# びdoubtnut 

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## MATHS

## BOOKS - CENGAGE PUBLICATION

## DIFFERENT PRODUCTS OF VECTORS AND THEIR GEOMETRICAL APPLICATIONS

## Illustration

1. Find the angle between the vectors $\hat{i}-2 \hat{j}+3 \hat{k}$ and $3 \hat{i}-2 \hat{j}+\hat{k}$.

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2. If $\vec{a}, \vec{b}$, and $\vec{c}$ are non-zero vectors such that $\vec{a}$. $\vec{b}=\vec{a}$. $\vec{c}$, then find the geometrical relation between the vectors.
3. if $\vec{r}$. $\vec{i}=\vec{r} . \vec{j}=\vec{r} . \vec{k}$ and $|\vec{r}|=6$, then find vector $\vec{r}$.

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4. If $\vec{a}, \vec{b}$ and $\vec{c}$ are unit vectors such that $\vec{a}+\vec{b}+\vec{c}=0$, then the value of $\vec{a} \cdot \vec{b}+\vec{b} \cdot \vec{c}+\vec{c} \cdot \vec{a}$ is

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5. If $\vec{a}, \vec{b}$, and $\vec{c}$ are mutually perpendicular vectors of equal magnitudes, then find the angle between vectors $\vec{a}$ and $\vec{a}+\vec{b}+\vec{c}$

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6. If $|\vec{a}|+|\vec{b}|=|\vec{c}|$ and $\vec{a}+\vec{b}=\vec{c}$, then find the angle between $\vec{a}$ and $\vec{b}$
7. If three unit vectors $\vec{a}, \vec{b}$ and $\vec{c}$ satisfy $\vec{a}+\vec{b}+\vec{c}=\overrightarrow{0}$. Then find the angle between $\vec{b}$ and $\vec{c}$.

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8. If $\theta$ is the angle between the unit vectors $\vec{a}$ and $\vec{b}$, then prove that
$\cos \left(\frac{\theta}{2}\right)=\frac{1}{2}|\vec{a}+\vec{b}|$

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9. find the projection of the vector $\hat{i}+2 \hat{j}+3 \hat{k}$ on the vector $5 \hat{i}-2 \hat{j}+4 \hat{k}$

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10. If the scalar projection of vector $x \hat{i}-\hat{j}+\hat{k}$ on vector $4 \hat{i}-2 \hat{j}+5 \hat{k}$ is $\frac{1}{3 \sqrt{5}}$. The find the value of $x$.

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11. If $\vec{a}=x \hat{i}+(x-1) \hat{j}+\hat{k}$ and $\vec{b}=(x+1) \hat{i}+\hat{j}+a \hat{k}$ make an acute angle $\forall x \in R$, then find the values of $a$

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12. If $\vec{a} . \vec{i}=\vec{a} \cdot(\hat{i}+\hat{j})=\vec{a}$. $(\hat{i}+\hat{j}+\hat{k})$. Then find the unit vector $\vec{a}$.

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13. Prove by vector method that $\cos (A+B)=\cos A \cos B-\sin A \sin B$
14. In any triangle $A B C$, prove the projection formula $a=b \cos C+c \cos B$ using vector method.

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15. Prove that an angle inscribed in a semi-circle is a right angle using vector method.

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16. Using dot product of vectors, prove that a parallelogram, whose diagonals are equal, is a rectangle

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17. If $a+2 b+3 c=4$, then find the least value (to the nearest integer) of
$a^{2}+b^{2}+c^{2}$
18. about to only mathematics

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19. vectors $\vec{a}, \vec{b}$ and $\vec{c}$ are of the same length and when take they form equal angles. If $\vec{a}=\hat{i}+\hat{j}$ and $\vec{b}=\hat{j}+\hat{k}$ then find vector $\vec{c}$.

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20. if $\vec{a}, \vec{b}$ and $\vec{c}$ are there mutually perpendicular unit vectors and $\vec{a}$ ia a unit vector then find the value of $|2 \vec{a}+\vec{b}+\vec{c}|^{2}$

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21. A particle acted by constant forces $4 \hat{i}+\hat{j}-3 \hat{k}$ and $3 \hat{i}+\hat{9} j-\hat{k}$ is displaced from point $\hat{i}+2 \hat{j}+3 \hat{k}$ to point $5 \hat{i}+4 \hat{j}+\hat{k}$ find the total work done by the forces in SI units.

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22. If $\vec{a}, \vec{b}, \vec{c}$ are mutually perpendicular vectors of equal magnitude show that $\vec{a}+\vec{b}+\vec{c}$ is equally inclined to $\vec{a}, \vec{b}$ and $\vec{c}$

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23. If $\vec{a}=4 \hat{i}+6 \hat{j}$ and $\vec{b}=3 \hat{i}+4 \hat{k}$ find the projection vector $\vec{a}$ to $\vec{b}$.

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24. If $|\vec{a}|=|\vec{b}|=|\vec{a}+\vec{b}|=1$ then find the value of $|\vec{a}-\vec{b}|$
25. If $\vec{a}=-\hat{i}+\hat{j}+\hat{k}$ and $\vec{b}=2 \hat{i}+0 \hat{j}+\hat{k}$ then find vector $\vec{c}$ satisfying the following conditions, (i) that it is coplaner with $\vec{a}$ and $\vec{b}$, (ii) that it is $\perp$ to $\vec{b}$ and (iii) that $\vec{a} . \vec{c}=7$.

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26. Let $\vec{a}, \vec{b}$, and $\vec{c}$ are vectors such that
$|\vec{a}|=3,|\vec{b}|=4$ and $|\vec{c}|=5$, and $(\vec{a}+\vec{b})$ is perpendicular to $\vec{c},(\vec{b}+\vec{c})$ is perpendicular to $\vec{a}$ and $(\vec{c}+\vec{a})$ is perpendicular to $\vec{b}$ Then find the value of $|\vec{a}+\vec{b}+\vec{c}|$.

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27. Prove that in a tetrahedron if two pairs of opposite edges are perpendicular , then the third pair is also perpendicular.
28. In isosceles triangles $A B C,|\vec{A} B|=|\vec{B} C|=8$, a point $E$ divides $A B$ internally in the ratio $1: 3$, then find the angle between $\vec{C}$ Eand $\vec{C} A($ where $|\vec{C} A|=12)$

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29. An arc $A C$ of a circle subtends a right angle at then the center $O$. the point B divides the arc in the ratio $1: 2$, If $\overrightarrow{O A}=a \& \vec{O} B=b$. then the vector $\vec{O} C$ in terms of $a \& b$, is

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30. Vector $\vec{O} A=\hat{i}+2 \hat{j}+2 \hat{k}$ turns through a right angle passing through the positive $x$-axis on the way. Show that the vector in its new position is

$$
\frac{4 \hat{i}-\hat{j}-\hat{k}}{\sqrt{2}}
$$

31. The foot of the perpendicular drawn from the origin to a plane is $(1,2,-3)$ Find the equation of the plane. or If $O$ is the origin and the coordinates of $P$ is $(1,2,-3)$, then find the equation of the plane passing through $P$ and perpendicular to $O P$

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32. Find $|\vec{a} \times \vec{b}|$, if $\vec{a}=\hat{i}-7 \hat{j}+7 \hat{k}$ and $\vec{b}=3 \hat{i}-2 \hat{j}+2 \hat{k}$.

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33. Let the vectors $\vec{a}$ and $\vec{b}$ be such that $|\vec{a}|=3$ and $|\vec{b}|=\frac{\sqrt{2}}{3}$, then, $\vec{a} \times \vec{b}$ is a unit vector, if the angel between $\vec{a}$ and $\vec{b}$ is?

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34. Prove that $(\vec{a}-\vec{b}) \times(\vec{a}+\vec{b})=2(\vec{a} \times \vec{b})$.

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35. Let $\vec{a}=\hat{i}+4 \hat{j}+2 \hat{k}, \vec{b}=3 \hat{i}-2 \hat{j}+7 \hat{k}$ and $\vec{c}=2 \hat{i}-\hat{j}+4 \hat{k}$ Find a vector $\vec{d}$ which is perpendicular to both $\vec{a}$ and $\vec{b}$ and $\vec{c} . \vec{d}=15$.

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36. If $A, B a n d C$ are the vetices of a triangle $A B C$, then prove sine rule $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$.

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37. Using cross product of vectors , prove that $\sin (A+B)=\sin A \cos B+\cos A \sin B$.
38. Find a unit vector perpendicular to the plane determined by the points (1, - 1, 2), (2, 0, - 1 ) and ( $0,2,1$ )

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39. If $\vec{a}$ and $\vec{b}$ are two vectors, then prove that $(\vec{a} \times \vec{b})^{2}=\left|\begin{array}{ll}\vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b}\end{array}\right|$.

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40. If $|\vec{a}|=2$, then find the value of $|\vec{a} \times \hat{i}|^{2}+|\vec{a} \times \hat{j}|^{2}+|\vec{a} \times \hat{k}|^{2}$

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41. $\vec{r} \times \vec{a}=\vec{b} \times \vec{a}, \vec{r} \times \vec{b}=\vec{a} \times \vec{b}, \vec{a} \neq \overrightarrow{0}, \vec{b} \neq \overrightarrow{0}, \vec{a} \neq \lambda \vec{b}$ and $\vec{a}$ is not perpendicular to $\vec{b}$, then find $\vec{r}$ in terms of $\vec{a}$ and $\vec{b}$.

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42. $A, B, C a n d D$ are any four points in the space, then prove that
$|\vec{A} B \times \vec{C} D+\vec{B} C \times \vec{A} D+\vec{C} A \times \vec{B} D|=4$ (area of $A B C)$.

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43. If $\vec{a}, \vec{b}$ and $\vec{c}$ are the position vectors of the vertices $A, B$ and $C$. respectively, of $\triangle A B C$. Prove that the perpendicualar distance of the vertex A from the base $B C$ of the triangle $A B C$ is $\frac{|\vec{a} \times \vec{b}+\vec{b} \times \vec{c}+\vec{c} \times \vec{a}|}{|\vec{c}-\vec{b}|}$

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44. Using vectors, find the area of the triangle with vertices $A(1,1,2), B(2$, $3,5)$ and $C(1,5,5)$.

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45. Find the area of the parallelogram whose adjacent sides are given by the vectors $\vec{a}=\hat{i}-\hat{j}+3 \hat{k}$ and $\vec{b}=2 \hat{i}-7 \hat{j}+\hat{k}$

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46. Find the area of a parallelogram whose diagonals are $\vec{a}=3 \hat{i}+\hat{j}-2 \hat{k}$ and $\vec{b}=\hat{i}-3 \hat{j}+4 \hat{k}$

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47. Let $\vec{a}, \vec{b}$ and $\vec{c}$ be three verctors such that $\vec{a} \neq 0,|\vec{a}|=|\vec{c}|=1,|\vec{b}|=4$ and $|\vec{b} \times \vec{c}|=\sqrt{15}$ If $\vec{b}-2 \vec{c}=\lambda \vec{a}$, then find the value of $\lambda$

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48. Find the moment about (1,-1,-1) of the force $3 \hat{i}+4 \hat{j}-5 \hat{k}$ acting at (1,0,-2)

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49. A rigid body is spinning about a fixed point ( $3,-2,-1$ ) with an angular velocity of $4 \mathrm{rad} / \mathrm{s}$, the axis of rotation being in the direction of $(1,2,-2)$.

Find the velocity of the particle at point $(4,1,1)$.

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50. If $\vec{a} \times \vec{b}=\vec{c} \times \vec{d}$ and $\vec{a} \times \vec{c}=\vec{b} \times \vec{d}$, then show that $\vec{a}-\vec{d}$, is parallel to $\vec{b}-\vec{c}$

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51. Show by a numerical example and geometrically also that $\vec{a} \times \vec{b}=\vec{a} \times \vec{c}$ does not imply $\vec{b}=\overrightarrow{.}$

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52. If $\vec{a}, \vec{b}, \vec{c}$ and $\vec{d}$ are the position vectors of the vertices of a cyclic quadrilateral

$$
A B C D,
$$

prove
that

$$
\frac{|\vec{a} \times \vec{b}+\vec{b} \times \vec{d}+\vec{d} \times \vec{a}|}{(\vec{b}-\vec{a}) \cdot(\vec{d}-\vec{a})}+\frac{|\vec{b} \times \vec{c}+\vec{c} \times \vec{d}+\vec{d} \times \vec{b}|}{(\vec{b}-\vec{c}) \cdot(\vec{d}-\vec{c})}=0
$$

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53. The position vectors of the vertices of a quadrilateral with $A$ as origin are $B(\vec{b}), D(\vec{d})$ andC $(\vec{l} \vec{b}+m \vec{d})$ Prove that the area of the quadral is $\frac{1}{2}(l+m)|\vec{b} \times \vec{d}|$

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54. Let $\vec{a}$ and $\vec{b}$ be unit vectors such that $|\vec{a}+\vec{b}|=\sqrt{3}$. Then find the value of $(2 \vec{a}+5 \vec{b}) \cdot((3 \vec{a}+\vec{b}+\vec{a} \times \vec{b}))$

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55. $u$ and $v$ are two non-collinear unit vectors such that $|\hat{u} \times \hat{v}|=\left|\frac{\hat{u}-\hat{v}}{2}\right|$. Find the value of $|\hat{u} \times(\hat{u} \times \hat{v})|^{2}$

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56. In triangle $A B C$, points $D$, EandF are taken on the sides $B C, C A a n d A B$, respectively, such that $\frac{B D}{D C}=\frac{C E}{E A}=\frac{A F}{F B}=n \quad$ Prove that $\triangle D E F=\frac{n^{2}-n+1}{(n+1)^{2}} \triangle(A B C)$

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57. Let $A, B, C$ be points with position vectors $2 \hat{i}-\hat{j}+\hat{k}, \hat{i}+2 \hat{j}+3 \hat{k}$ and $3 \hat{i}+\hat{j}+2 \hat{k}$ respectively. Find the shortest distance between point $B$ and plane $O A C$

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58. Let $\vec{a}=x \hat{i}+12 \hat{j}-\hat{k}, \vec{b}=2 \hat{i}+2 x \hat{j}+\hat{k}$ and $\vec{c}=\hat{i}+\hat{k}$ If the ordered set $[\vec{b} \vec{c} \vec{a}]$ is left handed, then find the values of $x$

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59. If $\vec{a}, \vec{b}$, and $\vec{c}$ are three non-coplanar vectors, then find the value of $\frac{\vec{a} \cdot(\vec{b} \times \vec{c})}{\vec{b} \cdot(\vec{c} \times \vec{a})}+\frac{\vec{b} \cdot(\vec{c} \times \vec{a})}{\vec{c} \cdot(\vec{a} \times \vec{b})}+\frac{\vec{c} \cdot(\vec{b} \times \vec{a})}{\vec{a} \cdot(\vec{b} \times \vec{c})}$

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60. If the vectors $2 \hat{i}-3 \hat{j}, \hat{i}+\hat{j}-\hat{k} a n d 3 \hat{i}-\hat{k}$ form three concurrent edges of a parallelepiped, then find the volume of the parallelepiped.

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61. The position vectors of the four angular points of a tetrahedron are
$A(\hat{j}+2 \hat{k}), B(3 \hat{i}+\hat{k}), C(4 \hat{i}+3 \hat{j}+6 \hat{k}) \operatorname{andD}(2 \hat{i}+3 \hat{j}+2 \hat{k})$ Find the volume of the tetrahedron $A B C D$

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62. Let $\vec{a}, \vec{b}, \vec{c}$ be three unit vectors and $\vec{a} \cdot \vec{b}=\vec{a} \cdot \vec{c}=0$. If the angle between $\vec{b}$ and $\vec{c}$ is $\frac{\pi}{3}$ then find the value of $|[\vec{a} \vec{b} \vec{c}]|$

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63. Prove that $[\vec{a}+\vec{b} \vec{b}+\vec{c} \vec{c}+\vec{a}]=2[\vec{a} \vec{b} \vec{c}]$
64. Prove that $[\vec{l} \vec{m} \vec{n}][\vec{a} \vec{b} \vec{c}]=\left|\begin{array}{lll}\vec{l} \cdot \vec{a} & \vec{l} \cdot \vec{b} & \vec{l} \cdot \vec{c} \\ \vec{m} \cdot \vec{a} & \vec{m} \cdot \vec{b} & \vec{m} \cdot \vec{c} \\ \vec{n} \cdot \vec{a} & \vec{n} \cdot \vec{b} & \vec{n} \cdot \vec{c}\end{array}\right|$

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65. If $\vec{a}=\hat{i}+\hat{j}+\hat{k}, \hat{b}=\hat{i}-\hat{j}+\hat{k}, \vec{c}=\hat{i}+2 \hat{j}-\hat{k}$, then find the value of
$\left|\begin{array}{lll}\vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} & \vec{a} \cdot \vec{c} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b} & \vec{b} \cdot \vec{c} \\ \vec{c} \cdot \vec{a} & \vec{c} \cdot \vec{b} & \vec{c} \cdot \vec{c}\end{array}\right|$

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66. Find the value of $a$ so that the volume of the parallelepiped formed by vectors $\hat{i}+a \hat{j}+k, \hat{j}+a \hat{k}$ and $a \hat{i}+\hat{k}$ becomes minimum.
67. If $\vec{u}, \vec{v}$ and $\vec{w}$ are three non-coplanar vectors, then prove that $(\vec{u}+\vec{v}-\vec{w}) \cdot[[(\vec{u}-\vec{v}) \times(\vec{v}-\vec{w})]]=\vec{u} .(\vec{v} \times \vec{w})$

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68. If $\vec{a}$ and $\vec{b}$ are two vectors, such that $|\vec{a} \times \vec{b}|=2$, then find the value of $[\vec{a} \vec{b} \vec{a} \times \vec{b}]$.

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69. Find the altitude of a parallelopiped whose three coterminous edges are vectors $\vec{A}=\hat{i}+\hat{j}+\hat{k}, \vec{B}=2 \hat{i}+4 \hat{j}-\hat{k}$ and $\vec{C}=\hat{i}+\hat{j}+3 \hat{k}$ with $\vec{A}$ and $\vec{B}$ as the sides of the base of the parallopiped.

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70. If $[\vec{a} \vec{b} \vec{c}]=2$, then find the value of $[(\vec{a}+2 \vec{b}-\vec{c})(\vec{a}-\vec{b})(\vec{a}-\vec{b}-\vec{c})]$

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71. If $\vec{a}, \vec{b}, \vec{c}$ are mutually perpendicular vector and $\vec{a}=\alpha(\vec{a} \times \vec{b})+\beta(\vec{b} \times \vec{c})+\gamma(\vec{c} \times \vec{a})$ and $[\vec{a} \vec{b} \vec{c}]=1$, then $\alpha+\beta+\gamma=(\mathrm{A})$ $|\vec{a}|^{2}$ (B) - $|\vec{a}|^{2}$ (C) 0 (D) none of these

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72. If $\vec{a}, \vec{b}$ and $\vec{c}$ are non- coplanar vecotrs, then prove that $|(\vec{a} \cdot \vec{d})(\vec{b} \times \vec{c})+(\vec{b} . \vec{d})(\vec{c} \times \vec{a})+(\vec{c} \cdot \vec{d})(\vec{a} \times \vec{b})|$ is independent of $\vec{d}$ where $\vec{d}$ is a unit vector.

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73. Prove that vectors $\vec{u}=\left(a l+a_{1} l_{1}\right) \hat{i}+\left(a m+a_{1} m_{1}\right) \hat{j}+\left(a n+a_{1} n_{1}\right) \hat{k}$ $\vec{v}=\left(b l+b_{1} l_{1}\right) \hat{i}+\left(b m+b_{1} m_{1}\right) \hat{j}+\left(b n+b_{1} n_{1}\right) \hat{k}$
$\vec{w}=\left(c l+c_{1} l_{1}\right) \hat{i}+\left(c m+c_{1} m_{1}\right) \hat{j}+\left(c n+c_{1} n_{1}\right) \hat{k}$ are coplanar.

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74. Let $G_{1}, G_{2}$ and $G_{3}$ be the centroids of the triangular faces OBC, OCAandOAB, respectively, of a tetrahedron $O A B C$ If $V_{1}$ denotes the volumes of the tetrahedron $O A B C a n d V_{2}$ that of the parallelepiped with $O G_{1}, O G_{2} a n d O G_{3}$ as three concurrent edges, then prove that $4 V_{1}=9 V_{2}$

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75. Prove that $\hat{i} \times(\vec{a} \times \vec{i})+\hat{j} \times(\vec{a} \times \vec{j})+\hat{k} \times(\vec{a} \times \vec{k})=2 \vec{a}$

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76. If $\hat{i} \times[(\vec{a}-\hat{j}) \times \hat{i}]+\hat{j} \times[(\vec{a}-\hat{k}) \times \hat{j}]+\hat{k} \times[(\vec{a}-\hat{i}) \times \hat{k}]=0$, then find vector $\vec{a}$.

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77. Let $\vec{a}$, $\vec{b}$, and $\vec{c}$ be any three vectors, then prove that $[\vec{a} \times \vec{b} \vec{b} \times \vec{c} \vec{c} \times \vec{a}$ $]=[\vec{a} \vec{b} \vec{c}]^{2}$

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78. For any four vectors prove that
$(\vec{b} \times \vec{c}) \cdot(\vec{a} \times \vec{d})+(\vec{c} \times \vec{a}) \cdot(\vec{b} \times \vec{d})+(\vec{a} \times \vec{b}) \cdot(\vec{c} \times \vec{d})=0$

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79. If $\vec{b}$ and $\vec{c}$ are two non-collinear such that $\vec{a} \mid(\vec{b} \times \vec{c})$. Then prove that $(\vec{a} \times \vec{b}) \cdot(\vec{a} \times \vec{c})$ is equal to $|\vec{a}|^{2}(\vec{b} \cdot \vec{c})^{\prime}$

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80. Find the vector of length 3 unit which is perpendicular to $\hat{i}+\hat{j}+\hat{k}$ and lies in the plane of $\hat{i}+\hat{j}+\hat{k}$ and $2 \hat{i}-3 \hat{j}$.

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81. Let $\hat{a}, \hat{b}$,and $\hat{c}$ be the non-coplanar unit vectors. The angle between $\hat{b}$ and $\hat{c}$ is $\alpha$, between $\hat{c}$ and $\hat{a}$ is $\beta$ and between $\hat{a}$ and $\hat{b}$ is $\gamma$. If $A(\hat{a} \cos \alpha, 0), B(\hat{b} \cos \beta, 0)$ and $C(\hat{c} \cos \gamma, 0)$, then show that in triangle
$A B C, \frac{|\hat{a} \times(\hat{b} \times \hat{c})|}{\sin A}=\frac{|\hat{b} \times(\hat{c} \times \hat{a})|}{\sin B}=\frac{|\hat{c} \times(\hat{a} \times \hat{b})|}{\sin C}$

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82. find the angle between the vectors $\vec{a}=3 \hat{i}+2 \hat{k}$ and

$$
\vec{b}=2 \hat{i}-2 \hat{j}+4 \hat{k}
$$

83. If $\vec{b}$ is not perpendicular to $\vec{c}$, then find the vector $\vec{r}$ satisfying the equation $\vec{r} \times \vec{b}=\vec{a} \times \vec{b}$ and $\vec{r} . \vec{c}=0$.

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84. If $\vec{a}$ and $\vec{b}$ are two given vectors and $k$ is any scalar, then find the vector $\vec{r}$ satisfying $\vec{r} \times \vec{a}+k \vec{r}=\vec{b}$.

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85. $\vec{r} \times \vec{a}=\vec{b} \times \vec{a}, \vec{r} \times \vec{b}=\vec{a} \times \vec{b}, \vec{a} \neq \overrightarrow{0}, \vec{b} \neq \overrightarrow{0}, \vec{a} \neq \lambda \vec{b}$ and $\vec{a}$ is not perpendicular to $\vec{b}$, then find $\vec{r}$ in terms of $\vec{a}$ and $\vec{b}$.

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86. if vectors $3 \hat{i}-2 \hat{j}+m \hat{k}$ and $-2 \hat{i}+\hat{j}+4 \hat{k}$ are perpendicular to each other, find the value of $m$

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87. $\vec{b}$ and $\vec{c}$ are unit vectors. Then for any arbitrary vector
$\vec{a},(((\vec{a} \times \vec{b})+(\vec{a} \times \vec{c})) \times(\vec{b} \times \vec{c})) \vec{b}-\vec{c}$ is always equal to $|\vec{a}|$ b. $\frac{1}{2}|\vec{a}|$ c. $\frac{1}{3}|\vec{a}|$ d. none of these

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88. If $\vec{a}, \vec{b}$ and $\vec{c}$ are non-coplanar unit vectors such that
$\vec{a} \times(\vec{b} \times \vec{c})=\frac{\vec{b}+\vec{c}}{\sqrt{2}}$, then the angle between $\vec{a}$ and $\vec{b}$ is $\mathrm{a} .3 \pi / 4 \mathrm{~b} . \pi / 4 \mathrm{c}$. $\pi / 2 \mathrm{~d} . \pi$

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89. 

$$
\frac{[\vec{R} \vec{\beta} \times(\vec{\beta} \times \vec{\alpha})] \vec{\alpha}}{|\vec{\alpha} \times \vec{\beta}|^{2}}+\frac{[\vec{R} \vec{\alpha} \times(\vec{\alpha} \times \vec{\beta})] \vec{\beta}}{|\vec{\alpha} \times \vec{\beta}|^{2}}=\frac{[\vec{R} \vec{\alpha} \vec{\beta}](\vec{\alpha} \times \vec{\beta})}{|\vec{\alpha} \times \vec{\beta}|^{2}}
$$

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90. If $\vec{a}$, $\vec{b}$ and $\vec{c}$ are three non-zero non-coplanar vectors, then the value of $(\vec{a} \cdot \vec{a}) \vec{b} \times \vec{c}+(\vec{a} \cdot \vec{b}) \vec{c} \times \vec{a}+(\vec{a} \cdot \vec{c}) \vec{a} \times \vec{b}$.

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91. Find a set of vectors reciprocal to the set $-\hat{i}+\hat{j}+\hat{k}, \hat{i}-\hat{j}+\hat{k}, \hat{i}+\hat{j}+\hat{k}$
92. find the projection of $3 \hat{i}-\hat{j}+4 \hat{k}$ on $2 \hat{i}+3 \hat{j}-6 \hat{k}$

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93. Let $\vec{a}, \vec{b}$, and $\vec{c}$ and $\vec{a}^{\prime}, \vec{b}^{\prime}, \vec{c}^{\prime}$ are reciprocal system of vectors, then prove that $\vec{a}^{\prime} \times \vec{b}^{\prime}+\vec{b}^{\prime} \times \vec{c}^{\prime}+\vec{c}^{\prime} \times \vec{a}^{\prime}=\frac{\vec{a}+\vec{b}+\vec{c}}{[\vec{a} \vec{b} \vec{c}]}$.

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94. $\vec{a}, \vec{b}$ and $\vec{c}$ are three non-coplanar vectors and $\vec{r}$. Is any arbitrary vector. Prove that $[\vec{b} \vec{c} \vec{r}] \vec{a}+[\vec{c} \vec{a} \vec{r}] \vec{b}+[\vec{a} \vec{b} \vec{r}] \vec{c}=[\vec{a} \vec{b} \vec{c}] \vec{r}$.

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95. Find the angle between the following pairs of vectors $3 \hat{i}+2 \hat{j}-6 \hat{k}, 4 \hat{i}-3 \hat{j}+\hat{k}, \hat{i}-2 \hat{j}+3 \hat{k}, 3 \hat{i}-2 \hat{j}+\hat{k}$

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96. If $\vec{a}$, $\vec{b}$, and $\vec{c}$ are non-zero vectors such that $\vec{a} \cdot \vec{b}=\vec{a}$. $\vec{c}$, then find the geometrical relation between the vectors.

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97. if $\vec{r} . \vec{i}=\vec{r} . \vec{j}=\vec{r} . \vec{k}$ and $|\vec{r}|=9$, then find vector $\vec{r}$.

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98. If $\vec{a}, \vec{b}$ and $\vec{c}$ are unit vectors such that $\vec{a}+\vec{b}+\vec{c}=3$, then the value of $\vec{a} \cdot \vec{b}+\vec{b} \cdot \vec{c}+\vec{c} \cdot \vec{a}$ is
99. If $\vec{a}, \vec{b}$, and $\vec{c}$ are mutually perpendicular vectors of equal magnitudes, then find the angle between vectors $\vec{a}$ and $\vec{a}+\vec{b}+\vec{c}$

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100. If $\vec{a}+\vec{b}=\vec{c}$, and $a+b=c$ then the angle between $\vec{a}$ and $\vec{b}$ is

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101. If three unit vectors $\vec{a}, \vec{b}$ and $\vec{c}$ satisfy $\vec{a}+\vec{b}+\vec{c}=\overrightarrow{0}$. Then find the angle between $\vec{a}$ and $\vec{c}$.

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102. If $\theta$ is the angle between the unit vectors $\vec{a}$ and $\vec{b}$, then prove that
$\sin \left(\frac{\theta}{2}\right)=\frac{1}{2}|\vec{a}-\vec{b}|$

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103. find the projection of vector $\hat{i}-3 \hat{j}-7 \hat{k}$ on the vector $7 \hat{i}-\hat{j}-8 \hat{k}$

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104. If the scalar projection of vector $x \hat{i}-\hat{j}+\hat{k}$ on vector $2 \hat{i}-\hat{j}+5 \hat{k}$, is $\frac{1}{\sqrt{30}}$ ,then find the value of $x$

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105. If $\vec{a}=x \hat{i}+(x-1) \hat{j}+\hat{k}$ and $\vec{b}=(x+1) \hat{i}+\hat{j}+a \hat{k}$ make an acute angle
$\forall x \in R$, then find the values of $a$
106. If $\vec{a} . \vec{i}=\vec{a} .(\hat{i}+\hat{j})=\vec{a} \cdot(\hat{i}+\hat{j}+\hat{k})$. Then find the unit vector $\vec{a}$.

## Watch Video Solution

107. Prove by vector method that $\cos (A+B)=\cos A \cos B-\sin A \sin B$

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108. In any triangle $A B C$, prove the projection formula $a=b \cos C+c \cos B$ using vector method.

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109. Prove that an angle inscribed in a semi-circle is a right angle using vector method.
110. Using dot product of vectors, prove that a parallelogram, whose diagonals are equal, is a rectangle

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111. If $a+2 b+3 c=4$, then find the least value (to the nearest integer) of $a^{2}+b^{2}+c^{2}$

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112. Definition of set

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113. Vectors $\vec{a}, \vec{b}$ and $\vec{c}$ are of the same length and when taken pair-wise they form equal angles. If $\vec{a}=\hat{i}+\hat{j}$ and $\vec{b}=\hat{j}+\hat{k}$ then find vector $\vec{c}$.

