

#### **MATHS**

#### **BOOKS - CENGAGE PUBLICATION**

## DIFFERENT PRODUCTS OF VECTORS AND THEIR **GEOMETRICAL APPLICATIONS**

#### Illustration

**1.** Find the angle between the vectors  $\hat{i} - 2\hat{j} + 3\hat{k}$  and  $3\hat{i} - 2\hat{j} + \hat{k}$ .



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**2.** If  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  are non-zero vectors such that  $\vec{a}$ .  $\vec{b} = \vec{a}$ .  $\vec{c}$ , then find the geometrical relation between the vectors.



**3.** if 
$$\vec{r}$$
.  $\vec{i} = \vec{r}$ .  $\vec{j} = \vec{r}$ .  $\vec{k}$  and  $|\vec{r}| = 6$ , then find vector  $\vec{r}$ .



- **4.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are unit vectors such that  $\vec{a} + \vec{b} + \vec{c} = 0$ , then the value of  $\vec{a}$ ,  $\vec{b} + \vec{b}$ ,  $\vec{c} + \vec{c}$ ,  $\vec{a}$  is
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- **5.** If  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  are mutually perpendicular vectors of equal magnitudes,
- then find the angle between vectors  $\vec{a}$  and  $\vec{a}$  +  $\vec{b}$  +  $\vec{c}$ 
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- **6.** If  $|\vec{a}| + |\vec{b}| = |\vec{c}|$  and  $\vec{a} + \vec{b} = \vec{c}$ , then find the angle between  $\vec{a}$  and  $\vec{b}$ 
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**7.** If three unit vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  satisfy  $\vec{a} + \vec{b} + \vec{c} = \vec{0}$ . Then find the angle between  $\vec{b}$  and  $\vec{c}$ .



**8.** If  $\theta$  is the angle between the unit vectors  $\vec{a}$  and  $\vec{b}$ , then prove that

$$\cos\left(\frac{\theta}{2}\right) = \frac{1}{2}\left|\vec{a} + \vec{b}\right|$$



- **9.** find the projection of the vector  $\hat{i} + 2\hat{j} + 3\hat{k}$  on the vector  $5\hat{i} 2\hat{j} + 4\hat{k}$ 
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**10.** If the scalar projection of vector  $x\hat{i} - \hat{j} + \hat{k}$  on vector  $4\hat{i} - 2\hat{j} + 5\hat{k}$  is  $\frac{1}{3\sqrt{5}}$ .

The find the value of x.



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**11.** If  $\vec{a} = x\hat{i} + (x - 1)\hat{j} + \hat{k}$  and  $\vec{b} = (x + 1)\hat{i} + \hat{j} + a\hat{k}$  make an acute angle

 $\forall x \in R$ , then find the values of a



**12.** If  $\vec{a}$ .  $\vec{i} = \vec{a}$ .  $(\hat{i} + \hat{j}) = \vec{a}$ .  $(\hat{i} + \hat{j} + \hat{k})$ . Then find the unit vector  $\vec{a}$ .



**13.** Prove by vector method that cos(A + B) = cosAcosB - sinAsinB



**14.** In any triangle ABC, prove the projection formula  $a = b\cos C + c\cos B$  using vector method.



**15.** Prove that an angle inscribed in a semi-circle is a right angle using vector method.



**16.** Using dot product of vectors, prove that a parallelogram, whose diagonals are equal, is a rectangle



17. If a + 2b + 3c = 4, then find the least value (to the nearest integer) of  $a^2 + b^2 + c^2$ 



## **18.** about to only mathematics



**19.** vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are of the same length and when taken pair-wise they form equal angles. If  $\vec{a} = \hat{i} + \hat{j}$  and  $\vec{b} = \hat{j} + \hat{k}$  then find vector  $\vec{c}$ .



**20.** if  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are there mutually perpendicular unit vectors and  $\vec{a}$  ia a unit vector then find the value of  $\left|2\vec{a} + \vec{b} + \vec{c}\right|^2$ 



**21.** A particle acted by constant forces  $4\hat{i} + \hat{j} - 3\hat{k}$  and  $3\hat{i} + 9\hat{j} - \hat{k}$  is displaced from point  $\hat{i} + 2\hat{j} + 3\hat{k}$  to point  $5\hat{i} + 4\hat{j} + \hat{k}$  find the total work done by the forces in SI units.



**22.** If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are mutually perpendicular vectors of equal magnitude show that  $\vec{a}$  +  $\vec{b}$  +  $\vec{c}$  is equally inclined to  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$ 



**23.** If 
$$\vec{a} = 4\hat{i} + 6\hat{j}$$
 and  $\vec{b} = 3\hat{i} + 4\hat{k}$  find the projection vector  $\vec{a}$  to  $\vec{b}$ .



**24.** If 
$$|\vec{a}| = |\vec{b}| = |\vec{a} + \vec{b}| = 1$$
 then find the value of  $|\vec{a} - \vec{b}|$ 



**25.** If  $\vec{a} = -\hat{i} + \hat{j} + \hat{k}$  and  $\vec{b} = 2\hat{i} + 0\hat{j} + \hat{k}$  then find vector  $\vec{c}$  satisfying the following conditions, (i) that it is coplaner with  $\vec{a}$  and  $\vec{b}$ , (ii) that it is  $\perp to\vec{b}$  and (iii) that  $\vec{a} \cdot \vec{c} = 7$ .



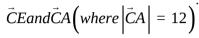
**26.** Let 
$$\vec{a}$$
,  $\vec{b}$ , and  $\vec{c}$  are vectors such that  $|\vec{a}| = 3$ ,  $|\vec{b}| = 4$  and  $|\vec{c}| = 5$ , and  $(\vec{a} + \vec{b})$  is perpendicular to  $\vec{c}$ ,  $(\vec{b} + \vec{c})$  is perpendicular to  $\vec{a}$  and  $(\vec{c} + \vec{a})$  is perpendicular to  $\vec{b}$ . Then find the value of  $|\vec{a} + \vec{b} + \vec{c}|$ .



**27.** Prove that in a tetrahedron if two pairs of opposite edges are perpendicular, then the third pair is also perpendicular.



**28.** In isosceles triangles ABC,  $\left| \vec{A}B \right| = \left| \vec{B}C \right| = 8$ , a point E divides AB internally in the ratio 1:3, then find the angle between





**29.** An arc AC of a circle subtends a right angle at then the center O. the point B divides the arc in the ratio 1:2, If  $\overrightarrow{O}A = a \& \overrightarrow{O}B = b$ . then the vector  $\overrightarrow{O}C$  in terms of a&b, is



**30.** Vector  $\vec{O}A = \hat{i} + 2\hat{j} + 2\hat{k}$  turns through a right angle passing through the positive x-axis on the way. Show that the vector in its new position is  $4\hat{i} - \hat{j} - \hat{k}$ .



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31. The foot of the perpendicular drawn from the origin to a plane is (1, 2, -3) Find the equation of the plane. or If O is the origin and the coordinates of P is (1, 2, -3), then find the equation of the plane passing through P and perpendicular to OP



**32.** Find 
$$|\vec{a} \times \vec{b}|$$
, if  $\vec{a} = \hat{i} - 7\hat{j} + 7\hat{k}$  and  $\vec{b} = 3\hat{i} - 2\hat{j} + 2\hat{k}$ .



the vectors  $\vec{a}$  and  $\vec{b}$  be 33. Let such that  $\left| \vec{a} \right| = 3$  and  $\left| \vec{b} \right| = \frac{\sqrt{2}}{3}$ , then,  $\vec{a} \times \vec{b}$  is a unit vector, if the angel between  $\vec{a}$  and  $\vec{b}$  is?



**34.** Prove that 
$$(\vec{a} - \vec{b}) \times (\vec{a} + \vec{b}) = 2(\vec{a} \times \vec{b})$$
.



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**35.** Let  $\vec{a} = \hat{i} + 4\hat{j} + 2\hat{k}$ ,  $\vec{b} = 3\hat{i} - 2\hat{j} + 7\hat{k}$  and  $\vec{c} = 2\hat{i} - \hat{j} + 4\hat{k}$  Find a vector  $\vec{d}$ which is perpendicular to both  $\vec{a}$  and  $\vec{b}$  and  $\vec{c}$ .  $\vec{d}$  = 15.



**36.** If A, BandC are the vetices of a triangle ABC, then prove sine rule

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$



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product of vectors , prove Using cross 37. that sin(A + B) = sinAcosB + cosAsinB.

**38.** Find a unit vector perpendicular to the plane determined by the points (1, -1, 2), (2, 0, -1) and (0, 2, 1)



**39.** If 
$$\vec{a}$$
 and  $\vec{b}$  are two vectors, then prove that  $(\vec{a} \times \vec{b})^2 = \begin{vmatrix} \vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b} \end{vmatrix}$ .



**40.** If 
$$|\vec{a}| = 2$$
, then find the value of  $|\vec{a} \times \hat{i}|^2 + |\vec{a} \times \hat{j}|^2 + |\vec{a} \times \hat{k}|^2$ 



**41.**  $\vec{r} \times \vec{a} = \vec{b} \times \vec{a}, \vec{r} \times \vec{b} = \vec{a} \times \vec{b}, \vec{a} \neq \vec{0}, \vec{b} \neq \vec{0}, \vec{a} \neq \lambda \vec{b}$  and  $\vec{a}$  is not perpendicular to  $\vec{b}$ , then find  $\vec{r}$  in terms of  $\vec{a}$  and  $\vec{b}$ .



**42.**  $\vec{A}$ ,  $\vec{B}$ ,  $\vec{C}$  and  $\vec{D}$  are any four points in the space, then prove that  $|\vec{A}\vec{B} \times \vec{C}\vec{D} + \vec{B}\vec{C} \times \vec{A}\vec{D} + \vec{C}\vec{A} \times \vec{B}\vec{D}| = 4$  (area of  $\vec{A}\vec{B}\vec{C}$ ).



**43.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are the position vectors of the vertices A,B and C. respectively, of  $\triangle$  ABC. Prove that the perpendicualar distance of the vertex A from the base BC of the triangle ABC is  $\frac{\left|\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a}\right|}{\left|\vec{c} \times \vec{c} + \vec{c} \times \vec{c}\right|}$ 



**44.** Using vectors, find the area of the triangle with vertices A (1, 1, 2), B (2, 3, 5) and C (1, 5, 5).



**45.** Find the area of the parallelogram whose adjacent sides are given by the vectors  $\vec{a} = \hat{i} - \hat{j} + 3\hat{k}$  and  $\vec{b} = 2\hat{i} - 7\hat{j} + \hat{k}$ 

are



**46.** Find the area of a parallelogram whose diagonals  $\vec{a} = 3\hat{i} + \hat{j} - 2\hat{k}$  and  $\vec{b} = \hat{i} - 3\hat{j} + 4\hat{k}$ 



**47.** Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be three verctors such that  $\vec{a} \neq 0$ ,  $|\vec{a}| = |\vec{c}| = 1$ ,  $|\vec{b}| = 4$  and  $|\vec{b} \times \vec{c}| = \sqrt{15}$  If  $\vec{b} - 2\vec{c} = \lambda \vec{a}$ , then find the value of  $\lambda$ 

**48.** Find the moment about (1,-1,-1) of the force  $3\hat{i} + 4\hat{j} - 5\hat{k}$  acting at (1,0,-2)



**49.** A rigid body is spinning about a fixed point (3,-2,-1) with an angular velocity of 4 rad/s, the axis of rotation being in the direction of (1,2,-2).

**50.** If  $\vec{a} \times \vec{b} = \vec{c} \times \vec{d}$  and  $\vec{a} \times \vec{c} = \vec{b} \times \vec{d}$ , then show that  $\vec{a} - \vec{d}$ , is parallel to

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Find the velocity of the particle at point (4,1,1).

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 $\vec{b} - \vec{c}$ 

**51.** Show by a numerical example and geometrically also that  $\vec{a} \times \vec{b} = \vec{a} \times \vec{c}$  does not imply  $\vec{b} = \vec{\cdot}$ 



**52.** If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  and  $\vec{d}$  are the position vectors of the vertices of a cyclic quadrilateral *ABCD*, prove that

$$\frac{\left|\vec{a}\times\vec{b}+\vec{b}\times\vec{d}+\vec{d}\times\vec{a}\right|}{\left(\vec{b}-\vec{a}\right).\left(\vec{d}-\vec{a}\right)}+\frac{\left|\vec{b}\times\vec{c}+\vec{c}\times\vec{d}+\vec{d}\times\vec{b}\right|}{\left(\vec{b}-\vec{c}\right).\left(\vec{d}-\vec{c}\right)}=0$$



**53.** The position vectors of the vertices of a quadrilateral with A as origin are  $B(\vec{b})$ ,  $D(\vec{d})$  and  $C(l\vec{b} + m\vec{d})$ . Prove that the area of the quadrialateral is  $\frac{1}{2}(l+m)|\vec{b} \times \vec{d}|$ .



**54.** Let  $\vec{a}$  and  $\vec{b}$  be unit vectors such that  $|\vec{a} + \vec{b}| = \sqrt{3}$ . Then find the value of  $(2\vec{a} + 5\vec{b})$ .  $((3\vec{a} + \vec{b} + \vec{a} \times \vec{b}))$ 



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**55.** u and v are two non-collinear unit vectors such that  $|\hat{u} \times \hat{v}| = \left| \frac{u - v}{2} \right|$ .

Find the value of  $|\hat{u} \times (\hat{u} \times \hat{v})|^2$ 



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**56.** In triangle ABC points D, EandF are taken on the sides BC, CAandAB,

 $\frac{BD}{DC} = \frac{CE}{FA} = \frac{AF}{FR} = n$  Prove such that respectively, that  $\triangle DEF = \frac{n^2 - n + 1}{(n+1)^2} \triangle (ABC)$ 

Let A, B, C be points with position vectors

$$2\hat{i} - \hat{j} + \hat{k}$$
,  $\hat{i} + 2\hat{j} + 3\hat{k}$  and  $3\hat{i} + \hat{j} + 2\hat{k}$  respectively. Find the shortest distance



between point B and plane OAC

**57.** 

**58.** Let  $\vec{a} = x\hat{i} + 12\hat{j} - \hat{k}$ ,  $\vec{b} = 2\hat{i} + 2x\hat{j} + \hat{k}$  and  $\vec{c} = \hat{i} + \hat{k}$  If the ordered set

$$\begin{bmatrix} \vec{b} \vec{c} \vec{a} \end{bmatrix}$$
 is left handed, then find the values of  $x$ 



**59.** If  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  are three non-coplanar vectors, then find the value of

$$\frac{\vec{a}.\left(\vec{b}\times\vec{c}\right)}{\vec{b}.\left(\vec{c}\times\vec{a}\right)} + \frac{\vec{b}.\left(\vec{c}\times\vec{a}\right)}{\vec{c}.\left(\vec{a}\times\vec{b}\right)} + \frac{\vec{c}.\left(\vec{b}\times\vec{a}\right)}{\vec{a}.\left(\vec{b}\times\vec{c}\right)}$$



**60.** If the vectors  $2\hat{i} - 3\hat{j}$ ,  $\hat{i} + \hat{j} - \hat{k}$  and  $3\hat{i} - \hat{k}$  form three concurrent edges of a parallelepiped, then find the volume of the parallelepiped.



**61.** The position vectors of the four angular points of a tetrahedron are  $A(\hat{j} + 2\hat{k})$ ,  $B(3\hat{i} + \hat{k})$ ,  $C(4\hat{i} + 3\hat{j} + 6\hat{k})$  and  $D(2\hat{i} + 3\hat{j} + 2\hat{k})$ . Find the volume



**62.** Let  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  be three unit vectors and  $\vec{a}$ .  $\vec{b} = \vec{a}$ .  $\vec{c} = 0$ . If the angle between  $\vec{b}$  and  $\vec{c}$  is  $\frac{\pi}{3}$  then find the value of  $\left| \left[ \vec{a} \vec{b} \vec{c} \right] \right|$ 



**64.** Prove that 
$$\begin{bmatrix} \vec{l} \vec{m} \vec{n} \end{bmatrix} \begin{bmatrix} \vec{a} \vec{b} \vec{c} \end{bmatrix} = \begin{vmatrix} \vec{l} \cdot \vec{a} & \vec{l} \cdot \vec{b} & \vec{l} \cdot \vec{c} \\ \vec{m} \cdot \vec{a} & \vec{m} \cdot \vec{b} & \vec{m} \cdot \vec{c} \\ \vec{n} \cdot \vec{a} & \vec{n} \cdot \vec{b} & \vec{n} \cdot \vec{c} \end{vmatrix}$$

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$$\begin{vmatrix} \vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} & \vec{a} \cdot \vec{c} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b} & \vec{b} \cdot \vec{c} \\ \vec{c} \cdot \vec{a} & \vec{c} \cdot \vec{b} & \vec{c} \cdot \vec{c} \end{vmatrix}$$
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**66.** Find the value of a so that the volume of the parallelepiped formed by vectors  $\hat{i} + a\hat{j} + k$ ,  $\hat{j} + a\hat{k}$  and  $a\hat{i} + \hat{k}$  becomes minimum.

**65.** If  $\vec{a} = \hat{i} + \hat{j} + \hat{k}$ ,  $\hat{b} = \hat{i} - \hat{j} + \hat{k}$ ,  $\vec{c} = \hat{i} + 2\hat{j} - \hat{k}$ , then find the value of



**67.** If  $\vec{u}$ ,  $\vec{v}$  and  $\vec{w}$  are three non-coplanar vectors, then prove that

$$\left(\vec{u} + \vec{v} - \vec{w}\right) \cdot \left[\left[\left(\vec{u} - \vec{v}\right) \times \left(\vec{v} - \vec{w}\right)\right]\right] = \vec{u} \cdot \left(\vec{v} \times \vec{w}\right)$$

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**68.** If  $\vec{a}$  and  $\vec{b}$  are two vectors, such that  $\left| \vec{a} \times \vec{b} \right| = 2$ , then find the value of  $\left[ \vec{a} \vec{b} \ \vec{a} \times \vec{b} \right]$ .



**69.** Find the altitude of a parallelopiped whose three coterminous edges are vectors  $\vec{A} = \hat{i} + \hat{j} + \hat{k}$ ,  $\vec{B} = 2\hat{i} + 4\hat{j} - \hat{k}$  and  $\vec{C} = \hat{i} + \hat{j} + 3\hat{k}$  with  $\vec{A}$  and  $\vec{B}$  as the sides of the base of the parallopiped.



**70.** If 
$$\begin{bmatrix} \vec{a} \ \vec{b} \ \vec{c} \end{bmatrix} = 2$$
, then find the value of  $\begin{bmatrix} (\vec{a} + 2\vec{b} - \vec{c})(\vec{a} - \vec{b})(\vec{a} - \vec{b} - \vec{c}) \end{bmatrix}$ 



**71.** If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are mutually perpendicular vector and  $\vec{a} = \alpha (\vec{a} \times \vec{b}) + \beta (\vec{b} \times \vec{c}) + \gamma (\vec{c} \times \vec{a})$  and  $[\vec{a}\vec{b}\vec{c}] = 1$ , then  $\alpha + \beta + \gamma = (A)$   $|\vec{a}|^2$  (B) -  $|\vec{a}|^2$  (C) 0 (D) none of these



**72.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are non-coplanar vecotrs, then prove that  $\left| \left( \vec{a} \cdot \vec{d} \right) \left( \vec{b} \times \vec{c} \right) + \left( \vec{b} \cdot \vec{d} \right) \left( \vec{c} \times \vec{a} \right) + \left( \vec{c} \cdot \vec{d} \right) \left( \vec{a} \times \vec{b} \right) \right|$  is independent of  $\vec{d}$  where  $\vec{d}$  is a unit vector.



**73.** Prove that vectors  $\vec{u} = (al + a_1l_1)\hat{i} + (am + a_1m_1)\hat{j} + (an + a_1n_1)\hat{k}$ 

$$\vec{v} = (bl + b_1 l_1)\hat{i} + (bm + b_1 m_1)\hat{j} + (bn + b_1 n_1)\hat{k}$$

$$\vec{w} = \left(cl + c_1 l_1\right)\hat{i} + \left(cm + c_1 m_1\right)\hat{j} + \left(cn + c_1 n_1\right)\hat{k} \text{ are coplanar.}$$



**74.** Let  $G_1$ ,  $G_2$  and  $G_3$  be the centroids of the triangular faces OBC, OCA and OAB, respectively, of a tetrahedron OABC If  $V_1$  denotes the volumes of the tetrahedron OABC and  $V_2$  that of the parallelepiped with  $OG_1$ ,  $OG_2$  and  $OG_3$  as three concurrent edges, then prove that  $AV_1 = 9V_2$ 



**75.** Prove that  $\hat{i} \times (\vec{a} \times \vec{i}) + \hat{j} \times (\vec{a} \times \vec{j}) + \hat{k} \times (\vec{a} \times \vec{k}) = 2\vec{a}$ 



**76.** If  $\hat{i} \times \left[ \left( \vec{a} - \hat{j} \right) \times \hat{i} \right] + \hat{j} \times \left[ \left( \vec{a} - \hat{k} \right) \times \hat{j} \right] + \hat{k} \times \left[ \left( \vec{a} - \hat{i} \right) \times \hat{k} \right] = 0$ , then find vector  $\vec{a}$ .



**77.** Let 
$$\vec{a}$$
,  $\vec{b}$ , and  $\vec{c}$  be any three vectors, then prove that  $[\vec{a} \times \vec{b}\vec{b} \times \vec{c}\vec{c} \times \vec{a}] = [\vec{a}\vec{b}\vec{c}]^2$ 

**78.** For any four vectors prove that

$$(\vec{b} \times \vec{c}) \cdot (\vec{a} \times \vec{d}) + (\vec{c} \times \vec{a}) \cdot (\vec{b} \times \vec{d}) + (\vec{a} \times \vec{b}) \cdot (\vec{c} \times \vec{d}) = 0$$



**79.** If  $\vec{b}$  and  $\vec{c}$  are two non-collinear such that  $\vec{a} \mid |(\vec{b} \times \vec{c})$ . Then prove that  $(\vec{a} \times \vec{b})$ .  $(\vec{a} \times \vec{c})$  is equal to  $|\vec{a}|^2(\vec{b}.\vec{c})$ 

**80.** Find the vector of length 3 unit which is perpendicular to  $\hat{i} + \hat{j} + \hat{k}$  and lies in the plane of  $\hat{i} + \hat{j} + \hat{k}$  and  $2\hat{i} - 3\hat{j}$ .



**81.** Let  $\hat{a}$ ,  $\hat{b}$  ,and  $\hat{c}$  be the non-coplanar unit vectors. The angle between  $\hat{b}$  and  $\hat{c}$  is  $\alpha$ , between  $\hat{c}$  and  $\hat{a}$  is  $\beta$  and between  $\hat{a}$  and  $\hat{b}$  is  $\gamma$ . If  $A(\hat{a}\cos\alpha,0),B(\hat{b}\cos\beta,0)$  and  $C(\hat{c}\cos\gamma,0)$ , then show that in triangle

ABC, 
$$\frac{\left|\hat{a} \times \left(\hat{b} \times \hat{c}\right)\right|}{\sin A} = \frac{\left|\hat{b} \times \left(\hat{c} \times \hat{a}\right)\right|}{\sin B} = \frac{\left|\hat{c} \times \left(\hat{a} \times \hat{b}\right)\right|}{\sin C}$$

**82.** find the angle between the vectors  $\vec{a}=3~\hat{i}$ +2  $\hat{k}$  and



$$\vec{b} = 2\hat{i} - 2\hat{j} + 4\hat{k}$$

**83.** If  $\vec{b}$  is not perpendicular to  $\vec{c}$ , then find the vector  $\vec{r}$  satisfying the equation  $\vec{r} \times \vec{b} = \vec{a} \times \vec{b}$  and  $\vec{r} \cdot \vec{c} = 0$ .



**84.** If  $\vec{a}$  and  $\vec{b}$  are two given vectors and k is any scalar, then find the vector  $\vec{r}$  satisfying  $\vec{r} \times \vec{a} + k\vec{r} = \vec{b}$ .



**85.**  $\vec{r} \times \vec{a} = \vec{b} \times \vec{a}, \ \vec{r} \times \vec{b} = \vec{a} \times \vec{b}, \ \vec{a} \neq \vec{0}, \ \vec{b} \neq \vec{0}, \ \vec{a} \neq \lambda \vec{b} \ \text{and} \ \vec{a} \quad \text{is} \quad \text{not}$  perpendicular to  $\vec{b}$ , then find  $\vec{r}$  in terms of  $\vec{a}$  and  $\vec{b}$ .



**86.** if vectors  $3\hat{i} - 2\hat{j} + m\hat{k}$  and  $-2\hat{i} + \hat{j} + 4\hat{k}$  are perpendicular to each other, find the value of m



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**87.**  $\vec{b}$  and  $\vec{c}$  are unit vectors. Then for any arbitrary vector

$$\vec{a}$$
,  $\left(\left(\left(\vec{a} \times \vec{b}\right) + \left(\vec{a} \times \vec{c}\right)\right) \times \left(\vec{b} \times \vec{c}\right)\right) \vec{b}$  -  $\vec{c}$  is always equal to  $|\vec{a}|$  b.  $\frac{1}{2}|\vec{a}|$  c.

$$\frac{1}{3} |\vec{a}|$$
 d. none of these



If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are non-coplanar unit vectors such that

$$\vec{a} \times (\vec{b} \times \vec{c}) = \frac{\vec{b} + \vec{c}}{\sqrt{2}}$$
, then the angle between  $\vec{a}$  and  $\vec{b}$  is a.  $3\pi/4$  b.  $\pi/4$  c.

$$\pi/2 d. \pi$$



$$\vec{R} + \frac{\left[\vec{R}\vec{\beta} \times (\vec{\beta} \times \vec{\alpha})\right] \vec{\alpha}}{\left|\vec{\alpha} \times \vec{\beta}\right|^{2}} + \frac{\left[\vec{R}\vec{\alpha} \times (\vec{\alpha} \times \vec{\beta})\right] \vec{\beta}}{\left|\vec{\alpha} \times \vec{\beta}\right|^{2}} = \frac{\left[\vec{R}\vec{\alpha}\vec{\beta}\right] (\vec{\alpha} \times \vec{\beta})}{\left|\vec{\alpha} \times \vec{\beta}\right|^{2}}$$



- **90.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three non-zero non-coplanar vectors, then the value of  $(\vec{a}.\vec{a})\vec{b} \times \vec{c} + (\vec{a}.\vec{b})\vec{c} \times \vec{a} + (\vec{a}.\vec{c})\vec{a} \times \vec{b}.$ 
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- **91.** Find a set of vectors reciprocal to the set  $-\hat{i}+\hat{j}+\hat{k}$ ,  $\hat{i}-\hat{j}+\hat{k}$ ,  $\hat{i}+\hat{j}+\hat{k}$ 
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**92.** find the projection of 
$$3\hat{i} - \hat{j} + 4\hat{k}$$

on 
$$2\hat{i} + 3\hat{j} - 6\hat{k}$$



- **93.** Let  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  and  $\vec{a}'$ ,  $\vec{b}'$ ,  $\vec{c}'$  are reciprocal system of vectors, then prove that  $\vec{a}' \times \vec{b}' + \vec{b}' \times \vec{c}' + \vec{c}' \times \vec{a}' = \frac{\vec{a} + \vec{b} + \vec{c}}{\left[\vec{a}\vec{b}\vec{c}\right]}$ .
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- **94.**  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three non-coplanar vectors and  $\vec{r}$ . Is any arbitrary vector. Prove that  $\begin{bmatrix} \vec{b} \vec{c} \vec{r} \end{bmatrix} \vec{a} + \begin{bmatrix} \vec{c} \vec{a} \vec{r} \end{bmatrix} \vec{b} + \begin{bmatrix} \vec{a} \vec{b} \vec{r} \end{bmatrix} \vec{c} = \begin{bmatrix} \vec{a} \vec{b} \vec{c} \end{bmatrix} \vec{r}$ .
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 $3\hat{i} + 2\hat{j} - 6\hat{k}, 4\hat{i} - 3\hat{j} + \hat{k}, \hat{i} - 2\hat{j} + 3\hat{k}, 3\hat{i} - 2\hat{j} + \hat{k}$ 

95.

**96.** If  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  are non-zero vectors such that  $\vec{a}$ .  $\vec{b} = \vec{a}$ .  $\vec{c}$ , then find the geometrical relation between the vectors.

Find the angle between the following pairs of vectors





**98.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are unit vectors such that  $\vec{a} + \vec{b} + \vec{c} = 3$ , then the value of  $\vec{a}$ .  $\vec{b}$  +  $\vec{b}$ .  $\vec{c}$  +  $\vec{c}$ .  $\vec{a}$  is

**97.** if  $\vec{r}$ .  $\vec{i} = \vec{r}$ .  $\vec{j} = \vec{r}$ .  $\vec{k}$  and  $|\vec{r}| = 9$ , then find vector  $\vec{r}$ .



**99.** If  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  are mutually perpendicular vectors of equal magnitudes, then find the angle between vectors  $\vec{a}$  and  $\vec{a}$  +  $\vec{b}$  +  $\vec{c}$ 



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**100.** If  $\vec{a} + \vec{b} = \vec{c}$ , and a + b = c then the angle between  $\vec{a}$  and  $\vec{b}$  is



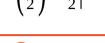
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**101.** If three unit vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  satisfy  $\vec{a} + \vec{b} + \vec{c} = \vec{0}$ . Then find the angle between  $\vec{a}$  and  $\vec{c}$ .



**102.** If  $\theta$  is the angle between the unit vectors  $\vec{a}$  and  $\vec{b}$ , then prove that

$$\sin\left(\frac{\theta}{2}\right) = \frac{1}{2}\left|\vec{a} - \vec{b}\right|$$





**103.** find the projection of the vector  $\hat{i} - 3\hat{j} - 7\hat{k}$  on the vector  $7\hat{i} - \hat{j} - 8\hat{k}$ 



**104.** If the scalar projection of vector 
$$x\hat{i} - \hat{j} + \hat{k}$$
 on vector  $2\hat{i} - \hat{j} + 5\hat{k}$ , is  $\frac{1}{\sqrt{30}}$ , then find the value of  $x$ 

**105.** If 
$$\vec{a} = x\hat{i} + (x-1)\hat{j} + \hat{k}$$
 and  $\vec{b} = (x+1)\hat{i} + \hat{j} + a\hat{k}$  make an acute angle  $\forall x \in R$ , then find the values of  $a$ 

**106.** If 
$$\vec{a}$$
.  $\vec{i} = \vec{a}$ .  $(\hat{i} + \hat{j}) = \vec{a}$ .  $(\hat{i} + \hat{j} + \hat{k})$ . Then find the unit vector  $\vec{a}$ .



# **107.** Prove by vector method that cos(A + B) = cosAcosB - sinAsinB



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using vector method.

**109.** Prove that an angle inscribed in a semi-circle is a right angle using vector method.

**108.** In any triangle ABC, prove the projection formula  $a = b\cos C + c\cos B$ 



**110.** Using dot product of vectors, prove that a parallelogram, whose diagonals are equal, is a rectangle



111. If a + 2b + 3c = 4, then find the least value (to the nearest integer) of  $a^2 + b^2 + c^2$ 



112. Definition of set



**113.** Vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are of the same length and when taken pair-wise they form equal angles. If  $\vec{a} = \hat{i} + \hat{j}$  and  $\vec{b} = \hat{j} + \hat{k}$  then find vector  $\vec{c}$ .



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**114.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three mutually perpendicular unit vectors and  $\vec{d}$  is a unit vector which makes equal angle with  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$ , then find the value of  $|\vec{a} + \vec{b} + \vec{c} + \vec{d}|^2$ .



