

India's Number 1 Education App

#### **MATHS**

### **BOOKS - CENGAGE PUBLICATION**

### **MATRICES**

#### **Example**

**1.** If 
$$e^A$$
 is defined as  $e^A = I + A + \frac{A^2}{2!} + \frac{A^3}{3!} + ... = \frac{1}{2} \begin{bmatrix} f(x) & g(x) \\ g(x) & f(x) \end{bmatrix}$ , where  $A = \begin{bmatrix} x & x \\ x & x \end{bmatrix}$ ,  $0 < x < 1$  and I is identity matrix, then find the

functions f(x) and g(x).



**2.** Prove that matrix  $\begin{bmatrix} \frac{b^2-a^2}{a^2+b^2} & \frac{-2ab}{a^2+b^2} \\ \frac{-2ab}{a^2+b^2} & \frac{a^2-b^2}{a^2+b^2} \end{bmatrix}$  is orthogonal.



**3.** If  $A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$ , where a, b, c and d are real numbers, then prove that

$$A^2-(a+d)A+(ad-bc)I=O.$$
 Hence or therwise, prove that if



 $A^3 = O$  then  $A^2 = O$ 

**4.** If  $A=\left(\left[a_{ij}
ight]
ight)_{n imes n}$  is such that  $(a)_{ij}=\overline{a_{ji}},\ orall i,\ j$  and  $A^2=O,\$ then

Statement 1: Matrix A null matrix.

Statement 2: |A| = 0.



5. Find the possible square roots of the two rowed unit matrix I.



6. Prove the orthogonal matrices of order two are of the form

$$\begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix} \text{ or } \begin{bmatrix} \cos \theta & \sin \theta \\ \sin \theta & -\cos \theta \end{bmatrix}$$



Watch Video Solution

7. Let  $A=egin{bmatrix} anrac{\pi}{3} & \secrac{2\pi}{3} \ \cot\left(2013rac{\pi}{3}
ight) & \cos(2012\pi) \end{bmatrix}$  and P be a 2 imes 2 matrix such that  $PP^T=I$ , where I is an identity matrix of order 2. If  $Q=PAP^T$ 

and  $R = [r_{ii}]_{2\times 2} = P^T Q^8 P$ , then find  $r_{11}$ .



**8.** Consider,  $A = \begin{bmatrix} a & 2 & 1 \\ 0 & b & 0 \\ 0 & -3 & c \end{bmatrix}$ , where a, b and c are the roots of the equation  $x^3-3x^2+2x-1=0$ . If matric B is such that AB=BA, A+B-2I 
eq O and  $A^2-B^2=4I-4B$ , then find the value of det. (B)



**9.** If A and B are square matrices of order 3 such that |A|=3 and |B|=2, then find the value of  $|A^{-1}adj(B^{-1})adj(2A^{-1})|$ 



## **ILLUSTRATION**

- 1. If a matrix has 28 elements, what are the possible orders it can have?
  - Watch Video Solution

- **2.** Construct a  $2 \times 2$  matrix, where
- (i)  $a_{
  m ij}=rac{\left(i-2j
  ight)^2}{2}$  (ii)  $a_{
  m ij}=\left|-2i+3j
  ight|$ 
  - Watch Video Solution

**3.** What is the maximum number of different elements required to form a symmetric matrix of order 12 ?



**4.** If a square matix a of order three is defined  $A=\left[a_{
m ij}
ight]$  where  $a_{
m ii}=sgn(i-j)$ , then prove that A is skew-symmetric matrix.



**5.** For what values of x and y are the following matrices equal?

$$A=egin{bmatrix} 2x+1 & 3y \ 0 & y^2-5y \end{bmatrix}, B=egin{bmatrix} x+3 & y^2+2 \ 0 & -6 \end{bmatrix}$$



**6.** For  $lpha,eta,\gamma\in R$ , let

$$A = \begin{bmatrix} \alpha^2 & 6 & 8 \\ 3 & \beta^2 & 9 \\ 4 & 5 & \gamma^2 \end{bmatrix} \text{ and } B = \begin{bmatrix} 2\alpha & 3 & 5 \\ 2 & 2\beta & 6 \\ 1 & 4 & 2\gamma - 3 \end{bmatrix} \text{ If tr(A)=tr(B), then }$$
 find the value of  $\left(\frac{1}{\alpha}\right) + \left(\frac{1}{\beta}\right) + \left(\frac{1}{\gamma}\right)$ 



- **7.** Find the values of x for which matrix  $\begin{bmatrix} 3 & -1+x & 2 \\ 3 & -1 & x+2 \\ x+3 & -1 & 2 \end{bmatrix}$  is singular.
  - Watch Video Solution

- **8.** If  $A=\begin{bmatrix}1&2\\3&4\\5&6\end{bmatrix}$  and  $B=\begin{bmatrix}-3&-2\\1&-5\\4&3\end{bmatrix}$ , then find  $D=\begin{bmatrix}p&q\\r&s\\t&u\end{bmatrix}$  such that A+B-D=O.
  - **Watch Video Solution**

**9.**  $A = \begin{bmatrix} \cos lpha & -\sin lpha \\ \sin lpha & \cos lpha \end{bmatrix}$  and  $A + A^T = I$ , find the value of lpha.



**10.** Let A be a square matrix. Then prove that  $(i)A+A^T$  is a symmetric matrix and, $(ii)A-A^T$  is a skew-symmetric matrix



**11.** If 
$$A=egin{bmatrix} 2 & -1 \ 3 & 1 \end{bmatrix}$$
 and  $B=egin{bmatrix} 1 & 4 \ 7 & 2 \end{bmatrix}$  , find  $3A-2B$ .



**12.** Find non-zero values of x satisfying the matrix equation:

$$xegin{bmatrix} 2x & 2 \ 3 & x \end{bmatrix} + 2egin{bmatrix} 8 & 5x \ 4 & 4x \end{bmatrix} = 2egin{bmatrix} x^2 + 8 & 24 \ 10 & 6x \end{bmatrix}$$



13. Let  $A+2B=\begin{bmatrix}1&2&0\\6&-3&3\\-5&3&1\end{bmatrix}$  and  $2A-B=\begin{bmatrix}2&-1&5\\2&-1&6\\0&1&2\end{bmatrix}$ , then find tr(A)-tr(B).



- **14.** If  $\begin{bmatrix} \lambda^2-2\lambda+1 & \lambda-2 \\ 1-\lambda^2+3\lambda & 1-\lambda^2 \end{bmatrix}=A\lambda^2+B\lambda+C$ , where A, B and C are matrices then find matrices B and C.
  - Watch Video Solution

- **15.** Prove that every square matrix can be uniquely expressed as the sum of a symmetric matrix and a skew-symmetric matrix.
  - Watch Video Solution

**16.** Matrix A ha s m rows and n+ 5 columns; matrix B has m rows and 11-n columns. If both AB and BA exist, then (A) AB and BA are square

matrix (B) AB and BA are of order  $8 \times 8$  and  $3 \times 13$ , respectively (C)

AB=BA (D) None of these



**17.** If 
$$A=\begin{bmatrix}2&3&-1\\1&4&2\end{bmatrix}$$
 and  $B=\begin{bmatrix}2&3\\4&5\\2&1\end{bmatrix}$  then prove that AB and BA are not equal.



$$\begin{bmatrix} 3 & -2 \\ 3 & 0 \\ 2 & 4 \end{bmatrix} \begin{bmatrix} y & y \\ x & x \end{bmatrix} = \begin{bmatrix} 3 & 3 \\ 3y & 3y \\ 10 & 10 \end{bmatrix}$$



**19.** Find the values of x, y, z if the matrix

$$A = egin{bmatrix} 0 & 2y & z \ x & y & -z \ \end{bmatrix}$$
 satisfy the equation  $A^T \, A = I_3$  .



**20.** If 
$$A = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$$
 then prove that  $A^n = \begin{bmatrix} \cos n\theta & \sin n\theta \\ -\sin n\theta & \cos n\theta \end{bmatrix}, n \in N.$ 

**22.** Let 
$$A=\begin{bmatrix}2&1\\0&3\end{bmatrix}$$
 be a matrix. If  $A^{10}=\begin{bmatrix}a&b\\c&d\end{bmatrix}$  then prove that  $a+d$  is divisible by 13.

**21.** If  $A=\begin{pmatrix}p&q\\0&1\end{pmatrix}$  , then show that  $A^8=\begin{pmatrix}p^8&q\left(rac{p^2-1}{p-1}
ight)\\0&1\end{pmatrix}$ 

23. Show that the solutions of the equation 
$$\begin{bmatrix} 1 & 2 & 5 & 3 \end{bmatrix}$$

$$\begin{bmatrix} x & y \\ z & t \end{bmatrix}^2 = 0 are \begin{bmatrix} x & y \\ z & t \end{bmatrix} = \begin{bmatrix} \pm \sqrt{\alpha\beta} & -\beta \\ \alpha & \pm \sqrt{\alpha\beta} \end{bmatrix} \text{,} \quad \text{where} \quad \alpha,\beta \quad \text{ are}$$
 arbitrary.



**24.** Let A be square matrix. Then prove that  $AA^T$  and  $A^TA$  are symmetric matrices.



**25.** If A, B are square materices of same order and B is a skewsymmetric matrix, show that  $A^TBA$  is skew-symmetric.



**26.** If A and B are square matrices of same order such that AB+BA=O, then prove that  $A^3-B^3=(A+B)\big(A^2-AB-B^2\big).$ 



**27.** Let  $A=\left[egin{array}{cc} 1 & 2 \ -1 & 3 \end{array}
ight]$  .If  $A^6=kA-205I$  then find the numerical quantity of k-40



**28.** Let A, B, C, D be (not necessarily square) real matrices such that  $A^T=BCD\colon B^T=CDA;\, C^T=DAB$  and  $D^T=ABC.$  For the matrix S=ABCD, consider the two statements. I.  $S^3=S$  II.  $S^2=S^4$  (A) II is true but not I (B) I is true but not II (C) both I and II are true (D) both I and II are false



**29.** If A and B are square matrices of the same order such that AB=BA, then prove by induction that  $AB^n=B^nA$ .



**30.** If A=[-110-2] , then prove that  $A^2+3A+2I=O$ . Hence, find BandC matrices of order 2 with integer elements, if  $A=B^3+C^3$ .



**31.** If  $A=\begin{bmatrix} 3 & -4 \\ 1 & -1 \end{bmatrix}$  then find tr.  $\left(A^{2012}\right)$ .



**32.** If A is a nonsingular matrix satisfying AB-BA=A, then prove that  $\det (B+I)=\det (B-I).$ 



**33.** If det,  $(A-B) \neq 0$ ,  $A^4=B^4$ ,  $C^3A=C^3B$  and  $B^3A=A^3B$ , then find the value of det.  $(A^3+B^3+C^3)$ .



**34.** Given a matrix  $A=\begin{bmatrix} a & b & c \\ b & c & a \\ c & a & b \end{bmatrix}$ , wherea,b,c are real positive numbers  $abc=1andA^TA=I$ , then find the value of  $a^3+b^3+c^3$ .



**35.** If M is a  $3 \times 3$  matrix, where  $\det M = 1 and M M^T = 1, where I$  is an identity matrix, prove theat  $\det (M-I) = 0.$ 



**36.** Consider point P(x, y) in first quadrant. Its reflection about x-axis is  $Q(x_1,y_1)$ . So,  $x_1=x$  and  $y_1=-y$ .

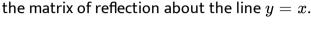
This may be written as :  $\left\{egin{array}{l} x_1=1.\ x+0.\ y \ y_1=0.\ x+(-1)y \end{array}
ight.$ 

This system of equations can be put in the matrix as:

Here, matrix 
$$\begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$$
 is the ma

 $\left|egin{array}{c} x_1 \ y_1 \end{array}
ight| = \left|egin{array}{cc} 1 & 0 \ 0 & -1 \end{array}
ight| \left|egin{array}{c} x \ y \end{array}
ight|$ 

Here, matrix  $\begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$  is the matrix of reflection about x-axis. Then find





37. If 
$$A=\begin{bmatrix}2&-2&-4\\-1&3&4\\1&-2&-3\end{bmatrix}$$
 then A is `1) an idempotent matrix 2) nilpotent matrix 3) involutary 4) orthogonal matrix

**38.** If 
$$A=egin{bmatrix}1&1&3\\5&2&6\\-2&-1&-3\end{bmatrix}$$
 then find  $A^{14}+3A-2I$ 



**39.** The matrix  $A = \lceil -5 - 8035012 - \rceil$  is a. idempotent matrix b.

involutory matrix c. nilpotent matrix d. none of these

A. idempotent matrix

B. involutory matrix

C. nilpotent matrix

D. none of these

### **Answer: involutory matrix**



**Watch Video Solution** 

**40.** If abc=p and  $A=\begin{bmatrix} a & b & c \\ c & a & b \\ b & c & a \end{bmatrix}$  , prove that A is orthogonal if and

only if a, b, c are the roots of the equation  $x^3 \pm x^2 - p = 0$ .



**Watch Video Solution** 

**41.** Let A be an orthogonal matrix, and B is a matrix such that AB=BA, then show that  $AB^T=B^TA$ .



- **42.** Find the adjoint of the matrix  $A=\begin{bmatrix}1&1&1\\2&1&-3\\-1&2&3\end{bmatrix}$ .
  - Watch Video Solution

**43.** If 
$$S = \begin{bmatrix} \frac{\sqrt{3}-1}{2\sqrt{2}} & \frac{\sqrt{3}+1}{2\sqrt{2}} \\ -\left(\frac{\sqrt{3}+1}{2\sqrt{2}}\right) & \frac{\sqrt{3}-1}{2\sqrt{2}} \end{bmatrix}$$
,  $A = \begin{bmatrix} 1 & 0 \\ -1 & 1 \end{bmatrix}$  and  $P = S(\text{adj.A})S^T$ ,

then find matrix  $S^T P^{10} S$ .



**44.** If A is a square matrix such that  $A(adjA) = \begin{bmatrix} 4 & 0 & 0 \\ 0 & 4 & 0 \\ 0 & 0 & 4 \end{bmatrix}$ , then

$$=rac{|adj(adjA)|}{2|adjA|}$$
 is equal to



**45.** Let A be a square matrix of order 3 such that

adj. (adj. (adj. A)) 
$$=egin{bmatrix} 16 & 0 & -24 \ 0 & 4 & 0 \ 0 & 12 & 4 \end{bmatrix}$$
 . Then find the value of  $|A|$ 



**46.** Let 
$$A = \begin{bmatrix} 1 & -1 & 1 \\ 2 & 1 & -3 \\ 1 & 1 & 1 \end{bmatrix}$$
 and  $10B = \begin{bmatrix} 4 & 2 & 2 \\ -5 & 0 & \alpha \\ 1 & -2 & 3 \end{bmatrix}$ . If B is the

inverse of A, then find the value of  $\alpha$ 



**47.** Matrices a and B satisfy  $AB=B^{-1}$ , where  $B=\begin{bmatrix} 2 & -1 \\ 2 & 0 \end{bmatrix}$ . Find

(i) without finding  $B^{-1}$ , the value of K for which

$$KA - 2B^{-1} + I = Q$$

(ii) without finding  $A^{-1}$ , find the matrix X satisfying  $A^{-1}XA=B$ .



**48.** Given the matrices A and B as  $A=\begin{bmatrix}1&-1\\4&-1\end{bmatrix}$  and  $B=\begin{bmatrix}1&-1\\2&-2\end{bmatrix}$ . The two matrices X and Y are such that XA=B and AY=B, then find

The two matrices X and Y are such that XA=B and AY=B, then fir the matrix 3(X+Y)



- **49.** If M is the matrix  $\begin{bmatrix} 1 & -3 \\ -1 & 1 \end{bmatrix}$  then find matrix  $\sum_{r=0}^{\infty} \left( \frac{-1}{3} \right)^r M^{r+1}$ 
  - Watch Video Solution

**50.** Let p be a non singular matrix, and  $I+P+p^2+\ldots+p^n=0$ , then find  $p^{-1}$ .



**51.** If A and B are square matrices of same order such that AB=O and  $B \neq O$ , then prove that |A|=0.



**52.** If A is a symmetric matrix, B is a skew-symmetric matrix, A+B is nonsingular and  $C=(A+B)^{-1}(A-B)$ , then prove that

(i) 
$$C^T(A+B)C=A+B$$
 (ii)  $C^T(A-B)C=A-B$ 

(iii) 
$$C^TAC = A$$



**53.** If the matrices,  $A,B,\left(A+B
ight)$  are non-singular, then prove that

$$\Big[A(A+B)^{-1}B\Big]^{-1}=B^{-1}+A^{-1}.$$



**54.** If matrix a satisfies the equation  $A^2=A^{-1}$ , then prove that  $A^{2^n}=A^{2^{(n-2)}}, n\in N.$ 



**55.** If A and B are non-singular symmetric matrices such that AB=BA, then prove that  $A^{-1}B^{-1}$  is symmetric matrix.