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114. If $\vec{a}, \vec{b}$ and $\vec{c}$ are three mutually perpendicular unit vectors and $\vec{d}$ is a unit vector which makes equal angle with $\vec{a}, \vec{b}$ and $\vec{c}$, then find the value of $|\vec{a}+\vec{b}+\vec{c}+\vec{d}|^{2}$.

## - Watch Video Solution

115. A particle acted by constant forces $4 \hat{i}+\hat{j}-3 \hat{k}$ and $3 \hat{i}+\hat{9} j-\hat{k}$ is displaced from point $\hat{i}+2 \hat{j}+3 \hat{k}$ to point $5 \hat{i}+4 \hat{j}+\hat{k}$ find the total work done by the forces in SI units.

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116. If $\vec{a}, \vec{b}$ and $\vec{c}$ are three mutually perpendicular vectors of equal magnitude, show that $\vec{a}+\vec{b}+\vec{c}$ is equally inclined to $\vec{a}, \vec{b}$ and $\vec{c}$. Also find the angle.

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117. If $\vec{a}=4 \hat{i}+6 \hat{j}$ and $\vec{b}=3 \hat{i}+4 \hat{k}$ find the vector component of $\vec{a}$ along $\vec{b}$.

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118. If $|\vec{a}|=|\vec{b}|=|\vec{a}+\vec{b}|=1$ then find the value of $|\vec{a}-\vec{b}|$

## - Watch Video Solution

119. If $\vec{a}=-\hat{i}+\hat{j}+\hat{k}$ and $\vec{b}=2 \hat{i}+0 \hat{j}+\hat{k}$ then find vector $\vec{c}$ satisfying the following conditions, (i) that it is coplaner with $\vec{a}$ and $\vec{b}$, (ii) that it is $\perp$ to $\vec{b}$ and (iii) that $\vec{a} . \vec{c}=7$.

## (D) Watch Video Solution

120. Let $\vec{a}, \vec{b}$, and $\vec{c}$ are vectors such that $|\vec{a}|=3,|\vec{b}|=4$ and $|\vec{c}|=5$, and $(\vec{a}+\vec{b})$ is perpendicular to $\vec{c},(\vec{b}+\vec{c})$ is perpendicular to $\vec{a}$ and $(\vec{c}+\vec{a})$ is perpendicular to $\vec{b}$ Then find the value of $|\vec{a}+\vec{b}+\vec{c}|$.

## - Watch Video Solution

121. Prove that in a tetrahedron if two pairs of opposite edges are perpendicular , then the third pair is also perpendicular.

## - Watch Video Solution

122. In isosceles triangles $A B C,|\vec{A} B|=|\vec{B} C|=8$, a point $E$ divides $A B$ internally in the ratio $1: 3$, then find the angle between $\vec{C}$ End $\vec{C} A($ where $|\vec{C} A|=12)$

## (D) Watch Video Solution

123. An arc $A C$ of a circle subtends a right angle at then the center $O$. the point B divides the arc in the ratio $1: 2$, If $\vec{O} A=a \& \vec{O} B=b$. then the vector $\vec{O} C$ in terms of $a \& b$, is

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124. Vector $\vec{O} A=\hat{i}+2 \hat{j}+2 \hat{k}$ turns through a right angle passing through the positive $x$-axis on the way. Show that the vector in its new position is $\frac{4 \hat{i}-\hat{j}-\hat{k}}{\sqrt{2}}$.

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125. The foot of the perpendicular drawn from the origin to a plane is
$(1,2,-3)$ Find the equation of the plane. or If $O$ is the origin and the
coordinates of $P$ is $(1,2,-3)$, then find the equation of the plane passing through $P$ and perpendicular to $O P$

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126. Find $|\vec{a} \times \vec{b}|$, if $\vec{a}=2 \hat{i}-7 \hat{j}+7 \hat{k}$ and $\vec{b}=3 \hat{i}-2 \hat{j}+2 \hat{k}$

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127. Let the vectors $\vec{a}$ and $\vec{b}$ be such that
$|\vec{a}|=3$ and $|\vec{b}|=\frac{\sqrt{2}}{3}$, then, $\vec{a} \times \vec{b}$ is a unit vector, if the angel between $\vec{a}$ and $\vec{b}$ is?

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128. Prove that $(\vec{a}-\vec{b}) \times(\vec{a}+\vec{b})=2(\vec{a} \times \vec{b})$.
129. answer any one question : (ii) let
$\vec{a}=\hat{i}+4 \hat{j}+2 \hat{k}, \vec{b}=3 \hat{i}-2 \hat{j}+7 \hat{k}$ and $\vec{c}=2 \hat{i}-\hat{j}+4 \hat{k}$. Find a vector $\vec{d}$ which is perpendicular to both the vectors $\vec{a}$ and $\vec{b}$ and $\vec{c} \cdot \vec{d}=18$

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130. If $A, B a n d C$ are the vetices of a triangle $A B C$, then prove sine rule $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$.

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131. Using cross product of vectors , prove that $\sin (A+B)=\sin A \cos B+\cos A \sin B$.

## - Watch Video Solution

132. Find a unit vector perpendicular to the plane determined by the points (1, - 1,2$),(2,0,-1)$ and $(0,2,1)$

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133. If $\vec{a}$ and $\vec{b}$ are two vectors, then prove that $(\vec{a} \times \vec{b})^{2}=\left|\begin{array}{ll}\vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b}\end{array}\right|$.

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134. If $|\vec{a}|=2$, then find the value of $|\vec{a} \times \hat{i}|^{2}+|\vec{a} \times \hat{j}|^{2}+|\vec{a} \times \hat{k}|^{2}$

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135. $\vec{r} \times \vec{a}=\vec{b} \times \vec{a}, \vec{r} \times \vec{b}=\vec{a} \times \vec{b}, \vec{a} \neq \overrightarrow{0}, \vec{b} \neq \overrightarrow{0}, \vec{a} \neq \lambda \vec{b}$ and $\vec{a}$ is not perpendicular to $\vec{b}$, then find $\vec{r}$ in terms of $\vec{a}$ and $\vec{b}$.
136. $A, B, C a n d D$ are any four points in the space, then prove that $|\vec{A} B \times \vec{C} D+\vec{B} C \times \vec{A} D+\vec{C} A \times \vec{B} D|=4($ area of $A B C)$.

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137. If $\vec{a}, \vec{b}$ and $\vec{c}$ are the position vectors of the vertices $A, B$ and $C$. respectively of $\triangle A B C$. Prove that the perpendicualar distance of the $|\vec{a} \times \vec{b}+\vec{b} \times \vec{c}+\vec{c} \times \vec{a}|$ vertex $A$ from the base $B C$ of the triangle $A B C$ is

$$
|\vec{c}-\vec{b}|
$$

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138. Using vectors, find the area of the triangle with vertices $A(1,1,2), B(2$, $3,5)$ and $C(1,5,5)$.
139. Find the area of the parallelogram whose adjacent sides are given by the vectors $\vec{a}=\hat{i}+2 \hat{j}+3 \hat{k}$ and $\vec{b}=2 \hat{i}-5 \hat{j}+2 \hat{k}$

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140. Find the area of a parallelogram whose diagonals are $\vec{a}=3 \hat{i}+\hat{j}-2 \hat{k}$ and $\vec{b}=\hat{i}-3 \hat{j}+4 \hat{k}$

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141. Let $\vec{a}$, $\vec{b}$ and $\vec{c}$ be three verctors such that $\vec{a} \neq 0,|\vec{a}|=|\vec{c}|=1,|\vec{b}|=4$ and $|\vec{b} \times \vec{c}|=\sqrt{15}$ If $\vec{b}-2 \vec{c}=\lambda \vec{a}$, then find the value of $\lambda$

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142. Find the moment about $(1,-1,-1)$ of the force $3 \hat{i}+4 \hat{j}-5 \hat{k}$ acting at (1,0,-2)
143. A rigid body is spinning about a fixed point ( $3,-2,-1$ ) with an angular velocity of $4 \mathrm{rad} / \mathrm{s}$, the axis of rotation being in the direction of $(1,2,2)$.

Find the velocity of the particle at point $(4,1,1)$.

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144. If $\vec{a} \times \vec{b}=\vec{c} \times \vec{d}$ and $\vec{a} \times \vec{c}=\vec{b} \times \vec{d}, \vec{a} \neq \vec{d}, \vec{b} \neq \vec{c}$ then show that $\vec{b}-\vec{c}$ is parallel to $\vec{a}-\vec{d}$

## - Watch Video Solution

145. Show by a numerical example and geometrically also that $\vec{a} \times \vec{b}=\vec{a} \times \vec{c}$ does not imply $\vec{b}=\overrightarrow{.}$

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146. If $\vec{a}, \vec{b}, \vec{c}$ and $\vec{d}$ are the position vectors of the vertices of a cycle quadrilateral
ABCD, prove that

$$
\frac{|\vec{a} \times \vec{b}+\vec{b} \times \vec{d}+\vec{d} \times \vec{a}|}{(\vec{b}-\vec{a}) \cdot(\vec{d}-\vec{a})}+\frac{|\vec{b} \times \vec{c}+\vec{c} \times \vec{d}+\vec{d} \times \vec{b}|}{(\vec{b}-\vec{c}) \cdot(\vec{d}-\vec{c})}=0
$$

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147. The position vectors of the vertices of a quadrilateral with $A$ as origin are $B(\vec{b}), D(\vec{d})$ and $C(\vec{l} \vec{b}+m \vec{d})$ Prove that the area of the quadrialateral is $\frac{1}{2}(l+m)|\vec{b} \times \vec{d}|$

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148. Let $\vec{a}$ and $\vec{b}$ be unit vectors such that $|\vec{a}+\vec{b}|=\sqrt{3}$. Then find the value of $(2 \vec{a}+5 \vec{b}) \cdot((3 \vec{a}+\vec{b}+\vec{a} \times \vec{b}))$

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149. $\hat{u}$ and $\hat{v}$ are two non-collinear unit vectors such that $\left|\frac{\hat{u}+\hat{v}}{2}+\hat{u} \times \vec{v}\right|=1$. Prove that $|\hat{u} \times \hat{v}|=\left|\frac{\hat{u}-\hat{v}}{2}\right|$

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150. In triangle $A B C$,points $D$, EandF are taken on the sides $B C, C A a n d A B$, respectively, such that $\frac{B D}{D C}=\frac{C E}{E A}=\frac{A F}{F B}=n$. Prove that $\triangle D E F=\frac{n^{2}-n+1}{(n+1)^{2}} \triangle(A B C)$

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151. Let $A, B, C$ be points with position vectors $2 \hat{i}-\hat{j}+\hat{k}, \hat{i}+2 \hat{j}+3 \hat{k}$ and $3 \hat{i}+\hat{j}+2 \hat{k}$ respectively. Find the shortest distance between point $B$ and plane $O A C$

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152. Let $\vec{a}=x \hat{i}+12 \hat{j}-\hat{k}, \vec{b}=2 \hat{i}+2 x \hat{j}+\hat{k} a n d \vec{c}=\hat{i}+\hat{k}$ If the ordered set $[\vec{b} \vec{c} \vec{a}]$ is left handed, then find the values of $x$

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153. If $\vec{a}, \vec{b}$ and $\vec{c}$ are three non-coplanar vectors, then find the value of $\underline{\vec{a} \cdot(\vec{b} \times \vec{c})}+\frac{\vec{b} \cdot(\vec{c} \times \vec{a})}{}+\underline{\vec{c} \cdot(\vec{b} \times \vec{a})}$
$\vec{b} .(\vec{c} \times \vec{a})$
$\vec{c} .(\vec{a} \times \vec{b})$
$\vec{a} .(\vec{b} \times \vec{c})$

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154. If the vectors $2 \hat{i}-3 \hat{j}, \hat{i}+\hat{j}-\hat{k}$ and $3 \hat{i}-\hat{k}$ form three concurrent edges of a parallelepiped, then find the volume of the parallelepiped.

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155. The position vectors of the four angular points of a tetrahedron are $A(\hat{j}+2 \hat{k}), B(3 \hat{i}+\hat{k}), C(4 \hat{i}+3 \hat{j}+6 \hat{k}) \operatorname{andD}(2 \hat{i}+3 \hat{j}+2 \hat{k})$ Find the volume of the tetrahedron $A B C D$

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156. Let $\vec{a}, \vec{b}, \vec{c}$ be three unit vectors and $\vec{a} \cdot \vec{b}=\vec{a} . \vec{c}=0$. If the angle between $\vec{b}$ and $\vec{c}$ is $\frac{\pi}{3}$ then find the value of $|[\vec{a} \vec{b} \vec{c}]|$

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157. Prove that $[\vec{a}+\vec{b} \vec{b}+\vec{c} \vec{c}+\vec{a}]=2[\vec{a} \vec{b} \vec{c}]$

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158. Prove that $[\vec{l} \vec{m} \vec{n}][\vec{a} \vec{b} \vec{c}]=\left|\begin{array}{lll}\vec{l} \cdot \vec{a} & \vec{l} \cdot \vec{b} & \vec{l} \cdot \vec{c} \\ \vec{m} . \vec{a} & \vec{m} \cdot \vec{b} & \vec{m} \cdot \vec{c} \\ \vec{n} \cdot \vec{a} & \vec{n} \cdot \vec{b} & \vec{n} \cdot \vec{c}\end{array}\right|$

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159. If $\vec{a}=\hat{i}+\hat{j}+\hat{k}, \hat{b}=\hat{i}-\hat{j}+\hat{k}, \vec{c}=\hat{i}+2 \hat{j}-\hat{k}$, then find the value of
$\left|\begin{array}{lll}\vec{a} \cdot \vec{a} & \vec{a} . \vec{b} & \vec{a} \cdot \vec{c} \\ \vec{b} \cdot \vec{a} & \vec{b} . \vec{b} & \vec{b} \cdot \vec{c} \\ \vec{c} . \vec{a} & \vec{c} . \vec{b} & \vec{c} . \vec{c}\end{array}\right|$

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160. Find the value of $a$ so that the volume of the parallelepiped formed by vectors $\hat{i}+a \hat{j}+k, \hat{j}+a \hat{k}$ and $a \hat{i}+\hat{k}$ becomes minimum.

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161. If $\vec{u}, \vec{v}$ and $\vec{w}$ are three non-coplanar vectors, then prove that $(\vec{u}+\vec{v}-\vec{w}) \cdot[[(\vec{u}-\vec{v}) \times(\vec{v}-\vec{w})]]=\vec{u} \cdot(\vec{v} \times \vec{w})$

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162. If $\vec{a}$ and $\vec{b}$ are two vectors, such that $|\vec{a} \times \vec{b}|=2$, then find the value of $[\vec{a} \vec{b} \vec{a} \times \vec{b}]$.

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163. Find the altitude of a parallelopiped whose three coterminous edges are vectors $\vec{A}=\hat{i}+\hat{j}+\hat{k}, \vec{B}=2 \hat{i}+4 \hat{j}-\hat{k}$ and $\vec{C}=\hat{i}+\hat{j}+3 \hat{k} w i t h \vec{A}$ and $\vec{B}$ as the sides of the base of the parallopiped.

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164. If $[\vec{a} \vec{b} \vec{c}]=2$, then find the value of $[(\vec{a}+2 \vec{b}-\vec{c})(\vec{a}-\vec{b})(\vec{a}-\vec{b}-\vec{c})]$

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165. If $\vec{a}, \vec{b}, \vec{c}$ are mutually perpendicular vector and $\vec{a}=\alpha(\vec{a} \times \vec{b})+\beta(\vec{b} \times \vec{c})+\gamma(\vec{c} \times \vec{a})$ and $[\vec{a} \vec{b} \vec{c}]=1$, then $\alpha+\beta+\gamma=(\mathrm{A})$ $|\vec{a}|^{2}$ (B) $-|\vec{a}|^{2}$ (C) 0 (D) none of these

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166. i. If $\vec{a}, \vec{b}$ and $\vec{c}$ are non-coplanar vectors, prove that vectors $3 \vec{a}-7 \vec{b}-4 \vec{c}, 3 \vec{a}-2 \vec{b}+\vec{c}$ and $\vec{a}+\vec{b}+2 \vec{c}$ are coplanar.

## - Watch Video Solution

167. Prove that vectors

$$
\begin{aligned}
& \vec{u}=\left(a l+a_{1} l_{1}\right) \hat{i}+\left(a m+a_{1} m_{1}\right) \hat{j}+\left(a n+a_{1} n_{1}\right) \hat{k} \\
& \vec{v}=\left(b l+b_{1} l_{1}\right) \hat{i}+\left(b m+b_{1} m_{1}\right) \hat{j}+\left(b n+b_{1} n_{1}\right) \hat{k} \\
& \vec{w}=\left(c l+c_{1} l_{1}\right) \hat{i}+\left(c m+c_{1} m_{1}\right) \hat{j}+\left(c n+c_{1} n_{1}\right) \hat{k}
\end{aligned}
$$

are coplannar.

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168. Let $G_{1}, G_{2}$ and $G_{3}$ be the centroids of the triangular faces $O B C, O C A a n d O A B$, respectively, of a tetrahedron $O A B C$ If $V_{1}$ denotes the volumes of the tetrahedron $O A B C a n d V_{2}$ that of the parallelepiped with $O G_{1}, O G_{2} a n d O G_{3}$ as three concurrent edges, then prove that $4 V_{1}=9 V_{2}$

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169. Prove that $\hat{i} \times(\vec{a} \times \vec{i})+\hat{j} \times(\vec{a} \times \vec{j})+\hat{k} \times(\vec{a} \times \vec{k})=2 \vec{a}$
170. If $\hat{i} \times[(\vec{a}-\hat{j}) \times \hat{i}]+\hat{j} \times[(\vec{a}-\hat{k}) \times \hat{j}]+\vec{k} \times[(\vec{a}-\vec{i}) \times \hat{k}]=0$, then find vector $\vec{a}$.

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171. Prove that: $[\vec{a} \times \vec{b} \vec{b} \times \vec{c} \vec{c} \times \vec{a}]=[\vec{a} \vec{b} \vec{c}]^{2}$

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$(\vec{b} \times \vec{c}) \cdot(\vec{a} \times \vec{d})+(\vec{c} \times \vec{a}) \cdot(\vec{b} \times \vec{d})+(\vec{a} \times \vec{b}) \cdot(\vec{c} \times \vec{d})=0$

## - Watch Video Solution

173. If $\vec{b}$ and $\vec{c}$ are two non-collinear such that $\vec{a}|\mid(\vec{b} \times \vec{c})$. Then prove that $(\vec{a} \times \vec{b}) .(\vec{a} \times \vec{c})$ is equal to $|\vec{a}|^{2}(\vec{b} \cdot \vec{c})$ '

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174. Find the vector of length 3 unit which is perpendicular to $\hat{i}+\hat{j}+\hat{k}$ and lies in the plane of $\hat{i}+\hat{j}+\hat{k}$ and $2 \hat{i}-3 \hat{j}$.

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175. Let $\hat{a}, \hat{b}$, and $\hat{c}$ be the non-coplanar unit vectors. The angle between $\hat{b}$ and $\hat{c}$ is $\alpha$, between $\hat{c}$ and $\hat{a}$ is $\beta$ and between $\hat{a}$ and $\hat{b}$ is $\gamma$. If $A(\hat{a} \cos \alpha, 0), B(\hat{b} \cos \beta, 0)$ and $C(\hat{c} \cos \gamma, 0)$, then show that in triangle
$A B C, \frac{|\hat{a} \times(\hat{b} \times \hat{c})|}{\sin A}=\frac{|\hat{b} \times(\hat{c} \times \hat{a})|}{\sin B}=\frac{|\hat{c} \times(\hat{a} \times \hat{b})|}{\sin C}$

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176. If $\vec{a}, \vec{b}$ and $\vec{c}$ are three non-coplanar non-zero vectors, then prove that $(\vec{a} \cdot \vec{a}) \vec{b} \times \vec{c}+(\vec{a} \cdot \vec{b}) \vec{c} \times \vec{a}+(\vec{a} \cdot \vec{c}) \vec{a} \times \vec{b}=[\vec{b} \vec{c} \vec{a}] \vec{a}$

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177. If $\vec{b}$ is not perpendicular to $\vec{c}$. Then find the vector $\vec{r}$ satisfying the equation $\vec{r} \times \vec{b}=\vec{a} \times \vec{b}$ and $\vec{r} . \vec{c}=0$

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178. If $\vec{a}$ and $\vec{b}$ are two given vectors and $k$ is any scalar, then find the vector $\vec{r}$ satisfying $\vec{r} \times \vec{a}+k \vec{r}=\vec{b}$.

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179. $\vec{r} \times \vec{a}=\vec{b} \times \vec{a}, \vec{r} \times \vec{b}=\vec{a} \times \vec{b}, \vec{a} \neq \overrightarrow{0}, \vec{b} \neq \overrightarrow{0}, \vec{a} \neq \lambda \vec{b}$ and $\vec{a}$ is not perpendicular to $\vec{b}$, then find $\vec{r}$ in terms of $\vec{a}$ and $\vec{b}$.

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180. If vector $\vec{x}$ satisfying $\vec{x} \times \vec{a}+(\vec{x} \cdot \vec{b}) \vec{c}=\vec{d}$ is given $\vec{x}=\lambda \vec{a}+\vec{a} \times \frac{\vec{a} \times(\vec{d} \times \vec{c})}{(\vec{a} \cdot \vec{c})|\vec{a}|^{2}}$, then find the value of $\lambda$

## ( Watch Video Solution

181. If $\vec{a}, \vec{b}$ and $\vec{c}$ be three non-coplanar vectors and $\mathrm{a}^{\prime}, \mathrm{b}$ ' and $\mathrm{c}^{\prime}$ constitute the reciprocal system of vectors, then prove that
i. $\vec{r}=\left(\vec{r} \cdot \vec{a}^{\prime}\right) \vec{a}+\left(\vec{r} \cdot \vec{b}^{\prime}\right) \vec{b}+\left(\vec{r} \cdot \vec{c}^{\prime}\right) \vec{c}$
ii. $\vec{r}=(\vec{r} \cdot \vec{a}) \vec{a}^{\prime}+(\vec{r} \cdot \vec{b}) \vec{b}^{\prime}+(\vec{r} \cdot \vec{c}) \vec{c}^{\prime}$

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182. If $\vec{a}, \vec{b}$ and $\vec{c}$ are non -coplanar unit vectors such that $\vec{a} \times(\vec{b} \times \vec{c})=\frac{\vec{b}+\vec{c}}{\sqrt{2}}, \vec{b}$ and $\vec{c}$ are non- parallel, then prove that the
angle between $\vec{a}$ and $\vec{b}$ is $3 \pi / 4$

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183. 

Prove
that

$$
\frac{[\vec{R} \vec{\beta} \times(\vec{\beta} \times \vec{\alpha})] \vec{\alpha}}{|\vec{\alpha} \times \vec{\beta}|^{2}}+\frac{[\vec{R} \vec{\alpha} \times(\vec{\alpha} \times \vec{\beta})] \vec{\beta}}{|\vec{\alpha} \times \vec{\beta}|^{2}}=\frac{[\vec{R} \vec{\alpha} \vec{\beta}](\vec{\alpha} \times \vec{\beta})}{|\vec{\alpha} \times \vec{\beta}|^{2}}
$$

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184. If $\vec{a}, \vec{b}$ and $\vec{c}$ are three non-coplanar non-zero vectors, then prove that $(\vec{a} \cdot \vec{a}) \vec{b} \times \vec{c}+(\vec{a} \cdot \vec{b}) \vec{c} \times \vec{a}+(\vec{a} \cdot \vec{c}) \vec{a} \times \vec{b}=[\vec{b} \vec{c} \vec{a}] \vec{a}$

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185. Find a set of vectors reciprocal to the set $-\hat{i}+\hat{j}+\hat{k}, \hat{i}-\hat{j}+\hat{k}, \hat{i}+\hat{j}+\hat{k}$
186. Let $\vec{a}, \vec{b}$ and $\vec{c}$ be a set of non- coplanar vectors and $\vec{a}^{\prime} \vec{b}^{\prime}$ and $\vec{c}^{\prime}$ be its reciprocal set.
prove that $\vec{a}=\frac{\vec{b} \times \vec{c}^{\prime}}{\left[\vec{a}^{\prime} \vec{b}^{\prime} \vec{c}^{\prime}\right]}, \vec{b}=\frac{\vec{c}^{\prime} \times \vec{a}^{\prime}}{\left[\vec{a}^{\prime} \vec{b}^{\prime} \vec{c}^{\prime}\right]}$ and $\vec{c}=\frac{\vec{a}^{\prime} \times \vec{b}^{\prime}}{\left[\vec{a}^{\prime} \vec{b}^{\prime} \vec{c}^{\prime}\right]}$

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187. If $\vec{a}, \vec{b}, \vec{c}$ and $\vec{a}^{\prime}, \vec{b}^{\prime}, \vec{c}^{\prime}$ are reciprocal system of vectors, then prove that $\vec{a}^{\prime} \times \vec{b}^{\prime}+\vec{b}^{\prime} \times \vec{c}^{\prime}+\vec{c}^{\prime} \times \vec{a}^{\prime}=\frac{\vec{a}+\vec{b}+\vec{c}}{[\vec{a} \vec{b} \vec{c}]}$

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188. If $\vec{a}, \vec{b}$ and $\vec{c}$ be three non-coplanar vectors and $\mathrm{a}^{\prime}, \mathrm{b}$ ' and c' constitute the reciprocal system of vectors, then prove that
i. $\vec{r}=\left(\vec{r} \cdot \vec{a}^{\prime}\right) \vec{a}+\left(\vec{r} \cdot \vec{b}^{\prime}\right) \vec{b}+\left(\vec{r} \cdot \vec{c}^{\prime}\right) \vec{c}$
ii. $\vec{r}=(\vec{r} \cdot \vec{a}) \vec{a}^{\prime}+(\vec{r} \cdot \vec{b}) \vec{b}^{\prime}+(\vec{r} \cdot \vec{c}) \vec{c}^{\prime}$

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## Exercise 2.1

1. Find $|\vec{a}|$ and $|\vec{b}|$, if $(\vec{a}+\vec{b}) \cdot(\vec{a}-\vec{b})=8$ and $|\vec{a}|=8|\vec{b}|$

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2. Show that $|\vec{a}| \vec{b}+|\vec{b}| \vec{a}$ is a perpendicular to $|\vec{a}| \vec{b}-|\vec{b}| \vec{a}$, for any two non-zero vectors $\vec{a} a n d \vec{b}$

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3. If the vectors $A, B, C$ of a triangle $A B C$ are $(1,2,3),(-1,0,0),(0,1,2)$, respectively then find $\angle A B C$

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4. If $|a|=3,|b|=4 a n d$ the angle between $a a n d b$ is $120^{\circ}$, then find the value of $|4 a+3 b|$

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5. If vectors $\hat{i}-2 x \hat{j}-3 y \hat{k}$ and $\hat{i}+3 x \hat{j}+2 y \hat{k}$ are orthogonal to each other, then find the locus of th point ( $\mathrm{x}, \mathrm{y}$ ).

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6. Let $\vec{a}, \vec{b}$ and $\vec{c}$ be pairwise mutually perpendicular vectors, such that $|\vec{a}|=2,|\vec{b}|=3,|\vec{c}|=6$, the find the length of $\vec{a}+\vec{b}+\vec{c}$.

## Watch Video Solution

7. If $\vec{a}+\vec{b}+\vec{c}=0,|\vec{a}|=3,|\vec{b}|=5,|\vec{c}|=7$, then find the angle between $\vec{b}$ and $\vec{c}$.

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8. If the angle between unit vectors $\vec{a}$ and $\vec{b}$ is $120^{\circ}$. Then find the value of $|\vec{a}+\vec{b}|$.

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9. Let $\vec{u}=\hat{i}+\hat{j}, \vec{v}=\hat{i}-\hat{j}$ and $\vec{w}=\hat{i}+2 \hat{j}+3 \hat{k}$. If $\hat{n}$ is a unit vector such that $\vec{u} \cdot \hat{n}=0$ and $\vec{v} \cdot \hat{n}=0,|\vec{w} \cdot \hat{n}|$ is equal to (A) 0 (B) 1 (C) 2 (D) 3
10. $A, B, C, D$ are any four points, prove that
$\vec{A} B \vec{C} D+\vec{B} C \vec{A} D+\vec{C} A \vec{B} D=4($ Area of $\triangle A B C)$.

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11. $P(1,0,-1), Q(2,0,-3), R(-1,2,0) \operatorname{and} S(3,-2,-1)$, then find the projection length of $\vec{P}$ Qon $\vec{R} S$

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12. If the vectors $3 \vec{p}+\vec{q} ; 5 p-3 \vec{q}$ and $2 \vec{p}+\vec{q} ; 3 \vec{p}-2 \vec{q}$ are pairs of mutually perpendicular vectors, then find the angle between vectors $\vec{p}$ and $\vec{q}$

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13. Let $\vec{A}$ and $\vec{B}$ be two non-parallel unit vectors in a plane. If $(\alpha \vec{A}+\vec{B})$ bisects the internal angle between $\vec{A}$ and $\vec{B}$, then find the value of $\alpha$

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14. Let $\vec{a}, \vec{b}$ and $\vec{c}$ be unit vectors, such that $\vec{a}+\vec{b}+\vec{c}=\vec{x}, \vec{a} \vec{x}=1, \vec{b} \vec{x}=\frac{3}{2},|\vec{x}|=2$. Then find the angle between $\vec{c}$ and $\vec{x}$

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15. If $\vec{a}$ and $\vec{b}$ are unit vectors, then find the greatest value of $|\vec{a}+\vec{b}|+|\vec{a}-\vec{b}|$.

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16. Constant forces $P_{1}=\hat{i}+\hat{j}+\hat{k}, P_{2}=-\hat{i}+2 \hat{j}-\hat{k}$ and $P_{3}=-\hat{j}-\hat{k}$ act on a particle at a point $A$ Determine the work done when particle is displaced from position $A(4 \hat{i}-3 \hat{j}-2 \hat{k})$ to $B(6 \hat{i}+\hat{j}-3 \hat{k})$

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17. Find $|\vec{a}|$ and $|\vec{b}|$, if $(\vec{a}+\vec{b}) \cdot(\vec{a}-\vec{b})=8$ and $|\vec{a}|=8|\vec{b}|$

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18. If $A, B, C, D$ are four distinct point in space such that $A B$ is not perpendicular to $C D$ and satisfies
$\overrightarrow{A B . C D}=k\left(|\overrightarrow{A D}|^{2}+|\overrightarrow{B C}|^{2}-|\overrightarrow{A C}|^{2}-|\overrightarrow{B D}|^{2}\right)$, then find the value of $k$

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1. If $\vec{a}=2 \hat{i}+3 \hat{j}-5 \hat{k}, \vec{b}=m \hat{i}+n \hat{j}+12 \hat{k}$ and $\vec{a} \times \vec{b}=\overrightarrow{0}$, then find (m,n)

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2. Find $\vec{a}$. $\vec{b}$ if $|\vec{a}|=3,|\vec{b}|=5$, and $|\vec{a} \times \vec{b}|=12$

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3. If $\vec{a} \times \vec{b}=\vec{b} \times \vec{c} \neq 0$ where $\vec{a}, \vec{b}$ and $\vec{c}$ are coplanar vectors, then for some scalar k prove that $\vec{a}+\vec{c}=k \vec{b}$.