**115.** A particle acted by constant forces  $4\hat{i} + \hat{j} - 3\hat{k}$  and  $3\hat{i} + 9\hat{j} - \hat{k}$  is displaced from point  $\hat{i} + 2\hat{j} + 3\hat{k}$  to point  $5\hat{i} + 4\hat{j} + \hat{k}$  find the total work done by the forces in SI units.



**116.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three mutually perpendicular vectors of equal magnitude, show that  $\vec{a} + \vec{b} + \vec{c}$  is equally inclined to  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$ . Also find the angle.



**117.** If 
$$\vec{a} = 4\hat{i} + 6\hat{j}$$
 and  $\vec{b} = 3\hat{i} + 4\hat{k}$  find the vector component of  $\vec{a}$  along  $\vec{b}$ .



**118.** If 
$$|\vec{a}| = |\vec{b}| = |\vec{a} + \vec{b}| = 1$$
 then find the value of  $|\vec{a} - \vec{b}|$ 



**119.** If 
$$\vec{a} = -\hat{i} + \hat{j} + \hat{k}$$
 and  $\vec{b} = 2\hat{i} + 0\hat{j} + \hat{k}$  then find vector  $\vec{c}$  satisfying the following conditions, (i) that it is coplaner with  $\vec{a}$  and  $\vec{b}$ , (ii) that it is  $\perp$  to  $\vec{b}$  and (iii) that  $\vec{a} \cdot \vec{c} = 7$ .

**120.** Let 
$$\vec{a}$$
,  $\vec{b}$ , and  $\vec{c}$  are vectors such that  $|\vec{a}| = 3$ ,  $|\vec{b}| = 4$  and  $|\vec{c}| = 5$ , and  $(\vec{a} + \vec{b})$  is perpendicular to  $\vec{c}$ ,  $(\vec{b} + \vec{c})$  is perpendicular to  $\vec{a}$  and  $(\vec{c} + \vec{a})$  is perpendicular to  $\vec{b}$ . Then find the value of  $|\vec{a} + \vec{b} + \vec{c}|$ .



**121.** Prove that in a tetrahedron if two pairs of opposite edges are perpendicular, then the third pair is also perpendicular.



**122.** In isosceles triangles 
$$ABC$$
,  $|\vec{A}B| = |\vec{B}C| = 8$ , a point  $E$  divides  $AB$  internally in the ratio 1:3, then find the angle between  $\vec{C}E$  and  $\vec{C}A$  (where  $|\vec{C}A| = 12$ )



**123.** An arc AC of a circle subtends a right angle at then the center O. the point B divides the arc in the ratio 1:2, If  $\overrightarrow{OA} = a \& \overrightarrow{OB} = b$ . then the vector OC in terms of a&b, is



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**124.** Vector  $\vec{O}A = \hat{i} + 2\hat{j} + 2\hat{k}$  turns through a right angle passing through the positive x-axis on the way. Show that the vector in its new position is  $4\hat{i} - \hat{j} - \hat{k}$ 



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125. The foot of the perpendicular drawn from the origin to a plane is (1, 2, -3) Find the equation of the plane. or If O is the origin and the coordinates of P is (1, 2, -3), then find the equation of the plane passing

through P and perpendicular to OP



**126.** Find 
$$|\vec{a} \times \vec{b}|$$
, if  $\vec{a} = 2\hat{i} - 7\hat{j} + 7\hat{k}$  and  $\vec{b} = 3\hat{i} - 2\hat{j} + 2\hat{k}$ 



**127.** Let the vectors 
$$\vec{a}$$
 and  $\vec{b}$  be such that  $|\vec{a}| = 3$  and  $|\vec{b}| = \frac{\sqrt{2}}{3}$ , then,  $\vec{a} \times \vec{b}$  is a unit vector, if the angel between  $\vec{a}$  and  $\vec{b}$  is?

**128.** Prove that  $(\vec{a} - \vec{b}) \times (\vec{a} + \vec{b}) = 2(\vec{a} \times \vec{b})$ .

**129.** answer any one question : (ii)

$$\vec{a} = \hat{i} + 4\hat{j} + 2\hat{k}$$
,  $\vec{b} = 3\hat{i} - 2\hat{j} + 7\hat{k}$  and  $\vec{c} = 2\hat{i} - \hat{j} + 4\hat{k}$ . Find a vector  $\vec{d}$  which is perpendicular to both the vectors  $\vec{a}$  and  $\vec{b}$  and  $\vec{c} \cdot \vec{d} = 18$ 

let



**130.** If A, B and C are the vetices of a triangle ABC, then prove sine rule

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$



**131.** Using cross product of vectors , prove that sin(A + B) = sinAcosB + cosAsinB .



**132.** Find a unit vector perpendicular to the plane determined by the points (1, -1, 2), (2, 0, -1) and (0, 2, 1)



**133.** If 
$$\vec{a}$$
 and  $\vec{b}$  are two vectors, then prove that  $(\vec{a} \times \vec{b})^2 = \begin{vmatrix} \vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b} \end{vmatrix}$ .



**134.** If 
$$|\vec{a}| = 2$$
, then find the value of  $|\vec{a} \times \hat{i}|^2 + |\vec{a} \times \hat{j}|^2 + |\vec{a} \times \hat{k}|^2$ .



**135.**  $\vec{r} \times \vec{a} = \vec{b} \times \vec{a}, \vec{r} \times \vec{b} = \vec{a} \times \vec{b}, \vec{a} \neq \vec{0}, \vec{b} \neq \vec{0}, \vec{a} \neq \lambda \vec{b}$  and  $\vec{a}$  is not perpendicular to  $\vec{b}$ , then find  $\vec{r}$  in terms of  $\vec{a}$  and  $\vec{b}$ .



**136.** A, B, CandD are any four points in the space, then prove that

$$|\vec{A}B \times \vec{C}D + \vec{B}C \times \vec{A}D + \vec{C}A \times \vec{B}D| = 4 \text{ (area of } ABC \text{ )}.$$



**137.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are the position vectors of the vertices A,B and C. respectively of  $\triangle$  ABC. Prove that the perpendicualar distance of the

vertex A from the base BC of the triangle ABC is 
$$\frac{\left|\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a}\right|}{\left|\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a}\right|}$$



**138.** Using vectors, find the area of the triangle with vertices A (1, 1, 2), B (2,

- 3, 5) and C (1, 5, 5).
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**139.** Find the area of the parallelogram whose adjacent sides are given by the vectors  $\vec{a} = \hat{i} + 2\hat{j} + 3\hat{k}$  and  $\vec{b} = 2\hat{i} - 5\hat{j} + 2\hat{k}$ 

**140.** Find the area of a parallelogram whose diagonals are 
$$\vec{a} = 3\hat{i} + \hat{j} - 2\hat{k}$$
 and  $\vec{b} = \hat{i} - 3\hat{j} + 4\hat{k}$ 

**141.** Let 
$$\vec{a}$$
,  $\vec{b}$  and  $\vec{c}$  be three verctors such that  $\vec{a} \neq 0$ ,  $|\vec{a}| = |\vec{c}| = 1$ ,  $|\vec{b}| = 4$  and  $|\vec{b} \times \vec{c}| = \sqrt{15}$  If  $\vec{b} - 2\vec{c} = \lambda \vec{a}$ , then find the value of  $\lambda$ 



**142.** Find the moment about (1,-1,-1) of the force  $3\hat{i} + 4\hat{j} - 5\hat{k}$  acting at (1,0,-2)

**143.** A rigid body is spinning about a fixed point (3,-2,-1) with an angular velocity of 4 rad/s, the axis of rotation being in the direction of (1,2,-2). Find the velocity of the particle at point (4,1,1).



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**144.** If  $\vec{a} \times \vec{b} = \vec{c} \times \vec{d}$  and  $\vec{a} \times \vec{c} = \vec{b} \times \vec{d}$ ,  $\vec{a} \neq \vec{d}$ ,  $\vec{b} \neq \vec{c}$  then show that  $\vec{b} - \vec{c}$ is parallel to  $\vec{a} - \vec{d}$ 



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145. Show by a numerical example and geometrically also that

$$\vec{a} \times \vec{b} = \vec{a} \times \vec{c}$$
 does not imply  $\vec{b} = \vec{\cdot}$ 



**146.** If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  and  $\vec{d}$  are the position vectors of the vertices of a cycle

quadrilateral that ABCD. prove

$$\frac{\left|\vec{a}\times\vec{b}+\vec{b}\times\vec{d}+\vec{d}\times\vec{a}\right|}{\left(\vec{b}-\vec{a}\right).\left(\vec{d}-\vec{a}\right)}+\frac{\left|\vec{b}\times\vec{c}+\vec{c}\times\vec{d}+\vec{d}\times\vec{b}\right|}{\left(\vec{b}-\vec{c}\right).\left(\vec{d}-\vec{c}\right)}=0$$



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**147.** The position vectors of the vertices of a quadrilateral with A as origin are  $B(\vec{b})$ ,  $D(\vec{d})$  and  $C(l\vec{b} + m\vec{d})$ . Prove that the area of the quadrial ateral is  $\frac{1}{2}(l+m)|\vec{b}\times\vec{d}|$ 



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**148.** Let  $\vec{a}$  and  $\vec{b}$  be unit vectors such that  $|\vec{a} + \vec{b}| = \sqrt{3}$ . Then find the value of  $(2\vec{a} + 5\vec{b})$ .  $((3\vec{a} + \vec{b} + \vec{a} \times \vec{b}))$ 



**149.**  $\hat{u}$  and  $\hat{v}$  are two non-collinear unit vectors such that

$$\left| \frac{\hat{u} + \hat{v}}{2} + \hat{u} \times \vec{v} \right| = 1$$
. Prove that  $\left| \hat{u} \times \hat{v} \right| = \left| \frac{\hat{u} - \hat{v}}{2} \right|$ 



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**150.** In triangle ABC ,points D, EandF are taken on the sides

BC, CAandAB, respectively, such that  $\frac{BD}{DC} = \frac{CE}{EA} = \frac{AF}{FR} = n$  Prove that

$$\triangle DEF = \frac{n^2 - n + 1}{(n+1)^2} \triangle (ABC)$$



Let A, B, C be points with position vectors 151.  $2\hat{i} - \hat{j} + \hat{k}$ ,  $\hat{i} + 2\hat{j} + 3\hat{k}$  and  $3\hat{i} + \hat{j} + 2\hat{k}$  respectively. Find the shortest distance

between point B and plane OAC



**152.** Let  $\vec{a} = x\hat{i} + 12\hat{j} - \hat{k}$ ,  $\vec{b} = 2\hat{i} + 2x\hat{j} + \hat{k}$  and  $\vec{c} = \hat{i} + \hat{k}$  If the ordered set

$$\begin{bmatrix} \vec{b} \vec{c} \vec{a} \end{bmatrix}$$
 is left handed, then find the values of  $\vec{x}$ 



**153.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three non-coplanar vectors, then find the value of

$$\frac{\vec{a}.\left(\vec{b}\times\vec{c}\right)}{\vec{b}.\left(\vec{c}\times\vec{a}\right)} + \frac{\vec{b}.\left(\vec{c}\times\vec{a}\right)}{\vec{c}.\left(\vec{a}\times\vec{b}\right)} + \frac{\vec{c}.\left(\vec{b}\times\vec{a}\right)}{\vec{a}.\left(\vec{b}\times\vec{c}\right)}$$



**154.** If the vectors  $2\hat{i} - 3\hat{j}$ ,  $\hat{i} + \hat{j} - \hat{k}$  and  $3\hat{i} - \hat{k}$  form three concurrent edges of a parallelepiped, then find the volume of the parallelepiped.



**155.** The position vectors of the four angular points of a tetrahedron are

$$A(\hat{j}+2\hat{k})$$
,  $B(3\hat{i}+\hat{k})$ ,  $C(4\hat{i}+3\hat{j}+6\hat{k})$  and  $D(2\hat{i}+3\hat{j}+2\hat{k})$ . Find the volume of the tetrahedron  $ABCD$ 



**156.** Let  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  be three unit vectors and  $\vec{a}$ .  $\vec{b} = \vec{a}$ .  $\vec{c} = 0$ . If the angle between  $\vec{b}$  and  $\vec{c}$  is  $\frac{\pi}{3}$  then find the value of  $\left| \left[ \vec{a} \vec{b} \vec{c} \right] \right|$ 



**157.** Prove that  $\begin{bmatrix} \vec{a} + \vec{b} \ \vec{b} + \vec{c} \ \vec{c} + \vec{a} \end{bmatrix} = 2 \begin{bmatrix} \vec{a} \ \vec{b} \ \vec{c} \end{bmatrix}$ 



**158.** Prove that 
$$[\vec{l} \, \vec{m} \, \vec{n}] [\vec{a} \, \vec{b} \, \vec{c}] = \begin{vmatrix} \vec{l} \, . \, \vec{a} & \vec{l} \, . \, \vec{b} & \vec{l} \, . \, \vec{c} \\ \vec{m} \, . \, \vec{a} & \vec{m} \, . \, \vec{b} & \vec{m} \, . \, \vec{c} \\ \vec{n} \, . \, \vec{a} & \vec{n} \, . \, \vec{b} & \vec{n} \, . \, \vec{c} \end{vmatrix}$$

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**159.** If 
$$\vec{a} = \hat{i} + \hat{j} + \hat{k}$$
,  $\hat{b} = \hat{i} - \hat{j} + \hat{k}$ ,  $\vec{c} = \hat{i} + 2\hat{j} - \hat{k}$ , then find the value of

$$\begin{vmatrix} \vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} & \vec{a} \cdot \vec{c} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b} & \vec{b} \cdot \vec{c} \\ \vec{c} \cdot \vec{a} & \vec{c} \cdot \vec{b} & \vec{c} \cdot \vec{c} \end{vmatrix}$$



**160.** Find the value of a so that the volume of the parallelepiped formed by vectors  $\hat{i} + a\hat{j} + k$ ,  $\hat{j} + a\hat{k}$  and  $a\hat{i} + \hat{k}$  becomes minimum.



**161.** If  $\vec{u}, \vec{v}$  and  $\vec{w}$  are three non-coplanar vectors, then prove that

$$(\vec{u} + \vec{v} - \vec{w}).[[(\vec{u} - \vec{v}) \times (\vec{v} - \vec{w})]] = \vec{u}.(\vec{v} \times \vec{w})$$

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- **162.** If  $\vec{a}$  and  $\vec{b}$  are two vectors, such that  $|\vec{a} \times \vec{b}| = 2$ , then find the value of  $|\vec{a}\vec{b}|\vec{a} \times \vec{b}|$ .
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**163.** Find the altitude of a parallelopiped whose three coterminous edges are vectors  $\vec{A} = \hat{i} + \hat{j} + \hat{k}$ ,  $\vec{B} = 2\hat{i} + 4\hat{j} - \hat{k}$  and  $\vec{C} = \hat{i} + \hat{j} + 3\hat{k}$  with  $\vec{A}$  and  $\vec{B}$  as the sides of the base of the parallopiped.



**164.** If  $\left[\vec{a}\vec{b}\vec{c}\right] = 2$  , then find the value of  $\left[\left(\vec{a} + 2\vec{b} - \vec{c}\right)\left(\vec{a} - \vec{b}\right)\left(\vec{a} - \vec{b} - \vec{c}\right)\right]$ 

**165.** If 
$$\vec{a}$$
,  $\vec{b}$ ,  $\vec{c}$  are mutually perpendicular vector and  $\vec{a} = \alpha (\vec{a} \times \vec{b}) + \beta (\vec{b} \times \vec{c}) + \gamma (\vec{c} \times \vec{a})$  and  $[\vec{a}\vec{b}\vec{c}] = 1$ , then  $\alpha + \beta + \gamma = (A)$   $|\vec{a}|^2$  (B) -  $|\vec{a}|^2$  (C) 0 (D) none of these

**166.** i. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are non-coplanar vectors, prove that vectors  $3\vec{a} - 7\vec{b} - 4\vec{c}$ ,  $3\vec{a} - 2\vec{b} + \vec{c}$  and  $\vec{a} + \vec{b} + 2\vec{c}$  are coplanar.



167. Prove that vectors

$$\vec{u} = (al + a_1 l_1)\hat{i} + (am + a_1 m_1)\hat{j} + (an + a_1 n_1)\hat{k}$$

$$\vec{v} = (bl + b_1 l_1)\hat{i} + (bm + b_1 m_1)\hat{j} + (bn + b_1 n_1)\hat{k}$$

 $\vec{w} = (cl + c_1 l_1)\hat{i} + (cm + c_1 m_1)\hat{j} + (cn + c_1 n_1)\hat{k}$ are coplannar.



**168.** Let  $G_1, G_2$  and  $G_3$  be the centroids of the triangular faces OBC, OCA and OAB, respectively, of a tetrahedron OABC If  $V_1$  denotes the volumes of the tetrahedron  $OABCandV_2$  that of the parallelepiped with  $OG_1$ ,  $OG_2$  and  $OG_3$  as three concurrent edges, then prove that  $4V_1 = 9V_2$ 



**170.** If 
$$\hat{i} \times \left[ \left( \vec{a} - \hat{j} \right) \times \hat{i} \right] + \hat{j} \times \left[ \left( \vec{a} - \hat{k} \right) \times \hat{j} \right] + \vec{k} \times \left[ \left( \vec{a} - \vec{i} \right) \times \hat{k} \right] = 0$$
, then find vector  $\vec{a}$ .



**171.** Prove that: 
$$\begin{bmatrix} \vec{a} \times \vec{b} & \vec{b} \times \vec{c} & \vec{c} \times \vec{a} \end{bmatrix} = \begin{bmatrix} \vec{a}\vec{b}\vec{c} \end{bmatrix}^2$$

172.

$$(\vec{b} \times \vec{c}). (\vec{a} \times \vec{d}) + (\vec{c} \times \vec{a}). (\vec{b} \times \vec{d}) + (\vec{a} \times \vec{b}). (\vec{c} \times \vec{d}) = 0$$

Prove

that:



**173.** If  $\vec{b}$  and  $\vec{c}$  are two non-collinear such that  $\vec{a} \mid (\vec{b} \times \vec{c})$ . Then prove that  $(\vec{a} \times \vec{b})$ .  $(\vec{a} \times \vec{c})$  is equal to  $|\vec{a}|^2 (\vec{b} \cdot \vec{c})$ .



**174.** Find the vector of length 3 unit which is perpendicular to  $\hat{i} + \hat{j} + \hat{k}$  and lies in the plane of  $\hat{i} + \hat{j} + \hat{k}$  and  $2\hat{i} - 3\hat{j}$ .



**175.** Let  $\hat{a}$ ,  $\hat{b}$  ,and  $\hat{c}$  be the non-coplanar unit vectors. The angle between  $\hat{b}$  and  $\hat{c}$  is  $\alpha$ , between  $\hat{c}$  and  $\hat{a}$  is  $\beta$  and between  $\hat{a}$  and  $\hat{b}$  is  $\gamma$ . If  $A(\hat{a}\cos\alpha,0),B(\hat{b}\cos\beta,0)$  and  $C(\hat{c}\cos\gamma,0)$ , then show that in triangle

$$ABC, \ \frac{\left|\hat{a} \times \left(\hat{b} \times \hat{c}\right)\right|}{\sin A} = \frac{\left|\hat{b} \times \left(\hat{c} \times \hat{a}\right)\right|}{\sin B} = \frac{\left|\hat{c} \times \left(\hat{a} \times \hat{b}\right)\right|}{\sin C}$$



**176.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three non-coplanar non-zero vectors, then prove that  $(\vec{a}.\vec{a})\vec{b} \times \vec{c} + (\vec{a}.\vec{b})\vec{c} \times \vec{a} + (\vec{a}.\vec{c})\vec{a} \times \vec{b} = [\vec{b}\vec{c}\vec{a}]\vec{a}$ 



**177.** If  $\vec{b}$  is not perpendicular to  $\vec{c}$  . Then find the vector  $\vec{r}$  satisfying the equation  $\vec{r} \times \vec{b} = \vec{a} \times \vec{b}$  and  $\vec{r} \cdot \vec{c} = 0$ 



178. If  $\vec{a}$  and  $\vec{b}$  are two given vectors and k is any scalar, then find the vector  $\vec{r}$  satisfying  $\vec{r} \times \vec{a} + k\vec{r} = \vec{b}$ .



**179.**  $\vec{r} \times \vec{a} = \vec{b} \times \vec{a}, \ \vec{r} \times \vec{b} = \vec{a} \times \vec{b}, \ \vec{a} \neq \vec{0}, \ \vec{b} \neq \vec{0}, \ \vec{a} \neq \lambda \vec{b} \ \text{and} \ \vec{a} \ \text{is} \ \text{not}$  perpendicular to  $\vec{b}$ , then find  $\vec{r}$  in terms of  $\vec{a}$  and  $\vec{b}$ .

**180.** If vector 
$$\vec{x}$$
 satisfying  $\vec{x} \times \vec{a} + (\vec{x}.\vec{b})\vec{c} = \vec{d}$  is given  $\vec{x} = \lambda \vec{a} + \vec{a} \times \frac{\vec{a} \times (\vec{d} \times \vec{c})}{(\vec{a}.\vec{c})|\vec{a}|^2}$ , then find the value of  $\lambda$ 

**181.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be three non-coplanar vectors and a',b' and c' constitute

the reciprocal system of vectors, then prove that 
$$i. \ \vec{r} = (\vec{r}. \ \vec{a}') \vec{a} + (\vec{r}. \ \vec{b}') \vec{b} + (\vec{r}. \ \vec{c}') \vec{c}$$
$$ii. \ \vec{r} = (\vec{r}. \ \vec{a}) \vec{a}' + (\vec{r}. \ \vec{b}) \vec{b}' + (\vec{r}. \ \vec{c}) \vec{c}'$$

$$\vec{a} imes \left( \vec{b} imes \vec{c} \right) = rac{\vec{b} + \vec{c}}{\sqrt{2}}, \, \vec{b} \, \, ext{and} \, \, \vec{c} \, \, \, ext{are non- parallel} \, \, , \, \, ext{then prove that the}$$

If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are non -coplanar unit vectors such

that

angle between  $\vec{a}$  and  $\vec{b}$  is  $3\pi/4$ 



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183. that Prove

**184.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three non-coplanar non-zero vectors, then prove

$$\vec{R} + \frac{\begin{bmatrix} \vec{R}\vec{\beta} \times (\vec{\beta} \times \vec{\alpha}) \end{bmatrix} \vec{\alpha}}{\begin{vmatrix} \vec{\alpha} \times \vec{\beta} \end{vmatrix}^2} + \frac{\begin{bmatrix} \vec{R}\vec{\alpha} \times (\vec{\alpha} \times \vec{\beta}) \end{bmatrix} \vec{\beta}}{\begin{vmatrix} \vec{\alpha} \times \vec{\beta} \end{vmatrix}^2} = \frac{\begin{bmatrix} \vec{R}\vec{\alpha}\vec{\beta} \end{bmatrix} (\vec{\alpha} \times \vec{\beta})}{\begin{vmatrix} \vec{\alpha} \times \vec{\beta} \end{vmatrix}^2}$$





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**185.** Find a set of vectors reciprocal to the set  $-\hat{i} + \hat{j} + \hat{k}$ ,  $\hat{i} - \hat{j} + \hat{k}$ ,  $\hat{i} + \hat{j} + \hat{k}$ 

that  $(\vec{a}.\vec{a})\vec{b} \times \vec{c} + (\vec{a}.\vec{b})\vec{c} \times \vec{a} + (\vec{a}.\vec{c})\vec{a} \times \vec{b} = [\vec{b}\vec{c}\vec{a}]\vec{a}$ 



**186.** Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be a set of non-coplanar vectors and  $\vec{a}'$   $\vec{b}'$  and  $\vec{c}'$  be its reciprocal set.

prove that 
$$\vec{a} = \frac{\vec{b}' \times \vec{c}'}{\left[\vec{a}' \, \vec{b}' \, \vec{c}'\right]}$$
,  $\vec{b} = \frac{\vec{c}' \times \vec{a}'}{\left[\vec{a}' \, \vec{b}' \, \vec{c}'\right]}$  and  $\vec{c} = \frac{\vec{a}' \times \vec{b}'}{\left[\vec{a}' \, \vec{b}' \, \vec{c}'\right]}$ 



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**187.** If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  and  $\vec{a}'$ ,  $\vec{b}'$ ,  $\vec{c}'$  are reciprocal system of vectors, then prove

that 
$$\vec{a}' \times \vec{b}' + \vec{b}' \times \vec{c}' + \vec{c}' \times \vec{a}' = \frac{\vec{a} + \vec{b} + \vec{c}}{\left[\vec{a}\vec{b}\vec{c}\right]}$$



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**188.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be three non-coplanar vectors and a',b' and c' constitute the reciprocal system of vectors, then prove that

$$i. \ \vec{r} = (\vec{r}. \ \vec{a}')\vec{a} + (\vec{r}. \ \vec{b}')\vec{b} + (\vec{r}. \ \vec{c}')\vec{c}$$

ii. 
$$\vec{r} = (\vec{r} \cdot \vec{a})\vec{a}' + (\vec{r} \cdot \vec{b})\vec{b}' + (\vec{r} \cdot \vec{c})\vec{c}'$$

### Exercise 2.1

**1.** Find 
$$|\vec{a}|$$
 and  $|\vec{b}|$ , if  $(\vec{a} + \vec{b})$ .  $(\vec{a} - \vec{b}) = 8$  and  $|\vec{a}| = 8 |\vec{b}|$ 



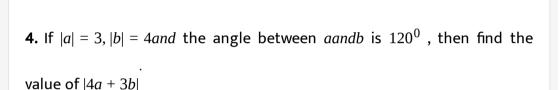
**2.** Show that  $|\vec{a}|\vec{b} + |\vec{b}|\vec{a}$  is a perpendicular to  $|\vec{a}|\vec{b} - |\vec{b}|\vec{a}$ , for any two non-zero vectors  $\vec{a}$  and  $\vec{b}$ .



respectively then find  $\angle ABC$ 



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**3.** If the vectors A, B, C of a triangle ABC are (1, 2, 3), (-1, 0, 0), (0, 1, 2),



**5.** If vectors 
$$\hat{i} - 2x\hat{j} - 3y\hat{k}$$
 and  $\hat{i} + 3x\hat{j} + 2y\hat{k}$  are orthogonal to each other, then find the locus of th point (x,y).



**6.** Let 
$$\vec{a}$$
,  $\vec{b}$  and  $\vec{c}$  be pairwise mutually perpendicular vectors, such that  $|\vec{a}| = 2$ ,  $|\vec{b}| = 3$ ,  $|\vec{c}| = 6$ , the find the length of  $\vec{a} + \vec{b} + \vec{c}$ .

**7.** If 
$$\vec{a} + \vec{b} + \vec{c} = 0$$
,  $|\vec{a}| = 3$ ,  $|\vec{b}| = 5$ ,  $|\vec{c}| = 7$ , then find the angle between  $\vec{b}$  and  $\vec{c}$ .



- **8.** If the angle between unit vectors  $\vec{a}$  and  $\vec{b}is120$  °. Then find the value of  $|\vec{a} + \vec{b}|$ .
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- **9.** Let  $\vec{u} = \hat{i} + \hat{j}$ ,  $\vec{v} = \hat{i} \hat{j}$  and  $\vec{w} = \hat{i} + 2\hat{j} + 3\hat{k}$ . If  $\hat{n}$  is a unit vector such that  $\vec{u} \cdot \hat{n} = 0$  and  $\vec{v} \cdot \hat{n} = 0$ ,  $|\vec{w} \cdot \hat{n}|$  is equal to (A) 0 (B) 1 (C) 2 (D) 3
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**10.** A, B, C, D are any four points, prove that

$$\vec{A}\vec{B}\vec{C}D + \vec{B}\vec{C}\vec{A}D + \vec{C}\vec{A}\vec{B}D = 4(Area\ of\ \triangle\ ABC).$$



**11.** P(1, 0, -1), Q(2, 0, -3), R(-1, 2, 0) and S(3, -2, -1), then find the projection length of  $\vec{P}Qon\vec{R}S$ 



**12.** If the vectors  $3\vec{p} + \vec{q}$ ;  $5p - 3\vec{q}$  and  $2\vec{p} + \vec{q}$ ;  $3\vec{p} - 2\vec{q}$  are pairs of mutually perpendicular vectors, then find the angle between vectors  $\vec{p}$  and  $\vec{q}$ 



**13.** Let  $\vec{A}$  and  $\vec{B}$  be two non-parallel unit vectors in a plane. If  $(\alpha \vec{A} + \vec{B})$ 

bisects the internal angle between  $\vec{A}$  and  $\vec{B}$ , then find the value of  $\alpha$ 



 $\vec{c}$  and  $\vec{x}$ 

- **14.** Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be unit vectors, such that  $\vec{a} + \vec{b} + \vec{c} = \vec{x}$ ,  $\vec{a}\vec{x} = 1$ ,  $\vec{b}\vec{x} = \frac{3}{2}$ ,  $|\vec{x}| = 2$ . Then find the angle between
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- **15.** If  $\vec{a}$  and  $\vec{b}$  are unit vectors, then find the greatest value of  $\left| \vec{a} + \vec{b} \right| + \left| \vec{a} - \vec{b} \right|.$ 
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**16.** Constant forces  $P_1 = \hat{i} + \hat{j} + \hat{k}$ ,  $P_2 = -\hat{i} + 2\hat{j} - \hat{k}$  and  $P_3 = -\hat{j} - \hat{k}$  act on a particle at a point  $\hat{A}$  Determine the work done when particle is displaced from position  $\hat{A}(4\hat{i} - 3\hat{j} - 2\hat{k})$  to  $\hat{B}(6\hat{i} + \hat{j} - 3\hat{k})$ 



**17.** Find 
$$|\vec{a}|$$
 and  $|\vec{b}|$ , if  $(\vec{a} + \vec{b})$ .  $(\vec{a} - \vec{b}) = 8$  and  $|\vec{a}| = 8|\vec{b}|$ 



**18.** If A, B, C, D are four distinct point in space such that AB is not perpendicular to CD and satisfies

$$\overrightarrow{AB}. \overrightarrow{CD} = k \left( \begin{vmatrix} \overrightarrow{AD} \end{vmatrix}^2 + \begin{vmatrix} \overrightarrow{BC} \end{vmatrix}^2 - \begin{vmatrix} \overrightarrow{AC} \end{vmatrix}^2 - \begin{vmatrix} \overrightarrow{DD} \end{vmatrix}^2 \right), \text{ then find the value of } k$$



1. If  $\vec{a} = 2\hat{i} + 3\hat{j} - 5\hat{k}$ ,  $\vec{b} = m\hat{i} + n\hat{j} + 12\hat{k}$  and  $\vec{a} \times \vec{b} = \vec{0}$ , then find (m, n)



**2.** Find  $\vec{a} \cdot \vec{b}$  if  $|\vec{a}| = 3$ ,  $|\vec{b}| = 5$ , and  $|\vec{a} \times \vec{b}| = 12$ 



**3.** If  $\vec{a} \times \vec{b} = \vec{b} \times \vec{c} \neq 0$  where  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are coplanar vectors, then for some scalar k prove that  $\vec{a} + \vec{c} = k\vec{b}$ .



**4.** If  $\vec{a} = 2\vec{i} + 3\vec{j} - \vec{k}$ ,  $\vec{b} = -\vec{i} + 2\vec{j} - 4\vec{k}$  and  $\vec{c} = \vec{i} + \vec{j} + \vec{k}$ , then find the value of  $(\vec{a} \times \vec{b})$ .  $(\vec{a} \times \vec{c})$ 

form a right-handed system, then find  $\vec{c}$ 

**5.** If the vectors 
$$\vec{c}$$
,  $\vec{a} = x\hat{i} + y\hat{j} + z\hat{k}$  and  $\vec{b} = \hat{j}$  are such that  $\vec{a}$ ,  $\vec{c}$  and  $\vec{b}$ 

A. (a) 
$$z\hat{i} - x\hat{k}$$

B. (b) 
$$\vec{0}$$

C. (c) 
$$y\hat{j}$$

D. (d) 
$$-z\hat{i} + x\hat{k}$$



**6.** Given that  $\vec{a}\vec{b}=\vec{a}\vec{c}$ ,  $\vec{a}\times\vec{b}=\vec{a}\times\vec{c}$  and  $\vec{a}$  is not a zero vector. Show that

$$\vec{b} = \vec{c}$$



7. Show that  $(\vec{a} - \vec{b}) \times (\vec{a} + \vec{b}) = 2\vec{a} \times \vec{b}$  and given a geometrical interpretation of it.



