MATHS

BOOKS - ARIHANT MATHS

SEQUENCES AND SERIES

Examples

1. If $f: N \rightarrow R$, where $f(n)=a_n=\frac{n}{(2n+1)^2}$ write the sequence in ordered pair from.

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2. The Fibonacci sequence is defined by $1=a_1=a_2$ and $a_n=a_{n-1}+a_{n-2}, n>2$. Find $\frac{a_{n+1}}{a_n}$, for n = 1, 2, 3, 4, 5

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3. If the sum of n terms of a series is $2n^2 + 5n$ for all values of n, find its 7th term.

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4. (i) Write $\sum_{r=1}^{n} \left(r^2 + 2\right)$ in expanded form.

(ii) Write the series $\frac{1}{3} + \frac{2}{4} + \frac{3}{5} + \frac{4}{6} + \ldots + \frac{n}{n+2}$ in sigma form.

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5. Which of the following are A.P. (i) 1,3,5,7,...

(ii) $\pi, \pi + e^{\pi}, \pi + 2e^{\pi}, \ldots.$

(iii) $a, a - b, a - 2b, a - 3b, \ldots.$

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6. Show that the sequence t_n defined by $t_n = 5n + 4$ is AP, also find its common difference.

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7. Show that the the sequence defined by $T_n = 3n^2 + 2$ is not an AP.

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8. Which term of the sequence $20, \ 19\frac{1}{4}, \ 18\frac{1}{2}, \ 17\frac{3}{4}, \ \cdot$ is the first negative term?

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9. If mth term of an AP is 1/n and its nth term is 1/m , then show that its (mn)th term is 1

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10. If $|x-1|, 3$ and $|x-3|$ are first three terms of an increasing AP, then find the 6th term of on AP .

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11. In the sequence 1,2,2,3,3,3,4,4,4,4, ... , where n consecutive terms have the value n, the 150th term, is

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12. Let $a_1, a_2, a_3, \ldots\ldots a_{10}$ are in GP with $a_{51} = 25$ and $\sum_{i=1}^{101} a_i = 125$ than the value of $\sum_{i=1}^{101} \left(\frac{1}{a_i}\right)$ equals.

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13. The ratio of the sums of m and n terms of an A.P. is $m^2 : n^2$. Show that the ratio of m^{th} and n^{th} term is (2m - 1) : (2n -1).

A. $(2m+1):(2n-1)$,

B. $m:n$

C. $(2m-1):(2n-1)$

D. None of these

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14. The sums of n terms of two arithmetic progresssions are in the ratio $(7n+1):(4n+17)$. Find the ratio of their mth terms.

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15. The sums of n terms of two AP's are in the ratio $(3n - 13) : (5n + 21)$. Find the ratio of their 24th terms.

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16. How many terms of the A.P. $20, 19\frac{1}{3}, 18\frac{2}{3},$ .... must be taken so that their sum is 300?

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17. If the arithmetic progression whose common difference is non-zero, the sum of first 3n terms isequal to the sum of the next n terms . The ratio of the next 2n terms is

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18. If the set of natural numbers is partitioned into subsets $S_1 = \{1\}, S_2 = \{2, 3\}, S_3 = \{4, 5, 6\}$ and so on then find the sum of the terms in S_{50}.

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19. Find the sum of first 24 terms of on AP $t_1, t_2, t_3, \ldots.,$ if it is known that $t_1 + t_5 + t_{10} + t_{15} + t_{20} + t_{24} = 225.$

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20. Solve $\int 2\cot^2 x\, dx$

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21. If S_1, S_2, S_3, S_m are the sums of n terms of m A.P. $'s$ whose first terms are $1, 2, 3, \ldots. m$ and common differences are $1, 3, 5, \ldots. (2m-1)$

respectively. Show that $S_1 + S_2.... + S_m = \frac{mn}{2}(mn+1)$

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22. Let α and β be roots of the equation $X^2 - 2x + A = 0$ and let γ and δ be the roots of the equation $X^2 - 18x + B = 0$. If $\alpha < \beta < \gamma < \delta$ are in arithmetic progression then find the valus of A and B.

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23. The digits of a positive integer, having three digits, are in A.P. and their sum is 15. The number obtained by reversing the digits is 594 less than the original number. Find the number.

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24. If a,b,c and d are four positive real numbers such that abcd=1 , what is the minimum value of $(1+a)(1+b)(1+c)(1+d)$.

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25. If a,b,c,d are distinct integers in an A.P. such that $d = a^2 + b^2 + c^2$, then find the value of a+b+c+d.

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26. Find the sum of the following APs :- 2, 7, 12, ... to 10 terms.

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27. $9, 3, 1, \frac{1}{3}, \frac{1}{9}, \dots$

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28. Find the 5th and nth term of sequence -2,-6,-18,....

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29. What is the sum of this series upto infinite terms $-8, \ -4, \ -2, \ -1, \ -\frac{1}{2}, \ldots$

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30. Find the nth and 5th term of sequence $5, \ -10, 20, \ldots.$

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31. Find the sum of series to n terms $5, 5, 5, 5, \ldots..$

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32. $1, 1+i, 2i, \ -2+2i, \ldots.where i = \sqrt{-1}$

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33. Show that the sequence t_n defined by $t_n = \frac{2^{2n-1}}{3}$ for all values of $n \in N$ is a GP. Also, find its common ratio.

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34. Show that the sequence t_n defined by $t_n = 2 \cdot 3^n + 1$ is not a GP.

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35. If first term of a GP is a, third term is b and $(n+1)th$ term is c. The $(2n+1)th$ term of a GP is

A. $c\sqrt{\frac{b}{a}}$

B. $\frac{bc}{a}$

C. abc

D. $\frac{c^2}{a}$

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36. In a GP if the $(m+n)th$ term is p and $(m-n)th$ term is q then mth term is

A. $p\left(\frac{q}{p}\right)^{\frac{m}{2n}}$

B. $\sqrt{pq}$

C. $\sqrt{\frac{p}{q}}$

D. None of these

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37. If $\sin\theta, \sqrt{2}(\sin\theta+1), 6\sin\theta+6$ are in GP, than the fifth term is

A. 81

B. $81\sqrt{2}$

C. 162

D. $162\sqrt{2}$

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38. The 1025th term in the sequence are $1, 22, 4444, 88888888, \ldots$ is

A. 2^9

B. 2^{10}

C. 2^{11}

D. 2^{12}

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39. If a, b, c are real numbers such that $3(a^2 + b^2 + c^2 + 1) = 2(a + b + c + ab + bc + ca)$, than a, b, c are in

A. AP only

B. GP only

C. GP and AP

D. None of these

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40. Find the value of $0.32\overline{58}$

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41. Find the sum upto n terms of the series $1 + 4 + 7 + 10 + 13 + 16 + \ldots\ldots$

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42. Find the sum of the series upto n terms

$0.\ b + 0.\ bb + 0.\ bbb + 0.\ bbbb + \ldots\ldots, \forall\ \ \text{b} \in N\ \ \text{and}\ \ 1 \leq b \leq 9.$

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43. If N, the set of natural numbers is partitionaed into groups $S_1 = \{1\}, S_2 = \{2, 3\}, S_3 = \{4, 5, 6\}, \ldots.$ find the sum of the numbers n C_{50}.

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44. If $S_n = 1 + \frac{1}{2} + \frac{1}{2^2} + \ldots + \frac{1}{2^{n-1}}$ and $2 - S_n < \frac{1}{100}$, then the least value of n must be :

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45. What is $\int \sin x \cos x dx$ equal to

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46. If $\frac{1+3p}{3}, \frac{1-p}{4}$ and $\frac{1-2p}{2}$ are the probabilities of the three mutually exclusive events, the p $\in$

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47. If x_1, x_2 be the roots of the equation $x^2 - 3x + A = 0$ and x_3, x_4 be those of the equation $x^2 - 12x + B = 0$ and x_1, x_2, x_3, x_4 be an increasing GP. find find A and B.

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48. Suppose a, b, c are in AP and a^2, b^2, c^2 are in GP, If $a > b > c$ and $a + b + c = \frac{3}{2}$, than find the values of a and c.

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49. If the continued product of three numbers in GP is 216 and the sum of their products in pairs is 156, then find the sum of three numbers.

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50. Find a three digit numberwhose consecutive digits form a GP. If we subtract 792 from this number, we get a number consisting of the same digits written in the reverse order. Now, if we increase the second digit of the required number by 2, then the resulting digits will form an AP.

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51. A square is drawn by joining mid pint of the sides of a square. Another square is drawn inside the second square in the same way and the process is continued in definitely. If the side of the first square is 16 cm, then what is the sum of the areas of all the squares ?

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52. One side of an equilateral triangle is 24 cm. The midpoints of its sides are joined to form another triangle whose midpoints are in turn joined to form still another triangle this process continues indefinitely. The sum of the perimeters of all the triangles is

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53. Let $S_1, S_2,$ be squares such that for each $n \geq 1,$ the length of a side of S_n equals the length of a diagonal of S_{n+1}. If the length of a side of S_1 is $10cm,$ then the least value of n is the area of S_n less than 1 sq. cm?

A. a. 5

B. b. 8

C. c. 9

D. d.10

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54. Find the surface area of a sphere of radius : 28cm

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55. Dipesh writes letters to four of his friends. He asks each of them to copy the letter and mail to four different persons with the request that they continue the chain similarly. Assuming that the chain is not broken and that it costs 25 paise to mail one letter, find the total money spent on postage till the 8th set of letters is mailed.

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56. An insect starts from a point and travels in a straight path 1 mm in the first second and half of the distance covered in the previous second in the succeeding second. In how much time would it reach a point 3 mm away from its starting point.

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57. Solve $\int (2x^2 + e^x)\, dx$

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58. If a, b, c are in HP, then $\frac{a-b}{b-c}$ is equal to

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59. Find the first term of a HP whpse secpmd ter, os $\frac{5}{4}$ and the third term is $\frac{1}{2}$.

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60. If $\frac{1}{a} + \frac{1}{a-b} + \frac{1}{c} + \frac{1}{c-b} = 0$ and $a + c - b \neq 0$, then prove that a, b, c are in H.P.

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61. $3, x, 9$ are in $A.P.$ Find the value of x

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62. Find $\frac{dy}{dx}$ if function is $\sin x \cos x$

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63. If pth, qth and rth terms of a HP be respectivelya, b and c, has prove that $(q-r)bc+(r-p)ca+(p-q)ab=0.$

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64. If $a, b, c,$ are in AP, a^2, b^2, c^2 are in HP, then prove that either $a=b=c$ or $a, b, -\frac{c}{2}$ from a GP (2003, 4M)

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65. Integrate $\int \frac{1}{1+x^2} dx$ for limit [0,1]

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66. Find the value of $\int 2x \cos\left(x^2 - 5\right) dx$

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67. If three positive numbers a, b and c are in AP, GP and HP as well, than find their values.

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68. If a, b, c are in AP and p is the AM between a and b and q is the AM between b and c, then show that b is the AM between p and q.

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69. Find the value of n so that $\frac{a^{n+1}+b^{n+1}}{a^n+b^n}$ may be the geometric mean between a and b.

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70. There are n AM's between 3 and 54.Such that the 8th mean and $(n-2)$th mean is 3 ratio 5. Find n.

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71. If 11 AM's are inserted between 28 and 10, than find the three middle terms in the series.

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72. If a, b, c are in AP, than show that $a^2(b+c)+b^2(c+a)+c^2(a+b)=\frac{2}{9}(a+b+c)^3$.

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73. If a is the A.M. of b and c and the two geometric means are G_1 and G_2, then prove that $G_1^3 + G_2^3 = 2abc$

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74. If one G.M., G and two A.M's p and q be inserted between two given numbers, prove that

$G^2 = (2p - q)(2q - p)$

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75. Solve $\int \cos x + x \, dx$

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76. Insert five geimetrec means between $\frac{1}{3}$ and 9 and verify that their product is the fifth power of the geometric mean between $\frac{1}{3}$ and 9.

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77. AM between two numbers whose sum is 100 is ti the GM as 5:4`, find the numbers.

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78. If $a_1, a_2, a_3, \ldots. a_n$ are positive real numbers whose product is a fixed number c, then the minimum value of $a_1 + a_2 + \ldots. + a_{n-1} + 3a_n$ is

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79. If 9 harmonic means be inserted between 2 and 3, then the value of $A + \frac{6}{H} + 5$ (where A is any of the AM's and H is the corresponding HM), is

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80. IF $a_1, a_2, a_3, \ldots.a_{10}$ be in AP and $h_1, h_2, h_3, \ldots.h_{10}$ be in HP. If $a_1 = h_1 = 2$ and $a_{10} = h_{10} = 3$, then find value of $a_4 h_7$.