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4. If $\vec{a}=2 \vec{i}+3 \vec{j}-\vec{k}, \vec{b}=-\vec{i}+2 \vec{j}-4 \vec{k}$ and $\vec{c}=\vec{i}+\vec{j}+\vec{k}$, then find the value of $(\vec{a} \times \vec{b}) \cdot(\vec{a} \times \vec{c})$
5. If the vectors $\vec{c}, \vec{a}=x \hat{i}+y \hat{j}+z \hat{k}$ and $\vec{b}=\hat{j}$ are such that $\vec{a}, \vec{c}$ and $\vec{b}$ form a right-handed system, then find $\vec{c}$
A. (a) $z \hat{i}-x \hat{k}$
B. (b) $\overrightarrow{0}$
C. (c) $y \hat{j}$
D. (d) $-z \hat{i}+x \hat{k}$

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6. Given that $\vec{a} \vec{b}=\vec{a} \vec{c}, \vec{a} \times \vec{b}=\vec{a} \times \vec{c}$ and $\vec{a}$ is not a zero vector. Show that $\vec{b}=\vec{c}$
7. Show that $(\vec{a}-\vec{b}) \times(\vec{a}+\vec{b})=2 \vec{a} \times \vec{b}$ and given a geometrical interpretation of it.

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8. If $\vec{x}$ and $\vec{y}$ are unit vectors and $|\vec{z}|=\frac{2}{\sqrt{7}}$ such that $\vec{z}+(\vec{z} \times \vec{x})=\vec{y}$ then find the angle $\theta$ between $\vec{x}$ and $\vec{z}$

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9. prove that $(\vec{a} . \hat{i})(\vec{a} \times \hat{i})+(\vec{a} . \hat{j})(\vec{a} \times \hat{j})+(\vec{a} . \hat{k})(\vec{a} \times \hat{k})=\overrightarrow{0}$

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10. Let $\vec{a}, \vec{b}$ and $\vec{c}$ be three non-zero vectors such that $\vec{a}+\vec{b}+\vec{c}=0$ and $\lambda \vec{b} \times \vec{a}+\vec{b} \times \vec{c}+\vec{c} \times \vec{a}=0$, then find the value of $\lambda$
11. A particle has an angular speed of $3 \mathrm{rad} / \mathrm{s}$ and the axis of rotation passes through the points $(1,1,2)$ and $(1,2,-2)$ Find the velocity of the particle at point $P(3,6,4)$

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12. Let $\vec{a}, \vec{b}$ and $\vec{c}$ be unit vectors such that $\vec{a} . \vec{b}=0=\vec{a}$. $\vec{c}$. It the angle between $\vec{b}$ and $\vec{c}$ is $\frac{\pi}{6}$ then find $\vec{a}$.

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13. If $|\vec{a} \times \vec{b}|^{2}+(\vec{a} . \vec{b})^{2}=256$ and $|\vec{a}|=4$, then $|\vec{b}|$ is equal to

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14. Given $|\vec{a}|=|\vec{b}|=1$ and $|\vec{a}+\vec{b}|=\sqrt{3}$ if $\vec{c}$ is a vector such that $\vec{c}-\vec{a}-2 \vec{b}=3(\vec{a} \times \vec{b})$ then find the value of $\vec{c} \cdot \vec{b}$.

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15. Find the moment of $\vec{F}$ about point $(2,-1,3)$, where force $\vec{F}=3 \hat{i}+2 \hat{j}-4 \hat{k}$ is acting on point ( $1,-1,2$ ).

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## Exercise 2.3

1. If $\vec{a}, \vec{b}, \vec{c}$ and $\vec{d}$ are four non-coplanar unit vectors such that $\vec{d}$ makes equal angles with all the three vectors $\vec{a}, \vec{b}, \vec{c}$ then prove that $[\vec{d} \vec{a} \vec{b}]=[\vec{d} \vec{c} \vec{b}]=[\vec{d} \vec{c} \vec{a}]$

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2. prove that if $[\vec{l} \vec{m} \vec{n}]$ are three non-coplanar vectors, then $[\vec{l} \vec{m} \vec{n}](\vec{a} \times \vec{b})=\left|\begin{array}{lll}\vec{l} \cdot \vec{a} & \vec{l} \cdot \vec{b} & \vec{l} \\ \vec{m} \cdot \vec{a} & \vec{m} \cdot \vec{b} & \vec{m} \\ \vec{n} \cdot \vec{a} & \vec{n} \cdot \vec{b} & \vec{n}\end{array}\right|$

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3. If the volume of a parallelepiped whose adjacent edges are $\vec{a}=2 \hat{i}+3 \hat{j}+4 \hat{k}, \vec{b}=\hat{i}+\alpha \hat{j}+2 \hat{k}, \vec{c}=\hat{i}+2 \hat{j}+\alpha \hat{k}$ is 15 , then find the value of $\alpha$ if $(\alpha>0)$

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4. If $\vec{a}=\hat{i}+\hat{j}+\hat{k}$ and $\vec{b}=\hat{i}-2 \hat{j}+\hat{k}$ then find the vector $\vec{c}$ such that $\vec{a} . \vec{c}=2$ and $\vec{a} \times \vec{c}=\vec{b}$.
5. If $\vec{x} \cdot \vec{a}=0 \vec{x} . \vec{b}=0$ and $\vec{x} \cdot \vec{c}=0$ for some non zero vector $\vec{x}$ then show that $[\vec{a} \vec{b} \vec{c}]=0$

## D Watch Video Solution

6. If $\vec{a}=\hat{i}+\hat{j}+\hat{k}$ and $\vec{b}=\hat{i}-2 \hat{j}+\hat{k}$ then find the vector $\vec{c}$ such that $\vec{a} \cdot \vec{c}=2$ and $\vec{a} \times \vec{c}=\vec{b}$.

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7. If $\vec{a}, \vec{b}, \vec{c}$ are three non-coplanar vectors such that $\vec{a} \times \vec{b}=\vec{c}, \vec{b} \times \vec{c}=\vec{a}, \vec{c} \times \vec{a}=\vec{b}$, then the value of $|\vec{a}|+|\vec{b}|+|\vec{c}|$ is

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$$
\vec{b} \times(\vec{a} \times \vec{b})
$$

8. If $\vec{a}=\vec{P}+\vec{q}, \vec{P} \times \vec{b}=\overrightarrow{0}$ and $\vec{q} \cdot \vec{b}=0$ then prove that
$\vec{b} . \vec{b}$
9. Prove that $(\vec{a} .(\vec{b} \times \hat{i})) \hat{i}+(\vec{a} .(\vec{b} \times \hat{j})) \hat{j}+(\vec{a} \cdot(\vec{b} \times \hat{k})) \hat{k}=\vec{a} \times \vec{b}$

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10. For any four vectors, $\vec{a}, \vec{b}, \vec{c}$ and $\vec{d}$ prove that
$\vec{d} \cdot(\vec{a} \times(\vec{b} \times(\vec{c} \times \vec{d})))=(\vec{b} \cdot \vec{d})[\vec{a} \vec{c} \vec{d}]$.

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11. If $\vec{a}$ and $\vec{b}$ be two non-collinear unit vector such that $\vec{a} \times(\vec{a} \times \vec{b})=\frac{1}{2} \vec{b}$, then find the angle between $\vec{a}$ and $\vec{b}$.

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12. show that $(\vec{a} \times \vec{b}) \times \vec{c}=\vec{a} \times(\vec{b} \times \vec{c})$ if and only if $\vec{a}$ and $\vec{c}$ are collinear or $(\vec{a} \times \vec{c}) \times \vec{b}=\overrightarrow{0}$

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13. Let $\vec{a}, \vec{b}$ and $\vec{c}$ be the non zero vectors such that $(\vec{a} \times \vec{b}) \times \vec{c}=\frac{1}{3}|\vec{b}||\vec{c}| \vec{a}$. if theta is the acute angle between the vectors
$\vec{b}$ and $\vec{c}$ then $\sin \theta$ equals (A) $\frac{1}{3}$ (B) $\frac{\sqrt{2}}{3}$ (C) $\frac{2}{3}$ (D) $2 \frac{\sqrt{2}}{3}$

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14. If $\vec{p}, \vec{q}, \vec{r}$ denote vector $\vec{b} \times \vec{c}, \vec{c} \times \vec{a}, \vec{a} \times \vec{b}$, respectively, show that $\vec{a}$ is parallel to $\vec{q} \times \vec{r}, \vec{b}$ is parallel $\vec{r} \times \vec{p}, \vec{c}$ is parallel to $\vec{p} \times \vec{q}$.

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15. Let $\vec{a}, \vec{b}, \vec{c}$ be non -coplanar vectors and let equations $\vec{a}^{\prime}, \vec{b}^{\prime}, \vec{c}^{\prime}$ are reciprocal system of vector $\vec{a}, \vec{b}, \vec{c}$ then prove that $\vec{a} \times \vec{a}^{\prime}+\vec{b} \times \vec{b}^{\prime}+\vec{c} \times \vec{c}^{\prime}$ is a null vector.

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16. Given unit vectors $\hat{m}, \hat{n}$ and $\hat{p}$ such that angel between $\hat{m}$ and $\hat{n}$ is $\alpha$ and angle between $\hat{p}$ and $(\hat{m} \times \hat{n})$ is also $\alpha$, then $[\hat{n} \hat{p} \hat{m}]=$

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17. $\vec{a}, \vec{b}, \vec{c}$ are threee unit vectors and every two are two inclined to each at an angle $\cos ^{-1}(3 / 5)$. If $\vec{a} \times \vec{b}=p \vec{a}+q \vec{b}+r \vec{c}$, where $p, q, r$ are scalars, then find the value of $q$.

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18. Let $\vec{a}=a_{1} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}, \vec{b}=b_{1} \hat{i}+b_{2} \hat{j}+b_{3} \hat{k}$ and $\vec{c}=c_{1} \hat{i}+c_{2} \hat{j}+c_{3} \hat{k}$ be three non-zero vectors such that $\vec{c}$ is a unit vector perpendicular to both
vectors, $\vec{a}$ and $\vec{b}$. If the angle between $\vec{a}$ and $\vec{b}$ is $\pi / 6$ then $\left|\begin{array}{lll}a_{1} & a_{2} & a_{3} \\ b_{1} & b_{2} & b_{3} \\ c_{1} & c_{2} & c_{3}\end{array}\right|$ is equal to

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## Exercises

1. Show that

$$
\left|\begin{array}{lll}
(a-x)^{2} & (a-y)^{2} & (a-z)^{2} \\
(b-x)^{2} & (b-y)^{2} & (b-z)^{2} \\
(c-x)^{2} & (c-y)^{2} & (c-z)^{2}
\end{array}\right|=2(a-b)(b-c)(c-a)(x-y)(y-z)(z-x)
$$

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2. If $O A B C$ is a tetrahedron where $O$ is the origin and $A, B$, and $C$ are the other three vertices with position vectors, $\vec{a}, \vec{b}$, and $\vec{c}$ respectively, then prove that the centre of the sphere circumscribing the tetrahedron is

$$
a^{2}(\vec{b} \times \vec{c})+b^{2}(\vec{c} \times \vec{a})+c^{2}(\vec{a} \times \vec{b})
$$

given by position vector

$$
2[\vec{a} \vec{b} \vec{c}]
$$

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3. Find the height of the regular pyramid with each edge measuring Icm . Also,
if $\alpha$ is angle between any edge and face not containing that edge, then prove that $\cos \alpha=\frac{1}{\sqrt{3}}$

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4. In $\triangle A B C$, a point $P$ is taken on $A B$ such that $A P / B P=1 / 3$ and point $Q$ is taken on $B C$ such that $C Q / B Q=3 / 1$. If $R$ is the point of intersection
of the lines AQandCP, using vector method, find the area of $A B C$ if the area of $B R C$ is 1 unit

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5. Let $O$ be an interior points of $\triangle A B C$ such that $O A+2 O B+3 O C=\overrightarrow{0}$, then the ratio of $\triangle A B C$ to area of $\triangle A O C$ is

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6. The lengths of two opposite edges of a tetrahedron of aandb; the shortest distane between these edgesis $d$, and the angel between them if $\theta$ Prove using vector 4 s that the volume of the tetrahedron is $\frac{a b d i s n \theta}{6}$.

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7. Find the volume of a parallelopiped having three coterminus vectors of equal magnitude $|\vec{a}|$ and equal inclination $\theta$ with each other.

## (D) Watch Video Solution

8. $\vec{p}, \vec{q}$, and $\vec{r}$ are three mutually perpendicular vectors of the same magnitude. If vector $\vec{x}$ satisfies the equation $\vec{p} \times((\vec{x}-\vec{q}) \times \vec{p})+\vec{q} \times((\vec{x}-\vec{r}) \times \vec{q})+\vec{r} \times((\vec{x}-\vec{p}) \times \vec{r})=0$, then $\vec{x}$ is given by $\frac{1}{2}(\vec{p}+\vec{q}-2 \vec{r})$ b. $\frac{1}{2}(\vec{p}+\vec{q}+\vec{r})$ c. $\frac{1}{3}(\vec{p}+\vec{q}+\vec{r})$ d. $\frac{1}{3}(2 \vec{p}+\vec{q}-\vec{r})$

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9. Given the vectors $\vec{A}, \vec{B}$, and $\vec{C}$ form a triangle such that $\vec{A}=\vec{B}+\vec{C}$ find $a, b, c, a n d d$ such that the area of the triangle is 56 where $\vec{A}=a \hat{i}+b \hat{j}+c \hat{k}$ $\vec{B}=d \hat{i}+3 \hat{j}+4 \hat{k} \vec{C}=3 \hat{i}+\hat{j}-2 \hat{k}$

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10. A line I is passing through the point $\vec{b}$ and is parallel to vector $\vec{c}$. Determine the distance of point $A(\vec{a})$ from the line $I$ in from
$\left|\vec{b}-\vec{a}+\frac{(\vec{a}-\vec{b}) \vec{c}}{|\vec{c}|^{2}} \vec{c}\right|$ or $\frac{|(\vec{b}-\vec{a}) \times \vec{c}|}{|\vec{c}|}$

## Watch Video Solution

11. If $\vec{e}_{1}, \vec{e}_{2}, \vec{e}_{3}$ and $\vec{E}_{1}, \vec{E}_{2}, \vec{E}_{3}$ are two sets of vectors such that $\vec{e}_{i} \vec{E}_{j}=1$, if $i=j$ and $\vec{e}_{i} \vec{E}_{j}=0$ and if $i \neq j$, then prove that $\left[\begin{array}{lll}\vec{e}_{1} & \vec{e}_{2} & \vec{e}_{3}\end{array}\right]\left[\begin{array}{lll}\vec{E}_{1} & \vec{E}_{2} & \vec{E}_{3}\end{array}\right]=1$.

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12. In a quadrillateral $A B C D$, it is given that $A B \| C D$ and the diagonals $A C$ and $B D$ are perpendiclar to each other . Show that $A D . B C=A B . C D$.

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13. $O A B C$ is regular tetrahedron in which $D$ is the circumcentre of $O A B$ and E is the midpoint of edge $A C$ Prove that $D E$ is equal to half the edge of tetrahedron.

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14. If $\mathrm{A}(\vec{a}) \cdot B(\vec{b})$ and $C(\vec{c})$ are three non-collinear point and origin does not lie in the plane of the points $\mathrm{A}, \mathrm{B}$ and C , then for any point $P(\vec{P})$ in the plane of the $\triangle A B C$ such that vector $\overrightarrow{O P}$ is $\perp$ to plane of triangIABC, show that $\overrightarrow{O P}=\frac{[\vec{a} \vec{b} \vec{c}](\vec{a} \times \vec{b}+\vec{b} \times \vec{c}+\vec{c} \times \vec{a})}{4 \Delta^{2}}$

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15. If $\vec{a}, \vec{b}, \vec{c}$ are three given non-coplanar vectors and any arbitrary vector
$\vec{r}$ in space, where $\Delta_{1}=\left|\begin{array}{lll}\vec{r} \cdot \vec{a} & \vec{b} \cdot \vec{a} & \vec{c} \cdot \vec{a} \\ \vec{r} \cdot \vec{b} & \vec{b} \cdot \vec{b} & \vec{c} \cdot \vec{b} \\ \vec{r} \cdot \vec{c} & \vec{b} \cdot \vec{c} & \vec{c} \cdot \vec{c}\end{array}\right|, \Delta_{2}=\left|\begin{array}{lll}\vec{a} \cdot \vec{a} & \vec{r} \cdot \vec{a} & \vec{c} \cdot \vec{a} \\ \vec{a} \cdot \vec{b} & \vec{r} \cdot \vec{b} & \vec{c} \cdot \vec{b} \\ \vec{a} \cdot \vec{c} & \vec{r} \cdot \vec{c} & \vec{c} \cdot \vec{c}\end{array}\right|$
$\Delta_{3}=\left|\begin{array}{lll}\vec{a} \cdot \vec{a} & \vec{b} \cdot \vec{a} & \vec{r} \cdot \vec{a} \\ \vec{a} \cdot \vec{b} & \vec{b} \cdot \vec{b} & \vec{r} \cdot \vec{b} \\ \vec{a} \cdot \vec{c} & \vec{b} \cdot \vec{c} & \vec{r} \cdot \vec{c}\end{array}\right|, \Delta=\left|\begin{array}{lll}\vec{a} \cdot \vec{a} & \vec{b} \cdot \vec{a} & \vec{c} \cdot \vec{a} \\ \vec{a} \cdot \vec{b} & \vec{b} \cdot \vec{b} & \vec{c} \cdot \vec{b} \\ \vec{a} \cdot \vec{c} & \vec{b} \cdot \vec{c} & \vec{c} \cdot \vec{c}\end{array}\right|$,
then prove that $\vec{r}=\frac{\Delta_{1}}{\Delta} \vec{a}+\frac{\Delta_{2}}{\Delta} \vec{b}+\frac{\Delta_{3}}{\Delta} \vec{c}$

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## Exercises MCQ

1. Two vectors in space are equal only if they have equal component in a. a
given direction
b. two given directions
c. three given
directions
d. in any arbitrary direction
A. a given direction
B. two given directions
C. three given direction
D. in any arbitrary direaction

## Answer: c

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2. Let $\vec{a}, \vec{b}$ and $\vec{c}$ be the three vectors having magnitudes, 1,5 and 3 , respectively, such that the angle between
$\vec{a}$ and $\vec{b}$ is $\theta$ and $\vec{a} \times(\vec{a} \times \vec{b})=\vec{c}$. Then $\tan \theta$ is equal to
A. 0
B. $\frac{2}{3}$
C. $\frac{3}{5}$
D. $\frac{3}{4}$

## Answer: d

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3. $\vec{a}, \vec{b}$, and $\vec{c}$ are three vectors of equal magnitude. The angle between each pair of vectors is $\pi / 3$ such that $|\vec{a}+\vec{b}+\vec{c}|=\sqrt{6}$. Then $|\vec{a}|$ is equal
to a. 2 b. -1 c. 1 d. $\sqrt{6} / 3$
A. 2
B. -1
C. 1
D. $\sqrt{6} / 3$

## Answer: c

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4. Let $\vec{p}$ and $\vec{q}$ be any two orthogonal vectors of equal magnitude 4 each. Let $\vec{a}$, $\vec{b}$, and $\vec{c}$ be any three vectors of lengths $7 \sqrt{15}$ and $2 \sqrt{33}$, mutually perpendicular to each other. Then find the distance of the vector

$$
(\vec{a} \vec{p}) \vec{p}+(\vec{a} \vec{q}) \vec{q}+(\vec{a} \vec{p} \times \vec{q})(\vec{p} \times \vec{q})+(\vec{b} \vec{p}) \vec{p}(\vec{b} \vec{q}) \vec{q}+(\vec{b} \vec{p} \times \vec{q})(\vec{p} \times \vec{q})+(
$$

from the origin.
A. $\vec{a}+\vec{b}+\vec{c}$
B. $\frac{\vec{a}}{|\vec{a}|}+\frac{\vec{b}}{|\vec{b}|}+\frac{\vec{c}}{|\vec{c}|}$
C. $\frac{\vec{a}}{|\vec{a}|^{2}}+\frac{\vec{b}}{|\vec{b}|^{2}}+\frac{\vec{c}}{|\vec{c}|^{2}}$
D. $|\vec{a}| \vec{a}-|\vec{b}| \vec{b}+|\vec{c}| \vec{c}$

## Answer: b

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5. Let $\vec{a}=\hat{i}+\hat{j}$ and $\vec{b}=2 \hat{i}-\hat{k}$, then the point of intersection of the $\vec{r} \times \vec{a}=\vec{b} \times \vec{a}$ and $\vec{r} \times \vec{b}=\vec{a} \times \vec{b}$ is a. $(3,-1,1)$ b. $(3,1,-1)$ c. $(-3,1,1) \mathrm{d}$. (-3,-1,-1)
A. $\hat{i}-\hat{j}+\hat{k}$
B. $3 \hat{i}-\hat{j}+\hat{k}$
C. $3 \hat{i}+\hat{j}-\hat{k}$
D. $\hat{i}-\hat{j}-\hat{k}$

## Answer: c

## D Watch Video Solution

6. If $\vec{a}$ and $\vec{b}$ are two vectors, such that $\vec{a} \cdot \vec{b}>0$ and $|\vec{a} \cdot \vec{b}|=|\vec{a} \times \vec{b}|$ then the angle between the vectors $\vec{a}$ and $\vec{b}$ is
A. $\pi$
B. $7 \pi / 4$
C. $\pi / 4$
D. $3 \pi / 4$

## Answer: d

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7. If $\hat{a}, \hat{b}$, and $\hat{c}$ are three unit vectors, such that $\hat{a}+\hat{b}+\hat{c}$ is also a unit vector and $\theta_{1}, \theta_{2}$ and $\theta_{3}$ are angles between the vectors $\hat{a}, \hat{b} ; \hat{b}, \hat{c} a n d \hat{c}, \hat{a}$
respectively, then among $\theta_{1}, \theta_{2}$ and $\theta_{3}$. a. all are acute angles b. all are right angles c. at least one is obtuse angle d. none of these
A. all are acute angles
B. all are right angles
C. at least one is obtuse angle
D. none of these

## Answer: c

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8. If $\vec{a}, \vec{b}, \vec{c}$ are unit vectors such that $\vec{a} . \vec{b}=0=\vec{a} . \vec{c}$ and the angle between $\vec{b}$ and $\vec{c}$ is $\frac{\pi}{3}$, then find the value of $|\vec{a} \times \vec{b}-\vec{a} \times \vec{c}|$.
A. $1 / 2$
B. 1
C. 2
D. none of these

## Answer: b

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9. about to only mathematics
A. a plane containing the origian O and parallel to two non-collinear
vectors $O P$ and $O Q$
B. the surface of a sphere described on PQ as its diameter
C. a line passing through points $P$ and $Q$
D. a set of lines parallel to line PQ

## Answer: c

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10. Two adjacent sides of a parallelogram $A B C D$ are $2 \hat{i}+4 \hat{j}-5 \hat{k}$ and $\hat{i}+2 \hat{j}+3 \hat{k}$. Then the value of $|A C \times B D|$ is a. $20 \sqrt{5}$ b. $22 \sqrt{5}$ c. $24 \sqrt{5}$ d. $26 \sqrt{5}$
A. $20 \sqrt{5}$
B. $22 \sqrt{5}$
C. $24 \sqrt{5}$
D. $26 \sqrt{5}$

## Answer: b

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11. If $\hat{a}, \hat{b}$, and $\hat{c}$ are three unit vectors inclined to each other at angle $\theta$, then the maximum value of $\theta$ is $\frac{\pi}{3}$ b. $\frac{\pi}{4}$ c. $\frac{2 \pi}{3}$ d. $\frac{5 \pi}{6}$
A. $\frac{\pi}{3}$
B. $\frac{\pi}{2}$
C. $\frac{2 \pi}{3}$
D. $\frac{5 \pi}{5}$

## Answer: c

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12. Let the pairs $a, b$, and $c, d$ each determine a plane. Then the planes are parallel if a. $(\vec{a} \times \vec{c}) \times(\vec{b} \times \vec{d})=\overrightarrow{0} \quad$ b. $\quad(\vec{a} \times \vec{c}) \cdot(\vec{b} \times \vec{d})=\overrightarrow{0} \quad$ c. $(\vec{a} \times \vec{b}) \times(\vec{c} \times \vec{d})=\overrightarrow{0}$ d. $(\vec{a} \times \vec{b}) \cdot(\vec{c} \times \vec{d})=\overrightarrow{0}$
A. $(\vec{a} \times \vec{c}) \times(\vec{b} \times \vec{d})=\overrightarrow{0}$
B. $(\vec{a} \times \vec{c}) \cdot(\vec{b} \times \vec{d})=\overrightarrow{0}$
C. $(\vec{a} \times \vec{b}) \times(\vec{c} \times \vec{d})=\overrightarrow{0}$
D. $(\vec{a} \times \vec{c}) \cdot(\vec{c} \times \vec{d})=\overrightarrow{0}$

## Answer: c

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13. If $\vec{r}$. $\vec{a}=\vec{r} \cdot \vec{b}=\vec{r} . \vec{c}=0$ where $\vec{a}, \vec{b}$ and $\vec{c}$ are non-coplanar, then
A. $\vec{r} \perp(\vec{c} \times \vec{a})$
B. $\vec{r} \perp(\vec{a} \times \vec{b})$
C. $\vec{r} \perp(\vec{b} \times \vec{c})$
D. $\vec{r}=\overrightarrow{0}$

## Answer: d

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14. If $\vec{a}$ satisfies $\vec{a} \times(\hat{i}+2 \hat{j}+\hat{k})=\hat{i}-\hat{k}$ then $\vec{a}$ is equal to
A. $\lambda \hat{i}+(2 \lambda-1) \hat{j}+\lambda \hat{k}, \lambda \in R$
B. $\lambda \hat{i}+(1-2 \lambda) \hat{j}+\lambda \hat{k}, \lambda \in R$
C. $\lambda \hat{i}+(2 \lambda+1) \hat{j}+\lambda \hat{k}, \lambda \in R$
D. $\lambda \hat{i}+(1+2 \lambda) \hat{j}+\lambda \hat{k}, \lambda \in R$

## Answer: c

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15. Vectors $3 \vec{a}-5 \vec{b}$ and $2 \vec{a}+\vec{b}$ are mutually perpendicular. If $\vec{a}+4 \vec{b}$ and
$\vec{b}-\vec{a}$ are also mutually perpendicular, then the cosine of the angle
between $a$ and $b$ is a. $\frac{19}{5 \sqrt{43}}$ b. $\frac{19}{3 \sqrt{43}}$ c. $\frac{19}{2 \sqrt{45}}$ d. $\frac{19}{6 \sqrt{43}}$
A. $\frac{19}{5 \sqrt{43}}$
B. $\frac{19}{3 \sqrt{43}}$
C. $\frac{19}{\sqrt{45}}$
D. $\frac{19}{6 \sqrt{43}}$

## Answer: a

16. The unit vector orthogonal to vector $-\hat{i}+\hat{j}+2 \hat{k}$ and making equal angles with the $x$ and $y$-axis a. $\pm \frac{1}{3}(2 \hat{i}+2 \hat{j}-\hat{k})$ b. $\pm \frac{1}{3}(\hat{i}+\hat{j}-\hat{k})$ C. $\pm \frac{1}{3}(2 \hat{i}-2 \hat{j}-\hat{k}) \mathrm{d}$. none of these
A. $\pm \frac{1}{3}(2 \hat{i}+2 \hat{j}-\hat{k})$
B. $\frac{19}{5 \sqrt{43}}$
C. $\pm \frac{1}{3}(\hat{i}+\hat{j}-\hat{k})$
D. none of these

## Answer: a

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17. The value of $x$ for which the angle between $\vec{a}=2 x^{2} \hat{i}+4 x \hat{j}+\hat{k}$ and $\vec{b}=7 \hat{i}-2 \hat{j}+\hat{k}$ is obtuse and the angle between $b$ and the z -axis acute and less than $\pi / 6$ is given by

$$
\text { A. } a<x<1 / 2
$$

B. $1 / 2<x<15$
C. $x<1 / 2$ or $x<0$
D. none of these

## Answer: b

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18. If vectors $\vec{a} a n d \vec{b}$ are two adjacent sides of a parallelogram, then the vector respresenting the altitude of the parallelogram which is the perpendicular to $a$ is a. $\vec{b}+\frac{\vec{b} \times \vec{a}}{|\vec{a}|^{2}}$ b. $\frac{\vec{a} \vec{b}}{|\vec{b}|^{2}}$ c. $\vec{b}-\frac{\vec{b} \vec{a}}{|\vec{a}|^{2}}$ d. $\frac{\vec{a} \times(\vec{b} \times \vec{a})}{|\vec{b}|^{2}}$
A. $\vec{b}+\frac{\vec{b} \times \vec{a}}{|\vec{a}|^{2}}$
B. $\frac{\vec{a} . \vec{b}}{}$
$|\vec{b}|^{2}$
C. $\vec{b}-\frac{\vec{b} \cdot \vec{a}}{|\vec{a}|^{2}} \vec{a}$
$\vec{a} \times(\vec{b} \times \vec{a})$
D.

$$
|\vec{b}|^{2}
$$

## Answer: a

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19. A parallelogram is constructed on $2 \vec{a}+\vec{b}$ and $\vec{a}-4 \vec{b}$, where $|\vec{a}|=6$ and $|\vec{b}|=8$, and $\vec{a}$ and $\vec{b}$ are anti-parallel. Then the length of the longer diagonal is 40 b .64 c .32 d .48
A. 40
B. 64
C. 32
D. 48