**56.** If A is a matrix of order n such that  $A^TA=I$  and X is any matrix such that  $X=(A+I)^{-1}(A-I)$ , then show that X is skew symmetric

matrix.



Watch Video Solution

# 57. Show that two matrices

$$A=egin{bmatrix}1&-1&0\2&1&1\end{bmatrix}$$
 and  $B=egin{bmatrix}3&0&1\0&3&1\end{bmatrix}$  are row equivalent.



Watch Video Solution

# 58. Using elementary transformations, find the inverse of the matrix :

$$\begin{bmatrix} 2 & 0 & 1 \\ 5 & 1 & 0 \\ 0 & 1 & 3 \end{bmatrix}$$



Watch Video Solution

## **59.** Let A be a $3 \times 3$ matric such that

$$\mathsf{A} \,. \, \begin{bmatrix} 1 & 2 & 3 \\ 0 & 2 & 3 \\ 0 & 1 & 1 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix} \mathsf{, then find } A^{-1}.$$

watch video Solution

**60.** Solve the following system of equations, using matrix method.

$$x + 2y + z = 7, x + 3z = 11, 2x - 3y = 1$$



**61.** Using matrix method, show that following system of equation is inconsistent : 2x+3y-z+4=0 x-y+2z-7=0

$$x + 4y - 3z + 5 = 0$$



**62.** If f(x) and g(x) are two functions with g(x)=x-1/x and  $f(x)=x^3-1/x^1$ , then f'(x) is equal to



**63.** Find the characteristic roots of the two-rowed orthogonal matrix

$$\begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$$
 and verify that they are of unit modulus.



**64.** Show that if  $\lambda_1, \lambda_2, \ldots, \lambda_n$  are n eigenvalues of a square matrix a of order n, then the eigenvalues of the matric  $A^2$  are  $\lambda_1^2, \lambda_2^2, \ldots, \lambda_n^2$ .



**65.** If A is nonsingular, prove that the eigenvalues of  $A^{-1}$  are the reciprocals of the eigenvalue of A.



**66.** If one of the eigenvalues of a square matrix a order 3 imes 3 is zero, then prove that  $\det A = 0$ .

#### **CAE 13.1**

1. Construct a  $3 \times 4$  matrix, whose elements are given by:

$$a_{ij}=rac{1}{2}|-3i+j|$$



- **2.** Find the value of a if [a-b2a+c2a-b3c+d]=[-15013]
  - Watch Video Solution

- **3.** Find the number of all possible matrices of order 3 imes 3 with each entry
- 0 or 1. How many of these are symmetric?
  - Watch Video Solution

**4.** Find the value of x for which the matrix  $A=\begin{bmatrix}2/x&-1&2\\1&x&2x^2\\1&1/x&2\end{bmatrix}$  is singular.



**5.** If matric A is skew-symmetric matric of odd order, then show that tr. A = det. A.



#### **CAE 13.2**

- **1.** Solve for x and y ,  $xigg[rac{2}{1}igg]+yigg[rac{3}{5}igg]+igg[-8\\-11igg]=0.$ 
  - Watch Video Solution

**2.** If  $A=\begin{bmatrix}1&5\\7&12\end{bmatrix}$  and  $B=\begin{bmatrix}9&1\\7&8\end{bmatrix}$  then find a matrix C such that

3A + 5B + 2C is a null matrix.



3. Solve the following equations for X and Y:

$$2X-Y=egin{bmatrix} 3&-3&0\ 3&3&2 \end{bmatrix}, 2Y+X=egin{bmatrix} 4&1&5\ -1&4&-4 \end{bmatrix}$$

Watch Video Solution

**4.** If 
$$A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 1 & 2 \\ 2 & 2 & 3 \end{bmatrix} B = \begin{bmatrix} 1 & 2 & 2 \\ -2 & -1 & -2 \\ 2 & 2 & 3 \end{bmatrix}$$

and

$$C = egin{bmatrix} -1 & -2 & -2 \ 2 & 1 & 2 \ 2 & 2 & 2 \end{bmatrix}$$
 then find the value of tr.  $ig(A+B^T+3Cig)$ .



**5.** If  $A=\begin{bmatrix} 3 & -2 \\ 4 & -1 \end{bmatrix}$ , then find all the possible values of  $\lambda$  such that the matrix  $(A-\lambda I)$  is singular.



Watch Video Solution

**6.** If matrix  $A=\begin{bmatrix}0&1&-1\\4&-3&4\\3&-3&4\end{bmatrix}=B+C$ , where B is symmetric matrix

and C is skew-symmetric matrix, then find matrices B and C.



Watch Video Solution

#### **CAE 13.3**

1. Consider the matrices

$$A = egin{bmatrix} 4 & 6 & -1 \ 3 & 0 & 2 \ 1 & -2 & 5 \end{bmatrix}, B = egin{bmatrix} 2 & 4 \ 0 & 1 \ -1 & 2 \end{bmatrix}, C = egin{bmatrix} 3 \ 1 \ 2 \end{bmatrix}$$

Out of the given matrix products, which one is not defined?

A. 
$$(AB)^TC$$

B.  $C^TC(AB)^T$ 

 $C.C^TAB$ 

D  $A^TABB^TC$ 

### **Answer: B**



Watch Video Solution

**2.** Let  $A=BB^T+CC^T$ , where  $B=\begin{bmatrix}\cos\theta\\\sin\theta\end{bmatrix}, C=\begin{bmatrix}\sin\theta\\-\cos\theta\end{bmatrix}, \theta\in R.$ 

Then prove that A is unit matrix.



Watch Video Solution

**3.** The matrix R(t) is defined by  $R(t) = \begin{bmatrix} \cos t & \sin t \\ -\sin t & \cos t \end{bmatrix}$ . Show that



R(s)R(t) = R(s+t).

**4.** if 
$$A=\left[egin{array}{cc} i & 0 \ 0 & i \end{array}
ight]$$
 where  $i=\sqrt{-1}$  and  $x\in N$  then  $A^{4x}$  equals to:



**5.** If  $A=\begin{bmatrix}3&-4\\1&-1\end{bmatrix}$  prove that  $A^k=\begin{bmatrix}1+2k&-4k\\k&1-2k\end{bmatrix}$  where k is any positive integer.



**6.** If 
$$A=\begin{bmatrix}1&2\\3&-5\end{bmatrix}$$
 and  $B=\begin{bmatrix}1&0\\0&2\end{bmatrix}$  and X is a matrix such that



A=BX, then X=

**7.** for what values of x: 
$$\begin{bmatrix} 1 & 2 & 0 \end{bmatrix}$$

$$egin{bmatrix} [1 & 2 & 1] & 1 & 2 & 0 \ 2 & 0 & 1 \ 1 & 0 & 2 \ \end{bmatrix} & 0 \ 2 \ x \ = 0?$$

**8.** Find the matrix X so that  $X[123456] = [\,-7-8-9246]$ 



**Watch Video Solution** 

**9.** 
$$If A = egin{bmatrix} \cos \theta & \sin \theta \ -\sin \theta & \cos \theta \end{bmatrix}, then \lim_{n o \infty} \ rac{1}{n} A^n$$
 is

A. (A) an identity matrix

B. (B) [O 10 -1 0]

C. (C) a null matrix

D. (D) none of these

#### **Answer: Zero Matrix**



**Watch Video Solution** 

**10.** 
$$A = \begin{bmatrix} 3 & a & -1 \\ 2 & 5 & c \\ b & 2 & 2 \end{bmatrix}$$

**10.**  $A = \begin{bmatrix} 3 & a & -1 \\ 2 & 5 & c \\ b & 8 & 2 \end{bmatrix}$  is symmetric and  $B = \begin{bmatrix} d & 3 & a \\ b - a & e & -2b - c \\ -2 & 6 & -f \end{bmatrix}$  is

skew-symmetric, then find AB.



#### **CAE 13.4**

1. If A and B are matrices of the same order, then  $AB^T-BA^T$  is a (a) skew-symmetric matrix (b) null matrix (c) unit matrix (d) symmetric matrix



**2.** If A and B are square matrices such that AB = BA then prove that

$$A^3 - B^3 = (A - B)(A^2 + AB + B^2).$$

Watch Video Solution

**3.** If A is a square matrix such that  $A^2=I$ , then  $(A-I)^3+(A+I)^3-7A$  is equal to

**4.** If B,C are square matrices of order nand if  $A=B+C,BC=CB,C^2=O,$  then without using mathematical induction, show that for any positive integer  $p,A^{p-1}=B^p[B+(p+1)C]$  .



Watch Video Solution

**6.** Let A be a matrix of order 3, such that 
$$A^TA=I$$
. Then find the value of det.  $ig(A^2-Iig)$ .

**5.** Let A be any 3 imes 2 matrix. Then prove that det.  $\left(AA^T
ight) = 0$ .

- **7.** A and B are different matrices of order n satisfying  $A^3=B^3$  and  $A^2B=B^2A$ . If det. (A-B) 
  eq 0, then find the value of det.  $(A^2+B^2)$ .
  - Watch Video Solution

- **8.** Statement 1: if  $D={
  m diag}[d_1,d_2,,d_n]$ ,then  $D^{-1}={
  m diag}[d_1^{-1},d_2^{-1},...,d_n^{-1}]$  Statement 2: if  $D={
  m diag}[d_1,d_2,,d_n]$ ,then  $D^n={
  m diag}[d_1^n,d_2^n,...,d_n^n]$ 
  - Watch Video Solution

- **9.** Point P(x, y) is rotated by an angle  $\theta$  in anticlockwise direction. The new position of point P is  $Q(x_1,y_1)$ . If  $\begin{bmatrix} x_1 \\ y_1 \end{bmatrix} = A \begin{bmatrix} x \\ y \end{bmatrix}$ , then find matrix A.
  - Watch Video Solution

10. How many different diagonal matrices of order n can be formed which are involuntary?

- A. A.  $2^{n}$
- B. B. $2^{n} 1$
- $\mathsf{C.}\,\mathsf{C.}\,2^{n-1}$
- D.D.n

Answer:  $2^n$ 



11. How many different diagonal matrices of order n can be formed which are idempotent?



**Watch Video Solution** 

12. If A and B are n-rowed unitary matrices, then AB and BA are also unitary matrices.



Watch Video Solution

# **CAE 13.5**

1. By the method of matrix inversion, solve the system.

$$egin{bmatrix} 1 & 1 & 1 \ 2 & 5 & 7 \ 2 & 1 & -1 \end{bmatrix} egin{bmatrix} x_1 & y_1 \ x_2 & y_2 \ x_3 & y_3 \end{bmatrix} = egin{bmatrix} 9 & 2 \ 52 & 15 \ 0 & -1 \end{bmatrix}$$



**2.** Let  $A = \begin{bmatrix} 2 & 0 & 7 \\ 0 & 1 & 0 \\ 1 & -2 & 1 \end{bmatrix}$  and  $B = \begin{bmatrix} -x & 14x & 7x \\ 0 & 1 & 0 \\ x & -4x & -2x \end{bmatrix}$  are two

matrices such that  $AB = (AB)^{-1}$  and AB 
eq I then

$$Trig((AB)+(AB)^2+(AB)^3+(AB)^4+(AB)^5+(AB)^6ig)=$$



Watch Video Solution

**3.** Find 
$$A^{-1}$$
 if  $A=\begin{bmatrix} 0 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \end{bmatrix}$  and show that  $A^{-1}=\frac{A^2-3I}{2}$ 



- **4.** For the matrix  $A=\left[egin{array}{cc} 3 & 1 \ 7 & 5 \end{array}
  ight]$  , find x and y so that  $A^2+xI=yA$ 
  - Watch Video Solution

- **5.** If  $A^3=O$ , then prove that  $(I-A)^{-1}=I+A+A^2$ .
  - Watch Video Solution

**6.** If  $A=egin{bmatrix}\cos lpha & -\sin lpha \\ \sin lpha & \cos lpha\end{bmatrix}, B=egin{bmatrix}\cos 2eta & \sin 2eta \\ \sin eta & -\cos eta\end{bmatrix}$  where  $0<eta<rac{\pi}{2}$ , then prove that  $BAB=A^{-1}$ . Also, find the least

value of lpha of which  $BA^4B=A^{-1}$ 

7. If 
$$A=\begin{bmatrix}1&2&2\\2&2&3\\1&-1&3\end{bmatrix}, C=\begin{bmatrix}2&1&1\\2&2&1\\1&1&1\end{bmatrix}, D=\begin{bmatrix}10\\13\\9\end{bmatrix}$$
, and  $CB=D$ .

Solve the equation AX = B.



**8.** If A is a 
$$2\times 2$$
 matrix such that  $A^2-4A+3I=O$ , then prove that  $(A+3I)^{-1}=rac{7}{24}I-rac{1}{24}A.$ 



- **9.** For two unimobular complex numbers  $z_1$  and  $z_2$ , find  $\begin{bmatrix} \bar{z}_1 & -z_2 \\ \bar{z}_2 & z_1 \end{bmatrix}^{-1} \begin{bmatrix} z_1 & z_2 \\ -\bar{z}_2 & \bar{z}_1 \end{bmatrix}^{-1}$ 
  - Watch Video Solution

**10.** Prove that inverse of a skew-symmetric matrix (if it exists) is skew-symmetric.



**11.** If square matrix a is orthogonal, then prove that its inverse is also orthogonal.



**12.** If A is a skew symmetric matrix, then  $B = (I - A)(I + A)^{-1}$  is (where I is an identity matrix of same order as of A)



**13.** Prove that  $(adj. A)^{-1} = (adj. A^{-1}).$ 



14. Using elementary transformation, find the inverse of the matrix

$$A = egin{bmatrix} a & b \ c & \left(rac{1+bc}{a}
ight) \end{bmatrix}\!.$$



**15.** If A and P are the square matrices of the same order and if P be invertible, show that the matrices A and `P^(-1) have the same characteristic roots.



**16.** Show that the characteristics roots of an idempotent matrix are either 0 or 1



17. If  $\alpha$  is a characteristic root of a nonsin-gular matrix, then prove that

 $\frac{|A|}{A}$  is a characteristic root of adj A.



Watch Video Solution

#### **Exercises**

1. If A is symmetric as well as skew-symmetric matrix, then A is

A. diagonal matrix

B. null matrix

C. triangular materix

D. none of these

#### Answer: B



**2.** Elements of a matrix A or orddr 10 imes 10 are defined as  $a_{ij} = w^{i+j}$ (where w is cube root of unity), then trace (A) of the matrix is a.0 b. 1 c. 3 d. none of these

A. 0

B. 1

C. 3

D. none of these

#### Answer: D



**Watch Video Solution** 

**3.** If  $A_1,\,A_2,\,,A_{2n-1}aren$  skew-symmetric matrices of same order, then  $B=\sum_{r=1}^{n}{(2r-1)ig(A^{2r-1}ig)^{2r-1}}$  will be symmetric skew-symmetric neither symmetric nor skew-symmetric data not adequate

A. symmetric

- B. skew-symmetric
- C. neither symmetric nor skew-symmetric
- D. data not adequate

#### **Answer: B**



- **4.** The equation  $\begin{bmatrix}1xy\end{bmatrix}\begin{bmatrix}1&3&1\\0&2&-1\\0&0&1\end{bmatrix}\begin{bmatrix}1\\x\\y\end{bmatrix}=[0]$  has
- i)for y=0 (p) rational roots
- ii) for y=-1 (q) irrational roots
- (r) integral roots
  - A. (i) (ii) (p) (r)(ii)
  - B. (i) (ii)
    - (q) (p)
  - (ii)(p) (q)
  - D. (i) (ii)
    - (r)(p)

#### **Answer: C**



#### **Watch Video Solution**

- **5.** Let AandB be two  $2\times 2$  matrices. Consider the statements (i)  $AB=O\Rightarrow A=O$  or B=O (ii)  $AB=I_2\Rightarrow A=B^{-1}$  (iii)  $(A+B)^2=A^2+2AB+B^2$  (a)(i) and (ii) are false, (iii) is true (b)(ii) and (iii) are false, (i) is true (c)(i) is false (ii) and, (iii) are true (d)(i) and (iii)
  - A. (i) and (ii) are false, (iii) is true

are false, (ii) is true

- B. (ii) and (iii) are false, (i) is true
- C. (i) is false, (ii) and (iii) are true
- D. (i) and (iii) are false, (ii) is true

#### **Answer: D**



**6.** The number of diagonal matrix, A or ordern which  $A^3=A$  is a. is a a. 1

b. 0 c.  $2^n$  d.  $3^n$ 

A. 1

В. О

 $\mathsf{C}.\,2^n$ 

D.  $3^n$ 

#### **Answer: D**



Watch Video Solution

**7.** A is a 2 imes 2 matrix such that

$$Aegin{bmatrix}1\\-1\end{bmatrix}=egin{bmatrix}-1\\2\end{bmatrix} \ ext{and}\ \ A^2egin{bmatrix}1\\-1\end{bmatrix}=egin{bmatrix}1\\0\end{bmatrix}.$$
 The sum of the elements of

A is a.—1 b. 0 c. 2 d. 5

$$A.-1$$

B. 0

C. 2

D. 5

Answer: D



Watch Video Solution

8.