- **8.** If  $\vec{x}$  and  $\vec{y}$  are unit vectors and  $|\vec{z}| = \frac{2}{\sqrt{7}}$  such that  $\vec{z} + (\vec{z} \times \vec{x}) = \vec{y}$ 
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then find the angle  $\theta$  between  $\vec{x}$  and  $\vec{z}$ 

- **9.** prove that  $(\vec{a}.\hat{i})(\vec{a}\times\hat{i})+(\vec{a}.\hat{j})(\vec{a}\times\hat{j})+(\vec{a}.\hat{k})(\vec{a}\times\hat{k})=\vec{0}$ 
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**10.** Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be three non-zero vectors such that  $\vec{a} + \vec{b} + \vec{c} = 0$  and  $\lambda \vec{b} \times \vec{a} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a} = 0$ , then find the value of  $\lambda$ 

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11. A particle has an angular speed of 3 rad/s and the axis of rotation passes through the points (1, 1, 2) and (1, 2, -2) Find the velocity of the particle at point P(3, 6, 4)



**12.** Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be unit vectors such that  $\vec{a}$ .  $\vec{b} = 0 = \vec{a}$ .  $\vec{c}$ . It the angle between  $\vec{b}$  and  $\vec{c}$  is  $\frac{\pi}{6}$  then find  $\vec{a}$ .



**13.** If  $|\vec{a} \times \vec{b}|^2 + (\vec{a} \cdot \vec{b})^2 = 256$  and  $|\vec{a}| = 4$ , then  $|\vec{b}|$  is equal to ......



**14.** Given  $|\vec{a}| = |\vec{b}| = 1$  and  $|\vec{a} + \vec{b}| = \sqrt{3}$  if  $\vec{c}$  is a vector such that  $\vec{c} - \vec{a} - 2\vec{b} = 3(\vec{a} \times \vec{b})$  then find the value of  $\vec{c} \cdot \vec{b}$ .



**15.** Find the moment of  $\vec{F}$  about point (2, -1, 3), where force  $\vec{F} = 3\hat{i} + 2\hat{j} - 4\hat{k}$  is acting on point (1, -1, 2).



### **Exercise 2.3**

**1.** If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  and  $\vec{d}$  are four non-coplanar unit vectors such that  $\vec{d}$  makes equal angles with all the three vectors  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  then prove that

$$\left[\vec{d}\vec{a}\vec{b}\right] = \left[\vec{d}\vec{c}\vec{b}\right] = \left[\vec{d}\vec{c}\vec{a}\right]$$



**2.** prove that if  $\begin{bmatrix} \vec{l} \, \vec{m} \vec{n} \end{bmatrix}$  are three non-coplanar vectors, then

$$\begin{bmatrix} \vec{l} \, \vec{m} \, \vec{n} \, \end{bmatrix} \begin{pmatrix} \vec{a} \times \vec{b} \, \end{pmatrix} = \begin{bmatrix} \vec{l} \cdot \vec{a} & \vec{l} \cdot \vec{b} & \vec{l} \\ \vec{m} \cdot \vec{a} & \vec{m} \cdot \vec{b} & \vec{m} \\ \vec{n} \cdot \vec{a} & \vec{n} \cdot \vec{b} & \vec{n} \end{bmatrix}$$



**3.** If the volume of a parallelepiped whose adjacent edges are  $\vec{a} = 2\hat{i} + 3\hat{j} + 4\hat{k}$ ,  $\vec{b} = \hat{i} + \alpha\hat{j} + 2\hat{k}$ ,  $\vec{c} = \hat{i} + 2\hat{j} + \alpha\hat{k}$  is 15, then find the value of  $\alpha$  if  $(\alpha > 0)$ 



- **4.** If  $\vec{a} = \hat{i} + \hat{j} + \hat{k}$  and  $\vec{b} = \hat{i} 2\hat{j} + \hat{k}$  then find the vector  $\vec{c}$  such that
- $\vec{a} \cdot \vec{c} = 2$  and  $\vec{a} \times \vec{c} = \vec{b}$ .
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**5.** If  $\vec{x}$ .  $\vec{a} = 0\vec{x}$ .  $\vec{b} = 0$  and  $\vec{x}$ .  $\vec{c} = 0$  for some non zero vector  $\vec{x}$  then show

that 
$$\left[\vec{a}\vec{b}\vec{c}\right] = 0$$



**6.** If 
$$\vec{a} = \hat{i} + \hat{j} + \hat{k}$$
 and  $\vec{b} = \hat{i} - 2\hat{j} + \hat{k}$  then find the vector  $\vec{c}$  such that  $\vec{a} \cdot \vec{c} = 2$  and  $\vec{a} \times \vec{c} = \vec{b}$ .



**7.** If 
$$\vec{a}$$
,  $\vec{b}$ ,  $\vec{c}$  are three non-coplanar vectors such that  $\vec{a} \times \vec{b} = \vec{c}$ ,  $\vec{b} \times \vec{c} = \vec{a}$ ,  $\vec{c} \times \vec{a} = \vec{b}$ , then the value of  $|\vec{a}| + |\vec{b}| + |\vec{c}|$  is



**8.** If 
$$\vec{a} = \vec{P} + \vec{q}$$
,  $\vec{P} \times \vec{b} = \vec{0}$  and  $\vec{q}$ .  $\vec{b} = 0$  then prove that 
$$\frac{\vec{b} \times (\vec{a} \times \vec{b})}{\vec{b} \cdot \vec{b}} = \vec{q}$$

**9.** Prove that 
$$(\vec{a}.(\vec{b}\times\hat{i}))\hat{i}+(\vec{a}.(\vec{b}\times\hat{j}))\hat{j}+(\vec{a}.(\vec{b}\times\hat{k}))\hat{k}=\vec{a}\times\vec{b}$$

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**10.** For any four vectors,  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  and  $\vec{d}$  prove that

$$\vec{d} \cdot (\vec{a} \times (\vec{b} \times (\vec{c} \times \vec{d}))) = (\vec{b} \cdot \vec{d})[\vec{a} \vec{c} \vec{d}].$$

- **11.** If  $\vec{a}$  and  $\vec{b}$  be two non-collinear unit vector such  $\vec{a} \times (\vec{a} \times \vec{b}) = \frac{1}{2}\vec{b}$ , then find the angle between  $\vec{a}$  and  $\vec{b}$ .
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**12.** show that  $(\vec{a} \times \vec{b}) \times \vec{c} = \vec{a} \times (\vec{b} \times \vec{c})$  if and only if  $\vec{a}$  and  $\vec{c}$  are collinear or  $(\vec{a} \times \vec{c}) \times \vec{b} = \vec{0}$ 



- Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be the non zero that vectors such  $(\vec{a} \times \vec{b}) \times \vec{c} = \frac{1}{3} |\vec{b}| |\vec{c}| \vec{a}$ . if theta is the acute angle between the vectors  $\vec{b}$  and  $\vec{c}$  then  $\sin\theta$  equals (A)  $\frac{1}{3}$  (B)  $\frac{\sqrt{2}}{3}$  (C)  $\frac{2}{3}$  (D)  $2\frac{\sqrt{2}}{3}$ 
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- **14.** If  $\vec{p}$ ,  $\vec{q}$ ,  $\vec{r}$  denote vector  $\vec{b} \times \vec{c}$ ,  $\vec{c} \times \vec{a}$ ,  $\vec{a} \times \vec{b}$  , respectively, show that  $\vec{a}$  is parallel to  $\vec{q} \times \vec{r}$ ,  $\vec{b}$  is parallel  $\vec{r} \times \vec{p}$ ,  $\vec{c}$  is parallel to  $\vec{p} \times \vec{q}$ .
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**15.** Let  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  be non -coplanar vectors and let equations  $\vec{a}'$ ,  $\vec{b}'$ ,  $\vec{c}'$  are reciprocal system of vector  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  then prove that  $\vec{a} \times \vec{a}' + \vec{b} \times \vec{b}' + \vec{c} \times \vec{c}'$  is a null vector.



**16.** Given unit vectors  $\hat{m}$ ,  $\hat{n}$  and  $\hat{p}$  such that angel between  $\hat{m}$  and  $\hat{n}$  is  $\alpha$  and angle between  $\hat{p}$  and  $(\hat{m} \times \hat{n})$  is also  $\alpha$ , then  $[\hat{n}\hat{p}\hat{m}] =$ 



**17.**  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are threee unit vectors and every two are two inclined to each at an angle  $\cos^{-1}(3/5)$ . If  $\vec{a} \times \vec{b} = p\vec{a} + q\vec{b} + r\vec{c}$ , where p,q,r are scalars, then find the value of q.



**18.** Let  $\vec{a} = a_1 \hat{i} + a_2 \hat{j} + a_3 \hat{k}$ ,  $\vec{b} = b_1 \hat{i} + b_2 \hat{j} + b_3 \hat{k}$  and  $\vec{c} = c_1 \hat{i} + c_2 \hat{j} + c_3 \hat{k}$  be three non-zero vectors such that  $ec{c}$  is a unit vector perpendicular to both

vectors,  $\vec{a}$  and  $\vec{b}$  . If the angle between  $\vec{a}$  and  $\vec{b}$  is  $\vec{b}$  and  $\vec{b}$  is  $\vec{c}_1$  and  $\vec{c}_2$  and  $\vec{c}_3$  and  $\vec{c}_4$  and  $\vec{c}_5$  and  $\vec{c}_7$  and  $\vec{c}_8$  and  $\vec{$ 



equal to

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### **Exercises**

#### 1. Show that

$$\begin{vmatrix} (a-x)^2 & (a-y)^2 & (a-z)^2 \\ (b-x)^2 & (b-y)^2 & (b-z)^2 \\ (c-x)^2 & (c-y)^2 & (c-z)^2 \end{vmatrix} = 2(a-b)(b-c)(c-a)(x-y)(y-z)(z-x)$$



**2.** If OABC is a tetrahedron where O is the origin and A, B, andC are the other three vertices with position vectors,  $\vec{a}$ ,  $\vec{b}$ ,  $and\vec{c}$  respectively, then prove that the centre of the sphere circumscribing the tetrahedron is

given by position vector 
$$\frac{a^2(\vec{b}\times\vec{c})+b^2(\vec{c}\times\vec{a})+c^2(\vec{a}\times\vec{b})}{2\left[\vec{a}\vec{b}\vec{c}\right]}.$$

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- **3.** Find the height of the regular pyramid with each edge measuring I cm. Also,
- if  $\alpha$  is angle between any edge and face not containing that edge, then prove that  $\cos \alpha = \frac{1}{\sqrt{3}}$ 
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**4.** In  $\triangle ABC$ , a point P is taken on AB such that AP/BP = 1/3 and point Q is taken on BC such that CQ/BQ = 3/1. If R is the point of intersection

of the lines *AQandCP*, using vector method, find the area of *ABC* if the area of *BRC* is 1 unit



**5.** Let O be an interior points of  $\triangle ABC$  such that  $\overrightarrow{OA} + 2\overrightarrow{OB} + 3\overrightarrow{OC} = \overrightarrow{0}$ , then the ratio of  $\triangle ABC$  to area of  $\triangle AOC$  is



**6.** The lengths of two opposite edges of a tetrahedron of aandb; the shortest distane between these edgesis d, and the angel between them if  $\theta$  Prove using vector4s that the volume of the tetrahedron is  $\frac{abdisn\theta}{6}$ .



**7.** Find the volume of a parallelopiped having three coterminus vectors of equal magnitude  $|\vec{a}|$  and equal inclination  $\theta$  with each other.

**8.**  $\vec{p}$ ,  $\vec{q}$ , and  $\vec{r}$  are three mutually perpendicular vectors of the same magnitude. If vector  $\vec{x}$  satisfies the equation  $\vec{p} \times ((\vec{x} - \vec{q}) \times \vec{p}) + \vec{q} \times ((\vec{x} - \vec{r}) \times \vec{q}) + \vec{r} \times ((\vec{x} - \vec{p}) \times \vec{r}) = 0$ , then  $\vec{x}$  is given by  $\frac{1}{2}(\vec{p} + \vec{q} - 2\vec{r})$  b.  $\frac{1}{2}(\vec{p} + \vec{q} + \vec{r})$  c.  $\frac{1}{3}(\vec{p} + \vec{q} + \vec{r})$  d.  $\frac{1}{3}(2\vec{p} + \vec{q} - \vec{r})$ 



- **9.** Given the vectors  $\vec{A}$ ,  $\vec{B}$ ,  $and\vec{C}$  form a triangle such that  $\vec{A} = \vec{B} + \vec{C}$  find  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$ , and  $\vec{d}$  such that the area of the triangle is 56 where  $\vec{A} = a\hat{i} + b\hat{j} + c\hat{k}$   $\vec{B} = d\hat{i} + 3\hat{i} + 4\hat{k} \vec{C} = 3\hat{i} + \hat{i} 2\hat{k}$ 
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Determine the distance of point  $A(\vec{a})$  from the line I in from

**10.** A line I is passing through the point  $\vec{b}$  and is parallel to vector  $\vec{c}$ .

$$\left| \vec{b} - \vec{a} + \frac{\left( \vec{a} - \vec{b} \right) \vec{c}}{\left| \vec{c} \right|^2} \vec{c} \right| \text{ or } \frac{\left| \left( \vec{b} - \vec{a} \right) \times \vec{c} \right|}{\left| \vec{c} \right|}$$



**11.** If 
$$\vec{e}_1$$
,  $\vec{e}_2$ ,  $\vec{e}_3$  and  $\vec{E}_1$ ,  $\vec{E}_2$ ,  $\vec{E}_3$  are two sets of vectors such that

 $\vec{e}_i \vec{E}_j = 1$ , if i = j and  $\vec{e}_i \vec{E}_j = 0$  and if  $i \neq j$ , then prove that  $\begin{bmatrix} \vec{e}_1 & \vec{e}_2 & \vec{e}_3 \end{bmatrix} \begin{bmatrix} \vec{E}_1 & \vec{E}_2 & \vec{E}_3 \end{bmatrix} = 1$ .

**12.** In a quadrillateral ABCD, it is given that AB 
$$\parallel$$
CD and the diagonals AC and BD are perpendiclar to each other . Show that  $AD$ .  $BC = AB$ .  $CD$ .



**13.** OABC is regular tetrahedron in which D is the circumcentre of OABand E is the midpoint of edge AC Prove that DE is equal to half the edge of tetrahedron.



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**14.** If A(
$$\vec{a}$$
). B( $\vec{b}$ ) and C( $\vec{c}$ ) are three non-collinear point and origin does not lie in the plane of the points A, B and C, then for any point  $P(\vec{P})$  in the plane of the  $\triangle$  ABC such that vector  $\vec{OP}$  is  $\bot$  to plane of trianglABC, show that  $\vec{OP} = \frac{\left[\vec{a}\vec{b}\vec{c}\right]\left(\vec{a}\times\vec{b}+\vec{b}\times\vec{c}+\vec{c}\times\vec{a}\right)}{4\Delta^2}$ 



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**15.** If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are three given non-coplanar vectors and any arbitrary vector

$$\vec{r} \text{ in space, where } \Delta_1 = \begin{bmatrix} \vec{r}. \ \vec{a} & \vec{b}. \ \vec{a} & \vec{c}. \ \vec{a} \\ \vec{r}. \ \vec{b} & \vec{b}. \ \vec{b} & \vec{c}. \ \vec{b} \end{bmatrix}, \Delta_2 = \begin{bmatrix} \vec{a}. \ \vec{a} & \vec{r}. \ \vec{a} & \vec{c}. \ \vec{a} \\ \vec{a}. \ \vec{b} & \vec{r}. \ \vec{b} & \vec{c}. \ \vec{b} \end{bmatrix}$$

$$\Delta_{3} = \begin{vmatrix} \vec{a}. \ \vec{a} & \vec{b}. \ \vec{a} & \vec{r}. \ \vec{a} \\ \vec{a}. \ \vec{b} & \vec{b}. \ \vec{b} & \vec{r}. \ \vec{b} \end{vmatrix}, \Delta = \begin{vmatrix} \vec{a}. \ \vec{a} & \vec{b}. \ \vec{a} & \vec{c}. \ \vec{a} \\ \vec{a}. \ \vec{b} & \vec{b}. \ \vec{b} & \vec{c}. \ \vec{b} \end{vmatrix},$$
 then prove that 
$$\vec{r} = \frac{\Delta_{1}}{\Delta} \vec{a} + \frac{\Delta_{2}}{\Delta} \vec{b} + \frac{\Delta_{3}}{\Delta} \vec{c}$$



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### **Exercises MCQ**

1. Two vectors in space are equal only if they have equal component in a. a given direction b. two given directions c. three given

directions d. in any arbitrary direction

A. a given direction

B. two given directions

C. three given direction

D. in any arbitrary direaction

Answer: c

**2.** Let 
$$\vec{a}$$
,  $\vec{b}$  and  $\vec{c}$  be the three vectors having magnitudes, 1,5 and 3, respectively, such that the angle between  $\vec{a}$  and  $\vec{b}$  is  $\theta$  and  $\vec{a} \times (\vec{a} \times \vec{b}) = \vec{c}$ . Then  $\tan \theta$  is equal to

B. 
$$\frac{2}{3}$$

C. 
$$\frac{3}{5}$$
D.  $\frac{3}{4}$ 

### Answer: d



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**3.**  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  are three vectors of equal magnitude. The angle between each pair of vectors is  $\pi/3$  such that  $|\vec{a} + \vec{b} + \vec{c}| = \sqrt{6}$ . Then  $|\vec{a}|$  is equal

to a.2 b. -1 c. 1 d.  $\sqrt{6}/3$ 

B. - 1

C. 1

D.  $\sqrt{6}/3$ 

Answer: c



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**4.** Let 
$$\vec{p}$$
 and  $\vec{q}$  be any two orthogonal vectors of equal magnitude 4 each.

Let  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  be any three vectors of lengths  $7\sqrt{15}$  and  $2\sqrt{33}$ , mutually

perpendicular to each other. Then find the distance of the vector  $\begin{pmatrix} \vec{a} \ \vec{p} \end{pmatrix} \vec{p} + \begin{pmatrix} \vec{a} \ \vec{q} \end{pmatrix} \vec{q} + \begin{pmatrix} \vec{a} \ \vec{p} \times \vec{q} \end{pmatrix} (\vec{p} \times \vec{q}) + \begin{pmatrix} \vec{b} \ \vec{p} \end{pmatrix} \vec{p} \begin{pmatrix} \vec{b} \ \vec{q} \end{pmatrix} \vec{q} + \begin{pmatrix} \vec{b} \ \vec{p} \times \vec{q} \end{pmatrix} (\vec{p} \times \vec{q}) + \begin{pmatrix} \vec{b} \ \vec{p} \times \vec{q} \end{pmatrix} \vec{q} + \begin{pmatrix} \vec{b} \ \vec{p} \times \vec{q} \end{pmatrix} \vec{q} + \begin{pmatrix} \vec{b} \ \vec{p} \times \vec{q} \end{pmatrix} \vec{q} + \begin{pmatrix} \vec{b} \ \vec{p} \times \vec{q} \end{pmatrix} \vec{q} + \begin{pmatrix} \vec{b} \ \vec{p} \times \vec{q} \end{pmatrix} \vec{q} + \begin{pmatrix} \vec{b} \ \vec{p} \times \vec{q} \end{pmatrix} \vec{q} + \begin{pmatrix} \vec{b} \ \vec{p} \times \vec{q} \end{pmatrix} \vec{q} + \begin{pmatrix} \vec{b} \ \vec{p} \times 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\vec{b} \ \vec{p} &$ 

$$\mathbf{A}.\,\vec{a}+\vec{b}+\vec{c}$$

from the origin.

$$\vec{b}$$
 +

B. 
$$\frac{\vec{a}}{\left|\vec{a}\right|} + \frac{\vec{b}}{\left|\vec{b}\right|} + \frac{\vec{c}}{\left|\vec{c}\right|}$$

C. 
$$\frac{\vec{a}}{|\vec{a}|^2} + \frac{\vec{b}}{|\vec{b}|^2} + \frac{\vec{c}}{|\vec{c}|^2}$$

## D. $\left| \vec{a} \right| \vec{a} - \left| \vec{b} \right| \vec{b} + \left| \vec{c} \right| \vec{c}$

#### Answer: b



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**5.** Let  $\vec{a} = \hat{i} + \hat{j}$  and  $\vec{b} = 2\hat{i} - \hat{k}$ , then the point of intersection of the lines

$$\vec{r} \times \vec{a} = \vec{b} \times \vec{a}$$
 and  $\vec{r} \times \vec{b} = \vec{a} \times \vec{b}$  is a. (3, -1, 1) b. (3, 1, -1) c. (-3, 1, 1) d.

A. 
$$\hat{i}$$
 -  $\hat{j}$  +  $\hat{k}$ 

$$\mathsf{B.}\,3\hat{i}\,-\hat{j}+\hat{k}$$

$$\mathsf{C.}\,\,3\hat{i}+\hat{j}-\hat{k}$$

D. 
$$\hat{i} - \hat{j} - \hat{k}$$

#### Answer: c



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**6.** If  $\vec{a}$  and  $\vec{b}$  are two vectors, such that  $\vec{a} \cdot \vec{b} > 0$  and  $|\vec{a} \cdot \vec{b}| = |\vec{a} \times \vec{b}|$  then the angle between the vectors  $\vec{a}$  and  $\vec{b}$  is

Α. π

B.  $7\pi/4$ 

 $C. \pi/4$ 

D.  $3\pi/4$ 

#### Answer: d



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**7.** If  $\hat{a}$ ,  $\hat{b}$ , and  $\hat{c}$  are three unit vectors, such that  $\hat{a} + \hat{b} + \hat{c}$  is also a unit vector and  $\theta_1$ ,  $\theta_2$  and  $\theta_3$  are angles between the vectors  $\hat{a}$ ,  $\hat{b}$ ;  $\hat{b}$ ,  $\hat{c}$  and  $\hat{c}$ ,  $\hat{a}$ 

respectively, then among  $\theta_1$ ,  $\theta_2$  and  $\theta_3$ . a. all are acute angles b. all are right angles c. at least one is obtuse angle d. none of these

- A. all are acute angles
- B. all are right angles
- C. at least one is obtuse angle
- D. none of these

#### Answer: c



- **8.** If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are unit vectors such that  $\vec{a}$ .  $\vec{b} = 0 = \vec{a}$ .  $\vec{c}$  and the angle between  $\vec{b}$  and  $\vec{c}$  is  $\frac{\pi}{3}$ , then find the value of  $|\vec{a} \times \vec{b} \vec{a} \times \vec{c}|$ .
  - **A.** 1/2
  - B. 1
  - C. 2

D. none of these

#### Answer: b



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- 9. about to only mathematics
  - A. a plane containing the origian O and parallel to two non-collinear

vectors OP and OQ

- B. the surface of a sphere described on PQ as its diameter
- C. a line passing through points P and Q
- D. a set of lines parallel to line PQ

#### Answer: c



**10.** Two adjacent sides of a parallelogram 
$$ABCD$$
 are  $2\hat{i} + 4\hat{j} - 5\hat{k}$  and  $\hat{i} + 2\hat{j} + 3\hat{k}$ . Then the value of  $|AC \times BD|$  is a.  $20\sqrt{5}$  b.  $22\sqrt{5}$  c.  $24\sqrt{5}$  d.  $26\sqrt{5}$ 

A. 
$$20\sqrt{5}$$

B.  $22\sqrt{5}$ 

D. 
$$26\sqrt{5}$$

#### Answer: b



11. If 
$$\hat{a}$$
,  $\hat{b}$ , and  $\hat{c}$  are three unit vectors inclined to each other at angle  $\theta$ , then the maximum value of  $\theta$  is  $\frac{\pi}{3}$  b.  $\frac{\pi}{4}$  c.  $\frac{2\pi}{3}$  d.  $\frac{5\pi}{6}$ 

A. 
$$\frac{\pi}{3}$$

B. 
$$\frac{\pi}{2}$$

c. 
$$\frac{2}{3}$$

**D**. 
$$\frac{5}{5}$$

#### Answer: c



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**12.** Let the pairs a, b, and c, d each determine a plane. Then the planes

are parallel if  $a.(\vec{a} \times \vec{c}) \times (\vec{b} \times \vec{d}) = \vec{0}$  b.  $(\vec{a} \times \vec{c}).(\vec{b} \times \vec{d}) = \vec{0}$  c.

$$(\vec{a} \times \vec{b}) \times (\vec{c} \times \vec{d}) = \vec{0} d. (\vec{a} \times \vec{b}). (\vec{c} \times \vec{d}) = \vec{0}$$

A. 
$$(\vec{a} \times \vec{c}) \times (\vec{b} \times \vec{d}) = \vec{0}$$

B. 
$$(\vec{a} \times \vec{c})$$
.  $(\vec{b} \times \vec{d}) = \vec{0}$ 

$$C. \left( \vec{a} \times \vec{b} \right) \times \left( \vec{c} \times \vec{d} \right) = \vec{0}$$

D. 
$$(\vec{a} \times \vec{c})$$
.  $(\vec{c} \times \vec{d}) = \vec{0}$ 

#### Answer: c



**13.** If  $\vec{r} \cdot \vec{a} = \vec{r} \cdot \vec{b} = \vec{r} \cdot \vec{c} = 0$  where  $\vec{a}, \vec{b}$  and  $\vec{c}$  are non-coplanar, then

A. 
$$\vec{r} \perp (\vec{c} \times \vec{a})$$

B. 
$$\vec{r} \perp (\vec{a} \times \vec{b})$$

C. 
$$\vec{r} \perp (\vec{b} \times \vec{c})$$

D. 
$$\vec{r} = \vec{0}$$

#### Answer: d



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**14.** If  $\vec{a}$  satisfies  $\vec{a} \times (\hat{i} + 2\hat{j} + \hat{k}) = \hat{i} - \hat{k}$  then  $\vec{a}$  is equal to

A. 
$$\lambda \hat{i} + (2\lambda - 1)\hat{j} + \lambda \hat{k}, \lambda \in R$$

B. 
$$\lambda \hat{i} + (1 - 2\lambda)\hat{j} + \lambda \hat{k}, \lambda \in R$$

$$C. \lambda \hat{i} + (2\lambda + 1)\hat{j} + \lambda \hat{k}, \lambda \in R$$

D. 
$$\lambda \hat{i} + (1 + 2\lambda)\hat{j} + \lambda \hat{k}, \lambda \in R$$



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**15.** Vectors  $3\vec{a} - 5\vec{b}$  and  $2\vec{a} + \vec{b}$  are mutually perpendicular. If  $\vec{a} + 4\vec{b}$  and  $\vec{b} - \vec{a}$  are also mutually perpendicular, then the cosine of the angle between  $\vec{a}$  and  $\vec{b}$  is a.  $\frac{19}{5\sqrt{43}}$  b.  $\frac{19}{3\sqrt{43}}$  c.  $\frac{19}{2\sqrt{45}}$  d.  $\frac{19}{6\sqrt{43}}$ 

- A.  $\frac{19}{5\sqrt{43}}$
- B.  $\frac{19}{3\sqrt{43}}$
- c.  $\frac{19}{\sqrt{45}}$
- D.  $\frac{19}{6\sqrt{43}}$

Answer: a



**16.** The unit vector orthogonal to vector  $-\hat{i} + \hat{j} + 2\hat{k}$  and making equal

angles with the x and y-axis  $a.\pm \frac{1}{3} \left( 2\hat{i} + 2\hat{j} - \hat{k} \right)$  b.  $\pm \frac{1}{3} \left( \hat{i} + \hat{j} - \hat{k} \right)$  c.

$$\pm \frac{1}{3} \left( 2\hat{i} - 2\hat{j} - \hat{k} \right)$$
 d. none of these

$$A. \pm \frac{1}{3} \left( 2\hat{i} + 2\hat{j} - \hat{k} \right)$$

B. 
$$\frac{19}{5\sqrt{43}}$$

$$C. \pm \frac{1}{3} \left( \hat{i} + \hat{j} - \hat{k} \right)$$

D. none of these

#### Answer: a



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17. The value of x for which the angle between  $\vec{a} = 2x^2\hat{i} + 4x\hat{j} + \hat{k}and\vec{b} = 7\hat{i} - 2\hat{j} + \hat{k}$  is obtuse and the angle between b and the z-axis acute and less than  $\pi/6$  is given by

A. 
$$a < x < 1/2$$

B. 
$$1/2 < x < 15$$

C. 
$$x < 1/2$$
 or  $x < 0$ 

D. none of these

#### Answer: b



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18. If vectors  $\vec{a}$  and  $\vec{b}$  are two adjacent sides of a parallelogram, then the vector respresenting the altitude of the parallelogram which is the

perpendicular to 
$$a$$
 is  $\vec{a} \cdot \vec{b} + \frac{\vec{b} \times \vec{a}}{\left|\vec{a}\right|^2}$  b.  $\frac{\vec{a}\vec{b}}{\left|\vec{b}\right|^2}$  c.  $\vec{b} - \frac{\vec{b}\vec{a}}{\left|\vec{a}\right|^2}$  d.  $\frac{\vec{a} \times \left(\vec{b} \times \vec{a}\right)}{\left|\vec{b}\right|^2}$ 

$$A. \vec{b} + \frac{\vec{b} \times \vec{a}}{|\vec{a}|^2}$$

B. 
$$\frac{\vec{a} \cdot \vec{b}}{\left|\vec{b}\right|^2}$$

$$C. \vec{b} - \frac{\vec{b}. \vec{a}}{|\vec{a}|^2} \vec{a}$$

D. 
$$\frac{\vec{a} \times \left(\vec{b} \times \vec{a}\right)}{\left|\vec{b}\right|^2}$$

Answer: a



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- **19.** A parallelogram is constructed on  $2\vec{a} + \vec{b}$  and  $\vec{a} 4\vec{b}$ , where  $|\vec{a}| = 6$  and  $|\vec{b}| = 8$ , and  $\vec{a}$  and  $\vec{b}$  are anti-parallel. Then
- the length of the longer diagonal is 40 b. 64 c. 32 d. 48
  - A. 40
  - B. 64
  - C. 32
  - D. 48

Answer: c



**20.** Let  $\vec{a}\vec{b}=0$ , where  $\vec{a}$  and  $\vec{b}$  are unit vectors and the unit vector  $\vec{c}$  is

inclined at an angle  $\theta$  to both  $\vec{a}$  and  $\vec{b}$ . If  $\vec{c} = m\vec{a} + n\vec{b} + p(\vec{a} \times \vec{b})$ ,  $(m, n, p \in R)$ , then  $\frac{\pi}{4} \le \theta \le \frac{\pi}{4}$  b.  $\frac{\pi}{4} \le \theta \le \frac{3\pi}{4}$  c.

$$0 \le \theta \le \frac{\pi}{4} d. \ 0 \le \theta \le \frac{3\pi}{4}$$

A. 
$$\frac{\pi}{4} \le \theta \le \frac{\pi}{4}$$
B.  $\frac{\pi}{4} \le \theta \le \frac{3\pi}{4}$ 

$$\mathsf{C.}\ 0 \leq \theta \leq \frac{\pi}{4}$$

$$\mathsf{D.}\,0 \leq \theta \leq \frac{3\pi}{4}$$

#### Answer: a



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**21.** If a and c are unit vectors and |b| = 4. The angel between a and c is  $\cos^{-1}(1/4)$  and  $a \times b = 2a \times c$  then,  $b - 2c = \lambda a$ . The value of  $\lambda$  is

- B. 1/4,3/4
- **C.** -3, 4
- D. -1/4,  $\frac{3}{4}$

#### Answer: a



- **22.** Let the position vectors of the points PandQ be  $4\hat{i} + \hat{j} + \lambda \hat{k} and 2\hat{i} \hat{j} + \lambda \hat{k}$ , respectively. Vector  $\hat{i} \hat{j} + 6\hat{k}$  is perpendicular to the plane containing the origin and the points PandQ. Then  $\lambda$  equals a -1/2 b. 1/2 c. 1 d. none of these
  - **A.** -1/2
  - **B.** 1/2
  - C. 1
  - D. none of these

#### Answer: a



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- **23.** A vector of magnitude  $\sqrt{2}$  coplanar with the vector  $\vec{a} = \hat{i} + \hat{j} + 2\hat{k}$  and  $\vec{b} = \hat{i} + 2\hat{j} + \hat{k}$ , and perpendicular to the vector  $\vec{c} = \hat{i} + \hat{j} + \hat{k}$ , is a.- $\hat{j} + \hat{k}$  b.  $\hat{i} \hat{k}$  c.  $\hat{i} \hat{j}$  d.  $\hat{i} \hat{j}$ 
  - A.  $-\hat{j} + \hat{k}$
  - $\mathbf{B}.\,\hat{i}$  and  $\hat{k}$
  - C.  $\hat{i}$   $\hat{k}$
  - D. hati- hatj`

#### Answer: a



**24.** Let P be a point interior to the acute triangle ABC If PA + PB + PC is a null vector, then w.r.t traingel ABC, point P is its a. centroid b. orthocentre c. incentre d. circumcentre

A. centroid

B. orthocentre

C. incentre

D. circumcentre

#### Answer: a



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**25.** G is the centroid of triangle ABC and  $A_1$  and  $B_1$  are the midpoints of sides AB and AC, respectively. If  $\Delta_1$  is the area of quadrilateral  $GA_1AB_1$  and  $\Delta$  is the area of triangle ABC, then  $\frac{\Delta}{\Delta_1}$  is equal to

a.<u>-</u> 2

**b**. 3

d. none of these

- A.  $\frac{3}{2}$
- B. 3
- c.  $\frac{1}{3}$ D. none of these

### Answer: b



26.

