



# MATHS

## **BOOKS - CENGAGE PUBLICATION**

## **INTRODUCTION TO VECTORS**

#### Illustration 1

**1.** The vector 
$$\overrightarrow{a} + \overrightarrow{b}$$
 bisects the angle between the vectors  $\widehat{a}$  and  $\widehat{b}$  if  
(A)  $|\overrightarrow{a}| + |\overrightarrow{b}| = 0$  (B) angle between  $\overrightarrow{a}$  and  $\overrightarrow{b}$  is zero (C)  
 $|\overrightarrow{a}| = |\overrightarrow{b}| = 0$  (D) none of these



**1.** if  $\overrightarrow{A}o + \overrightarrow{O}B = \overrightarrow{B}O + \overrightarrow{O}C$ , than prove that B is the midpoint of AC.



**Illustration 3** 

**1.** 
$$ABCDE$$
 is pentagon, prove that  $\overrightarrow{A}B + \overrightarrow{B}C + \overrightarrow{C}D + \overrightarrow{D}E + \overrightarrow{E}A = \overrightarrow{0}$   
 $\overrightarrow{A}B + \overrightarrow{A}E + \overrightarrow{B}C + \overrightarrow{D}C + \overrightarrow{E}D + \overrightarrow{A}C = 3\overrightarrow{A}C$ 

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### Illustration 4

**1.** Prove that the resultant of two forces acting at point O and represented by  $\overrightarrow{OB}$  and  $\overrightarrow{OC}$  is given by  $2\overrightarrow{OD}$ , where D is the midpoint of BC.

1. Prove that the sum of all vectors drawn from the centre of a regular

octagon to its vertices is the zero vector.

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### Illustration 6

**1.** ABC is a triangle and P any point on BC. if  $\overrightarrow{P}Q$  is the sum of  $\overrightarrow{A}P + \overrightarrow{P}B$ + $\overrightarrow{P}C$ , show that ABPQ is a parallelogram and Q, therefore, is a fixed point.



**1.** Two forces  $\overrightarrow{A}B$  and  $\overrightarrow{A}D$  are acting at vertex A of a quadrilateral ABCD and two forces  $\overrightarrow{C}B$  and  $\overrightarrow{C}D$  at C prove that their resultant is given by 4  $\overrightarrow{E}F$ , where E and F are the midpoints of AC and BD, respectively.

### **Illustration 8**

**1.** If  $O(\overrightarrow{0})$  is the circumcentre and O' the orthocentre of a triangle ABC, then prove that i.  $\overrightarrow{OA} + \overrightarrow{OB} + \overrightarrow{OC} = \overrightarrow{OO'}$ ii.  $\overrightarrow{O'A} + \overrightarrow{O'B} + \overrightarrow{O'C} = 2\overrightarrow{O'O}$ iii.  $\overrightarrow{AO'} + \overrightarrow{O'B} + \overrightarrow{O'C} = 2\overrightarrow{AO} = \overrightarrow{AP}$ 

where AP is the diameter through A of the circumcircle.



**1.** A unit vector of modulus 2 is equally inclined to x - and y -axes angle at

an angle  $\pi/3$  . Find the length of projection of the vector on the z -axis.



1. Find a vector of magnitude 8 units in the direction of the vector  $\Big(5\hat{i}-\hat{j}+2\hat{k}\Big).$ 

**1.** Find the unit vector in the direction of vector  $\overrightarrow{PQ}$ , where P and Q are the points (1, 2, 3) and (4, 5, 6), respectively.



Illustration 13

**1.** If 
$$\overrightarrow{a} = \left(-\hat{i} + \hat{j} - \hat{k}\right)$$
 and  $\overrightarrow{b} = \left(2\hat{i} - 2\hat{j} + 2\hat{k}\right)$  then find the unit vector in the direction of  $\left(\overrightarrow{a} + \overrightarrow{b}\right)$ .

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**1.** Show that the points A, B and C having position vectors  $(3\hat{i} - 4\hat{j} - 4\hat{k}), (2\hat{i} - \hat{j} + \hat{k})$  and  $(\hat{i} - 3\hat{j} - 5\hat{k})$  respectively, from the

vertices of a right-angled triangle.

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#### **Illustration 15**

**1.** If  $2\overrightarrow{A}C = 3\overrightarrow{C}B$ , then prove that  $2\overrightarrow{O}A = 3\overrightarrow{C}B$  then prove that  $2\overrightarrow{O}A + 3$  $\overrightarrow{O}B = 5\overrightarrow{O}C$  where O is the origin.

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**Illustration 16** 

1. Prove that points  $\hat{i}+2\hat{j}-3\hat{k}, 2\hat{i}-\hat{j}+\hat{k}$  and  $2\hat{i}+5\hat{j}-\hat{k}$  form a

#### triangle in space.



#### Illustration 17

**1.** Find the position vector of a point R which divides the line joining the point  $P(\hat{i} + 2\hat{j} - \hat{k})$  and  $Q(-\hat{i} + \hat{j} + \hat{k})$  in the ratio 2:1, (i) internally and (ii) externally.

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#### **Illustration 18**

**1.** If  $\overrightarrow{a}, \overrightarrow{b}, \overrightarrow{c}, \overrightarrow{d}$  are the position vectors of points A, B, C and D, respectively referred to the same origin O such that no three of these points are collinear and  $\overrightarrow{a} + \overrightarrow{c} = \overrightarrow{b} + \overrightarrow{d}$ , then prove that quadrilateral ABCD is a parallelogram.



**1.** i. Show that the lines joining the vertices of a tetrahedron to the centroids of opposite faces are concurrent.









**1.** If in parallelogram ABCD, diagonal vectors are  $\overrightarrow{AC} = 2\hat{i} + 3\hat{j} + 4\hat{k}$  and  $\overrightarrow{BD} = -6\hat{i} + 7\hat{j} - 2\hat{k}$ , then find the adjacent side vectors  $\overrightarrow{AB}$  and  $\overrightarrow{AD}$ .

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1. If two sides of a triangle are  $\hat{i}+2\hat{j}$  and  $\hat{i}+\hat{k}$ , then find the length of

the third side.



### Illustration 27

**1.** Three coinitial vectors of magnitudes a, 2a and 3a meet at a point and their directions are along the diagonals if three adjacent faces if a cube. Determined their resultant R. Also prove that the sum of the three vectors determinate by the diagonals of three adjacent faces of a cube passing through the same corner, the vectors being directed from the corner, is twice the vector determined by the diagonal of the cube.

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**1.** A stone is projectef from level ground such that its horizontal and vertical components of initial velocity are  $u_x = 10 \frac{m}{s}$  and  $u_y = 20 \frac{m}{s}$  respectively. Then the angle between velocity vector of stone one second before and one second after it attains maximum height is:

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### Illustration 29

**1.** If the resultant of two forces is equal in magnitude to one of the components and perpendicular to it direction, find the other components using the vector method.



**1.** A man travelling towards east at 8km/h finds that the wind seems to blow directly from the north On doubling the speed, he finds that it appears to come from the north-east. Find the velocity of the wind.

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#### **Illustration 31**

**1.** OABCDE is a regular hexagon of side 2 units in the XY-plane in the first quadrant. O being the origin and OA taken along the x-axis. A point P is taken on a line parallel to the z-axis through the centre of the hexagon at a distance of 3 unit from O in the positive Z direction. Then find vector AP.





### **Illustration 35**

**1.** Let  $\overrightarrow{a}$ ,  $\overrightarrow{b}$  and  $\overrightarrow{c}$  be three non-zero vectors which are positive noncollinear. If  $\overrightarrow{a} + 3\overrightarrow{b}$  is collinear with  $\overrightarrow{c}$  and  $\overrightarrow{b} + 2\overrightarrow{c}$  is collinear with  $\overrightarrow{a}$ then  $\overrightarrow{a}$  then  $\overrightarrow{a} + 3\overrightarrow{b} + 6\overrightarrow{c}$  is:

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### **Illustration 36**

**1.** i. Prove that the points  $\overrightarrow{a} - 2\overrightarrow{b} + 3\overrightarrow{c}, 2\overrightarrow{a} + 3\overrightarrow{b} - 4\overrightarrow{c}$  and  $-7\overrightarrow{b} + 10\overrightarrow{c}$  are collinear, where  $\overrightarrow{a}, \overrightarrow{b}$  and  $\overrightarrow{c}$  are non-coplanar. ii. Prove that the points A(1, 2, 3), B(3, 4, 7) and C(-3, -2, -5)are collinear. Find the ratio in which point C divides AB.

### Illustration 37

1. Check whether the given three vectors are coplnar or non- coplanar :

$$-2\hat{i}-2\hat{j}+4\hat{k},\ -2\hat{i}+4\hat{j}-2\hat{k},4\hat{i}-2\hat{j}-2\hat{k}.$$

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## Illustration 38

1.	Prove	that	the	four		points
$6\hat{i}$ –	$7\hat{j}, 16\hat{i}-19\hat{j}-$	$4\hat{k},3\hat{j}-6\hat{k}$	and $2\hat{i} + 5\hat{j}$	$+ \ 10 \hat{k}$	form	а

tetrahedron in spacel.



**1.** If  $\overrightarrow{a}$  and  $\overrightarrow{b}$  are two non-collinear vectors, show that points  $l_1\overrightarrow{a} + m_1\overrightarrow{b}, l_2\overrightarrow{a} + m_2\overrightarrow{b}$  and  $l_3\overrightarrow{a} + m_3\overrightarrow{b}$  are collinear if  $|l_1l_2l_3m_1m_2m_3111| = 0.$ 

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#### **Illustration 40**

**1.** The vectors  $\overrightarrow{a}$  and  $\overrightarrow{b}$  are non collinear. Find for what value of x the vectors  $\overrightarrow{c} = (x-2)\overrightarrow{a} + \overrightarrow{b}$  and  $\overrightarrow{d} = (2x+1)\overrightarrow{a} - \overrightarrow{b}$  are collinear.? View Text Solution

### **Illustration 41**

1. The median AD of the triangle ABC is bisected at E and BE meets AC at F.

#### Find AF:FC.

### Illustration 42

**1.** Prove that the necessary and sufficient condition for any four points in three-dimensional space to be coplanar is that there exists a liner relation connecting their position vectors such that the algebraic sum of the coefficients (not all zero) in it is zero.

