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## MATHS

# BOOKS - CENGAGE PUBLICATION 

## COORDINATE SYSYEM

## Illustration 11

1. Number of points with integral co-ordinates that lie inside a triangle whose co-ordinates are $(0,0),(0,21)$ and $(21,0)$.

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## Illustration 12

1. The point $(4,1)$ undergoes the following three transformations successively
(a) Reflection about the line $y=x$
(b)Translation through a distance 2 units along the positive direction of the $x$-axis
(c) Rotation through an angle $\pi / 4$ about the origin in the anti clockwise direction.

The final position of the point is given by the co-ordinates

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## Illustration 13

1. At what point should the origin be shifted if the coordinates of a point
$(4,5)$ become $(-3,9)$ ?

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## Illustration 14

1. If the axes are shifted to the point $(1,-2)$ without rotation, what do the following equations become? $2 x^{2}+y^{2}-4 x+4 y=0$, $y^{2}-4 x+4 y+8=0$

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## Illustration 15

1. Shift the origin to a suitable point so that the equation $y^{2}+4 y+8 x-2=0$ will not contain a term in $y$ and the constant term.

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## Illustration 16

1. The equation of curve referred to the new axes, axes retaining their directions, and origin $(4,5)$ is $X^{2}+Y^{2}=36$. Find the equation referred to the original axes.

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## Illustration 17

1. The axes are rotated through an angle $\pi / 3$ in the anticlockwise direction with respect to $(0,0)$. Find the coordinates of point $(4,2)$ (w.r.t. old coordinate system) in the new coordinates system.

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## Illustration 18

1. The equation of a curve referred to a given system of axes is $3 x^{2}+2 x y+3 y^{2}=10$. Find its equation if the axes are rotated through an angle $45^{\circ}$, the origin remaining unchanged.

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## Illustration 19

1. If $\theta$ is an angle by which axes are rotated about origin and equation $a x^{2}+2 h x y+b y^{2}=0$ does not contain xy term in the new system, then prove that $\tan 2 \theta=\frac{2 h}{a-b}$.

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## Illustration 110

1. In $A B C$ Prove that $A B^{2}+A C^{2}=2\left(A O^{2}=2\left(A O^{2}+B O^{2}\right)\right.$, where $O$ is the middle point of $B C$

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## Illustration 111

1. Find the coordinates of the circumcenter of the triangle whose vertices are $(A(5,-1), B(-1,5)$, and $C(6,6)$. Find its radius also.

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## Illustration 112

1. Two points $O(0,0)$ and $A(3, \sqrt{3})$ with another point $P$ form an equilateral triangle. Find the coordinates of $P$.

## Illustration 113

1. If $O$ is the origin and if the coordinates of any two points $Q_{1}$ and $Q_{2}$ are $\quad\left(x_{1}, y_{1}\right)$ and $\left(x_{2}, y_{2}\right)$, respectively, prove that $O Q_{1} . O Q_{2} \cos \angle Q_{1} O Q_{2}=x_{1} x_{2}+y_{1} y_{2}$.

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## Illustration 114

1. Given that $P(3,1), Q(6.5)$, and $R(x, y)$ are three points such that the angle $P Q R$ is a right angle and the area of $R Q P$ is 7 ,
find the value of $4 x-3 y+5$

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1. Find the area of a triangle whose vertices are $A(3,2), B(11,8)$ and $C(8,12)$.

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## Illustration 116

1. Prove that the area of the triangle whose vertices are $(t, t-2),(t+2, t+2)$, and $(t+3, t)$ is independent of $t$.

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## Illustration 117

1. Find the area of the quadrilateral $A B C D$ having vertices $A(1,1), B(7,-3), C(12,2)$, and $D(7,21)$.

## Illustration 118

1. For what value of $k$ are the points $(k, 2-2 k),(-k+1,2 k)$ and $(-4-k, 6-2 k)$ collinear?

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## Illustration 119

1. $A$ and $B$ are points $(3,4)$ and $(5,-2)$, find the co-ordinate of the point $P$ such that $|P A|=|P B|$ and area of $\triangle P A B=10$.

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## Illustration 120

1. If the vertices of a triangle have rational coordinates, then prove that the triangle cannot be equilateral.

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## Illustration 121

1. Given points $P(2,3), Q(4,-2)$, and $R(\alpha, 0)$. Find the value of $\alpha$ if $P R+R Q$ is minimum.

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## Illustration 122

1. If $A\left(\frac{3}{\sqrt{2}}, \sqrt{2}\right), \quad B\left(-\frac{3}{\sqrt{2}}, \sqrt{2}\right), C\left(-\frac{3}{\sqrt{2}},-\sqrt{2}\right) \quad$ and
$D(3 \cos \theta, 2 \sin \theta)$ are four points. If the area of the quadrilateral $A B C D$ is
maximum where $\theta \in\left(3 \frac{\pi}{2}, 2 \pi\right)$ then (a) maximum area is 10 sq units (b) $\theta=7 \frac{\pi}{4}$ (c) $\theta=2 \pi-\frac{\sin ^{-1} 3}{\sqrt{85}}$ (d) maximum area is 12 sq units

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## Illustration 123

1. Find the coordinates of the point which divides the line segments joining the points $(6,3)$ and $(-4,5)$ in the ratio $3: 2$ (i) internally and (ii) externally.

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## Illustration 124

1. Given that $A(1,1)$ and $B(2,-3)$ are two points and $D$ is a point on $A B$ produced such that $A D=3 A B$. Find the coordinates of $D$.

## Illustration 125

1. Determine the ratio in which the line $3 x+y-9=0$ divides the segment joining the points ( 1,3 ) and ( 2,7 ).

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## Illustration 126

1. Prove that the point $(-2,-1),(1,0),(4,3) \operatorname{and}(1,2)$ are the vertices of parallelogram. Is it a rectangle?

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## Illustration 127

1. Given that $A_{1}, A_{2}, A_{3}, A_{n}$ are $n$ points in a plane whose coordinates are $\left.x_{1}, y_{1}\right),\left(x_{2}, y_{2}\right),\left(x_{n}, y_{n}\right)$, respectively. $A_{1} A_{2}$ is bisected at the point $P_{1}, P_{1} A_{3}$ is divided in the ratio $A: 2$ at $P_{2}, P_{2} A_{4}$ is divided in the ratio 1:3 at $P_{3}, P_{3} A_{5}$ is divided in the ratio $1: 4$ at $P_{4}$, and so on until all $n$ points are exhausted. Find the final point so obtained.

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## Illustration 128

1. If vertex $A$ of triangle $A B C$ is $(3,5)$ and centroid is $(-1,2)$, then find the midpoint of side $B C$.

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## Illustration 129

1. Let $O(0,0), P(3,4)$, and $Q(6,0)$ be the vertices of triangle $O P Q$. The point $R$ inside the triangle $O P Q$ is such that the triangles $O P R, P Q R, O Q R$ are of equal area. The coordinates of $R$ are

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## Illustration 130

1. If $A\left(x_{1}, y_{1}\right), B\left(x_{2}, y_{2}\right)$, and $C\left(x_{3}, y_{3}\right)$ are three non-collinear points such that $x_{1}^{2}+y_{1}^{2}=x_{2}^{2}+y_{2}^{2}=x_{3}^{2}+y_{3}^{2}, \quad$ then prove that $x_{1} \sin 2 A+x_{2} \sin 2 B+x_{3} \sin 2 C=y_{1} \sin 2 A+y_{2} \sin 2 B+y_{3} \sin 2 C=0$.

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## Illustration 131

# 1. 

$A\left(a \cos \theta_{1}, a \sin \theta_{1}\right), B\left(a \cos \theta_{2} a \sin \theta_{2}\right), a n d C\left(a \cos \theta_{3}, a \sin \theta_{3}\right)$ equilateral, then prove
$\cos \theta_{1}+\cos \theta_{2}+\cos \theta_{3}=\sin \theta_{1}+\sin \theta_{2}+\sin \theta_{3}=0$.

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## Illustration 132

1. Find the orthocentre of the triangle whose vertices are $(0,0),(3,0)$, and $(0,4)$.

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## Illustration 133

1. If a vertex, the circumcenter, and the centroid of a triangle are ( 0,0 ), $(3,4)$, and ( 6,8 ), respectively, then the triangle must be (a) a right-angled triangle (b) an equilateral triangle (c) an isosceles triangle (d) a rightangled isosceles triangle

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## Illustration 134

1. If the circumcenter of an acute-angled triangle lies at the origin and the centroid is the middle point of the line joining the points $\left(a^{2}+1, a^{2}+1\right)$ and $(2 a,-2 a)$, then find the orthocentre.

