} r_{2} r_{3}=a^{2} b^{2} c^{2}$

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34. If in a triangle $\frac{r}{r_{1}}=\frac{r_{2}}{r_{3}}$, then
35. $H$ is orthocenter of the triangle $A B C$, then $A H$ is equal to :

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2. A circle touches two of the smaller sides of a $\triangle A B C(a<b<c)$ and has its centre on the greater side. Then, find the radius of the circle.

## - Watch Video Solution

3. Prove that $a \cos A+b \cos B+c \cos C=4 R \sin A \sin B \sin C$

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4. If the altitudes of a triangle be $2,4,6$, then find its in-radius.
5. In a $\triangle A B C$, if $a=3, b=4, c=5$, then find the distance between its incentre and circumcentre.

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6. If the lengths of the perpendiculars from the vertices of a triangle $A B C$ on the opposite sides are $p_{1}, p_{2}, p_{3}$ then prove that
$\frac{1}{p_{1}}+\frac{1}{p_{2}}+\frac{1}{p_{3}}=\frac{1}{r}=\frac{1}{r_{1}}+\frac{1}{r_{2}}+\frac{1}{r_{3}}$.

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7. Prove that the distance between the circumcenter and the incenter of triangle ABC is $\sqrt{R^{2}-2 R r}$

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8. Prove that the distance between the circucentre and the orthocentre of a triangle ABC is $R \sqrt{1-8 \cos A \cos B \cos C}$.

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9. In a triangle $A B C, A D, B E$ and $C F$ are the altitudes and $R$ is the circum radius, then the radius of the circle DEF is

## D Watch Video Solution

10. If $l, l_{1}, l_{2}$ and $l_{3}$ be respectively the radii of the in-circle and the three escribed circles of a $\Delta A B C$, then find $l_{1} l_{2} l_{3}-l\left(l_{1} l_{2}+l_{2} l_{3}+l_{1} l_{3}\right)$.

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1. Find the sum of the radii of the circles, which are respectively inscribed and circumscribed about the a regular polygon of $n$ sides.

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2. Find the radius of the circumscribing circle of a regular polygon of $n$ sides each of length is a.

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3. Find the area of a right angle $\triangle A B C$, whose base is 10 and perpendicular is 12 .

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4. A polygon of nine sides, each side of length 2 , is inscribed in a circle.

The radius of the circle is $\qquad$ .
5. The area of the circle and the area of a regular polygon of $n$ sides and the perimeter of polygon equal to that of the circle are in the ratio of (a) $\tan \left(\frac{\pi}{n}\right): \frac{\pi}{n}$ (b) $\cos \left(\frac{\pi}{n}\right): \frac{\pi}{n} \frac{\sin \pi}{n}: \frac{\pi}{n}$ (d) $\cot \left(\frac{\pi}{n}\right): \frac{\pi}{n}$

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6. Let $A_{1}, A_{2}, A_{3}, \ldots, A_{n}$ be the vertices of an $n$-sided regular polygon such that $\frac{1}{A_{1} A_{2}}=\frac{1}{A_{1} A_{3}}+\frac{1}{A_{1} A_{4}}$. Find the value of n .

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7. If $I_{n}$ is the area of $n$-sided regular polygon inscribed in a circle of unit radius and $O_{n}$ be the area of the polygon circumscribing the given circle, prove that $I_{n}=\frac{O_{n}}{2}\left(\sqrt{1+\left(\frac{2 I_{n}}{n}\right)^{2}}\right)$

## Exercise For Sesssion 6

1. The area of a cyclic quadrilateral $\operatorname{ABCD}$ is $\frac{3 \sqrt{3}}{4}$. The radius of the circle circumscribing cyclic quadrilateral is $1.1 \mathrm{f} A B=1$ and $B D=\sqrt{3}$, then $B C \cdot C D$ is equal to

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2. If two adjacent sides of a cyclic quadrilateral aré 2 and 5 and the angle between them is $60^{\circ}$. If the third side is 3 , then the remaining fourth side is (a) 2 (b) 3 (c) 4 (d) 5

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3. The ratio of the area of a regular polygon of $n$ sides inscribed in a circle to that of the polygon of same number of sides circumscribing the same is $3: 4$. Then the value of $n$ is

## ( Watch Video Solution

4. A right angled trapezium is circumscribed about a circle. Find the radius of the circle if the lengths of the bases (i.e.parallel sides ) are equal to $a$ and $b$.

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5. If $A, B, C, D$ are the angles of quadrilateral, then find $\frac{\sum \tan A}{\sum \cot A}$.

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## Exercise For Sesssion 7

1. In triangle $A B C, a: b: c=(1+x): 1:(1-x)$ where $x \in(0,1)$ If $\angle A=\frac{\pi}{2}+\angle C$, then $x$ equal to
2. In a $\Delta A B C, 2 s=$ perimeter and $\mathrm{R}=$ circumradius. Then, find $\frac{s}{R}$.

## D Watch Video Solution

3. If in a $\triangle A B C, \angle C=90^{\circ}$, then the maximum value of $\sin A \sin B$ is

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4. If the area of a triangle is 81 square cm and its perimeter is 27 cm , then find its in-radius in centi-metres.

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5. In triangle ABC , if $r_{1}=2 r_{2}=3 r_{3}$, then $a: b$ is equal to

## - Watch Video Solution

6. The radius of the larger circle lying in the first quadrant and touching the line $4 x+3 y-12=0$ and the coordinate axes, is
A. (a) 5
B. (b) 6
C. (c) 7
D. (d) 8

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7. In a $\triangle P Q R$ as show in figure given that $x: y: z:: 2: 3: 6$, then find value of $\angle Q P R$.


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8. In a $\triangle A B C$ if $\frac{R}{r} \leq 2$, then show that the triangle is equilateral.

## - Watch Video Solution

9. If the angle of a right angled triangle are in A.P. then the ratio of the in
-radius and the perimeter, is
10. If in a triangle $\left(1-\frac{r_{1}}{r_{2}}\right)\left(1-\frac{r_{1}}{r_{3}}\right)=2$ then the triangle is right angled (b) isosceles equilateral (d) none of these

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## Exercise For Sesssion 8

1. If a tower subtends angles $\theta, 2 \theta$ and $3 \theta$ at three points $A, B$,and $C$ respectively, lying on the same side of a horizontal line through the foot of the tower, show that $\frac{A B}{B C} \frac{\cot \theta-\cot 2 \theta}{\cot 2 \theta-\cot 3 \theta}$.

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2. A person stands at a point $A$ due south of a tower of height $h$ and observes that its elevation is $60^{\circ}$. He then walks westwards towards B , where the elevation is $45^{\circ}$. At a point $C$ on $A B$ produced, show that if he find it to be $30^{\circ} . O A, O B, O C$ are in GP.
3. A train travelling on one of two intersecting railway lines, subtends at a certain station on the other line, an/ angle $\alpha$ when the front of the carriage reaches the junction and an angle $\beta$ when the end of the carriage reaches it. Then, the two lines are inclined to each other at an angle $\theta$, show that $2 \cot \theta=\cot \alpha-\cot \beta$

## D Watch Video Solution

4. The angle of elevation of the top of the tower observed from each of three points $A, B, C$ on the ground, forming a triangle is observed to be ' $\theta$
'. If $R$ is the circum-radius of the triangle $A B C$, then find the height of the tower

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5. The length of the shadow of a pole inclined at $10^{\circ}$ to the vertical towards the sun is 2.05 metres, when the elevation of the sun is $38^{\circ}$. The length of the pole is

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## PROPERTIES AND SOLUTIONS OF TRIANGLES EXERSISE 1: SINGLE OPTION CORRECT TYPE QUESTIONS

1. In the adjoining figure, the circle meets the sides of an equilateral triangle at six points.


If $A G=2, G F=13, F C=1$ and $H J=7$, then DE equals to
A. $2 \sqrt{22}$
B. $7 \sqrt{3}$
C. 9
D. 10

Answer: A

1. In a $\triangle A B C$, if $a=13, b=14$ and $c=15$, then $\angle A$ is equal to (All symbols used have their usual meaning in a triangle.)
A. $\sin ^{-1} \frac{4}{5}$
B. $\sin ^{-1} \frac{3}{5}$
C. $\sin ^{-1} \frac{3}{4}$
D. $\sin ^{-1} \frac{2}{3}$

## Answer: A

## - Watch Video Solution

2. In a $\triangle A B C$, if $b=(\sqrt{3}-1) a$ and $\angle C=30^{\circ}$, then the value of ( $\mathrm{A}-\mathrm{B}$ ) is equal to (All symbols used have usual meaning in the triangel.)
A. $30^{\circ}$
B. $45^{\circ}$
C. $60^{\circ}$
D. $75^{\circ}$

## Answer: C

## - Watch Video Solution

3. In $a \triangle A B C$, if $\angle C=105^{\circ}, \angle B=45^{\circ}$ and length of side $\mathrm{AC}=2$ units, then the length of th side $A B$ is equal to
A. $\sqrt{2}$
B. $\sqrt{3}$
C. $\sqrt{2}+1$
D. $\sqrt{3}+1$

## Answer: C

4. If $P$ is a point on the altitude $A D$ of the triangle $A B C$ such the $\angle C B P=\frac{B}{3}$, then AP is equal to
A. $2 a \sin \frac{C}{3}$
B. $2 b \sin \frac{A}{3}$
C. $2 c \sin \frac{B}{3}$
D. $2 c \sin \frac{C}{3}$

## Answer: C

## - Watch Video Solution

5. In $\triangle A B C$, if $2 b=a+c$ and $A-C=90^{\circ}$, then $\sin \mathrm{B}$ equal All symbols used have usual meaning in $\triangle A B C$.]
A. $\frac{\sqrt{7}}{5}$
B. $\frac{\sqrt{5}}{8}$
C. $\frac{\sqrt{7}}{4}$
D. $\frac{\sqrt{5}}{3}$

## Answer: C

## - Watch Video Solution

6. Let ABC be a right triangle with length of side $A B=3$ and hyotenus $A C=5$. If D is a point on BC such that $\frac{B D}{D C}=\frac{A B}{A C}$, then AD is equal to
A. $\frac{4 \sqrt{3}}{3}$
B. $\frac{3 \sqrt{5}}{2}$
C. $\frac{4 \sqrt{5}}{3}$
D. $\frac{5 \sqrt{3}}{4}$