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81. Find n, so that $\frac{a^{n+1} + b^{n+1}}{a^n + b^n}(a \neq b)$ be HM beween a and b.

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82. Insert 6 harmonic means between 3 and $\frac{6}{23}$

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83. If $A^x = G^y = H^z$, where A, G, H are AM,GM and HM between two given quantities, then prove that x, y, z are in HP.

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84. The harmonic mean of two numbers is 4. Their arithmetic mean A and the geometric mean G satisfy the relation $2A + G^2 = 27$. Find two numbers.

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85. If the geometric mea is $\frac{1}{n}$ times the harmonic mean between two numbers, then show that the ratio of the two numbers is $1 + \sqrt{1 - n^2} : 1 - \sqrt{1 - n^2}$.

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86. Find $\frac{dy}{dx}$ if $f(x) = x^2e^x$

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87. Evaluate $\int \frac{\cos(\ln(x))}{x}dx$

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88. If a, b, c, d be four distinct positive quantities in GP,then show that

(a) $a+d > b+c$

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89. If a, b, c, d be four distinct positive quantities in HP, then

(a) $a+d > b+c$

(b)$ad > bc$

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90. Find the sum of the series $1 + \frac{4}{5} + \frac{7}{5^2} + \frac{10}{5^3} + \ldots..$

(ii) to infinity.

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91. The sum to infinity of the series

$1 + 2\left(1 - \frac{1}{n}\right) + 3\left(1 - \frac{1}{n}\right)^2 + \ldots\ldots\ldots,$ is (A)n^2 (B)$n(n+1)$ (C) $n\left(1 + \frac{1}{n}\right)^2$ (D)None of these

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92. If the sum to infinity of the series $1 + 4x + 7x^2 + 10x^3 + \ldots\ldots\ldots\ldots$ is $\frac{35}{16}$ then $x =$ (A) $\frac{1}{5}$ (B) $\frac{2}{5}$ (C) $\frac{3}{7}$ (D) $\frac{1}{7}$

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93. Evaluate $\int \frac{2x+3}{x^2+3x+2}dx$

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94. Find the sum of the series $1^2 + 3^2 + 5^2 + \rightarrow n$ terms.

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95. Find the sum of n terms of the series $1.\ 2^2 + 2.\ 3^2 + 3.\ 4^2 +$

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96. Find the sum of n terms of the series whose nth terms is

(i) $n(n-1)(n+1)$.

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97. Find the sum of n terms of the series whose nth terms is

(ii) $n^2 + 3^n$.

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98. Find the sum of the series $\frac{1^3}{1} + \frac{1^3 + 2^3}{1 + 3} + \frac{1^3 + 2^3 + 3^3}{1 + 3 + 5} +$ up to n terms.

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99. Show that $S_n = \frac{n(2n^2 + 9n + 13)}{24}$.

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100. Find the sum of n terms of the series $1.\ 2.\ 3 + 2.\ 3.\ 4 + 3.\ 4.\ 5 +$

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101. Find sum to n terms of the series $1+(2+3)+(4+5+6)+\ldots..$

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102. Find the sum of the series $1\cdot n+2\cdot(n-1)+3\cdot(n-2)+4\cdot(n-3)+\ldots+(n-1)\cdot 2+n\cdot 1$ also, find the coefficient of x^{n-1} in th cxpansion of $\left(1+2x+3x^2+\ldots.nx^{n-1}\right)^2$.

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103. Find the nth term and sum to n tems of the following series: 1+5+12+22+..............

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104. Find the sum upto n terms of the series $1 + 4 + 7 + 10 + 13 + 16 + \ldots..$

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105. Find the nth term of the series $2 + 5 + 12 + 31 + 86 + \ldots.$

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106. Find the nth term of the series $1 + 5 + 18 + 58 + 179 + \ldots.$

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107. Find the nth term and sum of n terms of the series $5 + 7 + 13 + 31 + 85 + \ldots.$

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108. Find the sum of the following series to n terms $5 + 7 + 13 + 31 + 85 +$

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109. Find the nth term of the series $2 + 5 + 12 + 31 + 86 + \ldots.$

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110. Find the nth term of the series $2 + 5 + 12 + 31 + 86 + \ldots.$

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111. Find the nth term and sum to n terms of the series $12 + 40 + 90 + 168 + 280 + 432 + \ldots..$

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112. Find the sum upto n terms of the series

$1 + 4 + 7 + 10 + 13 + 16 + \ldots..$

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113. Find the sum to n terms of the series $\frac{1}{1 \cdot 3 \cdot 5 \cdot 7 \cdot 9} + \frac{1}{3 \cdot 5 \cdot 7 \cdot 9 \cdot 11} + \frac{1}{5 \cdot 7 \cdot 9 \cdot 11 \cdot 13} + \ldots\ldots.$ Also, find the sum to infinty terms.

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114. If $\sum_{r=1}^{n} T_r = \frac{n(n+1)(n+2)(n+3)}{12}$ where T_r denotes the rth term of the series. Find $\lim_{n \to \infty} \sum_{r=1}^{n} \frac{1}{T_r}$.

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115. If $yz + zx + xy = 12$, where x,y,z` are positive values find the greatest value of xyz.

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116. Find the greatest value of x^3y^4 if $2x + 3y = 7$ and $x \geq 0, y \geq 0$.

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117. Find the least value of $3x + 4y$ for positive values of x and y, dubject to the condition $x^2y^3 = 6.$

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118. The minimum value of $P = bcx + cay + abz$, when $xyz = abc$, is

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119. If a, b, c are positive real numbers such that $a+b+c=1$, then prove that $\frac{a}{b+c}+\frac{b}{c+a}+\frac{c}{a+b} \geq \frac{3}{2}$

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120. If a + b = 1, a $>$ 0, prove that $\left(a+\frac{1}{a}\right)^2+\left(b+\frac{1}{b}\right)^2 \geq \frac{25}{2}$

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121. If $b-c, 2b-\lambda, b-a$ are in HP, then $a-\frac{\lambda}{2}, b-\frac{\lambda}{2}, c-\frac{\lambda}{2}$ are in

A. AP

B. GP

C. HP

D. None of these

Answer: B

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122. Let $a_1, a_2, a_3, \ldots\ldots a_{10}$ are in GP with $a_{51} = 25$ and $\sum_{i=1}^{101} a_i = 125$ than the value of $\sum_{i=1}^{101}\left(\frac{1}{a_i}\right)$ equals.

A. 5

B. $\frac{1}{5}$

C. $\frac{1}{25}$

D. $\frac{1}{125}$

Answer: B

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123. If $x = 111\ldots.(20 digits), y = 333\ldots.(10 digits)$ and $z = 222\ldots..2(10 digits), th$

equals.

A. $\frac{1}{2}$

B. 1

C. 2

D. 4

Answer: B

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124. Consider the sequence $1, 2, 2, 3, 3, 3, \ldots\ldots,$ where n occurs n times then the number at 2007th term is

A. 61

B. 62

C. 63

D. 64

Answer: C

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125. Let $S=\sum_{r=1}^{117}\frac{1}{2\left[\sqrt{r}\right]+1}$, when $[\cdot]$ denites the greatest integer function and if $S=\frac{p}{q}$, when p and q are co-primes, the value of $p+q$ is

A. 20

B. 76

C. 19

D. 69

Answer: B

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126. If a,b,c are non-zero real numbers, then the minimum value of the expression $\frac{\left(a^8+4a^4+1\right)\left(b^4+3b^2+1\right)\left(c^2+2c+2\right)}{a^4b^2}$ equals

A. 12

B. 24

C. 30

D. 60

Answer: C

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127. If the sum of m consecutive odd integers is m^4 , then the first integer is

A. $m^3 + m + 1$

B. $m^3 + m - 1$

C. $m^3 - m - 1$

D. $m^3 - m + 1$

Answer: D

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128. $\sum_{r=1}^{\infty} \frac{(4r+5)5^{-r}}{r(5r+5)}$

A. $\frac{1}{5}$

B. $\frac{2}{5}$

C. $\frac{1}{25}$

D. $\frac{2}{25}$

Answer: A

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129. Let λ be the greatest integer for which $5p^2 - 16, 2p\lambda, \lambda^2$ are jdistinct consecutive terms of an AP, where $p \in R$. If the common difference of the Ap is $\left(\frac{m}{n}\right), n \in N$ and m ,n are relative prime, the value of $m + n$ is

A. 133

B. 138

C. 143

D. 148

Answer: C

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130. If $2\lambda, \lambda$ and $\left[\lambda^2 - 14\right], \lambda \in R - \{0\}$ and $[\cdot]$ denotes the gratest integer function are the first three terms of a GP in order, then the 51th term of the sequence, $1, 3\lambda, 6\lambda, 10\lambda, \ldots.,$ is

A. 5104

B. 5304

C. 5504

D. 5704

Answer: B

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131. The first three terms of a sequence are $3, \ -1, \ -1$. The next terms are

A. 2

B. -3

C. $-\frac{5}{27}$

D. $-\frac{5}{9}$

Answer: B

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132. There are two numbers a and b whose product is 192 and the quotient of AM by HM of their greatest common divisor and least common multiple is `(169)/(48). The smaller of a and b is

A. 2

B. 4

C. 6

D. 12

Answer: B::D

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133. Evaluate $\int \left(2x^2 + \cos x + e^x\right) dx$

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134. If $S_r = \sqrt{r + \sqrt{r + \sqrt{r + \sqrt{......\infty}}}}, r > 0$ then which the following is\are correct.

A. $S_2, S_6, S_{12}, S_{20},$ are in AP

B. S_4, S_9, S_{16} are irrational

C. $(2S_2 - 1)^2, (2S_3 - 1)^2, (2S_4 - 1)^2$ are in AP

D. all of these

Answer: A::B::C::D

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135. If $\frac{1}{a}, \frac{1}{b}, \frac{1}{c}$ are in A.P and a,b -2c, are in G.P where a,b,c are non-zero then

A. $a^3 + b^3 + c^3 = 3abc$

B. $-2a, b, -2c$ are in AP

C. $-2a, b, -2c$ are inGP

D. $a^2, b^2, 4c^2$ are in GP

Answer: A::B::D

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136. The nature of the $S_n = 3n^2 + 5n$ series is

A. AP

B. GP

C. HP

D. AGP

Answer: A

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137. For the $S_n = 3n^2 + 5n$ sequence, the number 5456 is the

A. 153th term

B. 932th term

C. 707th term

D. 909th term

Answer: D

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138. Consider a sequence whose sum to n terms is given by the quadratic function Sn= 3(n^2) +5n. Then sum of the squares of the first 3 terms of the given series is

A. 1100

B. 660

C. 799

D. 1000

Answer: B

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139. Find the number of terms common to the two A.P. s : $3, 7, 11, 407 and 2, 9, 16, , 709.$

A. 14

B. 21

C. 28

D. 35

Answer: A

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140. The 10th common terms between the series $3 + 7 + 11 + ...$ And $1 + 6 + 11 + ...$ is

(i) 191

(ii) 193

(iii) 211

(iv) None of these

A. 189

B. 191

C. 211

D. 213

Answer: B

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141. The largest term common to the sequence 1,11,21,31,....to 100 terms and 31,36,41,46,...... to 100 tetms is

A. 281

B. 381

C. 471

D. 521

Answer: D

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142. If $x > 0, y > 0, z > 0$ and $x + y + z = 1$ then the minimum value of $\frac{x}{2-x} + \frac{y}{2-y} + \frac{z}{2-z}$ is:

a. 0.2

b. 0.4

c. 0.6

d. 0.8

A. (a) 0.2

B. (b) 0.4

C. (c) 0.6

D. (d) 0.8

Answer: C

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143. If $\sum_{i=1}^{n} a_i^2 = \lambda, \forall a_i \geq 0$ and if greatest and least values of $\left(\sum_{i=1}^{n} a_i\right)^2$ are λ_1 and λ_2 respectively, then $(\lambda_1 - \lambda_2)$ is

A. $n\lambda$

B. $(n-1)\lambda$

C. $(n+2)\lambda$

D. $(n+1)\lambda$

Answer: B

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144. If sum of the mth powers of first n odd numbers is λ, $Aam > 1$, then

(A)$\lambda < n^m$ (B)$\lambda > n^m$ (C)$\lambda < n^{m+1}$ (D)$\lambda > n^{m+1}$

A. $\lambda < n^m$

B. $\lambda > n^m$

C. $\lambda < n^{m+1}$

D. $\lambda > n^{m+1}$

Answer: D

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145. A squence of positive terms $A_1, A_2, A_3, ..., A_n$ satisfies the relation $A_{n+1} = \frac{3(1+A_n)}{(3+A_n)}$. Least integeral value of A_1 for which the sequence is decreasing can be

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146. When the ninth term of an AP is divided by its second term we get 5 as the quotient, when the thirteenth term ia devided ny sixth term the quotient is 2 and the remainderis 5, then the seonnd term is

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147. Match the following Column I to Column II

	Column I		Column II
(A)	If $a_1, a_2, a_3, \dots$ are in AP and $a_1 + a_6 + a_{10} + a_{21} + a_{25} + a_{30} = 120$, then $\sum_{i=1}^{30} a_i$ is	(p)	400
(B)	If $a_1, a_2, a_3, \dots$ are in AP and $a_1 + a_5 + a_9 + a_{13} + a_{17} + a_{21} + a_{25} = 112$, then $\sum_{i=1}^{25} a_i$ is	(q)	600
(C)	If $a_1, a_2, a_3, \dots$ are in AP and $a_1 + a_4 + a_7 + a_{10} + a_{13} + a_{16} = 375$, then $\sum_{i=1}^{16} a_i$ is	(r)	800
		(s)	1000

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148. Evaluate $\int_0^{\frac{\pi}{2}} \cos x \, dx$

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149. Statement 1 The sum of first n terms of the series $1^2 - 2^2 + 3^2 - 4^2 \_ 5^2 - \dots\dots$ can be $= \pm \frac{n(n+1)}{2}$. Statement 2 Sum of first n narural numbers is $\frac{n(n+1)}{2}$

A. Statement 1 is true, Statement 2 is true, Statement 2 is a corrct explanation for Statement 1.

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct explanation for Statement 1.