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### **Illustration 43**

**1.** i. If 
$$\overrightarrow{a}, \overrightarrow{b}$$
 and  $\overrightarrow{c}$  are non-coplanar vectors, prove that vectors  $3\overrightarrow{a} - 7\overrightarrow{b} - 4\overrightarrow{c}, 3\overrightarrow{a} - 2\overrightarrow{b} + \overrightarrow{c}$  and  $\overrightarrow{a} + \overrightarrow{b} + 2\overrightarrow{c}$  are coplanar.

**1.** If  $\overrightarrow{a}$ ,  $\overrightarrow{b}$  and  $\overrightarrow{c}$  are non-coplanar vectors, prove that the four points  $2\overrightarrow{a} + 3\overrightarrow{b} - \overrightarrow{c}$ ,  $\overrightarrow{a} - 2\overrightarrow{b} + 3\overrightarrow{c}$ ,  $3\overrightarrow{a} + 4\overrightarrow{b} - 2\overrightarrow{c}$  and  $\overrightarrow{a} - 6\overrightarrow{b} + 6\overrightarrow{c}$ 

are coplanar.

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### **Illustration 45**

**1.** let P an interioer point of a triangle ABC and AP, BP, CP meets the

sides BC, CA, AB in D, E, F, respectively, Show that  $\frac{AP}{PD} = \frac{AF}{FB} + \frac{AE}{EC}$ .



**1.** Points 
$$A(\overrightarrow{a}), B(\overrightarrow{b}), C(\overrightarrow{c}) and D(\overrightarrow{d})$$
 are relates as  $x\overrightarrow{a} + y\overrightarrow{b} + z\overrightarrow{c} + w\overrightarrow{d} = 0$  and

x + y + z + w = 0, where x, y, z, and w are scalars (sum of any two of x, y, znadw is not zero). Prove that if A, B, CandD are concylic, then  $|xy| \left| \overrightarrow{a} - \overrightarrow{b} \right|^2 = |wz| \left| \overrightarrow{c} - \overrightarrow{d} \right|^2$ .

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**Concept Application Exercise 11** 

**1.** Find the unit vector in the direction of the vector  $\overrightarrow{a} = \hat{i} + \hat{j} + 2\hat{k}.$ 



**3.** Find the direction cosines of the vector joining the points A(1, 2, -3) and B(-1, -2, 1) directed from A to B.



5. Given three points are A(-3, -2, 0), B(3, -3, 1) and C(5, 0, 2). Then find a vector having the same direction as that of  $\overrightarrow{A}B$  and magnitude equal to  $|\overrightarrow{A}C|$ .

6. Find a vector of magnitude 5 units, and parallel to the resultant of the

vectors

$$\overrightarrow{a} = 2\hat{i} + 3\hat{j} - \hat{k} ext{ and } \overrightarrow{b} = \hat{i} - 2\hat{j} + \hat{k}.$$

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**7.** Show that the points A(1, -2, -8), B(5, 0, -2) and C(11, 3, 7)

are collinear, and find the ratio in which B divides AC.

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8. If ABCD is a rhombus whose diagonals cut at the origin O, then proved that  $\overrightarrow{O}A + \overrightarrow{O}B + \overrightarrow{O}C + \overrightarrow{O}D + \overrightarrow{O}$ .

**9.** Let D, EandF be the middle points of the sides BC, CAandAB, respectively of a triangle ABC. Then prove that  $\overrightarrow{A}D + \overrightarrow{B}E + \overrightarrow{C}F = \overrightarrow{0}$ .

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**10.** Let ABCD be a p[arallelogram whose diagonals intersect at P and let O be the origin. Then prove that  $\overrightarrow{O}A + \overrightarrow{O}B + \overrightarrow{O}C + \overrightarrow{O}D = 4\overrightarrow{O}P$ .

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**11.** If ABCD is quadrilateral and EandF are the mid-points of ACandBD respectively, prove that  $\overrightarrow{A}B + \overrightarrow{A}D + \overrightarrow{C}B + \overrightarrow{C}D = 4\overrightarrow{E}F$ .

**12.** If  $\overrightarrow{A}O + \overrightarrow{O}B = \overrightarrow{B}O + \overrightarrow{O}C$ , then A, BnadC are (where O is the origin) a. coplanar b. collinear c. non-collinear d. none of these

**13.** If the sides of an angle are given by vectors  $\vec{a} = \hat{i} - 2\hat{j} + 2\hat{k}$  and  $\vec{b} = 2\hat{i} + \hat{j} + 2\hat{k}$ , then find the internal bisector of the angle.

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14. ABCD is a parallelogram. If LandM are the mid-points of BCandDC respectively, then express  $\overrightarrow{A}Land\overrightarrow{A}M$  in terms of  $\overrightarrow{A}Band\overrightarrow{A}D$ . Also, prove that  $\overrightarrow{A}L + \overrightarrow{A}M = \frac{3}{2}\overrightarrow{A}C$ .

**15.** ABCD is a quadrilateral and E and the point intersection of the lines joining the middle points of opposite side. Show that the resultant of  $\overrightarrow{O}A, \overrightarrow{O}B, \overrightarrow{O}Cand\overrightarrow{O}D$  is equal to  $\overrightarrow{O}E$ , where O is any point.

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**16.** What is the unit vector parallel to  $\vec{a} = 3\hat{i} + 4\hat{j} - 2\hat{k}$ ? What vector should be added to  $\vec{a}$  so that the resultant is the unit vector  $\hat{i}$ ?

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17. The position vectors of points A and B w.r.t. the origin are  $\vec{a} = \hat{i} + 3\hat{j} - 2\hat{k}$  and  $\vec{b} = 3\hat{i} + \hat{j} - 2\hat{k}$ , respectively. Determine vector  $\overrightarrow{OP}$  which bisects angle AOB, where P is a point on AB.

**18.** If  $\overrightarrow{r}_1, \overrightarrow{r}_2, \overrightarrow{r}_3$  are the position vectors off thee collinear points and scalar *pandq* exist such that  $\overrightarrow{r}_3 = p\overrightarrow{r}_1 + q\overrightarrow{r}_2$ , then show that p+q=1.

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**19.** If  $\overrightarrow{a}$  and  $\overrightarrow{b}$  are two vectors of magnitude 1 inclined at  $120^{\circ}$ , then find the angle between  $\overrightarrow{b}$  and  $\overrightarrow{b} - \overrightarrow{a}$ .

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20. Find the vector of magnitude 3, bisecting the angle between the

vectors 
$$\overrightarrow{a} = 2\hat{i} + \hat{j} - \hat{k} ext{ and } \overrightarrow{b} = \hat{i} - 2\hat{j} + \hat{k}.$$

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**Concept Application Exercise 12** 

**1.** If  $\overrightarrow{a}$ ,  $\overrightarrow{b}$ ,  $\overrightarrow{c}$  and  $\overrightarrow{d}$  are four vectors in three-dimensional space with the same initial point and such that  $3\overrightarrow{a} + 2\overrightarrow{b} + \overrightarrow{c} - 2\overrightarrow{d} = 0$ , Find the point at which ACandBD meet. Find the ratio in which P divides ACandBD.



**3.** Examine the following vectors for linear independence :

$$\begin{array}{l} \overrightarrow{i},\overrightarrow{i}+\overrightarrow{j}+\overrightarrow{k},2\overrightarrow{i}+\overrightarrow{j}-\overrightarrow{k},-\overrightarrow{i}-2\overrightarrow{j}+2\overrightarrow{k}\\ \overrightarrow{i},3\overrightarrow{i}+\overrightarrow{j}-\overrightarrow{k},2\overrightarrow{i}-\overrightarrow{j}+7\overrightarrow{k},7\overrightarrow{i}-\overrightarrow{j}+13\overrightarrow{k} \end{array}$$

**4.** If  $\overrightarrow{a}$  and  $\overrightarrow{b}$  are non-collinear vectors and  $\overrightarrow{A} = (p+4q)\overrightarrow{a} + (2p+q+1)\overrightarrow{b}$  and  $\overrightarrow{B} = (-2p+q+2)\overrightarrow{a} + (2p-3q)$ , and if  $3\overrightarrow{A} = 2\overrightarrow{B}$ , then determine p and q.

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5. If  $\overrightarrow{a}$ ,  $\overrightarrow{b}$  and  $\overrightarrow{c}$  are any three non-coplanar vectors, then prove that points  $l_1\overrightarrow{a} + m_1\overrightarrow{b} + n_1\overrightarrow{c}$ ,  $l_2\overrightarrow{a} + m_2\overrightarrow{b} + n_2\overrightarrow{c}$ ,  $l_3\overrightarrow{a} + m_3\overrightarrow{b} + n_3\overrightarrow{c}$ ,  $l_4\overrightarrow{a} + m_4$ are coplanar if  $\begin{vmatrix} l_1 & l_2 & l_3 & l_4 \\ m_1 & m_2 & m_3 & m_4 \\ n_1 & n_2 & n_3 & n_4 \\ 1 & 1 & 1 & 1 \end{vmatrix} = 0$ 

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**6.** If  $\overrightarrow{a}$ ,  $\overrightarrow{b}$  and  $\overrightarrow{c}$  are three non-zero, non-coplanar vectors, then find the linear relation between the following four vectors :

$$\overrightarrow{a} - 2\overrightarrow{b} + 3\overrightarrow{c}, 2\overrightarrow{a} - 3\overrightarrow{b} + 4\overrightarrow{c}, 3\overrightarrow{a} - 4\overrightarrow{b} + 5\overrightarrow{c}, 7\overrightarrow{a} - 11\overrightarrow{b} + 15\overrightarrow{c}$$

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7. Let a, b, c be distinct non-negative numbers and the vectors  $a\hat{i} + a\hat{j} + c\hat{k}$ ,  $\hat{i} + \hat{k}$ ,  $c\hat{i} + c\hat{j} + b\hat{k}$  lie in a plane, and then prove that the quadratic equation  $ax^2 + 2cx + b = 0$  has equal roots.