## Answer: B

7. Two medians drawn from the acute angles of a right angled triangle intersect at an angle $\frac{\pi}{6}$. If the length of the hypotenuse of the triangle is 3 units, then the area of the triangle (in sq. units) is $\sqrt{3}$ (b) 3 (c) $\sqrt{2}$ (d) 9
A. 3
B. $\frac{3 \sqrt{5}}{2}$
C. $\sqrt{3}$
D. None of these

## Answer: C

## - Watch Video Solution

8. If in a right angle $\triangle A B C, 4 \sin A \cos B-1=0$ and $\tan \mathrm{A}$ is finite, then
A. angles are in AP
B. angles are in GP
C. angles are in $H P$
D. None of these

## Answer: A

## - Watch Video Solution

9. Find $\frac{d^{2} y}{d x^{2}}$, if $y=\cos ^{-1} x$

## - Watch Video Solution

10. If in a $\triangle A B C$, the incricle passing through the point of intersection of perpendicular bisector of sides $\mathrm{BC}, \mathrm{AB}$, then $4 \sin \frac{A}{2} \sin \frac{B}{2} \sin \frac{C}{2}$ equal to
A. $\sqrt{2}$
B. $\sqrt{2}-1$
C. $\sqrt{2}+1$
D. $\frac{1}{2}$

## Answer: B

## - Watch Video Solution

11. If two sides of a triangle are roots of the equation $x^{2}-7 x+8=0$ and the angle between these sides is $60^{\circ}$ then the product of inradius and circumradius of the triangle is $\frac{8}{7}$ (b) $\frac{5}{3}$ (c) $\frac{5 \sqrt{2}}{3}$ (d) 8
A. $\frac{8}{7}$
B. $\frac{5}{3}$
C. $\frac{5 \sqrt{3}}{3}$
D. 8

## Answer: B

12. If median $A D$ of a triangle $A B C$ makes angle $\frac{\pi}{6}$ with side $B C$, then the valur of $(\cot B-\cot C)^{2}$ is equal to
A. 6
B. 9
C. 12
D. 15

## Answer: C

## - Watch Video Solution

13. If the perimeter of the triangle formed by feet of altitudes of the triangle $A B C$ is equal to four times the circumradius of $\triangle A B C$, then identify the type of $\triangle A B C$
A. isosceles triangle
B. equilateral triangle
C. right angled triangle
D. None of these

## Answer: D

## D Watch Video Solution

14. In a triangle with one angle $\frac{2 \pi}{3}$, the lengths of the sides form an A.P. If the length of the greatest side is 7 cm , the radius of the circumcircle of the triangle is
A. $\frac{7 \sqrt{3}}{3} \mathrm{~cm}$
B. $\frac{5 \sqrt{3}}{3} \mathrm{~cm}$
C. $\frac{2 \sqrt{3}}{3} \mathrm{~cm}$
D. $\sqrt{3} \mathrm{~cm}$
15. If the sides of a $\triangle A B C$ are in AP and a is the smallest sie, then $\cos \mathrm{A}$ equals
A. $\frac{3 c-4 b}{2 b}$
B. $\frac{3 c-4 b}{2 c}$
c. $\frac{4 c-3 b}{2 b}$
D. $\frac{4 c-3 b}{2 c}$

## Answer: D

## - Watch Video Solution

16. If $p$ is the produce of the since of angles of a triange, and $q$ the product of their consines then tangents of the angles are roots of the equation
A. $q x^{2}-p x^{2}+(1-x) x-p=0$
B. $q x^{3}-p x^{2}-(1-q) x-p=0$
C. $q x^{3}-p x^{2}+(1+q) x-p=0$
D. None of these

## Answer: A

## - Watch Video Solution

17. Let C be incircle of $\triangle A B C$. If the tangents of lengths $t_{1}, t_{2}$ and $t_{3}$ are drawn inside the given triangle parallel to side $\mathrm{a}, \mathrm{b}$, and c , respectively, then $\frac{t_{1}}{a}+\frac{t_{2}}{b}+\frac{t_{3}}{c}$ is equal to
A. 0
B. 1
C. 2
D. 3

## - Watch Video Solution

18. If the sine of the angles of $\triangle A B C$ satisfy the equation $c^{3} x^{3}-c^{2}(a+b+c) x^{2}+l x+m=0$
(where a,b,c are the sides of $\triangle A B C$ ), then $\triangle A B C$ is
A. A. always right angled for any I, m
B. B.
right angled
only
when
$l=c(a b+b c+c a)=c \sum a b, m=-a b c$
C. C. right angled only when $l=\frac{c \sum a b}{4}, m=-\frac{a b c}{8}$
D. D. never right angled

Answer: B

## - Watch Video Solution

19. In triangle $A B C$, medians $A D$ and $C E$ are drawn $A D=5, \angle D A C=\pi / 8$, and $\angle A C E=\pi / 4$, then the area of the triangle $A B C$ is equal to
A. $\frac{50}{9}$
B. $\frac{25}{9}$
C. $\frac{25}{3}$
D. $\frac{27}{7}$

## Answer: C

## - Watch Video Solution

20. In a triangle $A B C, a \geq b \geq c$. If
$\frac{a^{3}+b^{3}+c^{3}}{\sin ^{3} A+\sin ^{3} B+\sin ^{3} C}=8$, then the maximum value of $a$
A. $\frac{1}{2}$
B. 2
C. 8
D. 64

## Answer: B

## - Watch Video Solution

21. Solve the following system of inequalities graphically
$2 x+4 y \leq 8,3 x+y \geq 6$

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22. In a $\delta A B C, \mathrm{a}, \mathrm{c}, \mathrm{A}$ are given and $b_{1}, b_{2}$ are two values of third side b such that $b_{2}=2 b_{1}$. Then, the value of $\sin \mathrm{A}$.
A. $\sqrt{\frac{9 a^{2}-c^{2}}{8 a^{2}}}$
B. $\sqrt{\frac{9 a^{2}-c^{2}}{8 c^{2}}}$
C. $\sqrt{\frac{9 a^{2}-c^{2}}{8 b^{2}}}$
D. None of these

## Answer: B

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$$
\begin{aligned}
& \text { 23. } \begin{array}{c}
\text { In } \\
\cot A=\left(x^{3}+x^{2}+x\right)^{\frac{1}{2}}, \cot B=\left(x+x^{-1}+1\right)^{\frac{1}{2}} \\
\text { and } \cot C=\left(x^{-3}+a\right.
\end{array}
\end{aligned}
$$

then the triangle is
A. equilateral
B. isosceles
C. right angled
D. obtuse anguled

## Answer: C

## - Watch Video Solution

24. In a $\triangle A B C, a, b, A$ are given and $c_{1}, c_{2}$ are two values of the third side c . The sum of the areas two triangles with sides $\mathrm{a}, \mathrm{b}, c_{1}$ and $a, b, c_{2}$ is
A. $\frac{1}{2} a^{2} \sin 2 A$
B. $\frac{1}{2} b^{2} \sin 2 A$
C. $b^{2} \sin 2 A$
D. None of these

## Answer: A

## - Watch Video Solution

25. In $\triangle A B C$, if a $=10$ and $b \cot B+c \cot C=2(r+R)$ then the maximum area of $\triangle A B C$ will be
A. 50
B. $\sqrt{50}$
C. 25
D. 5

## Answer: C

## - Watch Video Solution

26. Find the second order derivative of the function
$x^{3}+4 x^{2}+2$

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27. Let $\mathrm{a}, \mathrm{b}, \mathrm{c}$ be the sides of a triangle. Now two of them are equal to $\lambda \varepsilon R$.

If the roots of the equation $x^{2}+2(a+b+c) x+3 \lambda(a b+b c+c a)=0$ are real then
A. $\lambda<\frac{4}{3}$
B. $\lambda>\frac{5}{3}$
C. $\lambda \in\left(\frac{1}{3}, \frac{5}{3}\right)$
D. $\lambda \in\left(\frac{4}{3}, \frac{5}{3}\right)$

## Answer: A

## - Watch Video Solution

28. In triangle $A B C$, if $P Q, R$ divides sides $B C, A C$, and $A B$, respectively, in the ratio $k: 1$ (in order).

If the ratio $\left(\frac{\operatorname{area} P Q R}{\text { area } A B C}\right)$ is $\frac{1}{3}$,then k is equal to
A. $\frac{1}{3}$
B. 2
C. 3
D. None of these

## Answer: B

29. Let $f(x+y)=f(x) . f(y)$ for all x and $\mathrm{y} f(1)=2$ If in a triangle ${ }^{`} A B C, a=f(3), b=f(1)+f(3), c=f(2)+f(3)$, then $2 A$ is equal to
A. C
B. 2 C
C. 3C
D. 4 C

## Answer: A

## - Watch Video Solution

30. Differentiate the following function w.r.t x $\sin ^{3} x+\cos ^{6} x$
31. If tangents PA and PB from a point to a circle with centre $O$ are inclined to each other at angle of $80 \circ$, then $\angle P O A$ is equal to ,
A. (a) 50
B. (b) 60
C. (c) 70
D. (d) 80

## Answer: B

## - Watch Video Solution

32. Differentiate the following w.r.t $x$

$$
\left(3 x^{2}-9 x+5\right)^{9}
$$

33. In a triangle $a=\sqrt{5}, b=2, \angle A=\frac{\pi}{6}$ and the two possible values of third side are $c_{1}$ and $c_{2}$, then
A. $\left|c_{1}-c_{2}\right|=2 \sqrt{6}$
B. $\left|c_{1}-c_{2}\right|=4 \sqrt{6}$
C. $\left|c_{1}-c_{2}\right|=4$
D. $\left|c_{1}-c_{2}\right|=6$

## Answer: C

## - Watch Video Solution

34. If $R_{1}$ is the circumradius of the pedal triangle of a given triangle ABC , and $R_{2}$ is the circumradius of the pedal triangle of the pedal triangle formed, and so on $R_{3}, R_{4} \ldots$, then the value of $\sum_{i=1}^{\infty} R_{i}$, where R (circumradius) of $\triangle A B C$ is 5 is
B. 10
C. 12
D. 15