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**26.** Points 
$$\vec{a}$$
,  $\vec{b}$ ,  $\vec{c}$ , and  $\vec{d}$  are coplanar and  $(s \in \alpha)\vec{a} + (2\sin 2\beta)\vec{b} + (3\sin 3\gamma)\vec{c} - \vec{d} = 0$ . Then the least value of  $\sin^2 \alpha + \sin^2 2\beta + \sin^2 3\gamma is \frac{1}{14}$  b. 14 c. 6 d.  $1/\sqrt{6}$ 

and

D. 
$$1/\sqrt{6}$$

#### Answer: a



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**27.** If  $\vec{a}$  and  $\vec{b}$  are any two vectors of magnitudes 1 and 2, respectively, and

$$(1 - 3\vec{a}.\vec{b})^2 + |2\vec{a} + \vec{b} + 3(\vec{a} \times \vec{b})|^2 = 47$$
, then the angel between  $\vec{a}$  and  $\vec{b}$ 

is 
$$\pi/3$$
 b.  $\pi$  -  $\cos^{-1}(1/4)$  c.  $\frac{2\pi}{3}$  d.  $\cos^{-1}(1/4)$ 

**A.** 
$$\pi/3$$

B. 
$$\pi$$
 -  $\cos^{-1}(1/4)$ 

C. 
$$\frac{2\pi}{3}$$

D. 
$$\cos^{-1}(1/4)$$

#### Answer: c

**28.** If  $\vec{a}$  and  $\vec{b}$  are any two vectors of magnitudes 2 and 3, respectively, such that  $\left|2(\vec{a} \times \vec{b})\right| + \left|3(\vec{a} \cdot \vec{b})\right| = k$ , then the maximum value of k is a.  $\sqrt{13}$  b.  $2\sqrt{13}$  c.  $6\sqrt{13}$  d.  $10\sqrt{13}$ 

**A.** 
$$\sqrt{13}$$

B. 
$$2\sqrt{13}$$

D. 
$$10\sqrt{13}$$

C.  $6\sqrt{13}$ 

#### Answer: c



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**29.**  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are unit vecrtors such that  $|\vec{a} + \vec{b} + 3\vec{c}| = 4$  Angle between  $ec{a}$  and  $ec{b}$  is  $heta_1$  , between  $ec{b}$  and  $ec{c}$  is  $heta_2$  and between  $ec{a}$  and  $ec{c}$  varies  $[\pi/6, 2\pi/3]$  . Then the maximum value of  $\cos\theta_1 + 3\cos\theta_2$  is

B. B. 4

C. C.  $2\sqrt{2}$ 

D. D. 6

#### Answer: b



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**30.** If the vector product of a constant vector  $\vec{O}A$  with a variable vector  $\vec{O}B$  in a fixed plane OAB be a constant vector, then the locus of B is a straight line perpendicular to  $\vec{O}A$  b. a circle with centre O and radius equal to  $|\vec{O}A|$  c. a straight line parallel to  $\vec{O}A$  d. none of these

A. a straight line perpendicular to OA

B. a circle with centre O and radius equal to  $\left|OA\right|$ 

C. a striaght line parallel to OA

D. none of these

#### Answer: c



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**31.** Let  $\vec{u}$ ,  $\vec{v}$  and  $\vec{w}$  be such that  $\left| \vec{u} \right| = 1$ ,  $\left| \vec{v} \right| = 2$  and  $\left| \vec{w} \right| = 3$ . If the projection of  $\vec{v}$  along  $\vec{u}$  is equal to that of  $\vec{w}$  along  $\vec{u}$  and vectors  $\vec{v}$  and  $\vec{w}$  are perpendicular to each other, then  $\left| \vec{u} - \vec{v} + \vec{w} \right|$  equals  $2 \text{ b. } \sqrt{7} \text{ c. } \sqrt{14} \text{ d. } 14$ 

- A. 2
- B.  $\sqrt{7}$
- $C.\sqrt{14}$
- D. 14

#### Answer: c



**32.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be three non-coplanar vectors and a',b' and c' constitute

the reciprocal system of vectors, then prove that

$$i. \ \vec{r} = (\vec{r}. \ \vec{a}') \vec{a} + (\vec{r}. \ \vec{b}') \vec{b} + (\vec{r}. \ \vec{c}') \vec{c}$$

ii. 
$$\vec{r} = (\vec{r}.\vec{a})\vec{a}' + (\vec{r}.\vec{b})\vec{b}' + (\vec{r}.\vec{c})\vec{c}'$$

$$A. -\cos^{-1}\left(\frac{19}{5\sqrt{43}}\right)$$

B. 
$$\cos^{-1}\left(\frac{19}{5\sqrt{43}}\right)$$

C. 
$$\pi \cos^{-1} \left( \frac{19}{5\sqrt{43}} \right)$$
D. cannot of these

#### Answer: b



**33.** if 
$$\vec{\alpha} \mid |\vec{\beta} \times \vec{\gamma}|$$
, then  $(\vec{\alpha} \times \vec{\beta}) \cdot (\vec{\alpha} \times \vec{\gamma})$  equals to  $\vec{\alpha} \cdot |\vec{\alpha}|^2 (\vec{\beta} \cdot \vec{\gamma})$  b.  $|\vec{\beta}|^2 (\vec{\gamma} \cdot \vec{\alpha}) \cdot |\vec{\gamma}|^2 (\vec{\alpha} \cdot \vec{\beta}) \cdot |\vec{\alpha}| |\vec{\beta}| |\vec{\gamma}|$ 

A. 
$$\left|\vec{\alpha}\right|^2 \left(\vec{\beta}.\vec{\gamma}\right)$$

B. 
$$\left| \vec{\beta} \right|^2 \left( \vec{\gamma} \cdot \vec{\alpha} \right)$$

C. 
$$|\vec{\gamma}|^2 (\vec{\alpha}. \vec{\beta})$$

D. 
$$\left| \vec{\alpha} \right| \left| \vec{\beta} \right| \left| \vec{\gamma} \right|$$

#### Answer: a



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position vectors of points A,B and 34. The C are  $\hat{i} + \hat{j} + \hat{k}$ ,  $\hat{i} + 5\hat{j} - \hat{k}$  and  $2\hat{i} + 3\hat{j} + 5\hat{k}$ , respectively the greatest angle of triangle ABC is

A. A. 120 
$$^{\circ}$$

C. C. 
$$\cos^{-1}(3/4)$$

D. D. none of these

#### Answer: b



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**35.** Given three vectors  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  two of which are non-collinear. Further if  $(\vec{a} + \vec{b})$  is collinear with  $\vec{c}$ ,  $(\vec{b} + \vec{c})$  is collinear with  $\vec{a}$ ,  $|\vec{a}| = |\vec{b}| = |\vec{c}| = \sqrt{2}$  Find the value of  $\vec{a}$ .  $\vec{b} + \vec{b}$ .  $\vec{c} + \vec{c}$ .  $\vec{a}$  a. 3 b. -3 c. 0 d. cannot be evaluated

- A. 3
- **B**. -3
- C. 0
- D. cannot of these

#### Answer: b



**36.** If 
$$\vec{a}$$
 and  $\vec{b}$  are unit vectors such that  $(\vec{a} + \vec{b})$ .  $[(2\vec{a} + 3\vec{b}) \times (3\vec{a} - 2\vec{b})] = 0$ , then angle between  $\vec{a}$  and  $\vec{b}$  is

D. indeterminate

#### Answer: d



 $\overrightarrow{AB} = p$ ,  $\overrightarrow{thenABAC} + \overrightarrow{BCBA} + \overrightarrow{CACB}$  is equal to  $2p^2$  b.  $\frac{p^2}{2}$  c.  $p^2$  d. none of these

**37.** If in a right-angled triangle ABC, the hypotenuse

A. 
$$2p^2$$

B.  $\frac{p^2}{2}$ 

D. none of these

# Answer: c

**38.** Resolved part of vector 
$$\vec{a}$$
 and along vector  $\vec{b}$  is  $\vec{a}_1$  and that

prependicular to 
$$\vec{b}$$
 is  $\vec{a}_2$  then  $\vec{a}_1 \times \vec{a}_2$  is equl to

A. 
$$\frac{\left(\vec{a} \times \vec{b}\right) \cdot \vec{b}}{\left|\vec{b}\right|^2}$$

$$\begin{vmatrix} \vec{b} \end{vmatrix}^2 \\ \frac{(\vec{a}.\vec{b})\vec{a}}{}$$

B. 
$$\frac{\left(\vec{a}.\vec{b}\right)\vec{a}}{\left|\vec{a}\right|^{2}}$$
C. 
$$\frac{\left(\vec{a}.\vec{b}\right)\left(\vec{b}\times\vec{a}\right)}{\left|\vec{b}\right|^{2}}$$

D. 
$$\frac{\left|\vec{b}\right|^2}{\left|\vec{b} \times \vec{a}\right|}$$



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**39.**  $\vec{a} = 2\hat{i} - \hat{j} + \hat{k}$ ,  $\vec{b} = \hat{i} + 2\hat{j} - \hat{k}$ ,  $\vec{c} = \hat{i} + \hat{j} - 2\hat{k}$  A vector coplanar with  $\vec{b}$  and  $\vec{c}$ 

whose projectin on  $\vec{a}$  is magnitude  $\sqrt{\frac{2}{3}}$  is  $2\hat{i} + 3\hat{j} - 3\hat{k}$  b.  $-2\hat{i} - \hat{j} + 5\hat{k}$  c.

$$2\hat{i} + 3\hat{j} + 3\hat{k} d. 2\hat{i} + \hat{j} + 5\hat{k}$$

A. 
$$2\hat{i} + 3\hat{j} - 3\hat{k}$$

B. 
$$-2\hat{i} - \hat{j} + 5\hat{k}$$

C. 
$$2\hat{i} + 3\hat{j} + 3\hat{k}$$

D. 
$$2\hat{i} + \hat{j} + 5\hat{k}$$

# Answer: b



**40.** If P is any arbitrary point on the circumcircle of the equilateral triangle of side length l units, then  $|\vec{P}A|^2 + |\vec{P}B|^2 + |\vec{P}C|^2$  is always equal to  $2l^2$  b.  $2\sqrt{3}l^2$  c.  $l^2$  d.  $3l^2$ 

- A.  $2l^2$
- B.  $2\sqrt{3}l^2$
- C.  $l^2$
- D.  $3l^2$

#### Answer: a



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**41.** If  $\vec{r}$  and  $\vec{s}$  are non-zero constant vectors and the scalar b is chosen such that  $|\vec{r} + b\vec{s}|$  is minimum, then the value of  $|b\vec{s}|^2 + |\vec{r} + b\vec{s}|^2$  is equal to  $2|\vec{r}|^2$  b.  $|\vec{r}|^2/2$  c.  $3|\vec{r}|^2$  d.  $|r|^2$ 

A. 
$$2|\vec{r}|^2$$

B. 
$$|\vec{r}|^2/2$$

C. 
$$3|\vec{r}|^2$$

D. 
$$|\vec{r}|^2$$

# Answer: d



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**42.**  $\vec{a}$  and  $\vec{b}$  are two unit vectors that are mutually perpendicular. A unit vector that is equally inclined to  $\vec{a}$ ,  $\vec{b}$  and  $\vec{a} \times \vec{b}$  is  $\frac{1}{\sqrt{2}} (\vec{a} + \vec{b} + \vec{a} \times \vec{b})$  b.

$$\frac{1}{2} \left( \vec{a} \times \vec{b} + \vec{a} + \vec{b} \right) \text{c.} \frac{1}{\sqrt{3}} \left( \vec{a} + \vec{b} + \vec{a} \times \vec{b} \right) \text{d.} \frac{1}{3} \left( \vec{a} + \vec{b} + \vec{a} \times \vec{b} \right)$$

A. 
$$\frac{1}{\sqrt{2}} \left( \vec{a} + \vec{b} + \vec{a} \times \vec{b} \right)$$

$$B. \frac{1}{2} \left( \vec{a} \times \vec{b} + \vec{a} + \vec{b} \right)$$

C. 
$$\frac{1}{\sqrt{3}} \left( \vec{a} + \vec{b} + \vec{a} \times \vec{b} \right)$$

D. 
$$\frac{1}{3} \left( \vec{a} + \vec{b} + \vec{a} \times \vec{b} \right)$$

# Answer: a

**43.** Given that 
$$\vec{a}, \vec{b}, \vec{p}, \vec{q}$$
 are four vectors such that

$$\vec{a} + \vec{b} = \mu \vec{p}, \ \vec{b} \vec{q} = 0$$
 and  $(\vec{b})^2 = 1$ , where  $\mu$  is a scalar. Then  $|\vec{d} \vec{q} \vec{p} - (\vec{p} \vec{q}) \vec{d}|$ 

is equal to 
$$2 \begin{vmatrix} \vec{p} & \vec{q} \\ \vec{p} & \vec{q} \end{vmatrix}$$
 b.  $(1/2) \begin{vmatrix} \vec{p} & \vec{q} \\ \vec{p} & \vec{q} \end{vmatrix}$  c.  $|\vec{p} \times \vec{q}|$  d.  $|\vec{p} \vec{q}|$ 

$$A. 2 \left| \vec{p} \vec{q} \right|$$

B. 
$$(1/2) | \vec{p} \cdot \vec{q} |$$

C. 
$$\left| \vec{p} \times \vec{q} \right|$$

D. 
$$|\vec{p}.\vec{q}|$$

## Answer: d



**44.** The position vectors of the vertices A, BandC of a triangle are three unit vectors  $\vec{a}, \vec{b}, and\vec{c}$ , respectively. A vector  $\vec{d}$  is such that  $\vec{d} \cdot \vec{a} = \vec{d} \cdot \vec{b} = \vec{d} \cdot \vec{c}$  and  $\vec{d} = \lambda \left( \vec{b} + \vec{c} \right)$ . Then triangle ABC is a acute angled b. obtuse angled c. right angled d. none of these

A. acute angled

B. obtuse angled

C. right angled

D. none of these

#### Answer: a



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**45.** If a is real constant A, B and C are variable angles and  $\sqrt{a^2 - 4} \tan A + a \tan B + \sqrt{a^2 + 4} \tan C = 6a$ , then the least value of  $\tan^2 A + \tan^2 B + \tan^2 C$  is a. 6 b. 10 c. 12 d. 3

- A. 6
- B. 10
  - C. 12
- D. 3

# Answer: d



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BandC have respective position vectors  $\hat{i}and\hat{j}$  Let  $\Delta$  be the area of the triangle and  $\Delta \left[ 3/2, \sqrt{33}/2 \right]$  . Then the range of values of  $\lambda$  corresponding to A is a.[ - 8, 4]  $\cup$  [4, 8] b. [ - 4, 4] c. [ - 2, 2] d. [ - 4, - 2]  $\cup$  [2, 4]

**46.** The vertex A triangle ABC is on the line  $\vec{r} = \hat{i} + \hat{j} + \lambda \hat{k}$  and the vertices

- A. [-8, -4]cup[4,8]`
- B.[-4,4]
- C. [-2,2]

D. [ - 4, - 2] U [2, 4]



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**47.** A non-zero vector  $\vec{a}$  is such that its projections along vectors

$$\frac{\hat{i}+\hat{j}}{\sqrt{2}}, \frac{-\hat{i}+\hat{j}}{\sqrt{2}}$$
 and  $\hat{k}$  are equal, then unit vector along  $\vec{a}$  is a.  $\frac{\sqrt{2}\hat{j}-\hat{k}}{\sqrt{3}}$  b.

$$\frac{\hat{j} - \sqrt{2}\hat{k}}{\sqrt{3}} \text{ c. } \frac{\sqrt{2}}{\sqrt{3}}\hat{j} + \frac{\hat{k}}{\sqrt{3}} \text{ d. } \frac{\hat{j} - \hat{k}}{\sqrt{2}}$$

A. 
$$\frac{\sqrt{2}\hat{j} - \hat{k}}{\sqrt{3}}$$

$$\hat{j} - \sqrt{2}\hat{k}$$
3.  $\frac{\hat{j}}{-}$ 

B. 
$$\frac{\hat{j} - \sqrt{2}\hat{k}}{\sqrt{3}}$$
C. 
$$\frac{\sqrt{2}}{\sqrt{3}}\hat{j} + \frac{\hat{k}}{\sqrt{3}}$$

D. 
$$\frac{\hat{j} - \hat{k}}{\sqrt{2}}$$

Answer: a



**48.** Position vector  $\hat{k}$  is rotated about the origin by angle  $135^0$  in such a way that the plane made by it bisects the angle between  $\hat{i}$  and  $\hat{j}$ . Then its new position is

$$A. \pm \frac{\hat{i}}{\sqrt{2}} \pm \frac{\hat{j}}{\sqrt{2}}$$

$$\mathsf{B.}\pm\frac{\hat{i}}{2}\pm\frac{\hat{j}}{2}-\frac{\hat{k}}{\sqrt{2}}$$

$$\mathsf{C.}\,\frac{\hat{i}}{\sqrt{2}}-\frac{\hat{k}}{\sqrt{2}}$$

D. none of these

## Answer: d



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**49.** In a quadrilateral ABCD,  $\vec{A}C$  is the bisector of  $\vec{A}Band\vec{A}D$ , angle between  $\vec{A}Band\vec{A}D$  is  $2\pi/3$ ,  $15\left|\vec{A}C\right|=3\left|\vec{A}B\right|=5\left|\vec{A}D\right|$ . Then the angle

between  $\vec{B}Aand\vec{C}D$  is  $(a)\cos^{-1}\left(\frac{\sqrt{14}}{7\sqrt{2}}\right)$  b.  $\cos^{-1}\left(\frac{\sqrt{21}}{7\sqrt{3}}\right)$  c.  $\cos^{-1}\left(\frac{2}{\sqrt{7}}\right)$  d.  $\cos^{-1}\left(\frac{2\sqrt{7}}{14}\right)$ 

C. 
$$\cos^{-1} \frac{2}{\sqrt{7}}$$
D.  $\cos^{-1} \frac{2\sqrt{7}}{14}$ 

Answer: c

 $A. \cos^{-1} \frac{\sqrt{14}}{7\sqrt{2}}$ 

 $B.\cos^{-1}\frac{\sqrt{21}}{7\sqrt{3}}$ 



**50.** In fig. AB, DE and GF are parallel to each other and AD, BG and EF are parallel to each other. If CD: CE = CG: CB = 2:1, then the value of area (AEG): area (ABD) is equal to 7/2 b. 3 c. 4 d. 9/2

**A.** 7/2

C. 4

D.9/2

## Answer: b



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**51.** Vector  $\vec{a}$  in the plane of  $\vec{b} = 2\hat{i} + \hat{j}and\vec{c} = \hat{i} - \hat{j} + \hat{k}$  is such that it is equally inclined to  $\vec{b}and\vec{d}$  where  $\vec{d} = \hat{j} + 2\hat{k}$ . The value of  $\vec{a}$  is  $\frac{\hat{i} + \hat{j} + \hat{k}}{\sqrt{2}}$  b.

$$\frac{\hat{i} - \hat{j} + \hat{k}}{\sqrt{3}} \text{ c. } \frac{2\hat{i} + \hat{j}}{\sqrt{5}} \text{ d. } \frac{2\hat{i} + \hat{j}}{\sqrt{5}}$$

A. 
$$\frac{\hat{i} + \hat{j} + \hat{k}}{\sqrt{3}}$$

B. 
$$\frac{\hat{i} - \hat{j} + \hat{k}}{\sqrt{3}}$$

$$C. \frac{2\hat{i} + \hat{j}}{\sqrt{5}}$$

D. 
$$\frac{2\hat{i} + \hat{j}}{\sqrt{5}}$$



- **52.** Let ABCD be a tetrahedron such that the edges AB, AC and AD are mutually perpendicular. Let the area of triangles ABC, ACD and ADB be
- 3, 4 and 5sq. units, respectively. Then the area of triangle BCD is

$$a.5\sqrt{2}$$

c. 
$$\frac{\sqrt{5}}{2}$$

d. 
$$\frac{5}{2}$$

A. 
$$5\sqrt{2}$$

c. 
$$\frac{\sqrt{5}}{2}$$

D. 
$$\frac{5}{2}$$

53. Let 
$$f(t) = [t]\hat{i} + (t - [t])\hat{j} + [t + 1]\hat{k}$$
, where[.] denotes the greatest integer

function. Then the vectors  $f\left(\frac{5}{4}\right)$  and f(t), 0 < t < 1 are (a) parallel to each other (b) perpendicular (c) inclined at  $\cos^{-1}2\left(\sqrt[4]{7\left(1-t^2\right)}\right)$  (d) inclined at

$$\cos^{-1}\left(\frac{8+t}{\sqrt{1+t^2}}\right);$$

A. parallel to each other

B. perpendicular to each other

C. inclined at 
$$\frac{\cos^{-1}2}{\sqrt{7}(1-t^2)}$$

D. inclined at 
$$\frac{\cos^{-1}(8+t)}{9\sqrt{1+t^2}}$$

#### Answer: d



**54.** If  $\vec{a}$  is parallel to  $\vec{b} \times \vec{c}$  , then  $(\vec{a} \times \vec{b}).(\vec{a} \times \vec{c})$  is equal to a.  $|\vec{a}|^2(\vec{b}.\vec{c})$ 

- b.  $|\vec{b}|^2(\vec{a}.\vec{c})$  c.  $|\vec{c}|^2(\vec{a}.\vec{b})$  d. none of these
  - A.  $|\vec{a}|^2 (\vec{b}. \vec{c})$
  - B.  $\left| \vec{b} \right|^2 \left( \vec{a} \cdot \vec{c} \right)$
  - C.  $|\vec{c}|^2 (\vec{a}.\vec{b})$
  - D. none of these

#### Answer: a



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**55.** The three vectors  $\hat{i} + \hat{j}$ ,  $\hat{j} + \hat{k}$ ,  $\hat{k} + \hat{i}$  taken two at a time form three planes, The three unit vectors drawn perpendicular to these planes form a parallelopiped of volume:

**A.** 1/3

B. 4

C. 
$$(3\sqrt{3})/4$$

D. 
$$4\sqrt{3}$$

# Answer: d



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**56.** If 
$$\vec{d} = \vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a}$$
 is non-zero vector and 
$$\left| (\vec{d} \cdot \vec{c}) (\vec{a} \times \vec{b}) + (\vec{d} \cdot \vec{a}) (\vec{b} \times \vec{c}) + (\vec{d} \cdot \vec{b}) (\vec{c} \times \vec{a}) \right| = 0, \text{ then}$$

$$\mathbf{a}.\left|\vec{a}\right| = \left|\vec{b}\right| = \left|\vec{c}\right|$$

b. 
$$|\vec{a}| + |\vec{b}| + |\vec{c}| = |d|$$

c.  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  are coplanar

d. none of these

A. 
$$\left| \vec{a} \right| = \left| \vec{b} \right| = \left| \vec{c} \right|$$

$$B. \left| \vec{a} \right| + \left| \vec{b} \right| + \left| \vec{c} \right| = \left| \vec{d} \right|$$

C. 
$$\vec{a}$$
,  $\vec{b}$  and  $\vec{c}$  are coplanar

D. none of these

#### Answer: c



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**57.** If

$$\left| \vec{a} \right| = 2$$
 and  $\left| \vec{b} \right| = 3$  and  $\vec{a} \cdot \vec{b} = 0$ , then  $\left| \left( \vec{a} \times \left( \vec{a} \times \left( \vec{a} \times \left( \vec{a} \times \vec{b} \right) \right) \right) \right) \right|$ 

- A.  $48\hat{b}$
- B. - $48\hat{b}$
- C. 48â
- D. -48â

## Answer: a



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**58.** If the two diagonals of one its faces are  $6\hat{i} + 6\hat{k}$  and  $4\hat{j} + 2\hat{k}$  and of the edges not containing the given diagonals is  $c = 4\hat{j} - 8\hat{k}$ , then the volume

of a parallelepiped is a. 60 b. 80 c. 100 d. 120 A. 60 B. 80 C. 100 D. 120 Answer: d Watch Video Solution 59. The volume of a tetrahedron formed by the coterminous edges  $\vec{a}, \vec{b}, and \vec{c}$  is 3. Then the volume of the parallelepiped formed by the coterminous edges  $\vec{a} + \vec{b}$ ,  $\vec{b} + \vec{c}$  and  $\vec{c} + \vec{a}$  is 6 b. 18 c. 36 d. 9 A. 6 B. 18 C. 36

## Answer: c



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- **60.** If  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  are three mutually orthogonal unit vectors, then the triple product  $\left[\vec{a} + \vec{b} + \vec{c}\vec{a} + \vec{b}\vec{b} + \vec{c}\right]$  equals: (a.) 0 (b.) 1 or -1 (c.) 6 (d.) 3
  - A. 0
  - B. 1 or -1
  - C. 1
  - D. 3

# Answer: b



**61.** Vector  $\vec{c}$  is perpendicular to vectors  $\vec{a}=(2,-3,1)$  and  $\vec{b}=(1,-2,3)$ and satisfies the condition  $\vec{x} \cdot (\hat{i} + 2\hat{j} - 7\hat{k}) = 10$ . Then vector  $\vec{c}$  is equal to a.(7, 5, 1) b. -7, -5, -1 c. 1, 1, -1 d. none of these

**62.** Given  $\vec{a} = x\hat{i} + y\hat{j} + 2\hat{k}$ ,  $\vec{b} = \hat{i} - \hat{j} + \hat{k}$ ,  $\vec{c} = \hat{i} + 2\hat{j}$ ,  $\vec{a} \perp \vec{b}$ ,  $\vec{a} \cdot \vec{c} = 4$  then

C. 1,1,-1

## Answer: a



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find the value of  $\begin{bmatrix} \vec{a} & \vec{b} & \vec{c} \end{bmatrix}$ .