If 
$$heta-\phi=rac{\pi}{2},$$

that, prove

$$egin{bmatrix} \cos^2 heta & \cos heta \sin heta \ \cos heta \sin heta & \sin^2 heta \end{bmatrix} egin{bmatrix} \cos^2 \phi & \cos \phi \sin \phi \ \cos \phi \sin \phi & \sin^2 \phi \end{bmatrix} = 0$$

A.  $2n\pi, \in Z$ 

B.  $nrac{\pi}{2}, n \in Z$ 

C.  $(2n+1)rac{\pi}{2}, n\in X$ 

D.  $n\pi$ ,  $n \in Z$ 

Answer: C



**9.** If A=[ab0a] is nth root of  $I_2$ , then choose the correct statements: If n is odd, a=1,b=0 If n is odd, a=-1,b=0 If n is even, a=1,b=0 If n is even, a=1,b=0 If n is even, a=-1,b=0 a. i, ii, iii, iv b.ii, iii, iv c. i, ii, iii, iv d. i, iii, iv

- A. i, ii, iii
- B. ii, iii, iv
- C. i, ii, iii, iv
- D. i, iii, iv

#### **Answer: D**



Watch Video Solution

**10.** If  $\begin{bmatrix} \alpha & \beta \\ \gamma & -\alpha \end{bmatrix}$  is to be square root of two-rowed unit matrix, then  $\alpha,\beta$  and  $\gamma$  should satisfy the relation. a.  $1-\alpha^2+\beta\gamma=0$  b.  $\alpha^2+\beta\gamma=0$  c.

$$1+lpha^2+eta\gamma=0$$
 d.  $1-lpha^2-eta\gamma=0$ 

A. 
$$1-lpha^2+eta\gamma=0$$

B. 
$$lpha^2 + eta \gamma - 1 = 0$$

C. 
$$1+lpha^2+eta\gamma=0$$

D. 
$$1-lpha^2-eta\gamma=0$$

### **Answer: B**



## Watch Video Solution

**11.** If 
$$A=\begin{bmatrix}i&-i\\-i&i\end{bmatrix}$$
 and  $B=\begin{bmatrix}1&-1\\-1&1\end{bmatrix}$ ,  $then, A^8$  equals a. $4B$  b.  $128B$  c.  $-128B$  d.  $-64B$ 

A. 4B

B. 128B

 $\mathsf{C.}-128~\mathsf{B}$ 

D.-64B

## **Answer: B**

**12.** If 
$$\begin{bmatrix}2&-1\\1&0\\-3&4\end{bmatrix}A=\begin{bmatrix}-1&-8&-10\\1&-2&-5\\9&22&15\end{bmatrix}$$
 , then sum of all the elements

of matrix A is

B. 1

D.-3

#### **Answer: B**



Watch Video Solution

**13.** For each real x, -1 < x < 1. Let A(x) be the matrix  $(1-x)^{-1}egin{bmatrix} 1 & -x \ -x & 1 \end{bmatrix}$  and  $z=rac{x+y}{1+xy}.$  Then

**14.** Let A = 
$$\begin{bmatrix} 0 & -\tan \alpha/2 \\ \tan \alpha/2 & 0 \end{bmatrix}$$
 and I, the indentity matrix of order 2.

Watch Video Solution

A. A(z) = A(x)A(y)

B. A(z) = A(x) - A(y)

C. A(z) = A(x) + A(y)

D.  $A(z) = A(x)[A(y)]^{-1}$ 

**4.** Let A = 
$$\begin{bmatrix} tax \\ tax \end{bmatrix}$$

**Answer: A** 

A. 
$$-I+A$$

B. 
$$I-A$$

 $\mathsf{C.} - I - A$ 

# **Answer: B**



**15.** The number of solutions of the matrix equation  $X^2=[1123]$  is a.

**16.** If  $A=\left[egin{array}{cc} a & b \\ c & d \end{array}
ight]$  (where bc
eq 0 ) satisfies the equations

more than 2 b. 2 c. 0 d. 1

A. more then 2

B. 2

C. 0

D. 1

#### Answer: A



$$x^2 + k = 0$$
, then

A. 
$$a+d=0$$

$$\mathsf{B.}\,k=\,-\,|A|$$

$$\mathsf{C.}\,k = |A|$$

D. none of these

#### Answer: C



Watch Video Solution

$$A=egin{bmatrix}2&1\\4&1\end{bmatrix}, B=egin{bmatrix}3&4\\2&3\end{bmatrix}$$
 and  $C=egin{bmatrix}3&-4\\-2&3\end{bmatrix}$  . Then the value of the

$$tr(A)+trigg(rac{ABC}{2}igg)+trigg(rac{A{(BC)}^2}{4}igg)+trigg(rac{A{(BC)}^3}{8}igg)+.....$$

is

(A) 
$$6$$
 (B)  $9$  (C)  $12$  (D) none of these

A. 6

B. 9

C. 12

D. none of these

#### **Answer: A**



### Watch Video Solution

**18.** If  $\begin{bmatrix} \frac{\cos{(2\pi)}}{7} & -\frac{\sin{(2\pi)}}{7} \\ \frac{\sin{(2\pi)}}{7} & \frac{\cos{(2\pi)}}{7} \end{bmatrix}^k = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ , then the least positive integral

value of k is (a) 3 (b) 4 (c) 6 (d) 7

- A. 3
- B. 6
- C. 7
- D. 14

Answer: C



**19.** If A and B are square matrices of order n, then prove that AandB will commute iff  $A - \lambda I and B - \lambda I$  commute for every scalar  $\lambda$ .

A. 
$$AB = BA$$

$$\operatorname{B.}AB+BA=O$$

$$\mathsf{C}.\,A=\,-\,B$$

D. none of these

#### Answer: A



Watch Video Solution

for  $n\geq 2.$   $A^n$  is equal to  $2^{n-1}A-(n-1)l$  b.  $2^{n-1}A-I$  c.

**20.** Matrix A such that  $A^2=2A-I, where I$  is the identity matrix, the

$$nA-(n-1)l$$
 d.  $nA-I$ 

A. 
$$2^{n-1}A - (n-1)I$$

B. 
$$2^{n-1}A - I$$

$$\mathsf{C}.\, nA - (n-1)I$$

D. nA-I

#### **Answer: C**



Watch Video Solution

- **21.** Let  $A=egin{bmatrix} 0 & lpha \ 0 & 0 \end{bmatrix}$  and  $(A+I)^{50}=50A=egin{bmatrix} a & b \ c & d \end{bmatrix}$  Then the value of
- a+b+c+d is (A) 2 (B) 1 (C) 4 (D) none of these
  - A. 2
  - B. 1
  - C. 4
  - D. none of these

#### **Answer: A**



**22.** If Z is an idempotent matrix, then  $\left(I+Z\right)^nI+2^nZ$  b.  $I+(2^n-1)Z$ 

c.  $I-(2^n-1)Z$  d. none of these

A. 
$$I+2^nZ$$

$$\mathsf{B}.\,I+(2^n-1)Z$$

$$\mathsf{C.}\,I-(2^n-1)Z$$

D. none of these

#### **Answer: B**



 $A^{2006}=O$  and  $AB=A+B, then, \det(B)$  equals a.0 b. 1 c. -1 d.

such

that

if A and B are squares matrices

none of these

23.

A. 0

B. 1

$$C. -1$$

D. none of these

#### Answer: A



Watch Video Solution

**24.** If matrix A is given by  $A=\left|egin{array}{cc} 6 & 11 \\ 2 & 4 \end{array}
ight|$  , then the determinant of

 $A^{2005}-6A^{2004}$  is a.  $2^{2006}$  b.  $(\,-11)2^{2005}$  c.  $-2^{2005}$  d.  $(\,-9)2^{2004}$ 

A. 
$$2^{2006}$$

B. 
$$(-11)2^{2005}$$

$$C. - 2^{2005}.7$$

D. 
$$(-9)2^{2004}$$

#### **Answer: B**



**25.** If A is non-diagonal involuntary matrix, then a. A-I=O b.

A+I=O c. A-I is nonzero singular d. none of these

A. 
$$A-I=O$$

$$\mathsf{B.}\,A+I=O$$

C. A-I is nonzero singular

D. none of these

#### Answer: C



**26.** If AandB are two nonzero square matrices of the same ordr such that the product  $AB=O,\,$  then both A and B must be singular exactly one of them must be singular both of them are non singular none of these

A. both A and B must be singular

B. exactly one of them must be singular

C. both of them are nonsingular

D. none of these

#### Answer: A



Watch Video Solution

**27.** If AandB are symmetric matrices of the same order and

 $X = AB + BAandY = AB - BA, then(XY)^T$  is equal to XY b. YX

 $\mathsf{c.}-YX$  d. none of these

A. *XY* 

 $\mathsf{B.}\ YX$ 

 $\mathsf{C.}-YX$ 

D. none of these

Answer: C

**28.** If 
$$A,B,A+I,A+B$$
 are idempotent matrices, then  $AB$  is equal to

**29.** If  $A = \begin{bmatrix} 0 & x \\ y & 0 \end{bmatrix}$  and  $A^3 + A = O$  then sum of possible values of xy is

A. 
$$BA$$

 $\mathsf{a}.BA \mathsf{b}.-BA \mathsf{c}.I \mathsf{d}.O$ 

$$\mathsf{B.}-BA$$

$$\mathsf{C}.\,I$$

$$\mathsf{D}.\,O$$

#### **Answer: B**



- A. 0
- B. 1

- C. 1
- D. 2

#### **Answer: B**



Watch Video Solution

A. 
$$\begin{bmatrix} 6/7 & 2/7 & -3/7 \\ 2/7 & 3/7 & 6/7 \\ 3/7 & -6/7 & 2/7 \end{bmatrix}$$
B. 
$$\begin{bmatrix} 6/7 & 2/7 & 3/7 \\ 2/7 & -3/7 & 6/7 \\ 3/7 & 6/7 & -2/7 \end{bmatrix}$$
C. 
$$\begin{bmatrix} -6/7 & -2/7 & -3/7 \\ 2/7 & 3/7 & 6/7 \\ -3/7 & 6/7 & 2/7 \end{bmatrix}$$

D. 
$$\begin{bmatrix} 6/7 & -2/7 & 3/7 \\ 2/7 & 2/7 & -3/7 \\ -6/7 & 2/7 & 3/7 \end{bmatrix}$$

#### Answer: A



Watch Video Solution

31. Let A and B be two square matrices of the same size such that

 $AB^T + BA^T = O$ . If A is a skew-symmetric matrix then BA is

A. a symmetric matrix

B. a skew-symmetric matrix

C. an orthogonal matrix

D. an invertible matrix

### Answer: B



**32.** In which of the following type of matrix inverse does not exist always?

a. idempotent b. orthogonal c. involuntary d. none of these

A. idempotent

B. orthogonal

C. involuntary

D. none of these

#### **Answer: A**



**Watch Video Solution** 

**33.** Let A be an nth-order square matrix and B be its adjoint, then

 $|AB+KI_n|$  is (where K is a scalar quantity) a.  $(|A|+K)^{n-2}$  b.

 $(|A|+K)^n$  c.  $(|A|+K)^{n-1}$  d. none of these

A.  $(|A| + K)^{n-2}$ 

B.  $(|A| + K)^n$ 

C. 
$$(|A| + K)^{n-1}$$

D. none of these

#### Answer: B



Watch Video Solution

**34.** If 
$$A=\begin{bmatrix}a&b&c\\x&y&z\\p&q&r\end{bmatrix}, B=\begin{bmatrix}q&-b&y\\-p&a&-x\\r&-c&z\end{bmatrix}$$
 and if  $A$  is invertible,

then which of the following is not true? (a) |A| = |B| (b) |A| = -|B|

(c) |adjA| = |adjB| (d) A is invertible if and only if B is invertible

A. 
$$|A|=|B|$$

B. 
$$|A| = -|B|$$

$$\mathsf{C}.\left|\mathrm{adj}\:\mathrm{A}\right|=\left|\mathrm{adj}\:\mathrm{B}\right|$$

D. A is invertible if and only if B is invertible

#### Answer: A



**35.** If  $A(lpha,eta)=\left[\coslpha s\inlpha 0-s\inlpha\coslpha 000e^eta
ight], then A(lpha,eta)^{-1}$  is equal to  $A(-\alpha, -\beta)$  b.  $A(-\alpha, \beta)$  c.  $A(\alpha, -\beta)$  d.  $A(\alpha, \beta)$ 

A. 
$$A(-\alpha, -\beta)$$

B.  $A(-\alpha, \beta)$ 

 $C.A(\alpha, -\beta)$ 

D.  $A(\alpha, \beta)$ 

## Answer: A



**36.** If 
$$A=\begin{bmatrix}a+ib&c+id\\-c+id&a-ib\end{bmatrix}$$
 and  $a^2+b^2+c^2+d^2=1, then, A^{-1}$  is equal to a.  $\begin{bmatrix}a+ib&-c+id\\c+id&a-ib\end{bmatrix}$  b.  $\begin{bmatrix}a-ib&-c-id\\-c-id&a+ib\end{bmatrix}$  c.  $\begin{bmatrix}a+ib&-c-id\\-c+id&a-ib\end{bmatrix}$  d. none of these

A. 
$$\left[egin{array}{ccc} a-ib & -c-id \ c-id & a+ib \end{array}
ight]$$

B. 
$$\begin{bmatrix} a+ib & -c+id \\ -c+id & a-ib \end{bmatrix}$$
C.  $\begin{bmatrix} a-ib & -c-id \\ -c-id & a+ib \end{bmatrix}$ 
D. none of these

## Answer: A



## Watch Video Solution

**37.** Id 
$$\begin{bmatrix} rac{1}{25} & 0 \\ x & rac{1}{25} \end{bmatrix} = \begin{bmatrix} 5 & 0 \\ -a & 5 \end{bmatrix}^{-2}$$
 , then the value of  $x$  is

a. 
$$\frac{a}{125}$$

b.  $\frac{2a}{125}$ 

c. 
$$\frac{2a}{25}$$

d. none of these

A. 
$$a\,/\,125$$

B. 
$$2a/125$$

$$\mathsf{C.}\,2a\,/\,25$$

## D. none of these

### Answer: B



**Watch Video Solution** 

**38.** If 
$$A=\begin{bmatrix}1&2\\2&1\end{bmatrix}$$
 and  $f(x)=\dfrac{1+x}{1-x},$  then  $f(A)$  is

$$A. \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$$

B. 
$$\begin{bmatrix} 2 & 2 \\ 2 & 2 \end{bmatrix}$$
C.  $\begin{bmatrix} -1 & -1 \\ -1 & -1 \end{bmatrix}$ 

D. none of these

#### **Answer: C**



Watch Video Solution

39. There are two possible values of A in the solution of the matrix

equation

 $\left[egin{array}{ccc} 2A+1 & -5 \ -4 & A \end{array}
ight]^{-1} \left[egin{array}{ccc} A-5 & B \ 2A-2 & C \end{array}
ight] = \left[egin{array}{ccc} 14 & D \ E & F \end{array}
ight]$ 

where A, B, C, D, E and F are real numbers. The absolute value of the difference of these two solutions, is

A. 
$$\frac{8}{3}$$

B.  $\frac{19}{3}$ 

C.  $\frac{1}{3}$ 

D.  $\frac{11}{3}$ 

### Answer: B



**40.** If A and B are two square matrices such that  $B=-A^{-1}BA, then(A+B)^2$  is equal to  $aA^2+B^2$  b. O c.

$$A^2+2AB+B^2$$
 d.  $A+B$ 

A. 
$$A^2 + B^2$$

B. *O* 

$$\mathsf{C.}\,A^2 + 2AB + B^2$$

$$\mathsf{D}.\,A+B$$

#### **Answer: A**



Watch Video Solution

**41.** If 
$$A=egin{bmatrix}1&\tan x\\-\tan x&1\end{bmatrix}$$
 , show that  $A^T\,A^{-1}=egin{bmatrix}\cos 2x&-\sin 2x\\\sin 2x&\cos 2x\end{bmatrix}$ 

•

A. 
$$\begin{bmatrix} -\cos 2x & \sin 2x \\ -\sin 2x & \cos 2x \end{bmatrix}$$

B. 
$$\begin{bmatrix} \cos 2x & -\sin 2x \\ \sin 2x & \cos 2x \end{bmatrix}$$

$$\mathsf{C.}\begin{bmatrix} \cos 2x & \cos 2x \\ \cos 2x & \sin 2x \end{bmatrix}$$