## Answer: B

## - Watch Video Solution

35. If in a triangle $\left(1-\frac{r_{1}}{r_{2}}\right)\left(1-\frac{r_{1}}{r_{3}}\right)=2$. then show that the triangle is right angled.
A. right angled
B. isosceles
C. equilateral
D. None of these

## Answer: A

36. If the median $A D$ of a triangle $A B C$ makes an angle $\theta$ with side, $A B$, then $\sin (A-\theta)$ is equal to
A. $\frac{b}{c} \sin \theta$
B. $\frac{c}{b} \sin \theta$
C. $\frac{c}{b} \cos \theta$
D. None of these

## Answer: B

## - Watch Video Solution

37. Differentiate the following w.r.t $x$
$(\sin x-\cos x)^{\sin x-\cos x}$
38. In a $\triangle A B C,(a+b+c)(b+c-a)=\lambda b c$, if
A. $\lambda<0$
B. $\lambda>6$
C. $0<\lambda<4$
D. $\lambda>4$

## Answer: C

## - Watch Video Solution

39. In the $\triangle A B C$, if $\left(a^{2}+b^{2}\right) \sin (A-B)=\left(a^{2}-b^{2}\right) \sin (A+B)$. Prove that the triangle is either isosceles or right angled.
A. either isosceles or right angled
B. only right angled
C. only isosceles triangle
D. None of the above

## - Watch Video Solution

40. Differentiate the following w.r.t $x$
$(5 x)^{3 \cos 2 x}$

## - Watch Video Solution

41. If $a, b, c$ be the sides of $a$ triangle $A B C$ and if roots of equation
$a(b-c) x^{2}+b(c-a) x+c(a-b)=90 \quad$ are equal then $\frac{\sin ^{2} A}{2}, \frac{\sin ^{2} B}{2}, \frac{\sin ^{2} C}{2}$ are in
A. (a)AP
B. (b) GP
C. (c) HP
D. (d)none of these

## Answer: C

## - Watch Video Solution

42. The ratio of the area of a regular polygon of $n$ sides inscribed in a circle to that of the polygon of same number of sides circumscribing the same is $3: 4$. Then the value of $n$ is
A. 6
B. 4
C. 8
D. 12

## Answer: A

43. In any triangle $\mathrm{ABC} \sum \frac{\sin ^{2} A+\sin A+1}{\sin A}$ is always greater than or equal
A. 9
B. 3
C. 27
D. None of these

## Answer: C

## - Watch Video Solution

44. If the incircel of the triangle $A B C$, through it's circumcentre, then the $\cos A+\cos B+\cos C$ is
A. -2
B. $\sqrt{2}$
C. $-\sqrt{2}$
D. None of these

## Answer: B

## - Watch Video Solution

45. The perimeter of a triangle $A B C$ is six times the arithmetic mean of the sines of its angles. If the side ais1 then find angle $A$.
A. $30^{\circ}$
B. $60^{\circ}$
C. $90^{\circ}$
D. $120^{\circ}$

## Answer: A

46. If there are only two linear functions $f$ and $g$ which map $[1,2]$ on $[4,6]$ and in a $\triangle A B C, c=f(1)+g(1)$ and a is the maximum valur of $r^{2}$, where $r$ is the distance of $a$ variable point on the curve $x^{2}+y^{2}-x y=10$ from the origin, then $\sin \mathrm{A}: \sin \mathrm{C}$ is
A. A. $1: 2$
B. B. 2: 1
C. C. $1: 1$
D. D. None of these

## Answer: C

## - Watch Video Solution

47. A circle is inscribed in an equilateral triangle of side $a$. The area of any square inscribed in this circle is $\qquad$ .
A. $a^{2}$
B. $\frac{a^{2}}{4}$
C. $\frac{a^{2}}{3}$
D. $\frac{a^{2}}{6}$

## Answer: D

## - Watch Video Solution

48. In any triangle $A B C$, if $\sin A, \sin B, \sin C$ are in $A P$, then the maximum value of $\tan \frac{B}{2}$ is
A. $-\frac{1}{\sqrt{3}}$
B. $\frac{1}{\sqrt{3}}$
C. $\frac{1}{3}$
D. None of these

## Answer: B

49. In a $\triangle A B C, 2 \cos A=\frac{\sin B}{\sin C}$ and $2^{\tan ^{2} B}$ is a solution of equation $x^{2}-9 x+8=0$, then $\triangle A B C$ is
A. equilateral
B. isosceles
C. scalene
D. right angled

## Answer: A

## - Watch Video Solution

50. Differentiate the following w.r.t x
$\sin ^{-1}\left(x^{\frac{3}{2}}\right)$
51. If $\mathrm{a}, \mathrm{b}$ and c arethe sides of a traiangle such that $b . c=\lambda^{2}$, then the relation is $a, \lambda$ and $A$ is
A. $c \geq 2 \lambda \sin \left(\frac{C}{2}\right)$
B. $b \geq 2 \lambda \sin \left(\frac{A}{2}\right)$
C. $a \geq 2 \lambda \sin \left(\frac{A}{2}\right)$
D. None of these

## Answer: C

## - Watch Video Solution

52. Differentiate the following w.r.t $x$
$\cos (a \cos x+b \sin x)$, for some constant $a$ and $b$

## - Watch Video Solution

53. In triangle $A B C, a=5, b=4$ and $\cos (A+B)=\frac{31}{32}$ In this triangle,$c=$
A. 3
B. 6
C. 7
D. 9

## Answer: B

## - Watch Video Solution

54. In a $A B C$, if $A B=x, B C=x+1, \angle C=\frac{\pi}{3}$, then the least integer value of $x$ is 6 (b) 7 (c) 8 (d) none of these
A. 6
B. 7
C. 8
D. None of these

## Answer: B

## - Watch Video Solution

55. In an equilateral triangle, three coins of radii 1 unit each are kept so that they touch each other and also the sides of the triangle. The area of the triangle is $2 \mathrm{sqrt}(3)(b) 6+4 \mathrm{sqrt}(3) 12+(7 \mathrm{sqrt}(3)) / 4(d) 3+(7 \mathrm{sqrt}(3)) / 4$
A. $(4+2 \sqrt{3}) \mathrm{cm}^{2}$
B. $\frac{1}{4}(12+7 \sqrt{3}) \mathrm{cm}^{2}$
C. $\frac{1}{4}(48+7 \sqrt{3}) \mathrm{cm}^{2}$
D. $(6+4 \sqrt{3}) \mathrm{cm}^{2}$

## Answer: D

## - Watch Video Solution

56. Differentiate the following w.r.t $x$
$2 x^{\left(x^{4}-3\right)}$

## D Watch Video Solution

57. Differentiate the following w.r.t $x$
$x^{x}+a^{a}$

## D Watch Video Solution

58. In a triangle $A B C$, the line joining the circumcentre and incentre is parallel to $B C$, then $\operatorname{Cos} B+\operatorname{Cos} C$ is equal to:
A. $\frac{3}{2}$
B. 1
C. $\frac{3}{4}$
D. $\frac{1}{2}$

## D Watch Video Solution

59. In the given figure, $A B$ is the diameter of the circle, centered at $O$. If $\angle C O A=60^{\circ}, A B=2 r, A c=d$ and $C D=l$, then $I$ is equal to

A. $d \sqrt{3}$
B. $\frac{d}{\sqrt{3}}$
C. $3 d$
D. $\frac{\sqrt{3} d}{2}$

## D Watch Video Solution

60. In a triangle $A B C, A D, B E$ and $C F$ are the altitudes and $R$ is the circum radius, then the radius of the circle DEF is
A. $2 R$
B. $R$
C. $\frac{R}{2}$
D. None of these

## Answer: C

## D Watch Video Solution

61. Find $\frac{d y}{d x}$, If $\mathrm{x}=\mathrm{a}(\sin \mathrm{t}-\mathrm{t} \cos \mathrm{t})$ and $\mathrm{y}=\mathrm{a}(\cos \mathrm{t}+\mathrm{t} \sin \mathrm{t})$
62. Differentiate the following w.r.t x
$(x-4)^{x^{3}}$

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63. Find $\frac{d y}{d x}$, if $\mathrm{x}=6(\mathrm{t}-\sin \mathrm{t}), \mathrm{y}=4(1-\cos \mathrm{t})$

## - Watch Video Solution

64. Using the fact that $\cos (A+B)=\cos A \cos B-\sin A \sin B$ and the differentiation, obtain the sum formula for sine.

## - Watch Video Solution

65. Find $\frac{d y}{d x}$, if $y=\sin ^{-1}\left(1-x^{2}\right)^{\frac{1}{2}}$

## Exercise (More Than One Correct Option Type Questions)

1. If area of $\Delta A B C(\Delta)$ and angle C are given and if c opposite to given angle is minimum, then
A. $a=\sqrt{\frac{2 \Delta}{\sin C}}$
B. $b=\sqrt{\frac{2 \Delta}{\sin C}}$
C. $a=\frac{4 \Delta}{\sin C}$
D. $b=\frac{4 \Delta}{\sin ^{2} C}$

## Answer: A

## - Watch Video Solution

2. Differentiate the following w.r.t x
$x^{a}+a^{x}$
3. In $\triangle A B C$, the value of $c \cos (A-\theta)+a \cos (C+\theta)=$

## Watch Video Solution

4. In $\triangle A B C$, If $a=4, b=3$ and $\operatorname{COS}(A-B)=\frac{3}{4}$, then
A. measure of $\angle A$ is $\frac{\pi}{2}$
B. measuere of $\angle B i s \frac{\pi}{2}$
C. $\cot \frac{C}{2}=\sqrt{7}$
D. circumradius of $\triangle A B C i s \frac{2}{7^{1 / 14}}$

## Answer: B::C::D

- Watch Video Solution

5. Find the second order derivative of the function
$2 \log x^{2}+4 x$

## Watch Video Solution

6. Is it possible to have $a \triangle A B C$ with $a=3, b=5, c=7$ and $C=\frac{2 \pi}{3}$ ?
A. (a) $(a+c-b)(a-c+b)=4 b c$
B. (b) $b^{2} \sin 2 C+\cos ^{2} \sin 2 B=a b$
C. (c) $a=3, b=5, c=7$ and $C=\frac{2 \pi}{3}$
D. (d) $\cos \left(\frac{A-C}{2}\right)=\cos \left(\frac{A+C}{2}\right)$