C. Statement 1 is true, Statement 2 is false.

D. Statement 1 is false, Statement 2 is true.

Answer: A

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150. Statement 1 If a,b,c are three positive numbers in GP, then $\left(\frac{a+b+c}{3}\right)\left(\frac{3abc}{ab+bc+ca}\right)=(abc)^{\frac{2}{3}}$.

Statement 2 $(AM)(HM)=(GM)^2$ is true for positive numbers.

A. Statement 1 is true, Statement 2 is true, Statement 2 is a corrct explanation for Statement 1.

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct explanation for Statement 1.

C. Statement 1 is true, Statement 2 is false.

D. Statement 1 is false, Statement 2 is true.

Answer: C

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151. Consider an AP with a as the first term and d is the common difference such that S_n denotes the sum to n terms and a_n denotes the nth term of the AP. Given that for some m,$n \in N$, $\frac{S_m}{S_n} = \frac{m^2}{n^2}(\neq n)$.

Statement 1 $d = 2a$ because

Statement 2 $\frac{a_m}{a_n} = \frac{2m+1}{2n+1}$.

A. Statement 1 is true, Statement 2 is true, Statement 2 is a corrct explanation for Statement 1.

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct explanation for Statement 1.

C. Statement 1 is true, Statement 2 is false.

D. Statement 1 is false, Statement 2 is true.

Answer: C

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152. Statement 1 $1, 2, 4, 8, \ldots..$ is a GP,$4, 8, 16, 32, \ldots.$ is a GP and $1+4, 2+8, 4+16, 8+32, \ldots.$ is also a GP. Statement 2 Let general term of a GP with common ratio r be T_{k+1} and general term of another GP with common ratio r be T'_{k+1}, then the series whode general term $T''_{k+1} = T_{k+1} + T'_{k+1}$ is also a GP woth common ratio r.

A. Statement 1 is true, Statement 2 is true, Statement 2 is a corrct explanation for Statement 1.

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct explanation for Statement 1.

C. Statement 1 is true, Statement 2 is false.

D. Statement 1 is false, Statement 2 is true.

Answer: A

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153. In a set of four numbers, the first three are in G.P. and the last three are in A.P. with difference 6. If the first number is the same as the fourth, find the four numbers.

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154. Find the natural number a for which $\sum_{k=1}^{n} f(a+k) = 16(2^n - 1)$, where the function f satisfies the relation $f(x+y) = f(x)f(y)$ for all natural number $x, yand, further, f(1) = 2$.

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155. If 9 harmonic means be inserted between 2 and 3, then the value of $A+\frac{6}{H}+5$ (where A is any of the AM's and H is the corresponding HM), is

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156. A number consists of three digits which are in GP the sum of the right hand and left hand digits exceeds twice the middle digits by 1 and the sum of the left hand and middle digits is two thirds of the sum of the middle and right hand digits. Find the number.

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157. $S=\sum_{i=1}^{n}\sum_{j=1}^{i}\sum_{k=1}^{j}1$

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158. Three numbers are in G.P. whose sum is 70. If the extremes be each multiplied by 4 and the means by 5, they will be in A.P. Find the numbers.

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159. If the sum of m terms of an A.P. is equal to the sum of either the next n terms or the next p terms, then prove that $(m+n)\left(\frac{1}{m}-\frac{1}{p}\right)=(m+p)\left(\frac{1}{m}-\frac{1}{n}\right)$.

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160. Find the sum of all possible products of the first n natural numbers taken two by two.

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161. If $l_n = \int_0^{\frac{\pi}{4}} \tan^n x dx$ show that $\frac{1}{l_2 + l_4}, \frac{1}{l_3 + l_5}, \frac{1}{l_4 + l_6}, \frac{1}{l_5 + l_7}, \ldots.$ from an AP. Find its common difference.

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162. If the sum of the terms of an infinitely decreasing GP is equal to the greatest value of the fuction $f(x) = x^3 + 3x - 9$ on the iterval $[-5, 3]$ and the difference between the first and second terms is $f'(0)$, then show that the common ratio of the progression is $\frac{2}{3}$.

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163. Find the relation between x and y: $\log_{10} x + \frac{1}{2}\log_{10} x + \frac{1}{4}\log_{10} x + \ldots. = y$

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164. If $0 < x < \frac{\pi}{2}$ exp $\left[\left(\sin^2 x + \sin^4 x + \sin^6 x + ' \ldots . + \infty\right)\log_e 2\right]$ satisfies the quadratic equation $x^2 - 9x + 8 = 0$, find the value of $\frac{\sin x - \cos x}{\sin x + \cos x}$.

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165. The natural numbers arearranged innthe form given below

1

2 3

4 5 6 7

8 9 10 11 12 13 14 15

....

....

The rth group containing 2^{r-1} numbers. Prove that sum of the numbers in the nth group is $2^{n-2}\left[2^n + 2^{n-1} - 1\right]$.

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166. If a,b,c are in HP, then prove that $\frac{a+b}{2a-b} + \frac{c+b}{2c-b} > 4$.

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167. Find the sum to n terms of the series

$$\frac{1}{1+1^2+1^4}+\frac{2}{1+2^2+2^4}+\frac{3}{1+3^2+3^4}+\ldots.$$

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168. The value of xyz is 55 or $\frac{343}{55}$ according as the series a, x, y, z, b is an AP or HP. Find the values of a and b given that they are positive integers.

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169. Find the sum of first n terms of the series $1^3+3\times2^2+3^3+3\times4^2+5^3+3\times6^2+ when\, n$ is even n is odd

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170. Find out the largest term of the sequence $\frac{1}{503}, \frac{4}{524}, \frac{9}{581}, \frac{16}{692}, \ldots.$

.

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171. IF $f(r)=1+\frac{1}{2}+\frac{1}{3}+\ldots.+\frac{1}{r}$ and $f(0)=0$, find $\sum_{r=1}^{n}(2r+1)f(r)$.

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172. If the equation $x^4-4x^3+ax^2+bx+1=0$ has four positive roots, find the values of a and b.

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173. Evaluate $\sum_{m=1}^{\infty}\sum_{n=1}^{\infty}\frac{m^2n}{3^m(n\cdot 3^m+m\cdot 3^n)}$.

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174. The value of $\sum_{i=0}^{\infty}\sum_{j=0}^{\infty}\sum_{k=0}^{\infty}\frac{1}{3^i 3^j 3^k}$ is

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175. If area of rectangle is $120m^2$ and lenght is $12m$ then find the value of breath

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176. The nth term of a series is given by $t_n = \frac{n^5+n^3}{n^4+n^2+1}$ and if sum of its n terms can be expressed as $S_n = a_n^2 + a + \frac{1}{b_n^2 + b}$ where a_n and b_n are the nth terms of some arithmetic progressions and a, b are some constants, prove that $\frac{b_n}{a_n}$ is a costant.

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Exercise For Session 1

1. First term of a sequence is 1 and the $(n+1)th$ term is obtained by adding $(n+1)$ to the nth term for all natural numbers n, the 6th term of the sequence is

A. 7

B. 13

C. 21

D. 27

Answer: C

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2. The first three terms of a sequence are $3, 3, 6$ and each term after the sum of two terms preceding it, then the $8th$ term of the sequence

A. 15

B. 24

C. 39

D. 63

Answer: D

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3. If $a_n = \sin\left(\frac{n\pi}{6}\right)$ then the value of $\sum_{n=2}^{6} a_n^2$

A. 2

B. 3

C. 4

D. 7

Answer: B

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4. If for a sequence $\{a_n\}$, $S_n = 2n^2 + 9n$, where S_n is the sum of n terms, the value of a_{20} is

A. 65

B. 75

C. 87

D. 97

Answer: C

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5. If $a_1 = 2$ and $a_n = 2a_{n-1} + 5$ for $n > 1$, the value of $\sum_{r=2}^{5} a_r$ is

A. 130

B. 160

C. 190

D. 220

Answer: C

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Exercise For Session 2

1. If nth term of the series $25 + 29 + 33 + 37......$ and $3 + 4 + 6 + 9 + 13 + ...$ are equal, then n equal

A. 11

B. 12

C. 13

D. 14

Answer: B

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2. The rth term of the series $2\left(\frac{1}{2}\right)+1\left(\frac{7}{13}\right)+1\left(\frac{1}{9}\right)+\frac{20}{23}+\ldots.$ is

A. $\frac{20}{5r+3}$

B. $\frac{20}{5r-3}$

C. $20(5r+3)$

D. $\frac{20}{5r^2+3}$

Answer: A

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3. In a certain A.P., 5 times the 5th term is equal to 8 times the 8th terms then find its 13th term.

A. 0

B. -1

C. -12

D. -13

Answer: A

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4. If 9th term of an A.P. is zero, prove that its 29th term is double the 19th term.

A. $1:2$

B. $2:1$

C. $1:3$

D. $3:1$

Answer: B

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5. If the cost of the 10 pens is Rs.180, calculate the cost of 2 pens

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6. The $6th$ term of an AP is equal to 2, the value of the common difference of the AP which makes the product $a_1a_4a_5$ least is given by

A. $\frac{8}{5}$

B. $\frac{5}{4}$

C. $\frac{2}{3}$

D. $\frac{1}{3}$

Answer: C

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7. The sum of first $2n$ terms of an AP is α. and the sum of next n terms is β, its common difference is

A. $\dfrac{\alpha - 2\beta}{3n^2}$

B. $\dfrac{2\beta - \alpha}{3n^2}$

C. $\dfrac{\alpha - 2\beta}{3n}$

D. $\dfrac{2\beta - \alpha}{3n}$

Answer: B

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8. The sum of three numbers in AP is -3 and their product is 8, then sum of squares of the numbers is

A. 9

B. 10

C. 12

D. 21

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9. Let S_n denote the sum of first n terms of an AP and $3S_n = S_{2n}$ What is $S_{3n} : S_n$ equal to? What is $S_{3n} : S_{2n}$ equal to?

A. (a) 9

B. (b) 6

C. (c) 16

D. (d) 12

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10. Find the sum of the products of the ten numbers $\pm 1, \pm 2, \pm 3, \pm 4, \text{ and } \pm 5$ taking two at a time.

A. -65

B. 165

C. -55

D. 95

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11. If $a_1, a_2, a_3, \ldots., a_n$ are in AP, where $a_i > 0$ for all I, the value of $\frac{1}{\sqrt{a_1}+\sqrt{a_2}}+\frac{1}{\sqrt{a_2}+\sqrt{a_3}}+\ldots..+\frac{1}{\sqrt{a_{n-1}}+\sqrt{a_n}}$ is

A. $\frac{1}{\sqrt{a_1}+\sqrt{a_n}}$

B. $\frac{1}{\sqrt{a_1}-\sqrt{a_n}}$

C. $\frac{n}{\sqrt{a_1}-\sqrt{a_n}}$

D. $\frac{n-1}{\sqrt{a_1}+\sqrt{a_n}}$

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Exercise For Session 3

1. The fourth, seventh, and the last term of a G.P. are 10, 80, and 2560, respectively. Find the first term and the number of terms in G.P.