D. none of these

#### **Answer: B**



**42.** If A is order 2 square matrix such that |A|=2, then |(adj(adj(adjA)))|is a, 512 b, 256 c, 64 d, none of these

**43.** If  $A = \begin{bmatrix} 0 & 1 & 2 \\ 1 & 2 & 3 \\ 3 & a & 1 \end{bmatrix}$  and  $A^{-1} \begin{bmatrix} 1/2 & -1/2 & 1/2 \\ -4 & 3 & b \\ 5/2 & -3/2 & 1/2 \end{bmatrix}$  then find a and b

A. 512

B. 256

C. 64

D. none of these

#### **Answer: B**



_		4	1
υ.	_	Ι,	1

#### **Answer: B**



**Watch Video Solution** 

- **44.** If nth-order square matrix A is a orthogonal, then  $|\operatorname{adj}(\operatorname{adjA})|$  is always
- -1 if niseven b. always 1 if nisodd c. always 1 d. none of these
  - A. always -1 if n is even
  - B. always 1 if n is odd
  - C. always 1
  - D. none of these

#### **Answer: B**



**45.** Let aandb be two real numbers such that a>1, b>1. If A=(a00b) , then  $(\lim_{n\to\infty}A^{-n}$  is a. unit matrix b. null matrix c. 2l d. none of these

A. unit matrix

B. null matrix

 $\mathsf{C.}\,2I$ 

D. none of these

#### Answer: B



## **Watch Video Solution**

**46.** If  $A=\left(\left[a_{ij}
ight]
ight)_{4 imes4,}$  such that

 $a_{ij} = \left\{2, when i = j0, when i 
eq j, then \left\{rac{\det(adj(adjA))}{7}
ight\} 
ight.$  is (where

{.} represents fractional part function) 1/7 b. 2/7 c. 3/7 d. none of these

A. 1/7

B. 
$$2/7$$

C.3/7

D. none of these

# **Answer: A**



Watch Video Solution

- **47.** A is an involuntary matrix given by  $A=egin{bmatrix} 0 & 1 & -1 \ 4 & -3 & 4 \ 3 & -3 & 4 \ \end{bmatrix}$  , then the inverse of A/2 will be 2A b.  $\frac{A^{-1}}{2}$  c.  $\frac{A}{2}$  d.  $A^2$ 
  - A. 2A
  - $\mathsf{B.}\;\frac{A^{\,-\,1}}{2}$
  - $C. \frac{A}{2}$
  - D.  $A^2$

# Answer: A

**48.** If A is a non-singular matrix such that  $AA^T=A^TA$  and  $B=A^{-1}A^T,$  the matrix B is a involuntary b. orthogonal c. idempotent d. none of these

A. involuntary

B. orthogonal

C. idempotent

D. none of these

#### Answer: B



Watch Video Solution

**49.** If P is an orthogonal matrix and  $Q = PAP^Tandx = P^T \ A$  b. I c.

 $A^{1000}$  d. none of these

 $\mathsf{A.}\,A$ 

B. I

C.  $A^{1000}$ 

D. none of these

## **Answer: B**



Watch Video Solution

for

# **50.** If AandB are two non-singular matrices of the same order such that

positive

integer

 $r>1, then A^{-1}B^{r-1}A-A^{-1}B^{-1}A=\ \ {
m a.}\ I\ {
m b.}\ 2I\ {
m c.}\ O\ {
m d.}$  -I

some

A. I

 $B^r = I$ ,

B.2I

C. *O* 

 $\mathsf{D}.-I$ 

**Answer: C** 

**51.** If 
$${\sf adj}B=A,$$
  $|P|=|Q|=1,$   $then.$   $adjig(Q^{-1}BP^{-1}ig)$  is  ${\sf a.}PQ$  b.  $QAP$  c.  $PAQ$  d.  $PA^{-1}Q$ 

**52.** If A is non-singular and (A-2I)(A-4I)=0, then,  $\frac{1}{6}A+\frac{4}{3}A^{-1}$ 

A. 
$$PQ$$

B. 
$$QAP$$

$$\mathsf{C.}\,PAQ$$

D. 
$$PA^{-1}Q$$

#### **Answer: C**



# Watch Video Solution

 $\mathsf{a}.0I\,\mathsf{b}.\,2I\,\mathsf{c}.\,6I\,\mathsf{d}.\,I$ 

is equal to

 $\mathsf{B}.\,I$ 

 $\mathsf{C}.\,2I$ 

D. 6I

### **Answer: B**



Watch Video Solution

# **53.** Let $f(x) = \frac{1+x}{1-x}$ . If A is matrix for which $A^3 = 0$ ,then f(A) is (a) $I+A+A^2$ (b) $I+2A+2A^2$ (c) $I-A-A^2$ (d) none of these

A. 
$$I+A+A^2$$

B.  $I + 2A + 2A^2$ 

C.  $I - A - A^2$ 

D. none of these

**Answer: B** 

54. Find the matrix A satisfying the matrix equation

$$\begin{bmatrix} 2 & 1 \\ 3 & 2 \end{bmatrix} A \begin{bmatrix} -3 & 2 \\ 5 & -3 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

A. 
$$\begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}$$
B. 
$$\begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix}$$

$$\mathsf{C}.\begin{bmatrix}1 & 0\\1 & 1\end{bmatrix}$$

$$\mathsf{D.} - \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}$$

#### **Answer: A**



Watch Video Solution

**55.** If  $A^2-A+I=0$ , then the inverse of A is a.  $A^{-2}$  b. A+I c. I-A

$$\mathsf{d.}\,A-I$$

A. 
$$A^{\,-\,2}$$

$$\operatorname{B.}A+I$$

$$\mathsf{C.}\,I-A$$

$$\operatorname{D.} A - I$$

#### **Answer: C**



# Watch Video Solution

**56.** If  $f(x) = \begin{bmatrix} \cos x & -\sin x & 0 \\ \sin x & \cos x & 0 \\ 0 & 0 & 1 \end{bmatrix}$  and  $g(y) = \begin{bmatrix} \cos y & 0 & \sin y \\ 0 & 1 & 0 \\ -\sin y & 0 & \cos y \end{bmatrix}$ ,

then 
$$[f(x)g(y)]^{-1}$$
 is equal to (a)  $f(-x)g(-y)$  (b)  $g(-y)f(-x)$  (c)  $fig(x^{-1}ig)gig(y^{-1}ig)$  (d)  $gig(y^{-1}ig)fig(x^{-1}ig)$ 

A. 
$$F(-x)G(-y)$$

B. 
$$G(-y)F(-x)$$

C. 
$$F(x^{-1})G(y^{-1})$$

D. 
$$G(y^{-1})F(x^{-1})$$

# Answer: B

A. 
$$A^{-n}B^nA^n$$

B. 
$$A^nB^nA^{-n}$$

$$\mathsf{C.}\,A^{-1}B^nA$$

D. 
$$n(A^{-1}BA)$$

**Answer: C** 



**58.** If  $k \in R_o then \det \{adj(kI_n)\}$  is equal to  $K^{n-1}$  b.  $K^{n\,(\,n-1\,)}$  c.  $K^n$  d. k

A. 
$$k^{n-1}$$

B. 
$$k^{n\,(\,n\,-\,1\,)}$$

C. 
$$k^n$$

#### **Answer: B**



Watch Video Solution

**59.** Given the matrix  $A = \begin{bmatrix} x & 3 & 2 \\ 1 & y & 4 \\ 2 & 2 & z \end{bmatrix}$ .

xyz = 60 and 8x + 4y + 3z = 20, then A(adjA) is equal to

A. 
$$\begin{bmatrix} 64 & 0 & 0 \\ 0 & 64 & 0 \\ 0 & 0 & 64 \end{bmatrix}$$
B. 
$$\begin{bmatrix} 88 & 0 & 0 \\ 0 & 88 & 0 \\ 0 & 0 & 88 \end{bmatrix}$$
C. 
$$\begin{bmatrix} 68 & 0 & 0 \\ 0 & 68 & 0 \\ 0 & 0 & 68 \end{bmatrix}$$
D. 
$$\begin{bmatrix} 34 & 0 & 0 \\ 0 & 34 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

#### **Answer: C**



**60.** Let 
$$A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 0 & 5 \\ 0 & 2 & 1 \end{bmatrix}$$
 and  $B = \begin{bmatrix} 0 \\ -3 \\ 1 \end{bmatrix}$ . Which of the following is a

true? a.AX=B has a unique solution b.AX=B has exactly three solutions c.Ax=B has infinitely many solutions d.AX=B is inconsistent

A. 
$$AX = B$$
 has a unique solution

B. 
$$AX=B$$
 has exactly three solutions

C. 
$$AX = B$$
 has infinitelt many solutions

D. 
$$AX = B$$
 is inconsistent

#### **Answer: A**



**Watch Video Solution** 

**61.** If A is a square matrix of order less than 4 such that  $\left|A-A^T\right| 
eq 0$  and  $B=\,$  adj. (A), then adj.  $\left(B^2A^{-1}B^{-1}A\right)$  is

A. 
$$A$$

 $\mathsf{B}.\,B$ 

 $\mathsf{C}.\,|A|A$ 

D. |B|B

# **Answer: A**



# Watch Video Solution

**62.** Let A be a square matrix of order 3 such that det.  $(A)=rac{1}{3}$  , then the

value of det.  $\left(\mathrm{adj.} \ \ A^{-1}\right)$  is

A. 1/9

B.1/3

**C**. 3

D. 9

Answer: D

63. If A and B are two non-singular matrices of order 3 such that

$$AA^T=2I$$
 and  $A^{-1}=A^T-A$ . Adj.  $\left(2B^{-1}
ight)$  , then det. (B) is equal to

A. 4

 $\mathrm{B.}\,4\sqrt{2}$ 

C. 16

D.  $16\sqrt{2}$ 

#### Answer: D



Watch Video Solution

**64.** If A is a square matric of order 5 and  $2A^{-1}=A^T$ , then the remainder when  $|adj.\ (adj.\ (adj.\ A))|$  is divided by 7 is

A. 2

- B. 3
- C. 4
- D. 5

#### **Answer: A**



## Watch Video Solution

**65.** Let 
$$P = \begin{bmatrix} 1 & 2 & 1 \\ 0 & 1 & -1 \\ 3 & 1 & 1 \end{bmatrix}$$
. If the product PQ has inverse

$$R=egin{bmatrix} -1&0&1\ 1&1&3\ 2&0&2 \end{bmatrix}$$
 then  $Q^{-1}$  equals

A. 
$$\begin{bmatrix} 3 & 2 & 9 \\ -1 & 1 & 1 \\ 0 & 1 & 8 \end{bmatrix}$$
B. 
$$\begin{bmatrix} 5 & 2 & 9 \\ -1 & 1 & 1 \\ 0 & 1 & 7 \end{bmatrix}$$
C. 
$$\begin{bmatrix} 2 & -1 & 0 \\ 10 & 6 & 3 \\ 8 & 6 & 4 \end{bmatrix}$$

B. 
$$\begin{bmatrix} -1 & 1 & 1 \\ 0 & 1 & 7 \end{bmatrix}$$

C. 
$$\begin{bmatrix} 2 & -1 & 0 \\ 10 & 6 & 3 \\ 8 & 6 & 4 \end{bmatrix}$$

D. none of these

#### **Answer: C**



Watch Video Solution

### **Multiple Correct Answer**

- **1.** If A is unimodular, then which of the following is unimodular?
- a. -A b.  $A^{-1}$  c. adjA d.  $\omega A$ , where  $\omega$  is cube root of unity

A. 
$$-A$$

B.  $A^{-1}$ 

C. adj A

D.  $\omega A$ , where  $\omega$  is cube root of unity

#### Answer: B::C



**2.** Let  $A=a_0$  be a matrix of order 3, where  $a_{ij}=x;$  if  $i=j, x\in R, 1$  if |i-j|=1, 0; otherwise then when of the following Hold (s) good: for x=2, (a) A is a diagonal matrix (b) A is a symmetric matrix for x=2, (c) det A has the value equal to 6 (d) Let f(x)=1, det A, then the function f(x) has both the maxima and minima.

A. for x = 2, A is a diagonal matrix

B. A is a symmetric matrix

C. for x = 2, det A has the value equal to 6

D. Let  $f(x) = \det A$ , then the function f(x) has both the maxima and . . .

minima

#### Answer: B::D



**3.** 

$$A = [1 - 121], B = [a1b - 1] and (A + B)^2 = A^2 + b^2 + 2AB, then$$

$$a=\,-1$$
 b.  $a=1$  c.  $b=2$  d.  $b=\,-2$ 

A. a = -1

B. a = 1

 $\mathsf{C}.\,b=2$ 

D. b = -2

#### Answer: A::D



# **Watch Video Solution**

**4.** If AB = AandBA = B, then which of the following is/are true? A is idempotent b. B is idempotent c.  $A^T$  is idempotent d. none of these

A. (a) A is idempotent

B. (b) B is idempotent

C. (c)  $A^T$  is idempotent

D. (d) none of these

Answer: A::B::C



Watch Video Solution

**5.** If  $A(\theta) = \begin{bmatrix} \sin \theta & i \cos \theta \\ i \cos \theta & \sin \theta \end{bmatrix}$ , then which of the following is not true?

A. 
$$A( heta)^{-1} = A(\pi - heta)$$

B.  $A( heta) + A(\pi + heta)$  is a null matrix

C. A( heta) is invertible for all  $heta \in R$ 

D. 
$$A(\theta)^{-1} = A(-\theta)$$

Answer: A::B::C



**6.** Let AandB be two nonsingular square matrices,  $A^TandB^T$  are the transpose matrices of AandB, respectively, then which of the following options are correct? (correct option may be more than one) (a).  $B^TAB$  is symmetric matrix (b). if A is symmetric  $B^TAB$  is symmetric matrix (c). if B is symmetric  $B^TAB$  is skew-symmetric matrix for every matrix A A0.  $B^TAB$ 1 is skew-symmetric matrix if A1 is skew-symmetric

- A.  $B^TAB$  is symmetric matrix if A is symmetric
- $\mathbf{B}.\,B^TAB$  is symmetric matrix if  $\mathbf{B}$  is symmetric
- $\operatorname{C.}B^TAB$  is skew-symmetric matrix for every matrix  $\operatorname{A}$
- $\operatorname{D.}B^TAB$  is skew-symmetric matrix if  $\operatorname{A}$  is skew-symmetric

#### Answer: A::D



**Watch Video Solution** 

**7.** If B is an idempotent matrix, and  $A=I-B, \ \mbox{then} \ A^2=A \ \mbox{b.} \ A^2=I$  c.  $AB=O \ \mbox{d.} \ BA=O$ 

$$\mathsf{A}.\,A^2=A$$

$$\mathsf{B.}\,A^2=I$$

$$\mathsf{C}.\,AB=O$$

$$D.BA = O$$

#### Answer: A::C::D



# Watch Video Solution

8. If 
$$A_1=egin{bmatrix}0&0&0&1\\0&0&1&0\\0&1&0&0\\1&0&0&0\end{bmatrix}, A_2=egin{bmatrix}0&0&0&i\\0&0&-i&0\\0&i&0&0\\-i&0&0&0\end{bmatrix}, then A_iA_k+A_kA_i$$

is equal to

A. 
$$2I$$
 if  $i=k$ 

B. 
$$O$$
 if  $i 
eq k$ 

C. 
$$2I$$
 if  $i 
eq k$ 



View Text Solution

**9.** Suppose  $a_1, a_2, ...$  Are real numbers, with  $a_1 \neq 0$ . If  $a_1, a_2, a_3, ...$  Are in

A.P., then

A. 1)
$$A=egin{bmatrix} a_1&a_2&a_3\ a_4&a_5&a_6\ a_5&a_6&a_7 \end{bmatrix}$$
 is singular (where  $i=\sqrt{-1}$ )

B. 2)the

system

of

equations

$$a_1x + a_2y + a_3z = 0, a_4x + a_5y + a_6z = 0, a_7x + a_8y + a_9z = 0$$

has infinite number of solutions

C. 3)
$$B\begin{bmatrix} a_1 & ia_2 \\ ia_2 & a_1 \end{bmatrix}$$
 is nonsingular

D. 4)All of these

Answer: A::B::C



**10.** If  $\alpha, \beta, \gamma$  are three real numbers and

$$A = egin{bmatrix} 1 & \cos(lpha-eta) & \cos(lpha-\gamma) \ \cos(eta-lpha) & 1 & \cos(eta-\gamma) \ \cos(\gamma-lpha) & \cos(\gamma-eta) & 1 \end{bmatrix}$$
 , then which of following

is/are true? a.A is singular b. A is symmetric c. A is orthogonal d. A is not invertible

- A. A is singular
- B. A is symmetric
- C. A is orthogonal
- D. A is not invertible

#### Answer: A::B::D



Watch Video Solution

**11.** If  $D_1$  and  $D_2$  are two 3 imes 3 diagonal matrices, then which of the following is/are true ?

A.  $D_1D_2$  is a diagonal matrix

$$\operatorname{B.}D_1D_2=D_2D_1$$

C. 
$$D_1^2 + D_2^2$$
 is a diagonal matrix

D. none of these



#### Watch Video Solution

**12.** Let A be the  $2\times 2$  matrix given by  $A=\left[a_{ij}\right]$  where  $a_{ij}\in\{0,1,2,3,4\}$  such theta  $a_{11}+a_{12}+a_{21}+a_{22}=4$  then which of the following statement(s) is/are true ?