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#### **Subjective**

**1.** The position vectors of the vertices A, B and C of triangle are  $\hat{i} + \hat{j}, \hat{j} + \hat{k}$  and  $\hat{i} + \hat{k}$ , respectively. Find the unit vectors  $\hat{r}$  lying in the plane of ABC and perpendicular to IA, where I is the incentre of the triangle.

**2.** A ship is sailing towards the north at a speed of 1.25 m/s. The current is taking it towards the east at the rate of 1 m/s and a sailor is climbing a vertical pole on the ship at the rate of 0.5 m/s. Find the velocity of the sailor in space.

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**3.** Given four points  $P_1, P_2, P_3 and P_4$  on the coordinate plane with origin

O which satisfy the condition  $\left(\overrightarrow{OP}\right)_{n-1} + \left(\overrightarrow{OP}\right)_{n+1} = \frac{3}{2}\overrightarrow{OP}_n$ . If P1

and P2 lie on the curve xy=1, then prove that P3 does not lie on the curve

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**4.** ABCD is a tetrahedron and O is any point. If the lines joining O to the vertices meet the opposite faces at P, Q, RandS, prove that  $\frac{OP}{AP} + \frac{OQ}{BQ} + \frac{OR}{CR} + \frac{OS}{DS} = 1.$ 

**5.** A pyramid with vertex at point P has a regular hexagonal base ABCDEF, Position vector of points A and B are  $\hat{i}$  and  $\hat{i} + 2\hat{j}$  The centre of base has the position vector  $\hat{i} + \hat{j} + \sqrt{3}\hat{k}$ . Altitude drawn from P on the base meets the diagonal AD at point G. find the all possible position vectors of G. It is given that the volume of the pyramid is  $6\sqrt{3}$  cubic units and AP is 5 units.

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**6.** A straight line L cuts the lines AB, ACandAD of a parallelogram

 $\begin{array}{ll} ABCD & \text{at} & \text{points} & B_1, C_1 and D_1, & \text{respectively.} & \text{If} \\ \left( \stackrel{\rightarrow}{A}B \right)_1, \lambda_1 \stackrel{\rightarrow}{A}B, \left( \stackrel{\rightarrow}{A}D \right)_1 = \lambda_2 \stackrel{\rightarrow}{A} Dand \left( \stackrel{\rightarrow}{A}C \right)_1 = \lambda_3 \stackrel{\rightarrow}{A}C, \text{ then prove} \\ \text{that} \ \frac{1}{\lambda_3} = \frac{1}{\lambda_1} + \frac{1}{\lambda_2} \ . \end{array}$ 

7. The position vectors of the points P and Q are  $5\hat{i} + 7\hat{j} - 2\hat{k}$  and  $-3\hat{i} + 3\hat{j} + 6\hat{k}$ , respectively. Vector  $\overrightarrow{A} = 3\hat{i} - \hat{j} + \hat{k}$  passes through point P and vector  $\overrightarrow{B} = -3\hat{i} + 2\hat{j} + 4\hat{k}$  passes through point Q. A third vector  $2\hat{i} + 7\hat{j} - 5\hat{k}$  intersects vectors A and B. Find the position vectors of points of intersection.

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**8.** Sow that 
$$x_1\hat{i}+y_1\hat{j}+z_1\hat{k}, x_2\hat{i}+y_2\hat{j}+z_2\hat{k}, and x_3\hat{i}+y_3\hat{j}+z_3\hat{k},$$
 are

if

non-coplanar

$$|x_1|>|y_1|+|z_1|, |y_2|>|x_2|+|z_2| and |z_3|>|x_3|+|y_3|$$
 .

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**9.** If  $\overrightarrow{A} n d\overrightarrow{B}$  are two vectors and k any scalar quantity greater than zero, then prove that  $\left|\overrightarrow{A} + \overrightarrow{B}\right|^2 \leq (1+k)\left|\overrightarrow{A}\right|^2 + \left(1 + \frac{1}{k}\right)\left|\overrightarrow{B}\right|^2$ .

**10.** Consider the vectors  $\hat{i} + \cos(\beta - \alpha)\hat{j} + \cos(\gamma - \alpha)\hat{k}, \cos(\alpha - \beta)\hat{i} + \hat{j} + \cos(\gamma - \beta)\hat{k}$  and  $\cos(\alpha - \gamma)\hat{i} + \cos(\beta - \gamma)\hat{k} + a\hat{k}$  where  $\alpha, \beta$ , and  $\gamma$  are different angles. If these vectors are coplanar, show that a is independent of  $\alpha, \beta$  and  $\gamma$ **Watch Video Solution** 

11. In a triangle PQR, SandT are points on QRandPR, respectively, such that QS = 3SRandPT = 4TR. Let M be the point of intersection of PSandQT. Determine the ratio QM:MT using the vector method.

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12. A boat moves in still water with a velocity which is k times less than the river flow velocity. Find the angle to the stream direction at which the boat should be rowed to minimize drifting. **13.** If D, E and F are three points on the sides BC, CA and AB, respectively, of a triangle ABC show that the  $\frac{BD}{CD} = \frac{CE}{AE} = \frac{AF}{BF} = -1$ View Text Solution

**14.** In a quadrilateral PQRS,  $\overrightarrow{P}Q = \overrightarrow{a}$ ,  $\overrightarrow{Q}R = \overrightarrow{b}$ ,  $\overrightarrow{S}P = \overrightarrow{a} - \overrightarrow{b}$ , M is the midpoint of  $\overrightarrow{Q}RandX$  is a point on SM such that  $SX = \frac{4}{5}SM$ . Prove that P, XandR are collinear.

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Single Correct Answer Type

**1.** Four non zero vectors will always be a. linearly dependent b. linearly

independent c. either a or b d. none of these

A. linearly dependent

B. linearly independent

C. either a or b

D. none of these

#### Answer: A

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**2.** Let  $\overrightarrow{a}, \overrightarrow{b}, \overrightarrow{c}$  be three unit vectors such that  $3\overrightarrow{a} + 4\overrightarrow{b} + 5\overrightarrow{c} = \overrightarrow{0}$ . Then which of the following statements is true? (A)  $\overrightarrow{a}$  is parallel to vecb (B)veca*isperpendic* $ar \rightarrow \overrightarrow{b}$  (C)  $\overrightarrow{a}$  is neither paralel nor perpendicular to  $\overrightarrow{b}$  (D)  $\overrightarrow{a}, \overrightarrow{b}, \overrightarrow{c}$  are copalanar

A.  $\overrightarrow{a}$  is parallel to  $\overrightarrow{b}$ 

B.  $\overrightarrow{a}$  is perpendicular to  $\overrightarrow{b}$ 

C.  $\overrightarrow{a}$  is neither parallel nor perpendicular to  $\overrightarrow{b}$ 

D. none of these
# Answer: D



**3.** Let ABC be a triangle the position vectors of whose vertices are respectively  $\hat{i} + 2\hat{j} + 4\hat{k}$ ,  $-2\hat{i} + 2\hat{j} + \hat{k}$  and  $2\hat{i} + 4\hat{j} - 3\hat{k}$ . Then the  $\triangle ABC$  is (A) isosceles (B) equilateral (C) righat angled (D) none of these

A. isosceles

B. equilateral

C. right angled

D. none of these

Answer: C

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**4.** If  $\left| \overrightarrow{a} + \overrightarrow{b} \right| < \left| \overrightarrow{a} - \overrightarrow{b} \right|$ , then the angle between  $\overrightarrow{a}$  and  $\overrightarrow{b}$  can lie in

the interval

- A.  $(\,-\pi\,/\,2,\,\pi\,/\,2)$ B.  $(0,\,\pi)$
- C.  $(\pi \, / \, 2, \, 3\pi \, / \, 2)$
- D.  $(0, 2\pi)$

# Answer: C

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**5.** A point *O* is the centre of a circle circumscribed about a triangle *ABC*. Then  $\overrightarrow{O}A\sin 2A + \overrightarrow{O}B\sin 2B + \overrightarrow{O}C\sin 2C$  is equal to a.  $\left(\overrightarrow{O}A + \overrightarrow{O}B + \overrightarrow{O}C\right)\sin 2A$  b.  $3\overrightarrow{O}G$ , where *G* is the centroid of triangle *ABC* c.  $\overrightarrow{O}$  d. none of these

A. 
$$\left(\overrightarrow{OA} + \overrightarrow{OB} + \overrightarrow{OC}\right)\sin 2A$$

B.  $3\overrightarrow{OG}$ , where G is the centroid of triangle ABC

 $\mathsf{C}.\overrightarrow{0}$ 

D. none of these

# Answer: C

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6. If G is the centroid of a triangle ABC, prove that  $\overrightarrow{G}A + \overrightarrow{G}B + \overrightarrow{G}C = \overrightarrow{0}$ . A.  $\overrightarrow{0}$ B.  $3\overrightarrow{GA}$ C.  $3\overrightarrow{GB}$ D.  $3\overrightarrow{GC}$ 

# Answer: A

7. If  $\overrightarrow{a}$  is a non zero vecrtor iof modulus  $\overrightarrow{a}$  and m is a non zero scalar such that ma is a unit vector, then`