## Answer: B::C

7. Find the second order derivative of the function X.CosX

## Watch Video Solution

8. Differentiate the following w.r.t $x$
$(x+3)^{2} \cdot(x+4)^{3}$

## - Watch Video Solution

9. Find the second order derivative of the function
$x^{6}+2$

## - Watch Video Solution

10. Given an isoceles triangle with equal side of length $b$ and angle $\alpha<\pi / 4$, then
the inradius $r$ is given by
A. $R=\frac{1}{2} b \cos e c \alpha$
B. $\Delta=2 b^{2} \sin 2 \alpha$
C. $r=\frac{b \sin 2 \alpha}{2(1+\cos \alpha)}$
D. $O I\left|\frac{b \cos \left(\frac{3 \alpha}{2}\right)}{2 \sin \alpha\left(\frac{\alpha}{2}\right)}\right|$

## Answer: A::C::D

## - Watch Video Solution

11. There can exist a triangle $A B C$ satisfying the condition $\frac{\sin A}{2}=\frac{\sin B}{3}=\frac{\sin C}{7}$
A. $\tan A+\tan B+\tan C=0$
B. $\frac{\sin A}{2}=\frac{\sin B}{3}=\frac{\sin C}{7}$
C. $(a+b)^{2}=c^{2}+a b$ and $\sqrt{2}(\sin A+\cos A)=\sqrt{3}$
D.
$\sin A+\sin B=\left(\frac{\sqrt{3}+1}{2}\right) \cos A \cos B=\frac{\sqrt{3}}{4}=\frac{\sqrt{3}}{4}=\sin A \sin B$

## Answer: C::D

## - Watch Video Solution

12. Find $\frac{d^{2} y}{d x^{2}}$, if $y=\log x$

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13. If in $\triangle A B C, A=90^{\circ}$ and $\mathrm{c}, \sin \mathrm{B}$ and $\cos \mathrm{B}$ are rational number, then
A. a is rational
B. $a$ is irrational
C. b is rational
D. $b$ is irational

## D Watch Video Solution

14. Find second order derivative of the function $\sin ^{-1} x$

## - Watch Video Solution

15. Let ' $I$ ' is the length of medians from the vertex $A$ to the side $B C$ of a $\triangle A B C$, then
A. $4 l^{2}=2 b^{2}+2 c^{2}-a^{2}$
B. $4 l^{2}=b^{2}+c^{2}+2 b c \cos A$
C. $4 l^{2}=b^{2}+4 b c \cos A$
D. $4 l^{2}-(2 s-a)^{2}-4 b c \sin ^{2}\left(\frac{A}{2}\right)$

## - Watch Video Solution

16. If $A, A_{1}, A_{2}$ and $A_{3}$ are the areas of the inscribed and escribed circles of a triangle, prove that $\frac{1}{\sqrt{A}}=\frac{1}{\sqrt{A_{1}}}+\frac{1}{\sqrt{A_{2}}}+\frac{1}{\sqrt{A_{3}}}$
A. (a) $\sqrt{A_{1}}+\sqrt{A_{2}}+\sqrt{A_{3}}=\sqrt{\pi}\left(r_{1}+r_{2}+r_{3}\right)$
B. (b) $\frac{1}{\sqrt{A_{1}}}+\frac{1}{\sqrt{A_{2}}}+\frac{1}{\sqrt{A_{3}}}=\frac{1}{\sqrt{A}}$
C. (c) $\frac{1}{\sqrt{A_{1}}}+\frac{1}{\sqrt{A_{2}}}+\frac{1}{\sqrt{A_{3}}}=\frac{s^{2}}{\sqrt{\pi} r_{1} r_{2} r_{3}}$
D. (d) $\sqrt{A_{1}}+\sqrt{A_{2}}+\sqrt{A_{3}}=\sqrt{\pi}(4 R+r)$

## Answer: A::B::C::D

## - Watch Video Solution

17. If $a, b, A$ be given in a triangle and $c_{1}$ and $c_{2}$ be two possible value of the third side such that $c_{1}^{2}+c_{1} c_{2}+c_{2}^{2}=a^{2}$, then a is equal to
A. (a) $30^{\circ}$
B. (b) $60^{\circ}$
C. (c) $90^{\circ}$
D. (d) $120^{\circ}$

## Answer: B::C

## - Watch Video Solution

18. $D, E$ and $F$ are the middle points of the sides of the triangle $A B C$, then
A. centroid of the triangle DEF is the same as that of ABC
B. orthocentre of the triangle DEF is the circumcentre of $A B C$
C. orthocentre of the triangle DEF is the incentre of ABC
D. centroid of the triangle DEF is not the same as that of $A B C$

## Answer: A: B

19. The sides of $A B C$ satisfy the equation $2 a^{2}+4 b^{2}+c^{2}=4 a b+2 a c$ Then a) the triangle is isosceles b) the triangle is obtuse c) $B=\cos ^{-1}\left(\frac{7}{8}\right)$ d) $A=\cos ^{-1}\left(\frac{1}{4}\right)$
A. the triangle is isosceles
B. the triangle is obtuse
C. $B=\cos ^{-1}\left(\frac{7}{8}\right)$
D. $A=\cos ^{-1}\left(\frac{1}{4}\right)$

## Answer: A::C::D

## - Watch Video Solution

20. If $\Delta$ represents the area of acute angled triangle $A B C$, then

$$
\begin{align*}
& \sqrt{a^{2} b^{2}-4 \Delta^{2}}+\sqrt{b^{2} c^{2}-4 \Delta^{2}}+\sqrt{c^{2} a^{2}-4 \Delta^{2}}=\text { (a) } a^{2}+b^{2}+c^{2}  \tag{b}\\
& \frac{a^{2}+b^{2}+c^{2}}{2} \\
& \text { (c) } a b \cos C+b c \cos A+c a \cos B
\end{align*}
$$

$a b \sin C+b c \sin A+c a \sin B$
A. ${ }^{`}\left(a^{\wedge}(2)+b^{\wedge}(2)+c^{\wedge}(2)\right)$
B. $\frac{a^{2}+b^{2}+c^{2}}{2}$
C. $a b \cos C+b c \cos A+c a \cos B$
D. $a b \sin C+b c \sin A+c a \sin B$

## Answer: B::C

## - Watch Video Solution

21. In triangle, $A B C$ if $2 a^{2} b^{2}+2 b^{2} c^{2}=a^{2}+b^{4}+c^{4}$, then angle B is equal to $45^{0}$ (b) $135^{0} 120^{\circ}$ (d) $60^{0}$
A. $45^{\circ}$
B. $135^{\circ}$
C. $120^{\circ}$
D. $60^{\circ}$
22. If H is the orthocentre of triangle $\mathrm{ABC}, \mathrm{R}=$ circumradius and $P=A H+B H+C H$, then
A. $p=2(R+r)$
B. max, of $P$ is $3 R$
C. min. of $P$ is $3 R$
D. $P=2(R-r)$

## Answer: A: B

## - Watch Video Solution

23. If inside a big circle exactly $n(n \leq 3)$ small circles, each of radius $r$, can be drawn in such a way that each small circle touches the big circle and also touches both its adjacent small circles, then the radius of big
circle is (a) $r\left(1+\operatorname{cosec} \frac{\pi}{n}\right)$
(b) $\left(\frac{1+\frac{\tan \pi}{n}}{\frac{\cos \pi}{\pi}}\right)$ (c) $r\left[1+\operatorname{cosec} \frac{2 \pi}{n}\right]$
$\frac{r\left[s \in \frac{\pi}{2 n}+\frac{\cos (2 \pi)}{n}\right]^{2}}{\frac{\sin \pi}{n}}$
A. $r\left(1+\operatorname{cosec} \frac{\pi}{n}\right)$
B. $\left(\frac{1+\tan \frac{\pi}{n}}{\cos \frac{\pi}{n}}\right)$
C. $r\left[1+\cos e c \frac{2 \pi}{n}\right]$
D. $\frac{r\left[\sin \frac{\pi}{2 n}+\cos \frac{2 \pi}{n}\right]^{2}}{\sin ^{\prime} \frac{\pi}{n}}$

## Answer: A: D

## - Watch Video Solution

24. If in triangle $\mathrm{ABC}, \mathrm{a}, \mathrm{C}$ and angle A are given and $c \sin A<a<c$, then ( $b_{1}$ and $b_{2}$ are values of b)
A. (a) $b_{1}+b_{2}=2 c \cos A$
B. (b) $b_{1}+b+2=c \cos A$
C. (c) $b_{1} b_{2}=c^{2}-a^{2}$
D. (d) $b_{1} b_{2}=c^{2}+a^{2}$

## Answer: A:C

## - Watch Video Solution

## Exercise (Statement I And li Type Questions)

1. In a triangle $A B C, a^{3}+b^{3}+c^{3}=c^{2}(a+b+c)$ (All symbol used have usual meaning in a triangle.) Statement-1: The value of $\angle C=60^{\circ}$. Statement-2: $\triangle A B C$ must be equilateral.
A. (a)Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I
B. (b)Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I
C. (c)Statement I is correct but Statement II is incorrect
D. (d)Statement I is correct but Statement I is incorrect

## Answer: C

## - Watch Video Solution

2. Let $\mathrm{a}=6, \mathrm{~b}=3$ and $\cos (A-B)=\frac{4}{5}$

Value of $\sin A$ is equal to
A. Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I
B. Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I
C. Statement I is correct but Statement II is incorrect
D. Statement I is correct but Statement I is incorrect

## Answer: D

3. Statement I: If in a triangle $A B C, \sin ^{2} A+\sin ^{2} B+\sin ^{2} C=2$, then one of the angles must be $90^{\circ}$.
Statement II: In any triangle $A B C$ $\cos 2 A+\cos 2 B+\cos 2 C=-1-4 \cos A \cos B \cos C$
A. (a) Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I
B. (b) Both Statement I and Statement II are correct but Statement II is not the correct explanation of Statement I
C. (c) Statement I is correct but Statement II is incorrect
D. (d) Statement II is correct but Statement I is incorrect

## Answer: A

## - Watch Video Solution

4. Statement I: If $A, B, C, D$ are angles of a cyclic quadrilateral then $\sum \sin A=0$.

Statement II: If $A, B, C, D$ are angles of cyclic quadrilateral then $\sum \cos A=0$.
A. (a) Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I
B. (b) Both Statement I and Statement II are correct but Statement II is not the correct explanation of Statement I
C. (c) Statement I is correct but Statement II is incorrect
D. (d) Statement II is correct but Statement I is incorrect

## Answer: D

## - Watch Video Solution

5. Statement I In any triangle ABC, the square of the length of the bisector AD is $b c\left(1-\frac{a^{2}}{(b+c)^{2}}\right)$.
Statement II In any triangle $A B C$ length of bisector $A D$ is $\frac{2 b c}{(b+c)} \cos \left(\frac{A}{2}\right)$.
A. (a)Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I
B. (b)Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I
C. (c)Statement I is correct but Statement II is incorrect
D. (d)Statement I is correct but Statement I is incorrect

## Answer: A

## - Watch Video Solution

6. Prove that $\sin 4 x=4 \sin x \cos ^{3} x-4 \cos x \sin ^{3} x$
7. All the notations used in statemnt I and statement II are usual.