A. Number of matrices A such that the trace of A equal to 4, is 5

B. Number of matrices A, such that A is invertible is 18

C. Absolute difference between maximum value and minimum value of det (A) is 8

D. Number of matrices A such that A is either symmetric (or) skew symmetric and det (A) is divisible by 2, is 5.

13. If 
$$S = \begin{bmatrix} 0 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \end{bmatrix} and A = \begin{bmatrix} b+c & c+a & b-c \\ c-b & c+b & a-b \\ b-c & a-c & a+b \end{bmatrix} (a,b,c \neq 0), then SAS^{-1}$$

A. symmetric matrix

is

B. diagonal matrix

C. invertible matrix

D. singular matrix



14. P is a non-singular matrix and A, B are two matrices such that

 $B=P^{\,-1}AP$ . The true statements among the following are

A. A is invertible iff B is invertible

B.  $B^n = P^{\,-1}A^nP\,orall n \in N$ 

C. 
$$\forall \lambda \in R, B - \lambda I = P^{-1}(A - \lambda I)P$$

D. A and B are both singular matrices



### Watch Video Solution

**15.** Let 
$$A = egin{bmatrix} 1 & 2 & 2 \ 2 & 1 & 2 \ 2 & 2 & 1 \end{bmatrix}$$
 . Then

A. 
$$A^2 - 4A - 5I_3 = O$$

B. 
$$A^{-1}=rac{1}{5}(A-4I_3)$$

 $\mathsf{C.}\,A^3$  is not invertible

 $\operatorname{D.}A^2$  is invertible



**16.** If  $A = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix}$ , then which is true (a)  $A^3 - A^2 = A - I$  (b) det.

$$egin{aligned} \left(A^{100}-I
ight)=0 ext{ (c) } A^{200}=egin{bmatrix} 1 & 0 & 0 \ 100 & 1 & 0 \ 100 & 0 & 1 \end{bmatrix} ext{ (d) } A^{100}=egin{bmatrix} 1 & 1 & 0 \ 50 & 1 & 0 \ 50 & 0 & 1 \end{bmatrix} \end{aligned}$$

$$A. A^3 - A^2 = A - I$$

B. det. 
$$\left(A^{100}-I
ight)=0$$

$$\mathsf{C.}\,A^{200} = egin{bmatrix} 1 & 0 & 0 \ 100 & 1 & 0 \ 100 & 0 & 1 \end{bmatrix} \ \mathsf{D.}\,A^{100} = egin{bmatrix} 1 & 1 & 0 \ 50 & 1 & 0 \ 50 & 0 & 1 \end{bmatrix}$$

D. 
$$A^{100} = egin{bmatrix} 1 & 1 & 0 \ 50 & 1 & 0 \ 50 & 0 & 1 \end{bmatrix}$$



17. If Ais symmetric and B is skew-symmetric matrix, then which of the following is/are CORRECT?

A.  $ABA^T$  is skew-symmetric matrix

B.  $AB^T + BA^T$  is symmetric matrix

C. (A + B)(A - B) is skew-symmetric

D. (A+I)(B-I) is symmetric



**18.** If 
$$A=ig(a_{ij}ig)_{n imes n}$$
 and  $f$  is a function, we define  $f(A)=ig(ig(fig(a_{ij}ig)ig)_{n imes n}$ , Let  $A=ig(\frac{\pi/2- heta}{- heta} \frac{ heta}{\pi/2- heta}ig)$  . Then

A.  $\sin A$  is invertible

 $B. \sin A = \cos A$ 

 $\mathsf{C}.\sin A$  is orthogonal

 $\mathsf{D.}\sin(2A) = 2\sin A\cos A$ 



**19.** If A is a matrix such that  $A^2 + A + 2I = O$ ; the which of the following is/are true? (a) A is non-singular (b) A is symmetric (c) A cannot be skew-symmetric (d)  $A^{-1} = -\frac{1}{2}(A+I)$ 

A. A is nonsingular

B. A is symmetric

C. A cannot be skew-symmetric

D. 
$$A^{-1} = -\frac{1}{2}(A+I)$$



**20.** If 
$$A=\begin{bmatrix}3&-3&4\\2&-3&4\\0&-1&1\end{bmatrix}$$
 , then the trace of the matrix  $Adj(AdjA)$  is

A. 
$$adj(adjA) = A$$

D. none of these

**Answer: B** 



Watch Video Solution

**21.** If 
$$\begin{bmatrix} 1 & - an heta \\ an heta & 1 \end{bmatrix} \begin{bmatrix} 1 & an heta \\ - an heta & 1 \end{bmatrix}^{-1} = \begin{bmatrix} a & -b \\ b & a \end{bmatrix}$$
, then

A. 
$$a=\cos 2 heta$$

B. 
$$a = 1$$

C. 
$$b=\sin 2 heta$$

D. 
$$b = -1$$



**22.** If 
$$A^{-1}=\begin{bmatrix} 1 & -1 & 2 \\ 0 & 3 & 1 \\ 0 & 0 & -\frac{1}{3} \end{bmatrix}$$
 , then  $|A|=-1$ 

22. If 
$$A^{-1} = \begin{bmatrix} 0 & 3 & 1 \\ 0 & 0 & -\frac{1}{3} \end{bmatrix}$$
 , then  $|A| = -1$  b.  $adjA = \begin{bmatrix} -1 & 1 & -2 \\ 0 & -3 & -1 \\ 0 & 0 & \frac{1}{3} \end{bmatrix}$  c.  $A = \begin{bmatrix} 1 & \frac{1}{3} & 7 \\ 0 & \frac{1}{3} & 1 \\ 0 & 0 & -3 \end{bmatrix}$  d.

$$A = egin{bmatrix} 1 & -rac{1}{3} & -7 \ 0 & -3 & 0 \ 0 & 0 & 1 \end{bmatrix}$$

A. 
$$|A|=-1$$

B. adj 
$$A=egin{bmatrix} -1&1&-2\0&-3&-1\0&0&1/3 \end{bmatrix}$$

C. 
$$A = \begin{bmatrix} 0 & 0 & 1/3 \\ 1 & 1/3 & 7 \\ 0 & 1/3 & 1 \\ 0 & 0 & -3 \end{bmatrix}$$
D.  $A = \begin{bmatrix} 1 & -1/3 & -7 \\ 0 & -3 & 0 \\ 0 & 0 & 1 \end{bmatrix}$ 

**23.** If 
$$A$$
 is an invertible matrix, then  $\left(adjA^{-1}\right)$  is equal to a.  $\left[adjA^{-1}\right]$  b.  $A$  c.  $A$  d.  $(\det A)A$ 

A. adj. 
$$\left(A^{\,-\,1}
ight)$$

B. 
$$\frac{A}{\det. A}$$

 $\mathsf{C}.\,A$ 



# **Watch Video Solution**

24. If A and B are two invertible matrices of the same order, then adj (AB)

is equal to

B. 
$$|B||A|B^{-1}A^{-1}$$

C. 
$$|B||A|A^{-1}B^{-1}$$

D. 
$$|A||B|(AB)^{-1}$$



**25.** If AandB are three square matrices of the same order, then AB=ACB=C. Then  $|A|\neq 0$  b. A is invertible c. A may be orthogonal d. is symmetric

A. 
$$|A| 
eq 0$$

B. A is invertible

C. A may be orthogonal

D. A is symmetric



**26.** If A and B are two non singular matrices and both are symmetric and commute each other, then

A. 
$$A^{-1}B$$

B.  $AB^{-1}$ 

$$C. A^{-1}B^{-1}$$

D. none of these



27. If A and B are square matrices of order 3 such that  $A^3=8B^3=8I$  and det.  $(AB-A-2B+2I)\neq 0$ , then identify the correct statement(s), where I is identity matrix of order 3. (A)  $A^2+2A+4I=O$  (B)  $A^2+2A+4I\neq O$  (C)  $B^2+B+I=O$  (D)

$$B^2+B+I 
eq O$$

$$\mathsf{A.}\,A^2+2A+4I=O$$

B.  $A^2 + 2A + 4I \neq O$ 

 $C \cdot B^2 + B + I = O$ 

 $\mathsf{D}.\,B^2+B+I\neq O$ 

## Answer: $A^{(2)}+2A+4I=0$ and $B^{(2)}+B+I=0$



Watch Video Solution

28. Let A, B be two matrices different from identify matrix such that

AB = BA and  $A^n - B^n$  is invertible for some positive integer n. If

 $A^{n} - B^{n} = A^{n+1} - B^{n+1} = A^{n+2} - B^{n+2}$ , then

A. I-A is non-singular

B. I-B is non-singular

C. I-A is singular

D. I-B is singular



**29.** Let A and B be square matrices of the same order such that  $A^2=I$  and  $B^2=I$ , then which of the following is CORRECT ?

A. IF A and B are inverse to each other, then A=B.

B. If AB=BA, then there exists matrix  $C=\dfrac{AB+BA}{2}$  such that  $C^2=C$ .

C. If AB=BA, then there exists matrix D=AB-BA such that

 $D^n=O$  for some  $n\in N$ .

D. If AB=BA then  $(A+B)^5=16(A+B)$ .



Watch Video Solution

**30.** Let B is an invertible square matrix and B is the adjoint of matrix A such that  $AB=B^T.$  Then

- A. A is an identity matrix
- B. B is symmetric matrix
- C. A is a skew-symmetric matrix
- D. B is skew symmetic matrix

#### **Answer: A**



- **31.** First row of a matrix A is [1, 3, 2]. If
- adj  $A=egin{bmatrix} -2 & 4 & lpha \ -1 & 2 & 1 \ 3lpha & -5 & -2 \end{bmatrix}$  , then a det (A) is
  - $\mathsf{A.}-2$
  - B. 1
  - C. 0
  - D. 1

32. Let A be a square matrix of order 3 satisfies the relation

$$A^3-6A^2+7A-8I={\it O}$$
 and  $B=A-2I$ . Also, det.  $A=8$ , then

A. det. 
$$\left( {{
m adj.} \ \, } \left( {I - 2{A^{ - 1}}} \right) = rac{{25}}{{16}}$$

B. adj. 
$$\left(\left(\frac{B}{2}\right)^{-1}\right)=\frac{B}{10}$$

C. det. 
$$\left(\operatorname{adj.}\ \left(I-2A^{-1}\right)\right)=\frac{75}{32}$$

D. adj. 
$$\left(\left(\frac{B}{2}\right)^{-1}\right) = \frac{2B}{5}$$



33. Which of the following matrices have eigen values as 1 and -1?

A. 
$$\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$$

B. 
$$\begin{bmatrix} 0 & -i \\ i & 0 \end{bmatrix}$$

$$\begin{array}{ccc}
\mathsf{C.} \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix} \\
\mathsf{D.} \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$



**34.** Let MandN be two  $3 \times 3$  non singular skew-symmetric matrices such that MN=NM. If  $P^T$  denote the transpose of P, $M^2N^2ig(M^TN^{-1}ig)^T$  is equal to  $M^2$  b.  $-N^2$  c.  $-M^2$  d. MN

A. 
$$M^2$$

$$B.-N^2$$

$$\mathsf{C.}-M^2$$

D. 
$$MN$$

#### **Answer: C**



**35.** Let  $\omega$  be a complex cube root of unity with  $\omega \neq 1 and P = \left[p_{ij}\right]$  be a  $n \times n$  matrix withe  $p_{ij} = \omega^{i+j}$ . Then  $p^2 \neq O, n = a$ . 57b. 55c. 58d. 56`

A. 57

B. 55

C. 58

D. 56

#### Answer: B::C::D



**Watch Video Solution** 

is symmetric or skew-symmetric.

**36.** For  $3 \times 3$  matrices M and N, which of the following statement (s) is (are) NOT correct ?

Statement - I :  $N^T M N$  is symmetric or skew-symmetric, according as M

Statement - II : MN-NM is skew-symmetric for all symmetric matrices

MandN.

Statement - III : MN is symmetric for all symmetric matrices MandN.

Statement - IV : (adjM)(adjN)=adj(MN) for all invertible matrices MandN.

A.  $N^TMN$  is symmetric or skew-symmetric, according as M is symmetric or skew-symmetric

B. MN-NM is skew0symmetric for all symmetric matrices M and N

D. (adj M ) (adj N) = adj (MN) for all inveriblr matrices M and N.

C. MN is symmetric for all symmetric matrices M and N

#### Answer: C::D



**37.** Let M be a  $2\times 2$  symmetric matrix with integer entries. Then M is invertible if The first column of M is the transpose of the second row of M The second row of M is the transpose of the first column of M is a diagonal matrix with non-zero entries in the main diagonal The product of entries in the main diagonal of M is not the square of an integer

- A. the first column of M is the transpose of the second row of M
- B. the second row of M is the transpose of the column of M
- C. M is a diagonal matrix with non-zero entries in the main diagonal
- D. the product of entries in the main diagonal of M is not the square of an integer

#### **Answer: C::D**



**Watch Video Solution** 

- **38.** Let m and N be two 3x3 matrices such that MN=NM. Further if  $M \neq N^2$  and  $M^2 = N^4$  then which of the following are correct.
  - A. determinant of  $\left(M^2+Mn^2
    ight)$  is 0
  - B. there is a 3 imes 3 non-zero matrix U such that  $ig(M^2+MN^2ig)U$  is the
  - C. determinant of  $(M^2 + MN^2) \geq 1$

zero matrix

D. for a 3 imes 3 matrix U, is the zero matrix

Answer: A::B



**Watch Video Solution** 

**39.** Let X and Y be two arbitrary,  $3\times 3$ , non-zero, skew-symmetric matrices and Z be an arbitrary  $3\times 3$ , non-zero, symmetric matrix. Then which of the following matrices is (are) skew symmetric?

A. 
$$Y^3Z^4-Z^4Y^3$$

B. 
$$X^{44} + Y^{44}$$

$$\mathsf{C.}\,X^4Z^3-Z^3X^4$$

D. 
$$X^{23} + Y^{23}$$

Answer: C::D



**40.** Let  $p=egin{bmatrix} 3&-1&-2\ 2&0&lpha\ 3&-5&0 \end{bmatrix}$  , where  $lpha\in\mathbb{R}.$  Suppose  $Q=egin{bmatrix} q_{ij} \end{bmatrix}$  is a

matrix such that PQ=kI, where  $k\in\mathbb{R}, k
eq 0$  and I is the identity matrix of order 3. If  $q_{23}=-rac{k}{8}$  and  $\det(Q)=rac{k^2}{2},$  then

A. 
$$\alpha=0$$
,  $k=8$ 

B.  $4\alpha - k + 8 = 0$ 

C. 
$$\mathsf{det}\left(\mathrm{P}\:\mathrm{adj}\left(\mathrm{Q}\right)\right)=2^{9}$$

D. 
$$\mathsf{det}\left(\mathrm{Q}\:\mathrm{adj}\left(\mathrm{P}
ight)
ight)=2^{13}$$

### Answer: B::C



**41.** Which of the following is(are) NOT of the square of a  $3\times 3$  matrix with real enteries?

A. 
$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{bmatrix}$$

B. 
$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{bmatrix}$$
C. 
$$\begin{bmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{bmatrix}$$
D. 
$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

#### Answer: A::C



## Watch Video Solution

**42.** Let S be the set of all column matrices 
$$egin{bmatrix} b_1 \ b_2 \ b_3 \end{bmatrix}$$
 such that  $b_1,b_2,b_2\in R$ 

and the system of equations (in real variables)

$$2x - 4y + 3z = b_2$$

 $-x + 2y + 5z = b_1$ 

 $x - 2y + 2z = b_3$ 

$$3z=t$$

has at least one solution. Then, which of the following system (s) (in real variables) has (have) at least one solution for each  $\left|egin{array}{c} b_1 \ b_2 \ \end{array}
ight| \ \in S$  ?