## Answer: c

20. Let $\vec{a} \vec{b}=0$, where $\vec{a} a n d \vec{b}$ are unit vectors and the unit vector $\vec{c}$ is inclined at an angle $\theta$ to both $\vec{a} a n d \vec{b}$ If $\vec{c}=m \vec{a}+n \vec{b}+p(\vec{a} \times \vec{b}),(m, n, p \in R)$, then $\frac{\pi}{4} \leq \theta \leq \frac{\pi}{4}$ b. $\frac{\pi}{4} \leq \theta \leq \frac{3 \pi}{4}$ c. $0 \leq \theta \leq \frac{\pi}{4}$ d. $0 \leq \theta \leq \frac{3 \pi}{4}$
A. $\frac{\pi}{4} \leq \theta \leq \frac{\pi}{4}$
B. $\frac{\pi}{4} \leq \theta \leq \frac{3 \pi}{4}$
C. $0 \leq \theta \leq \frac{\pi}{4}$
D. $0 \leq \theta \leq \frac{3 \pi}{4}$

## Answer: a

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21. If $a$ and $c$ are unit vectors and $|b|=4$. The angel between aandc is $\cos ^{-1}(1 / 4) a n d a \times b=2 a \times c$ then, $b-2 c=\lambda a$ The value of $\lambda$ is
A. 3,-4
B. 1/4,3/4
C. $-3,4$
D. $-1 / 4, \frac{3}{4}$

## Answer: a

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22. Let the position vectors of the points PandQ be $4 \hat{i}+\hat{j}+\lambda \hat{k}$ and $2 \hat{i}-\hat{j}+\lambda \hat{k}$, respectively. Vector $\hat{i}-\hat{j}+6 \hat{k}$ is perpendicular to the plane containing the origin and the points PandQ. Then $\lambda$ equals a $-1 / 2 \mathrm{~b} .1 / 2 \mathrm{c} .1 \mathrm{~d}$. none of these
A. $-1 / 2$
B. $1 / 2$
C. 1
D. none of these

Answer: a

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23. A vector of magnitude $\sqrt{2}$ coplanar with the vector $\vec{a}=\hat{i}+\hat{j}+2 \hat{k}$ and $\vec{b}=\hat{i}+2 \hat{j}+\hat{k}, \quad$ and perpendicular to the vector $\vec{c}=\hat{i}+\hat{j}+\hat{k}, \quad$ is a. $-\hat{j}+\hat{k} \mathrm{~b} . \hat{i}-\hat{k} \mathrm{c} . \hat{i}-\hat{j} \mathrm{~d} . \hat{i}-\hat{j}$
A. $-\hat{j}+\hat{k}$
B. $\hat{i}$ and $\hat{k}$
C. $\hat{i}-\hat{k}$
D. hati- hatj'

Answer: a

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24. Let $P$ be a point interior to the acute triangle $A B C$ If $P A+P B+P C$ is a null vector, then w.r.t traingel $A B C$, point $P$ is its $a$. centroid b . orthocentre c. incentre d. circumcentre
A. centroid
B. orthocentre
C. incentre
D. circumcentre

## Answer: a

## - Watch Video Solution

25. $G$ is the centroid of triangle $A B C$ and $A_{1}$ and $B_{1}$ are the midpoints of sides $A B$ and $A C$, respectively. If $\Delta_{1}$ is the area of quadrilateral $G A_{1} A B_{1}$ and $\Delta$ is the area of triangle $A B C$, then $\frac{\Delta}{\Delta_{1}}$ is equal to
a. $\frac{3}{2}$
b. 3
c. $\frac{1}{3}$
d. none of these
A. $\frac{3}{2}$
B. 3
C. $\frac{1}{3}$
D. none of these

Answer: b

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26. Points $\vec{a}, \vec{b}, \vec{c}$, and $\vec{d}$ are coplanar and $(s \in \alpha) \vec{a}+(2 \sin 2 \beta) \vec{b}+(3 \sin 3 \gamma) \vec{c}-\vec{d}=0$. Then the least value of $\sin ^{2} \alpha+\sin ^{2} 2 \beta+\sin ^{2} 3$ yis $\frac{1}{14}$ b. 14 c. 6 d. $1 / \sqrt{6}$
A. $1 / 14$
B. 14
C. 6
D. $1 / \sqrt{6}$

## Answer: a

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27. If $\vec{a} a n d \vec{b}$ are any two vectors of magnitudes 1 and 2 , respectively, and $(1-3 \vec{a} \cdot \vec{b})^{2}+|2 \vec{a}+\vec{b}+3(\vec{a} \times \vec{b})|^{2}=47$, then the angel between $\vec{a}$ and $\vec{b}$ is $\pi / 3 \mathrm{~b} \cdot \pi-\cos ^{-1}(1 / 4) \mathrm{c} \cdot \frac{2 \pi}{3} \mathrm{~d} \cdot \cos ^{-1}(1 / 4)$
A. $\pi / 3$
B. $\pi-\cos ^{-1}(1 / 4)$
C. $\frac{2 \pi}{3}$
D. $\cos ^{-1}(1 / 4)$

## Answer: c

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28. If $\vec{a}$ and $\vec{b}$ are any two vectors of magnitudes 2 and 3 , respectively, such that $|2(\vec{a} \times \vec{b})|+|3(\vec{a} \cdot \vec{b})|=k$, then the maximum value of $k$ is a. $\sqrt{13}$ b. $2 \sqrt{13}$ c. $6 \sqrt{13}$ d. $10 \sqrt{13}$
A. $\sqrt{13}$
B. $2 \sqrt{13}$
C. $6 \sqrt{13}$
D. $10 \sqrt{13}$

## Answer: c

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29. $\vec{a}, \vec{b}$ and $\vec{c}$ are unit vecrtors such that $|\vec{a}+\vec{b}+3 \vec{c}|=4$ Angle between $\vec{a}$ and $\vec{b}$ is $\theta_{1}$, between $\vec{b}$ and $\vec{c}$ is $\theta_{2}$ and between $\vec{a}$ and $\vec{c}$ varies $[\pi / 6,2 \pi / 3]$. Then the maximum value of $\cos \theta_{1}+3 \cos \theta_{2}$ is
A. A. 3
B. B. 4
C. C. $2 \sqrt{2}$
D. D. 6

## Answer: b

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30. If the vector product of a constant vector $\vec{O} A$ with a variable vector $\vec{O} B$ in a fixed plane $O A B$ be a constant vector, then the locus of $B$ is a straight line perpendicular to $\overrightarrow{O A}$ b. a circle with centre $O$ and radius equal to $|\vec{O} A|$ c. a straight line parallel to $\vec{O} A$ d. none of these
A. a straight line perpendicular to $O A$
B. a circle with centre $O$ and radius equal to $|\overrightarrow{O A}|$
C. a striaght line parallel to $O A$
D. none of these

## Answer: c

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31. Let $\vec{u}, \vec{v}$ and $\vec{w}$ be such that $|\vec{u}|=1,|\vec{v}|=2$ and $|\vec{w}|=3$. If the projection of $\vec{v}$ along $\vec{u}$ is equal to that of $\vec{w}$ along $\vec{u}$ and vectors $\vec{v}$ and $\vec{w}$ are perpendicular to each other, then $|\vec{u}-\vec{v}+\vec{w}|$ equals 2 b. $\sqrt{7}$ c. $\sqrt{14}$ d. 14
A. 2
B. $\sqrt{7}$
C. $\sqrt{14}$
D. 14

## Answer: c

## D Watch Video Solution

32. If $\vec{a}, \vec{b}$ and $\vec{c}$ be three non-coplanar vectors and $\mathrm{a}^{\prime}, \mathrm{b}$ ' and $\mathrm{c}^{\prime}$ constitute the reciprocal system of vectors, then prove that
i. $\vec{r}=\left(\vec{r} \cdot \vec{a}^{\prime}\right) \vec{a}+\left(\vec{r} \cdot \vec{b}^{\prime}\right) \vec{b}+\left(\vec{r} \cdot \vec{c}^{\prime}\right) \vec{c}$
ii. $\vec{r}=(\vec{r} \cdot \vec{a}) \vec{a}^{\prime}+(\vec{r} \cdot \vec{b}) \vec{b}^{\prime}+(\vec{r} \cdot \vec{c}) \vec{c}^{\prime}$
A. $-\cos ^{-1}\left(\frac{19}{5 \sqrt{43}}\right)$
B. $\cos ^{-1}\left(\frac{19}{5 \sqrt{43}}\right)$
C. $\pi \cos ^{-1}\left(\frac{19}{5 \sqrt{43}}\right)$
D. cannot of these

## Answer: b

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33. if $\left.\vec{\alpha}|\mid(\vec{\beta} \times \vec{\gamma})$, then $(\vec{\alpha} \times \beta) \cdot(\vec{\alpha} \times \vec{\gamma})$ equals to a. $| \vec{\alpha}\right|^{2}(\vec{\beta} \cdot \vec{\gamma})$ b.
$|\vec{\beta}|^{2}(\vec{\gamma} \cdot \vec{\alpha})$ c. $|\vec{\gamma}|^{2}(\vec{\alpha} \cdot \vec{\beta})$ d. $|\vec{\alpha}||\vec{\beta}||\vec{\gamma}|$
A. $|\vec{\alpha}|^{2}(\vec{\beta} \cdot \vec{\gamma})$
B. $|\vec{\beta}|^{2}(\vec{\gamma} \cdot \vec{\alpha})$
C. $|\vec{\gamma}|^{2}(\vec{\alpha} \cdot \vec{\beta})$
D. $|\vec{\alpha}||\vec{\beta}||\vec{\gamma}|$

## Answer: a

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34. The position vectors of points $A, B$ and $C$ are $\hat{i}+\hat{j}+\hat{k}, \hat{i}+5 \hat{j}-\hat{k}$ and $2 \hat{i}+3 \hat{j}+5 \hat{k}$, respectively the greatest angle of triangle $A B C$ is
A. A. $120^{\circ}$
B. B. $90^{\circ}$
C. C. $\cos ^{-1}(3 / 4)$
D. D. none of these

## D Watch Video Solution

35. Given three vectors $\vec{a}, \vec{b}$, and $\vec{c}$ two of which are non-collinear. Further if $(\vec{a}+\vec{b})$ is collinear with $\vec{c},(\vec{b}+\vec{c})$ is collinear with $\vec{a},|\vec{a}|=|\vec{b}|=|\vec{c}|=\sqrt{2}$ Find the value of $\vec{a} \cdot \vec{b}+\vec{b} \cdot \vec{c}+\vec{c} \cdot \vec{a}$ a. $3 \mathrm{~b} .-3 \mathrm{c} .0 \mathrm{~d}$. cannot be evaluated
A. 3
B. -3
C. 0
D. cannot of these

## Answer: b

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36. If $\vec{a}$ and $\vec{b}$ are unit vectors such that $(\vec{a}+\vec{b}) \cdot[(2 \vec{a}+3 \vec{b}) \times(3 \vec{a}-2 \vec{b})]=0$, then angle between $\vec{a}$ and $\vec{b}$ is
A. 0
B. $\pi / 2$
C. $\pi$
D. indeterminate

## Answer: d

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37. If in a right-angled triangle $A B C$, the hypotenuse
$A B=p$, then $\overrightarrow{A B A} \dot{C}+\vec{B} C \vec{B} A+\vec{C} A \vec{C} B$ is equal to $2 p^{2}$ b. $\frac{p^{2}}{2}$ c. $p^{2}$ d. none of these
A. $2 p^{2}$
B. $\frac{p^{2}}{2}$
C. $p^{2}$
D. none of these

## Answer: c

## - Watch Video Solution

38. Resolved part of vector $\vec{a}$ and along vector $\vec{b}$ is $\vec{a}_{1}$ and that prependicular to $\vec{b}$ is $\vec{a}_{2}$ then $\vec{a}_{1} \times \vec{a}_{2}$ is equal to
A. $\frac{(\vec{a} \times \vec{b}) \cdot \vec{b}}{|\vec{b}|^{2}}$
B. $\frac{(\vec{a} . \vec{b}) \vec{a}}{}$
$|\vec{a}|^{2}$
c. $\frac{(\vec{a} \cdot \vec{b})(\vec{b} \times \vec{a})}{}$
$|\vec{b}|^{2}$
D. $\frac{(\vec{a} \cdot \vec{b})(\vec{b} \times \vec{a})}{}$

$$
|\vec{b} \times \vec{a}|
$$

## Answer: c

## - Watch Video Solution

39. $\vec{a}=2 \hat{i}-\hat{j}+\hat{k}, \vec{b}=\hat{i}+2 \hat{j}-\hat{k}, \vec{c}=\hat{i}+\hat{j}-2 \hat{k}$ A vector coplanar with $\vec{b}$ and $\vec{c}$ whose projectin on $\vec{a}$ is magnitude $\sqrt{\frac{2}{3}}$ is $2 \hat{i}+3 \hat{j}-3 \hat{k}$ b. $-2 \hat{i}-\hat{j}+5 \hat{k}$ c. $2 \hat{i}+3 \hat{j}+3 \hat{k}$ d. $2 \hat{i}+\hat{j}+5 \hat{k}$
A. $2 \hat{i}+3 \hat{j}-3 \hat{k}$
B. $-2 \hat{i}-\hat{j}+5 \hat{k}$
C. $2 \hat{i}+3 \hat{j}+3 \hat{k}$
D. $2 \hat{i}+\hat{j}+5 \hat{k}$

## Answer: b

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40. If $P$ is any arbitrary point on the circumcircle of the equilateral triangle of side length $l$ units, then $|\vec{P} A|^{2}+|\vec{P} B|^{2}+|\vec{P} C|^{2}$ is always equal to $2 l^{2}$ b. $2 \sqrt{3} l^{2}$ c. $l^{2}$ d. $3 l^{2}$
A. $2 l^{2}$
B. $2 \sqrt{3} l^{2}$
C. $l^{2}$
D. $3 l^{2}$

## Answer: a

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41. If $\vec{r}$ and $\vec{s}$ are non-zero constant vectors and the scalar $b$ is chosen such that $|\vec{r}+b \vec{s}|$ is minimum, then the value of $|b \vec{s}|^{2}+|\vec{r}+b \vec{s}|^{2}$ is equal to 2| $|\vec{r}|^{2}$ b. $|\vec{r}|^{2} / 2$ c. $3|\vec{r}|^{2}$ d. $|r|^{2}$
A. $2|\vec{r}|^{2}$
B. $|\vec{r}|^{2 / 2}$
C. $3|\vec{r}|^{2}$
D. $|\vec{r}|^{2}$

## Answer: d

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42. $\vec{a} a n d \vec{b}$ are two unit vectors that are mutually perpendicular. A unit vector that is equally inclined to $\vec{a}$, $\vec{b}$ and $\vec{a} \times \vec{b}$ is $\frac{1}{\sqrt{2}}(\vec{a}+\vec{b}+\vec{a} \times \vec{b})$ b. $\frac{1}{2}(\vec{a} \times \vec{b}+\vec{a}+\vec{b})$ c. $\frac{1}{\sqrt{3}}(\vec{a}+\vec{b}+\vec{a} \times \vec{b})$ d. $\frac{1}{3}(\vec{a}+\vec{b}+\vec{a} \times \vec{b})$
A. $\frac{1}{\sqrt{2}}(\vec{a}+\vec{b}+\vec{a} \times \vec{b})$
B. $\frac{1}{2}(\vec{a} \times \vec{b}+\vec{a}+\vec{b})$
C. $\frac{1}{\sqrt{3}}(\vec{a}+\vec{b}+\vec{a} \times \vec{b})$
D. $\frac{1}{3}(\vec{a}+\vec{b}+\vec{a} \times \vec{b})$

## Answer: a

## (D) Watch Video Solution

43. Given that $\vec{a}, \vec{b}, \vec{p}, \vec{q}$ are four vectors such that
$\vec{a}+\vec{b}=\mu \vec{p}, \vec{b} \vec{q}=\operatorname{Oand}(\vec{b})^{2}=1$, where $\mu$ is a scalar. Then $|(\vec{a} \vec{q}) \vec{p}-(\vec{p} \vec{q}) \vec{a}|$
is equal to $2|\vec{p} \vec{q}|$ b. (1/2) $|\vec{p} \vec{q}|$ c. $|\vec{p} \times \vec{q}|$ d. $|\vec{p} \vec{q}|$
A. $2|\vec{p} \vec{q}|$
B. $(1 / 2)|\vec{p} \cdot \vec{q}|$
C. $|\vec{p} \times \vec{q}|$
D. $|\vec{p} . \vec{q}|$

## Answer: d

44. The position vectors of the vertices $A$, BandC of a triangle are three unit vectors $\vec{a}, \vec{b}$, and $\vec{c}$, respectively. A vector $\vec{d}$ is such that $\vec{d} \cdot \vec{a}=\vec{d} \cdot \vec{b}=\vec{d} \cdot \vec{c}$ and $\vec{d}=\lambda(\vec{b}+\vec{c})$ Then triangle $A B C$ is a. acute angled b. obtuse angled c. right angled d. none of these
A. acute angled
B. obtuse angled
C. right angled
D. none of these

## Answer: a

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45. If $a$ is real constant $A, B$ and $C$ are variable angles and $\sqrt{a^{2}-4} \tan A+a \tan B+\sqrt{a^{2}+4} \tan C=6 a$, then the least value of $\tan ^{2} A+\tan ^{2} B+\tan ^{2} C$ is a. 6 b. 10 c. 12 d. 3
A. 6
B. 10
C. 12
D. 3

## Answer: d

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46. The vertex $A$ triangle $A B C$ is on the line $\vec{r}=\hat{i}+\hat{j}+\lambda \hat{k}$ and the vertices

BandC have respective position vectors $\hat{i} a n d \hat{j}$ Let $\Delta$ be the area of the triangle and $\Delta[3 / 2, \sqrt{33} / 2]$. Then the range of values of $\lambda$ corresponding to $A$ is a. $[-8,4] \cup[4,8]$ b. $[-4,4]$ c. $[-2,2]$ d. $[-4,-2] \cup[2,4]$
A. $[-8,-4]$ cup $[4,8]^{`}$
B. $[-4,4]$
C. $[-2,2]$
D. $[-4,-2] \cup[2,4]$

## Answer: c

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47. A non-zero vector $\vec{a}$ is such that its projections along vectors
$\frac{\hat{i}+\hat{j}}{\sqrt{2}}, \frac{-\hat{i}+\hat{j}}{\sqrt{2}}$ and $\hat{k}$ are equal, then unit vector along $\vec{a}$ is a. $\frac{\sqrt{2} \hat{j}-\hat{k}}{\sqrt{3}}$ b.
$\frac{\hat{j}-\sqrt{2} \hat{k}}{\sqrt{3}}$ c. $\frac{\sqrt{2}}{\sqrt{3}} \hat{j}+\frac{\hat{k}}{\sqrt{3}}$ d. $\frac{\hat{j}-\hat{k}}{\sqrt{2}}$
$\sqrt{2} \hat{j}-\hat{k}$
A. $\frac{\sqrt{3}}{\sqrt{3}}$
$\hat{j}-\sqrt{2} \hat{k}$
B. $\frac{\sqrt{3}}{\sqrt{2}}$
C. $\frac{\sqrt{2}}{\sqrt{3}} \hat{j}+\frac{\hat{k}}{\sqrt{3}}$
D. $\frac{\hat{j}-\hat{k}}{\sqrt{2}}$

## Answer: a

48. Position vector $\hat{k}$ is rotated about the origin by angle $135^{\circ}$ in such a way that the plane made by it bisects the angle between $\hat{i}$ and $\hat{j}$. Then its new position is
A. $\pm \frac{\hat{i}}{\sqrt{2}} \pm \frac{\hat{j}}{\sqrt{2}}$
B. $\pm \frac{\hat{i}}{2} \pm \frac{\hat{j}}{2}-\frac{\hat{k}}{\sqrt{2}}$
C. $\frac{\hat{i}}{\sqrt{2}}-\frac{\hat{k}}{\sqrt{2}}$
D. none of these

## Answer: d

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49. In a quadrilateral $A B C D, \vec{A} C$ is the bisector of $\vec{A} B a n d \vec{A} D$, angle between $\vec{A} B$ and $\vec{A} D$ is $2 \pi / 3,15|\vec{A} C|=3|\vec{A} B|=5|\vec{A} D|$ Then the angle
between $\vec{B} A a n d \vec{C} D$ is $(a) \cos ^{-1}\left(\frac{\sqrt{14}}{7 \sqrt{2}}\right)$
b. $\cos ^{-1}\left(\frac{\sqrt{21}}{7 \sqrt{3}}\right)$ c. $\cos ^{-1}\left(\frac{2}{\sqrt{7}}\right)$ d.
$\cos ^{-1}\left(\frac{2 \sqrt{7}}{14}\right)$
A. $\cos ^{-1} \frac{\sqrt{14}}{7 \sqrt{2}}$
B. $\cos ^{-1} \frac{\sqrt{21}}{7 \sqrt{3}}$
C. $\cos ^{-1} \frac{2}{\sqrt{7}}$
D. $\cos ^{-1} \frac{2 \sqrt{7}}{14}$

## Answer: c

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50. In fig. $A B, D E a n d G F$ are parallel to each other and $A D, B G a n d E F$ are parallel to each other. If $C D: C E=C G: C B=2: 1$, then the value of area (AEG): area (ABD) is equal to $7 / 2$ b. 3 c. 4 d. $9 / 2$
B. 3
C. 4
D. $9 / 2$

## Answer: b

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51. Vector $\vec{a}$ in the plane of $\vec{b}=2 \hat{i}+\hat{j}$ and $\vec{c}=\hat{i}-\hat{j}+\hat{k}$ is such that it equally inclined to $\vec{b}$ and $\vec{d}$ where $\vec{d}=\hat{j}+2 \hat{k}$ The value of $\vec{a}$ is $\frac{\hat{i}+\hat{j}+\hat{k}}{\sqrt{2}}$ b. $\frac{\hat{i}-\hat{j}+\hat{k}}{\sqrt{3}}$ c. $\frac{2 \hat{i}+\hat{j}}{\sqrt{5}}$ d. $\frac{2 \hat{i}+\hat{j}}{\sqrt{5}}$
A. $\frac{\hat{i}+\hat{j}+\hat{k}}{\sqrt{3}}$
B. $\frac{\hat{i}-\hat{j}+\hat{k}}{\sqrt{3}}$
C. $\frac{2 \hat{i}+\hat{j}}{\sqrt{5}}$
D. $\frac{2 \hat{i}+\hat{j}}{\sqrt{5}}$

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52. Let $A B C D$ be a tetrahedron such that the edges $A B, A C$ and $A D$ are mutually perpendicular. Let the area of triangles $A B C, A C D$ and $A D B$ be 3,4 and 5 sq. units, respectively. Then the area of triangle $B C D$ is
a. $5 \sqrt{2}$
b. 5
c. $\frac{\sqrt{5}}{2}$
d. $\frac{5}{2}$
A. $5 \sqrt{2}$
B. 5
C. $\frac{\sqrt{5}}{2}$
D. $\frac{5}{2}$

## Answer: a

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53. Let $f(t)=[t] \hat{i}+(t-[t]) \hat{j}+[t+1] \hat{k}$, where[.] denotes the greatest integer
function. Then the vectors $f\left(\frac{5}{4}\right) \operatorname{andf}(t), 0<t<1$ are(a) parallel to each other(b) perpendicular(c) inclined at $\cos ^{-1} 2\left(\sqrt{7\left(1-t^{2}\right)}\right)$ (d)inclined at $\cos ^{-1}\left(\frac{8+t}{\sqrt{1+t^{2}}}\right) ;$
A. parallel to each other
B. perpendicular to each other
C. inclined at $\xrightarrow{\cos ^{-1} 2}$

$$
\sqrt{7}\left(1-t^{2}\right)
$$

D. inclined at $\frac{\cos ^{-1}(8+t)}{9 \sqrt{1+t^{2}}}$

## Answer: d

## - Watch Video Solution

54. If $\vec{a}$ is parallel to $\vec{b} \times \vec{c}$, then $(\vec{a} \times \vec{b}) \cdot(\vec{a} \times \vec{c})$ is equal to a. $|\vec{a}|^{2}(\vec{b} \cdot \vec{c})$ b. $|\vec{b}|^{2}(\vec{a} . \vec{c})$ c. $|\vec{c}|^{2}(\vec{a} \cdot \vec{b})$ d. none of these
A. $|\vec{a}|^{2}(\vec{b} . \vec{c})$
B. $|\vec{b}|^{2}(\vec{a} \cdot \vec{c})$
C. $|\vec{c}|^{2}(\vec{a} . \vec{b})$
D. none of these

## Answer: a

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55. The three vectors $\hat{i}+\hat{j}, \hat{j}+\hat{k}, \hat{k}+\hat{i}$ taken two at a time form three planes, The three unit vectors drawn perpendicular to these planes form a parallelopiped of volume: $\qquad$
A. $1 / 3$
B. 4
C. $(3 \sqrt{3}) / 4$
D. $4 \sqrt{3}$

## Answer: d

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56. If $\vec{d}=\vec{a} \times \vec{b}+\vec{b} \times \vec{c}+\vec{c} \times \vec{a}$ is non-zero vector and
$|(\vec{d} \cdot \vec{c})(\vec{a} \times \vec{b})+(\vec{d} \cdot \vec{a})(\vec{b} \times \vec{c})+(\vec{d} \cdot \vec{b})(\vec{c} \times \vec{a})|=0$, then
a. $|\vec{a}|=|\vec{b}|=|\vec{c}|$
b. $|\vec{a}|+|\vec{b}|+|\vec{c}|=|d|$
c. $\vec{a}, \vec{b}$, and $\vec{c}$ are coplanar
d. none of these
A. $|\vec{a}|=|\vec{b}|=|\vec{c}|$
B. $|\vec{a}|+|\vec{b}|+|\vec{c}|=|\vec{d}|$
C. $\vec{a}, \vec{b}$ and $\vec{c}$ are coplanar
D. none of these

## Answer: c

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57. 

$|\vec{a}|=2$ and $|\vec{b}|=3$ and $\vec{a} \cdot \vec{b}=0$, then $|(\vec{a} \times(\vec{a} \times(\vec{a} \times(\vec{a} \times \vec{b}))))|$
A. $48 \hat{b}$
B. $-48 \hat{b}$
C. 48 â
D. $-48 \hat{a}$

## Answer: a

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58. If the two diagonals of one its faces are $6 \hat{i}+6 \hat{k} a n d 4 \hat{j}+2 \hat{k}$ and of the edges not containing the given diagonals is $c=4 \hat{j}-8 \hat{k}$, then the volume
of a parallelepiped is a. 60 b .80 c .100 d .120
A. 60
B. 80
C. 100
D. 120

## Answer: d

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59. The volume of a tetrahedron formed by the coterminous edges $\vec{a}, \vec{b}$, and $\vec{c}$ is 3 . Then the volume of the parallelepiped formed by the coterminous edges $\vec{a}+\vec{b}, \vec{b}+\vec{c}$ and $\vec{c}+\vec{a}$ is 6 b .18 c .36 d .9
A. 6
B. 18
C. 36
D. 9

Answer: c

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60. If $\vec{a}, \vec{b}$, and $\vec{c}$ are three mutually orthogonal unit vectors, then the triple product $[\vec{a}+\vec{b}+\vec{c} \vec{a}+\vec{b} \vec{b}+\vec{c}]$ equals: (a.) 0 (b.) 1 or -1 (c.) 6 (d.) 3
A. 0
B. 1 or - 1
C. 1
D. 3

Answer: b
61. Vector $\vec{c}$ is perpendicular to vectors $\vec{a}=(2,-3,1) \operatorname{and} \vec{b}=(1,-2,3)$ and satisfies the condition $\vec{x} \cdot(\hat{i}+2 \hat{j}-7 \hat{k})=10$. Then vector $\vec{c}$ is equal to a. $(7,5,1)$ b. $-7,-5,-1$ c. $1,1,-1$ d. none of these
A. 7,5,1
B. $(-7,-5,-1)$
C. 1,1,-1
D. none of these

## Answer: a

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62. Given $\vec{a}=x \hat{i}+y \hat{j}+2 \hat{k}, \vec{b}=\hat{i}-\hat{j}+\hat{k}, \vec{c}=\hat{i}+2 \hat{j}, \vec{a} \perp \vec{b}, \vec{a} . \vec{c}=4$ then find the value of $\left[\begin{array}{lll}\vec{a} & \vec{b} & \vec{c}\end{array}\right]$.
A. A. $[\vec{a} \vec{b} \vec{c}]^{2}=|\vec{a}|$
B. B. $[\vec{a} \vec{b} \vec{c}]=|\vec{a}|$
C. C. $[\vec{a} \vec{b} \vec{c}]=0$
D. D. $[\vec{a} \vec{b} \vec{c}]=|\vec{a}|^{2}$

## Answer: d

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63. Let $\vec{a}=a_{1} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}, \vec{b}=b_{1} \hat{i}+b_{2} \hat{j}+b_{3} \hat{k}$ and $\vec{c}=c_{1} \hat{i}+c_{2} \hat{j}+c_{3} \hat{k}$ be three non-zero vectors such that $\vec{c}$ is a unit vector perpendicular to both $\vec{a}$ and $\vec{b}$. If the angle between $\vec{a}$ and $\vec{b}$ is t/6 then the value of

$$
\left|\begin{array}{lll}
a_{1} & b_{1} & c_{1} \\
a_{2} & b_{2} & c_{2} \\
a_{3} & b_{3} & c_{3}
\end{array}\right| \text { is }
$$

A. 0
B. 1
C. $\frac{1}{4}\left(a_{1}^{2}+a_{2}^{2}+a_{3}^{2}\right)\left(b_{1}^{2}+b_{2}^{2}+b_{3}^{2}\right)$
D. $\frac{3}{4}\left(a_{1}^{2}+a_{2}^{2}+a_{3}^{2}\right)\left(b_{1}^{2}+b_{2}^{2}+b_{3}^{2}\right)$

## Answer: c

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64. Let $\vec{r}, \vec{a}, \vec{b}$ and $\vec{c}$ be four non-zero vectors such that $\vec{r} \cdot \vec{a}=0,|\vec{r} \times \vec{b}|=|\vec{r}||\vec{b}|,|\vec{r} \times \vec{c}|=|\vec{r}||\vec{c}|$ then
$\left[\begin{array}{lll}\vec{a} & \vec{b} & \vec{c}\end{array}\right]=$
A. $|a||b||c|$
B. $-|a||b||c|$
C. 0
D. none of these

## Answer: c

65. If $\vec{a}, \vec{b}$ and $\vec{c}$ are such that $[\vec{a} \vec{b} \vec{c}]=1, \vec{c}=\lambda(\vec{a} \times \vec{b})$, angle between $\vec{c}$ and $\vec{b}$ is $2 \pi / 3,|\vec{a}|=\sqrt{2},|\vec{b}|=\sqrt{3}$ and $|\vec{c}|=\frac{1}{\sqrt{3}}$ then the angle between $\vec{a}$ and $\vec{b}$ is
A. (a) $\frac{\pi}{6}$
B. (b) $\frac{\pi}{4}$
C. (c) $\frac{\pi}{3}$
D. (d) $\frac{\pi}{2}$