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## Illustration 135

1. Orthocenter and circumcenter of a $\triangle A B C$ are $(a, b) \operatorname{and}(c, d)$, respectively. If the coordinates of the vertex $A$ are $\left(x_{1}, y_{1}\right)$, then find the coordinates of the middle point of $B C$.

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## Illustration 136

1. If a vertex of a triangle is $(1,1)$, and the middle points of two sides passing through it are $-2,3$ ) and ( 5,2 ), then find the centroid of the triangle.

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## Illustration 137

1. The vertices of a triangle are $A(-1,-7), B(5,1) \operatorname{and} C(1,4)$. If the internal angle bisector of $\angle B$ meets the side $A C$ in $D$, then find the length $A D$.

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## Illustration 138

1. Determine $x$ so that the line passing through $(3,4)$ and $(x, 5)$ makes an angle of $135^{0}$ with the positive direction of the $x$-axis.

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## Illustration 139

1. Which line is having the greatest inclination with the positive direction of the $x$-axis?
(i) Line joining the points $(1,3)$ and $(4,7)$
(ii)Line $3 x-4 y+3=0$

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## Illustration 140

1. If the point $(2,3),(1,1)$, and $(x, 3 x)$ are collinear, then find the value of $x$,using slope method.

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## Illustration 141

1. If the points $(a, 0),(b, 0),(0, c) \operatorname{and}(0, d)$ are concyclic $(a, b, c, d>0)$, then prove that $a b=c$.

## Illustration 142

1. If three points are $A(-2,1) B(2,3)$, and $C(-2,-4)$, then find the angle between $A B a n d B C$.

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## Illustration 143

1. Angle of a line with the positive direction of the $x$-axis is $\theta$. The line is rotated about some point on it in anticlockwise direction by angle $45^{0}$ and its slope becomes 3 . Find the angle $\theta$

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## Illustration 144

1. Let $A(6,4) \operatorname{and} B(2,12)$ be two given point. Find the slope of a line perpendicular to $A B$.

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## Illustration 145

1. If line $3 x-a y-1=0$ is parallel to the line $(a+2) x-y+3=0$ then find the value of $a$.

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## Illustration 146

1. If $A(2,-1) \operatorname{and} B(6,5)$ are two points, then find the ratio in which the foot of the perpendicular from $(4,1)$ to $A B$ divides it.

## Illustration 147

1. If $\left(b_{2}-b_{1}\right)\left(b_{3}-b_{1}\right)+\left(a_{2}-a_{1}\right)\left(a_{3}-a_{1}\right)=0$, then prove that the circumcenter of the triangle having vertices $\left(a_{1}, b_{1}\right),\left(a_{2}, b_{2}\right)$ and $\left(a_{3}, b_{3}\right)$ is $\left(\frac{a_{2}+a_{3}}{2}, \frac{b_{2}+b_{3}}{2}\right)$

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## Illustration 148

1. Find the orthocentre of $A B C$ with vertices $A(1,0), B(-2,1)$, and $C(5,2)$

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1. Two medians drawn from the acute angles of a right angled triangle intersect at an angle $\frac{\pi}{6}$. If the length of the hypotenuse of the triangle is 3 units, then the area of the triangle (in sq. units) is $\sqrt{3}$ (b) 3 (c) $\sqrt{2}$ (d) 9

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## Illustration 150

1. Plot the poitns whose coordinate are given below.
(i) $(2,3 \pi)$
(ii) $(2,-2 \pi / 3)$
(iii) $(-3,3 \pi / 4)$.

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## Illustration 151

1. Convert the following points from polar coordinates to the corresponding Cartesian coordinates.
$(2, \pi / 3)$

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## Illustration 152

1. Convert the following Cartesian coordinates to the corresponding polar coordinates using positive $r$ and negative $r$.
$(i i)(i i i)((i v)(v)-1,1(v i))(v i i)$
(viii)
$(i x)(x)((x i)(\xi i) 2,-3(x i i i))(x i v)(x v)$

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## Illustration 153

1. Convert $y=10$ into a polar equation.

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## Illustration 154

1. Express the polar equation $r-2 \cos \theta$ in rectangular coordinates.

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## Illustration 155

1. Convert $x^{2}-y^{2}=4$ into a polar equation.
2. Convert $r \sin \theta=r \cos \theta+4$ into its equivalent Cartesian equation.

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## Illustration 157

1. Convert $r=\cos e c \theta e^{r \cos \theta}$ into its equivalent Cartesian equation.

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## Illustration 158

1. Find the maximum distance of any point on the curve $x^{2}+2 y^{2}+2 x y=1$ from the origin.

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## Illustration 159

1. The sum of the squares of the distances of a moving point from two fixed points $(\mathrm{a}, \mathrm{0})$ and $(-a, 0)$ is equal to a constant quantity $2 c^{2}$. Find the equation to its locus.

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## Illustration 160

1. Find the locus of a point, so that the join of $(-5,1)$ and $(3,2)$ subtends a right angle at the moving point.

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## Illustration 161

1. Find the locus of a point such that the sum of its distance from the points $(0,2)$ and $(0,-2)$ is 6 .

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## Illustration 162

1. $A B$ is a variable line sliding between the coordinate axes in such a way that $A$ lies on the $x$-axis and $B$ lies on the $y$-axis. If $P$ is a variable point on $A B$ such that $P A=b, P b=a$, and $A B=a+b$, find the equation of the locus of $P$.

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## Illustration 163

1. Two points Pand $Q$ are given. $R$ is a variable point on one side of the line $P Q$ such that $\angle R P Q-\angle R Q P$ is a positive constant $2 \alpha$. Find the locus of the point $R$.

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## Illustration 164

1. If the coordinates of a variable point $P$ are $(a \cos \theta, b \sin \theta)$, where $\theta$ is a variable quantity, then find the locus of $P$.

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## Illustration 165

1. Find the locus of the point $\left(t^{2}+t+1, t^{2}-t+1\right), t \in R$.

## Illustration 166

1. Line segment joining $(5,0)$ and $(10 \cos \theta, 10 \sin \theta)$ is divided by a point $P$ in ratio 2:3 If $\theta$ varies then locus of $P$ is a;A) Pair of straight lines $B$ ) Straight line C) Circle D) Parabola

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## Illustration 167

1. If $A(\cos \alpha, \sin \alpha), B(\sin \alpha,-\cos \alpha), C(1,2)$ are the vertices of
$A B C$, then as $\alpha$ varies, find the locus of its centroid.

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1. If $a, b, c$ are the $p t h, q t h, r t h$ terms, respectively, of an $H P$, show that the points $(b c, p),(c a, q)$, and $(a b, r)$ are collinear.

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2. Prove that the circumcenter, orthocentre, incenter, and centroid of the triangle formed by the points $A(-1,11), B(-9,-8)$, and $C(15,-2)$ are collinear, without actually finding any of them.

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3. A rod of length $k$ slides in a vertical plane, its ends touching the coordinate axes. Prove that the locus of the foot of the perpendicular from the origin to the rod is $\left(x^{2}+y^{2}\right)^{3}=k^{2} x^{2} y^{2}$.

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4. $O X$ and $O Y$ are two coordinate axes. On $O Y$ a fixed point $P(0, c)$ is taken and on $O X$ any point $Q$ is taken. On $P Q$, an equilateral triangle is described, its vertex $R$ being on the side of $P Q$ away from $O$. Then prove that the locus of $R$ is $y=\sqrt{3} x-c$

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5. If $(x, y)$ and $(X, Y)$ are the coordinates of the same point referred to two sets of rectangular axes with the same origin and it $u x+v y$, where $u$ and $v$ are independent of xandy, becomes $V X+U Y$, show that $u^{2}+v^{2}=U^{2}+V^{2}$.

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6. What does the equation $2 x^{2}+4 x y-5 y^{2}+20 x-22 y-14=0$ become when referred to the rectangular axes through the point $(-2,-3)$, the new axes being inclined at an angle at $45^{0}$ with the old axes?

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7. Prove that the image of point $P(\cos \theta, \sin \theta)$ in the line having slope $\tan (\alpha / 2)$ and passing through origin is $Q(\cos (\alpha-\theta), \sin (\alpha-\theta))$.

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8. A line cuts the x -axis at $A(7,0)$ and the y -axis at $B(0,-5) \mathrm{A}$ variable line $P Q$ is drawn perpendicular to $A B$ cutting the $x$-axis in $P$ and the $y$-axis in $Q$. If $A Q$ and $B P$ intersect at $R$, find the locus of $R$.

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9. Two straight lines rotate about two fixed points. If they start from their position of coincidence such that one rotates at the rate double that of the other. Prove that the locus of their point of intersection is a circle.