A. 
$$m=\pm 1$$
  
B.  $a=|m|$   
C.  $a=1/|m|$   
D.  $a=rac{1}{m}$ 

### Answer: C

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8. ABCD parallelogram, and  $A_1 and B_1$  are the midpoints of sides BCandCD, respectivley. If  $\overrightarrow{A}A_1 + \overrightarrow{A}B_1 = \lambda \overrightarrow{A}C$ , then  $\lambda$  is equal to a.  $\frac{1}{2}$  b. 1 c.  $\frac{3}{2}$  d. 2 e.  $\frac{2}{3}$ A.  $\frac{1}{2}$ 

C. 
$$\frac{3}{2}$$

 $\mathsf{D.}\,2$ 

### Answer: C

Watch Video Solution

**9.** The position vectors of the points P and Q with respect to the origin O are  $\vec{a} = \hat{i} + 3\hat{j} - 2\hat{k}$  and  $\vec{b} = 3\hat{i} - \hat{j} - 2\hat{k}$ , respectively. If M is a point on PQ, such that OM is the bisector of POQ, then  $\overrightarrow{OM}$  is

$$egin{aligned} \mathsf{A.} & 2 \Big( \hat{i} - \hat{j} + \hat{k} \Big) \ \mathsf{B.} & 2 \hat{i} + \hat{j} - 2 \hat{k} \ \mathsf{C.} & 2 \Big( - \hat{i} + \hat{j} - \hat{k} \Big) \ \mathsf{D.} & 2 \Big( \hat{i} + \hat{j} + \hat{k} \Big) \end{aligned}$$

Answer: B



**10.** ABCD is a quadrilateral. E is the point of intersection of the line joining the midpoints of the opposite sides. If O is any point and  $\overrightarrow{O}A + \overrightarrow{O}B + \overrightarrow{O}C + \overrightarrow{O}D = x\overrightarrow{O}E$ , then x is equal to a. 3 b. 9 c. 7 d. 4

A. 3

B. 9

C. 7

D. 4

#### Answer: D

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11. The vector  $\overrightarrow{AB} = 3\hat{i} + 4\hat{k}$  and  $\overrightarrow{AC} = 5\hat{i} - 2\hat{j} + 4\hat{k}$  are sides of a triangle ABC. The length of the median through A is (A)  $\sqrt{18}$  (B)  $\sqrt{72}$  (C)  $\sqrt{33}$  (D)  $\sqrt{288}$ 

A.  $\sqrt{14}$ 

B.  $\sqrt{18}$ 

C.  $\sqrt{29}$ 

 $\mathsf{D.}\,5$ 

#### Answer: B

Watch Video Solution

**12.** A, B, C and D have position vectors  $\overrightarrow{a}, \overrightarrow{b}, \overrightarrow{c}$  and  $\overrightarrow{d}$ , repectively, such that  $\overrightarrow{a} - \overrightarrow{b} = 2\left(\overrightarrow{d} - \overrightarrow{c}\right)$ . Then

A. AB and CD bisect each other

B. BD and AC bisect each other

C. AB and CD trisect each other

D. BD and AC trisect each other

Answer: D

**13.** If  $\overrightarrow{a}$  and  $\overrightarrow{b}$  are two unit vectors and  $\theta$  is the angle between them, then the unit vector along the angular bisector of  $\overrightarrow{a}$  and  $\overrightarrow{b}$  will be given by

A. 
$$\frac{\overrightarrow{a} - \overrightarrow{b}}{2\cos(\theta/2)}$$
  
B. 
$$\frac{\overrightarrow{a} + \overrightarrow{b}}{2\cos(\theta/2)}$$
  
C. 
$$\frac{\overrightarrow{a} - \overrightarrow{b}}{\cos(\theta/2)}$$

D. none of these

# Answer: B

# Watch Video Solution

14. let us define , the length of a vector as |a|+|b|+|c|. this definition coincides with the usual definition of the length of a vector  $a\hat{i}+b\hat{j}+c\hat{k}$ 

A. 
$$a=b=c=0$$

B. any two of a, b and c are zero

C. any one of a, b and c is zero

D. a + b + c = 0

#### Answer: B

Watch Video Solution

15. Given three vectors  $\overrightarrow{a} = 6\hat{i} - 3\hat{j}, \ \overrightarrow{b} = 2\hat{i} - 6\hat{j} \ \text{and} \ \overrightarrow{c} = -2\hat{i} + 21\hat{j}$  such that  $\overrightarrow{\alpha} = \overrightarrow{a} + \overrightarrow{b} + \overrightarrow{c}$ . Then the resolution of te vector  $\overrightarrow{\alpha}$  into components with respect to  $\overrightarrow{a}$  and  $\overrightarrow{b}$  is given by (A)  $3\overrightarrow{a} - 2\overrightarrow{b}$  (B)  $2\overrightarrow{a} - 3\overrightarrow{b}$  (C)  $3\overrightarrow{b} - 2\overrightarrow{a}$  (D) none of these

A.  $3\overrightarrow{a} - 2\overrightarrow{b}$ B.  $3\overrightarrow{b} - 2\overrightarrow{a}$ 

$$C. 2\overrightarrow{a} - 3\overrightarrow{b} \\ D. \overrightarrow{a} - 2\overrightarrow{b}$$

Answer: C

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**16.** If 
$$\overrightarrow{\alpha} + \overrightarrow{\beta} + \overrightarrow{\gamma} = a \overrightarrow{\delta} and \overrightarrow{\beta} + \overrightarrow{\gamma} + \overrightarrow{\delta} = b \overrightarrow{\alpha}, \overrightarrow{\alpha} and \overrightarrow{\delta}$$
 are non-  
colliner, then  $\overrightarrow{\alpha} + \overrightarrow{\beta} + \overrightarrow{\gamma} + \overrightarrow{\delta}$  equals a.  $a \overrightarrow{\alpha}$  b.  $b \overrightarrow{\delta}$  c. 0 d.  $(a + b) \overrightarrow{\gamma}$ 

A. 
$$a\overrightarrow{\alpha}$$
  
B.  $b\overrightarrow{\delta}$ 

**C**. 0

 $\mathsf{D}.\,(a+b)\overrightarrow{\gamma}$ 

# Answer: C

**Watch Video Solution** 

17. In triangle ABC,  $\angle A = 30^{\circ}$ , H is the orthocenter and D is the midpoint of BC. Segment HD is produced to T such that HD = DT. The length AT is equal to a. 2BC b. 3BC c.  $\frac{4}{2}BC$  d. none of these

A. 2 BC

B. 3 BC

C. 
$$\frac{4}{3}BC$$

D. none of these

#### Answer: A



**18.** Let  $\overrightarrow{r}_1, \overrightarrow{r}_2, \overrightarrow{r}_3, \overrightarrow{r}_n$  be the position vectors of points  $P_1, P_2, P_3, P_n$  relative to the origin O. If the vector equation  $a_1 \overrightarrow{r}_1 + a_2 \overrightarrow{r}_2 + + a_n \overrightarrow{r}_n = 0$  hold, then a similar equation will also hold w.r.t. to any other origin provided a.  $a_1 + a_2 + a_n = n$  b.  $a_1 + a_2 + a_n = 1$  c.  $a_1 + a_2 + a_n = 0$  d.  $a_1 = a_2 = a_3 + a_n = 0$ 

A. 
$$a_1 + a_2 + \ldots + a_n = n$$
  
B.  $a_1 + a_2 + \ldots + a_n = 1$   
C.  $a_1 + a_2 + \ldots + a_n = 0$   
D.  $a_1 = a_2 = a_3 = \ldots = a_n = 0$ 

#### Answer: C

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**19.** Given three non-zero, non-coplanar vectors  $\overrightarrow{a}, \overrightarrow{b}$  and  $\overrightarrow{c}$ .  $\overrightarrow{r}_1 = p\overrightarrow{a} + q\overrightarrow{b} + \overrightarrow{c}$  and  $\overrightarrow{r}_2 = \overrightarrow{a} + p\overrightarrow{b} + q\overrightarrow{c}$ . If the vectors  $\overrightarrow{r}_1 + 2\overrightarrow{r}_2$  and  $2\overrightarrow{r}_1 + \overrightarrow{r}_2$  are collinear, then (p,q) is

A. (0, 0)

B. (1, -1)

C.(-1,1)

D.(1,1)

## Answer: D



**20.** If the vectors  $\overrightarrow{a}$  and  $\overrightarrow{b}$  are linearly independent and satisfying  $(\sqrt{3}\tan\theta + 1)\overrightarrow{a} + (\sqrt{3}\sec\theta - 2)\overrightarrow{b} = \overrightarrow{0}$ , then the most general values of  $\theta$  are:

A. 
$$n\pi - rac{\pi}{6}, n \in Z$$
  
B.  $2n\pi \pm rac{11\pi}{6}, n \in Z$   
C.  $n\pi \pm rac{\pi}{6}, n \in Z$   
D.  $2n\pi + rac{11\pi}{6}, n \in Z$ 

#### Answer: D

View Text Solution

**21.** In a trapezium ABCD the vector  $\overrightarrow{BC} = \alpha \overrightarrow{AD}$ . If  $\overrightarrow{p} = \overrightarrow{AC} + \overrightarrow{BD}$  is coillinear with  $\overrightarrow{AD}$  such that  $\overrightarrow{p} = \mu \overrightarrow{AD}$ , then

A.  $\mu=lpha+2$ B.  $\mu+lpha=1$ 

 $\mathsf{C}.\, \alpha = \mu + 1$ 

D.  $\mu = lpha + 1$ 

### Answer: D

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**22.** Vectors  $\overrightarrow{a} = \hat{i} + 2\hat{j} + 3\hat{k}$ ,  $\overrightarrow{b} = 2\hat{i} - \hat{j} + \hat{k}$  and  $\overrightarrow{c} = 3\hat{i} + \hat{j} + 4\hat{k}$  are so placed that the end point of one vector is the starting point of the next vector. Then the vectors are