## Answer: b

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66. If $4 \vec{a}+5 \vec{b}+9 \vec{c}=0$, then $(\vec{a} \times \vec{b}) \times[(\vec{b} \times \vec{c}) \times(\vec{c} \times \vec{a})]$ is equal to a. vector perpendicular to the plane of $a, b, c b$. a scalar quantity $c . \overrightarrow{0} \mathrm{~d}$. none of these
A. a vector perpendicular to the plane of $\vec{a}, \vec{b}$ and $\vec{c}$
B. a scalar quantity
C. $\overrightarrow{0}$
D. none of these

## Answer: c

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67. Value of $[\vec{a} \times \vec{b}, \vec{a} \times \vec{c}, \vec{d}]$ is always equal to a. $(\vec{a} \vec{d})[\vec{a} \vec{b} \vec{c}] \mathrm{b}$. $\left(\begin{array}{c}\vec{a} \vec{c}\end{array}\right)[\vec{a} \vec{b} \vec{d}]$ c. $\left(\begin{array}{c}\vec{a} \vec{b}\end{array}\right)[\vec{a} \vec{b} \vec{d}]$ d. none of these
A. $(\vec{a} . \vec{d})[\vec{a} \vec{b} \vec{c}]$
B. `(veca.vecc)[veca verb recd]
C. $(\vec{a} . \vec{b})[\vec{a} \vec{b} \vec{d}]$
D. none of these

## D Watch Video Solution

68. Let $\vec{a} a n d \vec{b}$ be mutually perpendicular unit vectors. Then for any
arbitrary $\vec{r}$,

$$
\vec{r}=(\stackrel{\rightharpoonup}{r} \hat{a}) \hat{a}+(\stackrel{\rightharpoonup}{r} \hat{b}) \hat{b}+(\vec{r} \hat{a} \times \hat{b})(\hat{a} \times \hat{b})
$$

$\vec{r}=(\vec{r} \dot{a})-(\vec{r} \hat{b}) \hat{b}-(\vec{r} \hat{a} \times \hat{b})(\hat{a} \times \hat{b})$
$\vec{r}=(\vec{r} \hat{a}) \hat{a}-(\vec{r} \hat{b}) \hat{b}+(\vec{r} \hat{a} \times \hat{b})(\hat{a} \times \hat{b})$ none of these
A. $\vec{r}=(\vec{r} \cdot \hat{a}) \hat{a}+(\vec{r} \cdot \hat{b}) \hat{b}+(\vec{r} \cdot(\vec{a} \times \hat{b}))(\hat{a} \times \hat{b})$
B. $\vec{r}=(\vec{r} \cdot \hat{a})-(\vec{r} \cdot \hat{b}) \hat{b}-(\vec{r} \cdot(\vec{a} \times \hat{b}))(\hat{a} \times \hat{b})$
C. $\vec{r}=(\vec{r} . \hat{a}) \hat{a}-(\vec{r} \cdot \hat{b}) \hat{b}-(\vec{r} \cdot(\vec{a} \times \hat{b}))(\hat{a} \times \hat{b})$
D. none of these

## Answer: a

69. Let $\vec{a} a n d \vec{b}$ be unit vectors that are perpendicular to each other. Then $[\vec{a}+(\vec{a} \times \vec{b}) \vec{b}+(\vec{a} \times \vec{b}) \vec{a} \times \vec{b}]$ will always be equal to 1 b. 0 c. -1 d. none of these
A. 1
B. 0
C. -1
D. none of these

## Answer: a

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70. $\vec{a}$ and $\vec{b}$ are two vectors such that $|\vec{a}|=1,|\vec{b}|=4$ and $\vec{a}$. $\vec{b}=2$. If $\vec{c}=$ $(2 \vec{a} \times \vec{b})-3 \vec{b}$ then find angle between $\vec{b}$ and $\vec{c}$.
71. If $\vec{b}$ and $\vec{c}$ are unit vectors, then for any arbitary vector $\vec{a},(((\vec{a} \times \vec{b})+(\vec{a} \times \vec{c})) \times(\vec{b} \times \vec{c})) \cdot(\vec{b}-\vec{c})$ is always equal to

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72. If $\vec{a} \cdot \vec{b}=\beta$ and $\vec{a} \times \vec{b}=\vec{c}$, then $\vec{b}$ is
A. $\frac{(\beta \vec{a}-\vec{a} \times \vec{c})}{|\vec{a}|^{2}}$
B. $\frac{(\beta \vec{a}+\vec{a} \times \vec{c})}{|\vec{a}|^{2}}$
C. $\frac{(\beta \vec{c}+\vec{a} \times \vec{c})}{|\vec{a}|^{2}}$
D. $\frac{(\beta \vec{c}+\vec{a} \times \vec{c})}{|\vec{a}|^{2}}$

$$
|\vec{a}|^{2}
$$

## Answer: a

73. If $a(\vec{\alpha} \times \vec{\beta})+b(\vec{\beta} \times \vec{\gamma})+c(\vec{\gamma} \times \vec{\alpha})=0$ and at least one of $a$, bandc is nonzero, then vectors $\vec{\alpha}, \vec{\beta}$ and $\vec{\gamma}$ are a. parallel b. coplanar c. mutually perpendicular d. none of these
A. parallel
B. coplanar
C. mutually perpendicular
D. none of these

## Answer: b

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74. If $(\vec{a} \times \vec{b}) \times(\vec{b} \times \vec{c})=\vec{b}$, where $\vec{a}$, $\vec{b}$, and $\vec{c}$ are nonzero vectors, then 1 . $\vec{a}, \vec{b}$, and $\vec{c}$ can be coplanar 2. $\vec{a}, \vec{b}$, and $\vec{c}$ must be coplanar $3 . \vec{a}, \vec{b}$, and $\vec{c}$ cannot be coplanar 4.none of these
A. $\vec{a}, \vec{b}$ and $\vec{v}$ can be coplanar
B. $\vec{a}, \vec{b}$ and $\vec{c}$ must be coplanar
C. $\vec{a}, \vec{b}$ and $\vec{c}$ cannot be coplanar
D. none of these

## Answer: c

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75. If $\vec{r} \cdot \vec{a}=\vec{r} \cdot \vec{b}=\vec{r} \cdot \vec{c}=\frac{1}{2}$ for some non zero vector $\vec{r}$ and $\vec{a}, \vec{b}, \vec{c}$ are non coplanar, then the area of the triangle whose vertices are $A(\vec{a}), B(\vec{b})$ and $C(\vec{c})$ is
A. $|[\vec{a} \vec{b} \vec{c}]|$
B. $|\vec{r}|$
C. $|[\vec{a} \vec{b} \vec{c}] \vec{r}|$
D. none of these
76. A vector of magnitude 10 along the normal to the curve $3 x^{2}+8 x y+2 y^{2}-3=0$ at its point $P(1,0)$ can be $6 \hat{i}+8 \hat{j}$ b. $-8 \hat{i}+3 \hat{j}$ c. $6 \hat{i}-8 \hat{j}$ d. $8 \hat{i}+6 \hat{j}$
A. $6 \hat{i}+8 \hat{j}$
B. $-8 \hat{i}+3 \hat{j}$
C. $6 \hat{i}-8 \hat{j}$
D. $8 \hat{i}+6 \hat{j}$

## Answer: a

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77. If $\vec{a} a n d \vec{b}$ are two unit vectors incline at angle $\pi / 3$, then
$\{\vec{a} \times(\vec{b}+\vec{a} \times \vec{b})\} \vec{b}$ is equal to $\frac{-3}{4}$ b. $\frac{1}{4}$ c. $\frac{3}{4}$ d. $\frac{1}{2}$
A. $\frac{-3}{4}$
B. $\frac{1}{4}$
C. $\frac{3}{4}$
D. $\frac{1}{2}$

## Answer: a

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78. If $\vec{a}$ and $\vec{b}$ are othogonal unit vectors, then for a vector $\vec{r}$ non coplanar with $\vec{a}$ and $\vec{b}$ vector $\vec{r} \times \vec{a}$ is equal to
A. $[\vec{r} \vec{a} \vec{b}] \vec{b}-(\vec{r} \cdot \vec{b})(\vec{b} \times \vec{a})$
B. $[\vec{r} \vec{a} \vec{b}](\vec{a}+\vec{b})$
C. $[\vec{r} \vec{a} \vec{b}] \vec{a}+(\vec{r} . \vec{a}) \vec{a} \times \vec{b}$
D. none of these

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79. If $\vec{a}, \vec{b}, \vec{c}$ are any three non- coplanar vectors then the equation
$[\vec{b} \times \vec{c} \vec{c} \times \vec{a} \vec{a} \times \vec{b}]^{2}+[\vec{a}+\vec{b} \vec{b}+\vec{c} \vec{c}+\vec{a}] x+1+[\vec{b}-\vec{c} \vec{c}-\vec{a} \vec{a}-\vec{b}]=0$ has roots (A) real and distinct (B) real (C) equal (D) imaginary
A. real and distinct
B. real
C. equal
D. imaginary

## Answer: c

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80. Solve the simultaneous vector equations for
$\vec{x}$ and $\vec{y}: \vec{x}+\vec{c} \times \vec{y}=\vec{a}$ and $\vec{y}+\vec{c} \times \vec{x}=\vec{b}, \vec{c} \neq 0$
A. $\vec{x}=\frac{\vec{b} \times \vec{c}+\vec{a}+(\vec{c} \cdot \vec{a}) \vec{c}}{1+\vec{c} \cdot \vec{c}}$
B. $\vec{x}=\frac{\vec{c} \times \vec{b}+\vec{b}+(\vec{c} \cdot \vec{a}) \vec{c}}{1+\vec{c} \cdot \vec{c}}$
C. $\vec{y}=\frac{1+\vec{c} \cdot \vec{c}}{1+\vec{c}}$
D. none of these

## Answer: b

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81. The condition for equations $\vec{r} \times \vec{a}=\vec{b}$ and $\vec{r} \times \vec{c}=\vec{d}$ to be consistent is
a. $\vec{b} \vec{c}=\vec{a} \vec{d}$ b. $\vec{a} \vec{b}=\vec{c} \vec{d}$ c. $\vec{b} \vec{c}+\vec{a} \vec{d}=0$ d. $\vec{a} \vec{b}+\vec{c} \vec{d}=0$
A. $\vec{b} \cdot \vec{c}=\vec{a} \cdot \vec{d}$
B. $\vec{a} \cdot \vec{b}=\vec{c} \cdot \vec{d}$
C. $\vec{b} \cdot \vec{c}+\vec{a} \cdot \vec{d}=0$
D. $\vec{a} \cdot \vec{b}+\vec{c} \cdot \vec{d}=0$

## Answer: c

## D Watch Video Solution

82. If $\vec{a}=2 \hat{i}+3 \hat{j}+\hat{k}, \vec{b}=\hat{i}-2 \hat{j}+\hat{k}$ and $\vec{c}=-3 \hat{i}+\hat{j}+2 \hat{k}$, then $[\vec{a} \vec{b} \vec{c}]=$

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83. If $\vec{a}=2 \hat{i}+3 \hat{j}+8 \hat{k}$ is perpendicular to $\vec{b}=4 \hat{i}-4 \hat{j}+\alpha \hat{k}$, then find the value of $\alpha$
A. $-\frac{1}{2}$
B. $\frac{1}{2}$
C. 1
D. -1

## Answer: a

84. Let $\vec{a}(x)=(\sin x) \hat{i}+(\cos x) \hat{j}$ and $\vec{b}(x)=(\cos 2 x) \hat{i}+(\sin 2 x) \hat{j}$ be two variable vectors $(x \in R)$. Then $\vec{a}(x)$ and $\vec{b}(x)$ are
A. collinear for unique value of $x$
B. perpendicular for infinte values of x .
C. zero vectors for unique value of x
D. none of these

## Answer: b

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85. 

For
any
vectors
$\vec{a}$ and $\vec{b},(\vec{a} \times \hat{i}) \cdot(\vec{b} \times \hat{i})+(\vec{a} \times \hat{j}) \cdot(\vec{b} \times \hat{j})+(\vec{a} \times \hat{k}) \cdot(\vec{b} \times \hat{k})$ is always equal to
A. A. $\vec{a} . \vec{b}$
B. B. $2 \vec{a} . \vec{b}$
C. C. zero
D. D. none of these

## Answer: b

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86. If $\vec{a}, \vec{b}$ and $\vec{c}$ are three non coplanar vectors and $\vec{r}$ is any vector in space, then
$(\vec{a} \times \vec{b}) \times(\vec{r} \times \vec{c})+(\vec{b} \times \vec{c}) \times(\vec{r} \times \vec{a})+(\vec{c} \times \vec{a}) \times(\vec{r} \times \vec{b})=$
$[\vec{a} \vec{b} \vec{c}]$ (B) $2[\vec{a} \vec{b} \vec{c}] \vec{r}$ (C) $3[\vec{a} \vec{b} \vec{c}] \vec{r}$ (D) $4[\vec{a} \vec{b} \vec{c}] \vec{r}$
A. $[\vec{a} \vec{b} \vec{c}] \vec{r}$
B. $2[\vec{a} \vec{b} \vec{c}] \vec{r}$
C. $3[\vec{a} \vec{b} \vec{c}] \vec{r}$
D. none of these

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 $[\vec{a} \vec{b} \vec{c}] \quad[\vec{a} \vec{b} \vec{c}] \quad[\vec{a} \vec{b} \vec{c}]$
three non- coplanar vectors then the value of the expression $(\vec{a}+\vec{b}+\vec{c}) \cdot(\vec{p}+\vec{q}+\vec{r})$ is
A. 3
B. 2
C. 1
D. 0

## Answer: a

88. $A(\vec{a}), B(\vec{b}), C(\vec{c})$ are the vertices of the triangle ABC and $R(\vec{r})$ is any point in the plane of triangle $A B C$, then $\vec{r} .(\vec{a} \times \vec{b}+\vec{b} \times \vec{c}+\vec{c} \times \vec{a})$ is always equal to
A. zero
B. $[\vec{a} \vec{b} \vec{c}]$
C. $-[\vec{a} \vec{b} \vec{c}]$
D. none of these

## Answer: b

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89. If $\vec{a}, \vec{b}$ and $\vec{c}$ are non-coplanar vectors and $\vec{a} \times \vec{c}$ is perpendicular to $\vec{a} \times(\vec{b} \times \vec{c})$, then the value of $[\vec{a} \times(\vec{b} \times \vec{c})] \times \vec{c}$ is equal to
A. $[\vec{a} \vec{b} \vec{c}] \vec{c}$
B. $[\vec{a} \vec{b} \vec{c}] \vec{b}$
C. $\overrightarrow{0}$
D. $[\vec{a} \vec{b} \vec{c}] \vec{a}$

## Answer: c

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90. If $V$ be the volume of a tetrahedron and $V^{\top}$ be the volume of another tetrahedran formed by the centroids of faces of the previous tetrahedron and $V=K V^{\prime}$, then $K$ is equal to a. 9 b .12 c .27 d .81
A. 9
B. 12
C. 27
D. 81

## Answer: c

91. $[(\vec{a} \times \vec{b}) \times(\vec{b} \times \vec{c})(\vec{b} \times \vec{c}) \times(\vec{c} \times \vec{a})(\vec{c} \times \vec{a}) \times(\vec{a} \times \vec{b})]$ is equal to (where $\vec{a}, \vec{b}$ and $\vec{c}$ are nonzero non-coplanar vector) a. $[\vec{a} \vec{b} \vec{c}]^{2}$ b. $[\vec{a} \vec{b} \vec{c}]^{3}$ c. $[\vec{a} \vec{b} \vec{c}]^{4}$ d. $[\vec{a} \vec{b} \vec{c}]$
A. $[\vec{a} \vec{b} \vec{c}]^{2}$
B. $[\vec{a} \vec{b} \vec{c}]^{3}$
C. $[\vec{a} \vec{b} \vec{c}]^{4}$
D. $[\vec{a} \vec{b} \vec{c}]$

## Answer: c

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92. 

$\vec{r}=x_{1}(\vec{a} \times \vec{b})+x_{2}(\vec{b} \times \vec{c})+x_{3}(\vec{c} \times \vec{a})$ and $4[\vec{a} \vec{b} \vec{c}]=1$ then $x_{1}+x_{2}+x_{3}$ is equal to
A. $\frac{1}{2} \vec{r} \cdot(\vec{a}+\vec{b}+\vec{c})$
B. $\frac{1}{4} \vec{r} \cdot(\vec{a}+\vec{b}+\vec{c})$
C. $2 \vec{r} \cdot(\vec{a}+\vec{b}+\vec{c})$
D. $4 \vec{r} \cdot(\vec{a}+\vec{b}+\vec{c})$

## Answer: d

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93. If $\vec{a} \perp \vec{b}$ then vector $\vec{v}$ in terms of $\vec{a}$ and $\vec{b}$ satisfying the equations
$\vec{v} \cdot \vec{a}=0$ and $\vec{v} \cdot \vec{b}=1$ and $[\vec{v} \cdot(\vec{a} \times \vec{b})]=1$ is
A. $\frac{\vec{b}}{|\vec{b}|^{2}}+\frac{\vec{a} \times \vec{b}}{|\vec{a} \times \vec{b}|^{2}}$
B. $\frac{\vec{b}}{}+\frac{\vec{a} \times \vec{b}}{}$
$|\vec{b}| \quad|\vec{a} \times \vec{b}|^{2}$
C. $\frac{\vec{b}}{|\vec{b}|}+\frac{\vec{a} \times \vec{b}}{|\vec{a} \times \vec{b}|}$
D. none of these

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94. If $\vec{a}^{\prime}=\hat{i}+\hat{j}, \vec{b}^{\prime} \hat{i}-\hat{j}+2 \hat{k} a n d \vec{c}^{\prime} 2 \hat{i}+\hat{j}-\hat{k}$, then the altitude of the parallelepiped formed by the vectors $\vec{a}$, $\vec{b}$ and $\vec{c}$ having base formed by $\vec{b}$ and $\vec{c}$ is (where $\vec{a}^{\prime}$ is reciprocal vector $\vec{a}$, et • ) 1 b. $3 \sqrt{2} / 2$ c. $1 / \sqrt{6} \mathrm{~d} .1 / \sqrt{2}$
A. 1
B. $3 \sqrt{2} / 2$
C. $1 / \sqrt{6}$
D. $1 / \sqrt{2}$

## Answer: d

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95. If $\vec{a}=\hat{i}+\hat{j}, \vec{b}=\hat{j}+\hat{k}, \vec{c}=\hat{k}+\hat{i}$ then in the reciprocal system of vectors
$\vec{a}, \vec{b}, \vec{c}$ reciprocal $\vec{a}$ of vector $\vec{a}$ is
A. $\frac{\hat{i}+\hat{j}+\hat{k}}{2}$
B. $\frac{\hat{i}-\hat{j}+\hat{k}}{2}$
C. $\frac{-\hat{i}-\hat{j}+\hat{k}}{2}$
D. $\frac{\hat{i}+\hat{j}-\hat{k}}{2}$

## Answer: d

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96. If unit vectors $\vec{a}$ and $\vec{b}$ are inclined at angle $2 \theta$ such that $|\vec{a}-\vec{b}|<1$ and $0 \leq \theta \leq \pi$, then $\theta$ lies in interval a. $[0, \pi / 6)$ b. $(5 \pi / 6, \pi]$ c. [ $\pi / 6, \pi / 2]$ d. $[\pi / 2,5 \pi / 6]$
A. $[0, \pi / 6)$
B. $(5 \pi / 6, \pi]$
C. $[\pi / 6, \pi / 2]$
D. $(\pi / 2,5 \pi / 6]$

## Answer: a,b

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97. 

$\vec{a}, \vec{b}$ and $\vec{c}$
are
non-collinear
$\vec{a} \times(\vec{b} \times \vec{c})+(\vec{a} \cdot \vec{b}) \vec{b}=(4-2 x-\sin y) \vec{b}+\left(x^{2}-1\right) \vec{c}$ and $(\vec{c} \cdot \vec{c}) \vec{a}=\vec{c}$ Then
a. $x=1$ b. $x=-1 \mathrm{c} . y=(4 n+1) \pi / 2, n \in I$ d. $y=(2 n+1) \pi / 2, n \in I$
A. $x=1$
B. $x=-1$
C. $y=(4 n+1) \frac{\pi}{2}, n \in I$
D. $y(2 n+1) \frac{\pi}{2}, n \in I$

## Answer: a,c

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98. Unit vectors $\vec{a}$ and $\vec{b}$ ar perpendicular, and unit vector $\vec{c}$ is inclined at an angle $\theta$ to both $\vec{a}$ and $\vec{b}$. If $\alpha \vec{a}+\beta \vec{b}+\gamma(\vec{a} \times \vec{b})$, then which of the following is incorrect?
A. $\alpha=\beta$
B. $\gamma^{2}=1-2 \alpha^{2}$
C. $y^{2}=-\cos 2 \theta$
D. $\beta^{2}=\frac{1+\cos 2 \theta}{2}$

## Answer: a,b,c,d

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99. If vectors $\vec{a} a n d \vec{b}$ are two adjacent sides of a parallelogram, then the vector respresenting the altitude of the parallelogram which is the
perpendicular to $a$ is a. $\vec{b}+\frac{\vec{b} \times \vec{a}}{|\vec{a}|^{2}}$ b. $\frac{\vec{a} \vec{b}}{|\vec{b}|^{2}}$ c. $\vec{b}-\frac{\vec{b} \vec{a}}{|\vec{a}|^{2}}$ d. $\frac{\vec{a} \times(\vec{b} \times \vec{a})}{|\vec{b}|^{2}}$
A. $\frac{(\vec{a} \cdot \vec{b})}{|\vec{a}|^{2}} \vec{a}-\vec{b}$
B. $\frac{1}{|\vec{a}|^{2}}\left\{|\vec{a}|^{2} \vec{b}-(\vec{a} \cdot \vec{b}) \vec{a}\right\}$
C. $\frac{\vec{a} \times(\vec{a} \times \vec{b})}{|\vec{a}|^{2}}$
D. $\vec{a} \times(\vec{b} \times \vec{a})$
$|\vec{b}|^{2}$

## Answer: a,b,c

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100. If $\vec{a} \times(\vec{b} \times \vec{c})$ is perpendicular to $(\vec{a} \times \vec{b}) \times \vec{c}$, we may have a.

$$
(\vec{a} \cdot \vec{c})|\vec{b}|^{2}=(\vec{a} \cdot \vec{b})(\vec{b} \cdot \vec{c})(\vec{c} \cdot \vec{a}) \text { b. } \vec{a} \vec{b}=0 \text { c. } \vec{a} \vec{c}=0 \text { d. } \vec{b} \vec{c}=0
$$

$$
\text { A. }(\vec{a} \cdot \vec{b})|\vec{b}|^{2}=(\vec{a} \cdot \vec{b})(\vec{b} \cdot \vec{c})
$$

B. $\vec{a} \cdot \vec{b}=0$
C. $\vec{a} \cdot \vec{c}=0$
D. $\vec{b} \cdot \vec{c}=0$

## Answer: ac

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101. Let $\vec{a}, \vec{b}$, and $\vec{c}$ be vectors forming right-hand traid. Let $\vec{p}=\frac{\vec{b} \times \vec{c}}{[\vec{a} \vec{b} \vec{c}]}, \vec{q}=\frac{\vec{c} \times \vec{a}}{[\vec{a} \vec{b} \vec{c}]}$, and $\vec{r}=\frac{\vec{a} \times \vec{b}}{[\vec{a} \vec{b} \vec{c}]}$, If $x \in R^{+}$, then
a. $x[\vec{a} \vec{b} \vec{c}]+\frac{[\vec{p} \vec{q} \vec{r}]}{x}$ has least value $=2$. b. $x^{4}[\vec{a} \vec{b} \vec{c}]^{2}+\frac{[\vec{p} \vec{q} \vec{r}]}{x^{2}}$ has least value $=\left(\frac{3}{2}\right)^{2 / 3}$ c. $[\vec{p} \vec{q} \vec{r}]>0 \mathrm{~d}$. none of these
A. $x[\vec{a} \vec{b} \vec{c}]+\frac{[\vec{p} \vec{q} \vec{r}]}{x}$ has least value 2
B. $x^{2}[\vec{a} \vec{b} \vec{c}]^{2}+\frac{[\vec{p} \vec{q} \vec{r}]}{x^{2}}$ has least value $\left(3 / 2^{2 / 3}\right)$
C. $[\vec{p} \vec{q} \vec{r}]>0$
D. none of these

## Answer: a,c

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102. $a_{1}, a_{2}, a_{3} \in R-\{0\}$ and $a_{1}+a_{2} \cos 2 x+a_{3} \sin ^{2} x=0$ " for all " x in R then
A. a) vectors $\vec{a}=a_{1} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}$ and $\vec{b}=4 \hat{i}+2 \hat{j}+\hat{k}$ are perpendicular to each other
B. b) vectors $\vec{a}=a_{1} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}$ and $\vec{b}=\hat{i}+\hat{j}+2 \hat{k}$ are parallel to each each other
C. c) if vector $\vec{a}=a_{1} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}$ is of length $\sqrt{6}$ units, then on of the ordered trippplet $\left(a_{1}, a_{2}, a_{3}\right)=(1,-1,-2)$
D. d) if $2 a_{1}+3 a_{2}+6 a_{3}+6 a_{3}=26$, then $\left|\vec{a} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}\right|$ is $2 \sqrt{6}$
103. If $\vec{a} a n d \vec{b}$ are two vectors and angle between them is $\theta$, then
$|\vec{a} \times \vec{b}|^{2}+(\vec{a} \vec{b})^{2}=|\vec{a}|^{2}|\vec{b}|^{2}$

$$
|\vec{a} \times \vec{b}|=(\vec{a} \vec{b}) \text {, if } \quad \theta=\pi / 4
$$

$\vec{a} \times \vec{b}=(\vec{a} \vec{b}) \hat{n}$, (wheren̂ is unit vector,) if $\theta=\pi / 4(\vec{a} \times \vec{b}) \vec{a}+\vec{b}=0$
A. $|\vec{a} \times \vec{b}|^{2}+(\vec{a} \cdot \vec{b})^{2}=|\vec{a}|^{2}|\vec{b}|^{2}$
B. $|\vec{a} \times \vec{b}|^{2}+(\vec{a} \cdot \vec{b})^{2}$, if $\theta=\pi / 4$
C. $\vec{a} \times \vec{b}=(\vec{a}$. Vecb $) \hat{n}$ ( where $\hat{n}$ is a normal unit vector ) if $\quad \theta f=\pi / 4$
D. $(\vec{a} \times \vec{b}) \cdot(\vec{a}+\vec{b})=0$

## Answer: a,b,c,d

104. Let $\vec{a}$ and $\vec{b}$ be two non- zero perpendicular vectors. A vector $\vec{r}$ satisfying the equation $\vec{r} \times \vec{b}=\vec{a}$ can be
A. $\vec{b}-\frac{\vec{a} \times \vec{b}}{}$ $|\vec{b}|^{2}$
B. $2 \vec{b}-\frac{\vec{a} \times \vec{b}}{}$
$|\vec{b}|^{2}$
C. $|\vec{a}| \vec{b}-\frac{\vec{a} \times \vec{b}}{|\vec{b}|^{2}}$
D. $|\vec{b}| \vec{b}-\frac{\vec{a} \times \vec{b}}{|\vec{b}|^{2}}$

## Answer: a,b,cd,

## D Watch Video Solution

105. If vector $\vec{b}=(\tan \alpha,-1,2 \sqrt{\sin \alpha / 2})$ and $\vec{c}=\left(\tan \alpha, \tan \alpha,-\frac{3}{\sqrt{\sin \alpha / 2}}\right)$ are orthogonal and vector $\vec{a}=(1,3, \sin 2 \alpha)$ makes an obtuse angle with the $z-$ axis, then the value of $\alpha$ is
A. $\alpha=(4 n+1) \pi+\tan ^{-1} 2$
B. $\alpha=(4 n+1) \pi-\tan ^{-1} 2$
C. $\alpha=(4 n+2) \pi+\tan ^{-1} 2$
D. $\alpha=(4 n+2) \pi-\tan ^{-1} 2$

## Answer: b,d

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106. Let $\vec{r}$ be a unit vector satisfying
$\vec{r} \times \vec{a}=\vec{b}$, where $|\vec{a}|=\sqrt{3}$ and $|\vec{b}|=\sqrt{2}$, then
A. $\vec{r}=\frac{2}{3}(\vec{a}+\vec{a} \times \vec{b})$
B. $\vec{r}=\frac{1}{3}(\vec{a}+\vec{a} \times \vec{b})$
C. $\vec{r}=\frac{2}{3}(\vec{a}-\vec{a} \times \vec{b})$
D. $\vec{r}=\frac{1}{3}(-\vec{a}+\vec{a} \times \vec{b})$
107. If $\vec{a}$ and $\vec{b}$ are unequal unit vectors such that $(\vec{a}-\vec{b}) \times[(\vec{b}+\vec{a}) \times(2 \vec{a}+\vec{b})]=\vec{a}+\vec{b}$ then angle $\theta$ between $\vec{a}$ and $\vec{b}$ is
A. 0
B. $\pi / 2$
C. $\pi / 4$
D. $\pi$

## Answer: b,d

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108. If $\vec{a}$ and $\vec{b}$ are two unit vectors perpenicualar to each other and $\vec{c}=\lambda_{1} \vec{a}+\lambda_{2} \vec{b}+\lambda_{3}(\vec{a} \times \vec{b})$, then which of the following is (are) true ?

$$
\text { A. } \lambda_{1}=\vec{a} \cdot \vec{c}
$$

B. $\lambda_{2}=|\vec{b} \times \vec{c}|$
C. $\lambda_{3}=\mid(\vec{a} \times \vec{b}|\times \vec{c}|$
D. $\vec{c}=\lambda_{1} \vec{a}+\lambda_{2} \vec{b}+\lambda_{3}(\vec{a} \times \vec{b})$

## Answer: a,d

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109. If vectors $\vec{a}$ and $\vec{b}$ are non collinear then $\frac{\vec{a}}{|\vec{a}|}+\frac{\vec{b}}{|\vec{b}|}$ is
A. a unit vector
B. in the plane of $\vec{a}$ and $\vec{b}$
C. equally inclined to $\vec{a}$ and $\vec{b}$
D. perpendicular to $\vec{a} \times \vec{b}$