## Concept Applications 11

1. What is the minimum area of a triangle with integral vertices ?

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2. What is length of the projection of line segment joining points $(2,3)$ and $(7,5)$ on $x$-axis.

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3. Point $P(2,3)$ goes through following transformations in successtion:
(i) reflection in line $y=x$
(ii) translation of 4 units to the right
(iii) translation of 5 units up
(iv) reflection in $y$-axis

Find the coordinates of final position of the point .

## (D) Watch Video Solution

4. Find the equation to which the equation $x^{2}+7 x y-2 y^{2}+17 x-26 y-60=0$ is transformed if the origin is shifted to the point $(2,-3)$, the axes remaining parallel to the original axies.

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5. Without rotating the original coordinate axes, to which point should origin be transferred, so that the equation $x^{2}+y^{2}-4 x+6 y-7=0$ is changed to an equation which contains no term of first degree?

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6. Given the equation $4 x^{2}+2 \sqrt{3} x y+2 y^{2}=1$. Through what angle should the axes be rotated so that the term $x y$ is removed from the transformed equation.

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## Concept Applications 12

1. Find the distance between the points $P(a \sin \alpha, a \cos \alpha)$ and $Q(a \cos \alpha,-a \sin \alpha)$

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2. Check how the points $A, B$ and $C$ are situated where $A(4,0), B(-1,-1), C(3,5)$.

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3. If the points $(1,1):\left(0, \sec ^{2} \theta\right)$; and $(\operatorname{cosec} 2,0)$ are collinear, then find the value of $\theta$
4. Area of the regular hexagon whose diagonal is the join of $(2,4)$ and $(6,7)$ is

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5. Let $A B C D$ be a rectangle and $P$ be any point in its plane. Show that $A P^{2}+P C^{2}=P B^{2}+P D^{2}$.

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6. Find the length of altitude through $A$ of the triangle $A B C$, where $A \equiv(-3,0) B \equiv(4,-1), C \equiv(5,2)$

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7. Find the area of the pentagon whose vertices are $A(1,1), B(7,21), C(7,-3)$

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8. Four points $A(6,3), B(-3,5), C(4,-2)$ and $D(x, 2 x)$ are given in such a way that $\frac{(\text { Areaof } D B C)}{(\text { Areaof } A B C)}=\frac{1}{2}$. find x

## (D) Watch Video Solution

## Concept Applications 13

1. If point $P(3,2)$ divides the line segment $A B$ internally in the ratio of 3:2 and point $Q(-2,3)$ divides AB externally in the ratio 4:3 then find the coordinates of points $A$ and $B$.

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2. If the point $(x,-1),(3, y),(-2,3)$, and $(-3,-2)$ taken in order are the vertices of a parallelogram, then find the values of $x a n d y$.
3. If the midpoints of the sides of a triangle are $(2,1),(-1,-3), \operatorname{and}(4,5)$, then find the coordinates of its vertices.

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4. The line joining $\mathrm{A}(b \cos \alpha, b \sin \alpha)$ and $\mathrm{B}(a \cos \beta, a \sin \beta)$, where $a \neq b$ , is produced to the point $M(x, y)$ so that $A M: M B=b$ :a Then $x \cos \frac{\alpha+\beta}{2}+y \sin \frac{\alpha+\beta}{2}$

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5. If the middle points of the sides of a triangle are $(-2,3),(4,-3)$, and $(4,5)$, then find the centroid of the triangle.

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6. Find the incentre of the triangle with vertices $(1, \sqrt{3}),(0,0)$ and $(2,0)$

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7. If $(1,4)$ is the centroid of a triangle and the coordinates of its any two vertices are $(4,-8)$ and $(-9,7)$, find the area of the triangle.

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8. The vertices of a triangle are $A\left(x_{1}, x_{1} \tan \alpha\right),\left(B x_{2}, x_{2} \tan \beta\right)$ and $C\left(x_{3}, x_{3} \tan \gamma\right)$. If the circumcentre of $\triangle A B C$ coincides with the origin and $H(a, b)$ be its orthocentre, then $a / b$ is equal to

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9. If $\left(x_{i}, y_{i}\right), i=1,2,3$, are the vertices of an equilateral triangle such that

$$
\left(x_{1}+2\right)^{2}+\left(y_{1}-3\right)^{2}=\left(x_{2}+2\right)^{2}+\left(y_{2}-3\right)^{2}=\left(x_{3}+2\right)^{2}+\left(y_{2}-3\right)^{2}=
$$ then find the value of $\frac{x_{1}+x_{2}+x_{3}}{y_{1}+y_{2}+y_{3}}$.

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10. 

$\cos ^{-1}(x)+\cos ^{-1}(y)+\cos ^{-1}(z)=\pi\left(\sec ^{2}(u)+\sec ^{4}(v)+\sec ^{6}(w)\right)$
,where $u, v, v, w$ are least non-negative angles such that $u<v<w$ then the value of $x^{2000}+y^{2000}+z^{2004}+\frac{36 \pi}{u+v+w}$ is

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## Concept Applications 14

1. The line joining the points $(x, 2 x) \operatorname{and}(3,5)$ makes an obtuse angle with the positive direction of the $x$-axis. Then find the values of $x$.

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2. If the line passing through $(4,3) \operatorname{and}(2, k)$ is parallel to the line $y=2 x+3$, then find the value of $k$.

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3. Triangle ABC lies in the cartesian plane and has an area of 70 sq. units. The coordinates of $B$ and $C$ are $(12,19)$, and $(23,20)$ respectively. The line containing the median to the side $B C$ has slope -5 . Find the possible coordinates of point A .

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4. For a given point $A(0,0), A B C D$ is a rhombus of side 10 units where slope of $A B$ is $\frac{4}{3}$ and slope of $A D$ is $\frac{3}{4}$. The sum of abscissa and ordinate of point C (where C lies in first quadrant) is

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5. The line joining the points $A(2,1)$ and $B(3,2)$ is perpendicular to the line $\left(a^{2}\right) x+(a+2) y+2=0$. Find the values of $a$.

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6. The angle between the line joining the points $(1,-2),(3,2)$ and the line $x+2 y-7=0$ is

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7. The othocenter of $\triangle A B C$ with vertices $B(1,-2)$ and $C(-2,0)$ is $H(3,-1)$.Find the vertex A .

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8. The medians $A D$ and $B E$ of a triangle $A B C$ with vertices $A(0, b), B(0,0)$ and $C(a, 0)$ are perpendicular to each other if $a^{2}: b^{2}$ is

## Concept Applications 15

1. Convert the polar coordinates to its equivalent Cartesian coordinates
$\left(2, \frac{\pi}{2}\right)$.

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2. Convert the following Cartesian coordinates to the cooresponding polar coordinates using positive r.
$(1,-1)$

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3. Convert $2 x^{2}+3 y^{2}=6$ into the polar equation.
4. Convert $r=4 \tan \theta \sec \theta$ into its equivalent Cartesian equation.

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5. Find the minimum distance of any point on the line $3 x+4 y-10=0$ from the origin using polar coordinates.

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## Concept Applications 16

1. Find the locus of a point whose distance from $(a, 0)$ is equal to its distance from the $y$-axis.

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2. The coordinates of the point $A$ and $B$ are $(a, 0)$ and $(-a, 0)$, respectively. If a point $P$ moves so that $P A^{2}-P B^{2}=2 k^{2}$, when $k$ is constant, then find the equation to the locus of the point $P$.

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3. Let $A(2,-3)$ and $B(-2,1)$ be the vertices of $\triangle A B C$. If the centroid of the triangle moves on the line $2 x+3 y=1$, then find the locus of the vertex $C$.

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4. $Q$ is a variable point whose locus is $2 x+3 y+4=0$; corresponding to a particular position of $Q, P$ is the point of section of $O Q, O$ being the origin, such that $O P: P Q=3: 1$. Find the locus of $P$.

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5. Find the locus of the middle point of the portion of the line $x \cos \alpha+y \sin \alpha=p$ which is intercepted between the axes, given that $p$ remains constant.

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6. Find the locus of the point of intersection of lines $x \cos \alpha+y \sin \alpha=a$ and $x \sin \alpha-y \cos \alpha=b(\alpha$ is a variable $)$.

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7. A point moves such that the area of the triangle formed by it with the points $(1,5)$ and $(3,-7)$ squinits. Then, find the locus of the point.

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8. A variable line through the point $P(2,1)$ meets the axes at a an d b .

Find the locus of the centroid of triangle $O A B$ (where $O$ is the origin).
9. A straight line is drawn through $P(3,4)$ to meet the axis of $x$ and $y$ at AandB , respectively. If the rectangle $O A C B$ is completed, then find the locus of $C$.