A. 
$$x + 2y + 3z = b_1$$
,  $4y + 5z = b_2$  and  $x + 2y + 6z = b_3$ 

B. 
$$x+y+3z=b_1,$$
  $5x+2y+6z=b_2$  and  $-2x-y-3z=b_3$ 

C. 
$$x+2y-5z=b_1, 2x-4y+10z=b_2$$
 and  $x-2y+5z=b_3$ 

D. 
$$x+2y+5z=b_1,$$
  $2x+3z=b_2$  and  $x+4y-5z=b_3$ 

#### Answer: A::D



**43.** If 
$$A=egin{bmatrix}1&0&0\\1&0&1\\0&1&0\end{bmatrix}$$
 , then which is true (a)  $A^3-A^2=A-I$  (b) det.

$$egin{aligned} \left(A^{100}-I
ight)=0 ext{ (c) } A^{200}=egin{bmatrix} 1 & 0 & 0 \ 100 & 1 & 0 \ 100 & 0 & 1 \end{bmatrix} ext{(d) } A^{100}=egin{bmatrix} 1 & 1 & 0 \ 50 & 1 & 0 \ 50 & 0 & 1 \end{bmatrix} \end{aligned}$$

A. 
$$A^3 - A^2 = A - I$$

$$\operatorname{B.} Det \left( A^{2010} - I \right) = 0$$

$$\mathsf{C.}\,A^{50} = egin{bmatrix} 1 & 0 & 0 \ 25 & 1 & 0 \ 25 & 0 & 1 \end{bmatrix}$$

D. 
$$A^{50}=egin{bmatrix} 1 & 1 & 0 \ 25 & 1 & 0 \ 25 & 0 & 1 \end{bmatrix}$$

## Answer: A::B::C



**Watch Video Solution** 

**44.** If the elements of a matrix A are real positive and distinct such that

- $\detig(A+A^Tig)^T=0$  then
  - A.  $\det A > 0$
  - B.  $\det A \geq 0$
  - $\mathsf{C}.\det(A-A^T)>0$
  - D.  $\det(A. A^T) > 0$

## Answer: A::C::D



**45.** If 
$$A = \begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{bmatrix}$$
 and  $X$  is a non zero column matrix such

that  $AX = \lambda X$ , where  $\lambda$  is a scalar, then values of  $\lambda$  can be

- A. 3
- B. 6
- C. 12
- D. 15

#### Answer: A::D



Watch Video Solution

**46.** If A, B are two square matrices of same order such that

A+B=AB and  $\emph{I}$  is identity matrix of order same as that of  $\emph{A,B}$  , then

A. A. 
$$AB=BA$$

B. B. 
$$|A - I| = 0$$

C. C. 
$$|B-I| 
eq 0$$

D. D. 
$$|A - B| = 0$$

#### Answer: A::C



Watch Video Solution

**47.** If A is a non-singular matrix of order n imes n such that

$$3ABA^{-1} + A = 2A^{-1}BA$$
, then

A. A and B both are identity matrices

$$|B| |A| + |B| = 0$$

$$\mathsf{C.} \left| ABA^{-1} - A^{-1}BA \right| = 0$$

D. A + B is not a singular matrix

#### Answer: B::C



**48.** If the matrix A and B are of  $3\times 3$  and (I-AB) is invertible, then which of the following statement is/are correct ?

A. I - BA is not invertible

B. I-BA is invertible

C. I-BA has for its inverse  $I+B(I-AB)^{-1}A$ 

D. I-BA has for its inverse  $I+A(I-BA)^{-1}B$ 

#### Answer: B::C



## Watch Video Solution

**49.** Let a be square matrix such that  $A(\mathrm{adj.\ A})=egin{bmatrix} 4&0&0\\0&4&0\\0&0&4 \end{bmatrix}$ 

then find the value of

(i)  $|adj.\ A|$  (ii)  $|adj.\ (adj.\ A)|$  (iii)  $|adj.\ (3A)|$ 

A. |A|=4

 $\operatorname{B.}|adjA|=16$ 

$$A^2-(\epsilon I)$$

C.  $\dfrac{|adj(adjA)|}{|adjA|}=16$ 

Watch Video Solution

**Linked Comprehension Type** 

 $\mathsf{D.}\left|adj2A\right|=128$ 

Answer: A::B::C

$$A^2-(a+d)A+(ad-bc)I$$
 is equal to

**1.** Let A be a matrix of order 2 imes 2 such that  $A^2 = O$ .

B. *O* 

 $\mathsf{C}.-I$ 

D. none of these

**Answer: B** 

**2.** Let A be a matrix of order 
$$2 \times 2$$
 such that  $A^2 = O$ .

tr (A) is equal to

- **A.** 1
- **B**. 0
- C. -1

D. none of these

#### Answer: B



Watch Video Solution

# **3.** Let A be a matrix of order 2 imes 2 such that $A^2 = O$ .

$$(I+A)^{100} =$$

A. 100 A

B. 100(I + A)

C. 100I + A

 $\mathsf{D}.\,I + 100A$ 

#### Answer: D



**Watch Video Solution** 

**4.** If A and B are two square matrices of order 3 imes 3 which satify AB = A

and BA = B, then

Which of the following is true?

A. If matrix A is singular, then matrix B is nonsingular.

B. If matrix A is nonsingular, then materix B is singular.

C. If matrix A is singular, then matrix B is also singular.

D. Cannot say anything.

Answer: C

**5.** if 
$$A$$
 and  $B$  are two matrices of order  $3 imes 3$ so that  $AB = A$  and

$$BA = B \operatorname{then} (A + B)^7 =$$

A. 
$$7(A + B)$$

B. 7. 
$$I_{3\times3}$$

$$\mathsf{C.}\,64(A+B)$$

D. 
$$128I$$

### Answer: C



**Watch Video Solution** 

**6.** If A and B are two square matrices of order 3 imes 3 which satify AB = A and BA = B, then

$$(A+I)^5$$
 is equal to (where I is idensity matric)

A. 
$$I+60A$$

 $\mathrm{B.}\,I+16A$ 

 $\mathsf{C}.\,I + 31A$ 

D. none of these

#### **Answer: C**



Watch Video Solution

**7.** Consider an arbitarary 3 imes 3 non-singular matrix  $Aig[a_{
m ij}ig].$  A matrix

 $B = igl[b_{
m ij}igr]$  is formed such that  $b_{
m ij}$  is the sum of all the elements except  $a_{
m ij}$ 

in the ith row of A. Answer the following questions:

If there exists a matrix X with constant elemts such that AX=B`, then X is

A. skew-symmetric

B. null matrix

C. diagonal matrix

D. none of these

#### **Answer: D**



**Watch Video Solution** 

- **8.** Let  $A=\left[a_{ij}\right]$  be 3 imes 3 matrix and  $B=\left[b_{ij}\right]$  be 3 imes 3 matrix such that  $b_{ij}$  is the sum of the elements of  $i^{th}$  row of A except  $a_{ij}$ . If det, (A)=19, then the value of det. (B) is \_\_\_\_\_\_.
  - A. |A|
  - B. |A|/2
  - $\mathsf{C}.\,2|A|$
  - D. none of these

#### **Answer: C**



**9.** Let 
$$A=egin{bmatrix}1&0&0\\1&0&1\\0&1&0\end{bmatrix}$$
 satisfies  $A^n=A^{n-2}+A^2-I$  for  $n\geq 3$ . And

trace of a square matrix X is equal to the sum of elements in its proncipal diagonal.

Further consider a matrix  $\bigcup_{3\times 3}$  with its column as  $\cup_1$  ,  $\cup_2$  ,  $\cup_3$  such that

$$A^{50} \cup_1 \ = egin{bmatrix} 1 \ 25 \ 25 \end{bmatrix}, A^{50} \cup_2 \ = egin{bmatrix} 0 \ 1 \ 0 \end{bmatrix}, A^{50} \cup_3 \ = egin{bmatrix} 0 \ 0 \ 1 \end{bmatrix}$$

Then answer the following question:

The value of  $|\cup|$  equals

A. 0

B. 1

C. -1

D. 25

#### **Answer: B**



**10.** Let 
$$A=\begin{bmatrix}1&0&0\\1&0&1\\0&1&0\end{bmatrix}$$
 satisfies  $A^n=A^{n-2}+A^2-I$  for  $n\geq 3$ . And

trace of a square matrix X is equal to the sum of elements in its proncipal diagonal.

Further consider a matrix  $\bigcup_{3\times 3}$  with its column as  $\cup_1$  ,  $\cup_2$  ,  $\cup_3$  such that

$$A^{50} \cup_1 \ = egin{bmatrix} 1 \ 25 \ 25 \end{bmatrix}, A^{50} \cup_2 \ = egin{bmatrix} 0 \ 1 \ 0 \end{bmatrix}, A^{50} \cup_3 \ = egin{bmatrix} 0 \ 0 \ 1 \end{bmatrix}$$

Then answer the following question:

The value of  $|\cup|$  equals

A. 0

B. 1

C. 2

D. 3

#### **Answer: D**



**11.** Let 
$$A=\begin{bmatrix}1&0&0\\1&0&1\\0&1&0\end{bmatrix}$$
 satisfies  $A^n=A^{n-2}+A^2-I$  for  $n\geq 3$ . And

trace of a square matrix X is equal to the sum of elements in its proncipal diagonal.

Further consider a matrix  $\bigcup_{3\times 3}$  with its column as  $\cup_1$  ,  $\cup_2$  ,  $\cup_3$  such that

$$A^{50} \cup_1 \ = egin{bmatrix} 1 \ 25 \ 25 \end{bmatrix}, A^{50} \cup_2 \ = egin{bmatrix} 0 \ 1 \ 0 \end{bmatrix}, A^{50} \cup_3 \ = egin{bmatrix} 0 \ 0 \ 1 \end{bmatrix}$$

Then answer the following question:

The value of  $|\cup|$  equals

A. 0

B. 1

C. 2

D. -1

#### Answer: B



**12.** Let for 
$$A=\begin{bmatrix}1&0&0\\2&1&0\\3&2&1\end{bmatrix}$$
 , there be three row matrices  $R_1,R_2$  and  $R_3$ , satisfying the relations,  $R_1A=\begin{bmatrix}1&0&0\end{bmatrix},R_2A=\begin{bmatrix}2&3&0\end{bmatrix}$  and

 $R_3A = [\, 2 \ \ 3 \ \ 1\,].$  If B is square matrix of order 3 with rows  $R_1,R_2$  and

 $R_3$  in order, then

The value of det.  $\left(2A^{100}B^3-A^{99}B^4
ight)$  is

$$A.-2$$

B. - 1

C. 2

D. -27

Answer: D



## Watch Video Solution

**13.** Let for  $A=egin{bmatrix}1&0&0\\2&1&0\\3&2&1\end{bmatrix}$  , there be three row matrices  $R_1,R_2$  and  $R_3$  , satifying the relations,  $R_1A= [\, 1 \ \ 0 \ \ 0\, ], R_2A= [\, 2 \ \ 3 \ \ 0\, ]$  and

 $R_3A = [\, 2 \quad 3 \quad 1\,].$  If B is square matrix of order 3 with rows  $R_1,\,R_2$  and

**14.** A and B are square matrices such that  $\det.\ (A)=1,BB^T=I$ ,  $\det$ 

 $R_3$  in order, then

The value of det. (B) is

A. 
$$-27$$

B. - 9

D. 9

**C**. 3

## \_\_\_

**Answer: A** 



(B)>0, and A( adj. A + adj. B)=B.

The value of  $\det (A + B)$  is

A. -2

B. -1

C. 0

D. 1

**Answer: D** 



Watch Video Solution

**15.** A and B are square matrices such that  $\det$   $(A)=1,BB^T=I$ ,  $\det$ 

(B) > 0, and A( adj. A + adj. B)=B.

The value of  $\det (A + B)$  is

A.  $B^{-1}A$ 

 $B.AB^{-1}$ 

C.  $A^{T}B^{-1}$ 

D.  $B^{T}A^{-1}$ 

#### Answer: A



**16.** Let A be an  $m \times n$  matrix. If there exists a matrix L of type  $n \times m$  such that  $LA = I_n$ , then L is called left inverse of A. Which of the following matrices is NOT left inverse of matrix  $\begin{bmatrix} 1 & -1 \\ 1 & 1 \\ 2 & 3 \end{bmatrix}$ ?

$$\begin{array}{ccccc} \text{A.} & \left[ \begin{array}{ccc} \frac{1}{2} & \frac{1}{2} & 0 \\ -\frac{1}{2} & \frac{1}{2} & 0 \end{array} \right] \\ \text{B.} & \left[ \begin{array}{cccc} 2 & -7 & 3 \\ -\frac{1}{2} & \frac{1}{2} & 0 \end{array} \right] \\ \text{C.} & \left[ \begin{array}{cccc} -\frac{1}{2} & \frac{1}{2} & 0 \\ -\frac{1}{2} & \frac{1}{2} & 0 \end{array} \right] \\ \text{D.} & \left[ \begin{array}{cccc} 0 & 3 & -1 \\ -\frac{1}{2} & \frac{1}{2} & 0 \end{array} \right] \end{array}$$

#### Answer: C



**Watch Video Solution** 

17. Let A be an m imes n matrix. If there exists a matrix L of type n imes m such that  $LA=I_n$ , then L is called left inverse of A. Similarly, if there exists a matrix R of type n imes m such that  $AR=I_m$ , then R is called right inverse

of A.

For example, to find right inverse of matrix

$$A=egin{bmatrix}1&-1\1&1\2&3\end{bmatrix}$$
 , we take  $R=egin{bmatrix}x&y&x\u&v&w\end{bmatrix}$ 

and solve $AR=I_3$ , i.e.,

$$\begin{bmatrix} 1 & -1 \\ 1 & 1 \\ 2 & 3 \end{bmatrix} \begin{bmatrix} x & y & z \\ u & v & w \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\implies x - u = 1 \quad y - v = 0 \quad z - w = 0$$

$$x + u = 0 \quad y + v = 1 \quad z + w = 0$$

$$2x + 3u = 0 \quad 2y + 3v = 0 \quad 2z + 3w = 1$$

As this system of equations is inconsistent, we say there is no right

inverse for matrix A.

The number of right inverses for the matrix  $\begin{bmatrix} 1 & -1 & 2 \\ 2 & -1 & 1 \end{bmatrix}$  is

A. 0

C. 2

B. 1

D. infinite

### Answer: D



**18.** Let A be an m imes n matrix. If there exists a matrix L of type n imes m such that  $LA = I_n$ , then L is called left inverse of A. Similarly, if there exists a matrix R of type n imes m such that  $AR = I_m$ , then R is called right inverse of A.

For example, to find right inverse of matrix

$$A = egin{bmatrix} 1 & -1 \ 1 & 1 \ 2 & 3 \end{bmatrix}$$
 , we take  $R = egin{bmatrix} x & y & x \ u & v & w \end{bmatrix}$ 

and solve $AR=I_3$ , i.e.,

$$\begin{bmatrix} 1 & -1 \\ 1 & 1 \\ 2 & 3 \end{bmatrix} \begin{bmatrix} x & y & z \\ u & v & w \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\implies x - u = 1 \quad y - v = 0 \quad z - w = 0$$

$$x + u = 0 \quad y + v = 1 \quad z + w = 0$$

$$2x + 3u = 0 \quad 2y + 3v = 0 \quad 2z + 3w = 1$$

As this system of equations is inconsistent, we say there is no right inverse for matrix A.

For which of the following matrices, the number of left inverses is greater than the number of right inverses ?

A. 
$$\begin{bmatrix} 1 & 2 & 4 \\ -3 & 2 & 1 \end{bmatrix}$$

B. 
$$\begin{bmatrix} 3 & 2 & 1 \\ 3 & 2 & 1 \end{bmatrix}$$
C. 
$$\begin{bmatrix} 1 & 4 \\ 2 & -3 \\ 2 & -3 \end{bmatrix}$$
D. None of these

## Answer: C



Watch Video Solution

are either 0 or 1. Five of these entries are 1 and four of them are 0. The number of matrices in A is

**19.** Let A be the set of all  $3 \times 3$  symmetric matrices all of whose entries

- A. 12

B. 6

- C. 9
- D. 3

Answer: A

**20.** Let A be the set of all  $3 \times 3$  symmetric matrices all of whose either 0 or 1. Five of these entries are 1 and four of them are 0.

The number of matrices A in A for which the system of linear equations

$$A \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$

is inconsistent is: (A) less than 4 (B) at least 4 but less than 7 (C) at least

7 but less than 10 (D) at least 10

A. less than 4

B. at least 4 but less than 7

C. at least 7 but less than 10

D. at leat 10

#### **Answer: B**



**21.** Let A be the set of all  $3 \times 3$  symmetric matrices all of whose either 0 or 1. Five of these entries are 1 and four of them are 0.

The number of matrices A in A for which the system of linear equations

$$A egin{bmatrix} x \ y \ z \end{bmatrix} = egin{bmatrix} 1 \ 0 \ 0 \end{bmatrix}$$

is inconsistent is: (A) less than 4 (B) at least 4 but less than 7 (C) at least

7 but less than 10 (D) at least 10

A. 0

B. more than 2

C. 2

D. 1

#### Answer: B



Watch Video Solution

**22.** Let P be an odd prime number and  $T_p$  be the following set of 2 imes 2

matrices :

The number of A in  $T_p$  such that the trace of a is not divisible by p but det (A) divisible by p is [Note : The trace of matrix is the sum of its diaginal entries].