A. not coplanar

B. coplanar but cannot form a triangle

C. coplanar and form a triangle

D. coplanar and can form a right-angled triangle

#### Answer: B

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**23.** Vectors  $\overrightarrow{a} = -4\hat{i} + 3\hat{k}$ ;  $\overrightarrow{b} = 14\hat{i} + 2\hat{j} - 5\hat{k}$  are laid off from one point. Vector  $\hat{d}$ , which is being laid of from the same point dividing the angle between vectors  $\overrightarrow{a} and \overrightarrow{b}$  in equal halves and having the magnitude  $\sqrt{6}$ , is a.  $\hat{i} + \hat{j} + 2\hat{k}$  b.  $\hat{i} - \hat{j} + 2\hat{k}$  c.  $\hat{i} + \hat{j} - 2\hat{k}$  d.  $2\hat{i} - \hat{j} - 2\hat{k}$ 

A.  $\hat{i}+\hat{j}+2\hat{k}$ B.  $\hat{i}-\hat{j}+2\hat{k}$ C.  $\hat{i}+\hat{j}-2\hat{k}$ D.  $2\hat{i}-\hat{j}-2\hat{k}$ 

# Answer: A



24. If  $\hat{i} - 3\hat{j} + 5\hat{k}$  bisects the angle between  $\hat{a}$  and  $-\hat{i} + 2\hat{j} + 2\hat{k}$ , where  $\hat{a}$  is a unit vector, then

$$\begin{array}{l} \mathsf{A.}\,\widehat{a} = \frac{1}{150} \Big( 41 \hat{i} + 88 \hat{j} - 40 \hat{k} \Big) \\ \mathsf{B.}\,\widehat{a} = \frac{1}{105} \Big( 41 \hat{i} + 88 \hat{j} + 40 \hat{k} \Big) \\ \mathsf{C.}\,\widehat{a} = \frac{1}{105} \Big( -41 \hat{i} + 88 \hat{j} - 40 \hat{k} \Big) \\ \mathsf{D.}\,\widehat{a} = \frac{1}{105} \Big( 41 \hat{i} - 88 \hat{j} - 40 \hat{k} \Big) \end{array}$$

#### Answer: D



**25.** If  $4\hat{i} + 7\hat{j} + 8\hat{k}, 2\hat{i} + 3\hat{j} + 4\hat{k}$  and  $2\hat{i} + 5\hat{j} + 7\hat{k}$  are the position

vectors of the vertices A, B and C, respectively, of triangle ABC, then the

position vector of the point where the bisector of angle A meets BC is

A. 
$$rac{2}{3}\Big(-6\hat{i}-8\hat{j}-6\hat{k}\Big)$$
  
B.  $rac{2}{3}\Big(6\hat{i}+8\hat{j}+6\hat{k}\Big)$   
C.  $rac{1}{3}\Big(6\hat{i}+13\hat{j}+18\hat{k}\Big)$   
D.  $rac{1}{3}\Big(5\hat{j}+12\hat{k}\Big)$ 

### Answer: C

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**26.** If  $\overrightarrow{b}$  is a vector whose initial point divides the join of  $5\hat{i}and5\hat{j}$  in the ratio k:1 and whose terminal point is the origin and  $\left|\overrightarrow{b}\right| \leq \sqrt{37}$ , thenk lies in the interval

A. 
$$[\,-6,\ -1/16]$$
  
B.  $(\,-\infty,\ -6]\cup[\,-1/6,\infty)$   
C.  $[0,6]$ 

# D. none of these

### Answer: B

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27. The value of the  $\lambda$  so that P, Q, R, S on the sides OA, OB, OC and AB of a regular tetrahedron are coplanar. When  $\frac{OP}{OA} = \frac{1}{3}$ ;  $\frac{OQ}{OB} = \frac{1}{2}$  and  $\frac{OS}{AB} = \lambda$  is (A)  $\lambda = \frac{1}{2}$  (B)  $\lambda = -1$  (C)  $\lambda = 0$  (D)  $\lambda = 2$ A.  $\lambda = \frac{1}{2}$ B.  $\lambda = -1$ C.  $\lambda = 0$ D. for no value of  $\lambda$ 

#### Answer: B

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28. 'I' is the incentre of triangle 
$$ABC$$
 whose corresponding sides are  
 $a, b, c$ , rspectively.  $a\overrightarrow{I}A + b\overrightarrow{I}B + c\overrightarrow{I}C$  is always equal to  $a. \overrightarrow{0} b.$   
 $(a + b + c)\overrightarrow{B}Cc.(\overrightarrow{a} + \overrightarrow{b} + \overrightarrow{c})\overrightarrow{A}Cd.(a + b + c)\overrightarrow{A}B$   
A.  $\overrightarrow{0}$   
B.  $(a + b + c)\overrightarrow{BC}$   
C.  $(\overrightarrow{a} + \overrightarrow{b} + \overrightarrow{c})\overrightarrow{AC}$   
D.  $(a + b + c)\overrightarrow{AB}$ 

#### Answer: A

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**29.** Let  $x^2 + 3y^2 = 3$  be the equation of an ellipse in the x - y plane. AandB are two points whose position vectors are  $-\sqrt{3}\hat{i}and - \sqrt{3}\hat{i} + 2\hat{k}$ . Then the position vector of a point P on the ellipse such that  $\angle APB = \pi/4$  is a.  $\pm \hat{j}$  b.  $\pm (\hat{i} + \hat{j})$  c.  $\pm \hat{i}$  d. none of these A.  $\pm \, \hat{j}$ 

 $\mathsf{B.}\pm\left(\hat{i}+\hat{j}
ight)$ 

 $\mathsf{C}.\pm\hat{i}$ 

D. none of these

### Answer: A

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**30.** Locus of the point P, for which  $\overrightarrow{OP}$  represents a vector with direction cosine  $\cos \alpha = \frac{1}{2}$  (where O is the origin) is

A. a circle parallel to the y-z plane with centre on the x-axis

B. a conic concentric with the positive x-axis having vertex at the

origin and slant height equal to the magnitude of the vector

C. a ray emanating from the origin and making an angle of  $60^\circ$  with



D. a dise parallel to the y-z plane with centre on the x-axis and radius

equal to  $\left| \overrightarrow{OP} \right| \sin 60^{\circ}$ .

#### Answer: B

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**31.** If  $\overrightarrow{x}$  and  $\overrightarrow{y}$  are two non-collinear vectors and ABC is a triangle with side lengths a, b, andc satisfying  $(20a - 15b)\overrightarrow{x} + (15b - 12c)\overrightarrow{y} + (12c - 20a)(\overrightarrow{x} \times \overrightarrow{y}) = 0$ , then triangle ABC is a. an acute-angled triangle b. an obtuse-angled triangle c. a right-angled triangle d. an isosceles triangle

A. an acute-angled triangle

B. an obtuse-angled triangle

C. a right-angled triangle

D. an isosceles triangle

#### Answer: C

**32.** A uni-modular tangent vector on the curve  

$$x = t^2 + 2, y = 4t - 5, z = 2t^2 - 6t = 2$$
 is a.  $\frac{1}{3}(2\hat{i} + 2\hat{j} + \hat{k})$  b.  
 $\frac{1}{3}(\hat{i} - \hat{j} - \hat{k})$  c.  $\frac{1}{6}(2\hat{i} + \hat{j} + \hat{k})$  d.  $\frac{2}{3}(\hat{i} + \hat{j} + \hat{k})$   
A.  $\frac{1}{3}(2\hat{i} + 2\hat{j} + \hat{k})$   
B.  $\frac{1}{3}(\hat{i} - \hat{j} - \hat{k})$   
C.  $\frac{1}{6}(2\hat{i} + \hat{j} + \hat{k})$   
D.  $\frac{2}{3}(\hat{i} + \hat{j} + \hat{k})$ 

# Answer: A

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**33.** If  $\overrightarrow{x}$  and  $\overrightarrow{y}$  are two non-collinear vectors and a, b, and c represent the sides of a ABC satisfying  $(a-b)\overrightarrow{x} + (b-c)\overrightarrow{y} + (c-a)(\overrightarrow{x}\times\overrightarrow{y}) = 0$ , then ABC is (where

 $\overrightarrow{x}$   $\overrightarrow{y}$  is perpendicular to the plane of xandy ) a. an acute-angled triangle b. an obtuse-angled triangle c. a right-angled triangle d. a scalene triangle

A. an acute-angled triangle

B. an obtuse-angled triangle

C. a right-angled triangle

D. a scalene triangle

# Answer: A

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**34.**  $\overrightarrow{A}$  is a vector with direction cosines  $\cos \alpha$ ,  $\cos \beta$  and  $\cos \gamma$ . Assuming the y - z plane as a mirror, the directin cosines of the reflected image of  $\overrightarrow{A}$  in the plane are a.  $\cos \alpha$ ,  $\cos \beta$ ,  $\cos \gamma$  b.  $\cos \alpha$ ,  $-\cos \beta$ ,  $\cos \gamma$  c.  $-\cos \alpha$ ,  $\cos \beta$ ,  $\cos \gamma$  d.  $-\cos \alpha$ ,  $-\cos \beta$ ,  $-\cos \gamma$ 

A.  $\cos \alpha$ ,  $\cos \beta$ ,  $\cos \gamma$ 

B.  $\cos \alpha$ ,  $-\cos \beta$ ,  $\cos \gamma$ 

$$\mathsf{C}.-\coslpha,\coseta,\cos\gamma$$

$$extsf{D.}-\coslpha,\ -\coseta,\ -\cos\gamma$$

### Answer: C

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**35.** The points with position vectors  $60\hat{i} + 3\hat{j}, 40\hat{i} - 8\hat{j}, a\hat{i} - 52\hat{j}$  are

collinear if (A) a = -40 (B) a = 40 (C) a = 20 (D) none of these

A. a = -40

B. a = 40

C. a = 20

D. none of these

### Answer: A

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**36.** Let a, b and c be distinct non-negative numbers. If vectos  $a\hat{i} + a\hat{j} + c\hat{k}, \hat{i} + \hat{k}$  and  $c\hat{i} + c\hat{j} + b\hat{k}$  are coplanar, then c is

A. the arithmetic mean of a and b

B. the geometric mean of a and b

C. the harmonic mean of a and b

D. equal to zero

#### Answer: B

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A. some values of x

B. some values of y

C. no values of x and y

D. for all values of x and y

#### Answer: D

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**38.** Let  $\alpha$ ,  $\beta$  and  $\gamma$  be distinct real numbers. The points whose position vector's are  $\alpha \hat{i} + \beta \hat{j} + \gamma \hat{k}$ ;  $\beta \hat{i} + \gamma \hat{j} + \alpha \hat{k}$  and  $\gamma \hat{i} + \alpha \hat{j} + \beta \hat{k}$  a. are collinear. b. forms an equilateral triangle. c. forms a scalene triangle. d. forms a right angled triangle.