## Answer: b,c,d

110. If $\vec{a}$ and $\vec{b}$ are non-zero vectors such that $|\vec{a}+\vec{b}|=|\vec{a}-2 \vec{b}|$ then
A. $2 \vec{a} \cdot \vec{b}=|\vec{b}|^{2}$
B. $\vec{a} \cdot \vec{b}=|\vec{b}|^{2}$
C. least value of $\vec{a} . \vec{b}+\frac{1}{|\vec{b}|^{2}+2}$ is $\sqrt{2}$
D. least value of $\vec{a} \cdot \vec{b}+\frac{1}{|\vec{b}|^{2}+2}$ is $\sqrt{2}-1$

## Answer: a,d

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111. Let $\vec{a} \vec{b}$ and $\vec{c}$ be non- zero vectors aned $\vec{V}_{1}=\vec{a} \times(\vec{b} \times \vec{c})$ and $\vec{V}_{2}=(\vec{a} \times \vec{b}) \times \vec{c}$.vectors $\vec{V}_{1}$ and $\vec{V}_{2}$ are equal. Then
A. $\vec{a}$ and $\vec{b}$ ar orthogonal
B. $\vec{a}$ and $\vec{c}$ are collinear
C. $\vec{b}$ and $\vec{c}$ ar orthogonal
D. $\vec{b}=\lambda(\vec{a} \times \vec{c})$ when $\lambda$ is a scalar

## Answer: b,d

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112. Vectors $\vec{A}$ and $\vec{B}$ satisfying the vector equation $\vec{A}+\vec{B}=\vec{a}, \vec{A} \times \vec{B}=\vec{b}$ and $\vec{A} \cdot \vec{a}=1$. where $\vec{a}$ and $\vec{b}$ are given vectors, are
A. 1. $\vec{A}=\frac{(\vec{a} \times \vec{b})-\vec{a}}{a^{2}}$
B. 2. $\vec{B}=\frac{(\vec{b} \times \vec{a})+\vec{a}\left(a^{2}-1\right)}{a^{2}}$
C. 3. $\vec{A}=\frac{(\vec{a} \times \vec{b})+\vec{a}}{a^{2}}$
D. 4. $\vec{B}=\frac{(\vec{b} \times \vec{a})-\vec{a}\left(a^{2}-1\right)}{a^{2}}$

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113. A vector $\vec{d}$ is equally inclined to three vectors $\vec{a}=\hat{i}+\hat{j}+\hat{k}, \vec{b}=2 \hat{i}+\hat{j}$ and $\vec{c}=3 \hat{j}-2 \hat{k}$ Let $\vec{x}, \vec{y}$, and $\vec{z}$ be three vectors in the plane of $\vec{a}, \vec{b} ; \vec{b}, \vec{c} ; \vec{c}, \vec{a}$, respectively. Then a. $\vec{x} . \vec{d}=-1 \mathrm{~b} . \vec{y} \cdot \vec{d}=1 \mathrm{c}$.
$\vec{z} \cdot \vec{d}=0$ d. $\vec{r} \cdot \vec{d}=0$, where $\vec{r}=\lambda \vec{x}+\mu \vec{y}+\delta \vec{z}$
A. $\vec{x} \cdot \vec{d}=-1$
B. $\vec{y} \cdot \vec{d}=1$
C. vecz.vecd=0`
D. vecr.vecd=0, " where " vecr=lambda vecx + mu vecy +deltavecz

## Answer: c.d

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114. Vectors Perpendicular to $\hat{i}-\hat{j}-\hat{k}$ and in the plane of $\hat{i}+\hat{j}+\hat{k}$ and $-\hat{i}+\hat{j}+\hat{k}$ are
A. $\hat{i}+\hat{k}$
B. $2 \hat{i}+\hat{j}+\hat{k}$
C. $3 \hat{i}+2 \hat{j}+\hat{k}$
D. $-4 \hat{i}-2 \hat{j}-2 \hat{k}$

## Answer: bed

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115. If side $\vec{A} B$ of an equilateral tangle $A B C$ lying in the $x-y$ plane $3 \hat{i}$, then side $\vec{C} B$ can be a. $-\frac{3}{2}(\hat{i}-\sqrt{3 \hat{j}})$ b. $\frac{3}{2}(\hat{i}-\sqrt{3} \hat{j})$ c. $-\frac{3}{2}(\hat{i}+\sqrt{3} \hat{j})$ d. $\frac{3}{2}(\hat{i}+\sqrt{3 \hat{j}})$
A. $-\frac{3}{2}(\hat{i}-\sqrt{3} \hat{j})$
B. $-\frac{3}{2}(\hat{i}-\sqrt{3} \hat{j})$
C. $-\frac{3}{2}(\hat{i}+\sqrt{3} \hat{j})$
D. $\frac{3}{2}(\hat{i}+\sqrt{3} \hat{j})$

## Answer: b,d

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116. The angles of triangle, two of whose sides are represented by vectors
$\sqrt{3}(\vec{a} \times \vec{b})$ and $\vec{b}-(\hat{a} \vec{b}) \hat{a}$, where $\vec{b}$ is a non zero vector and $\hat{a}$ is unit vector in the direction of $\vec{a}$, are
A. $\tan ^{-1}(\sqrt{3})$
B. $\tan ^{-1}(1 / \sqrt{3})$
C. $\cot ^{-1}(0)$
D. $\operatorname{tant}^{\wedge}(-1)(1)^{`}$

## Answer: a,b,c

117. $\vec{a}, \vec{b}$, and $\vec{c}$ are unimodular and coplanar. A unit vector $\vec{d}$ is perpendicular to then. If $(\vec{a} \times \vec{b}) \times(\vec{c} \times \vec{d})=\frac{1}{6} \hat{i}-\frac{1}{3} \hat{j}+\frac{1}{3} \hat{k}$, and the angel between $\vec{a}$ and $\vec{b}$ is $30^{0}$, thenc is $(\hat{i}-2 \hat{j}+2 \hat{k}) / 3 \mathrm{~b} .(-\hat{i}+2 \hat{j}-2 \hat{k}) / 3 \mathrm{c}$. $(2 \hat{i}+2 \hat{j}-\hat{k}) / 3$ d. $(-2 \hat{i}-2 \hat{j}+\hat{k}) / 3$
A. $(\hat{i}-2 \hat{j}+2 \hat{k}) / 3$
B. $(-\hat{i}+2 \hat{j}-2 \hat{k}) / 3$
C. $(-\hat{i}+2 \hat{j}-\hat{k}) / 3$
D. $(-2 \hat{i}-2 \hat{j}+\hat{k}) / 3$

## Answer: a,b

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118. If $\vec{a}+2 \vec{b}+3 \vec{c}=\overrightarrow{0}$ then $\vec{a} \times \vec{b}+\vec{b} \times \vec{c}+\vec{c} \times \vec{a}=$
A. $2(\vec{a} \times \vec{b})$
B. $6(\vec{b} \times \vec{c})$
C. $3(\vec{c} \times \vec{a})$
D. $\overrightarrow{0}$

## Answer: c,d

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119. Let $\vec{a}$ and $\vec{b}$ be two non-collinear unit vectors. If $\vec{u}=\vec{a}-(\vec{a} . \vec{b}) \vec{b}$ and $\vec{v}=\vec{a} \times \vec{b}$, then $|\vec{v}|$ is
A. $|\vec{u}|$
B. $|\vec{u}|+|\vec{u} . \vec{b}|$
C. $|\vec{u}|+|\vec{u} . \vec{a}|$
D. none of these

## Answer: b,d

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120. if $\vec{a} \times \vec{b}=\vec{c}, \vec{b} \times \vec{c}=\vec{a}$, where $\vec{c} \neq \overrightarrow{0}$ then (a) $|\vec{a}|=|\vec{c}|$ (b) $|\vec{a}|=|\vec{b}|$
(c) $|\vec{b}|=1$ (d) $|\vec{a}|=|\vec{b}|=|\vec{c}|=1$
A. $|\vec{a}|=|\vec{c}|$
B. $|\vec{a}|=|\vec{b}|$
C. $|\vec{b}|=1$
D. $|\vec{a}|=\vec{b}|=|\vec{c}|=1$

## Answer: ac

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121. Let $\vec{a}, \vec{b}$, and $\vec{c}$ be three non-coplanar vectors and $\vec{d}$ be a non -zero, which is perpendicular to $(\vec{a}+\vec{b}+\vec{c})$. Now
$\vec{d}=(\vec{a} \times \vec{b}) \sin x+(\vec{b} \times \vec{c}) \cos y+2(\vec{c} \times \vec{a})$. Then
A. $\frac{\vec{d} \cdot(\vec{a}+\vec{c})}{}=2$
$[\vec{a} \vec{b} \vec{c}]$
B. $\frac{\vec{d} \cdot(\vec{a}+\vec{c})}{=-2}$
$[\vec{a} \vec{b} \vec{c}]$
C. minimum value of $x^{2}+y^{2} i s \pi^{2} / 4$
D. minimum value of $x^{2}+y^{2} i s 5 \pi^{2} / 4$

## Answer: b,d

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122. If $\vec{a}, \vec{b}$, and $\leftrightarrow c$ are three unit vecrtors such that $\vec{a} \times(\vec{b} \times \vec{c})=\frac{1}{1} \vec{b}$, then ( $\vec{b}$ and $\vec{c}$ being non-parallel) angle between $\vec{a}$ and $\vec{b}$ is $\pi / 3$ b.anglebetweenaland $\vec{c} \mathrm{i} \pi / 3 \mathrm{c}$. a. angle between $\vec{a} a n d \vec{b}$ is $\pi / 2 \mathrm{~d}$.
a. angle between $\vec{a}$ and $\vec{c}$ is $\pi / 2$
A. angle between $\vec{a}$ and $\vec{b} i s \pi / 3$
B. angle between $\vec{a}$ and $\vec{c} i s \pi / 3$
C. angle between $\vec{a}$ and $\vec{b} i s \pi / 2$
D. angle between $\vec{a}$ and $\vec{c} i s \pi / 2$

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123. If in triangle $A B C, \overrightarrow{A B}=\frac{\vec{u}}{|\vec{u}|}-\frac{\vec{v}}{|\vec{v}|}$ and $\overrightarrow{A C}=\frac{2 \vec{u}}{|\vec{u}|}$, where $|\vec{u}| \neq|\vec{v}|$, then $(a) 1+\cos 2 A+\cos 2 B+\cos 2 C=0(b) \sin A=\cos C(c)$ projection of $A C$ on $B C$ is equal to $B C$ (d) projection of $A B$ on $B C$ is equal to $A B$
A. $1+\cos 2 A+\cos 2 B+\cos 2 C=0$
B. $\sin A=\cos C$
C. projection of $A C$ on $B C$ is equal to $B C$
D. projection of $A B$ on $B C$ is equal to $A B$

## Answer: a,b,c

124. $\left[\begin{array}{lll}\vec{a} \times \vec{b} & \vec{c} \times \vec{d} & \vec{e} \times \vec{f}\end{array}\right]$ is equal to
A. A. $[\vec{a} \vec{b} \vec{d}][\vec{c} \vec{e} \vec{f}]-[\vec{a} \vec{b} \vec{c}][\vec{d} \vec{e} \vec{f}]$
B. В. $[\vec{a} \vec{b} \vec{e}][\vec{f} \vec{c} \vec{d}]-[\vec{a} \vec{b} \vec{f}][\vec{e} \vec{c} \vec{d}]$
C. C. $[\vec{c} \vec{d} \vec{a}][\vec{b} \vec{e} \vec{f}]-[\vec{a} \vec{d} \vec{b}][\vec{a} \vec{e} \vec{f}]$
D. D. $[\vec{a} \vec{c} \vec{e}][\vec{b} \vec{d} \vec{f}]$

## Answer: a,b,c

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125. The scalars $l$ and $m$ such that $l \vec{a}+m \vec{b}=\vec{c}$, where $\vec{a}, \vec{b}$ and $\vec{c}$ are given vectors, are equal to
A. $I=\frac{(\vec{c} \times \vec{b}) \cdot(\vec{a} \times \vec{b})}{(\vec{a} \times \vec{b})^{2}}$
B. $I=\frac{(\vec{c} \times \vec{a}) \cdot(\vec{b} \times \vec{a})}{(\vec{b} \times \vec{a})}$

$$
(\vec{c} \times \vec{a}) \cdot(\vec{b} \times \vec{a})
$$

C. $m=$

$$
(\vec{b} \times \vec{a})^{2}
$$

D. $m=\frac{(\vec{c} \times \vec{a}) \cdot(\vec{b} \times \vec{a})}{(\vec{b} \times \vec{a})}$

## Answer: ac

## D Watch Video Solution

126. If $(\vec{a} \times \vec{b}) \times(\vec{c} \times \vec{d}) \cdot(\vec{a} \times \vec{d})=0$ then which of the following may be true?
A. A. $\vec{a}, \vec{b}$ and $\vec{d}$ are nenessarily coplanar
B. B. $\vec{a}$ lies in the plane of $\vec{c}$ and $\vec{d}$
C. C. $\vec{b}$ lies in the plane of $\vec{a}$ and $\vec{d}$
D. D. $\vec{c}$ lies in the plane of $\vec{a}$ and $\vec{d}$

## Answer: b,c,d

127. $A, B, C a n d D$ are four points such that
$\vec{A} B=m(2 \hat{i}-6 \hat{j}+2 \hat{k}), \vec{B} C=(\hat{i}-2 \hat{j})$ and $\overrightarrow{C D} D=n(-6 \hat{i}+15 \hat{j}-3 \hat{k}) \quad$ If $\quad C D$ intersects $A B$ at some point $E$, then a. $m \geq 1 / 2$ b. $n \geq 1 / 3$ c. $m=n$ d. $m<n$
A. $m \geq 1 / 2$
B. $n \geq 1 / 3$
C. $m=n$
D. $m<n$

## Answer: a,b

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128. If the vectors $\vec{a}, \vec{b}, \vec{c}$ are non-coplanar and $\mathrm{I}, \mathrm{m}, \mathrm{n}$ are distinct real numbers, then $[(l \vec{a}+m \vec{b}+n \vec{c})(l \vec{b}+m \vec{c}+n \vec{a})(l \vec{c}+m \vec{a}+n \vec{b})]=0$, implies
(A) $l m+m n+n l=0$
(B) $l+m+n=0$
(C) $l^{2}+m^{2}+n^{2}=0$
A. $l+m+n=0$
B. roots of the equation $l x^{2}+m x+n=0$ are equal
C. $l^{2}+m^{2}+n^{2}=0$
D. $l^{3}+m^{2}+n^{3}=3 l m n$

## Answer: a,b,d

## D Watch Video Solution

129. Let $\vec{\alpha}=a \hat{i}+b \hat{j}+c \hat{k}, \vec{\beta}=b \hat{i}+c \hat{j}+a \hat{k}$ and $\vec{\gamma}=c \hat{i}+a \hat{j}+b \hat{k}$ be three coplnar vectors with $a \neq b$, and $\vec{v}=\hat{i}+\hat{j}+\hat{k}$. Then $\vec{v}$ is perpendicular to
A. $\vec{\alpha}$
B. $\vec{\beta}$
C. $\vec{\gamma}$
D. none of these

## Answer: a,b,c

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130. If vectors $\vec{A}=2 \hat{i}+3 \hat{j}+4 \hat{k}, \vec{B}=\hat{i}+\hat{j}+5 \hat{k}$ and $\vec{C}$ form a left-handed system, then $\vec{C}$ is a. $11 \hat{i}-6 \hat{j}-\hat{k}$ b. $-11 \hat{i}+6 \hat{j}+\hat{k}$ c. $11 \hat{i}-6 \hat{j}+\hat{k}$ d. $-11 \hat{i}+6 \hat{j}-\hat{k}$
A. $11 \hat{i}-6 \hat{j}-\hat{k}$
B. $-11 \hat{i}-6 \hat{j}-\hat{k}$
C. $-11 \hat{i}-6 \hat{j}+\hat{k}$
D. $-11 \hat{i}+6 \hat{j}-\hat{k}$

## Answer: b,d

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131. If $\vec{a}=x \hat{i}+y \hat{j}+z \hat{k}, \vec{b}=y \hat{i}+z \hat{j}+x \hat{k}$ and $\vec{c}=z \hat{i}+x \hat{j}+y \hat{k}$, then $\vec{a} \times(\vec{b} \times \vec{c})$ is
A. A. parallel to $(y-z) \hat{i}+(z-x) \hat{j}+(x-y) \hat{k}$
B. B. orthogonal to $\hat{i}+\hat{j}+\hat{k}$
C. C. orthogonal to $(y+z) \hat{i}+(z+x) \hat{j}+(x+y) \hat{k}$
D. D. orthogonal to $x \hat{i}+y \hat{j}+z \hat{k}$

## Answer: a,b,c,d

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132. If $\vec{a} \times(\vec{b} \times \vec{c})=(\vec{a} \times \vec{b}) \times \vec{c}$ then
A. A. $(\vec{c} \times \vec{a}) \times \vec{b}=\overrightarrow{0}$
B. B. $\vec{c} \times(\vec{a} \times \vec{b})=\overrightarrow{0}$
C. C. $\vec{b} \times(\vec{c} \times \vec{a})=\overrightarrow{0}$
D. D. $\vec{c} \times \vec{a} \times \vec{b}=\vec{b} \times(\vec{c} \times \vec{a})=\overrightarrow{0}$

## Answer: a,c,d

133. A vector $(\vec{d})$ is equally inclined to three vectors $\vec{a}=\hat{i}-\hat{j}+\hat{k}, \vec{b}=2 \hat{i}+\hat{j}$ and $\vec{c}=3 \hat{j}-2 \hat{k}$ let $\vec{x}, \vec{y}, \vec{z}$ be three in the plane of $\vec{a}, \vec{b} ; \vec{b}, \vec{c} ; \vec{c}, \vec{a}$ respectively, then
A. $\vec{z} \cdot \vec{d}=0$
B. $\vec{x} \cdot \vec{d}=1$
C. $\vec{y} \cdot \vec{d}=32$
D. $\vec{r} \cdot \vec{d}=0$, where $\vec{r}=\lambda \vec{x}+\mu \vec{y}+\gamma \vec{z}$

## Answer: a,d

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134. A parallelogram is constructed on the vectors $\vec{a}=3 \vec{\alpha}-\vec{\beta}, \vec{b}=\vec{\alpha}+3 \vec{\beta} . I f|\vec{\alpha}|=|\vec{\beta}|=2$ and angle between $\vec{\alpha}$ and $\vec{\beta} i s \frac{\pi}{3}$ then the length of a diagonal of the parallelogram is
A. $4 \sqrt{5}$
B. $4 \sqrt{3}$
C. $4 \sqrt{7}$
D. none of these

## Answer: b,c

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## Reasoning type

1. Statement 1: Vector $\vec{c}=-5 \hat{i}+7 \hat{j}+2 \hat{k}$ is along the bisector of angel between $\vec{a}=\hat{i}+2 \hat{j}+2 \hat{k} a n d \vec{b}=8 \hat{i}+\hat{j}-4 \hat{k} \quad$ Statement $2: \quad \vec{c} \quad$ is equally inclined to $\vec{a} a n d \vec{b}$
A. Both the statements are true and statement 2 is the correct explanation for statement 1.
B. Both statements are true but statement 2 is not the correct
C. Statement 1 is true and Statement 2 is false
D. Statement 1 is false and Statement 2 is true.

## Answer: b

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2. Statement 1: A component of vector $\vec{b}=4 \hat{i}+2 \hat{j}+3 \hat{k}$ in the direction perpendicular totehdirectin of vector $\vec{a}=\hat{i}+\hat{j}+\hat{k} i s \hat{i}-\hat{j}$ Statement 2: A component of vector in the direction of $\vec{a}=\hat{i}+\hat{j}+\hat{k} i s 2 \hat{i}+2 \hat{j}+2 \hat{k}$
A. Both the statements are true and statement 2 is the correct explanation for statement 1.
B. Both statements are true but statement 2 is not the correct explanation for statement 1.
C. Statement 1 is true and Statement 2 is false
D. Statement 1 is false and Statement 2 is true.

## Answer: c

## D Watch Video Solution

3. Statement 1: Distance of point $D(1,0,-1)$ from the plane of points $A($ $1,-2,0), B(3,1,2)$ and $C(-1,1,-1)$ is $\frac{8}{\sqrt{229}}$

Statement 2: volume of tetrahedron formed by the points $A, B, C$ and $D$ is $\sqrt{229}$

2
A. Both the statements are true and statement 2 is the correct
explanation for statement 1.
B. Both statements are true but statement 2 is not the correct explanation for statement 1.
C. Statement 1 is true and Statement 2 is false
D. Statement 1 is false and Statement 2 is true.

## Answer: d

4. Let $\vec{r}$ be a non-zero vector satisfying $\vec{r} \cdot \vec{a}=\vec{r} \cdot \vec{b}=\vec{r} \cdot \vec{c}=0$ for given non- zero vectors $\vec{a}, \vec{b}$ and $\vec{c}$

Statement 1: $[\vec{a}-\vec{b} \vec{b}-\vec{c} \vec{c}-\vec{a}]=0$
Statement 2: $[\vec{a} \vec{b} \vec{c}]=0$
A. A. Both the statements are true and statement 2 is the correct explanation for statement 1.
B. B. Both statements are true but statement 2 is not the correct explanation for statement 1.
C. C. Statement 1 is true and Statement 2 is false
D. D. Statement 1 is false and Statement 2 is true.

Answer: b
5. Statement 1: If $a_{1} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}, \vec{b} \hat{i}+b_{2} \hat{j}+b_{3} \hat{k}$ and $c_{1} \hat{i}+c_{2} \hat{j}+c_{3} \hat{k}$ are three mutually perpendicular unit vectors then $a_{1} \hat{i}+b_{1} \hat{j}+c_{1} \hat{k}, a_{2} \hat{i}+b_{2} \hat{j}+c_{2} \hat{k}$ and $a_{3} \hat{i}+b_{3} \hat{j}+c_{3} \hat{k}$ may be mutually perpendicular unit vectors.

Statement 2 : value of determinant and its transpose are the same.
A. A. Both the statements are true and statement 2 is the correct explanation for statement 1.
B. B. Both statements are true but statement 2 is not the correct explanation for statement 1.
C. C. Statement 1 is true and Statement 2 is false
D. D. Statement 1 is false and Statement 2 is true.

## Answer: a

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6. Statement $1: \vec{A}=2 \hat{i}+3 \hat{j}+6 \hat{k}, \vec{B}=\hat{i}+\hat{j}-2 \hat{k}$ and $\vec{C}=\hat{i}+2 \hat{j}+\hat{k}$ then
$|\vec{A} \times(\vec{A} \times(\vec{A} \times \vec{B})) \cdot \vec{C}|=243$
Statement 2: $|\vec{A} \times(\vec{A} \times(\vec{A} \times \vec{B})) \cdot \vec{C}|=|\vec{A}|^{2}|[\vec{A} \vec{B} \vec{C}]|$
A. A. Both the statements are true and statement 2 is the correct explanation for statement 1.
B. B. Both statements are true but statement 2 is not the correct explanation for statement 1.
C. C. Statement 1 is true and Statement 2 is false
D. D. Statement 1 is false and Statement 2 is true.

## Answer: d

## - Watch Video Solution

7. Statement $1: \vec{a}, \vec{b}$, and $\vec{c}$ are three mutually perpendicular unit vectors and $\vec{d}$ is a vector such that $\vec{a}, \vec{b}, \vec{c} a n d \vec{d}$ are non-coplanar. If

$$
\begin{aligned}
& {[\vec{d} \vec{b} \vec{c}]=[\vec{d} \vec{a} \vec{b}]=[\vec{d} \vec{c} \vec{a}]=1 \text {, thend }=\vec{a}+\vec{b}+\vec{c} \text {. Statement }} \\
& {[\vec{d} \vec{b} \vec{c}]=[\vec{d} \vec{a} \vec{b}]=[\vec{d} \vec{c} \vec{a}] \text {; then } \vec{d} \text { equally inclined to } \vec{a}, \vec{b} \text { and } \vec{c} .}
\end{aligned}
$$

A. Both the statements are true and statement 2 is the correct explanation for statement 1.
B. Both statements are true but statement 2 is not the correct explanation for statement 1.
C. Statement 1 is true and Statement 2 is false
D. Statement 1 is false and Statement 2 is true.

## Answer: b

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8. Consider a vector $\vec{c}$

Prove that, $\vec{c}=(\hat{i} \cdot \vec{c}) \hat{i}+(\hat{j} \cdot \vec{c}) \hat{j}+(\hat{k} \cdot \vec{c}) \hat{k}$

1. Let $\vec{u}, \vec{v}$ and $\vec{w}$ be three unit vectors such that $\vec{u}+\vec{v}+\vec{w}=\vec{a}, \vec{u} \times(\vec{v} \times \vec{w})=\vec{b},(\vec{u} \times \vec{v}) \times \vec{w}=\vec{c}, \vec{a} \cdot \vec{u}=3 / 2, \vec{a} \cdot \vec{v}=7 / 4$ and Vector $\vec{w}$ is
A. $\vec{a}-\frac{2}{3} \vec{b}+\vec{c}$
B. $\vec{a}+\frac{4}{3} \vec{b}+\frac{8}{3} \vec{c}$
C. $2 \vec{a}-\vec{b}+\frac{1}{3} \vec{c}$
D. $\frac{4}{3} \vec{a}-\vec{b}+\frac{2}{3} \vec{c}$

## Answer: b

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2. Let $\vec{u}, \vec{v}$ and $\vec{w}$ be three unit vectors such that $\vec{u}+\vec{v}+\vec{w}=\vec{a}, \vec{u} \times(\vec{v} \times \vec{w})=\vec{b},(\vec{u} \times \vec{v}) \times \vec{w}=\vec{c}, \vec{a} \cdot \vec{u}=3 / 2, \vec{a} \cdot \vec{v}=7 / 4$ and
A. (a) $\vec{a}-\frac{2}{3} \vec{b}+\vec{c}$
B. (b) $\vec{a}+\frac{4}{3} \vec{b}+\frac{8}{3} \vec{c}$
C. (c) $2 \vec{a}-\vec{b}+\frac{1}{3} \vec{c}$
D. (d) $\frac{4}{3} \vec{a}-\vec{b}+\frac{2}{3} \vec{c}$

## Answer: c

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3. Let $\vec{u}, \vec{v}$ and $\vec{w}$ be three unit vectors such that $\vec{u}+\vec{v}+\vec{w}=\vec{a}, \vec{u} \times(\vec{v} \times \vec{w})=\vec{b},(\vec{u} \times \vec{v}) \times \vec{w}=\vec{c}, \vec{a} \cdot \vec{u}=3 / 2, \vec{a} \cdot \vec{v}=7 / 4$ and Vector $\vec{w}$ is
A. (a) $\vec{a}-\frac{2}{3} \vec{b}+\vec{c}$
B. (b) $\vec{a}+\frac{4}{3} \vec{b}+\frac{8}{3} \vec{c}$
C. (c) $2 \vec{a}-\vec{b}+\frac{1}{3} \vec{c}$
D. (a) $\frac{4}{3} \vec{a}-\vec{b}+\frac{2}{3} \vec{c}$

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4. Vectors $\vec{x}, \vec{y}, \vec{z}$ each of magnitude $\sqrt{2}$ make angles of $60^{\circ}$ with each other. If $\vec{x} \times(\vec{y} \times \vec{z})=\vec{a}, \vec{y} \times(\vec{z} \times \vec{x})=\vec{b}$ and $\vec{x} \times \vec{y}=\vec{c}$, find $\vec{x}, \vec{y}, \vec{z}$ in terms of $\vec{a}, \vec{b}$ and $\vec{c}$.

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5. Vectors $\vec{x}, \vec{y}, \vec{z}$ each of magnitude $\sqrt{2}$ make angles of $60^{\circ}$ with each other. If $\vec{x} \times(\vec{y} \times \vec{z})=\vec{a}, \vec{y} \times(\vec{z} \times \vec{x})=\vec{b}$ and $\vec{x} \times \vec{y}=\vec{c}$, find $\vec{x}, \vec{y}, \vec{z}$ in terms of $\vec{a}, \vec{b}$ and $\vec{c}$.
A. $\frac{1}{2}[(\vec{a}+\vec{c}) \times \vec{b}-\vec{b}-\vec{a}]$
B. $\frac{1}{2}[(\vec{a}-\vec{c}) \times \vec{b}+\vec{b}+\vec{a}]$
C. $\frac{1}{2}[(\vec{a}-\vec{b}) \times \vec{c}+\vec{b}+\vec{a}]$
D. $\frac{1}{2}[(\vec{a}-\vec{c}) \times \vec{a}+\vec{b}-\vec{a}]$

## Answer: c

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6. Vectors $\vec{x}, \vec{y}, \vec{z}$ each of magnitude $\sqrt{2}$ make angles of $60^{\circ}$ with each other. If $\vec{x} \times(\vec{y} \times \vec{z})=\vec{a}, \vec{y} \times(\vec{z} \times \vec{x})=\vec{b}$ and $\vec{x} \times \vec{y}=\vec{c}$, find $\vec{x}, \vec{y}, \vec{z}$ in terms of $\vec{a}, \vec{b}$ and $\vec{c}$.
A. $\frac{1}{2}[(\vec{a}-\vec{c}) \times \vec{c}-\vec{b}+\vec{a}]$
B. $\frac{1}{2}[(\vec{a}-\vec{b}) \times \vec{c}+\vec{b}-\vec{a}]$
C. $\frac{1}{2}[\vec{c} \times(\vec{a}-\vec{b})+\vec{b}+\vec{a}]$
D. none of these

## Answer: b

## - Watch Video Solution

7. If $\vec{x} \times \vec{y}=\vec{a}, \vec{y} \times \vec{z}=\vec{b}, \vec{x} . \vec{b}=\gamma, \vec{x} . \vec{y}=1$ and $\vec{y} \cdot \vec{z}=1$ then find $x, y, z$ in terms of $\vec{a}, \vec{b}$ and $\gamma$.