A. A. 
$$\left[\vec{a}\vec{b}\vec{c}\right]^2 = \left|\vec{a}\right|$$

$$B. B. \left[ \vec{a} \vec{b} \vec{c} \right] = \left| \vec{a} \right|$$

$$\mathsf{C.}\,\mathsf{C.}\!\left[\vec{a}\,\vec{b}\,\vec{c}\,\right] = 0$$

D. D. 
$$\left[\vec{a}\vec{b}\vec{c}\right] = \left|\vec{a}\right|^2$$

## Answer: d



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**63.** Let 
$$\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$$
,  $\vec{b} = b_1\hat{i} + b_2\hat{j} + b_3\hat{k}$  and  $\vec{c} = c_1\hat{i} + c_2\hat{j} + c_3\hat{k}$  be three non-zero vectors such that  $\vec{c}$  is a unit vector perpendicular to both  $\vec{a}$  and  $\vec{b}$ . If the angle between  $\vec{a}$  and  $\vec{b}is\pi/6$  then the value of

$$\begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{vmatrix}$$
 is

A. 0

B. 1

C. 
$$\frac{1}{4} \left( a_1^2 + a_2^2 + a_3^2 \right) \left( b_1^2 + b_2^2 + b_3^2 \right)$$

D. 
$$\frac{3}{4} \left( a_1^2 + a_2^2 + a_3^2 \right) \left( b_1^2 + b_2^2 + b_3^2 \right)$$

#### Answer: c



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**64.** Let  $\vec{r}$ ,  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be four non-zero vectors such that

$$\vec{r} \cdot \vec{a} = 0$$
,  $|\vec{r} \times \vec{b}| = |\vec{r}| |\vec{b}|$ ,  $|\vec{r} \times \vec{c}| = |\vec{r}| |\vec{c}|$  then

$$\begin{bmatrix} \vec{a} & \vec{b} & \vec{c} \end{bmatrix} =$$

A. |a||b||c|

 $\mathsf{B.-}|a||b||c|$ 

C. 0

D. none of these

#### Answer: c



**65.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are such that  $\begin{bmatrix} \vec{a} & \vec{b} & \vec{c} \end{bmatrix} = 1$ ,  $\vec{c} = \lambda (\vec{a} \times \vec{b})$ , angle between  $\vec{c}$ and  $\vec{b}$  is  $2\pi/3$ ,  $\left|\vec{a}\right| = \sqrt{2}$ ,  $\left|\vec{b}\right| = \sqrt{3}$  and  $\left|\vec{c}\right| = \frac{1}{\sqrt{3}}$  then the angle between  $\vec{a}$ 

A. (a) 
$$\frac{\pi}{6}$$
B. (b)  $\frac{\pi}{4}$ 

and  $\vec{b}$  is

C. (c) 
$$\frac{\pi}{3}$$
  
D. (d)  $\frac{\pi}{2}$ 

## Answer: b



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**66.** If  $4\vec{a} + 5\vec{b} + 9\vec{c} = 0$ , then  $(\vec{a} \times \vec{b}) \times [(\vec{b} \times \vec{c}) \times (\vec{c} \times \vec{a})]$  is equal to a. vector perpendicular to the plane of a, b, c b. a scalar quantity c.  $\vec{0}$  d. none of these

A. a vector perpendicular to the plane of  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$ 

- B. a scalar quantity
- $\vec{C}$ .  $\vec{0}$
- D. none of these

#### Answer: c



- **67.** Value of  $\left[\vec{a} \times \vec{b}, \vec{a} \times \vec{c}, \vec{d}\right]$  is always equal to a.  $\left(\vec{a}\vec{d}\right)\left[\vec{a}\vec{b}\vec{c}\right]$  b.
- $(\vec{a}\vec{c})[\vec{a}\vec{b}\vec{d}]$  c.  $(\vec{a}\vec{b})[\vec{a}\vec{b}\vec{d}]$  d. none of these
  - $A. \left(\vec{a}. \vec{d}\right) \left[\vec{a}\vec{b}\vec{c}\right]$
  - B. `(veca.vecc)[veca vecb vecd]
  - $\mathsf{C.}\left(\vec{a}.\,\vec{b}\right)\left[\vec{a}\,\vec{b}\,\vec{d}\right]$
  - D. none of these

#### Answer: a



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**68.** Let  $\vec{a}$  and  $\vec{b}$  be mutually perpendicular unit vectors. Then for any

$$\vec{r} = \left(\vec{r}\hat{a}\right)\hat{a} + \left(\vec{r}\hat{b}\right)\hat{b} + \left(\vec{r}\hat{a} \times \hat{b}\right)(\hat{a} \times \hat{b})$$

$$\vec{r} = \begin{pmatrix} \cdot \\ \vec{r} \hat{a} \end{pmatrix} - \begin{pmatrix} \cdot \\ \vec{r} \hat{b} \end{pmatrix} \hat{b} - \begin{pmatrix} \cdot \\ \vec{r} \hat{a} \times \hat{b} \end{pmatrix} (\hat{a} \times \hat{b})$$

$$\vec{r} = \begin{pmatrix} \cdot \\ \vec{r} \hat{a} \end{pmatrix} \hat{a} - \begin{pmatrix} \cdot \\ \vec{r} \hat{b} \end{pmatrix} \hat{b} + \begin{pmatrix} \cdot \\ \vec{r} \hat{a} \times \hat{b} \end{pmatrix} (\hat{a} \times \hat{b})$$
 none of these

A. 
$$\vec{r} = (\vec{r}.\hat{a})\hat{a} + (\vec{r}.\hat{b})\hat{b} + (\vec{r}.(\vec{a} \times \hat{b}))(\hat{a} \times \hat{b})$$

B. 
$$\vec{r} = (\vec{r}.\hat{a}) - (\vec{r}.\hat{b})\hat{b} - (\vec{r}.(\vec{a} \times \hat{b}))(\hat{a} \times \hat{b})$$

C. 
$$\vec{r} = (\vec{r}.\hat{a})\hat{a} - (\vec{r}.\hat{b})\hat{b} - (\vec{r}.(\vec{a} \times \hat{b}))(\hat{a} \times \hat{b})$$

D. none of these

## Answer: a



**69.** Let 
$$\vec{a}$$
 and  $\vec{b}$  be unit vectors that are perpendicular to each other. Then

$$\left[\vec{a} + \left(\vec{a} \times \vec{b}\right)\vec{b} + \left(\vec{a} \times \vec{b}\right)\vec{a} \times \vec{b}\right]$$
 will always be equal to 1 b. 0 c. -1 d. none of these

B. 0

**C**. - 1

D. none of these

## Answer: a



- **70.**  $\vec{a}$  and  $\vec{b}$  are two vectors such that  $|\vec{a}| = 1$ ,  $|\vec{b}| = 4$  and  $\vec{a}$ .  $\vec{b}$ =2. If  $\vec{c}$  =  $(2\vec{a} \times \vec{b})$  -  $3\vec{b}$  then find angle between  $\vec{b}$  and  $\vec{c}$ .
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**71.** If  $\vec{b}$  and  $\vec{c}$  are unit vectors, then for any arbitary vector

$$\vec{a}$$
,  $\left(\left(\left(\vec{a} \times \vec{b}\right) + \left(\vec{a} \times \vec{c}\right)\right) \times \left(\vec{b} \times \vec{c}\right)\right)$ .  $\left(\vec{b} - \vec{c}\right)$  is always equal to



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**72.** If  $\vec{a} \cdot \vec{b} = \beta$  and  $\vec{a} \times \vec{b} = \vec{c}$ , then  $\vec{b}$  is

A. 
$$\frac{\left(\beta \vec{a} - \vec{a} \times \vec{c}\right)}{|\vec{a}|^2}$$

B. 
$$\frac{\left(\beta \vec{a} + \vec{a} \times \vec{c}\right)}{|\vec{a}|^2}$$

C. 
$$\frac{\left(\beta\vec{c} + \vec{a} \times \vec{c}\right)}{|\vec{a}|^2}$$

D. 
$$\frac{\left(\beta\vec{c} + \vec{a} \times \vec{c}\right)}{|\vec{a}|^2}$$

Answer: a



**73.** If  $a(\vec{\alpha} \times \vec{\beta}) + b(\vec{\beta} \times \vec{\gamma}) + c(\vec{\gamma} \times \vec{\alpha}) = 0$  and at least one of a, b and c is nonzero, then vectors  $\vec{\alpha}$ ,  $\vec{\beta}$  and  $\vec{\gamma}$  are a. parallel b. coplanar c. mutually perpendicular d. none of these

A. parallel

B. coplanar

C. mutually perpendicular

D. none of these

## Answer: b



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**74.** If  $(\vec{a} \times \vec{b}) \times (\vec{b} \times \vec{c}) = \vec{b}$ , where  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  are nonzero vectors, then 1.

 $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  can be coplanar  $2.\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  must be coplanar  $3.\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$ 

cannot be coplanar 4.none of these

A.  $\vec{a}$ ,  $\vec{b}$  and  $\vec{v}$  can be coplanar

B.  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  must be coplanar

C.  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  cannot be coplanar

D. none of these

#### Answer: c



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**75.** If  $\vec{r} \cdot \vec{a} = \vec{r} \cdot \vec{b} = \vec{r} \cdot \vec{c} = \frac{1}{2}$  for some non zero vector  $\vec{r}$  and  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are non coplanar, then the area of the triangle whose vertices are

 $A(\vec{a}), B(\vec{b})$  and  $C(\vec{c})$  is

A. 
$$\left| \left[ \vec{a} \vec{b} \vec{c} \right] \right|$$

B.  $|\vec{r}|$ 

C. 
$$\left| \left[ \vec{a}\vec{b}\vec{c} \right] \vec{r} \right|$$

D. none of these

Answer: c

$$3x^2 + 8xy + 2y^2 - 3 = 0$$
 at its point  $P(1, 0)$  can be  $6\hat{i} + 8\hat{j}$  b.  $-8\hat{i} + 3\hat{j}$  c.  $6\hat{i} - 8\hat{j}$  d.  $8\hat{i} + 6\hat{j}$ 

A. 
$$6\hat{i} + 8\hat{j}$$

$$B. -8\hat{i} + 3\hat{j}$$

C. 
$$6\hat{i}$$
 -  $8\hat{j}$ 

D. 
$$8\hat{i} + 6\hat{j}$$

# Answer: a



**77.** If 
$$\vec{a}$$
 and  $\vec{b}$  are two unit vectors incline at angle  $\pi/3$  , then

$$\left\{\vec{a} \times \left(\vec{b} + \vec{a} \times \vec{b}\right)\right\}\vec{b}$$
 is equal to  $\frac{-3}{4}$  b.  $\frac{1}{4}$  c.  $\frac{3}{4}$  d.  $\frac{1}{2}$ 

- B.  $\frac{1}{4}$
- D.  $\frac{1}{2}$

# Answer: a



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coplanar with 
$$\vec{a}$$
 and  $\vec{b}$  vector  $\vec{r} imes \vec{a}$  is equal to

**78.** If  $\vec{a}$  and  $\vec{b}$  are othogonal unit vectors, then for a vector  $\vec{r}$  non -

A. 
$$\left[\vec{r}\vec{a}\vec{b}\right]\vec{b} - \left(\vec{r}.\vec{b}\right)\left(\vec{b}\times\vec{a}\right)$$

$$\mathsf{B.}\left[\vec{r}\vec{a}\vec{b}\right]\!\!\left(\vec{a}+\vec{b}\right)$$

$$\mathsf{C.}\left[\vec{r}\vec{a}\vec{b}\right]\vec{a}+\left(\vec{r}.\vec{a}\right)\vec{a}\times\vec{b}$$

D. none of these

# Answer: a

**79.** If  $\vec{a}, \vec{b}, \vec{c}$  are any three non-coplanar vectors then the equation

$$\left[\vec{b} \times \vec{c} \, \vec{c} \times \vec{a} \, \vec{a} \times \vec{b}\right] x^2 + \left[\vec{a} + \vec{b} \, \vec{b} + \vec{c} \, \vec{c} + \vec{a}\right] x + 1 + \left[\vec{b} - \vec{c} \, \vec{c} - \vec{a} \, \vec{a} - \vec{b}\right] = 0$$

has roots (A) real and distinct (B) real (C) equal (D) imaginary

A. real and distinct

B. real

C. equal

D. imaginary

## Answer: c



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**80.** Solve the simultaneous vector equations for  $\vec{x}$  and  $\vec{y}: \vec{x} + \vec{c} \times \vec{y} = \vec{a}$  and  $\vec{y} + \vec{c} \times \vec{x} = \vec{b}$ ,  $\vec{c} \neq 0$ 

A. 
$$\vec{x} = \frac{\vec{b} \times \vec{c} + \vec{a} + (\vec{c}.\vec{a})\vec{c}}{1 + \vec{c}.\vec{c}}$$

B. 
$$\vec{x} = \frac{\vec{c} \times \vec{b} + \vec{b} + (\vec{c} \cdot \vec{a})\vec{c}}{1 + \vec{c} \cdot \vec{c}}$$

$$C. \vec{y} = \frac{\vec{a} \times \vec{c} + \vec{b} + (\vec{c}. \vec{b})\vec{c}}{1 + \vec{c}. \vec{c}}$$

D. none of these

# Answer: b



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**81.** The condition for equations  $\vec{r} \times \vec{a} = \vec{b}$  and  $\vec{r} \times \vec{c} = \vec{d}$  to be consistent is

a. 
$$\vec{b}\vec{c} = \vec{a}\vec{d}$$
 b.  $\vec{a}\vec{b} = \vec{c}\vec{d}$  c.  $\vec{b}\vec{c} + \vec{a}\vec{d} = 0$  d.  $\vec{a}\vec{b} + \vec{c}\vec{d} = 0$ 

A. 
$$\vec{b}$$
.  $\vec{c} = \vec{a}$ .  $\vec{d}$ 

$$\mathbf{B}.\ \vec{a}.\ \vec{b} = \vec{c}.\ \vec{d}$$

C. 
$$\vec{b}$$
.  $\vec{c} + \vec{a}$ .  $\vec{d} = 0$ 

$$D. \vec{a}. \vec{b} + \vec{c}. \vec{d} = 0$$

# Answer: c



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- **82.** If  $\vec{a} = 2\hat{i} + 3\hat{j} + \hat{k}$ ,  $\vec{b} = \hat{i} 2\hat{j} + \hat{k}$  and  $\vec{c} = -3\hat{i} + \hat{j} + 2\hat{k}$ , then  $\left[\vec{a}\vec{b}\vec{c}\right] = -3\hat{i} + \hat{j} + 2\hat{k}$

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- **83.** If  $\vec{a} = 2\hat{i} + 3\hat{j} + 8\hat{k}$  is perpendicular to  $\vec{b} = 4\hat{i} 4\hat{j} + \alpha\hat{k}$ , then find the value of  $\alpha$ 
  - A.  $-\frac{1}{2}$
  - B.  $\frac{1}{2}$
  - C. 1
  - D. -1

# Answer: a



**84.** Let 
$$\vec{a}(x) = (\sin x)\hat{i} + (\cos x)\hat{j}$$
 and  $\vec{b}(x) = (\cos 2x)\hat{i} + (\sin 2x)\hat{j}$  be two variable vectors  $(x \in R)$ . Then  $\vec{a}(x)$  and  $\vec{b}(x)$  are

A. collinear for unique value of x

B. perpendicular for infinte values of x.

C. zero vectors for unique value of x

D. none of these

#### Answer: b



**85.** For any vectors 
$$\vec{a}$$
 and  $\vec{b}$ ,  $(\vec{a} \times \hat{i})$ .  $(\vec{b} \times \hat{i}) + (\vec{a} \times \hat{j})$ .  $(\vec{b} \times \hat{j}) + (\vec{a} \times \hat{k})$ .  $(\vec{b} \times \hat{k})$  is always equal to

A. A. 
$$\vec{a}$$
.  $\vec{b}$ 

B. B.  $2\vec{a}$ .  $\vec{b}$ 

C. C. zero

D. D. none of these

## Answer: b



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**86.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three non coplanar vectors and  $\vec{r}$  is any vector in space,

$$(\vec{a} \times \vec{b}) \times (\vec{r} \times \vec{c}) + (\vec{b} \times \vec{c}) \times (\vec{r} \times \vec{a}) + (\vec{c} \times \vec{a}) \times (\vec{r} \times \vec{b}) =$$
(A)

$$\left[\vec{a}\vec{b}\vec{c}\right] \text{(B) } 2\left[\vec{a}\vec{b}\vec{c}\right]\vec{r} \text{ (C) } 3\left[\vec{a}\vec{b}\vec{c}\right]\vec{r} \text{ (D) } 4\left[\vec{a}\vec{b}\vec{c}\right]\vec{r}$$

A. 
$$\left[\vec{a}\vec{b}\vec{c}\right]\vec{r}$$

$$\mathsf{B.}\,2\Big[\vec{a}\vec{b}\vec{c}\,\Big]\vec{r}$$

C. 
$$3\left[\vec{a}\vec{b}\vec{c}\right]\vec{r}$$

D. none of these



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**87.** If  $\vec{P} = \frac{\vec{b} \times \vec{c}}{\left[\vec{a}\vec{b}\vec{c}\right]}$ .  $\vec{q} = \frac{\vec{c} \times \vec{a}}{\left[\vec{a}\vec{b}\vec{c}\right]}$  and  $\vec{r} = \frac{\vec{a} \times \vec{b}}{\left[\vec{a}\vec{b}\vec{c}\right]}$ , where  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are

three non- coplanar vectors then the value of the expression

$$(\vec{a} + \vec{b} + \vec{c}).(\vec{p} + \vec{q} + \vec{r})$$
 is

- A. 3
- B. 2
- C. 1
- D. 0

Answer: a



**88.**  $A(\vec{a}), B(\vec{b}), C(\vec{c})$  are the vertices of the triangle ABC and  $R(\vec{r})$  is any point in the plane of triangle ABC , then  $\vec{r}$ .  $\left(\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a}\right)$  is always equal to

B. 
$$\left[\vec{a}\vec{b}\vec{c}\right]$$

C. - 
$$\left[\vec{a}\vec{b}\vec{c}\right]$$

D. none of these

## Answer: b



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$$\vec{a} \times (\vec{b} \times \vec{c})$$
, then the value of  $[\vec{a} \times (\vec{b} \times \vec{c})] \times \vec{c}$  is equal to

**89.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are non-coplanar vectors and  $\vec{a} \times \vec{c}$  is perpendicular to

A. 
$$\left[\vec{a}\vec{b}\vec{c}\right]\vec{c}$$

B. 
$$\left[\vec{a}\vec{b}\vec{c}\right]\vec{b}$$

$$\vec{c}$$
.  $\vec{0}$ 

D. 
$$\left[\vec{a}\vec{b}\vec{c}\right]\vec{a}$$

#### Answer: c



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**90.** If V be the volume of a tetrahedron and V' be the volume of another tetrahedran formed by the centroids of faces of the previous tetrahedron and V = KV', thenK is equal to a. 9 b. 12 c. 27 d. 81

A. 9

B. 12

C. 27

D. 81

#### Answer: c



**91.** 
$$\left[ \left( \vec{a} \times \vec{b} \right) \times \left( \vec{b} \times \vec{c} \right) \left( \vec{b} \times \vec{c} \right) \times \left( \vec{c} \times \vec{a} \right) \left( \vec{c} \times \vec{a} \right) \times \left( \vec{a} \times \vec{b} \right) \right]$$
 is equal to

(where  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are nonzero non-coplanar vector) a.  $\left[\vec{a}\vec{b}\vec{c}\right]^2$  b.  $\left[\vec{a}\vec{b}\vec{c}\right]^3$  c.

$$\left[\vec{a}\vec{b}\vec{c}\right]^4$$
 d.  $\left[\vec{a}\vec{b}\vec{c}\right]$ 

A. 
$$\left[\vec{a}\vec{b}\vec{c}\right]^2$$

B. 
$$\left[\vec{a}\vec{b}\vec{c}\right]^3$$

$$\mathsf{C.}\left[\vec{a}\vec{b}\vec{c}\right]^4$$

D. 
$$\left[\vec{a}\vec{b}\vec{c}\right]$$

#### Answer: c



92.

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$$\vec{r} = x_1 (\vec{a} \times \vec{b}) + x_2 (\vec{b} \times \vec{c}) + x_3 (\vec{c} \times \vec{a})$$
 and  $4 [\vec{a}\vec{b}\vec{c}] = 1$  then  $x_1 + x_2 + x_3$ 

If

is equal to

$$B. \frac{1}{4}\vec{r}. \left(\vec{a} + \vec{b} + \vec{c}\right)$$

A.  $\frac{1}{2}\vec{r}$ .  $(\vec{a} + \vec{b} + \vec{c})$ 

C. 
$$2\vec{r}$$
.  $\left(\vec{a} + \vec{b} + \vec{c}\right)$ 
D.  $4\vec{r}$ .  $\left(\vec{a} + \vec{b} + \vec{c}\right)$ 

### Answer: d



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**93.** If  $\vec{a} \perp \vec{b}$  then vector  $\vec{v}$  in terms of  $\vec{a}$  and  $\vec{b}$  satisfying the equations

$$\vec{v} \cdot \vec{a} = 0$$
 and  $\vec{v} \cdot \vec{b} = 1$  and  $\left[ \vec{v} \cdot \left( \vec{a} \times \vec{b} \right) \right] = 1$  is

A. 
$$\frac{\vec{b}}{\left|\vec{b}\right|^2} + \frac{\vec{a} \times \vec{b}}{\left|\vec{a} \times \vec{b}\right|^2}$$

B. 
$$\frac{\vec{b}}{\left|\vec{b}\right|} + \frac{\vec{a} \times \vec{b}}{\left|\vec{a} \times \vec{b}\right|^2}$$
C.  $\frac{\vec{b}}{\left|\vec{a} \times \vec{b}\right|^2}$ 

 $\left| \vec{b} \right| \quad \left| \vec{a} \times \vec{b} \right|$ 

#### Answer: a



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**94.** If  $\vec{a}' = \hat{i} + \hat{j}$ ,  $\vec{b}'\hat{i} - \hat{j} + 2\hat{k}and\vec{c}'2\hat{i} + \hat{j} - \hat{k}$ , then the altitude of the parallelepiped formed by the vectors  $\vec{a}$ ,  $\vec{b}and\vec{c}$  having base formed by  $\vec{b}and\vec{c}$  is (where  $\vec{a}'$  is reciprocal vector  $\vec{a}$ , et · ) 1 b.  $3\sqrt{2}/2$  c.  $1/\sqrt{6}$  d.  $1/\sqrt{2}$ 

- A. 1
- B.  $3\sqrt{2}/2$
- C.  $1/\sqrt{6}$
- D.  $1/\sqrt{2}$

#### Answer: d



**95.** If  $\vec{a} = \hat{i} + \hat{j}$ ,  $\vec{b} = \hat{j} + \hat{k}$ ,  $\vec{c} = \hat{k} + \hat{i}$  then in the reciprocal system of vectors

 $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  reciprocal  $\vec{a}$  of vector  $\vec{a}$  is

A. 
$$\frac{\hat{i} + \hat{j} + \hat{k}}{2}$$

$$B. \frac{\hat{i} - \hat{j} + \hat{k}}{2}$$

$$\mathsf{C.}\,\frac{-\hat{i}-\hat{j}+\hat{k}}{2}$$

D. 
$$\frac{\hat{i} + \hat{j} - \hat{k}}{2}$$

#### Answer: d



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**96.** If unit vectors  $\vec{a}$  and  $\vec{b}$  are inclined at angle  $2\theta$  such that

$$\left| \vec{a} - \vec{b} \right| < 1$$
 and  $0 \le \theta \le \pi$ , then  $\theta$  lies in interval a. $[0, \pi/6)$  b.  $(5\pi/6, \pi]$  c.

$$[\pi/6, \pi/2]$$
 d.  $[\pi/2, 5\pi/6]$ 

A. 
$$[0, \pi/6)$$

B. 
$$(5\pi/6, \pi]$$

C. 
$$[\pi/6, \pi/2]$$

D. 
$$(\pi/2, 5\pi/6]$$

### Answer: a,b



### **Watch Video Solution**

**97.** 
$$\vec{a}$$
,  $\vec{b}$  and  $\vec{c}$  are non-collinear if  $\vec{a} \times (\vec{b} \times \vec{c}) + (\vec{a} \cdot \vec{b}) \vec{b} = (4 - 2x - \sin y) \vec{b} + (x^2 - 1) \vec{c}$  and  $(\vec{c} \cdot \vec{c}) \vec{a} = \vec{c}$  Then

if

a. 
$$x = 1$$
 b.  $x = -1$  c.  $y = (4n + 1)\pi/2, n \in I$  d.  $y = (2n + 1)\pi/2, n \in I$ 

A. 
$$x = 1$$

B. x = -1

C. 
$$y = (4n + 1)\frac{\pi}{2}, n \in I$$

$$D. y(2n+1)\frac{\pi}{2}, n \in I$$

# Answer: a,c

**98.** Unit vectors  $\vec{a}$  and  $\vec{b}$  ar perpendicular, and unit vector  $\vec{c}$  is inclined at an angle  $\theta$  to both  $\vec{a}$  and  $\vec{b}$ . If  $\alpha \vec{a} + \beta \vec{b} + \gamma (\vec{a} \times \vec{b})$ , then which of the following is incorrect?

A. 
$$\alpha = \beta$$

B. 
$$y^2 = 1 - 2\alpha^2$$

$$C. y^2 = -\cos 2\theta$$

$$D. \beta^2 = \frac{1 + \cos 2\theta}{2}$$

Answer: a,b,c,d



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**99.** If vectors  $\vec{a}$  and  $\vec{b}$  are two adjacent sides of a parallelogram, then the vector respresenting the altitude of the parallelogram which is the

perpendicular to 
$$a$$
 is a. $\vec{b}$  +  $\frac{\vec{b} \times \vec{a}}{|\vec{a}|^2}$  b.  $\frac{\vec{a}\vec{b}}{|\vec{b}|^2}$  c.  $\vec{b}$  -  $\frac{\vec{b}\vec{a}}{|\vec{a}|^2}$  d.  $\frac{\vec{a} \times (\vec{b} \times \vec{a})}{|\vec{b}|^2}$ 

A. 
$$\frac{\left(\vec{a}.\vec{b}\right)}{|\vec{a}|^2}\vec{a}-\vec{b}$$

B. 
$$\frac{\left|\vec{a}\right|^{2}}{\left|\vec{a}\right|^{2}}\left\{\left|\vec{a}\right|^{2}\vec{b}-\left(\vec{a}.\vec{b}\right)\vec{a}\right\}$$

c. 
$$\frac{\vec{a} \times (\vec{a} \times \vec{b})}{|\vec{a}|^2}$$

D. 
$$\frac{\vec{a} \times (\vec{b} \times \vec{a})}{|\vec{b}|^2}$$

### Answer: a.b.c



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**100.** If  $\vec{a} \times (\vec{b} \times \vec{c})$  is perpendicular to  $(\vec{a} \times \vec{b}) \times \vec{c}$ , we may have a.

$$(\vec{a}.\vec{c})|\vec{b}|^2 = (\vec{a}.\vec{b})(\vec{b}.\vec{c})(\vec{c}.\vec{a}) \text{ b. } \vec{a}\vec{b} = 0 \text{ c. } \vec{a}\vec{c} = 0 \text{ d. } \vec{b}\vec{c} = 0$$

A. 
$$(\vec{a}.\vec{b})|\vec{b}|^2 = (\vec{a}.\vec{b})(\vec{b}.\vec{c})$$

$$\mathsf{B.}\;\vec{a}.\;\vec{b}\,=\,0$$

C. 
$$\vec{a}$$
.  $\vec{c} = 0$ 

$$\mathsf{D}.\,\vec{b}.\,\vec{c}=0$$

#### Answer: a,c



### Watch Video Solution

**101.** Let  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  be vectors forming right-hand traid. Let

$$\vec{p} = \frac{\vec{b} \times \vec{c}}{\left[\vec{a}\vec{b}\vec{c}\right]}, \vec{q} = \frac{\vec{c} \times \vec{a}}{\left[\vec{a}\vec{b}\vec{c}\right]}, and \vec{r} = \frac{\vec{a} \times \vec{b}}{\left[\vec{a}\vec{b}\vec{c}\right]}, \text{ If } x \in \mathbb{R}^+, \text{ then}$$

a.  $x \left[ \vec{a} \vec{b} \vec{c} \right] + \frac{\left[ \vec{p} \vec{q} \vec{r} \right]}{x}$  has least value = 2. b.  $x^4 \left[ \vec{a} \vec{b} \vec{c} \right]^2 + \frac{\left[ \vec{p} \vec{q} \vec{r} \right]}{x^2}$  has least value =  $\left(\frac{3}{2}\right)^{2/3}$  c.  $\left[\vec{p}\vec{q}\vec{r}\right] > 0$  d. none of these

A. 
$$x \left[ \vec{a} \vec{b} \vec{c} \right] + \frac{\left[ \vec{p} \vec{q} \vec{r} \right]}{x}$$
 has least value 2

B. 
$$x^2 \left[ \vec{a} \vec{b} \vec{c} \right]^2 + \frac{\left[ \vec{p} \vec{q} \vec{r} \right]}{x^2}$$
 has least value  $\left( 3/2^{2/3} \right)$   
C.  $\left[ \vec{p} \vec{q} \vec{r} \right] > 0$ 

D. none of these

Answer: a.c



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**102.**  $a_1, a_2, a_3 \in R - \{0\}$  and  $a_1 + a_2 \cos 2x + a_3 \sin^2 x = 0$  " for all " x in R then

A. a) vectors  $\vec{a}=a_1\hat{i}+a_2\hat{j}+a_3\hat{k}$  and  $\vec{b}=4\hat{i}+2\hat{j}+\hat{k}$  are perpendicular to each other

B. b) vectors  $\vec{a}=a_1\hat{i}+a_2\hat{j}+a_3\hat{k}$  and  $\vec{b}=\hat{i}+\hat{j}+2\hat{k}$  are parallel to each each other

C. c) if vector  $\vec{a}=a_1\hat{i}+a_2\hat{j}+a_3\hat{k}$  is of length  $\sqrt{6}$  units, then on of the ordered trippplet  $\left(a_1,a_2,a_3\right)=(1,-1,-2)$ 

D. d) if  $2a_1 + 3a_2 + 6a_3 + 6a_3 = 26$ , then  $\left| \vec{a}\hat{i} + a_2\hat{j} + a_3\hat{k} \right| is 2\sqrt{6}$ 

Answer: a,b,c,d

**103.** If  $\vec{a}$  and  $\vec{b}$  are two vectors and angle between them is  $\theta$ , then

$$\left| \vec{a} \times \vec{b} \right|^2 + \left( \vec{a} \vec{b} \right)^2 = \left| \vec{a} \right|^2 \left| \vec{b} \right|^2 \qquad \left| \vec{a} \times \vec{b} \right| = \left( \vec{a} \vec{b} \right), \quad \text{if} \quad \theta = \pi/4$$

$$\vec{a} \times \vec{b} = \left(\vec{a}\vec{b}\right)\hat{n}$$
, (where  $\hat{n}$  is unit vector,) if  $\theta = \pi/4$  ( $\vec{a} \times \vec{b}$ ) $\vec{a} + \vec{b} = 0$ 

A. 
$$|\vec{a} \times \vec{b}|^2 + (\vec{a}.\vec{b})^2 = |\vec{a}|^2 |\vec{b}|^2$$

B. 
$$|\vec{a} \times \vec{b}|^2 + (\vec{a} \cdot \vec{b})^2$$
, if  $\theta = \pi/4$ 

C. 
$$\vec{a} \times \vec{b} = (\vec{a}. Vecb)\hat{n}$$
 ( where  $\hat{n}$  is a normal unit vector ) if  $\theta f = \pi/4$ 

D. 
$$(\vec{a} \times \vec{b})$$
.  $(\vec{a} + \vec{b}) = 0$ 

#### Answer: a,b,c,d



**104.** Let  $\vec{a}$  and  $\vec{b}$  be two non-zero perpendicular vectors. A vector  $\vec{r}$  satisfying the equation  $\vec{r} \times \vec{b} = \vec{a}$  can be

A. 
$$\vec{b} - \frac{\vec{a} \times \vec{b}}{\left|\vec{b}\right|^2}$$

$$B. 2\vec{b} - \frac{\vec{a} \times \vec{b}}{|\vec{b}|^2}$$

C. 
$$|\vec{a}|\vec{b} - \frac{\vec{a} \times \vec{b}}{|\vec{b}|^2}$$

D. 
$$|\vec{b}|\vec{b} - \frac{\vec{a} \times \vec{b}}{|\vec{b}|^2}$$

### Answer: a,b,cd,



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**105.** If vector  $\vec{b} = \left(\tan\alpha, -1, 2\sqrt{\sin\alpha/2}\right)$  and  $\vec{c} = \left(\tan\alpha, \tan\alpha, -\frac{3}{\sqrt{\sin\alpha/2}}\right)$  are orthogonal and vector  $\vec{a} = (1, 3, \sin2\alpha)$  makes an obtuse angle with the z-axis, then the value of  $\alpha$  is

B. 
$$\alpha = (4n + 1)\pi - \tan^{-1}2$$

A.  $\alpha = (4n + 1)\pi + \tan^{-1}2$ 

C. 
$$\alpha = (4n + 2)\pi + \tan^{-1}2$$

D. 
$$\alpha = (4n + 2)\pi - \tan^{-1}2$$

# Answer: b,d



106.

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 $\vec{r}$ 

be

а

unit

vector

satisfying

$$\vec{r} \times \vec{a} = \vec{b}$$
, where  $|\vec{a}| = \sqrt{3}$  and  $|\vec{b}| = \sqrt{2}$ , then

Let

A. 
$$\vec{r} = \frac{2}{3} \left( \vec{a} + \vec{a} \times \vec{b} \right)$$

$$B. \ \vec{r} = \frac{1}{3} \left( \vec{a} + \vec{a} \times \vec{b} \right)$$

C. 
$$\vec{r} = \frac{2}{3} (\vec{a} - \vec{a} \times \vec{b})$$

D. 
$$\vec{r} = \frac{1}{3} \left( -\vec{a} + \vec{a} \times \vec{b} \right)$$

# Answer: b,d

**107.** If 
$$\vec{a}$$
 and  $\vec{b}$  are unequal unit vectors such that  $(\vec{a} - \vec{b}) \times [(\vec{b} + \vec{a}) \times (2\vec{a} + \vec{b})] = \vec{a} + \vec{b}$  then angle  $\theta$  between  $\vec{a}$  and  $\vec{b}$  is

B. 
$$\pi/2$$

$$\mathsf{C}.\,\pi/4$$

D. 
$$\pi$$

#### Answer: b,d



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**108.** If  $\vec{a}$  and  $\vec{b}$  are two unit vectors perpenicualar to each other and  $\vec{c} = \lambda_1 \vec{a} + \lambda_2 \vec{b} + \lambda_3 (\vec{a} \times \vec{b})$ , then which of the following is (are) true?

$$\mathbf{A.}\,\lambda_1=\vec{a}.\,\vec{c}$$

$$B. \lambda_2 = \left| \vec{b} \times \vec{c} \right|$$

$$C.\lambda_3 = ||(\vec{a} \times \vec{b}| \times \vec{c}|)$$

D. 
$$\vec{c} = \lambda_1 \vec{a} + \lambda_2 \vec{b} + \lambda_3 (\vec{a} \times \vec{b})$$

#### Answer: a,d



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A. a unit vector

B. in the plane of  $\vec{a}$  and  $\vec{b}$ 

**109.** If vectors  $\vec{a}$  and  $\vec{b}$  are non collinear then  $\frac{\vec{a}}{|\vec{a}|} + \frac{\vec{b}}{|\vec{b}|}$  is

C. equally inclined to  $\vec{a}$  and  $\vec{b}$ 

D. perpendicular to  $\vec{a} \times \vec{b}$ 

### Answer: b,c,d



**110.** If  $\vec{a}$  and  $\vec{b}$  are non - zero vectors such that  $|\vec{a} + \vec{b}| = |\vec{a} - 2\vec{b}|$  then

$$A. \, 2\vec{a}. \, \vec{b} = \left| \vec{b} \right|^2$$

$$\mathbf{B}.\ \vec{a}.\ \vec{b} = \left|\vec{b}\right|^2$$

C. least value of 
$$\vec{a}$$
.  $\vec{b}$  +  $\frac{1}{\left|\vec{b}\right|^2 + 2}$  is  $\sqrt{2}$ 

D. least value of 
$$\vec{a} \cdot \vec{b} + \frac{1}{\left|\vec{b}\right|^2 + 2}$$
 is  $\sqrt{2} - 1$ 

#### Answer: a,d



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**111.** Let  $\vec{a}\vec{b}$  and  $\vec{c}$  be non-zero vectors and

$$\vec{V}_1 = \vec{a} \times (\vec{b} \times \vec{c})$$
 and  $\vec{V}_2 = (\vec{a} \times \vec{b}) \times \vec{c}$ .vectors  $\vec{V}_1$  and  $\vec{V}_2$  are equal .