A. $\frac{4}{5}, 12$

B. $\frac{4}{5}, 10$

C. $\frac{5}{4}, 12$

D. $\frac{5}{4}, 10$

Answer: B

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2. If the first and the n^{th}term of a GP are a and b, respectively, and if P is the product of n terms, prove that $P^2 = (ab)^n$.

A. ab

B. $(ab)^{\frac{n}{2}}$

C. $(ab)^n$

D. None of these

Answer: C

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3. If $a_1, a_2, a_3(a_1 > 0)$ are three successive terms of a GP with common ratio r, the value of r for which $a_3 > 4a_2 - 3a_1$ holds is given by

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4. If $x, 2x+2$ and $3x+3$ are the first three terms of a G.P., then the fourth term is

A. 27

B. -27

C. 13.5

D. -13.5

Answer: C

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5. In a sequence of 21 terms the first 11 terms are in A.P. with common difference 2. and the last 11 terms are in G.P. with common ratio 2. If the middle tem of the A.P. is equal to the middle term of the G.P., then the middle term of the entire sequence is

A. $-\frac{10}{31}$

B. $\frac{10}{31}$

C. $-\frac{32}{31}$

D. $\frac{32}{31}$

Answer: D

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6. Three distinct numbers x,y,z form a GP in that order and the numbers $7x + 5y, 7y + 5z, 7z + 5x$ form an AP in that order. The common ratio of GP is

A. -4

B. -2

C. 10

D. 18

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7. Prove that the sum to n terms of the series 11 + 103 + 1005 + ... Is (10/9) $(10^n - 1) + n^2$.

A. $\frac{1}{9}(10^n - 1) + n^2$

B. $\frac{1}{9}(10^n - 1) + 2n$

C. $\frac{10}{9}(10^n - 1) + n^2$

D. $\frac{10}{9}(10^n - 1) + 2n$

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8. In a G.P the sum of the first and last terms is 66, the product of the second and the second last term is 128, and the sum of the terms is 126 If the decresing G.P is considered , then find the number of terms

A. 6

B. 8

C. 10

D. 12

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9. If S_1, S_2, S_3be respectively the sum of n, 2n and 3n terms of a GP, then $\frac{S_1(S_3 - S_2)}{(S_2 - S_1)^2}$ is equal to

A. (a) 1

B. (b) 2

C. (c) 3

D. (d) 4

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10. If $|a| < 1|b| < 1$ and $|x| < 1$ then the solution of $\sin^{-1}\left(\frac{2a}{1+a^2}\right) - \cos^{-1}\left(\frac{1-b^2}{1+b^2}\right) = \tan^{-1}\left(\frac{2x}{1-x^2}\right)$ is

A. $\frac{a-b}{1-ab}$

B. $\frac{a-b}{1+ab}$

C. $\frac{ab-1}{1+ab}$

D. none of these

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11. If the sides of a triangle are in GP and its largest angle is twice tha smallset then the common ratio r satisfies the inequality

A. $0 < r < \sqrt{2}$

B. $1 < r < \sqrt{2}$

C. $1 < r < 2$

D. $r > \sqrt{2}$

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12. If $ax^3 + bx^2 + cx + d$ is divisible by $ax^2 + c, then a, b, c, d$ are in a. A.P. b. G.P. c. H.P. d. none of these

A. AP

B. GP

C. HP

D. None of these

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13. If $(r)_n$, denotes the number $rrr...(ndigits)$, where $r = 1, 2, 3, ..., 9$ and $a = (6)_n, b = (8)_n, c = (4)_{2n}$, then

A. $a^2 + b + c = 0$

B. $a^2 + b - c = 0$

C. $a^2 + b2c = 0$

D. $a^2 + b - 9c = 0$

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14. $0.4\overline{27}$ represents the rational number

A. $\frac{47}{99}$

B. $\frac{47}{110}$

C. $\frac{47}{999}$

D. $\frac{49}{99}$

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15. If the product of three numbers in GP be 216 and their sum is 19, then the numbers are

A. $4, 6, 9$

B. $4, 7, 8$

C. $3, 7, 9$

D. None of these

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Exercise For Session 4

1. Find $\frac{dy}{dx}$ of $3x^3 + e^x + 4$

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2. If a,b,c are in AP, then $\frac{a}{bc}, \frac{1}{c}, \frac{1}{b}$ are in

A. AP

B. GP

C. HP

D. None of these

Answer: C

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3. Find the value of $\int x^2 dx$

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4. If $x, 1, z$ are in AP and $x, 2, z$ are in GP, then $x, 4, z$ will be in (a) AP (b) GP (c) HP (d) None Of These

A. AP

B. GP

C. HP

D. None of these

Answer: D

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5. If a, b, c are in G.P. and $a - b, c - a, and b - c$ are in H.P., then prove that $a + 4b + c$ is equal to 0.

A. 0

B. 1

C. -1

D. None of these

Answer: A

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6. If the $(m + 1)th, (n + 1)th, and (r + 1)th$ terms of an A.P., are in G.P. and m, n, r are in H.P., then find the value of the ratio of the common difference to the first term of the A.P.

A. $-\frac{2}{n}$

B. $\frac{2}{n}$

C. $-\frac{n}{2}$

D. $\frac{n}{2}$

Answer: A

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7. If a,b,c are in AP and a^2, b^2, c^2 are in HP, then

A. $a = b = c$

B. $2b = 3a + c$

C. $b^2 = \sqrt{\frac{ac}{8}}$

D. None of these

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8. If a, b, c are in HP., then $\frac{a}{b+c}, \frac{b}{c+a}, \frac{c}{a+b}$ are in

A. AP

B. GP

C. HP

D. None of these

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9. If $\frac{x+y}{2}, y, \frac{y+z}{2}$ are in HP, then x,y, z are in

A. AP

B. GP

C. HP

D. None of these

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10. if $\frac{a+b}{1-ab}, b, \frac{b+c}{1-bc}$ are in AP then $a, \frac{1}{b}, c$ are in

A. AP

B. GP

C. HP

D. None of these

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Exercise For Session 5

1. If the arithmetic means of two positive number a and b $(a > b)$ is twice their geometric mean, then find the ratio a: b

A. $2+\sqrt{3}:2-\sqrt{3}$

B. $7+4\sqrt{3}:7-4\sqrt{3}$

C. $2:7+4\sqrt{3}$

D. $2 : \sqrt{3}$

Answer: C

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2. Let α and β be two positive real numbers. Suppose A_1, A_2 are two arithmetic means; G_1, G_2 are tow geometrie means and $H_1 H_2$ are two harmonic means between α and β, then

A. $A_1 H_2$

B. $A_2 H_1$

C. $G_1 G_2$

D. None of these

Answer: A

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3. The geometric mean between -9 and -16 is

A. 12

B. -12

C. -13

D. None of these

Answer: A

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4. Let $n \in N, n > 25$. Let A, G, H deonote te arithmetic mean, geometric man, and harmonic mean of 25 and n. The least value of n for which $A, G, H \in \{25, 26.... . n\}$ is

A. 49

B. 81

C. 169

D. 225

Answer: C

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5. If nine arithmetic means and nine harmonic means are inserted between 2 and 3 alternatively, then prove that $A+6/H=5$ (where A is any of the A.M.'s and H the corresponding H.M.).

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6. If $H_1.,H_2,\ldots,H_{20}$ are 20 harmonic means between 2 and 3, then $\frac{H_1+2}{H_1-2}+\frac{H_{20}+3}{H_{20}-3}=$

A. n

B. $n+1$

C. 2n

D. $2n - 2$

Answer: B

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7. The A.M. of two given positive numbers is 2. If the larger number is increased by 1, the G.M. of the numbers becomes equal to the A.M. of the given numbers. Then find the H.M.

A. $\frac{3}{2}$

B. $\frac{2}{3}$

C. $\frac{1}{2}$

D. 2

Answer: B

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8. If $a, a_1, a_2, a_3, a_{2n}, b$ are in A.P. and $a, g_1, g_2, g_3, , g_{2n}, b$. are in G.P. and h s the H.M. of $a and b$, then prove that $\frac{a_1 + a_{2n}}{g_1 g_{2n}} + \frac{a_2 + a_{2n-1}}{g_1 g_{2n-1}} + + \frac{a_n + a_{n+1}}{g_n g_{n+1}} = \frac{2n}{h}$

A. $\frac{2n}{h}$

B. 2nh

C. nh

D. $\frac{n}{h}$

Answer: B

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Exercise For Session 6

1. Sum of the first n terms of the series $\frac{1}{2} + \frac{3}{4} + \frac{7}{8} + \frac{15}{16} + \ldots\ldots\ldots$ is equals to (a).$2^n + n - 1$ (b). $n - 1 + 2^{-n}$ (c). $n + 2^{-n} - 1$ (d). $2^n + 1$

A. $2^n + n - 1$

B. $1 - 2^{-n}$

C. $n + 26(-n) - 1$

D. $26(n) - 1$

Answer: B

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2. Find the value of x of equation $x^2 = 16$

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3. Sum to n terms the series $1 + 3 + 5 + 7 + 9 + \dots$

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4. 99^{th} term of the series $2 + 7 + 14 + 23 \dots$

A. 9998

B. 9999

C. 10000

D. 100000

Answer: C

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5. Find the sum of the series $1 \cdot 2 \cdot 3 + 2 \cdot 3 \cdot 4 + 3 \cdot 4 \cdot 5 + \ldots.$ upto n terms .

A. $n(n+1)(n+2)$

B. $(n+1)(n+2)(n+3)$

C. $\frac{1}{4}n(n+1)(n+2)(n+3)$

D. $\frac{1}{4}(n+1)(n+2)(n+3)$

Answer: A

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6. Find the sum of n terms of the series: $\frac{1}{1.2}+\frac{1}{2.3}+\frac{1}{3.4}+\dot{+}$ 1/n $(n\dot{+}1)$

A. $\frac{1}{n(n+1)}$

B. $\frac{n}{n+1}$

C. $\frac{2n}{n+1}$

D. $\frac{2}{n(n+1)}$

Answer: B

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7. Sum of the n terms of the series $\frac{3}{1^2}+\frac{5}{1^2+2^2}+\frac{7}{1^2+2^2+3^3}+\ldots\ldots$ is

A. $\frac{2n}{n+1}$

B. $\dfrac{4n}{n+1}$

C. $\dfrac{6n}{n+1}$

D. $\dfrac{9n}{n+1}$

Answer: A

Watch Video Solution

8. If $t_n = \dfrac{1}{4}(n+2)(n+3)$ for $n = 1, 2, 3, ,$ then $\dfrac{1}{t_1} + \dfrac{1}{t_2} + \dfrac{1}{t_3} + + \dfrac{1}{t_{2003}} =$

A. $\dfrac{4006}{3006}$

B. $\dfrac{4003}{3007}$

C. $\dfrac{4006}{3008}$

D. $\dfrac{4006}{3009}$

Answer: C

Watch Video Solution

9. The value of $(0.16)^{\log 2.5}\left\{\frac{1}{3}+\frac{1}{3^2}+...\right\}$ is

A. A. $\frac{1}{1+a}$

B. B. $\frac{2}{1+a}$

C. C. ∞

D. D. None of these

Answer: B

Watch Video Solution

10. If f is a function satisfying $f(x+y)=f(x)\times f(y)$ for all $x, y \in N$ such that $f(1)=3$ and $\sum_{x=1}^{n} f(x)=120,$ find the value of n .