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## Exercises

1. $A B C$ is an isosceles triangle. If the coordinates of the base are $B(1,3)$ and $C(-2,7)$, the coordinates of vertex $A$
A. $(1,6)$
B. $(-1 / 2,5)$
C. $(-5 / 6,6)$
D. none of these

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2. If two vertices of a triangle are $(1,3)$ and $(4,-1)$ and the area of triangle is 5 sq. units, then the angle at the third vertex lies in :

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3. Which of the following sets of points form an equilateral triangle?
$(a)(1,0),(4,0),(7,-1)$
$(b)(0,0),\left(\frac{3}{2}, \frac{4}{3}\right),\left(\frac{4}{3}, \frac{3}{2}\right)$
(c) $\left(\frac{2}{3}, 0\right),\left(0, \frac{2}{3}\right),(1,1)$ (d) None of these
A. $(1,0),(4,0),(7,-1)$
B. $(0,0),(3 / 2,4 / 3), 4 / 3,3 / 2)$
C. $(2 / 3,0),(0,2 / 3),(1,1)$
D. none of these

## Answer: D

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4. A particle $p$ moves from the point $A(0,4)$ to the point $10,-4)$. The particle $P$ can travel the upper-half plane $\{(x, y) \mid y \geq\}$ at the speed of $1 \mathrm{~m} / s$ and the lower-half plane $\{(x, y) \mid y \leq 0\}$ at the speed of $2 \mathrm{~m} / \mathrm{s}$. The coordinates of a point on the $x$-axis, if the sum of the squares of the travel times of the upper- and lower-half planes is minimum, are $(1,0)(b)$ $(2,0)(c)(4,0)(d)(5,0)$
A. $(1,0)$
B. $(2,0)$
C. $(4,0)$
D. $(5,0)$

## Answer: B

5. If $\left|x_{1} y_{1} 1 x_{2} y_{2} 1 x_{3} y_{3} 1\right|=\left|a_{1} b_{1} 1 a_{2} b_{2} 1 a_{3} b_{3} 1\right|$ then the two triangles with vertices $\left(x_{1}, y_{1}\right),\left(x_{2}, y_{2}\right),\left(x_{3}, y_{3}\right)$ and $\left(a_{1}, b_{1}\right),\left(a_{2}, b_{2}\right),\left(a_{3}, b_{3}\right)$ are equal to area (b) similar congruent (d) none of these
A. equal in area
B. similar
C. congruent
D. none of these

## Answer: A

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6. $O P Q R$ is a square and $M, N$ are the middle points of the sides $P Q a n d Q R$, respectively. Then the ratio of the area of the square to that of triangle $O M N$ is $4: 1$ (b) 2:1 (c) $8: 3$ (d) 7:3
A. $4: 1$
B. 2:1
C. 8:3
D. 7: 3

## Answer: C

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7. A straight line passing through $P(3,1)$ meets the coordinate axes at AandB. It is given that the distance of this straight line from the origin $O$ is maximum. The area of triangle $O A B$ is equal to
A. $50 / 3$ sq.units
B. $25 / 3$ sq.units
C. $20 / 3$ sq.units
D. $100 / 3$ sq.units

## Answer: A

8. Let $A \equiv(3,-4), B \equiv(1,2)$. Let $P \equiv(2 k-1,2 k+1)$ be a variable point such that $P A+P B$ is the minimum. Then $k$ is $7 / 9$ (b) 0 (c) $7 / 8$ (d) none of these
A. $7 / 9$
B. 0
C. $7 / 8$
D. none of these

## Answer: C

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9. The polar coordinates equivalent to $(-3, \sqrt{3})$ are
10. If the point $P\left[X_{1}+t\left(X_{2}-X_{1}\right), y_{1}+t\left(y_{2}-y_{1}\right]\right.$ divides AB internally where $\left(X_{1}, Y_{1}\right)$ and $\mathrm{B} \mathrm{B}\left(X_{2}, Y_{2}\right)$ then, if $t \in(0, k)$, find k
A. $t<0$
B. $0<t<1$
C. $t>1$
D. $t=1$

## Answer: B

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11. $P$ and $Q$ are points on the line joining $A(-2,5)$ and $B(3,1)$ such that $A P=P Q=Q B$. Then, the distance of the midpoint of $P Q$ from the origin is 3 (b) $\frac{\sqrt{37}}{2}$ (b) 4 (d) 3.5
A. 3
B. $\sqrt{37 / 2}$
C. 4
D. 3.5

## Answer: B

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12. In triangle ABC , angle B is right angled, $A C=2$ and $A(2,2), B(1,3)$ then the length of the median AD is
A. $\left(\frac{1}{2}\right)$
B. $\sqrt{\frac{5}{2}}$
C. $\frac{5}{\sqrt{2}}$
D. $\frac{1}{\sqrt{2}}$

## Answer: B

13. One vertex of an equilateral triangle is $(2,2)$ and its centroid is $\left(-\frac{2}{\sqrt{3}}, \frac{2}{\sqrt{3}}\right)$ then length of its side is
A. $4 \sqrt{2}$
B. $4 \sqrt{3}$
C. $3 \sqrt{2}$
D. $5 \sqrt{2}$

## Answer: A

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14. ABCD is a rectangle with $A(-1,2), B(3,7)$ and $A B: B C=4: 3$. If P is the centre of the rectangle, then the distance of $P$ from each corner is equal to
A. $\frac{\sqrt{14}}{2}$
B. $3 \frac{\sqrt{41}}{4}$
C. $2 \frac{\sqrt{41}}{3}$
D. $5 \frac{\sqrt{41}}{8}$

## Answer: D

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15. If $(2,-3),(6,5)$ and $(-2,1)$ are three consecutive vertices of a rhombus, then its area is (a) 24 (b) 36
(c) 18 (d) 48

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16. If poitns $A(3,5)$ and B are equidistant from $H(\sqrt{2}, \sqrt{5})$ and B has rational coordinates,then $A B=$ (A) $\sqrt{7}$ (B) $\sqrt{(3-\sqrt{2})^{2}+(5-\sqrt{5})^{2}}$
(C) $s \sqrt{34}$ (D) none of these
A. $\sqrt{7}$
B. $\sqrt{(3-\sqrt{2})^{2}+(5-\sqrt{5})^{2}}$
C. $s \sqrt{34}$
D. none of these

## Answer: D

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17. Let n be the number of points having rational coordinates equidistant from the point $(0, \sqrt{3})$, then
A. $n>2$
B. $n \leq 1$
C. $n \leq 2$
D. $n=1$

## Answer: C

18. In a $\triangle A B C$ the sides $B C=5, C A=4$ and $A B=3$. If $A(0,0)$ and the internal bisector of angle $A$ meets $B C$ in $D\left(\frac{12}{7}, \frac{12}{7}\right)$ then incenter of $\triangle A B C$ is
A. $(2,2)$
B. $(3,2)$
C. $(2,3)$
D. $(1,1)$

## Answer: D

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19. If $A(0,0), B(1,0)$ and $C\left(\frac{1}{2}, \frac{\sqrt{3}}{2}\right)$ then the centre of the circle for which the lines $A B, B C, C A$ are tangents is
A. $\left(\frac{1}{2}, \frac{1}{4}\right)$
B. $\left(\frac{3}{2}, \frac{\sqrt{3}}{2}\right)$
C. $\left(\frac{1}{2}, \frac{1}{2 \sqrt{3}}\right)$
D. $\left(\frac{1}{2},-\frac{1}{\sqrt{3}}\right)$

## Answer: C

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20. Statement 1: If in a triangle, orthocentre, circumcentre and centroid are rational points, then its vertices must also be rational points.

Statement : 2 If the vertices of a triangle are rational points, then the centroid, circumcentre and orthocentre are also rational points.
A. Statement 1 is true, Statement 2 is true and Statement 2 is correct explanation for Statement 1.
B. Statement 1 is true, Statement 2 is true and Statement 2 is not the correct exlpanation for Statement 1.
C. Statement 1 is true, Statement 2 is false.
D. Statement 1 is false, Statement 2 is true.