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8. If $\vec{x} \times \vec{y}=\vec{a}, \vec{y} \times \vec{z}=\vec{b}, \vec{x} . \vec{b}=\gamma, \vec{x} . \vec{y}=1$ and $\vec{y} \cdot \vec{z}=1$ then find $x, y, z$ in terms of $\vec{a}, \vec{b}$ and $\gamma$.
A. $\frac{\vec{a} \times \vec{b}}{\gamma}$
B. $\vec{a}+\frac{\vec{a} \times \vec{b}}{\gamma}$
C. $\vec{a}+\vec{b}+\frac{\vec{a} \times \vec{b}}{\gamma}$
D. none of these

## Answer: a

9. Vectors $\vec{x}, \vec{y}, \vec{z}$ each of magnitude $\sqrt{2}$ make angles of $60^{\circ}$ with each other. If $\vec{x} \times(\vec{y} \times \vec{z})=\vec{a}, \vec{y} \times(\vec{z} \times \vec{x})=\vec{b}$ and $\vec{x} \times \vec{y}=\vec{c}$, find $\vec{x}, \vec{y}, \vec{z}$ in terms of $\vec{a}, \vec{b}$ and $\vec{c}$.
A. $\frac{\gamma}{|\vec{a} \times \vec{b}|^{2}}[\vec{a}+\vec{b} \times(\vec{a} \times \vec{b})]$
B. $\frac{\gamma}{|\vec{a} \times \vec{b}|^{2}}[\vec{a}+\vec{b}-\vec{a} \times(\vec{a} \times \vec{b})]$
C. $\frac{\gamma}{|\vec{a} \times \vec{b}|^{2}}[\vec{a}+\vec{b}+\vec{a} \times(\vec{a} \times \vec{b})]$
D. none of these

## Answer: c

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10. Given two orthogonal vectors $\vec{A}$ and $\vec{B}$ each of length unity. Let $\vec{P}$ be the vector satisfying the equation $\vec{P} \times \vec{B}=\vec{A}-\vec{P}$. then $(\vec{P} \times \vec{B}) \times \vec{B}$ is equal to
A. $\vec{P}$
B. $-\vec{P}$
C. $2 \vec{B}$
D. $\vec{A}$

## Answer: b

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11. Given two orthogonal vectors $\vec{A}$ and $\vec{B}$ each of length unity. Let $\vec{P}$ be the vector satisfying the equation $\vec{P} \times \vec{B}=\vec{A}-\vec{P}$. then $\vec{P}$ is equal to
A. $\frac{\vec{A}}{2}+\frac{\vec{A} \times \vec{B}}{2}$
B. $\frac{\vec{A}}{2}+\frac{\vec{B} \times \vec{A}}{2}$
C. $\frac{\vec{A} \times \vec{B}}{2}-\frac{\vec{A}}{2}$
D. $\vec{A} \times \vec{B}$

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12. Given two orthogonal vectors $\vec{A}$ and VecB each of length unity. Let $\vec{P}$ be the vector satisfying the equation $\vec{P} \times \vec{B}=\vec{A}-\vec{P}$. then which of the following statements is false ?
A. vectors $\vec{P}, \vec{A}$ and $\vec{P} \times \vec{B}$ ar linearly dependent.
B. vectors $\vec{P}, \vec{B}$ and $\vec{P} \times \vec{B}$ ar linearly independent
C. $\vec{P}$ is orthogonal to $\vec{B}$ and has length $\frac{1}{\sqrt{2}}$.
D. none of these

## Answer: d

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13. Let $\vec{a}=2 \hat{i}+3 \hat{j}-6 \hat{k}, \vec{b}=2 \hat{i}-3 \hat{j}+6 \hat{k}$ and $\vec{c}=-2 \hat{i}+3 \hat{j}+6 \hat{k}$. Let $\vec{a}_{1}$ be the projection of $\vec{a}$ on $\vec{b}$ and $\vec{a}_{2}$ be the projection of $\vec{a}_{1}$ on $\vec{c}$. Then
$\vec{a}_{2}$ is equal to
$\frac{943}{49}(-2 \hat{i}+3 \hat{j}+6 \hat{k})$
(A) $\frac{943}{49}(2 \hat{i}-3 \hat{j}-6 \hat{k})$
(B) $\frac{943}{49^{2}}(2 \hat{i}-3 \hat{j}-6 \hat{k})$
$\frac{943}{49}(-2 \hat{i}+3 \hat{j}+6 \hat{k})$ (D) $\frac{943}{49^{2}}(-2 \hat{i}+3 \hat{j}+6 \hat{k})$
A. $\frac{943}{49}(2 \hat{i}-3 \hat{j}-6 \hat{k})$
B. $\frac{943}{49^{2}}(2 \hat{i}-3 \hat{j}-6 \hat{k})$
c. $\frac{943}{49}(-2 \hat{i}+3 \hat{j}+6 \hat{k})$
D. $\frac{943}{49^{2}}(-2 \hat{i}+3 \hat{j}+6 \hat{k})$

Answer: b

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14. Let $\vec{a}=2 \hat{i}+3 \hat{j}-6 \hat{k}, \vec{b}=2 \hat{i}-3 \hat{j}+6 \hat{k}$ and $\vec{c}=-2 \hat{i}+3 \hat{j}+6 \hat{k}$. Let $\vec{a}_{1}$ be the projection of $\vec{a}$ on $\vec{b}$ and $\vec{a}_{2}$ be the projection of $\vec{a}_{1}$ on $\vec{c}$. Then $\vec{a}_{1} \cdot \vec{b}$ is equal to (A) -41 (B) $-41 / 7$ (C) 41 (D) 287
A. -41
B. $-41 / 7$
C. 41
D. 287

## Answer: a

## D Watch Video Solution

15. Let $\vec{a}=2 \hat{i}+3 \hat{j}-6 \hat{k}, \vec{b}=2 \hat{i}-3 \hat{j}+6 \hat{k}$ and $\vec{c}=-2 \hat{i}+3 \hat{j}+6 \hat{k}$. Let $\vec{a}_{1}$ be the projection of $\vec{a}$ on $\vec{b}$ and $\vec{a}_{2}$ be the projection of $\vec{a}_{1}$ on $\vec{c}$. Then $\vec{a}_{2}$ is equal to (A) $\frac{943}{49}(2 \hat{i}-3 \hat{j}-6 \hat{k}) \quad$ (B) $\frac{943}{49^{2}}(2 \hat{i}-3 \hat{j}-6 \hat{k})$ $\frac{943}{49}(-2 \hat{i}+3 \hat{j}+6 \hat{k})$ (D) $\frac{943}{49^{2}}(-2 \hat{i}+3 \hat{j}+6 \hat{k})$
A. $\vec{a}$ and $v c e a_{2}$ are collinear
B. $\vec{a}_{1}$ and $\vec{c}$ are collinear
C. $\vec{a} m \vec{a}_{1}$ and $\vec{b}$ are coplanar
D. $\vec{a}, \vec{a}_{1}$ and $a_{2}$ are coplanar

## Answer: c

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16. Consider a triangular pyramid ABCD the position vectors of whose agular points are $A(3,0,1), B(-1,4,1), C(5,3,2)$ and $D(0,-5,4)$ Let $G$ be the point of intersection of the medians of the triangle BCD. The length
of the vector $A G$ is
A. $\sqrt{17}$
B. $\sqrt{51} / 3$
C. $3 / \sqrt{6}$
D. $\sqrt{59} / 4$

Answer: b
17. Consider a triangular pyramid $A B C D$ the position vectors of whose agular points are $A(3,0,1), B(-1,4,1), C(5,3,2)$ and $D(0,-5,4)$ Let $G$ be the point of intersection of the medians of the triangle BCD. The length
of the vector $A G$ is
A. 24
B. $8 \sqrt{6}$
C. $4 \sqrt{6}$
D. none of these

## Answer: c

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18. Consider a triangular pyramid $A B C D$ the position vectors of whose agular points are $A(3,0,1), B(-1,4,1), C(5,3,2)$ and $D(0,-5,4)$ Let $G$ be
the point of intersection of the medians of the triangle $B C D$. The length of the vector $A G$ is
A. $14 / \sqrt{6}$
B. $2 / \sqrt{6}$
C. $3 / \sqrt{6}$
D. none of these

## Answer: a

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19. Vertices of a parallelogram taken in order are $A,(2,-1,4), B(1,0,-1), C($ $1,2,3$ ) and $D(x, y, z)$ The distance between the parallel lines $A B$ and $C D$ is
A. $\sqrt{6}$
B. $3 \sqrt{6 / 5}$
C. $2 \sqrt{2}$
D. 3

Answer: c

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20. Vertices of a parallelogram taken in order are $A(2,-1,4) B(1,0,-1) C(1,2,3)$ and $D$.

Distance of the point $P(8,2,-12)$ from the plane of the parallelogram is
A. $\frac{4 \sqrt{6}}{9}$
$32 \sqrt{6}$
B. 9
C. $\frac{16 \sqrt{6}}{9}$
D. none

## Answer: b

21. Vertices of a parallelogram taken in order are $A,(2,-1,4), B(1,0,-1), C($ $1,2,3$ ) and $D$.

The distance between the parallel lines $A B$ and $C D$ is
A. $14,4,2$
B. $2,4,14$
C. $4,2,14$
D. 2,14,4

## Answer: d

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22. Let $\vec{r}$ be a position vector of a variable point in Cartesian OXY plane such $\begin{gathered}\text { that }(10 \hat{j}-8 \hat{i}-\vec{r})=40 \\ P_{1}=\max \left\{|\vec{r}+2 \hat{i}-3 \hat{j}|^{2}\right\}, P_{2}=\min \left\{|\vec{r}+2 \hat{i}-3 \hat{j}|^{2}\right\} . \text { A tangenty line is }\end{gathered}$ drawn to the curve $y=8 / x^{2}$ at point .A with abscissa 2. the drawn line

## cuts the x-axis at a point B.

$p_{2}$ is equal to
A. 9
B. $2 \sqrt{2}-1$
C. $6 \sqrt{6}+3$
D. $9-4 \sqrt{2}$

## Answer: d

## - Watch Video Solution

23. Let $\vec{r}$ be a position vector of a variable point in Cartesian OXY plane

$$
\begin{gathered}
\text { that } \quad \vec{r} \cdot(10 \hat{j}-8 \hat{i}-\vec{r})=40 \\
P_{1}=\max \left\{|\vec{r}+2 \hat{i}-3 \hat{j}|^{2}\right\}, P_{2}=\min \left\{|\vec{r}+2 \hat{i}-3 \hat{j}|^{2}\right\} \text { and }
\end{gathered}
$$ drawn to the curve $y=8 / x^{2}$ at point.$A$ with abscissa 2 . the drawn line cuts the $x$-axis at a point $B$.

$p_{1}+p_{2}$ is equal to
A. 2
B. 10
C. 18
D. 5

## Answer: c

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24. Let $\vec{r}$ be a position vector of a variable point in Cartesian OXY plane such that $\vec{r} .(10 \hat{j}-8 \hat{i}-\vec{r})=40 \quad$ and $P_{1}=\max \left\{|\vec{r}+2 \hat{i}-3 \hat{j}|^{2}\right\}, P_{2}=\min \left\{|\vec{r}+2 \hat{i}-3 \hat{j}|^{2}\right\}$. A tangenty line is drawn to the curve $y=8 / x^{2}$ at point.$A$ with abscissa 2. the drawn line cuts the $x$-axis at a point $B$.

Find $r$ is equal to
A. 1
B. 2
C. 3
D. 4

## Answer: c

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25. $A b, A C$ and $A D$ are three adjacent edges of a parallelpiped. The diagonal of the praallelepiped passing through A and direqcted away from it is vector $\vec{a}$. The vector of the faces containing vertices A, B, C and A, B, D are $\vec{b}$ and $\vec{c}$, respectively, i.e. $A B \times A C$ and $A D \times A B=\vec{c}$ the projection of each edge $A B$ and $A C$ on diagonal vector $\vec{a}$ is $\frac{|\vec{a}|}{3}$ vector $A D$ is
A. $\frac{1}{3} \vec{a}+\frac{\vec{a} \times(\vec{b}-\vec{c})}{|\vec{a}|^{2}}$
B. $\frac{1}{3} \vec{a}+\frac{\vec{a} \times(\vec{b}-\vec{c})}{|\vec{a}|^{2}}+\frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^{2}}$
C. $\frac{1}{3} \vec{a}+\frac{\vec{a} \times(\vec{b}-\vec{c})}{|\vec{a}|^{2}}-\frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^{2}}$
D. none of these

## Answer: a

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26. $A b, A C$ and $A D$ are three adjacent edges of a parallelpiped. The diagonal of the praallelepiped passing through A and direqcted away from it is vector $\vec{a}$. The vector of the faces containing vertices A, B, C and A, B, D are $\vec{b}$ and $\vec{c}$, respectively, i.e. $\overrightarrow{A B} \times \overrightarrow{A C}=\vec{b}$ and $\overrightarrow{A D} \times \overrightarrow{A B}=\vec{c}$ the projection of each edge $A B$ and $A C$ on diagonal vector $\vec{a} i s \frac{|\vec{a}|}{3}$
vector $A B$ is
A. $\frac{1}{3} \vec{a}+\frac{\vec{a} \times(\vec{b}-\vec{c})}{|\vec{a}|^{2}}$
B. $\frac{1}{3} \vec{a}+\frac{\vec{a} \times(\vec{b}-\vec{c})}{|\vec{a}|^{2}}+\frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^{2}}$
C. $\frac{1}{3} \vec{a}+\frac{\vec{a} \times(\vec{b}-\vec{c})}{|\vec{a}|^{2}}-\frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^{2}}$
D. none of these

## Answer: b

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27. Ab, AC and AD are three adjacent edges of a parallelpiped. The diagonal of the praallelepiped passing through A and direqcted away from it is vector $\vec{a}$. The vector of the faces containing vertices A, B, C and A, B, D are $\vec{b}$ and $\vec{c}$, respectively, i.e. $\overrightarrow{A B} \times \overrightarrow{A C}=\vec{b}$ and $\overrightarrow{A D} \times \overrightarrow{A B}=\vec{c}$ the projection of each edge $A B$ and $A C$ on diagonal vector $\vec{a} i s \frac{|\vec{a}|}{3}$ vector $A C$ is
A. $\frac{1}{3} \vec{a}+\frac{\vec{a} \times(\vec{b}-\vec{c})}{|\vec{a}|^{2}}$
B. $\frac{1}{3} \vec{a}+\frac{\vec{a} \times(\vec{b}-\vec{c})}{|\vec{a}|^{2}}+\frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^{2}}$
C. $\frac{1}{3} \vec{a}+\frac{\vec{a} \times(\vec{b}-\vec{c})}{|\vec{a}|^{2}}-\frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^{2}}$
D. none of these

## Answer: c

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Martrix - match type
1.
.

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2. Find a unit vector in the direction of $\vec{a}=3 \hat{i}-2 \hat{j}+6 \hat{k}$

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3. Find the value of $\lambda$ if the vectors $\vec{a}$ and $\vec{b}$ are perpendicular. where, $\vec{a}=$ $2 \hat{i}+\lambda \hat{j}+\hat{k}$ and $\vec{b}=\hat{i}-2 \hat{j}+3 \hat{k}$

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4. Given two vectors $\vec{a}=-\hat{i}+\hat{j}+2 \hat{k}$ and $\vec{b}=-\hat{i}-2 \hat{j}-\hat{k}$
find $|\vec{a} \times \vec{b}|$

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5. Given two vectors $\vec{a}=-\hat{i}+3 \hat{j}+\hat{k}$ and $\vec{b}=-3 \hat{i}+\hat{j}+\hat{k}$ find $|\vec{a} \times \vec{b}|$

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6. Show that the vectors $\hat{i}-2 \hat{j}+3 \hat{k},-2 \hat{i}+3 \hat{j}-4 \hat{k}$ and $\hat{i}-3 \hat{j}+5 \hat{k}$ are coplanar.

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7. find $|\vec{x}|$, if for a unit vector $\vec{a},(\vec{x}-\vec{a})(\vec{x}+\vec{a})=12$

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8. Write the value of p for which $\vec{a}=3 \hat{i}+2 \hat{j}+9 \hat{k}, \vec{b}=\hat{i}+p \hat{j}+3 \hat{k}$ are parallel

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9. Find the projection of $\vec{a}$ on $\vec{b}$ if $\vec{a} . \vec{b}=8$ and $\vec{b}=2 \hat{i}+6 \hat{j}+3 \hat{k}$

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10. If $\vec{a}=x \hat{i}+2 \hat{j}-z \hat{k}$ and $\vec{b}=3 \hat{i}-y \hat{j}+\hat{k}$ are two equal vecots then find the value of $x+y+z$

## Integer type

1. If $\vec{a} a n d \vec{b}$ are any two unit vectors, then find the greatest positive
integer in the range of $\frac{3|\vec{a}+\vec{b}|}{2}+2|\vec{a}-\vec{b}|$.

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2. Let $\vec{u}$ be a vector on rectangular coordinate system with sloping angle $60^{\circ}$ Suppose that $|\vec{u}-\hat{i}|$ is geometric mean of $|\vec{u}|$ and $|\vec{u}-2 \hat{i}|$, where $\hat{i}$ is the unit vector along the $x$-axis. Then find the value of $(\sqrt{2}+1)|\vec{u}|$

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3. Find the absolute value of parameter $t$ for which the area of the triangle whose vertices the $A(-1,1,2) ; B(1,2,3)$ and $C(5,1,1)$ is minimum.
4. If $\vec{a}=a_{1} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k} ; \vec{b}=b_{1} \hat{i}+b_{2} \hat{j}+b_{3} \hat{k}, . \vec{c}=c_{1} \hat{i}+c_{2} \hat{j}+c_{3} \hat{k} \quad$ and $[3 \vec{a}+\vec{b} 3 \vec{b}+\vec{c} 3 \vec{c}+\vec{a}]=\lambda[\vec{a} \vec{b} \vec{c}]$, then find the value of $\frac{\lambda}{4}$.

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5. Let $\vec{a}=\alpha \hat{i}+2 \hat{j}-3 \hat{k}, \vec{b}=\alpha \hat{i}+2 \alpha \hat{j}-2 \hat{k}$, and $\vec{c}=2 \hat{i}-\alpha \hat{j}+\hat{k}$ Find thevalue of $6 \alpha$, such that $\{(\vec{a} \times \vec{b}) \times(\vec{b} \times \vec{c})\} \times(\vec{c} \times \vec{a})=0$.

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6. If $\vec{x}, \vec{y}$ are two non-zero and non-collinear vectors satisfying $\left[(a-2) \alpha^{2}+(b-3) \alpha+c\right] \vec{x}+\left[(a-2) \beta^{2}+(b-3) \beta+c\right] \vec{y}+\left[(a-2) \gamma^{2}+(b-3) \gamma+c\right.$ are three distinct real numbers, then find the value of $\left(a^{2}+b^{2}+c^{2}-4\right)$

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7. Let $\vec{u}$ and $\vec{v}$ be unit vectors such that $\vec{u} \times \vec{v}+\vec{u}=\vec{w}$ and $\vec{w} \times \vec{u}=\vec{v}$. Find the value of $[\vec{u} \vec{v} \vec{w}]$.

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8. Find the value of $\lambda$ if the volume of a tetrahedron whose vertices are with position vectors $\hat{i}-6 \hat{j}+10 \hat{k},-\hat{i}-3 \hat{j}+7 \hat{k}, 5 \hat{i}-\hat{j}+\lambda \hat{k}$ and $7 \hat{i}-4 \hat{j}+7 \hat{k}$ is 11 cubic unit.

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9. Given that $\vec{u}=\hat{i}-2 \hat{j}+3 \hat{k}$,
$\vec{v}=2 \hat{i}+\hat{j}+4 \hat{k}$,
$\vec{w}=\hat{i}+3 \hat{j}+3 \hat{k}$ and $(\vec{u} \cdot \vec{R}-15) \hat{i}+(\vec{v} \cdot \vec{R}-30) \hat{j}+(\vec{w} \cdot \vec{R}-20) \vec{k}=0$. Then find the greatest integer less than or equal to $|\vec{R}|$.

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10. Let a three dimensional vector $\vec{V}$ satisfy the condition, $2 \vec{V}+\vec{V} \times(\hat{i}+2 \hat{j})=2 \hat{i}+\hat{k}$ If $3|\vec{V}|=\sqrt{m}$ Then find the value of $m$

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11. If $\vec{a}, \vec{b}, \vec{c}$ are unit vectors such that $\vec{a} . \vec{b}=0=\vec{a} . \vec{c}$ and the angle between $\vec{b}$ and $\vec{c}$ is $\frac{\pi}{3}$, then find the value of $|\vec{a} \times \vec{b}-\vec{a} \times \vec{c}|$.

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12. Let $\vec{O} A=\vec{a}, \hat{O} B=10 \vec{a}+2 \vec{b}$ and $\vec{O} C=\vec{b}$, where $O$, Aand $C$ are noncollinear points. Let $p$ denotes the areaof quadrilateral $O A C B$, and let $q$ denote the area of parallelogram with OAandOC as adjacent sides. If $p=k q$, then find $k$

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13. Find the work done by the force $F=3 \hat{i}-\hat{j}-2 \hat{k}$ acrting on a particle such that the particle is displaced from point $A(-3,-4,1) \rightarrow B(-1,-1,-2)$

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14. If $\vec{a}$ and $\vec{b}$ are vectors in space given by $\vec{a}=\frac{\hat{i}-2 \hat{j}}{\sqrt{5}}$ and $\vec{b}=\frac{2 \hat{i}+\hat{j}+3 \hat{k}}{\sqrt{14}}$ then find the value of $(2 \vec{a}+\vec{b}) \cdot[(\vec{a} \times \vec{b}) \times(\vec{a}-2 \vec{b})]$

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15. Let $\vec{a}=-\hat{i}-\hat{k}, \vec{b}=-\hat{i}+\hat{j}$ and $\vec{c}=i+2 \hat{j}+3 \hat{k}$ be three given vectors. If $\vec{r}$ is a vector such that $\vec{r} \times \vec{b}=\vec{c} \times \vec{b}$ and $\vec{r} . \vec{a}=0$ then find the value of $\vec{r} . \vec{b}$.

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16. If $\vec{a}$, $\vec{b}$ and $\vec{c}$ are unit vectors satisfying $|\vec{a}-\vec{b}|^{2}+|\vec{b}-\vec{c}|^{2}+|\vec{c}-\vec{a}|^{2}=9$, then $|2 \vec{a}+5 \vec{b}+5 \vec{c}|$ is.

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17. Let $\vec{a}, \vec{b}$, and $\vec{c}$ be three non coplanar unit vectors such that the angle between every pair of them is $\frac{\pi}{3}$. If $\vec{a} \times \vec{b}+\vec{b} \times \vec{c}=p \vec{a}+q \vec{b}+r \vec{c}$ where $\mathrm{p}, \mathrm{q}, \mathrm{r}$ are scalars then the value of $\frac{p^{2}+2 q^{2}+r^{2}}{q^{2}}$ is

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## Subjective type

1. from a point $O$ inside a triangle $A B C$, perpendiculars, $O D, O E$ and $O F$ are drawn to the sides, $B C, C A$ and $A B$ respectively, prove that the perpendiculars from $\mathrm{A}, \mathrm{B}$ and C to the sides $\mathrm{EF}, \mathrm{FD}$ and DE are concurrent.
2. about to only mathematics

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3. If $c$ is a given non-zero scalar, and $\vec{A}$ and $\vec{B}$ are given non-zero vector such that $\vec{A} \perp \vec{B}$, then find vector $\vec{X}$ which satisfies the equation
$\vec{A} \cdot \vec{X}=c$ and $\vec{A} \times \vec{X}=\vec{B}$

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4. $A, B, C a n d D$ are any four points in the space, then prove that $|\vec{A} B \times \vec{C} D+\vec{B} C \times \vec{A} D+\vec{C} A \times \vec{B} D|=4$ (area of $A B C$ ).

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5. If vectors $\vec{a}, \vec{b}$ and $\vec{c}$ are coplanar, show that $\left|\begin{array}{lll}\vec{a} & \vec{b} & \vec{c} \\ \vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} & \vec{a} \cdot \vec{c} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b} & \vec{b} \cdot \vec{c}\end{array}\right|=\overrightarrow{0}$

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6. Let $\vec{A}=2 \vec{i}+\vec{k}, \vec{B}=\vec{i}+\vec{j}+\vec{k} \quad \vec{C}=4 \hat{i}-3 \hat{j}+7 \hat{k}$ Determine a vector $\vec{R}$ satisfying $\vec{R} \times \vec{B}=\vec{C} \times \vec{B}$ and $\vec{R} . \vec{A}=0$.

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7. Determine the value of $c$ so that for all real $x$, vectors $c x \hat{i}-6 \hat{j}-3 \hat{k}$ and $x \hat{i}+2 \hat{j}+2 c x \hat{k}$ make an obtuse angle with each other.

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8. 

$$
(\vec{a} \times \vec{b}) \times(\vec{c} \times \vec{d})+(\vec{a} \times \vec{c}) \times(\vec{d} \times \vec{b})+(\vec{a} \times \vec{d}) \times(\vec{b} \times \vec{c})=-2[\vec{b} \vec{c} \vec{d}] \vec{a}
$$

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9. $\vec{a}, \vec{b}$ and $\vec{c}$ are vectors of magnitudes 1,1 and 2 , respectively. If $\vec{a} \times(\vec{a} \times \vec{c})+\vec{b}=\overrightarrow{0}$, then acute angle between $\vec{a}$ and $\vec{c}$ is

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10. Let $\vec{a}, \vec{b}$, and $\vec{c}$ be non-coplanar unit vectors, equally inclined to one another at an angle $\theta$ then $[\vec{a} \vec{b} \vec{c}]$ in terms of $\theta$ is equal to :

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11. If $\vec{a}, \vec{b}, \vec{c}$ are vectors such that $|\vec{b}|=|\vec{c}|$ then $\{(\vec{a}+\vec{b}) \times(\vec{a}+\vec{c})\} \times(\vec{b} \times \vec{c}) \cdot(\vec{b}+\vec{c})=$

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12. For any two vectors $\vec{u}$ and $\vec{v}$ prove that $\left(1+|\vec{u}|^{2}\right)\left(1+|\vec{v}|^{2}\right)=(1-\vec{u} \cdot \vec{v})^{2}+|\vec{u}+\vec{v}+(\vec{u} \times \vec{v})|^{2}$

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13. Let $\vec{u}$ and $\vec{v}$ be unit vectors. If $\vec{w}$ is a vector such that $\vec{w}+\vec{w} \times \vec{u}=\vec{v}$, then prove that $|(\vec{u} \times \vec{v}) \cdot \vec{w}| \leq \frac{1}{2}$ and that the equality holds if and only if $\vec{u}$ is perpendicular to $\vec{v}$.

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14. Find 3-dimensional vectors $\vec{v}_{1}, \vec{v}_{2}, \vec{v}_{3} \quad$ satisfying $\vec{v}_{1} \cdot \vec{v}_{1}=4, \vec{v}_{1} \cdot \vec{v}_{2}=-2, \vec{v}_{1} \cdot \vec{v}_{3}=6$, $\vec{v}_{2} \cdot \vec{v}_{2}=2, \vec{v}_{2} \cdot \vec{v}_{3}=-5, \vec{v}_{3} \cdot \vec{v}_{3}=29$
15. Let V be the volume of the parallelopiped formed by the vectors $\vec{a}=a_{1} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}$ and $\vec{b}=b_{1} \hat{i}+b_{2} \hat{j}+b_{3} \hat{k}$ and $\vec{c}=c_{1} \hat{i}+c_{2} \hat{j}+c_{3} \hat{k}$. If $a_{r}, b_{r}$ and $c_{r}$, where $r=1,2,3$, are non-negative real numbers and 3
$\sum_{r=1}\left(a_{r}+b_{r}+c_{r}\right)=3 L$ show that $V \leq L^{3}$

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16. $\vec{u}, \vec{v}$ and $\vec{w}$ are three non-coplanar unit vecrtors and $\alpha, \beta$ and $\gamma$ are the angles between $\vec{u}$ and $\vec{v}$, $\vec{v}$ and $\vec{w}$, and $\vec{w}$ and $\vec{u}$, respectively, and $\vec{x}, \vec{y}$ and $\vec{z}$ are unit vectors along the bisectors of the angles $\alpha, \beta a n d \gamma$, respectively.

Prove that $[\vec{x} \times \vec{y} \vec{y} \times \vec{z} \vec{z} \times \vec{x}]=\frac{1}{16}[\vec{u} \vec{v} \vec{w}]^{2} \sec ^{2}\left(\frac{\alpha}{2}\right) \sec ^{2}\left(\frac{\beta}{2}\right) \sec ^{2}\left(\frac{\gamma}{2}\right)$.

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17. If $\vec{a}, \vec{b}, \vec{c}$ and $\vec{d}$ are distinct vectors such that $\vec{a} \times \vec{c}=\vec{b} \times \vec{d}$ and $\vec{a} \times \vec{b}=\vec{c} \times \vec{d}$. Prove that $(\vec{a}-\vec{d}) \cdot(\vec{b}-\vec{c}) \neq 0$

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18. $P_{1}$ and $P_{2}$ are planes passing through origin $L_{1}$ and $L_{2}$ are two lines on $P_{1}$ and $P_{2}$, respectively, such that their intersection is the origin. Show that there exist points $A, B$ and $C$, whose permutation $A^{\prime}, B^{\prime}$ andC', respectively, can be chosen such that
i) $A$ is on $L_{1}$, BonP $_{1}$ but not on $L_{1}$ and $C$ not on $P_{1}$;
ii) $A^{\prime}$ is on $L_{2}, B^{\prime}$ on $P_{2}$ but not on $L_{2}$ and $C^{\prime}$ not on $P_{2}$

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19. Find the differential equation representing the family of curves $y=a e^{b x+5}$ where a and b are arbitrary constants.

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1. Let $\vec{A}, \vec{B}$ and $\vec{C}$ be vectors of legth, 3,4and 5 respectively. Let $\vec{A}$ be perpendicular to $\vec{B}+\vec{C}, \vec{B}$ to $\vec{C}+\vec{A}$ and $\vec{C}$ to $\vec{A}+\vec{B}$ then the length of vector $\vec{A}+\vec{B}+\vec{C}$ is $\qquad$ .

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2. The unit vector perendicular to the plane determined by $P(1,-1,2)$ , $\mathrm{C}(3,-1,2)$ is $\qquad$ .

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3. the area of the triangle whose vertices are $\mathrm{A}(1,-1,2), \mathrm{B}(1,2,-1), \mathrm{C}(3,-1$,
2) is $\qquad$ .

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4. If $\vec{A}, \vec{B}$ and $\vec{C}$ are three non - coplanar vectors, then
$\vec{A} \cdot \vec{B} \times \vec{C}$ $\vec{B} \cdot \vec{A} \times \vec{C}$
$\vec{C} \times \vec{A} \cdot \vec{B} \quad \vec{C} \cdot \vec{A} \times \vec{B}$
$\qquad$

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5. If $\vec{A}=(1,1,1)$ and $\vec{C}=(0,1,-1)$ are given vectors the vector $\vec{B}$ satisfying the equations $\vec{A} \times \vec{B}=\vec{C}$ and $\vec{A} \cdot \vec{B}=3$ is $\qquad$ .