A. are collinear

B. form an equilateral triangle

C. form a scalene triangle

D. form a right-angled triangle

# Answer: B



**39.** The number of distinct values of  $\lambda$ , for which the vectors  $-\lambda^2 \hat{i} + \hat{j} + \hat{k}$ ,  $\hat{i} - \lambda^2 \hat{j} + \hat{k}$  and  $\hat{i} + \hat{j} - \lambda^2 \hat{k}$  are coplanar, is

A. zero

B. one

C. two

D. three

Answer: C

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**40.** If 
$$\overrightarrow{a} = \hat{i} + \hat{j} + \hat{k}$$
,  $\overrightarrow{b} = 4\hat{i} + 3\hat{j} + 4\hat{k}$  and  $\overrightarrow{c} = \hat{i} + \alpha\hat{j} + \beta\hat{k}$ 

are linearly dependent vectors and  $\left| \stackrel{
ightarrow}{c} 
ight| = \sqrt{3}$  then:

A. 
$$lpha = 1, \, eta = -1$$
  
B.  $lpha = 1, \, eta = \pm 1$   
C.  $lpha = -1, \, eta = \pm 1$   
D.  $lpha = \pm 1, \, eta = 1$ 

### Answer: D

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Multiple Correct Answer Type

1.

The

vectors

 $x\hat{i} + (x+1)\hat{j} + (x+2)\hat{k}, (x+3)\hat{i} + (x+4)\hat{j} + (x+5)\hat{k} ext{ and } (x+6)\hat{i}$ 

# are coplanar if x is equal to

A. 1

B. -3

C. 4

# Answer: A::B::C::D

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**2.** The sides of a parallelogram are  $2\hat{i} + 4\hat{j} - 5\hat{k}$  and  $\hat{i} + 2\hat{j} + 3\hat{k}$ . The unit vector parallel to one of the diagonals is

A. 
$$rac{1}{7} \Big( 3 \hat{i} + 6 \hat{j} - 2 \hat{k} \Big)$$
  
B.  $rac{1}{7} \Big( 3 \hat{i} - 6 \hat{j} - 2 \hat{k} \Big)$   
C.  $rac{1}{\sqrt{69}} \Big( \hat{i} + 2 \hat{j} + 8 \hat{k} \Big)$   
D.  $rac{1}{\sqrt{69}} \Big( - \hat{i} - 2 \hat{j} + 8 \hat{k} \Big)$ 

### Answer: A::D

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**3.** The vector  $\overrightarrow{a}$  has the components 2p and 1 w.r.t. a rectangular Cartesian system. This system is rotated through a certain angle about the origin in the counterclockwise sense. If, with respect to a new system,  $\overrightarrow{a}$  has components (p+1)and1, then p is equal to a. -4 b. -1/3 c. 1 d. 2

 $\mathsf{A.}-1$ 

B. - 1/3

C. 1

 $\mathsf{D}.2$ 

# Answer: B::C

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**4.** If points  $\hat{i}+\hat{j},\,\hat{i}-\hat{j}\,\, ext{and}\,\,p\hat{i}+q\hat{j}+r\hat{k}$  are collinear, then

A. p=1

 $\mathsf{B.}\,r=0$ 

 $\mathsf{C}.\,q\in R$ 

D. q 
eq 1

#### Answer: A::B::D

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**5.** If  $\overrightarrow{a}$ ,  $\overrightarrow{b}$ ,  $\overrightarrow{c}$  are non coplanar vectors and  $\lambda$  is a real number, then the vectors  $\overrightarrow{a} + 2\overrightarrow{b} + 3\overrightarrow{c}$ ,  $\lambda\overrightarrow{b} + 4$  and  $(2\lambda - 1)\overrightarrow{c}$  are non coplanar for

A. 
$$\mu \in R$$

B. 
$$\lambda = rac{1}{2}$$

 $\mathsf{C}.\,\lambda=0$ 

D. no value of  $\lambda$ 

#### Answer: A::B::C

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**6.** If the resultant of three forces  $\vec{F}_1 = p\hat{i} + 3\hat{j} - \hat{k}, \vec{F}_2 = 6\hat{i} - \hat{k} \text{ and } \vec{F}_3 = -5\hat{i} + \hat{j} + 2\hat{k} \text{ acting on}$ 

a particle has a magnitude equal to 5 units, then the value of p is

- **A**. − 6
- $\mathsf{B.}-4$
- C. 2
- D. 4

# Answer: B::C

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7. If the vectors  $\hat{i} - \hat{j}, \hat{j} + \hat{k}$  and  $\overrightarrow{a}$  form a triangle then  $\overrightarrow{a}$  may be (A)  $-\hat{i} - \hat{k}$  (B)  $\hat{i} - 2\hat{j} - \hat{k}$  (C)  $2\hat{i} + \hat{j} + \hat{j}k$  (D)  $\hat{i} + \hat{k}$ 

A.  $-\,\hat{i}\,-\,\hat{k}$ 

B. 
$$\hat{i} - 2\hat{j} - \hat{k}$$
  
C.  $2\hat{i} + \hat{j} + \hat{k}$   
D.  $\hat{i} + \hat{k}$ 

### Answer: A::B::D

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8. The vector  $\hat{i} + x\hat{j} + 3\hat{k}$  is rotated through an angle  $\theta$  and doubled in magnitude, then it becomes  $4\hat{i} + (4x - 2)\hat{j} + 2\hat{k}$ . Then values of x are (A)  $-\frac{2}{3}$  (B)  $\frac{1}{3}$  (C)  $\frac{2}{3}$  (D) 2

A. 1

B. -2/3

C. 2

D. 4/3

# Answer: B::C



**9.**  $\overrightarrow{a}$ ,  $\overrightarrow{b}$  and  $\overrightarrow{c}$  are three coplanar vectors such that  $\overrightarrow{a} + \overrightarrow{b} + \overrightarrow{c} = 0$ . If three vectors  $\overrightarrow{p}$ ,  $\overrightarrow{q}$  and  $\overrightarrow{r}$  are parallel to  $\overrightarrow{a}$ ,  $\overrightarrow{b}$  and  $\overrightarrow{c}$ , respectively, and have integral but different magnitudes, then among the following options,  $\left|\overrightarrow{p} + \overrightarrow{q} + \overrightarrow{r}\right|$  can take a value equal to

A. 1

B.0

C.  $\sqrt{3}$ 

D. 2

Answer: C::D

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10. If non-zero vectors a annd b are equally inclined to coplanar vector c,

then c can be



#### Answer: B::D

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**11.** If A(-4, 0, 3)andB(14, 2, -5), then which one of the following points lie on the bisector of the angle between  $\overrightarrow{O}Aand\overrightarrow{O}B(O)$  is the origin of reference )? a. (2, 2, 4) b. (2, 11, 5) c. (-3, -3, -6) d. (1, 1, 2)

A. (2, 2, 4)

B. (2, 11, 5)

C. (-3, -3, -6)

D.(1, 1, 2)

#### Answer: A::C::D

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12. In a four-dimensional space where unit vectors along the axes are  $\hat{i}, \hat{j}, \hat{k}$  and  $\hat{l},$  and  $\overrightarrow{a}_1, \overrightarrow{a}_2, \overrightarrow{a}_3, \overrightarrow{a}_4$  are four non-zero vectors such that no vector can be expressed as a linear combination of others and  $(\lambda - 1)(\overrightarrow{a}_1 - \overrightarrow{a}_2) + \mu(\overrightarrow{a}_2 + \overrightarrow{a}_3) + \gamma(\overrightarrow{a}_3 + \overrightarrow{a}_4 - 2\overrightarrow{a}_2) + \overrightarrow{a}_3 + \delta\overrightarrow{a}$ .

then

A.  $\lambda=1$ B.  $\mu=-2/3$ C.  $\gamma=2/3$ D.  $\delta=1/3$
## Answer: A::B::D



**13.** Let ABC be a triangle, the position vectors of whose vertices are respectively

 $7\hat{j} + 10\hat{k}, \ - \hat{i} + 6\hat{j} + 6\hat{k} \ ext{ and } \ - 4\hat{i} + 9\hat{j} + 6\hat{k}. \ ext{ Then, } \ \Delta ABC$  is

A. isosceles

**B.** equilateral

C. right angled

D. none of these

#### Answer: A::C

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**Reasoning Type** 

**1.** A vector has components p and 1 with respect to a rectangular Cartesian system. The axes are rotated through an angle  $\alpha$  about the origin in the anticlockwise sense.

Statement 1: If the vector has component p+2 and 1 with respect to the new system, then  $p=\ -1.$ 

Statement 2: Magnitude of the original vector and new vector remains the same.

A. Both the statements are true, and Statement 2 is the correct explanation for Statement 1.

B. Both the statements are true, but Statement 2 is not the correct

explanation for Statement 1.

C. Statement 1 is true and Statement 2 is false.

D. Statement 1 is false and Statement 2 is true.

Answer: A

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2. Statement 1: if three points P, QandR have position vectors  $\overrightarrow{a}, \overrightarrow{b}, and \overrightarrow{c}$ , respectively, and  $2\overrightarrow{a} + 3\overrightarrow{b} - 5\overrightarrow{c} = 0$ , then the points P, Q, andR must be collinear. Statement 2: If for three points  $A, B, andC, \overrightarrow{A}B = \lambda \overrightarrow{A}C$ , then points A, B, andC must be collinear.