Then

A.  $\vec{a}$  and  $\vec{b}$  ar orthogonal

B.  $\vec{a}$  and  $\vec{c}$  are collinear

C.  $\vec{b}$  and  $\vec{c}$  ar orthogonal

D.  $\vec{b} = \lambda (\vec{a} \times \vec{c})$  when  $\lambda$  is a scalar

#### Answer: b,d



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112. Vectors  $\vec{A}$  and  $\vec{B}$  satisfying the vector equation

$$\vec{A} + \vec{B} = \vec{a}, \vec{A} \times \vec{B} = \vec{b}$$
 and  $\vec{A}$ .  $\vec{a} = 1$ . where  $\vec{a}$  and  $\vec{b}$  are given vectors, are

A. 1. 
$$\vec{A} = \frac{\left(\vec{a} \times \vec{b}\right) - \vec{a}}{a^2}$$

B. 2. 
$$\vec{B} = \frac{(\vec{b} \times \vec{a}) + \vec{a}(a^2 - 1)}{a^2}$$

C. 3. 
$$\vec{A} = \frac{(\vec{a} \times \vec{b}) + \vec{a}}{a^2}$$

D. 4. 
$$\vec{B} = \frac{(\vec{b} \times \vec{a}) - \vec{a}(a^2 - 1)}{a^2}$$

### Answer: b,c,



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**113.** A vector  $\vec{d}$  is equally inclined to three vectors  $\vec{a} = \hat{i} + \hat{j} + \hat{k}, \ \vec{b} = 2\hat{i} + \hat{j} and \vec{c} = 3\hat{j} - 2\hat{k}$  Let  $\vec{x}, \ \vec{y}, and \ \vec{z}$  be three vectors in the plane of  $\vec{a}, \ \vec{b}; \ \vec{b}, \ \vec{c}; \ \vec{c}, \ \vec{a}$ , respectively. Then  $\vec{a}.\vec{x}.\vec{d} = -1$  b.  $\vec{y}.\vec{d} = 1$  c.  $\vec{z}.\vec{d} = 0$  d.  $\vec{r}.\vec{d} = 0$ , where  $\vec{r} = \lambda \vec{x} + \mu \vec{y} + \delta \vec{z}$ 

A. 
$$\vec{x}$$
.  $\vec{d} = -1$ 

$$B. \vec{y}. \vec{d} = 1$$

D. vecr.vecd=0, " where " vecr=lambda vecx + mu vecy +deltavecz`

#### Answer: c.d



**114.** Vectors Perpendicular to  $\hat{i} - \hat{j} - \hat{k}$  and in the plane  $\hat{i} + \hat{j} + \hat{k}$  and  $-\hat{i} + \hat{j} + \hat{k}$  are

A. 
$$\hat{i} + \hat{k}$$

$$\mathsf{B.}\ 2\hat{i} + \hat{j} + \hat{k}$$

$$\mathsf{C.}\ 3\hat{i}\ +\ 2\hat{j}\ +\ \hat{k}$$

D. 
$$-4\hat{i} - 2\hat{j} - 2\hat{k}$$

### Answer: b,d



side  $\vec{C}B$  can be a.  $-\frac{3}{2}(\hat{i} - \sqrt{3}\hat{j})$  b.  $\frac{3}{2}(\hat{i} - \sqrt{3}\hat{j})$  c.  $-\frac{3}{2}(\hat{i} + \sqrt{3}\hat{j})$  d.  $\frac{3}{2}(\hat{i} + \sqrt{3}\hat{j})$ 

**115.** If side  $\vec{AB}$  of an equilateral trangle  $\vec{ABC}$  lying in the x-y plane  $3\hat{i}$ , then

A. 
$$-\frac{3}{2}(\hat{i}-\sqrt{3}\hat{j})$$

$$B. -\frac{3}{2} \left( \hat{i} - \sqrt{3} \hat{j} \right)$$

$$\mathsf{C.} - \frac{3}{2} \left( \hat{i} + \sqrt{3} \hat{j} \right)$$

D. 
$$\frac{3}{2} \left( \hat{i} + \sqrt{3} \hat{j} \right)$$

### Answer: b,d



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116. The angles of triangle, two of whose sides are represented by vectors

$$\sqrt{3}(\vec{a} \times \vec{b})$$
 and  $\vec{b} - (\hat{a}\vec{b})\hat{a}$ , where  $\vec{b}$  is a non zero vector and  $\hat{a}$  is unit vector

in the direction of  $\vec{a}$ , are

A. 
$$\tan^{-1}(\sqrt{3})$$

B. 
$$\tan^{-1}\left(1/\sqrt{3}\right)$$

C. 
$$\cot^{-1}(0)$$

#### Answer: a,b,c



**117.**  $\vec{a}$ ,  $\vec{b}$ ,  $and\vec{c}$  are unimodular and coplanar. A unit vector  $\vec{d}$  is perpendicular to then. If  $(\vec{a} \times \vec{b}) \times (\vec{c} \times \vec{d}) = \frac{1}{6}\hat{i} - \frac{1}{2}\hat{j} + \frac{1}{2}\hat{k}$ , and the angel between  $\vec{a}$  and  $\vec{b}$  is  $30^0$ , then  $\vec{c}$  is  $(\hat{i} - 2\hat{j} + 2\hat{k})/3$  b.  $(-\hat{i} + 2\hat{j} - 2\hat{k})/3$  c.  $(2\hat{i} + 2\hat{j} - \hat{k})/3$  d.  $(-2\hat{i} - 2\hat{j} + \hat{k})/3$ 

A. 
$$(\hat{i} - 2\hat{i} + 2\hat{k})$$

A. 
$$(\hat{i} - 2\hat{j} + 2\hat{k})/3$$

B. 
$$(-\hat{i} + 2\hat{j} - 2\hat{k})/3$$
  
C.  $(-\hat{i} + 2\hat{j} - \hat{k})/3$ 

D. 
$$(-2\hat{i}-2\hat{j}+\hat{k})/3$$

### Answer: a,b



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**118.** If  $\vec{a} + 2\vec{b} + 3\vec{c} = \vec{0}$  then  $\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a} = \vec{0}$ 

A. 
$$2(\vec{a} \times \vec{b})$$

B. 
$$6(\vec{b} \times \vec{c})$$

$$C.3(\vec{c} \times \vec{a})$$

 $\vec{D}$ .  $\vec{0}$ 

### Answer: c,d



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# **119.** Let $\vec{a}$ and $\vec{b}$ be two non-collinear unit vectors. If $\vec{u} = \vec{a} - (\vec{a} \cdot \vec{b})\vec{b}$ and

 $\vec{v} = \vec{a} \times \vec{b}$ , then  $|\vec{v}|$  is

A. 
$$|\vec{u}|$$

B.  $\left| \vec{u} \right| + \left| \vec{u} \cdot \vec{b} \right|$ 

C.  $|\vec{u}| + |\vec{u}.\vec{a}|$ 

D. none of these

#### Answer: b.d



**120.** if 
$$\vec{a} \times \vec{b} = \vec{c}$$
,  $\vec{b} \times \vec{c} = \vec{a}$ , where  $\vec{c} \neq \vec{0}$  then (a)  $|\vec{a}| = |\vec{c}|$  (b)  $|\vec{a}| = |\vec{b}|$ 

(c) 
$$|\vec{b}| = 1$$
 (d)  $|\vec{a}| = |\vec{b}| = |\vec{c}| = 1$ 

A. 
$$\left| \vec{a} \right| = \left| \vec{c} \right|$$

$$B. \left| \vec{a} \right| = \left| \vec{b} \right|$$

C. 
$$\left| \vec{b} \right| = 1$$

D. 
$$|\vec{a}| = \vec{b}| = |\vec{c}| = 1$$

#### Answer: a,c



### **Watch Video Solution**

**121.** Let  $\vec{a}, \, \vec{b}, \,$  and  $\, \vec{c} \,$  be three non-coplanar vectors and  $\, \vec{d} \,$  be a non-zero ,  $(\vec{a} + \vec{b} + \vec{c}).$ perpendicular to which

Now

 $\vec{d} = (\vec{a} \times \vec{b}) \sin x + (\vec{b} \times \vec{c}) \cos y + 2(\vec{c} \times \vec{a})$ . Then

A. 
$$\frac{\vec{d}. (\vec{a} + \vec{c})}{\left[ \vec{a} \vec{b} \vec{c} \right]} = 2$$

is

B. 
$$\frac{\vec{d}. (\vec{a} + \vec{c})}{\left[\vec{a}\vec{b}\vec{c}\right]} = -2$$

C. minimum value of  $x^2 + y^2 i s \pi^2 / 4$ 

D. minimum value of  $x^2 + y^2 i s 5\pi^2 / 4$ 

#### Answer: b,d



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**122.** If  $\vec{a}$ ,  $\vec{b}$ , and  $\leftrightarrow c$  are three unit vectors such that

$$\vec{a} \times (\vec{b} \times \vec{c}) = \frac{1}{1}\vec{b}$$
, then  $(\vec{b}and\vec{c}$  being non-parallel) angle between  $\vec{a}and\vec{b}$ 

is $\pi/3$  b.a n g l eb e t w e e n $\vec{a}$  and  $\vec{c}$  is  $\pi/3$  c. a. angle between  $\vec{a}$  and  $\vec{b}$  is  $\pi/2$  d.

a. angle between  $\vec{a}$  and  $\vec{c}$  is  $\pi/2$ 

A. angle between  $\vec{a}$  and  $\vec{b}$  is  $\pi/3$ 

B. angle between  $\vec{a}$  and  $\vec{c}$  is  $\pi/3$ 

C. angle between  $\vec{a}$  and  $bis\pi/2$ 

D. angle between  $\vec{a}$  and  $\vec{c}$  is  $\pi/2$ 

#### Answer: b,c



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**123.** If in triangle ABC,  $\overrightarrow{AB} = \frac{\overrightarrow{u}}{\left|\overrightarrow{u}\right|} - \frac{\overrightarrow{v}}{\left|\overrightarrow{v}\right|}$  and  $\overrightarrow{AC} = \frac{2\overrightarrow{u}}{\left|\overrightarrow{u}\right|}$ , where  $\left|\overrightarrow{u}\right| \neq \left|\overrightarrow{v}\right|$ , then  $(a)1 + \cos 2A + \cos 2B + \cos 2C = 0$  (b)  $\sin A = \cos C$  (c) projection of AC on BC is equal to BC (d) projection of AB on BC is equal to AB

A. 
$$1 + \cos 2A + \cos 2B + \cos 2C = 0$$

$$B. \sin A = \cos C$$

C. projection of AC on BC is equal to BC

D. projection of AB on BC is equal to AB

#### Answer: a,b,c



**124.** 
$$\left[ \vec{a} \times \vec{b} \quad \vec{c} \times \vec{d} \quad \vec{e} \times \vec{f} \right]$$
 is equal to

A. A. 
$$\left[\vec{a}\vec{b}\vec{d}\right]\left[\vec{c}\vec{e}\vec{f}\right] - \left[\vec{a}\vec{b}\vec{c}\right]\left[\vec{d}\vec{e}\vec{f}\right]$$

$$\text{B. B. } \left[\vec{a}\vec{b}\vec{e}\right] \left[\vec{f}\vec{c}\vec{d}\right] \text{-} \left[\vec{a}\vec{b}\vec{f}\right] \left[\vec{e}\vec{c}\vec{d}\right]$$

C. C. 
$$\left[\vec{c}\vec{d}\vec{a}\right]\left[\vec{b}\vec{e}\vec{f}\right]$$
 -  $\left[\vec{a}\vec{d}\vec{b}\right]\left[\vec{a}\vec{e}\vec{f}\right]$ 

D. D. 
$$\left[\vec{a}\vec{c}\vec{e}\right]\left[\vec{b}\vec{d}\vec{f}\right]$$

### Answer: a,b,c



**125.** The scalars l and m such that  $l\vec{a}+m\vec{b}=\vec{c}$  ,where  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are given vectors, are equal to

A. 
$$l = \frac{\left(\vec{c} \times \vec{b}\right).\left(\vec{a} \times \vec{b}\right)}{\left(\vec{a} \times \vec{b}\right)^2}$$

B. 
$$l = \frac{\left(\vec{c} \times \vec{a}\right). \left(\vec{b} \times \vec{a}\right)}{\left(\vec{b} \times \vec{a}\right)}$$

C. 
$$m = \frac{(\vec{c} \times \vec{a}). (\vec{b} \times \vec{a})}{(\vec{b} \times \vec{a})^2}$$
  
D.  $m = \frac{(\vec{c} \times \vec{a}). (\vec{b} \times \vec{a})}{(\vec{b} \times \vec{a})}$ 

### Answer: a,c



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**126.** If 
$$(\vec{a} \times \vec{b}) \times (\vec{c} \times \vec{d})$$
.  $(\vec{a} \times \vec{d}) = 0$  then which of the following may be true?

A. A.  $\vec{a}$ ,  $\vec{b}$  and  $\vec{d}$  are nenessarily coplanar

B. B.  $\vec{a}$  lies iin the plane of  $\vec{c}$  and  $\vec{d}$ 

C. C.  $\vec{b}$  lies in the plane of  $\vec{a}$  and  $\vec{d}$ 

D. D.  $\vec{c}$  lies in the plane of  $\vec{a}$  and  $\vec{d}$ 

### Answer: b,c,d



**127.** *A, B, CandD* 

that

$$\vec{A}B = m(2\hat{i} - 6\hat{j} + 2\hat{k}), \vec{B}C = (\hat{i} - 2\hat{j}) and \vec{C}D = n(-6\hat{i} + 15\hat{j} - 3\hat{k})$$
 If  $CD$  intersects  $AB$  at some point  $E$ , then a.  $m \ge 1/2$  b. $n \ge 1/3$  c.  $m = n$  d.  $m < n$ 

are

A. 
$$m \ge 1/2$$

B. 
$$n \ge 1/3$$

#### Answer: a,b



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**128.** If the vectors  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are non-coplanar and l,m,n are distinct real numbers, then  $[(l\vec{a}+m\vec{b}+n\vec{c})\Big(l\vec{b}+m\vec{c}+n\vec{a}\Big)\Big(l\vec{c}+m\vec{a}+n\vec{b})]=0$ , implies (A) lm+mn+nl=0 (B) l+m+n=0 (C)  $l^2+m^2+n^2=0$ 

A. 
$$1 + m + n = 0$$

B. roots of the equation  $lx^2 + mx + n = 0$  are equal

C. 
$$l^2 + m^2 + n^2 = 0$$

D. 
$$l^3 + m^2 + n^3 = 3lmn$$

### Answer: a,b,d



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**129.** Let 
$$\vec{\alpha} = a\hat{i} + b\hat{j} + c\hat{k}$$
,  $\vec{\beta} = b\hat{i} + c\hat{j} + a\hat{k}$  and  $\vec{\gamma} = c\hat{i} + a\hat{j} + b\hat{k}$  be three coplaar vectors with  $a \neq b$ , and  $\vec{v} = \hat{i} + \hat{j} + \hat{k}$ . Then  $\vec{v}$  is perpendicular to

$$\vec{\alpha}$$

 $\mathbf{B}.\,\vec{\boldsymbol{\beta}}$ 

 $\vec{C}$ .  $\vec{\gamma}$ 

D. none of these

## Answer: a,b,c

**130.** If vectors 
$$\vec{A} = 2\hat{i} + 3\hat{j} + 4\hat{k}$$
,  $\vec{B} = \hat{i} + \hat{j} + 5\hat{k}$  and  $\vec{C}$  form a left-handed system, then  $\vec{C}$  is a.11 $\hat{i}$  - 6 $\hat{j}$  -  $\hat{k}$  b.-11 $\hat{i}$  + 6 $\hat{j}$  +  $\hat{k}$  c. 11 $\hat{i}$  - 6 $\hat{j}$  +  $\hat{k}$  d. -11 $\hat{i}$  + 6 $\hat{j}$  -  $\hat{k}$ 

If  $\vec{a} = x\hat{i} + y\hat{j} + z\hat{k}$ ,  $\vec{b} = y\hat{i} + z\hat{j} + x\hat{k}$  and  $\vec{c} = z\hat{i} + x\hat{j} + y\hat{k}$ ,

A. 
$$11\hat{i} - 6\hat{j} - \hat{k}$$

B. - 
$$11\hat{i}$$
 -  $6\hat{j}$  -  $\hat{k}$ 

D. 
$$-11\hat{i} + 6\hat{i} - \hat{k}$$

C.  $-11\hat{i} - 6\hat{i} + \hat{k}$ 

### Answer: b,d



131.

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then  $\vec{a} \times (\vec{b} \times \vec{c})$  is

A. A. parallel to  $(y - z)\hat{i} + (z - x)\hat{j} + (x - y)\hat{k}$ 

B. B. orthogonal to  $\hat{i} + \hat{j} + \hat{k}$ 

C. C. orthogonal to  $(y+z)\hat{i} + (z+x)\hat{j} + (x+y)\hat{k}$ 

D. D. orthogonal to  $x\hat{i} + y\hat{j} + z\hat{k}$ 

### Answer: a,b,c,d



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# **132.** If $\vec{a} \times (\vec{b} \times \vec{c}) = (\vec{a} \times \vec{b}) \times \vec{c}$ then

A. A. 
$$(\vec{c} \times \vec{a}) \times \vec{b} = \vec{0}$$

B. B. 
$$\vec{c} \times (\vec{a} \times \vec{b}) = \vec{0}$$

C. C. 
$$\vec{b} \times (\vec{c} \times \vec{a}) = \vec{0}$$

D. D. 
$$\vec{c} \times \vec{a} \times \vec{b} = \vec{b} \times (\vec{c} \times \vec{a}) = \vec{0}$$

#### Answer: a,c,d



**133.** A vector  $(\vec{d})$  is equally inclined to three vectors  $\vec{a} = \hat{i} - \hat{j} + \hat{k}$ ,  $\vec{b} = 2\hat{i} + \hat{j}$  and  $\vec{c} = 3\hat{j} - 2\hat{k}$  let  $\vec{x}, \vec{y}, \vec{z}$  be three in the plane of  $\vec{a}, \vec{b}; \vec{b}, \vec{c}; \vec{c}, \vec{a}$  respectively, then

A. 
$$\vec{z}$$
.  $\vec{d} = 0$ 

$$\mathbf{B}.\,\vec{x}.\,\vec{d}=1$$

C. 
$$\vec{y}$$
.  $\vec{d} = 32$ 

D. 
$$\vec{r}$$
.  $\vec{d} = 0$ , where  $\vec{r} = \lambda \vec{x} + \mu \vec{y} + \gamma \vec{z}$ 

#### Answer: a,d



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**134.** A parallelogram is constructed on the vectors  $\vec{a} = 3\vec{\alpha} - \vec{\beta}$ ,  $\vec{b} = \vec{\alpha} + 3\vec{\beta}$ . If  $|\vec{\alpha}| = |\vec{\beta}| = 2$  and angle between  $\vec{\alpha}$  and  $\vec{\beta}$  is  $\frac{\pi}{3}$  then the length of a diagonal of the parallelogram is

A. 
$$4\sqrt{5}$$

B. 
$$4\sqrt{3}$$

C.  $4\sqrt{7}$ 

D. none of these

### Answer: b,c



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# Reasoning type

**1.** Statement 1: Vector  $\vec{c} = -5\hat{i} + 7\hat{j} + 2\hat{k}$  is along the bisector of angel between  $\vec{a} = \hat{i} + 2\hat{j} + 2\hat{k}$  and  $\vec{b} = 8\hat{i} + \hat{j} - 4\hat{k}$  Statement 2:  $\vec{c}$  is equally inclined to  $\vec{a}$  and  $\vec{h}$ 

A. Both the statements are true and statement 2 is the correct explanation for statement 1.

B. Both statements are true but statement 2 is not the correct explanation for statement 1.

- C. Statement 1 is true and Statement 2 is false
- D. Statement 1 is false and Statement 2 is true.

#### Answer: b



- **2.** Statement 1: A component of vector  $\vec{b} = 4\hat{i} + 2\hat{j} + 3\hat{k}$  in the direction perpendicular totehdirectin of vector  $\vec{a} = \hat{i} + \hat{j} + \hat{k}is\hat{i} \hat{j}$  Statement 2: A component of vector in the direction of  $\vec{a} = \hat{i} + \hat{j} + \hat{k}is2\hat{i} + 2\hat{j} + 2\hat{k}$ 
  - A. Both the statements are true and statement 2 is the correct explanation for statement 1.
  - B. Both statements are true but statement 2 is not the correct explanation for statement 1.
  - C. Statement 1 is true and Statement 2 is false
  - D. Statement 1 is false and Statement 2 is true.



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3. Statement 1: Distance of point D( 1,0,-1) from the plane of points A(

1,-2,0) , B ( 3, 1,2) and C( -1,1,-1) is 
$$\frac{8}{\sqrt{229}}$$

Statement 2: volume of tetrahedron formed by the points A,B, C and D is

$$\frac{\sqrt{229}}{2}$$

- A. Both the statements are true and statement 2 is the correct explanation for statement 1.
- B. Both statements are true but statement 2 is not the correct explanation for statement 1.
- C. Statement 1 is true and Statement 2 is false
- D. Statement 1 is false and Statement 2 is true.

#### Answer: d

**4.** Let  $\vec{r}$  be a non - zero vector satisfying  $\vec{r}$ .  $\vec{a}=\vec{r}$ .  $\vec{b}=\vec{r}$ .  $\vec{c}=0$  for given non-zero vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$ 

Statement 1: 
$$\left[\vec{a} - \vec{b}\vec{b} - \vec{c}\vec{c} - \vec{a}\right] = 0$$

Statement 2: 
$$\left[\vec{a}\vec{b}\vec{c}\right] = 0$$

A. A. Both the statements are true and statement 2 is the correct explanation for statement 1.

B. B. Both statements are true but statement 2 is not the correct explanation for statement 1.

C. C. Statement 1 is true and Statement 2 is false

D. D. Statement 1 is false and Statement 2 is true.

#### Answer: b



**5.** Statement 1: If  $a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$ ,  $\vec{b}\hat{i} + b_2\hat{j} + b_3\hat{k}$  and  $c_1\hat{i} + c_2\hat{j} + c_3\hat{k}$  are three mutually perpendicular unit vectors then  $a_1\hat{i} + b_1\hat{j} + c_1\hat{k}$ ,  $a_2\hat{i} + b_2\hat{j} + c_2\hat{k}$  and  $a_3\hat{i} + b_3\hat{j} + c_3\hat{k}$  may be mutually perpendicular unit vectors.

Statement 2 : value of determinant and its transpose are the same.

A. A. Both the statements are true and statement 2 is the correct explanation for statement 1.

B. B. Both statements are true but statement 2 is not the correct explanation for statement 1.

C. C. Statement 1 is true and Statement 2 is false

D. D. Statement 1 is false and Statement 2 is true.

#### Answer: a



**6.** Statement 1:  $\vec{A} = 2\hat{i} + 3\hat{j} + 6\hat{k}$ ,  $\vec{B} = \hat{i} + \hat{j} - 2\hat{k}$  and  $\vec{C} = \hat{i} + 2\hat{j} + \hat{k}$  then

$$\left| \vec{A} \times \left( \vec{A} \times \left( \vec{A} \times \vec{B} \right) \right) \cdot \vec{C} \right| = 243$$

Statement 2:  $|\vec{A} \times (\vec{A} \times (\vec{A} \times \vec{B})) \cdot \vec{C}| = |\vec{A}|^2 ||\vec{A}\vec{B}\vec{C}||$ 

A. A. Both the statements are true and statement 2 is the correct explanation for statement 1.

B. B. Both statements are true but statement 2 is not the correct explanation for statement 1.

C. C. Statement 1 is true and Statement 2 is false

D. D. Statement 1 is false and Statement 2 is true.

#### Answer: d



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**7.** Statement 1:  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  are three mutually perpendicular unit vectors and  $\vec{d}$  is a vector such that  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  and  $\vec{d}$  are non-coplanar. If

A. Both the statements are true and statement 2 is the correct explanation for statement 1.

2:

B. Both statements are true but statement 2 is not the correct explanation for statement 1.

C. Statement 1 is true and Statement 2 is false

D. Statement 1 is false and Statement 2 is true.

# Answer: b



**8.** Consider a vector  $\vec{c}$ 

Prove that,  $\vec{c} = (\hat{i}.\vec{c})\hat{i} + (\hat{j}.\vec{c})\hat{j} + (\hat{k}.\vec{c})\hat{k}$ 



# Comprehension type

**1.** Let 
$$\vec{u}$$
,  $\vec{v}$  and  $\vec{w}$  be three unit vectors such that  $\vec{u} + \vec{v} + \vec{w} = \vec{a}$ ,  $\vec{u} \times (\vec{v} \times \vec{w}) = \vec{b}$ ,  $(\vec{u} \times \vec{v}) \times \vec{w} = \vec{c}$ ,  $\vec{a}$ .  $\vec{u} = 3/2$ ,  $\vec{a}$ .  $\vec{v} = 7/4$  and

Vector 
$$\vec{w}$$
 is

A. 
$$\vec{a} - \frac{2}{3}\vec{b} + \vec{c}$$

B. 
$$\vec{a} + \frac{4}{3}\vec{b} + \frac{8}{3}\vec{c}$$

C. 
$$2\vec{a} - \vec{b} + \frac{1}{3}\vec{c}$$

D. 
$$\frac{4}{3}\vec{a} - \vec{b} + \frac{2}{3}\vec{c}$$



Vector  $\vec{w}$  is

Answer: b

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 $\vec{u}$ ,  $\vec{v}$  and  $\vec{w}$ 

be

 $\vec{u} + \vec{v} + \vec{w} = \vec{a}, \vec{u} \times (\vec{v} \times \vec{w}) = \vec{b}, (\vec{u} \times \vec{v}) \times \vec{w} = \vec{c}, \vec{a}. \vec{u} = 3/2, \vec{a}. \vec{v} = 7/4$  and

three unit

vectors

such

that

B. (b) 
$$\vec{a} + \frac{4}{3}\vec{b} + \frac{8}{3}\vec{c}$$

A. (a)  $\vec{a} - \frac{2}{3}\vec{b} + \vec{c}$ 

C. (c) 
$$2\vec{a} - \vec{b} + \frac{1}{3}\vec{c}$$

D. (d)  $\frac{4}{3}\vec{a} - \vec{b} + \frac{2}{3}\vec{c}$ 

# Answer: c

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Let 
$$\vec{u}$$
,

Let 
$$\vec{u}$$
,  $\vec{v}$ 

$$+\vec{v}+\vec{N}$$

$$\vec{u} + \vec{v} + \vec{w} = \vec{a}, \vec{u} \times (\vec{v} \times \vec{w}) = \vec{b}, (\vec{u} \times \vec{v}) \times \vec{w} = \vec{c}, \vec{a}. \vec{u} = 3/2, \vec{a}. \vec{v} = 7/4$$
 and

ctor 
$$\vec{w}$$

Vector 
$$\vec{w}$$
 is

A. (a)  $\vec{a} - \frac{2}{3}\vec{b} + \vec{c}$ 

B. (b)  $\vec{a} + \frac{4}{3}\vec{b} + \frac{8}{3}\vec{c}$ 

C. (c)  $2\vec{a} - \vec{b} + \frac{1}{3}\vec{c}$ 

D. (a)  $\frac{4}{3}\vec{a} - \vec{b} + \frac{2}{3}\vec{c}$ 

$$\vec{u}$$
,  $\vec{v}$  and  $\vec{w}$  be

three

unit

vectors

that

such

#### Answer: d



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**4.** Vectors  $\vec{x}$ ,  $\vec{y}$ ,  $\vec{z}$  each of magnitude  $\sqrt{2}$  make angles of  $60^0$  with each other. If  $\vec{x} \times (\vec{y} \times \vec{z}) = \vec{a}$ ,  $\vec{y} \times (\vec{z} \times \vec{x}) = \vec{b}$  and  $\vec{x} \times \vec{y} = \vec{c}$ , find  $\vec{x}$ ,  $\vec{y}$ ,  $\vec{z}$  in terms of  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$ .



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**5.** Vectors  $\vec{x}$ ,  $\vec{y}$ ,  $\vec{z}$  each of magnitude  $\sqrt{2}$  make angles of  $60^0$  with each other. If  $\vec{x} \times (\vec{y} \times \vec{z}) = \vec{a}$ ,  $\vec{y} \times (\vec{z} \times \vec{x}) = \vec{b}$  and  $\vec{x} \times \vec{y} = \vec{c}$ , find  $\vec{x}$ ,  $\vec{y}$ ,  $\vec{z}$  in terms of  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$ .

A. 
$$\frac{1}{2} \left[ \left( \vec{a} + \vec{c} \right) \times \vec{b} - \vec{b} - \vec{a} \right]$$

B. 
$$\frac{1}{2} \left[ \left( \vec{a} - \vec{c} \right) \times \vec{b} + \vec{b} + \vec{a} \right]$$

C. 
$$\frac{1}{2} \left[ \left( \vec{a} - \vec{b} \right) \times \vec{c} + \vec{b} + \vec{a} \right]$$

D. 
$$\frac{1}{2} \left[ \left( \vec{a} - \vec{c} \right) \times \vec{a} + \vec{b} - \vec{a} \right]$$

#### Answer: c



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- **6.** Vectors  $\vec{x}$ ,  $\vec{y}$ ,  $\vec{z}$  each of magnitude  $\sqrt{2}$  make angles of  $60^0$  with each other. If  $\vec{x} \times (\vec{y} \times \vec{z}) = \vec{a}$ ,  $\vec{y} \times (\vec{z} \times \vec{x}) = \vec{b}$  and  $\vec{x} \times \vec{y} = \vec{c}$ , find  $\vec{x}$ ,  $\vec{y}$ ,  $\vec{z}$  in terms of  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$ .
  - A.  $\frac{1}{2} \left[ \left( \vec{a} \vec{c} \right) \times \vec{c} \vec{b} + \vec{a} \right]$
  - B.  $\frac{1}{2} \left[ \left( \vec{a} \vec{b} \right) \times \vec{c} + \vec{b} \vec{a} \right]$
  - $\mathsf{C.} \; \frac{1}{2} \left[ \vec{c} \times \left( \vec{a} \vec{b} \right) + \vec{b} + \vec{a} \right]$

D. none of these

#### Answer: b



**7.** If  $\vec{x} \times \vec{y} = \vec{a}$ ,  $\vec{y} \times \vec{z} = \vec{b}$ ,  $\vec{x}$ .  $\vec{b} = \gamma$ ,  $\vec{x}$ .  $\vec{y} = 1$  and  $\vec{y}$ .  $\vec{z} = 1$  then find x,y,z in terms of  $\vec{a}$ ,  $\vec{b}$  and  $\gamma$ .



