



MATHS

BOOKS - CENGAGE PUBLICATION

GRAPHS OF POLYNOMIAL AND RATIONAL FUNCTIONS



1. Draw the rough sketch of the curve $y = (x-1)^2(x-3)^3$.

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2. Draw a rough sketch of the curve y= $(x-1)^2(x-2)(x-3)^3$





root(s) of the equation $x^3 - x^2 + x - 2 = 0$. Also locate the root.

7. Sketch the graph of the following functions y = f(x) and find the number of real roots of the corresponding equation f(x) = 0.

 $(i)f(x)=2x^3-9x^2+12x-(9/2)$ $(ii)f(x)=2x^3-9x^2+12x-3$



8. Draw the graph of $y = x^4 + 2x^2 - 8x + 3$

Find the number of real roots of the equation $x^4 + 2x^2 - 8x + 3 = 0$.

Also find the sum of the integral parts of all real roots.

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9. Let $a \in R$ and let $f: R^{\longrightarrow}$ be given by $f(x) = x^5 - 5x + a$, then (a) f(x) has three real roots if a > 4 (b)f(x) has only one real roots if a > 4(c)f(x) has three real roots if a < -4 (d)f(x) has three real roots if '-4



11. Find the area bounded by the curves $y=\sqrt{1-x^2}$ and $y=x^3-x$

without using integration.

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12. Draw the graph of $f(x) = 4x^3 - 3x$ and hence draw the graph of $g(x) = \cos^{-1} \bigl(4x^3 - 3x \bigr).$

13. Let
$$f(x) = 1 + 4x - x^2, \ orall x \in R$$
 $g(x) = \max \ \{f(t), x \le t \le (x+1), 0 \le x < 3\} = \min \ \{(x+3), 3 \le x$ Verify conntinuity of g(x), for all $x \in [0, 5]$



14. Find the value of a if $x^3 - 3x + a = 0$ has three distinct real roots.

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15. If t is a real number satisfying the equation $2t^3 - 9t^2 + 30 - a = 0$, then find the values of the parameter a for which the equation $x + \frac{1}{x} = t$ gives six real and distinct values of x.

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16. Let $f(x) = x^3 - 9x^2 + 24x + c = 0$ have three real and distinct roots lpha, eta and λ .

(i) Find the possible values of c.

(ii) If $[lpha]+[eta]+[\lambda]=8$, then find the values of c, where $[\ \cdot\]$ represents

the greatest integer function.

(ii) If $[lpha]+[eta]+[\lambda]=$ 7, then find the values of c, where $[\ \cdot\]$ represents

the greatest integer functions



17. Draw the graph of
$$y=f(x)=rac{x+1}{x^2+1}$$

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18. Draw the graph of
$$y = rac{x-1}{x^2}$$
 and hence the graph of $y = rac{|x-1|}{x^2}$.

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19. Write a possible rational function f that has a vertical asymptote at x =

2, a horizontal asymptote y = 3 and a zero at x = -5. Also draw the graph of



a horizontal asymptote at y = -4 and with no x-intercept.

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21. Draw the graph of
$$y=f(x)=rac{x+1}{x^2+1}$$

22. Draw the graph of the function
$$f: R - \{-1, 1\} \rightarrow R.$$
 $f(x) = \frac{x}{1 - |x|}.$

23. Draw the graph of
$$f(x) = rac{1}{x^2-2x+2}.$$

24. From the graph of
$$y = x^2 - 4$$
, draw the graph of $y = \frac{1}{x^2 - 4}$.

•

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25. Draw the graph of
$$y=x^2+rac{1}{x^2}, x
eq 0.$$

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26. Draw the graph of
$$f(x) = \left| rac{x^2-2}{x^2-1}
ight|$$

27. Draw the graph of
$$y = \cos^{-1} \cdot rac{1-x^2}{1+x^2}$$



31. Draw the graph of
$$y=rac{x^3}{3(x+1)}$$

32. Draw the graph of
$$y = \frac{1}{x} + \frac{1}{x-2}$$
.
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33. Find the greatest value of $f(x) = \frac{1}{2ax - x^2 - 5a^2} \in [-3, 5]$ depending upon the parameter a .
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Exercises
1. Draw the graph of $y = (x - 1)(x^2 - x + 1)$.
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2. Draw the graph of
$$y=\left(x^2-x^5
ight)\left(x-2
ight)^3$$
.

3. Let P and Q be any two points. Find the coordinates of the point R which divides PQ externally in the ratio 2:1 and verify that Q is the mid point of PR.

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4. Draw the graphs of

(i)
$$y = x^2(x-1)|x-2|$$

(ii)
$$y=x^3(x-1)|x-2|$$

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5. Write a possible rational function h with a hole at x = 5, a vertical asymptote at x = -1, a horizontal asymptote at y = 2 and x-intercept at x = -1.



6. Draw the graph of
$$y=f(x)=rac{x^2}{x^2+1}.$$

7. Draw graph of
$$y=rac{x^2-6x+4}{x^2+2x+4}$$

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8. Draw the graph of
$$f(x)=rac{x^2-8x+15}{x^2-2x}.$$

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9. Draw the graph of
$$f(x)=rac{5x^2}{\left(x-1
ight)^3}$$
 .

10. Draw the graph of
$$f(x)=rac{2|x-1|}{x^2+1}.$$

11. Draw the graph of
$$y=rac{1}{x+1}+rac{1}{x}+rac{1}{x-2}$$
 .

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12. Draw the graph of
$$y=x+rac{1}{x}$$

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13. Draw the graph of
$$y = rac{(x+6)(x+2)x(x-2)}{(x-3)(x^2-x+1)}.$$

14. Draw the graph of
$$y=rac{1}{x^2}.$$

15. Draw graph of
$$y=rac{x^3-2x^2}{3{(x+1)}^2}.$$

16. Draw graph of
$$y=rac{x^3-5x}{x^2+1}.$$

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17. Given $C_1 < C_2 < C_3 < C_4 < C_5$ and the function y = f(x) is twice differentiable .

f'(x) > 0 for $x \in (C_2, C_4)$, $f'(C_2) = f'(C_4) = 0$ and f'(x) < 0 for all the remaining values. Also $f''(C_1) = f''(C_3) = f''(C_5) = 0$ and f''(x) > 0 for $x \in (C_1, C_3) \cup (C_5, \infty)$ and f''(x) < 0 for remaining values. Answer the following:

(i) What is the minimum number of asymptotes parallel to the x-axis for

y = f(x)?

(ii) What is the maximum number of asymptotes parallel to the x-axis of y = f(x)? (iii) If the range of y = f(x) is $[a, b], a, b \in R$, then what is the minimum number of asymptotes parallel to the x-axis of y = f(x)? (iv) If the range of y = f(x) is non-finite interval, then what is the

maximum number of asymptotes parallel to the x-axis ?

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