## Answer: D

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21. Consider three points $P=(-\sin (\beta-\alpha),-\cos \beta)$,
$Q=(\cos (\beta-\alpha), \sin \beta), \quad$ and $\quad R=((\cos (\beta-\alpha+\theta), \sin (\beta-\theta))$,
where $0<\alpha, \beta, \theta<\frac{\pi}{4}$ Then
A. $P$ lies on the line segment RQ
B. Q lies on the segment PR
C. $R$ lies on the line segment PR
D. P,Q,R are non-collinear

## Answer: D

22. If two vertices of a triangle are $(-2,3)$ and $(5,-1)$ the orthocentre lies at the origin, and the centroid on the line $x+y=7$, then the third vertex lies at
A. A. $(7,4)$
B. B. $(8,14)$
C. C. $(12,21)$
D. D. none of these

## Answer: D

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23. The vertices of a triangle are $\left(p q, \frac{1}{p q}\right),\left(q r, \frac{1}{q r}\right)$, and $\left(r p, \frac{1}{r p}\right)$, where $p, q$ and $r$ are the roots of the equation $y^{3}-3 y^{2}+6 y+1=0$. The coordinates of its centroid are
B. B. $(2,-1)$
C. C. $(1,-1)$
D. D. $(2,3)$

## Answer: B

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24. If the vertices of a triangle are $(\sqrt{5,0}),(\sqrt{3}, \sqrt{2})$, and $(2,1)$, then the orthocenter of the triangle is
A. A. $(\sqrt{5}, 0)$
B. B. $(0,0)$
C. C. $(\sqrt{5}+\sqrt{3}+2, \sqrt{2}+1)$
D. D. none of these

## Answer: C

25. Two vertices of a triangle are $(4,-3) \&(-2,5)$. If the orthocentre of the triangle is at $(1,2)$, find coordinates of the third vertex.
A. $(-33,-26)$
B. $(33,26)$
C. $(26,33)$
D. none of these

## Answer: B

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26. In $\triangle A B C$ if the orthocentre is $(1,2)$ and the circumcenter is $(0,0)$ then centroid of $\triangle A B C$ is.
A. $(1 / 2,2 / 3)$
B. $(1 / 3,2 / 3)$
C. $(2 / 3,1)$
D. none of these

## Answer: B

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27. A triangle $A B C$ with vertices $A(-1,0), B\left(-2, \frac{3}{4}\right)$, and $C\left(-3,-\frac{7}{6}\right)$ has its orthocentre at $H$. Then, the orthocentre of triangle $B C H$ will be
A. $(-3,-2)$
B. $(1,3)$
C. ( $-1,2$ )
D. none of these

## Answer: D

28. If in triangle $A B C, A=(1,10)$, circumcentre $=\left(-\frac{1}{3}, \frac{2}{3}\right)$ and orthocentre $=\left(\frac{11}{3}, \frac{4}{3}\right)$ then the co-ordinates of mid-point of side opposite to A is:
A. $(1,-11 / 3)$
B. $(1 / 5)$
C. $(1,-3)$
D. $(1,6)$

## Answer: A

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29. In the $\triangle A B C$, the coordinates of B are $(0,0), A B=2, \angle A B C=\frac{\pi}{3}$ and the middle point of $B C$ has the coordinates $(2,0)$. The centroid of the triangle is
A. $(1 / 2, \sqrt{3} / 2)$
B. $(5 / 3,1 / \sqrt{3})$
C. $(4+\sqrt{3} / 3,1 / 3)$
D. none of these

## Answer: B

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30. If the origin is shifted to the point $\left(\frac{a b}{a-b}, 0\right)$ without rotation, then the equation $(a-b)\left(x^{2}+y^{2}\right)-2 a b x=0$ becomes
A. A. $(a-b)\left(x^{2}+y^{2}\right)-(a+b) x y+a b x=a^{2}$
B. B. $(a+b)\left(x^{2}+y^{2}\right)=2 a b$
C. C. $\left(x^{2}+y^{2}\right)=\left(a^{2}+b^{2}\right)$
D. D. $(a-b)^{2}\left(x^{2}+y^{2}\right)=a^{2} b^{2}$
31. A light ray emerging from the point source placed at $P(2,3)$ is reflected at a point $Q$ on the $y$-axis. It then passes through the point $R(5,10)$. The coordinates of $Q$ are
A. A. $(0,3)$
B. B. $(0,2)$
C. C. (0,5)
D. D. none of these

## Answer: C

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32. Point $P(p, 0), Q(q, 0), R(0, p), S(0, q)$ from.
A. A. parallelogram
B. B. rhombus
C. C. cyclic quadrilateral
D. D. none of these

## Answer: C

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33. A rectangular billiard table has vertices at $P(0,0), Q(0,7), R(10,7)$, and $S(10,0)$. A small billiard ball starts at $M(3,4)$, moves in a straight line to the top of the table, bounces to the right side of the table, and then comes to rest at $N(7,1)$. The $y$ - coordinate of the point where it hits the right side is 3.7 (b) 3.8 (c) 3.9 (d) 4
A. 3.7
B. 3.8
C. 3.9
D. 4

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34. ABCD is a square Points $E(4,3)$ and $F(2,5)$ lie on AB and CD , respectively,such that EF divides the square in two equal parts. If the coordinates of $A$ are $(7,3)$, then the coordinates of other vertices can be
A. A. $(7,2)$
B. B. $(7,5)$
C. C. $(-1,3)$
D. D. $(-1,5)$

## Answer: D

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35. If one side of a rhombus has endpoints $(4,5)$ and $(1,1)$, then the maximum area of the rhombus is
A. A. 50 sq.units
B. B. 25 sq.units
C. C. 30 sq.units
D. D. 20 sq.units

## Answer: B

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36. A rectangle
$A B C D$,
where
$A \equiv(0,0), B \equiv(4,0), C \equiv(4,2) D \equiv(0,2)$, undergoes the following transformations successively:
$f_{1}(x, y) \rightarrow(y, x)$
$f_{2}(x, y) \rightarrow(x+3 y, y)$
$\left.f_{3}(x, y) \rightarrow\left(\frac{x-y}{2}\right), \frac{x+y}{2}\right)$

The final figure will be
(a) square
(b) a rhombus
(c) a rectangle
(d) a parallelogram
A. a square
B. a rhombus
C. a rectangle
D. a parallelogram

## Answer: D

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37. If a straight line through the origin bisects the line passing through the given points $(a \cos \alpha, a \sin \alpha)$ and $(a \cos \beta, a \sin \beta)$, then the lines
A. are perpendicular
B. are parallel
C. have an angle between them of $\pi / 4$
D. none of these

## Answer: A

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38. Let $A_{r}, r=1,2,3$, be the points on the number line such that $O A_{1}, O A_{2}, O A_{3}$. are in $G P$, where $O$ is the origin, and the common ratio of the $G P$ be a positive proper fraction. Let $M$, be the middle point of the line segment $A_{r} A_{r+1}$. Then the value of $\sum_{r=1}^{\infty} O M_{r}$ is equal to
(a) $\frac{O A_{1}\left(O S A_{1}-O A_{2}\right)}{2\left(O A_{1}+O A_{2}\right)}$
(b) $\frac{O A_{1}\left(O A_{2}+O A_{1}\right)}{2\left(O A_{1}-O A_{2}\right)}$
(c) $\frac{O A_{1}}{2\left(O A_{1}-O A_{2}\right)}$

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39. The vertices of a parallelogram $A B C D$ are $A(3,1), B(13,6), C(13,21)$, and $D(3,16)$. If a line passing through the origin divides the parallelogram into two congruent parts, then the slope of the line is (a) $\frac{11}{12}$ (b) $\frac{11}{8}$ (c) $\frac{25}{8}$ (d) $\frac{13}{8}$
A. $11 / 12$
B. $11 / 8$
C. $25 / 8$
D. $13 / 8$

## Answer: B

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40. Point $A$ and $B$ are in the first quadrant,point $O$ is the origin. If the slope of $O A$ is 1, slope of $O B$ is 7 and $O A=O B$, Then slope of $A B$ is:
A. $-1 / 5$
B. $-1 / 4$
C. $-1 / 3$
D. $-1 / 2$

## Answer: D

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41. Let $\mathrm{a}, \mathrm{b}, \mathrm{c}$ be in A.P and $\mathrm{x}, \mathrm{y}, \mathrm{z}$ be in G.P.. Then the points $(a, x),(b, y)$ and $(c, z)$ will be collinear if
A. A. $x^{2}=y$
B. В. $x=y=z$
C. C. $y^{2}=z$
D. D. $x=z^{2}$

## Answer: B

42. If $\sum_{i=1}^{4}\left(x 1^{2}+y 1^{2}\right) \leq 2 x_{1} x_{3}+2 x_{2} x_{4}+2 y_{2} y_{3}+2 y_{1} y_{4}$, the points $\left(x_{1}, y_{1}\right),\left(x_{2}, y_{2}\right),\left(x_{3}, y_{3}\right),\left(x_{4}, y_{4}\right)$ are
A. the vertices of a rectangle
B. collinear
C. the vertices of a trapezium
D. none of these