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**8.** If  $\vec{x} \times \vec{y} = \vec{a}$ ,  $\vec{y} \times \vec{z} = \vec{b}$ ,  $\vec{x}$ .  $\vec{b} = \gamma$ ,  $\vec{x}$ .  $\vec{y} = 1$  and  $\vec{y}$ .  $\vec{z} = 1$  then find x,y,z in terms of  $\vec{a}$ ,  $\vec{b}$  and  $\gamma$ .

A. 
$$\frac{\vec{a} \times \vec{b}}{\gamma}$$

B. 
$$\vec{a} + \frac{\vec{a} \times \vec{b}}{\gamma}$$

$$C. \vec{a} + \vec{b} + \frac{\vec{a} \times \vec{b}}{\gamma}$$

D. none of these

#### Answer: a



**9.** Vectors  $\vec{x}$ ,  $\vec{y}$ ,  $\vec{z}$  each of magnitude  $\sqrt{2}$  make angles of  $60^0$  with each other. If  $\vec{x} \times (\vec{y} \times \vec{z}) = \vec{a}$ ,  $\vec{y} \times (\vec{z} \times \vec{x}) = \vec{b}$  and  $\vec{x} \times \vec{y} = \vec{c}$ , find  $\vec{x}$ ,  $\vec{y}$ ,  $\vec{z}$  in terms of  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$ .

A. 
$$\frac{\gamma}{\left|\vec{a} \times \vec{b}\right|^{2}} \left[\vec{a} + \vec{b} \times \left(\vec{a} \times \vec{b}\right)\right]$$
B. 
$$\frac{\gamma}{\left|\vec{a} \times \vec{b}\right|^{2}} \left[\vec{a} + \vec{b} - \vec{a} \times \left(\vec{a} \times \vec{b}\right)\right]$$
C. 
$$\frac{\gamma}{\left|\vec{a} \times \vec{b}\right|^{2}} \left[\vec{a} + \vec{b} + \vec{a} \times \left(\vec{a} \times \vec{b}\right)\right]$$

D. none of these

#### Answer: c



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**10.** Given two orthogonal vectors  $\vec{A}$  and  $\vec{B}$  each of length unity. Let  $\vec{P}$  be the vector satisfying the equation  $\vec{P} \times \vec{B} = \vec{A} - \vec{P}$ . then

$$(\vec{P} \times \vec{B}) \times \vec{B}$$
 is equal to

$$\vec{A} \cdot \vec{P}$$

$$\mathsf{B.} \, \text{-} \vec{P}$$

$$C. 2\vec{B}$$

$$\vec{\mathsf{D}}.\vec{A}$$

### Answer: b



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11. Given two orthogonal vectors  $\vec{A}$  and  $\vec{B}$  each of length unity. Let  $\vec{P}$  be the vector satisfying the equation  $\vec{P} \times \vec{B} = \vec{A} - \vec{P}$ . then

 $\vec{P}$  is equal to

A. 
$$\frac{\vec{A}}{2} + \frac{\vec{A} \times \vec{B}}{2}$$

$$B. \frac{\vec{A}}{2} + \frac{\vec{B} \times \vec{A}}{2}$$

$$C. \frac{\vec{A} \times \vec{B}}{2} - \frac{\vec{A}}{2}$$

$$\vec{D} \cdot \vec{A} \times \vec{B}$$

#### Answer: b



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- **12.** Given two orthogonal vectors  $\vec{A}$  and VecB each of length unity. Let  $\vec{P}$  be the vector satisfying the equation  $\vec{P} \times \vec{B} = \vec{A} \vec{P}$ . then which of the following statements is false ?
  - A. vectors  $\vec{P}$ ,  $\vec{A}$  and  $\vec{P} \times \vec{B}$  ar linearly dependent.
  - B. vectors  $\vec{P}$ ,  $\vec{B}$  and  $\vec{P} \times \vec{B}$  ar linearly independent
  - C.  $\vec{P}$  is orthogonal to  $\vec{B}$  and has length  $\frac{1}{\sqrt{2}}$ .
  - D. none of these

#### Answer: d



**13.** Let  $\vec{a} = 2\hat{i} + 3\hat{j} - 6\hat{k}$ ,  $\vec{b} = 2\hat{i} - 3\hat{j} + 6\hat{k}$  and  $\vec{c} = -2\hat{i} + 3\hat{j} + 6\hat{k}$ . Let  $\vec{a}_1$  be

the projection of  $\vec{a}$  on  $\vec{b}$  and  $\vec{a}_2$  be the projection of  $\vec{a}_1$  on  $\vec{c}$  . Then

$$\vec{a}_2$$
 is equal to (A)  $\frac{943}{49} \left( 2\hat{i} - 3\hat{j} - 6\hat{k} \right)$  (B)  $\frac{943}{49^2} \left( 2\hat{i} - 3\hat{j} - 6\hat{k} \right)$  (C)  $\frac{943}{49} \left( -2\hat{i} + 3\hat{j} + 6\hat{k} \right)$  (D)  $\frac{943}{49^2} \left( -2\hat{i} + 3\hat{j} + 6\hat{k} \right)$ 

A. 
$$\frac{943}{49} \left( 2\hat{i} - 3\hat{j} - 6\hat{k} \right)$$

B. 
$$\frac{943}{49^2} \left( 2\hat{i} - 3\hat{j} - 6\hat{k} \right)$$
  
C.  $\frac{943}{49} \left( -2\hat{i} + 3\hat{j} + 6\hat{k} \right)$ 

D. 
$$\frac{943}{49^2} \left( -2\hat{i} + 3\hat{j} + 6\hat{k} \right)$$

## Answer: b



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**14.** Let  $\vec{a} = 2\hat{i} + 3\hat{j} - 6\hat{k}$ ,  $\vec{b} = 2\hat{i} - 3\hat{j} + 6\hat{k}$  and  $\vec{c} = -2\hat{i} + 3\hat{j} + 6\hat{k}$ . Let  $\vec{a}_1$  be the projection of  $\vec{a}$  on  $\vec{b}$  and  $\vec{a}_2$  be the projection of  $\vec{a}_1$  on  $\vec{c}$ . Then  $\vec{a}_1$ .  $\vec{b}$  is equal to (A) -41 (B) -41/7 (C) 41 (D)287

B. -41/7

C. 41

D. 287

#### Answer: a



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**15.** Let  $\vec{a} = 2\hat{i} + 3\hat{j} - 6\hat{k}$ ,  $\vec{b} = 2\hat{i} - 3\hat{j} + 6\hat{k}$  and  $\vec{c} = -2\hat{i} + 3\hat{j} + 6\hat{k}$ . Let  $\vec{a}_1$  be

the projection of  $\vec{a}$  on  $\vec{b}$  and  $\vec{a}_2$  be the projection of  $\vec{a}_1$  on  $\vec{c}$  . Then

$$\vec{a}_2$$
 is equal to (A)  $\frac{943}{49} \left( 2\hat{i} - 3\hat{j} - 6\hat{k} \right)$  (B)  $\frac{943}{49^2} \left( 2\hat{i} - 3\hat{j} - 6\hat{k} \right)$  (C)

$$\frac{943}{49} \left( -2\hat{i} + 3\hat{j} + 6\hat{k} \right) \text{(D)} \frac{943}{49^2} \left( -2\hat{i} + 3\hat{j} + 6\hat{k} \right)$$

A.  $\vec{a}$  and  $vcea_2$  are collinear

B.  $\vec{a}_1$  and  $\vec{c}$  are collinear

C.  $\vec{a}m\vec{a}_1$  and  $\vec{b}$  are coplanar

D.  $\vec{a}$ ,  $\vec{a}_1$  and  $a_2$  are coplanar

#### Answer: c



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**16.** Consider a triangular pyramid ABCD the position vectors of whose agular points are A(3,0,1), B(-1,4,1), C(5,3,2) and D(0,-5,4) Let G be the point of intersection of the medians of the triangle BCD. The length — of the vector AG is

A.  $\sqrt{17}$ 

B.  $\sqrt{51}/3$ 

c.  $3/\sqrt{6}$ 

D.  $\sqrt{59}/4$ 

#### Answer: b



17. Consider a triangular pyramid ABCD the position vectors of whose agular points are A(3,0,1), B(-1,4,1), C(5,3,2) and D(0,-5,4) Let G be the point of intersection of the medians of the triangle BCD. The length — of the vector AG is

- A. 24
- B.  $8\sqrt{6}$
- $C.4\sqrt{6}$
- D. none of these

#### Answer: c



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**18.** Consider a triangular pyramid ABCD the position vectors of whose agular points are A(3, 0, 1), B(-1, 4, 1), C(5, 3, 2) and D(0, -5, 4) Let G be

the point of intersection of the medians of the triangle BCD. The length

of the vector AG is

A. 
$$14/\sqrt{6}$$

B. 
$$2/\sqrt{6}$$

**C.** 
$$3/\sqrt{6}$$

D. none of these

#### Answer: a



- 19. Vertices of a parallelogram taken in order are A, (2,-1,4), B (1,0,-1), C (
- 1,2,3) and D (x,y,z) The distance between the parallel lines AB and CD is

A. 
$$\sqrt{6}$$

**B.** 
$$3\sqrt{6/5}$$

C. 
$$2\sqrt{2}$$

#### Answer: c



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20. Vertices of a parallelogram taken in order are A(2,-1,4)B(1,0,-1)C(1,2,3) and D.

Distance of the point P (8, 2,-12) from the plane of the parallelogram is

A. 
$$\frac{4\sqrt{6}}{2}$$

B. 
$$\frac{32\sqrt{6}}{9}$$

$$c. \frac{16\sqrt{6}}{9}$$

D. none

### Answer: b



21. Vertices of a parallelogram taken in order are A, (2,-1,4), B (1,0,-1), C (

1,2,3) and D.

The distance between the parallel lines AB and CD is

- A. 14, 4,2
- B. 2,4,14
- C. 4,2,14
- D. 2,14,4

#### Answer: d



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**22.** Let  $\vec{r}$  be a position vector of a variable point in Cartesian OXY plane

that such

$$\vec{r} \cdot \left(10\hat{j} - 8\hat{i} - \vec{r}\right) = 40$$

and

 $P_1 = \max \left\{ \left| \vec{r} + 2\hat{i} - 3\hat{j} \right|^2 \right\}, P_2 = \min \left\{ \left| \vec{r} + 2\hat{i} - 3\hat{j} \right|^2 \right\}.$  A tangenty line is

drawn to the curve  $y = 8/x^2$  at point .A with abscissa 2. the drawn line

cuts the x-axis at a point B.

 $p_2$  is equal to

A. 9

B.  $2\sqrt{2} - 1$ 

C.  $6\sqrt{6} + 3$ 

D. 9 -  $4\sqrt{2}$ 

#### Answer: d



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such that  $\vec{r} \cdot \left(10\hat{j} - 8\hat{i} - \vec{r}\right) = 40$  and  $P_1 = \max\left\{\left|\vec{r} + 2\hat{i} - 3\hat{j}\right|^2\right\}$ ,  $P_2 = \min\left\{\left|\vec{r} + 2\hat{i} - 3\hat{j}\right|^2\right\}$ . A tangenty line is drawn to the curve  $y = 8/x^2$  at point .A with abscissa 2. the drawn line cuts the x-axis at a point B.

**23.** Let  $\vec{r}$  be a position vector of a variable point in Cartesian OXY plane

 $p_1 + p_2$  is equal to

#### Answer: c



# Watch Video Solution

**24.** Let  $\vec{r}$  be a position vector of a variable point in Cartesian OXY plane such that  $\vec{r} \cdot \left(10\hat{j} - 8\hat{i} - \vec{r}\right) = 40$  and

 $P_1 = \max\left\{\left|\vec{r} + 2\hat{i} - 3\hat{j}\right|^2\right\}$ ,  $P_2 = \min\left\{\left|\vec{r} + 2\hat{i} - 3\hat{j}\right|^2\right\}$ . A tangenty line is drawn to the curve  $y = 8/x^2$  at point .A with abscissa 2. the drawn line cuts the x-axis at a point B.

Find r is equal to

B. 2

C. 3

D. 4

#### Answer: c



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**25.** Ab, AC and AD are three adjacent edges of a parallelpiped. The diagonal of the praallelepiped passing through A and direqcted away from it is vector  $\vec{a}$ . The vector of the faces containing vertices A, B, C and A, B, D are  $\vec{b}$  and  $\vec{c}$ , respectively, i.e.  $\overrightarrow{AB} \times \overrightarrow{AC}$  and  $\overrightarrow{AD} \times \overrightarrow{AB} = \vec{c}$  the projection of each edge AB and AC on diagonal vector  $\vec{a}$  is  $\frac{|\vec{a}|}{3}$  vector  $\overrightarrow{AD}$  is

A. 
$$\frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2}$$
B. 
$$\frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2} + \frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^2}$$

C. 
$$\frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2} - \frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^2}$$

D. none of these

#### Answer: a



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diagonal of the praallelepiped passing through A and directed away from it is vector  $\vec{a}$ . The vector of the faces containing vertices A, B, C and

26. Ab, AC and AD are three adjacent edges of a parallelpiped. The

A, B, D are  $\vec{b}$  and  $\vec{c}$ , respectively , i.e.  $\overrightarrow{AB} \times \overrightarrow{AC} = \vec{b}$  and  $\overrightarrow{AD} \times \overrightarrow{AB} = \vec{c}$  the projection of each edge AB and AC on diagonal vector  $\vec{a}$  is  $\frac{|\vec{a}|}{2}$ vector AB is

A. 
$$\frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2}$$
B. 
$$\frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2} + \frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^2}$$

$$C. \frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2} - \frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^2}$$

D. none of these

#### Answer: b



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diagonal of the praallelepiped passing through A and directed away from it is vector  $\vec{a}$ . The vector of the faces containing vertices A, B, C and

27. Ab, AC and AD are three adjacent edges of a parallelpiped. The

A, B, D are  $\vec{b}$  and  $\vec{c}$ , respectively , i.e.  $\overrightarrow{AB} \times \overrightarrow{AC} = \vec{b}$  and  $\overrightarrow{AD} \times \overrightarrow{AB} = \vec{c}$  the projection of each edge AB and AC on diagonal vector  $\vec{a}$  is  $\frac{|\vec{a}|}{2}$ vector AC is

A. 
$$\frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2}$$
B. 
$$\frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2} + \frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^2}$$

C. 
$$\frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2} - \frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^2}$$
D. none of these

# Answer: c



# Martrix - match type





- **2.** Find a unit vector in the direction of  $\vec{a} = 3\hat{i} 2\hat{j} + 6\hat{k}$ 
  - Watch Video Solution

**3.** Find the value of 
$$\lambda$$
 if the vectors  $\vec{a}$  and  $\vec{b}$  are perpendicular, where,  $\vec{a}$ =

$$2\hat{i} + \lambda \hat{j} + \hat{k}$$
 and  $\vec{b} = \hat{i} - 2\hat{j} + 3\hat{k}$ 



**4.** Given two vectors 
$$\vec{a} = -\hat{i} + \hat{j} + 2\hat{k}$$
 and  $\vec{b} = -\hat{i} - 2\hat{j} - \hat{k}$  find  $|\vec{a} \times \vec{b}|$ 



**5.** Given two vectors 
$$\vec{a} = -\hat{i} + 3\hat{j} + \hat{k}$$
 and  $\vec{b} = -3\hat{i} + \hat{j} + \hat{k}$  find  $|\vec{a} \times \vec{b}|$ 



**6.** Show that the vectors  $\hat{i} - 2\hat{j} + 3\hat{k}$ ,  $-2\hat{i} + 3\hat{j} - 4\hat{k}$  and  $\hat{i} - 3\hat{j} + 5\hat{k}$  are coplanar.

7. find 
$$|\vec{x}|$$
, if for a unit vector  $\vec{a}$ ,  $(\vec{x} - \vec{a})(\vec{x} + \vec{a})$ =12

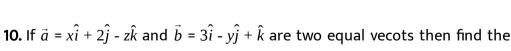
**9.** Find the projection of  $\vec{a}$  on  $\vec{b}$  if  $\vec{a}$ .  $\vec{b}$  =8 and  $\vec{b}$  =  $2\hat{i}$  +  $6\hat{j}$  +  $3\hat{k}$ 



**8.** Write the value of p for which 
$$\vec{a} = 3\hat{i} + 2\hat{j} + 9\hat{k}$$
,  $\vec{b} = \hat{i} + p\hat{j} + 3\hat{k}$  are parallel







value of x + y + z



# Integer type

**1.** If  $\vec{a}$  and  $\vec{b}$  are any two unit vectors, then find the greatest positive

integer in the range of  $\frac{3\left|\vec{a}+\vec{b}\right|}{2}+2\left|\vec{a}-\vec{b}\right|$ .



**2.** Let  $\vec{u}$  be a vector on rectangular coordinate system with sloping angle  $60^{\circ}$  Suppose that  $|\vec{u} - \hat{i}|$  is geometric mean of  $|\vec{u}|$  and  $|\vec{u} - 2\hat{i}|$ , where  $\hat{i}$  is

the unit vector along the x-axis. Then find the value of  $(\sqrt{2} + 1) |\vec{u}|$ 



**3.** Find the absolute value of parameter t for which the area of the triangle whose vertices the A(-1, 1, 2); B(1, 2, 3) and C(5, 1, 1) is minimum.

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**4.** If 
$$\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$$
;  $\vec{b} = b_1\hat{i} + b_2\hat{j} + b_3\hat{k}$ ,  $\vec{c} = c_1\hat{i} + c_2\hat{j} + c_3\hat{k}$  and  $\left[3\vec{a} + \vec{b} \ 3\vec{b} + \vec{c} \ 3\vec{c} + \vec{a}\right] = \lambda \left[\vec{a}\vec{b}\vec{c}\right]$ , then find the value of  $\frac{\lambda}{4}$ .

**5.** Let  $\vec{a} = \alpha \hat{i} + 2\hat{j} - 3\hat{k}$ ,  $\vec{b} = \alpha \hat{i} + 2\alpha \hat{j} - 2\hat{k}$ ,  $and\vec{c} = 2\hat{i} - \alpha \hat{j} + \hat{k}$  Find the value of



$$6\alpha$$
, such that  $\left\{ \left( \vec{a} \times \vec{b} \right) \times \left( \vec{b} \times \vec{c} \right) \right\} \times \left( \vec{c} \times \vec{a} \right) = 0$ .

**6.** If 
$$\vec{x}$$
,  $\vec{y}$  are two non-zero and non-collinear vectors satisfying 
$$\left[ (a-2)\alpha^2 + (b-3)\alpha + c \right] \vec{x} + \left[ (a-2)\beta^2 + (b-3)\beta + c \right] \vec{y} + \left[ (a-2)\gamma^2 + (b-3)\gamma + c \right] \vec{y}$$

are three distinct real numbers, then find the value of  $\left(a^2+b^2+c^2-4\right)$ 



**7.** Let  $\vec{u}$  and  $\vec{v}$  be unit vectors such that  $\vec{u} \times \vec{v} + \vec{u} = \vec{w}$  and  $\vec{w} \times \vec{u} = \vec{v}$ . Find the value of  $[\vec{u} \ \vec{v} \ \vec{w}]$ .



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**8.** Find the value of  $\lambda$  if the volume of a tetrahedron whose vertices are with position vectors  $\hat{i} - 6\hat{j} + 10\hat{k}$ ,  $-\hat{i} - 3\hat{j} + 7\hat{k}$ ,  $5\hat{i} - \hat{j} + \lambda\hat{k}$  and  $7\hat{i} - 4\hat{j} + 7\hat{k}$  is 11 cubic unit.



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**9.** Given that  $\vec{u} = \hat{i} - 2\hat{j} + 3\hat{k}$ ,

$$\vec{v} = 2\hat{i} + \hat{j} + 4\hat{k},$$

 $\vec{w} = \hat{i} + 3\hat{j} + 3\hat{k}$  and  $(\vec{u} \cdot \vec{R} - 15)\hat{i} + (\vec{v} \cdot \vec{R} - 30)\hat{j} + (\vec{w} \cdot \vec{R} - 20)\vec{k} = 0$ . Then find the greatest integer less than or equal to  $|\vec{R}|$ .



**10.** Let a three dimensional vector  $\vec{V}$  satisfy the condition,

$$2\vec{V} + \vec{V} \times (\hat{i} + 2\hat{j}) = 2\hat{i} + \hat{k}$$
 If  $3|\vec{V}| = \sqrt{m}$ . Then find the value of  $m$ 



**11.** If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are unit vectors such that  $\vec{a}$ .  $\vec{b} = 0 = \vec{a}$ .  $\vec{c}$  and the angle between  $\vec{b}$  and  $\vec{c}$  is  $\frac{\pi}{3}$ , then find the value of  $|\vec{a} \times \vec{b} - \vec{a} \times \vec{c}|$ .



**12.** Let  $\vec{O}A = \vec{a}$ ,  $\hat{O}B = 10\vec{a} + 2\vec{b}$  and  $\vec{O}C = \vec{b}$ , where O, A and C are non-collinear points. Let p denotes the area of quadrilateral OACB, and let q denote the area of parallelogram with OA and OC as adjacent sides. If p = kq, then find k



**13.** Find the work done by the force  $F = 3\hat{i} - \hat{j} - 2\hat{k}$  acrting on a particle such that the particle is displaced from point

$$A(-3, -4, 1) \rightarrow B(-1, -1, -2)$$



**14.** If  $\vec{a}$  and  $\vec{b}$  are vectors in space given by  $\vec{a} = \frac{\hat{i} - 2\hat{j}}{\sqrt{5}}$  and  $\vec{b} = \frac{2\hat{i} + \hat{j} + 3\hat{k}}{\sqrt{14}}$  then find the value of  $(2\vec{a} + \vec{b})$ .  $[(\vec{a} \times \vec{b}) \times (\vec{a} - 2\vec{b})]$ 



**15.** Let  $\vec{a} = -\hat{i} - \hat{k}$ ,  $\vec{b} = -\hat{i} + \hat{j}$  and  $\vec{c} = i + 2\hat{j} + 3\hat{k}$  be three given vectors. If  $\vec{r}$  is a vector such that  $\vec{r} \times \vec{b} = \vec{c} \times \vec{b}$  and  $\vec{r} \cdot \vec{a} = 0$  then find the value of  $\vec{r} \cdot \vec{b}$ .



**16.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are unit vectors satisfying  $|\vec{a} - \vec{b}|^2 + |\vec{b} - \vec{c}|^2 + |\vec{c} - \vec{a}|^2 = 9$ ,

then  $\left| 2\vec{a} + 5\vec{b} + 5\vec{c} \right|$  is.



**17.** Let  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  be three non coplanar unit vectors such that the angle between every pair of them is  $\frac{\pi}{3}$ . If  $\vec{a} \times \vec{b} + \vec{b} \times \vec{c} = p\vec{a} + q\vec{b} + r\vec{c}$  where p,q,r are scalars then the value of  $\frac{p^2 + 2q^2 + r^2}{q^2}$  is



# Subjective type

**1.** from a point O inside a triangle ABC, perpendiculars, OD, OE and OF are drawn to the sides, BC, CA and AB respectively, prove that the perpendiculars from A, B and C to the sides EF, FD and DE are concurrent.

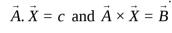


2. about to only mathematics



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**3.** If c is a given non-zero scalar, and  $\vec{A}$  and  $\vec{B}$  are given non-zero vector such that  $\vec{A} \perp \vec{B}$ , then find vector  $\vec{X}$  which satisfies the equation





**4.** A, B, CandD are any four points in the space, then prove that

$$\left| \vec{A}B \times \vec{C}D + \vec{B}C \times \vec{A}D + \vec{C}A \times \vec{B}D \right| = 4 \text{ (area of } ABC \text{ )}.$$



**5.** If vectors 
$$\vec{a}$$
,  $\vec{b}$  and  $\vec{c}$  are coplanar, show that 
$$\begin{vmatrix} \vec{a} & \vec{b} & \vec{c} \\ \vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} & \vec{a} \cdot \vec{c} \end{vmatrix} = \vec{0}$$
$$\begin{vmatrix} \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b} & \vec{b} \cdot \vec{c} \end{vmatrix}$$



**6.** Let  $\vec{A} = 2\vec{i} + \vec{k}$ ,  $\vec{B} = \vec{i} + \vec{j} + \vec{k}$   $\vec{C} = 4\hat{i} - 3\hat{j} + 7\hat{k}$  Determine a vector  $\vec{R}$  satisfying  $\vec{R} \times \vec{B} = \vec{C} \times \vec{B}$  and  $\vec{R}$ ,  $\vec{A} = 0$ .



**7.** Determine the value of c so that for all real x, vectors  $cx\hat{i} - 6\hat{j} - 3\hat{k}$  and  $x\hat{i} + 2\hat{j} + 2cx\hat{k}$  make an obtuse angle with each other.



8. Prove that 
$$(\vec{a} \times \vec{b}) \times (\vec{c} \times \vec{d}) + (\vec{a} \times \vec{c}) \times (\vec{d} \times \vec{b}) + (\vec{a} \times \vec{d}) \times (\vec{b} \times \vec{c}) = -2 [\vec{b}\vec{c}\vec{d}]\vec{a}$$

**9.**  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are vectors of magnitudes 1, 1 and 2, respectively. If

**10.** Let  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  be non-coplanar unit vectors, equally inclined to one

 $\vec{a} \times (\vec{a} \times \vec{c}) + \vec{b} = \vec{0}$ , then acute angle between  $\vec{a}$  and  $\vec{c}$  is

another at an angle $\theta$  then  $\begin{bmatrix} \vec{a} \, \vec{b} \, \vec{c} \end{bmatrix}$  in terms of  $\theta$  is equal to :

that:

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- If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are vectors such that  $\left| \vec{b} \right| = \left| \vec{c} \right|$ 11.  $\left\{ \left( \vec{a} + \vec{b} \right) \times \left( \vec{a} + \vec{c} \right) \right\} \times \left( \vec{b} \times \vec{c} \right) \cdot \left( \vec{b} + \vec{c} \right) =$

**12.** For any two vectors 
$$\vec{u}$$
 and  $\vec{v}$  prove that 
$$\left(1 + \left|\vec{u}\right|^2\right) \left(1 + \left|\vec{v}\right|^2\right) = \left(1 - \vec{u} \cdot \vec{v}\right)^2 + \left|\vec{u} + \vec{v} + \left(\vec{u} \times \vec{v}\right)\right|^2$$



**13.** Let  $\vec{u}$  and  $\vec{v}$  be unit vectors. If  $\vec{w}$  is a vector such that  $\vec{w} + \vec{w} \times \vec{u} = \vec{v}$ , then prove that  $\left| \left( \vec{u} \times \vec{v} \right) \cdot \vec{w} \right| \leq \frac{1}{2}$  and that the equality holds if and only if  $\vec{u}$  is perpendicular to  $\vec{v}$ .

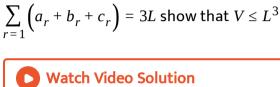


**14.** Find 3-dimensional vectors  $\vec{v}_1, \vec{v}_2, \vec{v}_3$  satisfying  $\vec{v}_1 \cdot \vec{v}_1 = 4, \vec{v}_1 \cdot \vec{v}_2 = -2, \vec{v}_1 \cdot \vec{v}_3 = 6,$ 

$$\vec{v}_2 \cdot \vec{v}_2 = 2, \vec{v}_2 \cdot \vec{v}_3 = -5, \vec{v}_3 \cdot \vec{v}_3 = 29$$



**15.** Let V be the volume of the parallelopiped formed by the vectors  $\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$  and  $\vec{b} = b_1\hat{i} + b_2\hat{j} + b_3\hat{k}$  and  $\vec{c} = c_1\hat{i} + c_2\hat{j} + c_3\hat{k}$ . If  $a_r, b_r$  and  $c_r$ , where r = 1, 2, 3, are non-negative real numbers and  $a_r$ 



**16.**  $\vec{u}$ ,  $\vec{v}$  and  $\vec{w}$  are three non-coplanar unit vectors and  $\alpha$ ,  $\beta$  and  $\gamma$  are the angles between  $\vec{u}$  and  $\vec{v}$ ,  $\vec{v}$  and  $\vec{w}$ , and  $\vec{w}$  and  $\vec{u}$ , respectively, and  $\vec{x}$ ,  $\vec{y}$  and  $\vec{z}$  are unit vectors along the bisectors of the angles  $\alpha$ ,  $\beta$  and  $\gamma$ , respectively.

Prove that 
$$\left[\vec{x} \times \vec{y} \, \vec{y} \times \vec{z} \, \vec{z} \times \vec{x}\right] = \frac{1}{16} \left[\vec{u} \, \vec{v} \, \vec{w}\right]^2 \sec^2 \left(\frac{\alpha}{2}\right) \sec^2 \left(\frac{\beta}{2}\right) \sec^2 \left(\frac{\gamma}{2}\right)$$
.



**17.** If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  and  $\vec{d}$  are distinct vectors such that  $\vec{a} \times \vec{c} = \vec{b} \times \vec{d}$  and  $\vec{a} \times \vec{b} = \vec{c} \times \vec{d}$ . Prove that  $(\vec{a} - \vec{d}) \cdot (\vec{b} - \vec{c}) \neq 0$ 

**18.**  $P_1$  and  $P_2$  are planes passing through origin  $L_1$  and  $L_2$  are two lines on  $P_1$  and  $P_2$ , respectively, such that their intersection is the origin. Show that there exist points A, B and C, whose permutation A', B' and C', respectively, can be chosen such that

ii)A' is on  $L_2$ , B' on  $P_2$  but not on  $L_2$  and C' not on  $P_2$ 

i) A is on  $L_1$ ,  $BonP_1$  but not on  $L_1$  and C not on  $P_1$ ;



**19.** Find the differential equation representing the family of curves  $y = ae^{bx+5}$  where a and b are arbitrary constants.



**1.** Let  $\vec{A}$ ,  $\vec{B}$  and  $\vec{C}$  be vectors of legth , 3,4and 5 respectively. Let  $\vec{A}$  be perpendicular to  $\vec{B} + \vec{C}$ ,  $\vec{B}$  to  $\vec{C} + \vec{A}$  and  $\vec{C}$  to  $\vec{A} + \vec{B}$  then the length of vector  $\vec{A} + \vec{B} + \vec{C}$  is \_\_\_\_\_.



**2.** The unit vector perendicular to the plane determined by P (1,-1,2) ,C(3,-1,2) is



**3.** the area of the triangle whose vertices are A (1,-1,2), B (1,2,-1), C (3,-1, 2) is \_\_\_\_\_.



**4.** If  $\vec{A}, \vec{B}$  and  $\vec{C}$  are three non - coplanar vectors, then

$$\frac{\vec{A}.\vec{B} \times \vec{C}}{\vec{C} \times \vec{A}.\vec{B}} + \frac{\vec{B}.\vec{A} \times \vec{C}}{\vec{C}.\vec{A} \times \vec{B}} = \underline{\qquad}$$



**5.** If  $\vec{A}=(1,1,1)$  and  $\vec{C}=(0,1,-1)$  are given vectors the vector  $\vec{B}$  satisfying the equations  $\vec{A}\times\vec{B}=\vec{C}$  and  $\vec{A}.\vec{B}=3$  is



**6.** Let  $\vec{b} = 4\hat{i} + 3\hat{j}$  and  $\vec{c}$  be two vectors perpendicular to each other in the xy- plane. All vectors in the sme plane having projections 1 and 2 along  $\vec{b}$  and  $\vec{c}$ , respectively, are given by \_\_\_\_\_



**7.** The components of a vector  $\vec{a}$  along and perpendicular to a non-zero vector  $\vec{b}$  are and , respectively.