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6. Let $\vec{b}=4 \hat{i}+3 \hat{j}$ and $\vec{c}$ be two vectors perpendicular to each other in the xy - plane. All vectors in the sme plane having projections 1 and 2 along $\vec{b}$ and $\vec{c}$, respectively, are given by $\qquad$

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7. The components of a vector $\vec{a}$ along and perpendicular to a non-zero vector $\vec{b}$ are $\qquad$ and $\qquad$ , respectively.

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8. A unit vector coplanar with $\vec{i}+\vec{j}+2 \vec{k}$ and $\vec{i}+2 \vec{j}+\vec{k}$ and perpendicular to $\vec{i}+\vec{j}+\vec{k}$ is $\qquad$

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9. A non vector $\vec{a}$ is parallel to the line of intersection of the plane determined by the vectors $\vec{i}, \vec{i}+\vec{j}$ and thepane determined by the vectors $\vec{i}-\vec{j}, \vec{i}+\vec{k}$ then angle between $\vec{a}$ and $\vec{i}-2 \vec{j}+2 \vec{k}$ is $=$ (A) $\frac{\pi}{2}$ (B) $\frac{\pi}{3}$ (C) $\frac{\pi}{6}$ (D) $\frac{\pi}{4}$

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10. Find a unit vector perpendicular to each of the vector $\vec{a}+\vec{b}$ and $\vec{a}-\vec{b}$, where $\vec{a}=3 \hat{i}+2 \hat{j}+2 \hat{k}$ and $\vec{b}=\hat{i}+2 \hat{j}-2 \hat{k}$

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11. let $\vec{a}, \vec{b}$ and $\vec{c}$ be three vectors having magnitudes 1,1 and 2 , respectively, if $\vec{a} \times(\vec{a} \times \vec{c})+\vec{b}=\overrightarrow{0}$, then the acute angle between $\vec{a}$ and $\vec{c}$ is $\qquad$

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12. A, B C and D are four points in a plane with position vectors, $\vec{a}, \vec{b}, \vec{c}$ and $\vec{d}$ respectively, such that $(\vec{a}-\vec{d}) \cdot(\vec{b}-\vec{c})=(\vec{b}-\vec{d}) \cdot(\vec{c}-\vec{a})=0$ then point D is the ___ of triangle $A B C$.

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13. Let $\vec{O} A=\vec{a}, \hat{O} B=10 \vec{a}+2 \vec{b}$ and $\vec{O} C=\vec{b}$, where , AandC are noncollinear points. Let $p$ denotes the areaof quadrilateral $O A C B$, and let $q$ denote the area of parallelogram with $O A a n d O C$ as adjacent sides. If $p=k q$, then find $k$

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14. If $\vec{a}=\hat{j}+\sqrt{3} k, \vec{b}=-\hat{j}+\sqrt{3} \hat{k}$ and $\vec{c}=2 \sqrt{3} \hat{k}$ form a triangle, then the internal angle of the triangle between $\vec{a}$ and $\vec{b}$ is

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## True and false

1. Let $\vec{a}, \vec{b}$ and $\vec{c}$ be unit vectors such that $\vec{a} \cdot \vec{b}=0=\vec{a}$. $\vec{c}$. It the angle between $\vec{b}$ and $\vec{c} i s \frac{\pi}{6}$ then find $\vec{a}$.
2. If $\vec{x} \cdot \vec{a}=0 \vec{x} . \vec{b}=0$ and $\vec{x} \cdot \vec{c}=0$ for some non zeror $\vec{x}$ then show that $[\vec{a} \vec{b} \vec{c}]=0$

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3. for any three vectors, $\vec{a}, \vec{b}$ and $\vec{c},(\vec{a}-\vec{b}) \cdot(\vec{b}-\vec{c}) \times(\vec{c}-\vec{a})=$

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single correct answer type

1. The scalar $\vec{A}((\vec{B}+\vec{C}) \times(\vec{A}+\vec{B}+\vec{C}))$ equals
a. 0 b. $[\vec{A} \vec{B} \vec{C}]+[\vec{B} \vec{C} \vec{A}]$ c. $[\vec{A} \vec{B} \vec{C}]$ d. none of these
A. 0
B. $[\vec{A} \vec{B} \vec{C}]+[\vec{B} \vec{C} \vec{A}]$
C. $[\vec{A} \vec{B} \vec{C}]$
D. none of these

## Answer: a

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2. For non-zero vectors $\vec{a}, \vec{b}$ and $\vec{c},|(\vec{a} \times \vec{b}) \cdot \vec{c}|=|\vec{a}||\vec{b}||\vec{c}|$ holds if and only if
A. A. $\vec{a} \cdot \vec{b}=0, \vec{b} \cdot \vec{c}=0$
B. B. $\vec{b} \cdot \vec{c}=0, \vec{c}, \vec{a}=0$
C. C. $\vec{c} . \vec{a}=0, \vec{a}, \vec{b}=0$
D. D. $\vec{a} \cdot \vec{b}=\vec{b} \cdot \vec{c}=\vec{c} \cdot \vec{a}=0$

Answer: d
3. The volume of he parallelepiped whose sides are given by $\vec{O} A=2 i-2 j, \vec{O} B=i+j-k a n d \vec{O} C=3 i-k$ is a. $\frac{4}{13}$ b. 4 c. $\frac{2}{7}$ d. 2
A. $4 / 13$
B. 4
C. 2/7
D. 2

## Answer: d

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4. Let $\vec{a}$, $\vec{b}$ and $\vec{c}$ be three non-coplanar vectors and $\vec{p}$, $\vec{q} a n d \vec{r}$ the vectors
defined by the relation $\vec{p}=\frac{\vec{b} \times \vec{c}}{[\vec{a} \vec{c}]}, \vec{q}=\frac{\vec{c} \times \vec{a}}{[\vec{a} \vec{b}]}$ and $\vec{r}=\frac{\vec{a} \times \vec{b}}{[\vec{a} \vec{c}]}$ Then the $[\vec{a} \vec{b} \vec{c}] \quad[\vec{a} \vec{b} \vec{c}] \quad[\vec{a} \vec{b} \vec{c}]$
value of the expression $(\vec{a}+\vec{b}) \vec{p}+(\vec{b}+\vec{c}) \vec{q}+(\vec{c}+\vec{a}) \vec{r}$ is 0 b .1 c .2 d .3
A. 0
B. 1
C. 2
D. 3

## Answer: d

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5. Let $\vec{a}=\hat{i}-\hat{j}, \vec{b}=\hat{j}-\hat{k}, \vec{c}=\hat{k}-\hat{i}$. If $\hat{d}$ is a unit vector such that $\vec{a} \cdot \hat{d}=0=[\vec{b} \vec{c} \vec{d}]$ then $\hat{d}$ equals
A. A. $\pm \frac{\hat{i}+\hat{j}-2 \hat{k}}{\sqrt{6}}$
B. В. $\pm \frac{\hat{i}+\hat{j}-\hat{k}}{\sqrt{3}}$
C. C. $\pm \frac{\hat{i}+\hat{j}+\hat{k}}{\sqrt{3}}$
D. D. $\pm \hat{k}$

## Answer: a

## D Watch Video Solution

6. If $\vec{a}, \vec{b}$ and $\vec{c}$ are non-coplanar unit vectors such that $\vec{a} \times(\vec{b} \times \vec{c})=\frac{\vec{b}+\vec{c}}{\sqrt{2}}$, then the angle between $\vec{a}$ and $\vec{b}$ is a. $3 \pi / 4 \mathrm{~b} . \pi / 4 \mathrm{c}$. $\pi / 2 \mathrm{~d} . \pi$
A. $3 \pi / 4$
B. $\pi / 4$
C. $\pi / 2$
D. $\pi$

## Answer: a

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7. Let $\vec{u}, \vec{v}$ and $\vec{w}$ be vectors such that $\vec{u}+\vec{v}+\vec{w}=0$ if $|\vec{u}|=2,|\vec{v}|=3$ and $|\vec{w}|=5$ then $\vec{u} \cdot \vec{v}+\vec{v} \cdot \vec{w}+\vec{w} \cdot \vec{u}$ is
A. 47
B. -19
C. 0
D. 19

Answer: b

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8. If $\vec{a}, \vec{b}$ and $\vec{c}$ are three non coplanar vectors, then $(\vec{a}+\vec{b}+\vec{c})[(\vec{a}+\vec{b}) \times(\vec{a}+\vec{c})]$ is :
A. 0
B. $[\vec{a} \vec{b} \vec{c}]$
C. $2[\vec{a} \vec{b} \vec{c}]$
D. $-[\vec{a} \vec{b} \vec{c}]$

Answer: d

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9. $\vec{p}, \vec{q}$ and $\vec{r}$ are three mutually prependicular vectors of the same magnitude . If vector $\vec{x}$ satisfies the equation $\vec{p} \times((\vec{x}-\vec{q}) \times \vec{p})+\vec{q} \times((\vec{x}-\vec{r}) \times \vec{q})+\vec{r} \times((\vec{x}-\vec{p}) \times \vec{r})=\overrightarrow{0}$ then $\vec{x}$ is given by
A. A. $\frac{1}{2}(\vec{p}+\vec{q}-2 \vec{r})$
B. B. $\frac{1}{2}(\vec{p}+\vec{q}+\vec{r})$
C. C. $\frac{1}{3}(\vec{p}+\vec{q}+\vec{r})$
D. D. $\frac{1}{3}(2 \vec{p}+\vec{q}-\vec{r})$

## Answer: b

10. Let $\vec{a}=2 \hat{i}+\hat{j}-2 \hat{k}$, and $\vec{b}=\hat{i}+\hat{j}$ if c is a vector such that $\vec{a} . \vec{c}=|\vec{c}|,|\vec{c}-\vec{a}|=2 \sqrt{2}$ and the angle between $\vec{a} \times \vec{b}$ and $\vec{c}$ is $30^{\circ}$, then $|(\vec{a} \times \vec{b})| \times \vec{c} \mid$ is equal to
A. A. $2 / 3$
B. B. $3 / 2$
C. C. 2
D. D. 3

Answer: b

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11. Let $\vec{a}=2 i+j+k, \vec{b}=i+2 j-k$ and $a$ unit vector $\vec{c}$ be coplanar. If $\vec{c}$ is pependicular to $\vec{a}$. Find $\vec{c}$.
A. $\frac{1}{\sqrt{2}}(-j+k)$
B. $\frac{1}{\sqrt{3}}(i-j-k)$
C. $\frac{1}{\sqrt{5}}(i-2 j)$
D. $\frac{1}{\sqrt{3}}(i-j-k)$

## Answer: a

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12. If the vectors $\vec{a}, \vec{b}$, and $\vec{c}$ form the sides $B C$, CAand $A B$, respectively, of triangle $A B C$, then
A. $\vec{a} \cdot \vec{b}+\vec{b} \cdot \vec{c}+\vec{c} \cdot \vec{a}=0$
B. $\vec{a} \times \vec{b}=\vec{b} \times \vec{c}=\vec{c} \times \vec{a}$
C. $\vec{a} \cdot \vec{b}=\vec{b} \cdot \vec{c}=\vec{c} \cdot \vec{a}$
D. $\vec{a} \times \vec{b}+\vec{b} \times \vec{c}+\vec{c} \times \vec{a}=\overrightarrow{0}$

## Answer: b

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13. Let vectors $\vec{a}, \vec{b}, \vec{c}$, and $\vec{d}$ be such that $(\vec{a} \times \vec{b}) \times(\vec{c} \times \vec{d})=0$. Let $P_{1} a n d P_{2}$ be planes determined by the pair of vectors $\vec{a}, \vec{b}$, and $\vec{c}, \vec{d}$, respectively. Then the angle between $P_{1}$ andP $P_{2}$ is $0 \mathrm{~b} . \pi / 4 \mathrm{c} . \pi / 3 \mathrm{~d} . \pi / 2$
A. 0
B. $\pi / 4$
C. $\pi / 3$
D. $\pi / 2$

## Answer: a

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14. If $\vec{a}, \vec{b}$ and $\vec{c}$ are unit coplanar vectors, then the scalar triple product $[2 \vec{a}-\vec{b} 2 \vec{b}-\vec{c} 2 \vec{c}-\vec{a}]$ is 0 b. 1 c. $-\sqrt{3}$ d. $\sqrt{3}$
A. 0
B. 1
C. $-\sqrt{3}$
D. $\sqrt{3}$

## Answer: a

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15. If $\hat{a}, \hat{b}$, and $\hat{c}$ are unit vectors, then $|\hat{a}-\hat{b}|^{2}+|\hat{b}-\hat{c}|^{2}+|\hat{c}-\hat{a}|^{2}$ does not exceed
A. 4
B. 9
C. 8
D. 6

## Answer: b

16. If $\vec{a}$ and $\vec{b}$ are two unit vectors such that $\vec{a}+2 \vec{b}$ and $5 \vec{a}-4 \vec{b}$ are perpendicular to each other then the angle between $\vec{a}$ and $\vec{b}$ is
A. $45^{\circ}$
B. $60^{\circ}$
C. $\cos ^{-1}(1 / 3)$
D. $\cos ^{-1}(2 / 7)$

## Answer: b

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17. Let $\vec{V}=2 \hat{i}+\hat{j}-\hat{k}$ and $\vec{W}=\hat{i}+3 \hat{k}$ If $\vec{U}$ is a unit vector, then the maximum value of the scalar triple product $[U V W]$ is a.- 1 b. $\sqrt{10}+\sqrt{6} c . \sqrt{59}$ d. $\sqrt{60}$
A. -1
B. $\sqrt{10}+\sqrt{6}$
C. $\sqrt{59}$
D. $\sqrt{60}$

## Answer: c

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18. Find the value of $a$ so that the volume of the parallelepiped formed by vectors $\hat{i}+a \hat{j}+k, \hat{j}+a \hat{k}$ and $a \hat{i}+\hat{k}$ becomes minimum.
A. -3
B. 3
C. $1 / \sqrt{3}$
D. $\sqrt{3}$

## Answer: c

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19. If $\vec{a}=(\hat{i}+\hat{j}+\hat{k}), \vec{a} \cdot \vec{b}=1$ and $\vec{a} \times \vec{b}=\hat{j}-\hat{k}$, then $\vec{b}$ is
A. $\hat{i}-\hat{j}+\hat{k}$
B. $2 \hat{i}-\hat{k}$
c. $\hat{i}$
D. $2 \hat{i}$

## Answer: c

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20. The unit vector which is orthogonal to the vector $3 \hat{i}+2 \hat{j}+6 \hat{k}$ and is coplanar with vectors $2 \hat{i}+\hat{j}+\hat{k}$ and $\hat{i}-\hat{j}+\hat{k}$ is $\frac{2 \hat{i}-6 \hat{j}+\hat{k}}{\sqrt{41}}$ b. $\frac{2 \hat{i}-3 \hat{j}}{\sqrt{13}}$ c. $\frac{3 \hat{j}-\hat{k}}{\sqrt{10}}$
d. $\frac{4 \hat{i}+3 \hat{j}-3 \hat{k}}{\sqrt{34}}$
A. $\frac{2 \hat{i}-6 \hat{j}+\hat{k}}{\sqrt{41}}$
B. $\frac{2 \hat{i}-3 \hat{j}}{\sqrt{13}}$
c. $\frac{3 \hat{i}-\hat{k}}{\sqrt{10}}$
D. $\frac{4 \hat{i}+3 \hat{j}-3 \hat{k}}{\sqrt{34}}$

## Answer: c

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21. If $\vec{a}, \vec{b}$ and $\vec{c}$ are three nonzero, non- coplanar vectors and
$\vec{b}_{1}=\vec{b}-\frac{\vec{b} \cdot \vec{a}}{|\vec{a}|^{2}} \vec{a}, \vec{b}_{2}=\vec{b}+\frac{\vec{b} \cdot \vec{a}}{|\vec{a}|^{2}} \vec{a}, \vec{c}_{1}=\vec{c}-\frac{\vec{c} \cdot \vec{a}}{|\vec{a}|^{2}} \vec{a}+\frac{\vec{b} \cdot}{\mid \vec{c}} \vec{c}^{2} \vec{b}_{1}$,
$\vec{c}_{2}=\vec{c}-\frac{\vec{c} \cdot \vec{a}}{|\vec{a}|^{2}} \vec{a}-\frac{\vec{b} \vec{c}}{\left|\vec{b}_{1}\right|^{2}} \vec{b}_{1}, \vec{c}_{3}=\vec{c}-\frac{\vec{c} \cdot \vec{a}}{|\vec{c}|^{2}} \vec{a}+\frac{\vec{b} \cdot \vec{c}}{|\vec{c}|^{2}} \vec{b}_{1}$,
$\vec{c}_{4}=\vec{c}-\frac{\vec{c} \cdot \vec{a}}{|\vec{c}|^{2}} \vec{a}=\frac{\vec{b} \cdot \vec{c}}{|\vec{b}|^{2}} \vec{b}_{1}$, then the set of mutually orthogonal vectors is
A. (a) $\left(\vec{a}, \vec{b}_{1}, \vec{c}_{3}\right)$
B. (b) $\left(\vec{a}, \vec{b}_{1}, \vec{c}_{2}\right)$
C. (c) $\left(\vec{a}, \vec{b}_{1}, \vec{c}_{1}\right)$
D. (d) $\left(\vec{a}, \vec{b}_{2}, \vec{c}_{2}\right)$

Answer: c

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22. Let $\vec{a}=\hat{i}+2 \hat{j}+\hat{k}, \vec{b}=\hat{i}-\hat{j}+\hat{k}$ and $\vec{c}=\hat{i}-\hat{j}-\hat{k} \mathrm{~A}$ vector in the plane of $\vec{a}$ and $\vec{b}$ whose projections on $\vec{c}$ is $1 / \sqrt{3}$ is
A. A. $4 \hat{i}-\hat{j}+4 \hat{k}$
B. $B .3 \hat{i}+\hat{j}-3 \hat{k}$
C. C. $2 \hat{i}+\hat{j}-2 \hat{k}$
D. D. $-4 \hat{i}+\hat{j}-4 \hat{k}$

## Answer: a

23. Let two non-collinear unit vector $\hat{a}$ a $\mathrm{n} \mathrm{d} \hat{b}$ form an acute angle. A point $P$ moves so that at any time $t$, the position vector $O P$ (where $O$ is the origin) is given by âcost $+\hat{b} \sin t W h e n P$ is farthest from origin $O$, let $M$ be the length of OPandû be the unit vector along $O P$ Then (a)
$\hat{u}=\frac{\hat{a}+\hat{b}}{|\hat{a}+\hat{b}|} \operatorname{andM}=(1+\hat{a} \hat{b})^{1 / 2}$ (b) $\hat{u}=\frac{\hat{a}-\hat{b}}{|\hat{a}-\hat{b}|}$ andM $=\left(1+\hat{a}^{\wedge}\right)^{1 / 2}$
$\hat{u}=\frac{\hat{a}+\hat{b}}{|\hat{a}+\hat{b}|} \operatorname{andM}=(1+2 \hat{a} \hat{b})^{1 / 2}$ (d) $\hat{u}=\frac{\hat{a}-\hat{b}}{|\hat{a}-\hat{b}|} \operatorname{andM}=(1+2 \hat{a} \hat{b})^{1 / 2}$
A.,$\hat{u}=\frac{\hat{a}+\hat{b}}{|\hat{a}+\hat{b}|}$ and $M=(1+\hat{a} . \hat{b})^{1 / 2}$
B. , $\hat{u}=\frac{\hat{a}-\hat{b}}{|\hat{a}-\hat{b}|}$ and $M=(1+\hat{a} . \hat{b})^{1 / 2}$
C. $\hat{u}=\frac{\hat{a}+\hat{b}}{|\hat{a}+\hat{b}|}$ and $M=(1+2 \hat{a} . \hat{b})^{1 / 2}$
D. $\hat{u}=\frac{\hat{a}-\hat{b}}{|\hat{a}-\hat{b}|}$ and $M=(1+2 \hat{a} . \hat{b})^{1 / 2}$

## Answer: a

24. If $\vec{a}, \vec{b}, \vec{c}$ and $\vec{d}$ are unit vectors such that $(\vec{a} \times \vec{b}) \cdot(\vec{c} \times \vec{d})=1$ and $\vec{a} \cdot \vec{c}=\frac{1}{2}$ then
A. $\vec{a}, \vec{b}$ and $\vec{c}$ are non- coplanar
B. $\vec{b}, \vec{c}$ and $\vec{d}$ are non-coplanar
C. $\vec{b}$ and $\vec{d}$ are non- parallel
D. $\vec{a}$ and $\vec{d}$ are parallel and $\vec{b}$ and $\vec{c}$ are parallel

## Answer: c

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25. Two adjacent sides of a parallelogram $A B C D$ are given by
$\vec{A} B=2 \hat{i}+10 \hat{j}+11 \hat{k}$ and $\vec{A} D=-\hat{i}+2 \hat{j}+2 \hat{k}$ The side $A D$ is rotated by an acute angle $\alpha$ in the plane of the parallelogram so that $A D$ becomes $A D^{\prime}$

If $A D^{\prime}$ makes a right angle with the side $A B$, then the cosine of the angel $\alpha$ is given by $\frac{8}{9}$ b. $\frac{\sqrt{17}}{9}$ c. $\frac{1}{9}$ d. $\frac{4 \sqrt{5}}{9}$
A. $\frac{8}{9}$
B. $\frac{\sqrt{17}}{9}$
C. $\frac{1}{9}$
D. $\frac{4 \sqrt{5}}{9}$

## Answer: b

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26. Let $P, Q, R$ and $S$ be the points on the plane with position vectors $-2 i-j, 4 i, 3 i+3 j a n d-3 i+2 j$, respectively. The quadrilateral PQRS must be (a) Parallelogram, which is neither a rhombus nor a rectangle (b)

Square (c) Rectangle but not a square (d) Rhombus, but not a square
A. Parallelogram, which is neither a rhombus nor a rectangle
B. square
C. rectangle, but not a square
D. rhombus, but not a square.

## Answer: a

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27. Let $\vec{a}=\hat{i}+2 \hat{j}+\hat{k}, \vec{b}=\hat{i}-\hat{j}+\hat{k}$ and $\vec{c}=\hat{i}-\hat{j}-\hat{k} \mathrm{~A}$ vector in the plane of $\vec{a}$ and $\vec{b}$ whose projections on $\vec{c}$ is $1 / \sqrt{3}$ is
A. $\hat{i}-3 \hat{j}+3 \hat{k}$
B. $-3 \hat{i}-3 \hat{j}+\hat{k}$
C. $3 \hat{i}-\hat{j}+3 \hat{k}$
D. $\hat{i}+3 \hat{j}-3 \hat{k}$

## Answer: c

28. Let $\vec{P} R=3 \hat{i}+\hat{j}-2 \hat{k} a n d \vec{S} Q=\hat{i}-3 \hat{j}-4 \hat{k}$ determine diagonals of a parallelogram PQRS, and $\vec{P} T=\hat{i}+2 \hat{j}+3 \hat{k}$ be another vector. Then the volume of the parallelepiped determine by the vectors $\vec{P} T, \vec{P} Q$ and $\vec{P} S$ is 5 b. 20 c. 10 d. 30
A. 5
B. 20
C. 10
D. 30

## Answer: c

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## Multiple correct answers type

1. Let $\vec{a}=a_{1} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}, \vec{b}=b_{1} \hat{i}+b_{2} \hat{j}+b_{3} \hat{k}$ and $\vec{c}=c_{1} \hat{i}+c_{2} \hat{j}+c_{3} \hat{k}$ be three non-zero vectors such that $\vec{c}$ is a unit vector perpendicular to both
$\vec{a}$ and $\vec{b}$. If the angle between $\vec{a}$ and $\vec{b}$ ist/6 then the value of $\left|\begin{array}{lll}a_{1} & b_{1} & c_{1} \\ a_{2} & b_{2} & c_{2} \\ a_{3} & b_{3} & c_{3}\end{array}\right|$ is
A. 0
B. 1
C. $\frac{1}{4}\left(a_{1}^{2}+a_{2}^{2}+a_{2}^{2}\right)\left(b_{1}^{2}+b_{2}^{2}+b_{2}^{2}\right)$
D. $\frac{3}{4}\left(a_{1}^{2}+a_{2}^{2}+a_{2}^{2}\right)\left(b_{1}^{2}+b_{2}^{2}+b_{2}^{2}\right)\left(c_{1}^{2}+c_{2}^{2}+c_{2}^{2}\right)$

## Answer: c

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2. The number of vectors of unit length perpendicular to vectors $\vec{a}=(1,1,0) a n d \vec{b}=(0,1,1)$ is a. one b. two c. three d. infinite
A. one
B. two
C. three
D. infinite

## Answer: b

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3. $\vec{a}=2 \hat{i}-\hat{j}+\hat{k}, \vec{b}=\hat{i}+2 \hat{j}-\hat{k}, \vec{c}=\hat{i}+\hat{j}-2 \hat{k}$ A vector coplanar with $\vec{b}$ and $\vec{c}$ whose projectin on $\vec{a}$ is magnitude $\sqrt{\frac{2}{3}}$ is $2 \hat{i}+3 \hat{j}-3 \hat{k}$ b. $-2 \hat{i}-\hat{j}+5 \hat{k}$ c.
$2 \hat{i}+3 \hat{j}+3 \hat{k} \mathrm{~d} .2 \hat{i}+\hat{j}+5 \hat{k}$
A. $2 \hat{i}+3 \hat{j}-3 \hat{k}$
B. $2 \hat{i}+3 \hat{j}+3 \hat{k}$
C. $-2 \hat{i}-\hat{j}+5 \hat{k}$
D. $2 \hat{i}+\hat{j}+5 \hat{k}$

## Answer: a,c

## D Watch Video Solution

4. For three vectors $\vec{u}, \vec{v} a n d \vec{w}$ which of the following expressions is not equal to any of the remaining three ? $\vec{u} \vec{v} \times \vec{w} \mathrm{~b} .(\vec{v} \times \vec{w}) \vec{u}$ c. $\vec{v} \vec{u} \times \vec{w} \mathrm{~d}$. $(\vec{u} \times \vec{v}) \vec{w}$
A. $\vec{u} .(\vec{v} \times \vec{w})$
B. $(\vec{v} \times \vec{w}) \cdot \vec{u}$
C. $\vec{v} \cdot(\vec{u} \times \vec{w})$
D. $(\vec{u} \times \vec{v}) \cdot \vec{w}$

## Answer: c

## D Watch Video Solution

5. Which of the following expressions are meaningful? a. $\vec{u} \cdot(\vec{v} \times \vec{w})$ b. $\vec{u} \cdot \vec{v} \cdot \vec{w} \mathrm{c} \cdot(\vec{u} \vec{v}) \cdot \vec{w} \mathrm{~d} \cdot \vec{u} \times(\vec{v} \cdot \vec{w})$
A. $\vec{u} .(\vec{v} \times \vec{w})$
B. $(\vec{u} \cdot \vec{v}) \cdot \vec{w}$
C. $(\vec{u} \cdot \vec{v}) \vec{w}$
D. $\vec{u} \times(\vec{v} . V e c w)$

## Answer: a,c

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6. $\vec{a}$ and $\vec{b}$ are two non - collinear unit vectors, and $\vec{u}=\vec{a}-(\vec{a} \cdot \vec{b}) \vec{b}$ and $\vec{v}=\vec{a} \times \vec{b}$. then $|\vec{v}|$ is
A. $|\vec{u}|+\vec{u} .(\vec{a} \times \vec{b})$
B. $|\vec{u}|+|\vec{u} . \vec{a}|$
C. $|\vec{u}|+|\vec{u} \cdot \vec{b}|$
D. $|\vec{u}|+\vec{u} \cdot(\vec{a}+\vec{b})$

## Answer: a,c

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7. Find the modulus of the Vector $\frac{1}{3}(2 \hat{i}-2 \hat{j}+\hat{k})$ is

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8. Let $\vec{A}$ be a vector parallel to the line of intersection of planes $P_{1} a n d P_{2}$ Plane $P_{1}$ is parallel to vectors $2 \hat{j}+3 \hat{k} a n d 4 \hat{j}-3 k a n d P_{2}$ is parallel to $\hat{j}-\hat{k} a n d 3 \hat{i}+3 \dot{j}$ Then the angle betweenvector $\vec{A}$ and a given vector $2 \hat{i}+\hat{j}-2 \hat{k}$ is $\pi / 2$ b. $\pi / 4$ c. $\pi / 6$ d. $3 \pi / 4$
A. $\pi / 2$
B. $\pi / 4$
C. $\pi / 6$
D. $3 \pi / 4$

## Answer: b,d

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9. The vector(s) which is/are coplanar with vectors $\hat{i}+\hat{j}+2 \hat{k}$ and $\hat{i}+2 \hat{j}+\hat{k}$, and perpendicular to vector $\hat{i}+\hat{j}+\hat{k}$, is/are a. $\hat{j}-\hat{k}$ b. $-\hat{i}+\hat{j}$ c. $\hat{i}-\hat{j}$ d. $-\hat{j}+\hat{k}$
A. $\hat{j}-\hat{k}$
B. $-\hat{i}+\hat{j}$
C. $\hat{i}-\hat{j}$
D. $-\hat{j}+\hat{k}$

## Answer: a,d

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10. Let $\vec{x}, \vec{y}$ and $\vec{z}$ be three vector each of magnitude $\sqrt{2}$ and the angle between each pair of them is $\frac{\pi}{3}$. if vcea is a non - zero vector perpendicular to $\vec{x}$ and $\vec{y} \times \vec{z}$ and $\vec{b}$ is a non-zero vector perpendicular to $\vec{y}$ and $\vec{z} \times \vec{x}$, then
A. $\vec{b}=(\vec{b} \cdot \vec{z})(\vec{z}-\vec{x})$
B. $\vec{a}=(\vec{a} \cdot \vec{y})(\vec{y}-\vec{z})$
C. $\vec{a} \cdot \vec{b}=-(\vec{a} \cdot \vec{y})(\vec{b} \cdot \vec{z})$
D. $\vec{a}=(\vec{a} \cdot \vec{y})(\vec{z}-\vec{y})$

## Answer: a,b,c

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11. 

Let
$\triangle P Q R$
be
a triangle
Let
$\vec{a}=Q R, \vec{b}=R P$ and $\vec{c}=P Q$ if $|\vec{a}|=12,|\vec{b}|=4 \sqrt{3}$ and $\vec{b} . \vec{c}=24$, then which of the following is (are) true ?
A. $\frac{|\vec{c}|^{2}}{2}-|\vec{a}|=12$
B. $\frac{|\vec{c}|^{2}}{2}-|\vec{a}|=30$
C. $|\vec{a} \times \vec{b}+\vec{c} \times \vec{a}|=48 \sqrt{3}$
D. $\vec{a} \cdot \vec{b}=-72$

## Answer: a,c,d

## - Watch Video Solution