## Answer: A

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43. The vertices $A$ and $D$ of square $A B C D$ lie on the positive sides of $x$ - and $y$-axis, respectively. If the vertex $C$ is the point $(12,17)$, then the coordinates of vertex $B$ are (a) $(14,16)$ (b) $(15,3)$ (c) 17,5 ) (d) $(17,12)$
A. $(14,16)$
B. $(15,3)$
C. $(17,5)$
D. $(17,12)$

## Answer: C

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44. Through the point $P(\alpha, \beta)$, where $\alpha \beta>0$, the straight line $\frac{x}{a}+\frac{y}{b}=1$ is drawn so as to form a triangle of area $S$ with the axes. If $a b>0$, then the least value of $S$ is
A. $\alpha \beta$
B. $2 \alpha \beta$
C. $3 \alpha \beta$
D. none

## Answer: B

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45. The locus of the moving point whose coordinates are given by $\left(e^{t}-e^{-t}, e^{t}+e^{-t}\right)$ where $t$ is a parameter, is (a) $x y=1$ (b) $y+x=2$
(c) $y^{2}-x^{2}=4$ (d) $y^{2}-x^{2}=2$

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46. The locus of a point reprersented by $x=\frac{a}{2}\left(\frac{t+1}{t}\right), y=\frac{a}{2}\left(\frac{t-1}{t}\right) \quad$, where $\quad t \in R-\{0\}, \quad$ is $x^{2}+y^{2}=a^{2}$ (b) $x^{2}-y^{2}=a^{2}$ (c) $x+y=a$ (d) $x-y=a$
A. $x^{2}+y^{2}=a^{2}$
B. $x^{2}-y^{2}=a^{2}$
C. $x+y=a$
D. $x-y=a$

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47. Vertices of a variable triangle are $\mathrm{A}(3,4), B(5 \cos \theta, 5 \sin \theta)$ and C $(5 \sin \theta,-5 \cos \theta)$ where $\theta$ is a parameter then, find the locus of its orthocentre.

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48. Vertices of a variable triangle are $\mathrm{A}(3,4), B(5 \cos \theta, 5 \sin \theta)$ and C $(5 \sin \theta,-5 \cos \theta)$ where $\theta$ is a parameter then, find the locus of its orthocentre.
A. $(x+y-1)^{2}+(x-y-7)^{2}=100$
B. $(x+y-7)^{2}+(x-y-1)^{2}=100$
C. $(x+y-7)^{2}+(x+y-1)^{2}=100$
D. $(x+y-7)^{2}+(x-y+1)^{2}=100$

## Answer: D

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49. From a point, $P$ perpendicular $P M$ and $P N$ are drawn to $x$ and $y$ axis, respectively. If $M N$ passes through fixed point $(a, b)$, then locus of $P$ is
A. A. $x y=a x+b y$
B. B. $x y=a b$
C. C. $x y=b x+a y$
D. D. $x+y=x y$

## Answer: C

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50. The locus of point of intersection of the lines $y+m x=\sqrt{a^{2} m^{2}+b^{2}}$ and $m y-x=\sqrt{a^{2}+b^{2} m^{2}}$ is
A. $x^{2}+y^{2}=\frac{1}{a^{2}}+\frac{1}{b^{2}}$
B. $x^{2}+y^{2}=a^{2}+b^{2}$
C. $x^{2}+y^{2}=a^{2}-b^{2}$
D. $\frac{1}{x^{2}}+\frac{1}{y^{2}}=a^{2}-b^{2}$

## Answer: B

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51. If the roots of the equation
$\left(x_{1}^{2}-a^{2}\right) m^{2}-2 x_{1} y_{1} m+y_{1}^{2}+b^{2}=0(a>b)$ are the slopes of two perpendicular lies intersecting at $P\left(x_{1}, y_{1}\right)$, then the locus of P is
A. A. $x^{2}+y^{2}=a^{2}+b^{2}$
B. B. $x^{2}+y^{2}=a^{2}-b^{2}$
C. C. $x^{2}-y^{2}=a^{2}+b^{2}$
D. D. $x^{2}-y^{2}=a^{2}-b^{2}$

## Answer: B

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52. Through point $P(-1,4)$, two perpendicular lines are drawn which intersect x -axis at Q and R . find the locus of incentre of $\triangle P Q R$.
A. $x^{2}+y^{2}+2 x-8 y-17=0$
B. $x^{2}-y^{2}+2 x-8 y+17=0$
C. $x^{2}+y^{2}-2 x-8 y-17=0$
D. $x^{2}-y^{2}+8 x-2 y-17=0$

## Answer: B

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53. The number of integral points ( $\mathrm{x}, \mathrm{y}$ ) (i.e, x and y both are integers) which lie in the first quadrant but not on the coordinate axes and also on
the straight line $3 x+5 y=2007$ is equal to (A) 133 (B) 135 (C) 138 (D) 140
A. 133
B. 135
C. 138
D. 140

## Answer: A

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54. The foot of the perpendicular on the line $3 x+y=\lambda$ drawn from the origin is $C$. If the line cuts the $x$ and the $y$-axis at $\operatorname{AandB}$, respectively, then $B C: C A$ is
A. 1:3
B. 3: 1
C. 1:9

## D. 9:1

Answer: D

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55. The image of $P(a, b)$ on the line $y=-x$ is Q and the image of Q on the line $y=x$ is R find the mid-point of P and R
A. $(a+b, b+a)$
B. $((a+b) / 2,(b+2) / 2)$
C. $(a-b, b-a)$
D. $(0,0)$

## Answer: D

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56. If the equation of the locus of a point equidistant from the points $\left(a_{1}, b_{1}\right)$ and $\left(a_{2}, b_{2}\right)$ is $\left(a_{1}-a_{2}\right) x+\left(b_{1}-b_{2}\right) y+c=0$, then the value of $C$ is
A. $a_{1}^{2}-a_{2}^{2}+b_{1}^{2}-b_{2}^{2}$
B. $\sqrt{a_{1}^{2}+b_{1}^{2}-a_{2}^{2}-b_{2}^{2}}$
C. $\frac{1}{2}\left(a_{2}^{2}+b_{2}^{2}-a_{2}^{2}-b_{1}^{2}\right)$
D. $\frac{1}{2}\left(a_{1}^{2}+b_{2}^{2}+a_{1}^{2}+b_{2}^{2}\right)$

## Answer: D

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57. Consider three lines as follows. $L_{1}: 5 x-y+4=0$ $L_{2}: 3 x-y+5=0 L_{3}: x+y+8=0$ If these lines enclose a triangle $A B C$ and the sum of the squares of the tangent to the interior angles can be expressed in the form $\frac{p}{q}$, where $p$ and $q$ are relatively prime numbers, then the value of $p+q$ is
A. A. 500
B. B. 450
C. C. 230
D. D. 465

## Answer: D

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58. Consider a point $A(m, n)$, where $m$ and $n$ are positve intergers. $B$ is the reflection of A in the line $y=x, \mathrm{C}$ is the reflaction of B in the y axis, D is the reflection of $C$ in the $x$ axis and $E$ is the reflection of $D$ is the $y$ axis. The area of the pentagon $A B C D E$ is a. $2 m(m+n)$
b. $m(m+3 n)$
c. $m(2 m+3 n)$ d. $2 m(m+3 n)$
59. In the given figure, $O A B C$ is a rectangle. Slope of $O B$ is

A. $1 / 4$
B. $1 / 3$
C. $1 / 2$
D. Cannot be determined

## Answer: C

1. If $(-6,-4),(3,5),(-2,1)$ are the vertices of a parallelogram, then remaining vertex cannot be
A. $(0,-1)$
B. $(7,10)$
C. $(-1,0)$
D. $(-11,-8)$

## Answer: B::C::D

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2. Let $0 \equiv(0,0), A \equiv(0,4), B \equiv(6,0)$. Let $P$ be a moving point such that the area of triangle $P O A$ is two times the area of triangle $P O B$. The locus of $P$ will be a straight line whose equation can be

$$
\text { A. } x+3 y=0
$$

B. $x+2 y=0$
C. $2 x-3 y=0$
D. $3 y-x=0$

## Answer: A: D

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3. If $(-4,0)$ and $(1,-1)$ are two vertices of a triangle of area 4squinits, then its third vertex lies on (a) $y=x$ (b) $5 x+y+12=0$ (c) $x+5 y-4=0$ (d) $x+5 y+12=0$
A. $y=x$
B. $5 x+y+12=0$
C. $x+5 y-4=0$
D. $x+5 y+12=0$
4. The area of triangle $A B C$ is $20 \mathrm{~cm}^{2}$. The coordinates of vertex $A$ are $(-5,0)$ and those of $B$ are $(3,0)$. The vertex $C$ lies on the line $x-y=2$. The coordinates of $C$ are
(a) $(5,3)$
(b) $(-3,-5)(-5,-7)$
(d) $(7,5)$
A. $(5,3)$
B. $(-3,-5)$
C. $(-5,-7)$
D. $(7,5)$

## Answer: B

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5. 