A. 4

B. 5

C. 6

D. None of these

Answer: C

Watch Video Solution

Exercise For Session 7

1. The minimum value of $4^{x} + 4^{2-x}, x \in R$ is

A. 0

B. 2

C. 4

D. 8

Answer: A

Watch Video Solution

2. If $0 < x < \frac{\pi}{2}$, then the minimum value of $2(\sin x + \cos x + \cos ec2x)^3$ is

A. 0

B. 2

C. 4

D. 8

Answer: C

Watch Video Solution

3. If a,b,c and d are four real numbers of the same sign, then the value of $\frac{a}{b} + \frac{b}{c} + \frac{c}{d} + \frac{d}{a}$ lies in the interval

A. $[2, \infty)$

B. $[3, \infty)$

C. $[4, \infty)$

D. $(4, \infty)$

Answer: B

Watch Video Solution

4. If $0 < x < \frac{\pi}{2}$, then the minimum value of $2(\sin x + \cos x + \cos ec2x)^3$ is

A. (a) 27

B. (b) 13.5

C. (c) 6.75

D. (d) 0

Answer: D

Watch Video Solution

5. If $a+b+c=3$ and $a>0, b>0, c>0$ then the greatest value of $a^2b^3c^2$ is

A. $\frac{3^4 \cdot 2^{10}}{7^7}$

B. $\frac{3^{10} \cdot 2^4}{7^7}$

C. $\frac{3^2 \cdot 2^{12}}{7^7}$

D. $\frac{3^{12} \cdot 2^2}{7^7}$

Answer: C

Watch Video Solution

6. If $x+y+z=a$ and the minimum value of $\frac{a}{x}+\frac{a}{y}+\frac{a}{z}$ is 81^{λ}, then the value of . λ is

A. $\frac{1}{2}$

B. 1

C. $\frac{1}{4}$

D. 2

Answer: C

Watch Video Solution

7. If a, b, c be three positive numbers such that abc^2 has the greatest value $\frac{1}{64}$, then

A. $a = b = \frac{1}{2}, c = \frac{1}{4}$

B. $a = b = c = \frac{1}{3}$

C. $a = b = \frac{1}{4}, c = \frac{1}{2}$

D. $a = b = c = \frac{1}{4}$

Answer: A

Watch Video Solution

Exercise (Single Option Correct Type Questions)

1. If the number x,y,z are in H.P. , then $\frac{\sqrt{yz}}{\sqrt{y}+\sqrt{z}}, \frac{\sqrt{xz}}{\sqrt{x}+\sqrt{z}}, \frac{\sqrt{xy}}{\sqrt{x}+\sqrt{y}}$ are in

A. AP

B. GP

C. HP

D. None of these

Answer: A

Watch Video Solution

2. If $a_1, a_2, \ldots.,$ are in HP and $f_k = \sum_{r=1}^{n} a_r - a_k,$ then $2^{\alpha_1}, 2^{\alpha_2}, 2^{\alpha_3} 2^{\alpha_4}, \ldots..$ are in $\left\{ \text{where } \alpha_1 = \frac{a_1}{f_1}, \alpha_2 = \frac{a_2}{f_2}, \alpha_3 = \frac{a_3}{f_3}, \ldots.. \right\}.$

A. AP

B. GP

C. HP

D. None of these

Answer: D

Watch Video Solution

3. ABC is a right-angled triangle in which $\angle B = 90^\circ$ and $BC = a.$ If n points $L_1, L_2, \ldots, L_n$ on AB is divided in n+1 equal parts and $L_1M_1, L_2M_2, \ldots, L_nM_n$ are line segments paralllel to BC and $M_1, M_2, \ldots., M_n$ are on AC, then the sum of the lengths of $L_1M_1, L_2M_2, \ldots, L_nM_n$ is

A. $\frac{n(n+1)}{(2)}$

B. $\frac{a(n-1)}{2}$

C. $\frac{an}{2}$

D. Impossible to find from the given data

Answer: C

Watch Video Solution

4. Find the two-hundredth term a_{200} of the sequence: $2; 5; 8; 11.......$

Watch Video Solution

5. If a, b, c are in GP, show that the equations $ax^2 + 2bx + c = 0$ and $dx^2 + 2ex + f = 0$ have a common root if $\frac{a}{d}, \frac{b}{e}, \frac{c}{f}$ are in

A. AP

B. GP

C. HP

D. None of these

Answer: A

Watch Video Solution

6. Sum of the first n terms of the series $\frac{1}{2}+\frac{3}{4}+\frac{7}{8}+\frac{15}{16}+\ldots\ldots\ldots$ is equals to (a).2^n+n-1 (b). $n-1+2^{-n}$ (c). $n+2^{-n}-1$ (d). 2^n+1

A. 2^n+n-1

B. $1-2^{-n}$

C. $n+2^{-n}-1$

D. 2^n-1

Answer: C

Watch Video Solution

7. If in a triangle PQR; $\sin P, \sin Q, \sin R$ are in A.P; then (A)the altitudes are in AP (B)the altitudes are in HP (C)the altitudes are in GP (D)the medians are in AP

A. the altitudes are in AP

B. the altitudes are in HP

C. the medians are in GP

D. the medians are in AP

Answer: B

Watch Video Solution

8. Let $a_1, a_2, , a_{10}$ be in A.P. and h_1, h_2, h_{10} be in H.P. If $a_1 = h_1 = 2 and a_{10} = h_{10} = 3, then a_4 h_7$ is 2 b. 3 c. 5 d. 6

A. 2

B. 3

C. 5

D. 6

Answer: D

Watch Video Solution

9. If $I_n = \int_0^{\pi} \frac{1 - \sin 2nx}{1 - \cos 2x} dx$ then $I_1, I_2, I_3, \ldots$... are in

A. AP

B. GP

C. HP

D. None of these

Answer: A

Watch Video Solution

10. Find the value of λ the equation is $5x + y + \lambda = 0$ where $x = 1$ and $y = 5$

Watch Video Solution

11. The sum to infinity of the series

$1+2\left(1-\frac{1}{n}\right)+3\left(1-\frac{1}{n}\right)^2+\ldots\ldots,$ is (A)n^2 (B)$n(n+1)$ (C) $n\left(1+\frac{1}{n}\right)^2$ (D)None of these

A. n^2

B. $n(n+1)$

C. $n\left(1+\frac{1}{n}\right)^2$

D. None of these

Answer: A

Watch Video Solution

12. If $\log_3 2, \log_3(2^x-5)$ and $\log_3\left(2^x-\frac{7}{2}\right)$ are in A.P., then x is equal to

A. 2

B. 3

C. 4

D. $2, 3$

Answer: B

Watch Video Solution

13. If x,y,z be three positive prime numbers. The progression in which $\sqrt{x}, \sqrt{y}, \sqrt{z}$ can be three terms (not necessarily consecutive) is

A. AP

B. GP

C. HP

D. None of these

Answer: D

Watch Video Solution

14. If n is an odd integer greater than or equal to 1, then the value of

$n^3 - (n-1)^3 + (n-2)^3 - (n-3)^3 + ... + (-1)^{n-1}1^3$

A. $\dfrac{(n+1)^2(2n-1)}{4}$

B. $\dfrac{(n-1)^2(2n-1)}{4}$

C. $\dfrac{(n+1)^2(2n+1)}{4}$

D. None of these

Answer: A

Watch Video Solution

15. If the sides of a right angled triangle are in A.P then the sines of the acute angles are

A. $\dfrac{3}{5}, \dfrac{4}{5}$

B. $\sqrt{3}, \dfrac{1}{3}$

C. $\sqrt{\dfrac{\sqrt{5}-1}{2}}, \sqrt{\dfrac{\sqrt{5}+1}{2}}$

D. $\frac{\sqrt{3}}{2}, \frac{1}{2}$

Answer: A

Watch Video Solution

16. The $6th$ term of an AP is equal to 2. The value of the common difference of the AP which makes the product $a_1a_4a_5$ least is given by

A. $\frac{8}{5}$

B. $\frac{5}{4}$

C. $\frac{2}{3}$

D. None of these

Answer: C

Watch Video Solution

17. If the arithmetic progression whose common difference is nonzero the sum of first $3n$ terms is equal to the sum of next n terms. Then, find the ratio of the sum of the $2n$ terms to the sum of next $2n$ terms.

A. $\frac{1}{5}$

B. $\frac{2}{3}$

C. $\frac{3}{4}$

D. None of these

Answer: A

Watch Video Solution

18. The coefficient of x^n in the expansion of $(1+x)(1-x)^n$ is

A. $\frac{n\left(n^2+2\right)(3n+1)}{24}$

B. $\frac{n\left(n^2-1\right)(3n+2)}{24}$

C. $\frac{n\left(n^2+1\right)(3n+4)}{24}$

D. None of these

Answer: B

Watch Video Solution

19. Consider the pattern shown below:

$$\begin{array}{llllll} \text{Row} & 1 & 1 & & & \\ \text{Row} & 2 & 3 & 5 & & \\ \text{Row} & 3 & 7 & 9 & 11 & \\ \text{Row} & 4 & 13 & 15 & 17 & 19 \end{array} \quad etc.$$

The number at the end of row 60 is

A. 3659

B. 3519

C. 3681

D. 3731

Answer: A

Watch Video Solution

20. Let a_n be the nth term of an AP, if $\sum_{r=1}^{100} a_{2r} = \alpha$ and $\sum_{r=1}^{100} a_{2r-1} = \beta$, then the common difference of the AP is

A. (a) $\alpha - \beta$

B. (b) $\beta - \alpha$

C. (c) $\frac{\alpha - \beta}{100}$

D. (d) None of these

Answer: D

Watch Video Solution

21. If a_1, a_2, a_3, a_4, a_5 are in HP, then $a_1a_2 + a_2a_3 + a_3a_4 + a_4a_5$ is equal to

A. $2a_1a_5$

B. $3a_1a_5$

C. $4a_1a_5$

D. $6a_1a_5$

Answer: C

Watch Video Solution

22. If a,b,c and d are four positive real numbers such that abcd=1 , what is the minimum value of $(1+a)(1+b)(1+c)(1+d)$.

A. 1

B. 4

C. 16

D. 64

Answer: C

Watch Video Solution

23. If a,b,c are in AP and $(a+2b-c)(2b+c-a)(c+a-b)=\lambda abc$, then λ is

A. 1

B. 2

C. 4

D. None of these

Answer: C

Watch Video Solution

24. If $a_1, a_2, a_3.....$ are in GP with first term a and common ratio r, then $\frac{a_1a_2}{a_1^2-a_2^2}+\frac{a_2a_3}{a_2^2-a_3^2}+\frac{a_3a_4}{a_3^2-a_4^2}+.....+\frac{a_{n-1}a_n}{a_{n-1}^2-a_n^2}$ is equal to

A. $\frac{nr}{1-r^2}$

B. $\frac{(n-1)r}{1-r^2}$

C. $\frac{nr}{1-r}$

D. $\frac{(n-1)r}{1-r}$

Answer: B

Watch Video Solution

25. If the sum of first 10 terms of an A.P. is 4 times the sum of its first 5 terms, then find the ratio of first term and common difference.

A. $\frac{1}{2}$

B. 2

C. $\frac{1}{4}$

D. 4

Answer: A

Watch Video Solution

26. If $\cos(x-y)$, $\cos x$ and $\cos(x+y)$ are in H.P., then $\cos x \sec\left(\frac{y}{2}\right) is$

A. $\pm\sqrt{2}$

B. $\frac{1}{\sqrt{2}}$

C. $-\frac{1}{\sqrt{2}}$

D. None of these

Answer: A

Watch Video Solution

27. If 11 AM's are inserted between 28 and 10, than find the three middle terms in the series.

A. 5

B. 6

C. 7

D. 8

Answer: A

Watch Video Solution

28. If $x > 1, y > 1, and z > 1$ are in G.P., then $\frac{1}{1+\ln x}, \frac{1}{1+lny} and \frac{1}{1+lnz}$ are in a. $A\dot{P}.$ b. $H\dot{P}.$ c. $G\dot{P}.$ d. none of these

A. AP

B. GP

C. HP

D. None of these

Answer: C

Watch Video Solution

29. The minimum value of $\frac{(a^2+3a+1)(b^2+3b+1)(c^2+3c+1)}{abc}$ The minimum value of , where $a, b, c \in R^+$ is

A. $\frac{11^3}{2^3}$

B. 125

C. 25

D. 27

Answer: B

Watch Video Solution

30. Let $a_1, a_2, \ldots.$ be in AP and $q_1, q_2, \ldots.$ be in GP. If $a_1 = q_1 = 2$ and $a_{10} = q_{10} = 3$, then

A. $a_7 q_{19}$ is not an integer

B. $a_{19} q_7$ is an integer

C. $a_7 q_{19} = a_{19} q_{10}$

D. None of these

Answer: C

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Exercise (More Than One Correct Option Type Questions)

1. For a positive integer n let $a(n) = 1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \ldots. + \frac{1}{(2^n) - 1}$. Then

A. $a(100) < 100$

B. $a(100) > 100$

C. $a(200) > 100$

D. $a(200) < 100$

Answer: A::C

Watch Video Solution

2. The corresponding first and the (2n-1)th terms of an A.P a G.P and a H.P are equal ,If their nth terms are a, b and c , respectively , then

A. $a = b = c$

B. $a \geq b \geq c$

C. $a + c = b$

D. $ac - b^2 = 0$

Answer: B::D

Watch Video Solution

3. If $0 < \theta < \frac{\pi}{2}, x = \sum_{n=0}^{\infty} \cos^{2n}\theta, y = \sum_{n=0}^{\infty} \sin^{2n}\theta$ and $z = \sum_{n=0}^{\infty} \cos^{2n}\theta \cdot \sin^{2n}\theta$, then show $xyz = xy + z$.