**8.** A unit vector coplanar with  $\vec{i} + \vec{j} + 2\vec{k}$  and  $\vec{i} + 2\vec{j} + \vec{k}$  and perpendicular to  $\vec{i} + \vec{j} + \vec{k}$  is



**9.** A non vector  $\vec{a}$  is parallel to the line of intersection of the plane determined by the vectors  $\vec{i}$ ,  $\vec{i}$  +  $\vec{j}$  and thepane determined by the vectors  $\vec{i}$  -  $\vec{j}$ ,  $\vec{i}$  +  $\vec{k}$  then angle between  $\vec{a}$  and  $\vec{i}$  -  $2\vec{j}$  +  $2\vec{k}$  is = (A)  $\frac{\pi}{2}$  (B)  $\frac{\pi}{3}$  (C)  $\frac{\pi}{6}$  (D)  $\frac{\pi}{4}$ 



**10.** Find a unit vector perpendicular to each of the vector  $\vec{a} + \vec{b}$  and  $\vec{a} - \vec{b}$ ,

where 
$$\vec{a} = 3\hat{i} + 2\hat{j} + 2\hat{k}$$
 and  $\vec{b} = \hat{i} + 2\hat{j} - 2\hat{k}$ 



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**11.** let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be three vectors having magnitudes 1, 1 and 2, respectively, if  $\vec{a} \times (\vec{a} \times \vec{c}) + \vec{b} = \vec{0}$ , then the acute angle between  $\vec{a}$  and  $\vec{c}$  is



12. A, B C and D are four points in a plane with position vectors,  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  and  $\vec{d}$ respectively, such that  $(\vec{a} - \vec{d}) \cdot (\vec{b} - \vec{c}) = (\vec{b} - \vec{d}) \cdot (\vec{c} - \vec{a}) = 0$  then point D is the \_\_\_\_ of triangle ABC.



**13.** Let  $\overrightarrow{OA} = \overrightarrow{a}$ ,  $\widehat{OB} = 10\overrightarrow{a} + 2\overrightarrow{b}$  and  $\overrightarrow{OC} = \overrightarrow{b}$ , where O, A and C are non-collinear points. Let p denotes the area of quadrilateral OACB, and let q denote the area of parallelogram with OA and OC as adjacent sides. If



p = kq, then findk

**14.** If 
$$\vec{a} = \hat{j} + \sqrt{3}k$$
,  $\vec{b} = -\hat{j} + \sqrt{3}\hat{k}$  and  $\vec{c} = 2\sqrt{3}\hat{k}$  form a triangle, then the internal angle of the triangle between  $\vec{a}$  and  $\vec{b}$  is



### True and false

**1.** Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be unit vectors such that  $\vec{a}$ .  $\vec{b} = 0 = \vec{a}$ .  $\vec{c}$ . It the angle between  $\vec{b}$  and  $\vec{c}$  is  $\frac{\pi}{6}$  then find  $\vec{a}$ .

**2.** If 
$$\vec{x}$$
.  $\vec{a} = 0\vec{x}$ .  $\vec{b} = 0$  and  $\vec{x}$ .  $\vec{c} = 0$  for some non zero vector  $\vec{x}$  then show that  $\left[\vec{a}\vec{b}\vec{c}\right] = 0$ 



**3.** for any three vectors, 
$$\vec{a}$$
,  $\vec{b}$  and  $\vec{c}$ ,  $(\vec{a} - \vec{b})$ .  $(\vec{b} - \vec{c}) \times (\vec{c} - \vec{a}) =$ 



#### single correct answer type

**1.** The scalar 
$$\vec{A} \left( \left( \vec{B} + \vec{C} \right) \times \left( \vec{A} + \vec{B} + \vec{C} \right) \right)$$
 equals a.0 b.  $\left[ \vec{A} \vec{B} \vec{C} \right] + \left[ \vec{B} \vec{C} \vec{A} \right]$  c.  $\left[ \vec{A} \vec{B} \vec{C} \right]$  d. none of these

$$\mathsf{B.}\left[\vec{A}\vec{B}\vec{C}\right] + \left[\vec{B}\vec{C}\vec{A}\right]$$

C. 
$$\left[ \vec{A}\vec{B}\vec{C} \right]$$

D. none of these

#### Answer: a



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**2.** For non-zero vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$ ,  $\left| \left( \vec{a} \times \vec{b} \right) \cdot \vec{c} \right| = \left| \vec{a} \right| \left| \vec{b} \right| \left| \vec{c} \right|$  holds if and only if

A. A. 
$$\vec{a}$$
.  $\vec{b} = 0$ ,  $\vec{b}$ .  $\vec{c} = 0$ 

B. B. 
$$\vec{b}$$
.  $\vec{c} = 0$ ,  $\vec{c}$ ,  $\vec{a} = 0$ 

C. C. 
$$\vec{c}$$
.  $\vec{a} = 0$ ,  $\vec{a}$ ,  $\vec{b} = 0$ 

D. D. 
$$\vec{a}$$
.  $\vec{b} = \vec{b}$ .  $\vec{c} = \vec{c}$ .  $\vec{a} = 0$ 

#### Answer: d



3. The volume of he parallelepiped whose sides are given by

$$\vec{O}A = 2i - 2j$$
,  $\vec{O}B = i + j - kand\vec{O}C = 3i - k$  is a.  $\frac{4}{13}$  b. 4 c.  $\frac{2}{7}$  d. 2

- A.4/13
- B. 4
- C.2/7
- D. 2

#### Answer: d



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**4.** Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be three non-coplanar vectors and  $\vec{p}$ ,  $\vec{q}$  and  $\vec{r}$  the vectors

defined by the relation  $\vec{p} = \frac{\vec{b} \times \vec{c}}{\left[\vec{a}\vec{b}\vec{c}\right]}$ ,  $\vec{q} = \frac{\vec{c} \times \vec{a}}{\left[\vec{a}\vec{b}\vec{c}\right]}$  and  $\vec{r} = \frac{\vec{a} \times \vec{b}}{\left[\vec{a}\vec{b}\vec{c}\right]}$ . Then the

value of the expression  $(\vec{a} + \vec{b})\vec{p} + (\vec{b} + \vec{c})\vec{q} + (\vec{c} + \vec{a})\vec{r}$  is 0 b. 1 c. 2 d. 3

#### Answer: d



**5.** Let 
$$\vec{a} = \hat{i} - \hat{j}$$
,  $\vec{b} = \hat{j} - \hat{k}$ ,  $\vec{c} = \hat{k} - \hat{i}$ . If  $\hat{d}$  is a unit vector such that

$$\vec{a} \cdot \hat{d} = 0 = \left[ \vec{b} \vec{c} \vec{d} \right]$$
 then  $\hat{d}$  equals

A. A. 
$$\pm \frac{\hat{i} + \hat{j} - 2\hat{k}}{\sqrt{6}}$$

B. B. 
$$\pm \frac{\hat{i} + \hat{j} - \hat{k}}{\sqrt{3}}$$

$$C. C. \pm \frac{\hat{i} + \hat{j} + \hat{k}}{\sqrt{3}}$$

D. D. 
$$\pm \hat{k}$$

#### Answer: a



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**6.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are non-coplanar unit vectors such that

$$\vec{a} \times (\vec{b} \times \vec{c}) = \frac{\vec{b} + \vec{c}}{\sqrt{2}}$$
, then the angle between  $\vec{a}$  and  $\vec{b}$  is a.  $3\pi/4$  b.  $\pi/4$  c.

$$\pi/2$$
 d.  $\pi$ 

**A.** 
$$3\pi/4$$

$$B.\pi/4$$

$$C. \pi/2$$

D. 
$$\pi$$

#### Answer: a



$$\left| \vec{u} \right| = 2$$
,  $\left| \vec{v} \right| = 3$  and  $\left| \vec{w} \right| = 5$  then  $\vec{u} \cdot \vec{v} + \vec{v} \cdot \vec{w} + \vec{w} \cdot \vec{u}$  is

Let  $\vec{u}$ ,  $\vec{v}$  and  $\vec{w}$  be vectors such that  $\vec{u} + \vec{v} + \vec{w} = 0$  if

coplanar vectors,

non

then

7.

D. 19

Answer: b

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8.

If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three

 $(\vec{a} + \vec{b} + \vec{c})[(\vec{a} + \vec{b}) \times (\vec{a} + \vec{c})]$  is:

B. 
$$\left[\vec{a}\vec{b}\vec{c}\right]$$

C. 
$$2\left[\vec{a}\vec{b}\vec{c}\right]$$

D. - 
$$\left[\vec{a}\vec{b}\vec{c}\right]$$

#### Answer: d



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**9.**  $\vec{p}$ ,  $\vec{q}$  and  $\vec{r}$  are three mutually prependicular vectors of the same magnitude . If vector  $\vec{x}$  satisfies the equation  $\vec{p} \times \left( \left( \vec{x} - \vec{q} \right) \times \vec{p} \right) + \vec{q} \times \left( \left( \vec{x} - \vec{r} \right) \times \vec{q} \right) + \vec{r} \times \left( \left( \vec{x} - \vec{p} \right) \times \vec{r} \right) = \vec{0}$  then  $\vec{x}$  is given by

A. A. 
$$\frac{1}{2} (\vec{p} + \vec{q} - 2\vec{r})$$

$$B. B. \frac{1}{2} \left( \vec{p} + \vec{q} + \vec{r} \right)$$

C. C. 
$$\frac{1}{3} (\vec{p} + \vec{q} + \vec{r})$$

D. D. 
$$\frac{1}{3} (2\vec{p} + \vec{q} - \vec{r})$$

#### Answer: b



**10.** Let 
$$\vec{a} = 2\hat{i} + \hat{j} - 2\hat{k}$$
, and  $\vec{b} = \hat{i} + \hat{j}$  if c is a vector such that  $\vec{a} \cdot \vec{c} = |\vec{c}|, |\vec{c} - \vec{a}| = 2\sqrt{2}$  and the angle between  $\vec{a} \times \vec{b}$  and  $\vec{c}$  is 30°, then

**11.** Let  $\vec{a} = 2i + j + k$ ,  $\vec{b} = i + 2j - k$  and  $\vec{a}$  unit vector  $\vec{c}$  be coplanar. If  $\vec{c}$  is

$$\left| \left( \vec{a} \times \vec{b} \right) \right| \times \vec{c} \left| \right|$$
 is equal to

Answer: b



pependicular to 
$$ec{a}$$
 .Find  $ec{c}$  .

$$A. \frac{1}{\sqrt{2}}(-j+k)$$

$$B. \frac{1}{\sqrt{3}}(i-j-k)$$

C. 
$$\frac{1}{\sqrt{5}}(i-2j)$$
D.  $\frac{1}{\sqrt{3}}(i-j-k)$ 

#### Answer: a



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- 12. If the vectors  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$  form the sides BC, CA and AB, respectively, of triangle ABC, then
  - A.  $\vec{a}$ .  $\vec{b}$  +  $\vec{b}$ .  $\vec{c}$  +  $\vec{c}$ .  $\vec{a}$  = 0
  - B.  $\vec{a} \times \vec{b} = \vec{b} \times \vec{c} = \vec{c} \times \vec{a}$
  - C.  $\vec{a}$ .  $\vec{b} = \vec{b}$ .  $\vec{c} = \vec{c}$ .  $\vec{a}$
  - D.  $\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a} = \vec{0}$

#### Answer: b



**13.** Let vectors  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$ , and  $\vec{d}$  be such that  $(\vec{a} \times \vec{b}) \times (\vec{c} \times \vec{d}) = 0$ . Let  $P_1 and P_2$  be planes determined by the pair of vectors  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$ ,  $\vec{d}$ , respectively. Then the angle between  $P_1 and P_2$  is  $0 \text{ b.} \pi/4 \text{ c.} \pi/3 \text{ d.} \pi/2$ 

A. 0

B.  $\pi/4$ 

**C.**  $\pi/3$ 

D.  $\pi/2$ 

#### Answer: a



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**14.** If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are unit coplanar vectors, then the scalar triple product

$$[2\vec{a} - \vec{b}2\vec{b} - \vec{c}2\vec{c} - \vec{a}]$$
 is 0 b. 1 c.  $-\sqrt{3}$  d.  $\sqrt{3}$ 

A. 0

B. 1

$$C. -\sqrt{3}$$

D. 
$$\sqrt{3}$$

#### Answer: a



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# **15.** If $\hat{a}$ , $\hat{b}$ , and $\hat{c}$ are unit vectors, then $\left|\hat{a} - \hat{b}\right|^2 + \left|\hat{b} - \hat{c}\right|^2 + \left|\hat{c} - \hat{a}\right|^2$ does not

exceed

B. 9

C. 8

D. 6

#### Answer: b



**16.** If  $\vec{a}$  and  $\vec{b}$  are two unit vectors such that  $\vec{a} + 2\vec{b}$  and  $5\vec{a} - 4\vec{b}$  are perpendicular to each other than the angle between  $\vec{a}$  and  $\vec{b}$  is

- A. 45  $^{\circ}$
- B. 60  $^{\circ}$
- C.  $\cos^{-1}(1/3)$
- D.  $\cos^{-1}(2/7)$

#### Answer: b



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**17.** Let  $\vec{V}=2\hat{i}+\hat{j}-\hat{k}and\vec{W}=\hat{i}+3\hat{k}$  If  $\vec{U}$  is a unit vector, then the maximum value of the scalar triple product [UVW] is a.-1 b.  $\sqrt{10}+\sqrt{6}$  c.  $\sqrt{59}$  d.  $\sqrt{60}$ 

- **A.** -1
- $B.\sqrt{10}+\sqrt{6}$
- C.  $\sqrt{59}$

D. 
$$\sqrt{60}$$



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**18.** Find the value of a so that the volume of the parallelepiped formed by vectors  $\hat{i} + a\hat{j} + k$ ,  $\hat{j} + a\hat{k}$  and  $a\hat{i} + \hat{k}$  becomes minimum.

**A.** -3

B. 3

C.  $1/\sqrt{3}$ 

D.  $\sqrt{3}$ 

#### Answer: c



**19.** If 
$$\vec{a} = (\hat{i} + \hat{j} + \hat{k})$$
,  $\vec{a} \cdot \vec{b} = 1$  and  $\vec{a} \times \vec{b} = \hat{j} - \hat{k}$ , then  $\vec{b}$  is

A. 
$$\hat{i} - \hat{j} + \hat{k}$$

B. 
$$2\hat{i} - \hat{k}$$



**20.** The unit vector which is orthogonal to the vector 
$$3\hat{i} + 2\hat{j} + 6\hat{k}$$
 and is coplanar with vectors  $2\hat{i} + \hat{j} + \hat{k}$  and  $\hat{i} - \hat{j} + \hat{k}$  is  $\frac{2\hat{i} - 6\hat{j} + \hat{k}}{\sqrt{41}}$  b.  $\frac{2\hat{i} - 3\hat{j}}{\sqrt{13}}$  c.  $\frac{3\hat{j} - \hat{k}}{\sqrt{10}}$ 

d. 
$$\frac{4\hat{i} + 3\hat{j} - 3\hat{k}}{\sqrt{34}}$$

A. 
$$\frac{2\hat{i} - 6\hat{j} + \hat{k}}{\sqrt{41}}$$
B.  $\frac{2\hat{i} - 3\hat{j}}{\sqrt{13}}$ 

c. 
$$\frac{3\hat{i} - \hat{k}}{\sqrt{10}}$$
  
D.  $\frac{4\hat{i} + 3\hat{j} - 3\hat{k}}{\sqrt{34}}$ 



**21.** If 
$$\vec{a}$$
,  $\vec{b}$  and  $\vec{c}$  are three non-zero, non-coplanar vectors and

$$\vec{b}_1 = \vec{b} - \frac{\vec{b} \cdot \vec{a}}{|\vec{a}|^2} \vec{a}, \ \vec{b}_2 = \vec{b} + \frac{\vec{b} \cdot \vec{a}}{|\vec{a}|^2} \vec{a}, \ \vec{c}_1 = \vec{c} - \frac{\vec{c} \cdot \vec{a}}{|\vec{a}|^2} \vec{a} + \frac{\vec{b} \cdot \vec{c}}{|\vec{c}|^2} \vec{b}_1,$$

$$\vec{c}_2 = \vec{c} - \frac{\vec{c} \cdot \vec{a}}{\left|\vec{a}\right|^2} \vec{a} - \frac{\vec{b} \cdot \vec{c}}{\left|\vec{b}_1\right|^2} \vec{b}_1, \ \vec{c}_3 = \vec{c} - \frac{\vec{c} \cdot \vec{a}}{\left|\vec{c}\right|^2} \vec{a} + \frac{\vec{b} \cdot \vec{c}}{\left|\vec{c}\right|^2} \vec{b}_1,$$

$$\vec{c}_4 = \vec{c} - \frac{\vec{c} \cdot \vec{a}}{|\vec{c}|^2} \vec{a} = \frac{\vec{b} \cdot \vec{c}}{|\vec{b}|^2} \vec{b}_1$$
, then the set of mutually orthogonal vectors is

A. (a) 
$$\left(\vec{a}, \vec{b}_1, \vec{c}_3\right)$$

B. (b) 
$$(\vec{a}, \vec{b}_1, \vec{c}_2)$$

C. (c) 
$$(\vec{a}, \vec{b}_1, \vec{c}_1)$$

D. (d) 
$$\left(\vec{a}, \vec{b}_2, \vec{c}_2\right)$$



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- **22.** Let  $\vec{a} = \hat{i} + 2\hat{j} + \hat{k}$ ,  $\vec{b} = \hat{i} \hat{j} + \hat{k}$  and  $\vec{c} = \hat{i} \hat{j} \hat{k}$  A vector in the plane of
- $\vec{a}$  and  $\vec{b}$  whose projections on  $\vec{c}$  is  $1/\sqrt{3}$  is
  - A. A.  $4\hat{i} \hat{j} + 4\hat{k}$
  - B. B.  $3\hat{i} + \hat{j} 3\hat{k}$
  - C. C.  $2\hat{i} + \hat{j} 2\hat{k}$
  - D. D.  $-4\hat{i} + \hat{j} 4\hat{k}$

#### Answer: a



**23.** Let two non-collinear unit vector  $\hat{a}$  a n d  $\hat{b}$  form an acute angle. A point P moves so that at any time t, the position vector OP(whereO is the origin) is given by  $\hat{a}\cos t + \hat{b}\sin tWhenP$  is farthest from origin O, let M be the length of  $OPand\hat{u}$  be the unit vector along OP. Then (a)

$$\hat{u} = \frac{\hat{a} + \hat{b}}{\left|\hat{a} + \hat{b}\right|} andM = \left(1 + \hat{a}\hat{b}\right)^{1/2} \quad \text{(b)} \quad \hat{u} = \frac{\hat{a} - \hat{b}}{\left|\hat{a} - \hat{b}\right|} andM = \left(1 + \hat{a}^{\wedge}\right)^{1/2} \quad \text{(c)}$$

$$\hat{u} = \frac{\hat{a} + \hat{b}}{\left|\hat{a} + \hat{b}\right|} andM = \left(1 + 2\hat{a}\hat{b}\right)^{1/2} (d) \hat{u} = \frac{\hat{a} - \hat{b}}{\left|\hat{a} - \hat{b}\right|} andM = \left(1 + 2\hat{a}\hat{b}\right)^{1/2}$$

A., 
$$\hat{u} = \frac{\hat{a} + \hat{b}}{|\hat{a} + \hat{b}|}$$
 and  $M = (1 + \hat{a}. \hat{b})^{1/2}$ 

B., 
$$\hat{u} = \frac{\hat{a} - \hat{b}}{|\hat{a} - \hat{b}|}$$
 and  $M = (1 + \hat{a}. \hat{b})^{1/2}$ 

C. 
$$\hat{u} = \frac{\hat{a} + \hat{b}}{|\hat{a} + \hat{b}|}$$
 and  $M = (1 + 2\hat{a}. \hat{b})^{1/2}$ 

D., 
$$\hat{u} = \frac{\hat{a} - \hat{b}}{|\hat{a} - \hat{b}|}$$
 and  $M = (1 + 2\hat{a}. \hat{b})^{1/2}$ 

#### Answer: a

**24.** If 
$$\vec{a}$$
,  $\vec{b}$ ,  $\vec{c}$  and  $\vec{d}$  are unit vectors such that  $(\vec{a} \times \vec{b})$ .  $(\vec{c} \times \vec{d}) = 1$  and  $\vec{a}$ .  $\vec{c} = \frac{1}{2}$ then

- A.  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are non-coplanar
- B.  $\vec{b}$ ,  $\vec{c}$  and  $\vec{d}$  are non-coplanar
- C.  $\vec{b}$  and  $\vec{d}$  are non-parallel
- D.  $\vec{a}$  and  $\vec{d}$  are parallel and  $\vec{b}$  and  $\vec{c}$  are parallel



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**25.** Two adjacent sides of a parallelogram ABCD are given by  $\vec{A}B = 2\hat{i} + 10\hat{j} + 11\hat{k}$  and  $\vec{A}D = -\hat{i} + 2\hat{j} + 2\hat{k}$ . The side AD is rotated by an acute angle  $\alpha$  in the plane of the parallelogram so that AD becomes AD.

If AD' makes a right angle with the side AB, then the cosine of the angel

$$\alpha$$
 is given by  $\frac{8}{9}$  b.  $\frac{\sqrt{17}}{9}$  c.  $\frac{1}{9}$  d.  $\frac{4\sqrt{5}}{9}$ 

- A.  $\frac{8}{9}$
- B.  $\frac{\sqrt{17}}{9}$
- c.  $\frac{1}{9}$
- D.  $\frac{4\sqrt{5}}{9}$

#### Answer: b



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**26.** Let P, Q, R and S be the points on the plane with position vectors -2i - j, 4i, 3i + 3j and -3i + 2j, respectively. The quadrilateral PQRS must

be (a) Parallelogram, which is neither a rhombus nor a rectangle (b)

A. Parallelogram, which is neither a rhombus nor a rectangle

Square (c) Rectangle but not a square (d) Rhombus, but not a square

B. square

C. rectangle, but not a square

D. rhombus, but not a square.

#### Answer: a



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## **27.** Let $\vec{a} = \hat{i} + 2\hat{j} + \hat{k}$ , $\vec{b} = \hat{i} - \hat{j} + \hat{k}$ and $\vec{c} = \hat{i} - \hat{j} - \hat{k}$ A vector in the plane of

 $\vec{a}$  and  $\vec{b}$  whose projections on  $\vec{c}$  is  $1/\sqrt{3}$  is

$$A. \hat{i} - 3\hat{j} + 3\hat{k}$$

$$\mathsf{B.-3}\hat{i}-3\hat{j}+\hat{k}$$

$$\mathsf{C.}\,\,3\hat{i}\,-\hat{j}\,+\,3\hat{k}$$

D. 
$$\hat{i} + 3\hat{j} - 3\hat{k}$$

#### Answer: c



**28.** Let  $\vec{P}R = 3\hat{i} + \hat{j} - 2\hat{k}and\vec{S}Q = \hat{i} - 3\hat{j} - 4\hat{k}$  determine diagonals of a parallelogram PQRS,  $and\vec{P}T = \hat{i} + 2\hat{j} + 3\hat{k}$  be another vector. Then the volume of the parallelepiped determine by the vectors  $\vec{P}T$ ,  $\vec{P}Q$  and  $\vec{P}S$  is 5 b. 20 c. 10 d. 30

- **A.** 5
- B. 20
- C. 10
- D. 30

Answer: c



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Multiple correct answers type

**1.** Let  $\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$ ,  $\vec{b} = b_1\hat{i} + b_2\hat{j} + b_3\hat{k}$  and  $\vec{c} = c_1\hat{i} + c_2\hat{j} + c_3\hat{k}$  be three non-zero vectors such that  $\vec{c}$  is a unit vector perpendicular to both  $\vec{a}$  and  $\vec{b}$ . If the angle between  $\vec{a}$  and  $\vec{b}is\pi/6$  then the value of

$$\begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{vmatrix}$$
 is

A. 0

C. 
$$\frac{1}{4} \left( a_1^2 + a_2^2 + a_2^2 \right) \left( b_1^2 + b_2^2 + b_2^2 \right)$$

D. 
$$\frac{3}{4} \left( a_1^2 + a_2^2 + a_2^2 \right) \left( b_1^2 + b_2^2 + b_2^2 \right) \left( c_1^2 + c_2^2 + c_2^2 \right)$$

#### Answer: c



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2. The number of vectors of unit length perpendicular to vectors

 $\vec{a}=(1,1,0)$  and  $\vec{b}=(0,1,1)$  is a. one b. two c. three d. infinite

B. two

C. three

D. infinite

#### Answer: b



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**3.** 
$$\vec{a} = 2\hat{i} - \hat{j} + \hat{k}$$
,  $\vec{b} = \hat{i} + 2\hat{j} - \hat{k}$ ,  $\vec{c} = \hat{i} + \hat{j} - 2\hat{k}$  A vector coplanar with  $\vec{b}$  and  $\vec{c}$  whose projectin on  $\vec{a}$  is magnitude  $\sqrt{\frac{2}{3}}$  is  $2\hat{i} + 3\hat{j} - 3\hat{k}$  b.  $-2\hat{i} - \hat{j} + 5\hat{k}$  c.

 $2\hat{i} + 3\hat{i} + 3\hat{k} d$ .  $2\hat{i} + \hat{i} + 5\hat{k}$ 

A. 
$$2\hat{i} + 3\hat{j} - 3\hat{k}$$

$$\mathsf{B.}\,2\hat{i}+3\hat{j}+3\hat{k}$$

$$\mathbf{C.} - 2\hat{i} - \hat{j} + 5\hat{k}$$

$$D.\ 2\hat{i} + \hat{j} + 5\hat{k}$$

#### Answer: a,c



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- **4.** For three vectors  $\vec{u}$ ,  $\vec{v}$  and  $\vec{w}$  which of the following expressions is not equal to any of the remaining three ?  $\vec{u}$   $\vec{v}$   $\times$   $\vec{w}$  b.  $(\vec{v} \times \vec{w})\vec{u}$  c.  $\vec{v}$   $\vec{u}$   $\times$   $\vec{w}$  d.  $(\vec{u} \times \vec{v})\vec{w}$ 
  - A.  $\vec{u}$ .  $(\vec{v} \times \vec{w})$
  - B.  $(\vec{v} \times \vec{w})$ .  $\vec{u}$
  - C.  $\vec{v}$ .  $(\vec{u} \times \vec{w})$
  - D.  $(\vec{u} \times \vec{v})$ .  $\vec{w}$

#### Answer: c



**5.** Which of the following expressions are meaningful? a. 
$$\vec{u}$$
.  $(\vec{v} \times \vec{w})$  b.  $\vec{u}$ .  $\vec{v}$ .  $\vec{w}$  c.  $(\vec{u}\vec{v})$ .  $\vec{w}$  d.  $\vec{u}$  ×  $(\vec{v}$ .  $\vec{w})$ 

A. 
$$\vec{u}$$
.  $(\vec{v} \times \vec{w})$ 

B. 
$$(\vec{u}.\ \vec{v}).\ \vec{w}$$

C. 
$$(\vec{u}. \vec{v})\vec{w}$$

D. 
$$\vec{u} \times (\vec{v}. Vecw)$$

#### Answer: a,c



 $\vec{u} = \vec{a} - (\vec{a} \cdot \vec{b})\vec{b}$  and  $\vec{v} = \vec{a} \times \vec{b}$ . then  $|\vec{v}|$  is

are

two

non

collinear

unit

vectors,

and

A. 
$$|\vec{u}| + \vec{u} \cdot (\vec{a}x\vec{b})$$

 $\vec{a}$  and  $\vec{b}$ 

6.

$$B. |\vec{u}| + |\vec{u}. \vec{a}|$$

C. 
$$\left| \vec{u} \right| + \left| \vec{u} \cdot \vec{b} \right|$$

D. 
$$|\vec{u}| + \vec{u} \cdot (\vec{a} + \vec{b})$$

Answer: a,c



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7. Find the modulus of the Vector  $\frac{1}{3}(2\hat{i}-2\hat{j}+\hat{k})$  is



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Plane  $P_1$  is parallel to vectors  $2\hat{j} + 3\hat{k}and4\hat{j} - 3kandP_2$  is parallel to  $\hat{j}$  -  $\hat{k}$ and $3\hat{i}$  +  $3\hat{j}$  Then the angle betweenvector  $\vec{A}$  and a given vector

**8.** Let  $\vec{A}$  be a vector parallel to the line of intersection of planes  $P_1$  and  $P_2$ 

 $2\hat{i} + \hat{j} - 2\hat{k}$  is  $\pi/2$  b.  $\pi/4$  c.  $\pi/6$  d.  $3\pi/4$ 

 $A. \pi/2$ 

 $B.\pi/4$ 

 $C. \pi/6$ 

#### Answer: b,d



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9. The vector(s) which is/are coplanar with vectors

$$\hat{i} + \hat{j} + 2\hat{k}$$
 and  $\hat{i} + 2\hat{j} + \hat{k}$ , and perpendicular to vector  $\hat{i} + \hat{j} + \hat{k}$ , is/are a.

$$\hat{j} - \hat{k}$$
 b.  $-\hat{i} + \hat{j}$  c.  $\hat{i} - \hat{j}$  d.  $-\hat{j} + \hat{k}$ 

A. 
$$\hat{j} - \hat{k}$$

B. 
$$-\hat{i} + \hat{j}$$

C. 
$$\hat{i} - \hat{j}$$

D. 
$$-\hat{j} + \hat{k}$$

#### Answer: a,d



**10.** Let  $\vec{x}$ ,  $\vec{y}$  and  $\vec{z}$  be three vector each of magnitude  $\sqrt{2}$  and the angle between each pair of them is  $\frac{n}{3}$ . if vcea is a non - zero vector perpendicular to  $\vec{x}$  and  $\vec{y} \times \vec{z}$  and  $\vec{b}$  is a non-zero vector perpendicular to  $\vec{y}$  and  $\vec{z} \times \vec{x}$ , then

A. 
$$\vec{b} = (\vec{b}. \vec{z})(\vec{z} - \vec{x})$$

$$B. \vec{a} = (\vec{a}. \vec{y})(\vec{y} - \vec{z})$$

$$C. \vec{a}. \vec{b} = -(\vec{a}. \vec{y})(\vec{b}. \vec{z})$$

D. 
$$\vec{a} = (\vec{a} \cdot \vec{y})(\vec{z} - \vec{y})$$

#### Answer: a,b,c



11.

### **Watch Video Solution**

Let

 $\Delta PQR$ 

$$\vec{a}=QR, \vec{b}=RP \text{ and } \vec{c}=PQ \text{ if } \left|\vec{a}\right|=12, \left|\vec{b}\right|=4\sqrt{3} \text{ and } \vec{b}. \vec{c}=24, \text{ then}$$
 which of the following is (are ) true ?

be

a

triangle

Let

A. 
$$\frac{\left|\vec{c}\right|^2}{2} - \left|\vec{a}\right| = 12$$

B. 
$$\frac{|\vec{c}|^2}{2} - |\vec{a}| = 30$$

$$C. \left| \vec{a} \times \vec{b} + \vec{c} \times \vec{a} \right| = 48\sqrt{3}$$

D. 
$$\vec{a}$$
.  $\vec{b} = -72$ 

#### Answer: a,c,d