If
$A B C$
having
vertices
$A\left(a \cos \theta_{1}, a \sin \theta_{1}\right), B\left(a \cos \theta_{2} a \sin \theta_{2}\right), a n d C\left(a \cos \theta_{3}, a \sin \theta_{3}\right)$
$\cos \theta_{1}+\cos \theta_{2}+\cos \theta_{3}=\sin \theta_{1}+\sin \theta_{2}+\sin \theta_{3}=0$.
A. $\cos \theta_{1}+\cos \theta_{2}+\cos \theta_{3}=0$
B. $\sin \theta_{1}+\sin \theta_{2}+\sin \theta_{3}=0$
C. $\tan \theta_{1}+\tan \theta_{2}+\tan \theta_{3}=0$
D. $\cot \theta_{1}+\cot \theta_{2}+\cot \theta_{3}=0$

## Answer: A: B

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6. The points $A(0,0), B(\cos \alpha, \sin \alpha)$ and $C(\cos \beta, \sin \beta)$ are the vertices of a right-angled triangle then
A. $\sin \frac{\alpha-\beta}{2}=\frac{1}{\sqrt{2}}$
B. $\cos \frac{\alpha-\beta}{2}=\frac{1}{\sqrt{2}}$
C. $\cos \frac{\alpha-\beta}{2}=-\frac{1}{\sqrt{2}}$
D. $\sin \frac{\alpha-\beta}{2}=-\frac{1}{\sqrt{2}}$

## Answer: A::C::D

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7. The ends of a diagonal of a square are $(2,-3)$ and $(-1,1)$. Another vertex of the square can be
A. $(-3, / 2,-5 / 2)$
B. $(5 / 2,1 / 2)$
C. $(1 / 2,5 / 2)$
D. none of these

## Answer: A: B

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8. If all the vertices of a triangle have integral coordinates, then the triangle may be (a) right-angle (b) equilateral (c) isosceles (d) none of these
A. right-angled
B. equilateral
C. isosceles
D. none of these

## Answer: A:C

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9. In a $A B C, A \equiv(\alpha, \beta), B \equiv(1,2), C \equiv(2,3)$, point $A$ lies on the line $y=2 x+3$, where $\alpha, \beta$ are integers, and the area of the triangle is $S$ such that $[S]=2$ where [ .] denotes the greatest integer function. Then the possible coordinates of $A$ can be (A) $(-7,-11)$ (B) $(-6,-9)(C)(2,7)(D)(3,9)$
A. $(-7,-11)$
B. $(-6,-9)$
C. $(2,7)$
D. $(3,9)$

## Answer: A::B::C::D

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10. In an acute triangle $A B C$, if the coordinates of orthocentre $H$ are $(4, b)$, of centroid $G$ are $(b, 2 b-8)$ and of circumcenter $S$ are $(-4,8)$, then $b$ cannot be (a) 4 (b) 8 (c) 12 (d) -12
A. (a) 4
B. (b) 8
C. (c) 12
D. (d) -12

## D Watch Video Solution

11. Consider the points $O(0,0), A(0,1)$, and $B(1,1)$ in the $x-y$ plane. Suppose that points $C(x, 1)$ and $D(1, y)$ are chosen such that $0<x<1$. And such that $O, C$, and $D$ are collinear. Let the sum of the area of triangles $O A C$ and $B C D$ be denoted by $S$. Then which of the following is/are correct?.
A. Minimum value of $S$ is irrational lying in $(1 / 3,1 / 2)$.
B. Minimum value of $S$ is irrational in $(2 / 3,1)$.
C. The value of x for the minimum value of S lies in $(2 / 3,1)$.
D. The value of x for the minimum values of S lies in $(1 / 3,1 / 2)$.

## Answer: A:C

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12. Two sides of a rhombus $A B C D$ are parallel to the lines $y=x+2$ and $y=7 x+3$. If the diagonal of the rhombus intersect at the point $(1,2)$ and the vertex. A is on the $y$-axis, then find the possible coodinates of $A$.
A. $(0,3)$
B. $(0,5 / 2)$
C. $(0,0)$
D. $(0,6)$

## Answer: B::C

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13. A right angled triangle $A B C$ having a right angle at $C, C A=b$ and $C B=a$, move such that angular points $A$ and $B$ slide along $x$-axis and $y$-axis respectively. Find the locus of $C$
A. (a) $a x+b y+1=0$
B. (b) $a y \pm b x=0$
C. (c) $a x^{2} \pm 2 b t+y^{2}=0$
D. (d) $a x-b y=0$

## Answer: B::D

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## Linked

1. For points $P=\left(x_{1}, y_{1}\right)$ and $Q=\left(x_{2}, y_{2}\right)$ of the co-ordinate plane a new distance $\mathrm{d}(\mathrm{P}, \mathrm{Q})=\left|x_{1}-x_{2}\right|+\left|y_{1}-y_{2}\right|$ is defined .Let $\mathrm{O}(0,0)$ and $\mathrm{A}(3,2)$. The set of points in first quadrant which are equidistant from O and A is
A. one straight line only
B. union of two line segments
C. union of two infinite rays
D. union of a line segment of finite length and an infinite ray

## Answer: D

## D Watch Video Solution

2. For points $P \equiv\left(x_{1} y_{1}\right)$ and $Q \equiv\left(x_{2}, y_{2}\right)$ of the coordinate plane, a new distance $\mathrm{d}(\mathrm{P}, \mathrm{Q})$ is defined by $\mathrm{d}(P, Q)=\left|X_{1}-X_{2}\right|+\left|y_{1}-y_{2}\right|$ Let $O=(0,0), A=(1,2), B \equiv(2,3)$ and $C \equiv(4,3)$ are four fixed points on $x$ - $y$ plane

Answer the following questions based on above passage:
Let $\mathrm{S}(\mathrm{x}, \mathrm{y})$, such that S is equidistant from the points O and B with respect to new distance and if $x \geq 2$ and $0 \leq y<3$, then locus of $S$ is
A. 2sq.units
B. 4 sq.units
C. 6 sq.units
D. noen of these

## Answer: B

3. For points $P=\left(x_{1}, y_{1}\right)$ and $Q=\left(x_{2}, y_{2}\right)$ of the co-ordinate plane a new distance $\mathrm{d}(\mathrm{P}, \mathrm{Q})=\left|x_{1}-x_{2}\right|+\left|y_{1}-y_{2}\right|$ is defined .Let $\mathrm{O}(0,0)$ and $\mathrm{A}(3,2)$. The set of points in first quadrant which are equidistant from O and A is
A. one -one and onto function
B. many one and onto function
C. one-one and into function
D. relation but not function

## Answer: D

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4. Let $O(0,0), A(2,0)$, $\operatorname{andB}\left(1, \frac{1}{\sqrt{3}}\right)$ be the vertices of a triangle. Let $R$ be the region consisting of all those points $P$ inside $O A B$ which satisfy $d(P, O A) \leq \min [d(P, O B), d(P, A B)]$, where $d$ denotes the
distance from the point to the corresponding line. Sketch the region $R$ and find its area.
A. $\sqrt{3}$ sq,units
B. $(2+\sqrt{3})$ sq.units
C. $\sqrt{3} / 2$ sq.units
D. $1 / \sqrt{3}$ sq.units

## Answer: D

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5. Let $O(0,0), A(2,0), \operatorname{and} B\left(1, \frac{1}{\sqrt{3}}\right)$ be the vertices of a triangle. Let $R$ be the region consisting of all those points $P$ inside $O A B$ which satisfy $d(P, O A) \leq \min [d(P, O B), d(P, A B)]$, where $d$ denotes the distance from the point to the corresponding line. Sketch the region $R$ and find its area.
A. $\sqrt{3}$ sq,units
B. $1 / \sqrt{3}$ sq.units
C. $\sqrt{3} / 2$ sq,units
D. none of these

## Answer: B

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6. Let $A B C D$ is a square with sides of unit length. Points $E$ and $F$ are taken om sides $A B$ and $A D$ respectively so that $A E=A F$. Let $P$ be a point inside the square $A B C D$. The maximum possible area of quadrilateral CDFE is-
A. $1 / 8$
B. $1 / 4$
C. $5 / 8$
D. $3 / 8$

## Answer: C

7. Let $A B C D$ be a square with sides of unit lenght. Points $E$ and $F$ are taken on sides AB and AD , respectively,so that $A E=A F$. Let P be a point inside the squre $A B C D$.