A. $xyz = xz + y$

B. $xyz = xy + z$

C. $xyz = x + y + z$

D. $xyz = yz + x$

Answer: B::C

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4. If a,b,c are in A.P. and a^2, b^2, c^2 are in H.P. then which of the following could and true (A) $-\frac{a}{2}, b, care \in G.P.$ (B) $a = b = c$ (C) a^3, b^3, c^3 are in G.P. (D) none of these

A. $-\frac{a}{2}, b, c$ are in GP

B. $a = b = c$

C. a^2, b^2, c^2 are in GP

D. None of these

Answer: A::B

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5. The next term of the G.P. $x, x^2+2, and x^3+10$ is

A. 0

B. 6

C. $\frac{729}{16}$

D. 54

Answer: C::D

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6. Consecutive odd integers whose sum is 25^2-11^2 are

A. $n=14$

B. $n=16$

C. first odd number is 23

D. last odd number is 49

Answer: A::C::D

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7. The geometric mean G of two positive numbers is 6. Their arithmetic mean A and harmonic mean H satisfy the equation $90A + 5H = 918,$ then A may be equal to:

A. (A) $\frac{5}{2}$

B. (B) 10

C. (C) 5

D. (D) $\frac{1}{5}$

Answer: A::D

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8. If the sum to n terms of the series $\frac{1}{1\cdot3\cdot5\cdot7}+\frac{1}{3\cdot5\cdot7\cdot9}+\frac{1}{5\cdot7\cdot9\cdot11}+\ldots\ldots$ is $\frac{1}{90}-\frac{\lambda}{f(n)}$, then find $f(0)$, $f(1)$ and $f(\lambda)$

A. $f(0)=15$

B. $f(1)=105$

C. $f(\lambda)=\frac{640}{27}$

D. $\lambda=\frac{1}{3}$

Answer: A::B::C

Watch Video Solution

9. Find the value of λ the equation is $2x+3y+\lambda$ where $x=2$ and $y=1$

Watch Video Solution

10. Let $E = \frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} +$ Then,

A. $E < 3$

B. $E > \frac{3}{2}$

C. $E < 2$

D. $E > 2$

Answer: B::C

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11. Let $S_n (n \leq 1)$ be a sequence of sets defined by $S_1\{0\}, S_2 = \left\{\frac{3}{2}, \frac{5}{2}\right\}, S_3 = \left\{\frac{15}{4}, \frac{19}{4}, \frac{23}{4}, \frac{27}{4}\right\}, \ldots\ldots.$ then

A. (a)third element in S_{20} is $\frac{439}{20}$

B. (b)third element in S_{20} is $\frac{431}{20}$

C. (c)sum of the element inS_{20} is 589

D. (d)sum of the element inS_{20} is 609

Answer: A::C

Watch Video Solution

12. Find the sum of the sequence $-8, \ -5, \ -2, \ldots 7$

Watch Video Solution

13. Let a sequence$\{a_n\}$ be defined by $a_n = \frac{1}{n+1} + \frac{1}{n+2} + \frac{1}{n+3} + \ldots . + \frac{1}{3n}$. Then:

A. (a) $a_2 = \frac{11}{12}$

B. (b) $a_2 = \frac{19}{20}$

C. (c) $a_{n+1} - a_n = \frac{(9n+5)}{(3n+1)(3n+2)(3n+3)}$

D. (d) $a_{n+1} - a_n = \frac{-2}{3(n+1)}$

Answer: B::C

Watch Video Solution

14. Find $\frac{dy}{dx}$, if $y + \sin y = \cos x$

Watch Video Solution

15. All the terms of an AP are natural numbers and the sum of the first 20 terms is greater than 1072 and lss than 1162.If the sixth term is 32, then

A. first term is 7

B. first term is 12

C. common difference is 4

D. common difference is 5

Answer: A::D

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Exercise (Passage Based Questions)

1. Find the value of x of equation $4x^2 = 16$

Watch Video Solution

2. S_n be the sum of n terms of the series $\frac{8}{5} + \frac{16}{65} + \frac{24}{325} + \dots\dots$

The seveth term of the series is (a) $\frac{56}{2505}$ (b) $\frac{56}{6505}$ (c) $\frac{56}{5185}$ (d) $\frac{107}{9605}$

A. $\frac{56}{2505}$

B. $\frac{56}{6505}$

C. $\frac{56}{5185}$

D. $\frac{107}{9605}$

Answer: D

Watch Video Solution

3. S_n be the sum of n terms of the series $\frac{8}{5} + \frac{16}{65} + \frac{24}{325} + \dots\dots$

The value of S_8, is (a) $\frac{288}{145}$ (b) $\frac{1088}{545}$ (c) $\frac{81}{41}$ (d) $\frac{107}{245}$

A. $\frac{288}{145}$

B. $\frac{1088}{545}$

C. $\frac{81}{41}$

D. $\frac{107}{245}$

Answer: A

Watch Video Solution

4. If the sum of first n terms of a series is $(n + 12)$ then what is its third term?

Watch Video Solution

5. Find the value of $\int 2x^2 dx$

Watch Video Solution

6. Two consecutive numbers from 1,2,3 ...., n are removed .The arithmetic mean of the remaining numbers is 105/4

The sum of all numbers

A. less than 1000

B. lies between 1200 to 1500

C. greater than 1500

D. None of these

Answer: B

Watch Video Solution

7. There are two sets A and B each of which consists of three numbers in AP whose sum is 15 and where D and d are the common differences such that $D = 1 + d, d > 0$. If p=7(q-p)`, where p and q are the product of the nymbers respectively in the two series.

The value of p is

A. 105

B. 140

C. 175

D. 210

Answer: A

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8. There are two sets A and B each of which consists of three numbers in AP whose sum is 15 and where D and d are the common differences such that $D = 1 + d, d > 0$. If $p = 7(q - p)$, where p and q are the product of the nymbers respectively in the two series.

The value of q is

A. 200

B. 160

C. 120

D. 80

Answer: C

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9. There are two sets A and B each of which consists of three numbers in AP whose sum is 15 and where D and d are the common differences such that $D = 1 + d, d > 0$. If $p = 7(q - p)$, where p and q are the product of the nymbers respectively in the two series.

The value of $7D + 8d$ is

A. 37

B. 22

C. 67

D. 52

Answer: B

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10. There are two sets A and B each of which consists of three numbers in GP whose product is 64 and R and r are the common ratios sich that $R = r + 2$. If $\frac{p}{q} = \frac{3}{2}$, where p and q are sum of numbers taken two at a time respectively in the two sets.

The value of $r^R + R^r$ is

A. 66

B. 72

C. 78

D. 84

Answer: D

Watch Video Solution

11. Find the area of Rectangle Whose length is 7 m and breath is 5 m

A. 35

B. 56

C. 58

D. 60

Answer: B

Watch Video Solution

12. There are two sets A and B each of which consists of three numbers in GP whose product is 64 and R and r are the common ratios sich that $R = r + 2$. If $\frac{p}{q} = \frac{3}{2}$, where p and q are sum of numbers taken two at a time respectively in the two sets.

The value of $r^R + R^r$ is

A. 5392

B. 368

C. 32

D. 4

Answer: C

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13. The numbers $1, 3, 6, 10, 15, 21, 28...$ are called triangular numbers. Let t_n denote the n^{th} triangular number such that $t_n = t_{n-1} + n, \forall n \geq 2.$ The value of t_{50} is:

A. (a) 1075

B. (b) 1175

C. (c) 1275

D. (d) 1375

Answer: C

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14. The numbers $1, 3, 6, 10, 15, 21, 28...$ are called triangular numbers. Let t_n denote the n^{th} triangular number such that $t_n = t_{n-1} + n, \forall n \geq 2.$ The number of positive integers lying between t_{100} and t_{101} are:

A. (a) 99

B. (b) 100

C. (c) 101

D. (d) 102

Answer: B

Watch Video Solution

15. The numbers $1, 3, 6, 10, 15, 21, 28...$ are called triangular numbers. Let t_n denote the n^{th} triangular number such that $t_n = t_{n-1} + n, \forall n \geq 2.$ If $(m+1)$ is the n^{th} triangular number, then $(n-m)$ is

A. (a) $1 + \sqrt{(m^2 + 2m)}$

B. (b) $1 + \sqrt{(m^2 + 2)}$

C. (c) $1+\sqrt{(m^2+m)}$

D. (d) None of these

Answer: D

Watch Video Solution

16. Let $A_1, A_2, A_3, \ldots\ldots.A_m$ be arithmetic means between -3 and 828 and $G_1, G_2, G_3, \ldots\ldots.G_n$ be geometric means between 1 and 2187. Product of geometric means is 3^{35} and sum of arithmetic means is 14025. The value of n is

A. 45

B. 30

C. 25

D. 10

Answer: D

Watch Video Solution

Watch Video Solution

17. Let $A_1, A_2, A_3, ...A_m$ be arithmetic means between -3 and 828 and $G_1, G_2, G_3, ...G_n$ be geometric means between 1 and 2187. Product of geometric means is 3^{35} and sum of arithmetic means is 14025. The value of m is

A. 17

B. 34

C. 51

D. 68

Answer: B

Watch Video Solution

18. Let $A_1, A_2, A_3, ...A_m$ be arithmetic means between -3 and 828 and $G_1, G_2, G_3, ...G_n$ be geometric means between 1 and 2187.

Product of geometric means is 3^{35} and sum of arithmetic means is 14025.

The value of m is

A. 2044

B. 1022

C. 511

D. None of these

Answer: D

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19. Suppose α, β are roots of $ax^2 + bx + c = 0$ and γ, δ are roots of $Ax^2 + Bx + C = 0$.

If $\alpha, \beta, \gamma, \delta$ are in AP, then common difference of AP is

A. $\frac{1}{4}\left(\frac{b}{a} - \frac{B}{A}\right)$

B. $\frac{1}{3}\left(\frac{b}{a} - \frac{B}{A}\right)$

C. $\frac{1}{2}\left(\frac{c}{a} - \frac{B}{A}\right)$

D. $\frac{1}{3}\left(\frac{c}{a}-\frac{C}{A}\right)$

Answer: A

Watch Video Solution

20. Suppose α, β are roots of $ax^2+bx+c=0$ and γ, δ are roots of $Ax^2+Bx+C=0$. If a, b, c are in GP as well as $\alpha, \beta, \gamma, \delta$, then A, B, C are in:

A. (a) AP only

B. (b) GP only

C. (c) AP and GP

D. (d) None of these

Answer: B

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21. Suppose α, β are roots of $ax^2 + bx + c = 0$ and γ, δ are roots of $Ax^2 + Bx + C = 0$.

If $\alpha, \beta, \gamma, \delta$ are in GP, then common ratio of GP is

A. $\sqrt{\left(\frac{bA}{aB}\right)}$

B. $\sqrt{\left(\frac{aB}{bA}\right)}$

C. $\sqrt{\left(\frac{bC}{cB}\right)}$

D. $\sqrt{\left(\frac{cB}{bC}\right)}$

Answer: B

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22. Suppose p is the first of $n(n > 1)$ arithmetic means between two positive numbers a and b and q the first of n harmonic means between the same two numbers.

The value of p is

A. $\frac{na+b}{n+1}$

B. $\frac{nb+a}{n+1}$

C. $\frac{na-b}{n+1}$

D. $\frac{nb-a}{n+1}$

Answer: A

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23. Suppose p is the first of $n(n > 1)$ arithmetic means between two positive numbers a and b and q the first of n harmonic means between the same two numbers.

The value of q is

A. $\frac{(n-1)ab}{nb+a}$

B. $\frac{(n+1)ab}{nb+a}$

C. $\frac{(n-1)ab}{na+b}$

D. $\frac{(n-1)ab}{na+b}$

Answer: B

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24. The perimeter of a square is $96\ cm$. Find the area of the square.