Statement I: In triangle ABC , if $\frac{\cos A}{a}=\frac{\cos B}{b}=\frac{\cos C}{c}$. then value of $\frac{r_{1}+r_{2}+r_{3}}{r}$ is equal to 9 .
Statement II: In $\triangle A B C: \frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}=2 R$, where R is circumradius.
A. a) Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I
B. b) Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I
C. c) Statement I is correct but Statement II is incorrect
D. d) Statement II is correct but Statement I is incorrect

## Answer: A

## - Watch Video Solution

8. Statement I In a triangle ABC if $\tan A: \tan B: \tan C=1: 2: 3$, then

$$
A=45^{\circ}
$$

Statement II If $p: q: r=1: 2: 3$, then $p=1$
A. A. Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I
B. B. Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I
C. C. Statement I is correct but Statement II is incorrect
D. D. Statement I is correct but Statement I is incorrect

## Answer: C

## - Watch Video Solution

9. Statement I: In any right angled triangle $\frac{a^{2}+b^{2}+c^{2}}{R^{2}}$ is always equal to 8 .

Statement II: $a^{2}=b^{2}+c^{2}$
A. a) Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I
B. b) Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I
C. c) Statement I is correct but Statement II is incorrect
D. d) Statement I is incorrect but Statement II is correct

## Answer: A

## - Watch Video Solution

10. Statement I perimeter of a regular pentagon inscribed in a circle with centre O and radius a cm equals $10 a \sin 36^{\circ} \mathrm{cm}$.

Statement II Perimeter of a regular polygon inscribed in a circle with centre $O$ and radius a cm equals $(3 n-5) \sin \left(\frac{360^{\circ}}{2 n}\right) c m$, then it is $n$ sided, where $n \geq 3$.
A. (a)Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I
B. (b)Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I
C. (c)Statement I is correct but Statement II is incorrect
D. (d)Statement I is correct but Statement I is incorrect

## Answer: C

## - Watch Video Solution

11. Statement I In any triangle $A B C$
$a \cos A+b \cos B+c \cos C \leq s$.

Statement II In any triangle ABC
$\sin \left(\frac{A}{2}\right) \sin \left(\frac{B}{2}\right) \sin \left(\frac{C}{2}\right) \leq \frac{1}{8}$
A. Both Statement I and Statement II are correct and Statement II is
B. Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I
C. Statement I is correct but Statement II is incorrect
D. Statement I is correct but Statement I is incorrect

## Answer: A

## - Watch Video Solution

12. Statement I In a $\Delta A B C$, if $\cos ^{2} \frac{A}{2}+\cos ^{2} \frac{B}{2}+\cos ^{2} \frac{C}{2}=y\left(x^{2}+\frac{1}{x^{2}}\right)$ then the maximum value of yis $\frac{9}{8}$.
Statement II In a $\triangle A B C, \sin \frac{A}{2} \cdot \sin \frac{B}{2} \sin \frac{C}{2} \leq \frac{1}{8}$
A. Both Statement I and Statement II are correct and Statement II is the correct explanation of Statement I
B. Both Statement I and Statement II are correct and Statement II is not the correct explanation of Statement I
C. Statement I is correct but Statement II is incorrect
D. Statement I is correct but Statement I is incorrect

## Answer: A

## - Watch Video Solution

13. Find the second order derivative of the given function
$e^{y}(x+1)=1$

## Watch Video Solution

14. Find $\frac{d y}{d x}, \quad$ if $y=3 \cos (\log x)+4 \sin (\log x)$
A.
B.
C.
D.

## Answer: A

## - Watch Video Solution

15. Find second order derivative of the function
$5 \cos x-3 \sin x$

## ( Watch Video Solution

## Exercise (Passage Based Questions)

1. Find $\frac{d y}{d x}, \quad$ if $y=500 e^{7 x}+600 e^{-7 x}$

## - Watch Video Solution

2. Find the second order derivative of the function
$A e^{m x}+B e^{n x}$
3. If $x$ and $y$ are connected parameterically by the equation, without eliminating the parameter, find $\frac{d y}{d x}$
$x=a \cos (\theta), y=b \sin (\theta)$

## - Watch Video Solution

4. Let ABC to be an acute triangle with $B C=a, C A=b$ and $A B=c$, where $a \neq b \neq c$. From any point 'p' inside $\triangle A B C \leq D, E, F$ denot foot of perpendiculars form ' $p$ ' noto the sides, $B C, C A$ and $A B$, respectively.

Now, answer the following equations.
If $\triangle D E F$ is equilateral, then ' P '
A. the incircle of $\triangle A B C$
$B$. line of intternal angle bisectors from $A, B$ and $C$
C. arcs of 3 circles
D. None of the above

## Answer: C

## D Watch Video Solution

5. Let ABC to be an acute triangle with $B C=a, C A=b$ and $A B=c$, where $a \neq b \neq c$. From any point 'p' inside $\triangle A B C \leq D, E, F$ denot foot of perpendiculars form ' $p$ ' noto the sides, $B C, C A$ and $A B$, respectively. Now, answer the following equations.

If $\triangle D E F$ is equilateral, then ' P '
A. $x=4$ or $x+y y=7$ or $4 x=3 y$
B. $x=4$ or $x^{2}+y^{2}=4 x+4 y$
C. $3\left(x^{2}+y^{2}\right)+196=49(x+y)$
D. None of the above

## Answer: C

## - Watch Video Solution

6. Let ABC to be an acute triangle with $B C=a, C A=b$ and $A B=c$, where $a \neq b \neq c$. From any point 'p' inside $\triangle A B C \leq D, E, F$ denot foot of perpendiculars form ' $p$ ' noto the sides, $B C, C A$ and $A B$, respectively. Now, answer the following equations.

If $\triangle D E F$ is equilateral, then ' P '
A. coincides with incentre of $\triangle A B C$
B. coincides with orthocentre of $\triangle A B C$
C. lies on padal $\Delta$ of $\triangle A B C$
D. None of the above

## Answer: D

## - Watch Video Solution

7. In an acute angled triangle $A B C$, let $A D, B E$ and $C F$ be the perpendicular opposite sides of the triangle. The ratio of the product of the side lengths of the triangles $D E F$ and $A B C$, is equal to
A. A. $\frac{3(a b c)^{\frac{1}{3}}}{4(a+b+c)}$
B. B. $\frac{1}{4}$
C. C. $\cos A \cos B \cos C$
D. D. $\sin \left(\frac{A}{2}\right) \sin \left(\frac{B}{2}\right) \sin \left(\frac{C}{2}\right)$

## Answer: C

## - Watch Video Solution

8. In an acute angle $\triangle A B C$, let $\mathrm{AD}, \mathrm{BE}$ and CF be the perpendicular from
$A, B$ and $C$ upon the opposite sides of the triangle. (All symbols used have usual meaning in a tiangle.)

The orthocentre of the $\triangle A B C$, is the
A. centroid of the $\triangle D E F$
B. circum-centre of the $\triangle D E F$
C. incentre of the $\triangle D E F$
D. orthocentre of the $\triangle D E F$

## Answer: C

## - Watch Video Solution

9. In an acute angle $\triangle A B C$, let $\mathrm{AD}, \mathrm{BE}$ and CF be the perpendicular from A, B and C upon the opposite sides of the triangle. (All symbols used have usual meaning in a tiangle.)

The circum-radius of the $\Delta D E F$ can be equal to
A. $\frac{a b c}{8 \Delta}$
B. $\frac{a}{4 \sin A}$
C. $\frac{R}{2}$
D. $\frac{r}{8} \operatorname{cosec} \frac{A}{2} \operatorname{cosec} \frac{B}{2} \operatorname{cosec} \frac{C}{2}$

## Answer: A::B::C::D

## D Watch Video Solution

10. Let $\mathrm{a}, \mathrm{b}, \mathrm{c}$ are the sides opposite to angles $\mathrm{A}, \mathrm{B}, \mathrm{C}$ respectively in a $\triangle A B C \tan \frac{A-B}{2}=\frac{a-b}{a+b} \cot \frac{C}{2}$ and $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$, If $a=6, b=3$ and $\cos (A-B)=\frac{4}{5}$

Angle $C$ is equal to
A. $\frac{\pi}{4}$
B. $\frac{\pi}{2}$
C. $\frac{3 \pi}{4}$
D. $\frac{2 \pi}{3}$

## Answer: B

## - Watch Video Solution

11. Let $\mathrm{a}, \mathrm{b}, \mathrm{c}$ are the sides opposite to angles $\mathrm{A}, \mathrm{B}, \mathrm{C}$ respectively in a $\triangle A B C \tan \frac{A-B}{2}=\frac{a-b}{a+b} \cot \frac{C}{2}$ and $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$, If $a=6, b=3$ and $\cos (A-B)=\frac{4}{5}$

Area of the trianlge is equal to
A. 8
B. 9
C. 10
D. 11

## Answer: B

## - Watch Video Solution

12. Let $\mathrm{a}, \mathrm{b}, \mathrm{c}$ are the sides opposite to angles $\mathrm{A}, \mathrm{B}, \mathrm{C}$ respectively in a $\triangle A B C \tan \frac{A-B}{2}=\frac{a-b}{a+b} \cot \frac{C}{2}$ and $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$, If $a=6, b=3$ and $\cos (A-B)=\frac{4}{5}$