The value of $(P A)^{2}-(P B)^{2}+(P C)^{2}-(P D)^{2}$ is equal to
A. 3
B. 2
C. 1
D. 0

## Answer: D

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8. Let $A B C D$ be a square with sides of unit lenght. Points $E$ and $F$ are taken on sides AB and AD , respectively,so that $A E=A F$. Let P be a point
inside the squre $A B C D$.
Let a line passing through point $A$ divides the sqaure $A B D$ into two parts so that the area of one portion is double the other. then the length of the protion of line inside the square is
A. $\sqrt{10} / 3$
B. $\sqrt{13} / 3$
C. $\sqrt{11} / 3$
D. $2 / \sqrt{3}$

## Answer: B

## D Watch Video Solution

9. Let $A B C$ be an acute- angled triangle and $A D, B E$, and $C F$ be its medians, where E and F are at $(3,4)$ and $(1,2)$ respectively. The centroid of $\Delta A B C$ $G(3,2)$.

The coordinates of point $D$ is $\qquad$
A. $(7,-4)$
B. $(5,0)$
C. $(7,4)$
D. $(-3,0)$

## Answer: B

## - Watch Video Solution

10. Let $A B C$ be an acute- angled triangle and $A D, B E$, and $C F$ be its medians, where E and F are at $(3,4)$ and $(1,2)$ respectively. The centroid of $\Delta A B C$ $G(3,2)$.

The coordinates of point $D$ is $\qquad$

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## Matrix Match Type

1. Consider the lines represented by equation $\left(x^{2}+x y-x\right) \times(x-y)=0$ forming a triangle. Then match the following lists:

| List I | List II |
| :--- | :--- |
| a. Orthocenter of triangle | p. $(1 / 6,1 / 2)$ |
| b. Circumcenter | q. $(1 /(2+2 \sqrt{2}), 1 / 2)$ |
| c. Centroid | r. $(0,1 / 2)$ |
| d. Incenter | s. $(1 / 2,1 / 2)$ |

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2. Consider the triangle whose vetices are ( 0,0 ) , ( 5,12 ) and ( 16,12 ).


## List I

a. The locus of $P(x, y)$ such that

$$
\begin{aligned}
& \sqrt{x^{2}+y^{2}+8 y+16} \\
& -\sqrt{x^{2}+y^{2}-6 x+9}=5
\end{aligned}
$$

## List II

p. No such point $P$ exists
q. Line segment

$$
\begin{aligned}
& \sqrt{x^{2}+y^{2}+8 y+16} \\
& -\sqrt{x^{2}+y^{2}-6 x+9}= \pm 5
\end{aligned}
$$

c. The locus of $P(x, y)$ such

$$
\begin{aligned}
& \text { that } \sqrt{x^{2}+y^{2}+8 y+16} \\
& +\sqrt{x^{2}+y^{2}-6 x+9}=5
\end{aligned}
$$

d. The locus of $P(x, y)$ such

$$
\text { that } \sqrt{x^{2}+y^{2}+8 y+16}
$$

$$
-\sqrt{x^{2}+y^{2}-6 x+9}=7
$$

3. 

## - View Text Solution

4. 

View Text Solution

1. Line $A B$ passes through point $(2,3)$ and intersects the positive $x$ and $y$ axes at $\mathrm{A}(\mathrm{a}, 0)$ and $\mathrm{B}(0, \mathrm{~b})$ respectively. If the area of $\triangle A O B$ is 11 . then the value of $4 b^{2}+9 a^{2}$ is

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2. A point $A$ divides the join of $P(-5,1)$ and $Q(3,5)$ in the ratio $k: 1$. Then the integral value of $k$ for which the area of $A B C$, where $B$ is $(1,5)$ and $C$ is $(7,-2)$, is equal to 2 units in magnitude is

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3. The distance between the circumcenter and the orthocentre of the triangle whose vertices are $(0,0),(6,8)$, and $(-4,3)$ is $L$. Then the value of $\frac{2}{\sqrt{5}} L$ is
4. A man starts from the point $P(-3,4)$ and reaches point $Q(0,1)$ touching $x$ axis at $R$ such that $P R+R Q$ is minimum, then the point $R$ is

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5. Let $A(0,1), B(1,1), C(1,-1), D(-1,0)$ be four points. If P is any other point, then $P A+P B+P C+P D \geq d$, where [ $d$ ] represents greatest integer.

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6. A triangle ABC has vertices $A(5,1), B(-1,-7)$ and $C(1,4)$ respectively. $L$ be the line mirror passing through $C$ and parallel to $A B$ and a light ray eliminating from point A goes along the direction of internal bisector of the angle $A$, which meets the mirror and $B C$ at $E$, D
respectively. If sum of the areas of $\triangle A C E$ and $\triangle A B E$ is $K$ sq units then $\frac{2 K}{5}-6$ is

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7. If the area of the triangle formed by the points $(2 a, b)(a+b, 2 b+a)$, and $(2 b, 2 a)$ is 2 quinits, then the area of the triangle whose vertices are $(a+b, a-b),(3 b-a, b+3 a)$, and $(3 a-b, 3 b-a)$ will be $\qquad$

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8. Lines $L_{1}$ and $L_{2}$ have slopes m and n , respectively, suppose $L_{1}$ makes twice as large angle with the horizontal (mesured counter clockwise from the positive x-axis) as does $L_{2}$ and $L_{1}$ has 4 times the slope of $L_{2}$. If $L_{1}$ is not horizontal, then the value of the proudct mn equals.

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9. If lines $2 x-3 y+6=0$ and $k x+2 y+2=0$ cut the coordinate axes in concyclic points, then the value of $|k|$ is

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10. If from point $P(4,4)$ perpendiculars to the straight lines $3 x+4 y+5=0$ and $y=m x+7$ meet at $Q$ and $R$ area of triangle $P Q R$ is maximum, then m is equal to

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11. The value of $a$ for which the image of the point $(a, a-1)$ w.r.t the line mirror $3 x+y=6 a$ is the point $\left(a^{2}+1, a\right)$ is (A) 0 (B) 1 (C) 2 (D) none of these

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12. The maximum area of the convex polygon formed by joining the points $A(0,0), B\left(2 t^{2}, 0\right), C(18,2), D\left(\frac{8}{r^{2}}, 4\right)$ and $E(0,2)$ where $t \in R-\{0\}$ and interior angle at vertex $B$ is greater than or equal to $90^{\circ}$

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## Jee Main

1. The lines $p\left(p^{2}+1\right) x-y+q=0 \quad$ and
$\left(p^{2}+1\right)^{2} x+\left(p^{2}+1\right) y+2 q=0$ are perpendicular to a common line for
A. no value of $p$.
B. exactly one value of $p$.
C. exactly two values of $p$.
D. more than two values of $p$.

## Answer: B

2. If the line $2 x+y=k$ passes through the point which divides the line segment joining the points $(1,1)$ and $(2,4)$ in the ratio $3: 2$, then $k$ equals
A. $\frac{29}{5}$
B. 5
C. 6
D. $\frac{11}{5}$

## Answer: C

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3. The number of points, having both co-ordinates as integers, that lie in the interior of triangle with vertices $(0,0),(0,41)$, and $(41,0)$ is :
A. 901
B. 861
C. 820
D. 780

## Answer: D

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4. Let $k$ be an integer such that the triangle with vertices $(k,-3 k),(5, k)$ and $(-k, 2)$ has area $28 s q$. units. Then the orthocentre of this triangle is at the point : (1) $\left(1,-\frac{3}{4}\right)$ (2) $\left(2, \frac{1}{2}\right)$
$\left(2,-\frac{1}{2}\right)(4)\left(1, \frac{3}{4}\right)$
A. $\left(2, \frac{1}{2}\right)$
B. $\left(2,-\frac{1}{2}\right)$
C. $\left(1, \frac{3}{4}\right)$
D. $\left(1,-\frac{3}{4}\right)$

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5. If the orthocentre and centroid of a triangle are $(-3,5)$ and $(3,3)$ then its circumcentre is :
A. $\frac{3 \sqrt{5}}{2}$
B. $\sqrt{10}$
C. $2 \sqrt{10}$
D. $3 \frac{\sqrt{5}}{2}$

## Answer: D

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6. The straight line through a fixed point $(2,3)$ intersects the coordinate axes at distinct point $P$ and $Q$. If $O$ is the origin and the rectangle $O P R Q$ is
completed then the locus of $R$ is
A. $3 x+2 y=6 x y$
B. $3 x+2 y=6$
C. $2 x+3 y=x y$
D. $3 x+2 y=x y$

## Answer: D

## D Watch Video Solution