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Exercise (Single Integer Answer Type Questions)

1. Let a, b, c, d be positive real numbers with $a < b < c < d$. Given that a, b, c, d are the first four terms of an AP and a, b, d are in GP. The value of $\frac{ad}{bc}$ is $\frac{p}{q}$, where p and q are prime numbers, then the value of q is ____

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2. If the coefficient of x in the expansion of $\prod_{r=1}^{110}(1+rx)$ is $\lambda(1+10)\left(1+10+10^2\right)$, then the value of λ is

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3. A 3 digit palindrome is a 3 digit number (not starting with zero) which reads the same backwards as forwards For example, 242. The sum of all even 3 digit palindromes is $2^{n_1}\cdot 3^{n_2}\cdot 5^{n_3}\cdot 7^{n_4}\cdot 11^{n_5}\cdot$ value of $n_1+n_2+n_3+n_4+n_5$ is

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4. If n is a positive integer satisfying the equation $2+\left(6\cdot 2^2-4\cdot 2\right)+\left(6\cdot 3^2-4\cdot 3\right)+\ldots\ldots+\left(6\cdot n^2-4\cdot n\right)=140$ then the value of n is

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5. Let $S(x) = 1 + x - x^2 - x^3 + x^4 + x^5 - x^6 - x^7 + \dots\dots.+\infty$, where $0 < x < 1$. If $S(x) = \frac{\sqrt{2}+1}{2}$, then the value of $(x+1)^2$ is

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6. The sequence $a_1, a_2, a_3, \dots\dots.,$ is a geometric sequence with common ratio r. The sequence $b_1, b_2, b_3, \dots\dots.,$ is also a geometric sequence. If $b_1 = 1, b_2 = \sqrt[4]{7} - \sqrt[4]{28} + 1, a_1 = \sqrt[4]{28}$ and $\sum_{n=1}^{\infty} \frac{1}{a_n} = \sum_{n=1}^{\infty} (b_n)$, then the value of $(1 + r^2 + r^4)$ is

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7. Let (a_1, b_1) and (a_2, b_2) are the pair of real numbers such that 10,a,b,ab constitute an arithmetic progression. Then, the value of $\left(\frac{2a_1a_2 + b_1b_2}{10}\right)$ is

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8. If one root of $Ax^3+Bx^2+Cx+D=0, D\neq 0$ is the arithmetic mean of the other two roots, then the relation $2B^3+\lambda ABC+\mu A^2D=0$ holds good. Then, the value of $2\lambda+\mu$ is

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9. If $|x|>1$,then sum of the series $\frac{1}{1+x}+\frac{2}{1+x^2}+\frac{2^2}{1+x^4}+\frac{2^3}{1+x^8}+\ldots\ldots \text{ upto terms } \infty$ is $\frac{1}{x-\lambda}$,then the value of λ is

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10. Three non-zero real numbers form a AP and the squares of these numbers taken in same order form a GP. If the possible common ratios are $(3\pm\sqrt{k})$ where $k\in N$, then the value of $\left[\frac{k}{8}-\frac{8}{k}\right]$ is (where [] denotes the greatest integer function).

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Exercise (Matching Type Questions)

1. Evaluate $\int_0^{\frac{\pi}{2}} \sin x \, dx$

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2. Find the area of Square whose side is 10 m

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3. Find the area of circle whose radius is 25 m

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Matching Type Questions

1. In Which quadrant Point $(2, \ -3)$ will be lie.

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Exercise (Statement I And Ii Type Questions)

1. Statement 1 $4, 8, 16,$ are in GP and 12,16,24 are in HP.

Statement 2 If middle term is added in three consecutive terms of a GP, resultant will be in HP.

A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct explanation for Statement 1

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct explanation for Statement 1

C. Statement 1 is true, Statement 2 is false

D. Statement 1 is false, Statement 2 is true

Answer: A

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2. Satement 1 If the nth termn of a series is $2n^3 + 3n^2 - 4$, then the second order differences must be an AP.

Statement 2 If nth term of a series is a polynomial of degree m, then mth order differences of series are constant.

A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct explanation for Statement 1

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct explanation for Statement 1

C. Statement 1 is true, Statement 2 is false

D. Statement 1 is false, Statement 2 is true

Answer: A

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3. Find the area of circle having radius $2m$

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4. Statement 1 $a+b+c=18(a, b, c>0)$, then the maximum value of abc is 216.

Statement 2 Maximum value occurs when $a=b=c$.

A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct explanation for Statement 1

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct explanation for Statement 1

C. Statement 1 is true, Statement 2 is false

D. Statement 1 is false, Statement 2 is true

Answer: A

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5. If $4a^2 + 9b^2 + 16c^2 = 2(3ab + 6bc + 4ca)$, where a,b,c are non-zero real numbers, then a,b,c are in GP.

Statement 2 If $(a_1 - a_2)^2 + (a_2 - a_3)^2 + (a_3 - a_1)^2 = 0$, then $a_1 = a_2 = a_3, \forall a_1, a_2, a_3 \in R$.

A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct explanation for Statement 1

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct explanation for Statement 1

C. Statement 1 is true, Statement 2 is false

D. Statement 1 is false, Statement 2 is true

Answer: D

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6. Statement 1 If a and b be two positive numbers, where $a > b$ and $4 \times GM = 5 \times HM$ for the numbers. Then, $a = 4b$.

Statement 2 $(AM)(HM) = (GM)^2$ is true for positive numbers.

A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct explanation for Statement 1

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct explanation for Statement 1

C. Statement 1 is true, Statement 2 is false

D. Statement 1 is false, Statement 2 is true

Answer: C

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7. Statement 1 The difference between the sum of the first 100 even natural numbers and the sum of the first 100 odd natural numbers is 100.

Statement 2 The difference between the sum opf the first n even natural numbers and sum of the first n odd natural numbers is n.

A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct explanation for Statement 1

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct explanation for Statement 1

C. Statement 1 is true, Statement 2 is false

D. Statement 1 is false, Statement 2 is true

Answer: A

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Exercise (Subjective Type Questions)

1. The pth, $(2p)th$ and $(4p)th$ terms of an AP, are in GP, then find the common ratio of GP.

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2. Find the sum of n terms of the series $(a+b)+(a^2+ab+b^2)+(a^3+a^2b+ab^2+b^3)+\ldots\ldots$ where $a \neq 1, b \neq 1$ and $a \neq b$.

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3. The sequence of odd natural numbers is divided into groups $1, 3, 5, 7, 9, 11, \ldots.$ and so on. Show that the sum of the numbers in nth group is n^3.

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4. The area of a square is $625\ cm$. Find the perimeter of the square.

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5. If the first four terms of an arithmetic sequence are $a, 2a, b$ and $(a-6-b)$ for some numbers a and b, find the sum of the first 100 terms of the sequence.

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6. If $\frac{1}{1^2}+\frac{1}{2^2}+\frac{1}{3^2}+\dots\infty=\frac{\pi^2}{6}$ then value of $1-\frac{1}{2^2}+\frac{1}{3^2}-\frac{1}{4^2}+\dots\infty=$

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7. If the arithmetic mean of $a_1, a_2, a_3, \dots\dots\dots a_n$ is a and $b_1, b_2, b_3, \dots\dots\dots b_n$ have the arithmetic mean b and $a_i+b_i=1$ for $i=1, 2, 3, \dots\dots n,$ prove that $\sum_{i=1}^{n}(a_i-a)^2+\sum_{i=1}^{n}a_ib_i=nab.$

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8. If $a_1, a_2, a_3, ...$ is an arithmetic progression with common difference 1 and $a_1 + a_2 + a_3 + ... + a_{98} = 137$, then find the value of $a_2 + a_4 + a_6 + ... + a_{98}$.

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9. If $t_1 = 1, t_r - t_{r-1} = 2^{r-1}, r \geq 2$, find $\sum_{r=1}^{n} t_r$.

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10. Prove that $I_1, I_2, I_3...$ form an AP, if

$$I_n = \int_0^\pi \frac{\sin 2nx}{\sin x} dx \; .$$

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11. Consider the sequence $S = 7 + 13 + 21 + 31 + ...+T_n$, find the value of T_{70}.

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12. Find value of $\left(x+\frac{1}{x}\right)^3+\left(x^2+\frac{1}{x^2}\right)^3+\ldots\ldots+\left(x^n+\frac{1}{x^n}\right)^3$.

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13. If the sequence $a_1, a_2, a_3, \ldots\ldots a_n, \cdot$ forms an A.P., then prove that $a_1^2-a_2^2+a_3^2-a_4^2+\ldots\ldots+a_{2n-1}^2-a_{2n}^2=\frac{n}{2n-1}\left(a_1^2-a_{2n}^2\right)$

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14. If three unequel numbers are in HP and their squares are in AP, show that they are in the ratio $1+\sqrt{3}:-2:1-\sqrt{3}$ or $1-\sqrt{3}:-2:1+\sqrt{3}$.

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15. If$a_1, a_2, a_3, \ldots\ldots.., a_n$ are in AP with $a_1 = 0$, prove that $\frac{a_3}{a_2} + \frac{a_4}{a_3} + \ldots\ldots + \frac{a_n}{a_{n-1}} - a_2\left(\frac{1}{a_2} + \frac{1}{a_3} + \ldots\ldots.. + \frac{1}{a_{n-2}}\right)$= $\frac{a_{n-1}}{a_2} + \frac{a_2}{a_{n-1}}$.

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16. Balls are arranged in rows to form an equilateral triangle. The first row consists of one ball, the second row of two balls and so on. If 669 more balls are added,then all the balls can be arranged in the shape of a square and each of the sides, then contains 8 balls less than each side of the triangle. Determine the initial number of balls.

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17. If $\theta_1, \theta_2, \theta_2, \theta_3, \ldots\ldots\ldots\ldots\Theta_n$ are in AP whose common difference is d, show that sec $\theta_1 \sec\theta_2 + \sec_3 + \quad \ldots + \sec\theta_{n-1} \sec\theta_n = \frac{\tan\theta_n - \tan\theta_1}{\sin d}$

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18. Show that, $\left(1+5^{-1}\right)\left(1+5^{-2}\right)\left(1+5^{-4}\right)\left(1+5^{-8}\right).....\left(1+5^{-2n}\right)=\frac{5}{4}\left(1-5^{-2(n+$

.

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19. Evaluate $\int_0^{\frac{\pi}{4}} \sec^2 x\, dx$

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20. Find the sum of the series : $\tan^{-1}\left(\frac{1}{3}\right)+\tan^{-1}\left(\frac{2}{9}\right)+....+\tan^{-1}\left(\frac{2^{n-1}}{1+2^{2n-1}}\right)+......\infty$

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21. Find the sum to n terms, whose nth term is $\tan[\alpha+(n-1)\beta]\tan(\alpha+n\beta)$.

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22. If $\sum_{r=1}^{n} t_r = \frac{n}{8}(n+1)(n+2)(n+3)$, then find $\sum_{r=1}^{n}\frac{1}{t_r}$.

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23. If s_1, s_2, s_3 denote the sum of n terms of 3 arithmetic series whose first terms are unity and their common difference are in H.P., Prove that $n = \frac{2s_3s_1 - s_1s_2 - s_2s_3}{s_1 - 2s_2 + s_3}$

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24. Three friends whose ages form a G.P. divide a certain sum of money in proportion to their ages. If they do that three years later, when the youngest is half the age of the oldest, then he will receive 105 rupees more that the he gets now and the middle friends will get 15 rupees more that he gets now, then ages of the friends are

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Exercise (Questions Asked In Previous 13 Years Exam)

1. Let a,b,c be in A.P. and $|a| < 1, |b| < 1|c| < 1.\ \text{ if } x = 1 + a + a^2 + \dots . \text{ to } \infty, y = 1 + b + b^2$, then x,y,z are in

A. AP

B. GP

C. HP

D. None of these

Answer: C

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2. Evluate $\int \frac{\tan^{-1} x}{1+x^2} dx$

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3. If $a_1, a_2, a_3,$ be terms of an A.P. and $\frac{a_1 + a_2 + \dots + a_p}{a_1 + a_2 + \dots + a_q} = \frac{p^2}{q^2}, p \neq q, then \frac{a_6}{a_{21}}$ equals to (a).41/11 (b). 7/2 (c). 2/7 (d). 11/41

A. $\frac{41}{11}$

B. $\frac{7}{2}$

C. $\frac{2}{7}$

D. $\frac{11}{41}$

Answer: D

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4. If $a_1, a_2, a_3, \ldots . a_n$ are in H.P. and $a_1a_2 + a_2a_3 + a_3a_4 + \ldots\ldots a_{n-1}a_n = ka_1a_n$, then k is equal to

A. $n(a_1 - a_n)$

B. $(n-1)(a_1 - a_n)$

C. na_1a_n

D. $(n-1)a_1a_n$

Answer: D

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5. Let V_r denotes the sum of the first r terms of an arithmetic progression whose first term is r and the common difference is $(2r-1)$. Let $T_r = V_{r+1} - V_r - 2$ and $Q_r = T_{r+1} - T_r$ for $r = 1, 2, \ldots$

The sum V1+V2+...+Vn is

A. $\frac{1}{12}n(n+1)\left(3n^2 - n + 1\right)$

B. $\frac{1}{12}n(n+1)(3n^2+n+2)$

C. $\frac{1}{2}n(2n^2-n+1)$

D. $\frac{1}{3}(2n^3-2n+3)$

Answer: B

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6. Let V_r denote the sum of the first r terms of an arithmetic progression (AP) whose first term is r and the common difference is $(2r-1). Let$ T_r=V_(r+1)-V_r-2 and Q_r =T_(r+1)-T_r for r=1,2...T_r` is always (A) an odd number (B) an even number (C) a prime number (D) a composite num,ber

A. an odd number

B. an even number

C. a prime number

D. a composite number

Answer: D

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7. Let V_r denotes the sum of the first r terms of an arithmetic progression whose first term is r and the common difference is $(2r-1)$. Let $T_r = V_{r+1} - V_r - 2$ and $Q_r = T_{r+1} - T_r$ for $r = 1, 2, \dots$.