A. Both the statements are true, and Statement 2 is the correct explanation for Statement 1.

B. Both the statements are true, but Statement 2 is not the correct

explanation for Statement 1.

C. Statement 1 is true and Statement 2 is false.

D. Statement 1 is false and Statement 2 is true.

## Answer: A



**3.** Statement 1: If  $\overrightarrow{u}$  and  $\overrightarrow{v}$  are unit vectors inclined at an angle  $\alpha$  and  $\overrightarrow{x}$  is a unit vector bisecting the angle between them, then  $\overrightarrow{x} = \left(\overrightarrow{u} + \overrightarrow{v}\right) / (2\sin(\alpha/2))$ . Statement 2: If Delta*ABC* is an isosceles triangle with AB = AC = 1, then the vector representing the bisector of angel A is given by  $\overrightarrow{A}D = \left(\overrightarrow{A}B + \overrightarrow{A}C\right)/2$ .

A. Both the statements are true, and Statement 2 is the correct explanation for Statement 1.

B. Both the statements are true, but Statement 2 is not the correct explanation for Statement 1.

C. Statement 1 is true and Statement 2 is false.

D. Statement 1 is false and Statement 2 is true.

### Answer: D

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**4.** Statement 1: If  $\cos \alpha$ ,  $\cos \beta$ , and  $\cos \gamma$  are the direction cosines of any line segment, then  $\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = 1$ . Statement 2: If  $\cos \alpha$ ,  $\cos \beta$ , and  $\cos \gamma$  are the direction cosines of any line segment, then  $\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = 1$ .

A. Both the statements are true, and Statement 2 is the correct explanation for Statement 1.

B. Both the statements are true, but Statement 2 is not the correct

explanation for Statement 1.

C. Statement 1 is true and Statement 2 is false.

D. Statement 1 is false and Statement 2 is true.

### Answer: B



5. Statement 1: The direction cosines of one of the angular bisectors of two intersecting line having direction cosines as  $l_1, m_1, n_1 and l_2, m_2, n_2$ are proportional to  $l_1 + l_2, m_1 + m_2, n_1 + n_2$ . Statement 2: The angle between the two intersection lines having direction cosines as  $l_1, m_1, n_1 and l_2, m_2, n_2$  is given by  $\cos \theta = l_1 l_2 + m_1 m_2 + n_1 n_2$ .

A. Both the statements are true, and Statement 2 is the correct explanation for Statement 1.

B. Both the statements are true, but Statement 2 is not the correct explanation for Statement 1.

C. Statement 1 is true and Statement 2 is false.

D. Statement 1 is false and Statement 2 is true.

### Answer: B

6. Statement 1: In DeltaABC,  $\overrightarrow{A}B + \overrightarrow{A}B + \overrightarrow{C}A = 0$  Statement 2: If  $\overrightarrow{O}A = \overrightarrow{a}$ ,  $\overrightarrow{O}B = \overrightarrow{b}$ ,  $then\overrightarrow{A}B = \overrightarrow{a} + \overrightarrow{b}$ 

A. Both the statements are true, and Statement 2 is the correct explanation for Statement 1.

B. Both the statements are true, but Statement 2 is not the correct

explanation for Statement 1.

- C. Statement 1 is true and Statement 2 is false.
- D. Statement 1 is false and Statement 2 is true.

### Answer: C

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7. Statement 1:  $\overrightarrow{a} = 3\overrightarrow{i} + p\overrightarrow{j} + 3\overrightarrow{k}$  and  $\overrightarrow{b} = 2\overrightarrow{i} + 3\overrightarrow{j} + q\overrightarrow{k}$  are parallel vectors if p = 9/2 and q = 2.

### Statement

:

lf

$$\overrightarrow{a} = a_1 \overrightarrow{i} + a_2 \overrightarrow{j} + a_3 \overrightarrow{k}$$
 and  $\overrightarrow{b} = b_1 \overrightarrow{i} + b_2 \overrightarrow{j} + b_3 \overrightarrow{k}$  are parallel,  
then  $\frac{a_1}{b_1} = \frac{a_2}{b_2} = \frac{a_3}{b_3}$ .

A. Both the statements are true, and Statement 2 is the correct explanation for Statement 1.

B. Both the statements are true, but Statement 2 is not the correct

explanation for Statement 1.

C. Statement 1 is true and Statement 2 is false.

D. Statement 1 is false and Statement 2 is true.

### Answer: A

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8. Statement 1 : If 
$$\left| \overrightarrow{a} + \overrightarrow{b} \right| = \left| \overrightarrow{a} - \overrightarrow{b} \right|$$
, then  $\overrightarrow{a}$  and  $\overrightarrow{b}$  are

perpendicular to each other.

Statement 2 : If the diagonals of a parallelogram are equal in magnitude, then the parallelogram is a rectangle. A. Both the statements are true, and Statement 2 is the correct

explanation for Statement 1.

B. Both the statements are true, but Statement 2 is not the correct

explanation for Statement 1.

- C. Statement 1 is true and Statement 2 is false.
- D. Statement 1 is false and Statement 2 is true.

#### Answer: A

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**9.** Statement 1 : Let  $A(\overrightarrow{a}), B(\overrightarrow{b})$  and  $C(\overrightarrow{c})$  be three points such that  $\overrightarrow{a} = 2\hat{i} + \hat{k}, \overrightarrow{b} = 3\hat{i} - \hat{j} + 3\hat{k}$  and  $\overrightarrow{c} = -\hat{i} + 7\hat{j} - 5\hat{k}$ . Then OABC is tetrahedron.

Statement 2 : Let  $A(\overrightarrow{a}), B(\overrightarrow{b})$  and  $C(\overrightarrow{c})$  be three points such that vectors  $\overrightarrow{a}, \overrightarrow{b}$  and  $\overrightarrow{c}$  are non-coplanar. Then OABC is a tetrahedron, where O is the origin.

A. Both the statements are true, and Statement 2 is the correct

explanation for Statement 1.

B. Both the statements are true, but Statement 2 is not the correct

explanation for Statement 1.

- C. Statement 1 is true and Statement 2 is false.
- D. Statement 1 is false and Statement 2 is true.

#### Answer: A

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10. Statement 1: Let  $\overrightarrow{a}, \overrightarrow{b}, \overrightarrow{c} and \overrightarrow{d}$  be the position vectors of four points A, B, CandD and  $3\overrightarrow{a} - 2\overrightarrow{b} + 5\overrightarrow{c} - 6\overrightarrow{d} = 0$ . Then points A, B, C, andD are coplanar. Statement 2: Three non-zero, linearly dependent coinitial vector  $\left(\overrightarrow{P}Q, \overrightarrow{P}Rand\overrightarrow{P}S\right)$  are coplanar. Then  $\overrightarrow{P}Q = \lambda \overrightarrow{P}R + \mu \overrightarrow{P}S$ , where  $\lambda and \mu$  are scalars. A. Both the statements are true, and Statement 2 is the correct

explanation for Statement 1.

B. Both the statements are true, but Statement 2 is not the correct

explanation for Statement 1.

- C. Statement 1 is true and Statement 2 is false.
- D. Statement 1 is false and Statement 2 is true.

#### Answer: A

**View Text Solution** 

**11.** Statement 1 : If 
$$\left|\overrightarrow{a}\right| = 3$$
,  $\left|\overrightarrow{b}\right| = 4$  and  $\left|\overrightarrow{a} + \overrightarrow{b}\right| = 5$ , then  $\left|\overrightarrow{a} - \overrightarrow{b}\right| = 5$ .

Statement 2 : The length of the diagonals of a rectangle is the same.

A. Both the statements are true, and Statement 2 is the correct

explanation for Statement 1.

B. Both the statements are true, but Statement 2 is not the correct

explanation for Statement 1.

C. Statement 1 is true and Statement 2 is false.

D. Statement 1 is false and Statement 2 is true.

### Answer: A

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Linked Comprehension Type

1. ABCD is a parallelogram. L is a point on BC which divides BC in the ratio

1:2. AL intersects BD at P.M is a point on DC which divides DC in the ratio

1:2 and AM intersects BD in Q.

Point P divides AL in the ratio

A. 1:2

B. 1:3

C.3:1

D. 2:1

Answer: C

View Text Solution

2. ABCD is a parallelogram. L is a point on BC which divides BC in the ratio

1:2. AL intersects BD at P.M is a point on DC which divides DC in the ratio

 $1\!:\!2$  and AM intersects BD in Q.

Point Q divides DB in the ratio

A. 1:2

 $B.\,1:3$ 

C.3:1

 $\mathsf{D}.\,2\!:\!1$ 

Answer: B





**3.** ABCD is a parallelogramm. L is a point on BC which divides BC in the ratio 1:2 AL intersects BD at P.M is a point onn DC which divides DC in the ratio 1:2 and AM intersects BD in Q.

Q. PQ: DB is equal to

A. 2/3

- B. 1/3
- C.1/2
- D. 3/4

## Answer: C

View Text Solution

**4.** Let OABCD be a pentagon in which the sides OA and CB are parallel and the sides OD and AB are parallel as shown in figure. Also, OA:CB=2:1 and

OD:AB=1:3. if the diagonals OC and AD meet at x, find OX:OC.

A. 3/4

B. 1/3

C.2/5

D. 1/2

Answer: C

View Text Solution

**5.** Let OABCD be a pentagon in which the sides OA and CB are parallel and the sides OD and AB are parallel as shown in figure. Also, OA:CB=2:1 and OD:AB=1:3. if the diagonals OC and AD meet at x, find OX:OC.