Valus of $\sin \mathrm{A}$ is equal to
A. $\frac{1}{\sqrt{5}}$
B. $\frac{2}{\sqrt{5}}$
C. $\frac{1}{2 \sqrt{5}}$
D. $\frac{1}{\sqrt{3}}$

## Answer: B

## - Watch Video Solution

13. Find $\frac{d y}{d x}, \quad$ if $x=\frac{4}{t}$ and $y=4 t$

## - Watch Video Solution

14. If $x$ and $y$ are connected parametrically by the equation, without eliminating parameter, find $\frac{d y}{d x}$ $x=a \sec (\theta), y=b \tan (\theta)$

## - Watch Video Solution

15. Find $\frac{d y}{d x}$, if $x=a \sin t, y=a\left(\cos t+\log \left(\tan \left(\frac{t}{2}\right)\right)\right.$

## - Watch Video Solution

16. Find $\frac{d y}{d x}, \quad$ if $x=\cos (\theta)$ and $y=\sin (2 \theta)$

## - Watch Video Solution

17. Differentiate the following function w.r.t x
$\frac{\cos ^{-1} x}{(2 x+7)^{\frac{1}{2}}}$

## - Watch Video Solution

18. Consider a triangle $A B C$, where $x, y, z$ are the length of perpendicular drawn from the vertices of the triangle to the opposite sides $a, b, c$ respectively. Let the letters $R, r S, \Delta$ denote the circumradius, inradius semi-perimeter and area of the triangle respectively.
If $\frac{b x}{c}+\frac{c y}{a}+\frac{a z}{b}=\frac{a^{2}+b^{2}+c^{2}}{k}$, then the value of k is
A. R
B. S
C. 2 R
D. $\frac{3}{2} R$

## Answer: C

## - Watch Video Solution

19. Consider a triangle $A B C$, where $x, y, z$ are the length of perpendicular drawn from the vertices of the triangle to the opposite sides $a, b, c$ respectively. Let the letters $R, r S, \Delta$ denote the circumradius, inradius semi-perimeter and area of the triangle respectively.

If $\cot A+\cot B+\cot C=k\left(\frac{1}{x^{2}}+\frac{1}{y^{2}}+\frac{1}{z^{2}}\right)$, then the value of k is
A. $R^{2}$
B. rR
C. $\Delta$
D. $a^{2}+b^{2}+c^{2}$

## Answer: C

20. Consider a triangle $A B C$, where $x, y, z$ are the length of perpendicular drawn from the vertices of the triangle to the opposite sides $a, b, c$ respectively. Let the letters $R, r, S, \Delta$ denote the circumradius, inradius semi-perimeter and area of the triangle respectively.
The valur of $\frac{c \sin B+b \sin C}{x}+\frac{a \sin C+c \sin A}{y}+\frac{b \sin A+a \sin B}{z}$ is equal to
A. $\frac{R}{r}$
B. $\frac{S}{R}$
C. 2
D. 6

## Answer: D

21. $A L, B M$ and $C N$ are perpendicular from angular points of a triangle $A B C$ on the opposite sides $\mathrm{BC}, \mathrm{CA}$ and AB respectively. $\Delta$ is the area of triangle $A B C,(r)$ and $R$ are the inradius and circumradius.

If perimeters of $\Delta L M N$ and $\Delta A B C a n \lambda$ and $\mu$, then the value of $\frac{\lambda}{\mu}$ is
A. $\frac{r}{R}$
B. $\frac{R}{r}$
C. $\frac{r R}{\Delta}$
D. $\frac{\Delta}{r R}$

## Answer: B

## - Watch Video Solution

22. The angle of triangle $A, B, C$ are in $A P$ and $C=3 A$. Find angle $B$

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23. AL, BM and CN are perpendicular from angular points of a triangle $A B C$ on the opposite sides $B C, C A$ and $A B$ respectively. $\Delta$ is the area of triangle $A B C,(r)$ and $R$ are the inradius and circumradius. If area of $\Delta L M N$ is $\Delta^{\prime}$, then the value of $\frac{\Delta^{\prime}}{\Delta}$ is
A. $2 \sin A \sin B \sin C$
B. $2 \cos A \cos B \cos C$
C. $\sin A \sin B \sin C$
D. $\cos A \cos B \cos C$

## Answer: D

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24. AL, BM and CN are perpendicular from angular points of a triangle $A B C$ on the opposite sides $B C, C A$ and $A B$ respectively. $\Delta$ is the area of triangle $A B C,(r)$ and $R$ are the inradius and circumradius. Radius is the circum circle of $\triangle L M N$ is
A. 2 R
B. R
C. $\frac{R}{2}$
D. $\frac{R}{4}$

## Answer: B

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25. Differentiate the following w.r.t $x$
$\left(2 x^{2}-6 x+4\right)^{3}$

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PROPERTIES AND SOLUTIONS OF TRIANGLES EXERCISE 5: MATCHING TYPE QUESTIONS

1. Match the statement of Colume I with values of Column II.

## Column 1

Column II
(A) In a $\triangle A B C$, let $\angle C=\frac{\pi}{2}, r=$ inradius, $R=$ (p) $a+b+c$ circumradius then $2(r+R)$
(B) If $l, m, n$ are perpendicular drawn from $\quad$ (q) $a-b$ the vertices of triangle having sides $a, b$ and $c$ then
$\sqrt{2 R\left(\frac{b l}{c}+\frac{c m}{a}+\frac{a n}{b}\right)+2 a b+2 b c+2 c a}$
(C) In a $\triangle A B C, R\left(b^{2} \sin 2 C+c^{2} \sin 2 B\right)$
(r) $a+b$ equals
(D) In a right angle triangle $A B C, \angle C=\frac{\pi}{2}$, (s) $a b c$
then $4 R \sin \frac{A+B}{2} \sin \frac{(A-B)}{2}$

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2. Find the radian measure of the following degree measure $40^{\circ} 20^{\prime}$
3. Match the statement of Column I with values of Column II.

## Column I

Column II
(A) In a $\triangle A B C,(a+b+c)(b+c-a)=\lambda b c$, (p) 3 where $\lambda \in I$, then greatest value of $\lambda$ is
(B) In a $\triangle A B C, \tan A+\tan B+\tan C=9$. If (q) $9(3)^{1 / 3}$ $\tan ^{2} A+\tan ^{2} B+\tan ^{2} C=k$, then least
value of $k$ satisfying is
(C) In a triangle $A B C$, then line joining the (r) 1 circumcentre to the incentre is parallel to $B C$, then value of $\cos B+\cos C$ is
(D) If in a $\triangle A B C, a=5, b=4$ and (s) 6
$\cos (A-B)=\frac{31}{32}$, then the third side $c$ is equal to

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4. Find the radian measure corresponding to the degree measure $300^{\circ}$

## - Watch Video Solution

1. If in $\triangle A B C, \angle C=\frac{\pi}{8}, a=\sqrt{2}$ and $b=\sqrt{2+\sqrt{2}}$ then find the measure of angle $A$ (in degree).

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2. If in $A B C, A=\frac{\pi}{7}, B=\frac{2 \pi}{7}, C=\frac{4 \pi}{7}$ then $a^{2}+b^{2}+c^{2}$ must be (a) $R^{2}$ (b) $3 R^{2}$ (c) $4 R^{2}$ (d) $7 R^{2}$

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3. Find the radian measure corresponding to the following degree measure $15^{\circ}$

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4. The orthocenter of the triangle formed by $(0,0),(5,-1)$ and $(-2,3)$ is
A. (a) $(4,-7)$
B. (b) $(-4,7)$
C. (c) $(-4,-7)$
D. (d) none of above

## Answer: 4

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5. With usual notation in $\triangle A B C$, the numerical value of
$\left(\frac{a+b+c}{r_{1}+r_{2}+r_{3}}\right)\left(\frac{a}{r_{1}}+\frac{b}{r_{2}}+\frac{c}{r_{3}}\right)$ is

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6. $A B C$ is a triangle and $D$ is the middle point of $B C$. If $A D$ is perpendicular to AC , then prove that $\cos A \cdot \cos C=\frac{2\left(c^{2}-a^{2}\right)}{3 a c}$
7. The rational number which equals the number 2.357 with recurring decimal is $\frac{2355}{1001}$ b. $\frac{2379}{997}$ c. $\frac{2355}{999}$ d. none of these

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8. In triangle $A B C, r=\frac{R}{6}$ and $r_{1}=7 r$. Then the measure of angle $\mathrm{A}=$

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9. In a $\triangle A B C$, the maximum value of $120\left(\frac{\sum a \cos ^{2}\left(\frac{A}{2}\right)}{a+b+c}\right)$ must be

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10. The sides of a triangle are three consecutive natural numbers and its largest angle is twice the smalles one. Determine the largest and smallest sides of the triangle.

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11. In $\triangle A B C, \angle C=2 \angle A$, and $A C=2 B C$, then the value of $\frac{a^{2}+b^{2} c^{2}}{R^{2}}$ (where R is circumradius of triangle) is $\qquad$

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12. If a,b and A are given in a triangle and $C_{1}, C_{2}$ are the possible values of the third side, prove that : $C_{1}^{2}+C_{2}^{2}-2 C_{1} C_{2} \cos 2 A=4 a^{2} \cos ^{2} A$

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13. In $\triangle A B C, \mathrm{a}=5, \mathrm{~b}=4, \mathrm{c}=3$. G is the centroid of triangle. If $R_{1}$ be the circum radius of triangle GAB then the value of $\frac{a}{65} R_{1}^{2}$ must be

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14. A triangle $A B C$ is inscribed in a circle with centre at $O$, The lines $A O, B O a n d C O$ meet the opposite sides at $D, E$, and $F$, respectively. Prove that $\frac{1}{A D}+\frac{1}{B E}+\frac{1}{C F}=\frac{a \cos A+b \cos B+\mathrm{os} C}{\triangle}$

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15. In a triangle $A B C, a \geq b \geq c$. If
$\frac{a^{3}+b^{3}+c^{3}}{\sin ^{3} A+\sin ^{3} B+\sin ^{3} C}=8$, then the maximum value of $a$

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16. In a cyclic quadrilateral $P Q R S, P Q=2$ units, $Q R=5$ units, $R S=3$ units and $\angle P Q R=60^{\circ}$, then what is the measure of SP ?