A. 
$$(p-1)^2$$

B. 
$$2(p-1)$$

C. 
$$(p-1)^2 + 1$$

D. 
$$2p - 1$$

#### Answer: D



## Watch Video Solution

**23.** Let P be an odd prime number and  $T_p$  be the following set of 2 imes 2 matrices :

$$T_P = \left\{A = \left[egin{array}{cc} a & b \ c & a \end{array}
ight] : a,b,c \in \{0,1,...,p-1\}
ight\}$$

The number of A in  $T_P$  such that det (A) is not divisible by p is

A. 
$$(p-1)ig(p^2-p+1ig)$$

B. 
$$p^3 - (p-1)^2$$

C. 
$$(p-1)^2$$

D. 
$$(p-1)(p^2-2)$$

#### Answer: C



Watch Video Solution

**24.** Let p be an odd prime number and  $T_p$ , be the following set of 2 imes 2 matrices  $T_p = \left\{A = \begin{bmatrix} a & b \\ c & a \end{bmatrix} : a,b,c \in \{0,1,2,......p-1\}\right\}$  The

number of A in  $T_p$ , such that A is either symmetric or skew-symmetric or

both, and det (A) divisible by p is

B. 
$$p^3-5p$$

D. 
$$p^3-p^2$$

#### **Answer: D**



### **Watch Video Solution**

25. Let a,b, and c be three real numbers satistying

$$[a,b,c]egin{bmatrix}1&9&7\8&2&7\7&3&7\end{bmatrix}=[0,0,0]$$
 If the point  $P(a,b,c)$  with reference to (E),

lies on the plane 2x+y+z=1, the the value of 7a+b+c is

A. 0

B. 12

C. 7

D. 6

#### **Answer: D**



26. Let a,b, and c be three real numbers satistying

$$[a,b,c]egin{bmatrix}1&9&7\8&2&7\7&3&7\end{bmatrix}=[0,0,0]$$
 If the point  $P(a,b,c)$  with reference to (E),

lies on the plane 2x + y + z = 1, the the value of 7a + b + c is

$$A.-2$$

B. 2

C. 3

D.-3

#### Answer: A



## Watch Video Solution

a,b, and c be three real numbers satistying  $[a,b,c]egin{bmatrix}1&9&7\8&2&7\7&3&7\end{bmatrix}=[0,0,0]$  Let b=6, with a and c satisfying (E). If lpha and

$$eta$$
 are the roots of the quadratic equation  $ax^2+bx+c=0 then \sum_{n=0}^{\infty} \left(rac{1}{lpha}+rac{1}{eta}
ight)^n$  is (A) 6 (B) 7 (C)  $rac{6}{7}$  (D) oo

$$\mathsf{C.}\;\frac{6}{7}$$

D. 
$$\infty$$

## Answer: B



Matrix Type

## **1.** Match the following lists:

List I	List II
<b>a.</b> $(I-A)^n$ is if A is idempotent	<b>p.</b> $2^{n-1}(I-A)$
<b>b.</b> $(I - A)^n$ is if A is involuntary	$\mathbf{q.} I - nA$
<b>c.</b> $(I-A)^n$ is if A is nilpotent of index 2	r. A
<b>d.</b> If A is orthogonal, then $(A^T)^{-1}$	s. I – A



Watch Video Solution

## 2. Match the following lists:

List I	List II
a. If A is an idempotent matrix and I is an identity matrix of the same order, then the value of $n$ , such that $(A + I)^n = I + 127$ is	<b>p.</b> 9
<b>b.</b> If $(I - A)^{-1} = I + A + A^2 + \dots + A^7$ , then $A^n = O$ , where <i>n</i> is	<b>q.</b> 10
<b>c.</b> If <i>A</i> is matrix such that $a_{ij} = (i + j)(i - j)$ , then <i>A</i> is singular if order of matrix is	r. 7
<b>d.</b> If a nonsingular matrix $A$ is symmetric, show that $A^{-1}$ is also symmetric, then order of $A$ can be	s. 8

# 3. Match the following lists:

List I (A, B, C are matrices)	List II
<b>a.</b> If $ A  = 2$ , then $ 2A^{-1}  = $ (where <i>A</i> is of order 3)	p. 1
<b>b.</b> If $ A  = 1/8$ , then $ adj(adj(2A))  =$ (where A is of order 3)	q. 4
c. If $(A + B)^2 = A^2 + B^2$ , and $ A  = 2$ , then $ B  = $ (where $A$ and $B$ are of odd order)	r. 24
<b>d.</b> $ A_{2\times 2}  = 2$ , $ B_{3\times 3}  = 3$ and $ C_{4\times 4}  = 4$ , then $ ABC $ is equal to	s. 0
	t. does not exist



# Watch Video Solution

**4.** Consider a matrix  $A = \left[a_{ ext{ij}}
ight]$  of order 3 imes 3 such that  $a_{ ext{ij}} = \left(k
ight)^{i+j}$ where  $k \in I$ .

Match List I with List II and select the correct answer using the codes

given below the lists.

List I	List II
a. A is singular if	p. $k \in \{0\}$
b. A is null matrix if	$q. k \in \phi$
c. A is skew-symmetric which is not null matrix if	<b>r.</b> <i>k</i> ∈ <i>I</i>
$d.  A^2 = 3A \text{ if}$	$s. k \in \{-1, 0, 1\}$

a b c dr p s q

c.  $\begin{pmatrix} a & b & c & d \end{pmatrix}$ 

D.  $a \quad b \quad c \quad d$ 

**Answer: C** 



# **5.** Match the following lists:

	List I	List II
a.	If $M_r = \begin{bmatrix} r-1 & \frac{1}{r} \\ 1 & \frac{1}{(r-1)^2} \end{bmatrix}$ and $ M_r $ is the corresponding determinant, then $\lim_{n \to \infty} ( M_2  +  M_3  + \dots +  M_n ) =$	<b>p.</b> 0
b.	If $(A + B)^2 = A^2 + B^2$ and $ A  = 2$ then $ B  =$ (where A and B are matrices of odd order)	q. 1
c.	If $A = \begin{bmatrix} 3 & 1 \\ -1 & 1 \end{bmatrix}$ and a matrix $C$ is defined as $C = (BAB^{-1}) (B^{-1}A^{T}B)$ , where $ C  = K^{2} (K \in N)$ then $K =$	r. 2
d.	If $A = \begin{bmatrix} 1 & 1 \\ -1 & 1 \end{bmatrix}$ and $A^4 = -\lambda I$ then $\lambda - 2$ is equal to	s. 4

$$s$$
  $r$   $q$   $p$ 

B. 
$$egin{array}{cccccc} a & b & c & d \ s & p & q & r \end{array}$$

$$\vec{q}$$
  $p$   $s$   $r$ 

D. 
$$\begin{pmatrix} a & b & c & d \\ s & q & r & p \end{pmatrix}$$

### **Answer: C**



# **Numerical Value Type**

1. 
$$A=egin{bmatrix}0&1\\3&0\end{bmatrix}$$
  $and(A^8+A^6+A^4+A^2+I)V=egin{bmatrix}0\\11\end{bmatrix}$   $(where Iis ext{ the }2 imes2 ext{ identity matrix}), ext{ then the product of all elements of matrix }V ext{ is }$ 



**2.** If 
$$[abc1-a]$$
 is an idempotent matrix and  $f(x)=x-^2=bc=1/4$  , then the value of  $1/f(a)$  is \_\_\_\_\_.

be the



3.

Let

$$A^x=I; where A+[01-14-343-34] and I$$
 is the corresponding unit matrix and  $x\subseteq N,$  then the minimum value of  $\sum{(\cos^x{ heta}+\sin^x{ heta}), heta\in R}.$ 

solution

set

of

equation

**4.** 
$$A=egin{bmatrix}1&tanx\\-tanx&1\end{bmatrix}$$
 and  $f(x)$  is defined as  $f(x)=detig(A^TA^{-1}ig)$  for all x in domain, then the value of  $(f(f(f(f.....f(x)))))$  for  $(n\geq 2)$  is



**5.** The equation 
$$\begin{bmatrix} 1 & 2 & 2 \\ 1 & 3 & 4 \\ 2 & 4 & k \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$
 has  $a$  solution for  $(x, y, z)$  besides  $(0, 0, 0)$ . Then the value of  $k$  is \_\_\_\_\_.



**6.** If 
$$A$$
 is an idempotent matrix satisfying,  $\left(I-0.4A\right)^{-1}=I-\alpha A, where I$  is the unit matrix of the name order as that of  $A$ , then th value of  $|9\alpha|$  is equal to \_\_\_\_\_.

Water video Solution

7. Let

 $A=\left[3x^216x
ight], B=\left[abc
ight], and C=\left[\left(x+2
ight)^25x^22x5x^22x(x+2)^22x(x+2)^22x(x+2)^2\right]$  be three given matrices, where  $a,b,candx\in R$ . Given that  $f(x)=ax^2+bx+c$ , then the value of f(I) is \_\_\_\_\_.



**8.** Let A be the set of all  $3 \times 3$  skew-symmetri matrices whose entries are either  $-1,0,\ \, {\rm or}\ \, 1.$  If there are exactly three Os three 1s, and there (-1)'s, then the number of such matrices is \_\_\_\_\_.

**9.** Let 
$$A=\left(\left[a_{ij}\right]\right)_{3 imes3}$$
 be a matrix such that  $orall^T=4Ianda_{ij}+2c_{ij}=0, where c_{ij}$  is the cofactor of  $a_{ij}andI$  is the unit matrix of order 3.

 $|a_{11}+4a_{12}a_{13}a_{21}a_{22}+4a_{23}a_{31}a_{32}a_{33}+4|+5\lambda|a_{11}+1a_{12}a_{13}a_{21}a_{22}+1a_{23}$  then the value of  $10\lambda$  is

Watch Video Solution



10. Let S be the set which contains all possible values of l,m,n,p,q,r for which  $A=\begin{bmatrix}l^2-3&p&0\\0&m^2-8&q\\&0&n^2-15\end{bmatrix}$  be non-singular idempotent

matrix. Then the sum of all the elements of the set S is \_\_\_\_\_.



11. If A is a diagonal matrix of order  $3 \times 3$  is commutative with every square matrix or order  $3 \times 3$  under multiplication and tr(A)=12, then the value of  $|A|^{1/2}$  is \_\_\_\_\_.



**12.** If A is a square matrix of order 3 such that  $|A|=2, thenig|ig(adjA^{-1}ig)^{-1}ig|$  is \_\_\_\_\_\_.



**13.** If A and B are two matrices of order 3 such that AB=O and  $A^2+B=I$ , then tr.  $\left(A^2+B^2\right)$  is equal to \_\_\_\_\_.



**14.** If a, b, and c are integers, then number of matrices  $A=\begin{bmatrix} a & b & c \\ b & c & a \\ c & a & b \end{bmatrix}$  which are possible such that  $AA^T=I$  is \_\_\_\_\_.

Watch Video Solution

**15.** Let  $A=\left[a_{ij}
ight]$  be 3 imes3 matrix and  $B=\left[b_{ij}
ight]$  be 3 imes3 matrix such that  $b_{ij}$  is the sum of the elements of  $i^{th}$  row of A except  $a_{ij}$ . If  $\det$ , (A)=19,

then the value of det. (B) is \_\_\_\_\_\_.



**16.** A square matrix M of order 3 satisfies  $M^2=I-M$ , where I is an identity matrix of order 3. If  $M^n=5I-8M$ , then n is equal to \_\_\_\_\_.



**17.** Let  $A=\left[a_{ij}
ight]_{3 imes3}, B=\left[b_{ij}
ight]_{3 imes3}$  and  $C=\left[c_{ij}
ight]_{3 imes3}$  be any three matrices, where  $b_{ij}=3^{i-j}a_{ij}$  and  $c_{ij}=4^{i-j}b_{ij}$ . If det. A=2, then det.

(BC) is equal to  $\_\_\_$ .



**18.** If A is a square matrix of order  $2 \times 2$  such that |A|=27, then sum of the infinite series  $|A|+\left|\frac{1}{2}A\right|+\left|\frac{1}{4}A\right|+\left|\frac{1}{8}A\right|+...$  is equal to \_\_\_\_\_.



**19.** If A is a square matrix of order 2 and det. A=10, then  $\left((tr.\,A)^2-tr.\,\left(A^2
ight)
ight)$  is equal to \_\_\_\_\_ .



Watch Video Solution

**20.** Let A and B are two square matrices of order 3 such that det. (A)=3 and det. (B)=2, then the value of det.  $\left(\left(\mathrm{adj.}\ \left(B^{-1}A^{-1}\right)\right)^{-1}\right)$  is equal to



**21.** Let P, Q and R be invertible matrices of order 3 such  $A=PQ^{-1}, B=QR^{-1}$  and  $C=RP^{-1}$ . Then the value of det. (ABC+BCA+CAB) is equal to \_\_\_\_\_.



**22.** If  $P = \begin{bmatrix} 1 & \alpha & 3 \\ 1 & 3 & 3 \\ 2 & 4 & 4 \end{bmatrix}$  is the adjoint of a  $3 \times 3$  matrix A and det.

(A)=4, then the value of alpha is  $_{----}$  .



**23.** A, B and C are three square matrices of order 3 such that A= diag (x,y,z), det (B)=4 and det (C)=2, where  $x,y,z\in I^+$ . If det  $(adj(adj(ABC)))=2^{16}\times 3^8\times 7^4$ , then the number of distinct possible matrices A is \_\_\_\_\_.



**24.** Let  $A=\left[a_{\mathrm{ij}}
ight]$  be a matrix of order 2 where  $a_{\mathrm{ij}}\in\{-1,0,1\}$  and adj.

$$A=\,-\,A.$$
 If  ${\sf det.}\,(A)=\,-\,1$  , then the number of such matrices is \_\_\_\_\_ .



**25.** Let K be a positive real number and 
$$A=\begin{bmatrix}2k-1 & 2\sqrt{k} & 2\sqrt{k} \\ 2\sqrt{k} & 1 & -2k \\ -2\sqrt{k} & 2k & -1\end{bmatrix}$$
 and

$$B=egin{bmatrix} 0&2k-1&\sqrt{k}\ 1-2k&0&2\sqrt{k}\ -\sqrt{k}&-2\sqrt{k}&0 \end{bmatrix}$$
 . If det (adj A) + det (adj B)  $=10^6$ , then

[k] is equal to \_\_\_\_\_ .  $[ \hbox{Note : adj M denotes the adjoint of a square matrix M and } [k] \ \hbox{denotes}$ 

the largest integer less than or equal to k.]

$$M[010]=M[1-10]=[11-1], and M[111]=[0012]$$
 Then the sum of the diagonal entries of  $M$  is \_\_\_\_\_.

Let M be a 3 imes 3 matrix



26.

satisfying

and I be the idenfity matrix or order 2. Then the total number of ordered pairs (r,s) for which  $P^2=\,-\,I$  is



Watch Video Solution

# **Archives (Single correct Answer type)**

**1.** Let A be a 2 imes 2 matrix

Statement -1 adj (adjA)=A

Statement-2 |adjA|=|A|

A. Statement 1 is true, statement 2 is true, statement 2 is a correct

explanation for statement 1.

B. Statement 1 is true, statement 2 is true, statement 2 is a correct

explanation for statement 1.

C. Statement 1 is true, statement 2 is false.

D. Statement 1 is false, statement 2 is true.

### **Answer: B**



Watch Video Solution

2. The number of 3 x 3 non-singular matrices, with four entries as 1 and all other entries as 0, is:- (1) 5 (2) 6 (3) at least 7 (4) less than 4

A. 5

B. 6

C. at least 7

D. less than 4

### **Answer: C**



Watch Video Solution

3. Let A be a  $2 \times 2$  matrix with non-zero entries and let A^2=I, where i is a

2 imes 2 identity matrix, Tr(A) i= sum of diagonal elements of A and |A| =

determinant of matrix A. Statement 1:Tr(A)=0 Statement 2:|A|=1. then (A) Statement 1 is false, statement 2 is true. (B) Statement 1 is true, statement 2 is true, statement 2 is a correct explanation for statement 1. (C) Statement 1 is true, statement 2 is true, statement 2 is a correct explanation for statement 1. (D) Statement 1 is true, statement 2 is false.

A. Statement 1 is false, statement 2 is true.

B. Statement 1 is true, statement 2 is true, statement 2 is a correct explanation for statement 1.

C. Statement 1 is true, statement 2 is true, statement 2 is a correct explanation for statement 1.

D. Statement 1 is true, statement 2 is false.

### **Answer: D**



4. Let A and B two symmetric matrices of order 3.

Statement 1: A(BA) and (AB)A are symmetric matrices.