The sum V1+V2+...+Vn is

A. $Q_1, Q_2, Q_3, \dots\dots$ are in AP with common difference 5

B. $Q_1, Q_2, Q_3, \dots\dots$ are in AP with common differemce 6

C. $Q_1, Q_2, Q_3, \dots\dots$ are in AP with common difference 11

D. $Q_1 = Q_2 = Q_3 = \dots\dots$

Answer: B

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8. Let A_1, G_1, H_1 denote the arithmetic, geometric and harmonic means respectively, of two distinct positive numbers. For $n \geq 2$, let A_{n-1}, G_{n-1} and H_{n-1} has arithmetic,geometric and harmonic means as A_n, G_n, H_n respectively.

Which of the following statement is correct?

A. $G_1 > G_2 > G_3 > \dots\dots.$

B. $G_1 < G_2 < G_3 < \dots\dots.$

C. $G_1 = G_2 = G_3 = \dots\dots.$

D. $G_1 < G_3 < G_5 < \dots\dots. \text{ and } G\_(2)gtG\_(4)gtG\_(6)gt\dots\dots.$

Answer: C

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9. Let A_1, G_1, H_1denote the arithmetic, geometric and harmonic means respectively, of two distinct positive numbers. For $n > 2$, let A_{n-1}, G_{n-1} and H_{n-1} has arithmetic, geometric and harmonic means as

$A_n, G_N, H_N,$ respectively

a. $A_1 > A_2 > A_3 > \ldots\ldots.$

b. $A_1 < A_2 < A_3 < \ldots\ldots.$

c. $A_1 > A_3 > A_5 > \ldots\ldots. \text{ and } A_2 < A_4 < A_6 < \ldots\ldots.$

d. $A_1 < A_3 < A_5 < \ldots\ldots. \text{ and } A_2 > A_4 > A_6 > \ldots\ldots.$

A. $A_1 > A_2 > A_3 > \ldots\ldots.$

B. $A_1 < A_2 < A_3 < \ldots\ldots.$

C. $A_1 > A_3 > A_5 > \ldots\ldots. \text{ and } A_2 < A_4 < A_6 < \ldots\ldots.$

D. $A_1 < A_3 < A_5 < \ldots\ldots. \text{ and } A_2 > A_4 > A_6 > \ldots\ldots.$

Answer: A

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10. Let A_1, G_1, H_1 denote the arithmetic, geometric and harmonic means respectively, of two distinct positive numbers. For $n \geq 2,$ let A_{n-1}, G_{n-1} and H_{n-1} has arithmetic,geometric and harmonic means as A_n, G_n, H_n respectively.

Which of the following statement is correct?

a. $H_1 > H_2 > H_3 > \ldots\ldots.$

b. $H_1 < H_2 < H_3 < \ldots\ldots.$

c. $H_1 > H_3 > H_5 > \ldots\ldots. \text{ and } H_2 < H_4 < H_6 < \ldots\ldots.$

d. $H_1 < H_3 < H_5 < \ldots\ldots. \text{ and } H_2 > H_4 > H_6 > \ldots\ldots.$

A. $H_1 > H_2 > H_3 > \ldots\ldots.$

B. $H_1 < H_2 < H_3 < \ldots\ldots.$

C. $H_1 > H_3 > H_5 > \ldots\ldots. \text{ and } H_2 < H_4 < H_6 < \ldots\ldots.$

D. $H_1 < H_3 < H_5 < \ldots\ldots. \text{ and } H_2 > H_4 > H_6 > \ldots\ldots.$

Answer: B

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11. In a G.P of positive terms if any term is equal to the sum of the next two terms, then the common ratio of the G.P is

A. $\frac{1}{2}(1-\sqrt{5})$

B. $\frac{1}{2}\sqrt{5}$

C. $\sqrt{5}$

D. $\frac{1}{2}(\sqrt{5}-1)$

Answer: D

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12. Suppose four distinct positive numbers a_1, a_2, a_3, a_4 are in G.P. Let $b_1 = a_1, b_2 = b_1 + a_2, b_3 = b_2 + a_3$ and $b_4 = b_3 + a_4$.

Statement -1 : The numbers b_1, b_2, b_3, b_4 are neither in A.P. nor in G.P.

Statement -2: The numbers b_1, b_2, b_3, b_4 are in H.P.

A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct explanation for Statement 1

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct explanation for Statement 1

C. Statement 1 is true, Statement 2 is false

D. Statement 1 is false, Statement 2 is true

Answer: C

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13. The first two terms of a geometric progression add up to 12. The sum of the third and the fourth terms is 48. If the terms of the geometric progression are alternately positive and negative, then the first term is

A. -12

B. 12

C. 4

D. -4

Answer: A

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14. If the sum of first n terms of an A.P. is cn^2 then the sum of squares of these n terms is

A. $\frac{n(4n^2-1)c^2}{6}$

B. $\frac{n(4n^2+1)c^2}{3}$

C. $\frac{n(4n^2-1)c^2}{3}$

D. $\frac{n(4n^2+1)c^2}{6}$

Answer: C

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15. The sum to infinity of the series $1+\frac{2}{3}+\frac{6}{3^2}+\frac{14}{3^4}+\dots is$

A. 6

B. 2

C. 3

D. 4

Answer: C

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16. Let $S_k, k = 1, 2, \ldots. 100$ denote the sum of the infinite geometric series whose first term is $\frac{k-1}{K!}$ and the common ratio is $\frac{1}{k}$ then the value of $\frac{(100)^2}{100!} + \sum_{k=1}^{100} \left|\left(k^2 - 3k + 1\right) S_k\right|$ is __________

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17. Let $a_1, a_2, a_3, , a_{11}$ be real numbers satisfying $a_1 = 15, 27 - 2a_2 > 0$ and $a_k = 2a_{k-1} - a_{k-2}$ for $k = 3, 4, , 11.$ If $\frac{a_1^2 + a_2^2 + \ldots + a_{11}^2}{11} = 90,$ then the value of $\frac{a1 + a2 + \ + a11}{11}$ is equals to ______.

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18. Check $2, 4, 6, 8, 10$ are in $A.P$ or not

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19. The minimum value of the sum of real numbers $a^{-5}, a^{-4}, 3a^{-3}, 1, a^8$ and a^{10} with $a > 0$ is ________.

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20. A man saves ₹ 200 in each of the first three months of his servies.In each of the subsequent monts his saving increases by ₹ 40 more than the saving of immediately previous month.His total saving from the start of service will be ₹ 11040 after .

A. 19 months

B. 20 months

C. 21 months

D. 18 months

Answer: C

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21. Let a_n be the nth term of an AP, if $\sum_{r=1}^{100} a_{2r} = \alpha \text{ and } \sum_{r=1}^{100} a_{2r-1} = \beta$, then the common difference of the AP is

A. $\frac{\alpha - \beta}{200}$

B. $\alpha - \beta$

C. $\frac{\alpha - \beta}{100}$

D. $\beta - \alpha$

Answer: C

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22. Let,$a_1, a_2 \_ a, a_3, \ldots.$ be in harmonic progression with $a_1 = 5$ and $a_{20} = 25$ The least positive integer n for which $a_n < 0$

A. 22

B. 23

C. 24

D. 25

Answer: D

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23. Statement 1: The sum of the series $1 + (1 + 2 + 4) + (4 + 6 + 9) + (9 + 12 + 16) + \ldots\ldots$ $+ (361 + 380 + 400) is 8000$. Statement 2: $\sum_{k=1}^{n} \left(k^3 - (k-1)^3\right) = n^3$ for any natural number n. (1) Statement 1 is false, statement 2 is true (2) Statement 1 is true, statement 2 is true; statement 2 is a correct explanation for statement 1 (3) Statement 1 is true, statement 2 is true;

statement 2 is not a correct explanation for statement 1 (4) Statement 1 is true, statement 2 is false

A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct explanation for Statement 1

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct explanation for Statement 1

C. Statement 1 is true, Statement 2 is false

D. Statement 1 is false, Statement 2 is true

Answer: A

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24. If 100 times the 100 th term of an A.P with non- zero common difference equals the 50 times its 50th term,then the 150th term of this A.P is

a. 150 times its 50th term

b. 150

c. 0

d. -150

A. 150 times its 50th term

B. 150

C. zero

D. -150

Answer: C

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25. If x,y,z are in AP and $\tan^{-1}x, \tan^{-1}y, \tan^{-1}z$ are also in AP, then

A. $2x = 3y = 6z$

B. $6x = 3y = 2z$

C. $6x = 4y = 3z$

D. $x = y = z$

Answer: D

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26. The sum of first 20 terms of the sequence 0.7 ,0.77 , 0.777 ...., is

A. $\frac{7}{9}(99 - 10^{-20})$

B. $\frac{7}{81}(179 + 10^{-20})$

C. $\frac{7}{9}(99 + 10^{-20})$

D. $\frac{7}{81}(179 - 10^{-20})$

Answer: B

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27. $Let S_n = \sum_{k=1}^{4n} (-1)^{\frac{k(k+1)}{2}} k^2$.Then S_n can take value (s)

A. 1056

B. 1088

C. 1120

D. 1332

Answer: A::D

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28. A pack contains n cards numbered from 1 to n . Two consecutive numbered cards are removed from the pack and the sum of the numbers on the remaining cards is 1224. If the smaller of the numbers on the removed cards is k, then $k - 20 =$ ________.

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29. If $(10)^9 + 2(11)^1(10)^8 + \ldots. + 10(11)^9 = k(10)^9$

A. 100

B. 110

C. $\frac{121}{10}$

D. $\frac{441}{100}$

Answer: A

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30. Three positive numbers form an increasing GP. If the middle terms in this GP is doubled, the new numbers are in AP. Then, the common ratio of the GP is

A. $2-\sqrt{3}$

B. $2+\sqrt{3}$

C. $\sqrt{2}+\sqrt{3}$

D. $3+\sqrt{2}$

Answer: B

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31. find the 3rd term in the sequence: an =(-1)n+15n+1

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32. The sum of first 9 terms of the series $\frac{1^3}{1} + \frac{1^3+2^3}{1+3} + \frac{1^3+2^3+3^3}{1+3+5} + \dots\dots\dots$ is

A. 192

B. 71

C. 96

D. 142

Answer: C

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33. If m is the A.M. of two distinct real numbers l and $n(l, n > 1)$ and G1, G2 and G3 are three geometric means between l and n, then $G1^4 + 2G2^4 + G3^4$ equals, (1) $4l^2$ mn (2) $4l^m$ ^ 2 mn (3) $4lmn^2$ (4) $4l^2m^2n^2$

A. $4l^2m^2n^2$

B. $4l^2mn$

C. $4lm^2n$

D. $4lmn^2$

Answer: C

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34. Soppose that all the terms of an arithmetic progression (AP) are natural numbers. If the ratio of the sum of the first seven terms to the sum of the first eleven terms is $6:11$ and the seventh term lies between 130 and 140, then the common difference of this AP is

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35. If the 2nd , 5th and 9th terms of a non-constant A.P are in G.P then the common ratio of this G.P is

A. 1

B. $\frac{7}{4}$

C. $\frac{8}{5}$

D. $\frac{4}{3}$

Answer: D

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36. If the sum of the first ten terms of the series $\left(1\frac{3}{5}\right)^2 + \left(2\frac{2}{5}\right)^2 + \left(3\frac{1}{5}\right)^2 + 4^2 + \left(4\frac{4}{5}\right)^2 + \ldots\ldots,$ is $\frac{16}{5}$ m, then m is equal to: (1) 102 (2) 101 (3) 100 (4) 99

A. 100

B. 99

C. 102

D. 101

Answer: D

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37. Find the value of x of the equation $x + 2m - 9 = 0$ where $m = 4$

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38. For any three positive real numbers a, b and c, $9(25a^2 + b^2) + 25(c^2 - 3ac) = 15b(3a + c)$. Then :

A. a,b and c are in GP

B. b,c and a are in GP

C. b,c and a are in AP

D. a,b and c are in AP

Answer: C

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