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1. Find the value of trigonometric function $\cos \left(\frac{2 \pi}{3}\right)$

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## Exercise (Subjective Type Questions)

1. In a $\triangle A B C$, the angles A and B are two values of $\theta$ satisfying $\sqrt{3} \cos \theta+\sin \theta=k$, where $|K|<2$, then show triangles is obtuse angled.

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2. In an obtuse angled triangle, the obtuse angle is $\frac{3 \pi}{4}$ and the other two angles are equal to two values of $\theta$ satisfying
$a \tan \theta+b \sec \theta=c$, where $|b| \leq \sqrt{a^{2}+c^{2}}$, then $a^{2}-c^{2}$ is equal to

## - Watch Video Solution

3. If in trianlge $A B C, a, b, c$ and angle $A$ are given and $c \sin A<a<c$, then ( $b_{1}$ and $b_{2}$ are values of b )
A. (a) $b_{1}+b_{2}=2 c \cos A$
B. (b) $b_{1}+b_{2}=c \cos A$
C. (c) $b_{1} b_{2}=c^{2}-a^{2}$
D. (d) $b_{1} b_{2}=c^{2}+a^{2}$

Answer: $\sqrt{\frac{9 a^{2}-c^{2}}{8 c^{2}}}$

## - Watch Video Solution

4. If $P$ is a point on the altitude $A D$ of the triangle $A B C$ such the $\angle C B P=\frac{B}{3}$, then AP is equal to
5. If R denotes circumradius, then in $\triangle A B C, \frac{b^{2}-c^{2}}{2 a R}$ is equal to

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6. 

In
$\triangle A B C, A=\frac{2 \pi}{3}, b-c=3 \sqrt{3} \mathrm{~cm}$ and $\quad$ area of $\triangle A B C=\frac{9 \sqrt{3}}{2} \mathrm{~cm}^{2}$, then $\mathrm{a}=$

## - Watch Video Solution

7. If $\Delta=a^{2}-(b-c)^{2}, \Delta$ is the area of the $\Delta A B C$ then $\tan A=$ ?

## - Watch Video Solution

8. In a $\triangle A B C, B=90^{\circ}, A C=h$ and the length of perpendicular from B to AC is p such that $h=4 p$. If $A B<B C$, then measure $\angle C$.

## - Watch Video Solution

9. If in a $\triangle A B C, \sin ^{3} A+\sin ^{3} B+\sin ^{3} C$
$=3 \sin A \cdot \sin B \cdot \sin C$, then find the valueof determinant
$\left|\begin{array}{lll}a & b & c \\ b & c & a \\ c & a & b\end{array}\right|$.

## - Watch Video Solution

10. In $a$ triangle $A B C$, if the sides $a, b, c$, are roots of $x^{3}-11 x^{2}+38 x-40=0, \quad$ then find the value of $\frac{\cos A}{a}+\frac{\cos B}{b}+\frac{\cos C}{c}$

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11. If the sides $a, b, c$ are in A.P., prove that $(\tan ) \frac{A}{2}+(\tan ) \frac{c}{2}=\frac{2}{3}(\cot ) \frac{B}{2}$.
12. The sides of a triangle are in A.P. and its area is $\frac{3}{5}$ th of an equilateral triangle of the same perimeter. Find the greatest angle of the triangle

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13. If $\mathrm{AD}, \mathrm{BE}$ and CF are the medians of a $\triangle A B C$, then evaluate $\left(A D^{2}+B E^{2}+C F^{2}\right):\left(B C^{2}+C A^{2}+A B^{2}\right)$.

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14. Let AD be a median of the $\triangle A B C$.

If AE and AF are medians of the triangle ABD and ADC, respectively, and $B D=\frac{a}{2} A D=m_{1}, A E=m_{2}, A F=m_{3}$, then $\frac{a^{2}}{8}$ is equal to

## - Watch Video Solution

15. Find the radian measure corresponding to following degree measure $340^{\circ}$

## - Watch Video Solution

16. $\triangle A B C$ is equilateral triangle of side a . P lies on AB such that A is midpoint of PB. If $r_{1}$ is inradius of PAC and $r_{2}$ is ex radius of PBC opposite to P , then $r_{1}+r_{2}=$

## - Watch Video Solution

17. The base of a triangle is divided into three equal parts.

If $\theta_{1}, \theta_{2}, \theta_{3}$ be the angles subtended by these parts at the vertex, then prove that $\left(\cot \theta_{1}+\cot \theta_{2}\right)\left(\cot \theta_{2}+\cot \theta_{3}\right)=4 \operatorname{cosec}^{2} \theta_{2}$

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18. Find the value of $\sin \left(\frac{31 \pi}{3}\right)$

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19. If the angle at the vertex of an isosceles triangle having the maximum area for the given length of the median to one of its equal sides, is $x$ then $5 \cos x$ is equal to

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20. Find the value of trigonometric function $\sin \left(\frac{5 \pi}{3}\right)$

## - Watch Video Solution

21. Solve $\cos ^{2}(4 x)-\cos ^{2}(2 x)$
22. A hexagon is inscribed in a circle of radius $r$. Two of its sides have length 1, two have length 2 and the last two have length 3. Prove that $r$ is a root of the equation $2 r^{3}-7 r-3=0$.

## - Watch Video Solution

2. Prove that $a^{2}+b^{2}+c^{2}+2 a b c<2$, where $\mathrm{a}, \mathrm{b}, \mathrm{c}$ are the sides of triangle ABC such that $a+b+c=2$.

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3. Find the radian measure corresponding to the following degree measure $25^{\circ}$
4. A polygon of $n$ sides, inscribed in a circle, is such that its sides subtend angle $2 \alpha, 4 \alpha, \ldots, 2 n \alpha$ at the centre of the circles. Prove that its area $A_{1}$, is to the area $A_{2}$ of the regular polygon of n sides inscribed in the same circle, as $\sin n \alpha$ : $n \sin \alpha$.

## - Watch Video Solution

5. Find the radian measure corresponding to the following degree measure $50^{\circ}$

## - Watch Video Solution

6. Find the value of the trigonometric function $\sin \left(\frac{5 \pi}{6}\right)$
7. Find the radian measure of the following degree measure $75^{\circ}$

## - Watch Video Solution

8. If in a $\triangle A B C, \frac{a \cos A+b \cos B+c \cos C}{a \sin B+b \sin C+c \sin A}=\frac{a+b+c}{9 R}$, then prove that $\Delta$ is equilateral.

## - Watch Video Solution

9. In $\triangle A B C$, ' $h$ ' is the length of altitude drawn from vertex A on the side $B C$. Prove that:
$2\left(b^{2}+c^{2}\right) \geq 4 h^{2}+a^{2}$. Also, discuss the case when equality holds true.

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10. Find the value of other five trigonometric functions if $\cos x=-\frac{3}{5}, \mathrm{x}$ lies in third quadrant.

## Watch Video Solution

11. If in a $\triangle A B C, b=\sqrt{ } 3, c=1$ and $B-C=90 \circ$, then $\angle A$ is
A. (a) 30
B. (b) 60
C. (c) 90
D. (d) 120

## - Watch Video Solution

12. An equilateral triangle PQR is circumscribed about a given $\triangle A B C$.

Prove that the maximum area of $\triangle P Q R$ is $\left.2 \Delta+\frac{a^{2}+b^{2}+c^{2}}{2 \sqrt{3}}\right)$. Where
$\mathrm{a}, \mathrm{b}, \mathrm{c}$ are the sides of $\triangle A B C a n \Delta$ is its area.

## - Watch Video Solution

13. Find the other five trigonometric functions if $\cos x=\frac{4}{5}, \mathrm{x}$ lies in the fourth quadrant.

## - Watch Video Solution

14. Find the points inside a $\Delta$ from which the sum of the squares of distance to the three sides is minimum.

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15. In triangle $A B C$, line joining the circumcenter and orthocentre is parallel to side $A C$, then the value of $t$ a $n$ AtanCi se $q u a l l o s q r t(3)(b) 3$
(c) 3 sqrt(3) (d) none of these
16. Find the value of trigonometric function $\cot \left(\frac{-15 \pi}{4}\right)$

## - Watch Video Solution

17. Prove that $\sin ^{2}\left(30^{\circ}\right)+\cos ^{2}\left(60^{\circ}\right)-\tan ^{2}\left(45^{\circ}\right)=-\frac{1}{2}$

## - Watch Video Solution

18. Prove that $\frac{2 \cos ^{3} x-\cos x}{\sin x-2 \sin ^{3} x}=\cot x$

## - Watch Video Solution

## Exercise (Questions Asked In Previous 13 Years Exam)

1. Prove that $2 \sin ^{2}\left(\frac{\pi}{6}\right)-\sec ^{2}\left(\frac{\pi}{3}\right)=-\frac{7}{2}$
2. In a triangle the sum of two sides is $x$ and the product of the same is $y$. If $x^{2}-c^{2}=y$ where c is the third side. Determine the ration of the inradius and circum-radius
A. $\frac{3 y}{2 x(x+c)}$
B. $\frac{3 y}{2 c(x+c)}$
C. $\frac{3 y}{4 x(x+c)}$
D. $\frac{3 y}{4 c(x+c)}$

## Answer: B

## - Watch Video Solution

3. Consider a triangle $A B C$ and let $a, b$ and $c$ denote the lengths of the sides opposite to vertices $A, B$, and $C$, respectively. Suppose $a=6, b=10$, and the area of triangle is $15 \sqrt{3}$. If $\angle A C B$ is obtuse and
if $r$ denotes the radius of the incircle of the triangle, then the value of $r^{2}$ is

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4. Solution of differential equation $2 x y \frac{d y}{d x}=x^{2}+3 y^{2}$ is $\qquad$ .