A. 5/2

 $\mathsf{B.}\,6$ 

C.7/3

## Answer: B



6. If ABCDEF is regular hexagon, then AD+EB+FC is

A. 2  $\overrightarrow{AB}$ 

B. 3  $\overrightarrow{AB}$ 

C. 4 $\overrightarrow{AB}$ 

D. none of these

# Answer: C

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7. Consider the regular hexagon ABCDEF with centre at O (origin).

Q. Five forces AB,AC,AD,AE,AF act at the vertex A of a regular hexagon ABCDEF. Then, their resultant is (a)3AO (b)2AO (c)4AO (d)6AO



D.  $\overrightarrow{6AO}$ 

### Answer: D

**View Text Solution** 

8. Let A,B,C,D,E represent vertices of a regular pentangon ABCDE. Given the position vector of these vertices be a,a+b,b, $\lambda a$  and  $\lambda b$  respectively.

Q. AD divides EC in the ratio

A. 
$$1-\cosrac{3\pi}{5}$$
 :  $\cosrac{3\pi}{5}$ 

B. 
$$1 + 2\cos\frac{2\pi}{5}: \cos\frac{\pi}{5}$$
  
C.  $1 + 2\cos\frac{\pi}{5}: 2\cos\frac{\pi}{5}$ 

D. None of these

## Answer: C

View Text Solution

**9.** Let A,B,C,D,E represent vertices of a regular pentangon ABCDE. Given the position vector of these vertices be a,a+b,b, $\lambda a$  and  $\lambda b$  respectively.

Q. AD divides EC in the ratio

A. 
$$\cos \frac{2\pi}{5}: 1$$
  
B.  $\cos \frac{3\pi}{5}: 1$   
C.  $1: 2 \cos \frac{2\pi}{5}$   
D.  $1: 2$ 

### Answer: C



**10.** In a parallelogram OABC vectors a,b,c respectively, THE POSITION VECTORS OF VERTICES A,B,C with reference to O as origin. A point E is taken on the side BC which divides it in the ratio of 2:1 also, the line segment AE intersects the line bisecting the angle  $\angle AOC$  internally at point P. if CP when extended meets AB in points F, then

Q. The position vector of point P is



D. None of these

### Answer: B

**11.** In a parallelogram OABC vectors a,b,c respectively, THE POSITION VECTORS OF VERTICES A,B,C with reference to O as origin. A point E is taken on the side BC which divides it in the ratio of 2:1 also, the line segment AE intersects the line bisecting the angle  $\angle AOC$  internally at point P. if CP when extended meets AB in points F, then

Q. The position vector of point P is



### Answer: D

View Text Solution

**Matrix Match Type** 

1. Refer to the following diagram :

	Column I		Column II
a.	Collinear vectors	p.	$\overrightarrow{a}$
b.	Coinitial vectors	q.	$\overrightarrow{b}$
с.	Equal vectors	r.	$\overrightarrow{c}$
d.	Unlike vectors (same initial point)	s.	$\overrightarrow{d}$

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# 2. a and b form the consecutive sides of a regular hexagon ABCDEF.

	Column I		Column II
a.	If $\mathbf{C}\mathbf{D} = x\mathbf{a} + y\mathbf{b}$ , then	p.	<i>x</i> = -2
b.	If $CE = xa + yb$ , then	q.	x = -1
c.	If $\mathbf{AE} = x\mathbf{a} + y\mathbf{b}$ , then	r.	<i>y</i> = 1
d.	If $\mathbf{A}\mathbf{D} = -x\mathbf{b}$ , then	s.	<i>y</i> = 2

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## **Integer Type**

3. 🔛

**1.** Let ABC be a triangle whose centroid is G, orthocentre is H and circumcentre is the origin 'O'. If D is any point in the plane of the triangle such that no three of O,A,C and D are collinear satisfying the relation. AD+BD+CH+3HB= $\lambda HD$ , then what is the value of the scalar  $\Delta$ .



**2.** If the resultant of three forces  $\overrightarrow{F}_1 = p\hat{i} + 3\hat{j} - \hat{k}, \overrightarrow{F}_2 = -5\hat{i} + \hat{j} + 2\hat{k}$  and  $\overrightarrow{F}_3 = 6\hat{i} - \hat{k}$  acting on a particle has a magnitude equal to 5 units, then what is difference in the values of p?



**3.** Let  $\overrightarrow{a}$ ,  $\overrightarrow{b}$  and  $\overrightarrow{c}$  be unit vector such that  $\overrightarrow{a} + \overrightarrow{b} - \overrightarrow{c} = 0$ . If the area of triangle formed by vectors  $\overrightarrow{a}$  and  $\overrightarrow{b}$  is A, then what is the value of  $4A^2$ ?

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**4.** Find the least positive integral value of x for which the angle between

vectors  $\overrightarrow{a} = x\hat{i} - 3\hat{j} - \hat{k}$  and  $\overrightarrow{b} = 2x\hat{i} + x\hat{j} - \hat{k}$  is acute.

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5. Vectors along the adjacent sides of parallelogram are  $\vec{a} = 2\hat{i} + 4\hat{j} - 5\hat{k}$  and  $\vec{b} = \hat{i} + 2\hat{j} + 3\hat{k}$ . Find the length of the longer diagonal of the parallelogram.

6. If vectors 
$$\overrightarrow{a} = \hat{i} + 2\hat{j} - \hat{k}$$
,  $\overrightarrow{b} = 2\hat{i} - \hat{j} + \hat{k}$  and  $\overrightarrow{c} = \lambda\hat{i} + \hat{j} + 2\hat{k}$ 

are coplanar, then find the value of  $\lambda$ .



7. Consider the set of eight vector 
$$V = \left\{a\hat{i} + b\hat{j} + c\hat{k}; a, bc \in \{-1, 1\}\right\}$$
. Three non-coplanar vectors can be chosen from  $V$  is  $2^p$  ways. Then  $p$  is\_\_\_\_\_.

8. Suppose that  $\overrightarrow{p}$ ,  $\overrightarrow{q}$  and  $\overrightarrow{r}$  are three non- coplaner in  $R^3$ , Let the components of a vector  $\overrightarrow{s}$  along  $\overrightarrow{p}$ ,  $\overrightarrow{q}$  and  $\overrightarrow{r}$  be 4,3, and 5, respectively, if the components this vector  $\overrightarrow{s}$  along  $(-\overrightarrow{p} + \overrightarrow{q} + \overrightarrow{r}), (\overrightarrow{p} - \overrightarrow{q} + \overrightarrow{r})$  and  $(-\overrightarrow{p} - \overrightarrow{q} + \overrightarrow{r})$  are x, y

and z , respectively , then the value of 2x+y+z is

**1.** Find the all the values of lamda such that  $(x, y, z) \neq (0, 0, 0)$ and  $x(\hat{i} + \hat{j} + 3\hat{k}) + y(3\hat{i} - 3\hat{j} + \hat{k}) + z(-4\hat{i} + 5\hat{j}) = \lambda(x\hat{i} + y\hat{j} + z\hat{k})$ 

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**2.** A vector a has components  $a_1, a_2$  and  $a_3$  in a right handed rectangular cartesian system OXYZ. The coordinate system is rotated about Z-axis through angle  $\frac{\pi}{2}$ . Find components of a in the new system.

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**3.** The position vectors of the points A,B, C and D are  $3\hat{i} - 2\hat{j} - \hat{k}, 2\hat{i} + 3\hat{j} - 34\hat{k}, -\hat{i} + \hat{j} + 2\hat{k}$  and  $4\hat{i} + 5\hat{j} + \lambda\hat{k}$ respectively. If the points A, B ,C and D lie on a plane, find the value of  $\lambda$ .

**4.** Let OACB be a parallelogram with O at the origin and OC a diagonal. Let D be the mid-point of OA. Using vector methods prove that BD and CO intersects in the same ratio. Determine this ratio.

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5. In a triangle ABC, DandE are points on BCandAC, respectivley, such that BD = 2DCandAE = 3EC. Let P be the point of intersection of ADandBE. Find BP/PE using the vector method.



**6.** Prove, by vector method or otherwise, that the point of intersection of the diagonals of a trapezium lies on the line passing through the midpoint of the parallel sides (you may assume that the trapezium is not a parallelogram).

## 7. about to only mathematics



## 8.

Let

 $\overrightarrow{A}(t) = f_1(t)\hat{i} + f_2(t)\hat{j}$  and  $\overrightarrow{B}(t) = g(t)\hat{i} + g_2(t)\hat{j}, t \in [0, 1], f_1, f_2, g_1g_2$ are continuous functions. If  $\overrightarrow{A}(t)$  and  $\overrightarrow{B}(t)$  are non-zero vectors for all t and  $\overrightarrow{A}(0) = 2\hat{i} + 3\hat{j}, \overrightarrow{A}(1) = 6\hat{i} + 2\hat{j}, \overrightarrow{B}(0) = 3\hat{i} + 2\hat{i}$  and  $\overrightarrow{B}(1) = 2\hat{i}$ Then,show that  $\overrightarrow{A}(t)$  and  $\overrightarrow{B}(t)$  are parallel for some t.

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9. about to only mathematics



Fill In The Blanks

1. If a,b, and c are all different and if

 $\begin{vmatrix} a & a^2 & 1 + a^3 \\ b & b^2 & 1 + b^3 \\ c & c^2 & 1 + c^3 \end{vmatrix} = 0$  Prove that abc =-1.

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**2.** If the vectors 
$$a\hat{i} + \hat{j} + \hat{k}$$
,  $\hat{i} + b\hat{j} + \hat{k}$ ,  $\hat{i} + \hat{j} + c\hat{k}$  ( $a \neq 1, b \neq 1, c \neq 1$ )  
are coplanar then the value of  $\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c}$  is (A) 0 (B) 1 (C)  
-1 (D) 2

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True Or False

**1.** The points with position vectors  $\overrightarrow{x} + \overrightarrow{y}, \overrightarrow{x} - \overrightarrow{y}$  and  $\overrightarrow{x} + \lambda \overrightarrow{y}$  are

collinear for all real values of  $\lambda$ .