## - Watch Video Solution

5. Let PQR be a triangle of area $\Delta$ with $a=2, b=7 / 2$, and $c=5 / 2$, where $\mathrm{a}, \mathrm{b}$ and c are the lengths of the sides of the triangle opposite to the angles at $\mathrm{P}, \mathrm{Q}$ and R , respectively. Then $\frac{2 \sin P-\sin 2 P}{2 \sin P+\sin 2 P}$ equals
A. $\frac{3}{4 D e t l a}$
B. $\frac{45}{4 \Delta}$
C. $\left(\frac{3}{4 \Delta}\right)^{2}$
D. $\left(\frac{45}{4 \Delta}\right)^{5}$

## D Watch Video Solution

6. If the angle $A, B a n d C$ of a triangle are in an arithmetic propression and if $a$, bandc denote the lengths of the sides opposite to $A, B a n d C$ respectively, then the value of the expression $\frac{a}{c} \sin 2 C+\frac{c}{a} \sin 2 A$ is (a) $\frac{1}{2}$ (b) $\frac{\sqrt{3}}{2}$ (c) 1 (d) $\sqrt{3}$
A. $\frac{1}{2}$
B. $\frac{\sqrt{3}}{2}$
C. 1
D. $\sqrt{3}$

## Answer: D

## - Watch Video Solution

7. Let $A B C$ be a triangle such that $\angle A C B=\frac{\pi}{6}$ and let $a, b$ and $c$ denote the lengths of the side opposite to $A, B$, and $C$ respectively. The value(s) of $x$ for which $a=x^{2}+x+1, b=x^{2}-1$, and $c=2 x+1$ is(are) $-(2+\sqrt{3})$ (b) $1+\sqrt{3}$ (c) $2+\sqrt{3}$ (d) $4 \sqrt{3}$
A. $-(2+\sqrt{3})$
B. $1+\sqrt{3}$
C. $2+\sqrt{3}$
D. $4 \sqrt{3}$

## Answer: B

## - Watch Video Solution

8. A triangle $A B C$ with fixed base $B C$, the vertex $A$ moves such that $\cos B+\cos C=4 \sin ^{2}\left(\frac{A}{2}\right)$. If $a, b$ and $c$, denote the length of the sides of the triangle opposite to the angles $A, B, a n d C$, respectively, then
(a) $b+c=4 a$
(b) $b+c=2 a$
(c)the locus of point $A$ is an ellipse
(d)the locus of point $A$ is a pair of straight lines
A. $b+c=4 a$
B. $b+c=2 a$
C. locus of point $A$ is an ellipes
D. locus of point $A$ is a pair of straight line

## Answer: B::C

## D Watch Video Solution

9. Let $A B C a n d A B C$ ' be two non-congruent triangles with sides $A B=4, A C=A C^{\prime}=2 \sqrt{2}$ and angle $B=30^{\circ}$. The absolute value of the difference between the areas of these triangles is
10. A straight line through the vertex $P$ of a triangle $P Q R$ intersects the side $Q R$ at the points $S$ and the cicumcircle of the triangle $P Q R$ at the point $T$. If $S$ is not the center of the circumcircle, then

$$
\begin{array}{ll}
\frac{1}{P S}+\frac{1}{S T}<\frac{2}{\sqrt{Q S \times S R}} & \frac{1}{P S}+\frac{1}{S T}>\frac{2}{\sqrt{Q S \times S R}} \\
\frac{1}{P S}+\frac{1}{S T}<\frac{4}{Q R} \frac{1}{P S}+\frac{1}{S T}>\frac{4}{Q R} &
\end{array}
$$

$$
\text { A. } \frac{1}{P S}+\frac{1}{S T}<\frac{2}{\sqrt{Q S \times S R}}
$$

$$
\text { B. } \frac{1}{P S}+\frac{1}{S T}>\frac{2}{\sqrt{Q S \times S R}}
$$

$$
\text { c. } \frac{1}{P S}+\frac{1}{S T}<\frac{4}{Q R}
$$

$$
\text { D. } \frac{1}{P S}+\frac{1}{S T}>\frac{4}{Q R}
$$

## Answer: D

## - Watch Video Solution

11. Consider the circle $x^{2}+y^{2}=9$ and the parabola $y^{2}=8 x$. They intersect at $P$ and $Q$ in first and fourth quadrant respectively. Tangents to the circle at $P$ and $Q$ intersect the $x$-axis at $R$ and tangents at the parabola
at $P$ and $Q$ intersect the $x$-axis at $S$. The radius of the circumcircle of the triangle PRS is-
A. 4
B. 3
C. $\frac{8}{3}$
D. 2

## Answer: B

## - Watch Video Solution

12. Consider the circle $x^{2}+y^{2}=9$ and the parabola $y^{2}=8 x$. They intersect at $P$ and $Q$ in first and fourth quadrant respectively. Tangents to the circle at $P$ and $Q$ intersect the $x$-axis at $R$ and tangents at the parabola at $P$ and $Q$ intersect the $x$-axis at $S$. The radius of the circumcircle of the triangle PRS is-
A. 5
B. $3 \sqrt{3}$
C. $3 \sqrt{2}$
D. $2 \sqrt{3}$

## Answer: B

## - Watch Video Solution

13. Consider the circle $x^{2}+y^{2}=9$ and the parabola $y^{2}=8 x$. They intersect at $P$ and $Q$ in first and fourth quadrant respectively. Tangents to the circle at $P$ and $Q$ intersect the $x$-axis at $R$ and tangents at the parabola at $P$ and $Q$ intersect the $x$-axis at $S$. The radius of the circumcircle of the triangle PRS is-
A. $1: \sqrt{2}$
B. 1:2
C. 1: 4
D. 1:8

## Answer: C

## - Watch Video Solution

14. Internal bisector of $\angle A$ of triangle ABC meets side BC at D . A line drawn through $D$ perpendicular to $A D$ intersects the side $A C$ at $E$ and the side AB at F . If $\mathrm{a}, \mathrm{b}, \mathrm{c}$ represent sides of $\triangle A B C$, then
A. AE is HM of $b$ and $a$
B. $A D=\frac{2 b c}{b+c} \cos \frac{A}{2}$
C. $E F=\frac{4 b c}{b+c} \sin \frac{A}{2}$
D. $\triangle A E F$ is isosceles

## Answer: A::B::C::D

## - Watch Video Solution

15. One angle of an isosceles triangle is $120^{\circ}$ and the radius of its incricle is $\sqrt{3}$. Then the area of the triangle in sq. units is
(a) $7+12 \sqrt{3}$
(b) $12-7 \sqrt{3}$
$12+7 \sqrt{3}$
(d) $4 \pi$
A. $4 \sqrt{3}$
B. $12-7 \sqrt{3}$
C. $12+7 \sqrt{3}$
D. None of the above

## Answer: C

## - Watch Video Solution

16. In $\triangle A B C$, which one is true among the following ?
A. $(b+c) \cos \frac{A}{2}=a \sin \left(\frac{B+C}{2}\right)$
B. $(b+c) \cos \left(\frac{B+C}{2}\right)=a \sin \frac{A}{2}$
C. $(b-c) \cos \left(\frac{B-C}{2}\right)=a \cos \left(\frac{A}{2}\right)$
D. $(b-c) \cos \frac{A}{2}=a \sin \left(\frac{B-C}{2}\right)$

## Answer: D

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17. Let a vertical tower $A B$ have its end $A$ on the level ground. Let $C$ be the mid point of $A B$ and $P$ be a point on the ground such that $A P=2 A B$. If $\angle B P C=\beta$, then $\tan \beta$ is equal to :
(1) $\frac{2}{9}$ (2) $\frac{4}{9}$ (3) $\frac{6}{7}$ (4) $\frac{1}{4}$
A. $\frac{6}{7}$
B. $\frac{1}{4}$
C. $\frac{2}{9}$
D. $\frac{4}{9}$
18. ABCD is a trapezium such that AB and CD are parallel and $B C \perp C D$. If $\angle A D B=\theta, B C=p$ and $C D=q$, then AB is equal to
(a) $\frac{\left(p^{2}+q^{2}\right) \sin \theta}{p \cos \theta+q \sin \theta}$
(b) $\frac{p^{2}+q^{2} \cos \theta}{p \cos \theta+q \sin \theta}$
(c) $\frac{p^{2}+q^{2}}{p^{2} \cos \theta+q^{2} \sin \theta}$
(d) $\frac{\left(p^{2}+q^{2}\right) \sin \theta}{(p \cos \theta+\sin \theta)^{2}}$
A. $\frac{\left(p^{2}+q^{2}\right) \sin \theta}{p \cos \theta+q \sin \theta}$
B. $\frac{p^{2}+q^{2} \cos \theta}{p \cos \theta+q \sin \theta}$
C. $\frac{p^{2}+q^{2}}{p^{2} \cos \theta+q^{2} \sin \theta}$
D. $\frac{\left(p^{2}+q^{2}\right) \sin \theta}{(p \cos \theta+\sin \theta)^{2}}$

## Answer: A

## D Watch Video Solution

19. For a regular polygon, let $r$ and $R$ be the radii of the inscribed and the cirumscribed circles, respectively. A false statement among the following is
(a)there is a regular polygon with $\frac{r}{R}=\frac{1}{2}$
(b)there is a regular polygon with $\frac{r}{R}=\frac{1}{\sqrt{2}}$
(c)there is a regular plygon with $\frac{r}{R}=\frac{2}{3}$
(d)there is a regular plygon with $\frac{r}{R}=\frac{\sqrt{3}}{2}$
A. there is a regular polygon with $\frac{r}{R}=\frac{1}{2}$
B. there is a regular polygon with $\frac{r}{R}=\frac{1}{\sqrt{2}}$
C. there is a regular plygon with $\frac{r}{R}=\frac{2}{3}$
D. there is a regular plygon with $\frac{r}{R}=\frac{\sqrt{3}}{2}$

Answer: A::B::D
20. In triangle $A B C$, let $\angle c=\frac{\pi}{2}$. If $r$ is the inradius and $R$ is circumradius of the triangle, then $2(r+R)$ is equal to
A. $c+a$
B. $a+b+c$
C. $a+b$
D. $b+c$

## Answer: A

## - Watch Video Solution

21. If in a $\triangle A B C$, the altitudes from the vertices $\mathrm{A}, \mathrm{B}, \mathrm{C}$ on opposite sides are in H.P, then $\sin A, \sin B, \sin C$ are in
A. HP
B. AGP
C. AP
D. GP

## Answer: C

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