Statement 2 : AB is symmetric matrix if matrix multiplication of A with B is commutative.

A. Statement 1 is false, statement 2 is true.

B. Statement 1 is true, statement 2 is true, statement 2 is a correct explanation for statement 1.

C. Statement 1 is true, statement 2 is true, statement 2 is not a correct

explanation for statement 1.

D. Statement 1 is true, statement 2 is false.

### **Answer: C**



**5.** Let 
$$A=egin{pmatrix}1&0&0\\2&1&0\\3&2&1\end{pmatrix}$$
 . If  $u_1$  and  $u_2$  are column matrices such that

$$Au_1=egin{pmatrix}1\0\0\end{pmatrix}$$
 and  $Au_2=egin{pmatrix}0\1\0\end{pmatrix}$  , then  $u_1+u_2$  is equal to :

$$Au_1=egin{pmatrix} 0\ 0 \end{pmatrix}$$
 and  $Au_2=egin{pmatrix} 1\ 0 \end{pmatrix}$  , then  $u_1+u_2$  is  $A.egin{pmatrix} -1\ 1\ 0 \end{pmatrix}$  B.  $egin{pmatrix} -1\ -1\ 0 \end{pmatrix}$  C.  $egin{pmatrix} -1\ 0\ \end{pmatrix}$ 

# Answer: D



- **6.** Let P and Q be 3 imes 3 matrices with P 
  eq Q . If  $P^3 = Q^3 and P^2 Q = Q^2 P$  , then determinant of  $\left(P^2 + Q^2\right)$  is equal to
- (1) 2 (2) 1 (3) 0 (4) 1

$$A.-2$$

B. 1

C. 0

D. - 1

### **Answer: C**



# Watch Video Solution

**7.** If 
$$P=egin{bmatrix}1&lpha&3\\1&3&3\\2&4&4\end{bmatrix}$$
 is the adjoint of a  $3 imes3$  matrix A and det.  $(A)=4$ ,

then the value of alpha is \_\_\_\_\_.

A. 4

B. 11

C. 5

D. 0

### **Answer: B**



Watch Video Solution

**8.** If A is an 3 imes 3 non-singular matrix such that  $AA^T = A^TA$  and

 $B=A^{-1}A^{T}$  , then  $BB^{T}$  equals (1) I+B (2) I (3)  $B^{-1}$  (4)  $\left(B^{-1}
ight)^{T}$ 

A. 
$$I + B$$

В. *I* 

 $C. B^{-1}$ 

D.  $(B^{-1})'$ 

### **Answer: B**



Watch Video Solution

**9.** If A=[12221-2a2b] is a matrix satisfying the equation  $\ orall^T=9I$  , where I is 3 imes 3 identity matrix, then the ordered pair (a, b) is equal to :

(1) 
$$(2, -1)$$
  $(2)$   $(-2, 1)$   $(3)$   $(2, 1)$   $(4)$   $(-2, -1)$ 

A.  $(2, -1)$ 

B.  $(-2, 1)$ 

C.  $(2, 1)$ 

D.  $(-2, -1)$ 

Answer: D

10. If  $A = \begin{bmatrix} 5a & -b \\ 3 & 2 \end{bmatrix}$  and  $AadjA = AA^T$ , then  $5a + b$  is equal to: (1)  $-1$  (2) 5 (3) 4 (4) 13

A. 5

B. 4

C. 13

D.-1

### **Answer: A**



Watch Video Solution

**11.** if 
$$A=\left[egin{array}{cc} 2 & -3 \ -4 & 1 \end{array}
ight]$$
 then  $\left(3A^2+12A\right)=?$ 

A. 
$$\begin{bmatrix} 72 & -63 \\ -84 & 51 \end{bmatrix}$$

$$\mathsf{B.} \left[ \begin{array}{cc} 72 & -84 \\ -63 & 51 \end{array} \right]$$

$$\mathsf{C.}\begin{bmatrix}51 & 63\\84 & 72\end{bmatrix}$$

D. 
$$\begin{bmatrix} 51 & 84 \\ 63 & 72 \end{bmatrix}$$

### **Answer: C**



Watch Video Solution

JEE Advanced (Single Correct Answer Type)

1. The number of 3 imes 3 matrices A whose entries are either  $0 \ {
m or} \ 1$  and

for which the system 
$$Aegin{pmatrix} x \\ y \\ z \end{bmatrix} = egin{pmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$
 has exactly two distinct solution is a. 0

b. 
$$2^9-1$$
 c.  $168$  d.  $2$ 

B. 
$$2^9 - 1$$

#### **Answer: A**



# **Watch Video Solution**

**2.** Let  $\omega \neq 1$  be cube root of unity and S be the set of all non-singular

matrices of the form  $\left[egin{array}{ccc} 1 & a & b \\ \omega & 1 & c \\ \omega^2 & \omega & 1 \end{array}
ight], \,\,$  where each of  $a,b,\,\,$  and  $\,c$  is either  $\omega$ 

or  $\omega^2$  . Then the number of distinct matrices in the set S is (a) 2 (b) 6 (c) 4 (d) 8

B. 6

C. 4

D. 8

A. 2

# Answer: A



**3.** Let  $P=ig[a_{ij}ig]$  be a 3 imes3 matrix and let  $Q=ig[b_{ij}ig], where <math>b_{ij}=2^{i+j}a_{ij}f$  or  $1\leq i,j\leq 3$ . If the determinant of

 $Q=\lfloor b_{ij}
floor, where b_{ij}=2^{i+j}a_{ij}f ext{ or } 1\leq i,j\leq 3.$  If the determinant ooP is 2, then the determinant of the matrix Q is  $2^{10}$  b.  $2^{11}$  c.  $2^{12}$  d.  $2^{13}$ 

A.  $2^{10}$ 

 $\mathsf{B.}\ 2^{11}$ 

 $\mathsf{C.}\ 2^{12}$ 

### **Answer: D**



Watch Video Solution

**4.** Let  $P=egin{bmatrix}1&0&0\\3&1&0\\9&3&1\end{bmatrix}$  and Q =  $egin{bmatrix}q_{ij}\end{bmatrix}$  be two 3 imes3 matrices such that

$$Q-P^5=I_3.$$
 Then  $rac{q_{21}+q_{31}}{q_{32}}$  is equal to

- A. 52
- B. 103
- C. 201
- D. 205

#### **Answer: B**



**5.** How many  $3 \times 3$  matrices M with entries from  $\{0, 1, 2\}$  are there, for which the sum of the diagonal entries of  $M^TMis5$ ? 126 (b) 198 (c) 162 (d)

135

A. 198

B. 126

D. 162

C. 135

# Answer: A



Watch Video Solution

# **Single correct Answer**

**1.** If 
$$A=egin{bmatrix}0&c&-b\\-c&0&a\\b&-a&0\end{bmatrix}$$
 and  $B=egin{bmatrix}a^2&ab∾\\ab&b^2&bc\\ac&bc&c^2\end{bmatrix}$  , then  $(A+B)^2=$ 

(a) A (b) B (c) I (d)  $A^2 + B^2$ 

A. 
$$A$$

B.B

 $\mathsf{C}.\,I$ 

D.  $A^2 + B^2$ 

# Answer: D



Watch Video Solution

- **2.** If the value of  $\prod_{k=1}^{50} \begin{bmatrix} 1 & 2k-1 \\ 0 & 1 \end{bmatrix}$  is equal to  $\begin{bmatrix} 1 & r \\ 0 & 1 \end{bmatrix}$  then r is equal to
  - A. A. 62500
  - C. C. 1250

B. B. 2500

D. D. 12500

# **Answer: B**



**3.** A square matrix P satisfies  $P^2=I-P$ , where I is identity matrix. If

$$P^n = 5I - 8P$$
, then n is :

**B**. 5

 $\mathsf{C.}\,6$ 

D. 7

#### **Answer: C**



# Watch Video Solution

**4.** A and B are two square matrices such that  $A^2B=BA$  and if  $(AB)^{10}=A^kB^{10}$ , then k is

A. 1001

B.1023

C. 1042

D. none of these

**Answer: B** 



Watch Video Solution

**5.** If matrix  $A=\left[a_{ij}
ight]_{3 imes3}$ , matrix  $B=\left[b_{ij}
ight]_{3 imes3}$ , where  $a_{ij}+a_{ji}=0$  and

 $b_{ij} - b_{ji} = 0 \, orall i, j$ , then  $A^4 \cdot B^3$  is

A. Singular

B. Zero matrix

C. Symmetric

D. Skew-Symmetric matrix

**Answer: A** 



**6.** If 
$$A \begin{pmatrix} 1 & 3 & 4 \ 3 & -1 & 5 \ -2 & 4 & -3 \end{pmatrix} = \begin{pmatrix} 3 & -1 & 5 \ 1 & 3 & 4 \ +4 & -8 & 6 \end{pmatrix}$$
, then  $A =$ 

A. 
$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -2 \end{pmatrix}$$
B. 
$$\begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

D. 
$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & - \end{pmatrix}$$

# Answer: D



Watch Video Solution

7. Let  $A=\begin{bmatrix} -5 & -8 & -7 \ 3 & 5 & 4 \ 2 & 2 & 2 \end{bmatrix}$  and  $B=\begin{bmatrix} x \ y \ 1 \end{bmatrix}$  . If AB is a scalar multiple of

$$B$$
, then the value of  $x+y$  is

$$\mathsf{A.}-1$$

B.-2

**C**. 1

D. 2

### **Answer: B**



# Watch Video Solution

**8.**  $A=egin{bmatrix} a & b \ b & -a \end{bmatrix}$  and  $MA=A^{2m}$ ,  $m\in N$  for some matrix M, then which one of the following is correct?

A. A. 
$$M=egin{bmatrix} a^{2m} & b^{2m} \ b^{2m} & -a^{2m} \end{bmatrix}$$

B. B. 
$$M=\left(a^2+b^2
ight)^m\!\left[egin{array}{cc} 1 & 0 \ 0 & 1 \end{array}
ight]$$

C. C. 
$$M=(a^m+b^m)egin{bmatrix}1&0\0&1\end{bmatrix}$$
D. D.  $M=egin{bmatrix}a^2+b^2\end{pmatrix}^{m-1}egin{bmatrix}a&b\b=-a\end{bmatrix}$ 

### Answer: D



**9.** If  $A=\left[a_{ij}
ight]_{m imes n}$  and  $a_{ij}=\left(i^2+j^2-ij\right)(j-i), n$  odd, then which of the following is not the value of Tr(A) (a) 0 (b) |A| (c) 2|A| (d) none of these

**A.** 0

B. |A|

 $\mathsf{C.}\,2|A|$ 

D. none of these

### **Answer: D**



**Watch Video Solution** 

**10.** If det,  $(A-B) \neq 0,$   $A^4=B^4,$   $C^3A=C^3B$  and  $B^3A=A^3B$ , then find the value of det.  $\left(A^3+B^3+C^3\right)$ .

**A.** 0

**B**. 1

 $\mathsf{C.}\left.3|A|^3\right.$ 

D. 6

# Answer: A



# Watch Video Solution

11. If AB + BA = 0, then which of the following is equivalent to  $A^{3} - B^{3}$ 

A. A.  $(A-B)(A^2+AB+B^2)$ 

B. B.  $(A - B)(A^2 - AB - B^2)$ 

C. C.  $(A + B)(A^2 - AB - B^2)$ 

D. D.  $(A + B)(A^2 + AB - B^2)$ 

### **Answer: C**



**12.** A,B,C are three matrices of the same order such that any two are symmetric and the  $3^{rd}$  one is skew symmetric. If X=ABC+CBA and Y=ABC-CBA, then  $(XY)^T$  is

A. A. symmetric

B. B. skew symmetric

 $\mathsf{C.}\,\mathsf{C.}\,I-XY$ 

D. D. -YX

### Answer: D



**Watch Video Solution** 

**13.** If A and P are different matrices of order n satisfying  $A^3=P^3$  and  $A^2P=P^2A$  (where |A-P| 
eq 0) then  $\left|A^2+P^2\right|$  is equal to (A) n (B) 0

(C) 
$$|A||P|$$
 (D)  $|A+P|$ 

A. n

**B**. 0

 $\mathsf{C}.\,|A||P|$ 

D. |A+P|

# **Answer: B**



# Watch Video Solution

**14.** Let A, B are square matrices of same order satisfying AB=A and BA=B then  $\left(A^{2010}+B^{2010}
ight)^{2011}$  equals.

A.A + B

B. 2010(A + B)

C. 2011(A + B)

D.  $2^{2011}(A+B)$ 

# Answer: D

**15.** The number of  $2\times 2$  matrices A, that are there with the elements as real numbers satisfying  $A+A^T=I$  and  $AA^T=I$  is (a) zero (b) one (c) two (d) infinite

A. zero

B. one

C. two

D. infinite

#### **Answer: C**



**Watch Video Solution** 

**16.** If the orthogonal square matrices A and B of same size satisfy  $\det A + \det B = 0$  then the value of  $\det(A+B)$ 

$$A. - 1$$

**B**. 1

C.0

D. none of these

### **Answer: C**



# Watch Video Solution

**17.** If 
$$A=egin{bmatrix}\cos\theta&\sin\theta\\\sin\theta&-\cos\theta\end{bmatrix}, B=egin{bmatrix}1&0\\-1&1\end{bmatrix}, C=ABA^T, ext{ then}$$
  $A^TC^nA, n\in I^+$  equals to

A. 
$$\begin{bmatrix} -n & 1 \\ 1 & 0 \end{bmatrix}$$

$$\mathsf{B.} \begin{bmatrix} 1 & -n \\ 0 & 1 \end{bmatrix}$$

$$\mathsf{C.}\begin{bmatrix}0&1\\1&-n\end{bmatrix}$$

D. 
$$\begin{bmatrix} 1 & 0 \\ -n & 1 \end{bmatrix}$$

## Answer: D

**18.** Let A be a 3 imes 3 matrix given by  $A = \left(a_{ij}\right)_{3 imes 3}$ . If for every column vector X satisfies X'AX = 0 and  $a_{12} = 2008$ ,  $a_{13} = 2010$  and

 $a_{23}={}-2012$ . Then the value of  $a_{21}+a_{31}+a_{32}=$ 

A. 
$$-6$$

B. 2006

 $\mathsf{C.}-2006$ 

**D**. 0

## **Answer: C**



**Watch Video Solution** 

**19.** Let A and B be two non-singular matrices such that  $A\ne I,$   $B^3=I$  and  $AB=BA^2$ , where I is the identity matrix, the least value of k such that  $A^k=I$  is

A. 4 B.5**C**. 10 D. 7 **Answer: D** Watch Video Solution **20.** Let A be a  $2 \times 3$  matrix, whereas B be a  $3 \times 2$  amtrix. If  $\det (AB) = 4$ , then the value of  $\det (BA)$  is A.-4B. 2  $\mathsf{C.}-2$ D.0**Answer: D** 

**21.** Let A be a square matrix of order 3 so that sum of elements of each row is 1. Then the sum elements of matrix  $A^2$  is

- A. A. 1
- B. B. 3
- $\mathsf{C.\,C.}\,0$
- D. D. 6

Answer: B



Watch Video Solution

**22.** A and B be 3 imes 3 matrices such that AB + A + B = 0, then

A. A. 
$$(A+B)^2 = A^2 + 2AB + B^2$$

$$\operatorname{B.B.}|A|=|B|$$

$$\mathsf{C.\,C.\,}A^2=B^2$$

D. D. none of these

#### **Answer: A**



Watch Video Solution

# **23.** If $(A+B)^2=A^2+B^2$ and |A| eq 0 , then |B|= (where A and B

are matrices of odd order)

B.-2

**C**. 1

**D**. 0

## **Answer: D**



**24.** If A is a square matrix of order 3 such that  $\left|A\right|=5$ , then

$$|Adj(4A)| =$$

A. 
$$5^3 imes 4^2$$

$$\text{B.}\,5^2\times4^3$$

$$\text{C.}~5^2\times16^3$$

D. 
$$5^3 imes 16^2$$

## Answer: C



# Watch Video Solution

**25.** If A and B are two non singular matrices and both are symmetric and commute each other, then

A. Both  $A^{-1}B$  and  $A^{-1}B^{-1}$  are symmetric.

B.  $A^{-1}B$  is symmetric but  $A^{-1}B^{-1}$  is not symmetric.

C.  $A^{-1}B^{-1}$  is symmetric but  $A^{-1}B$  is not symmetric.

D. Neither  $A^{-1}B$  nor  $A^{-1}B^{-1}$  are symmetric

Answer: A



Watch Video Solution

- **26.** If A is a square matrix of order 3 such that  $\left|A\right|=2$ , then  $\left|\left(adjA^{-1}
  ight)^{-1}
  ight|$  is
  - **A.** 1
  - B. 2
  - **C**. 4
  - D. 8

**Answer: C** 



**27.** Let matrix 
$$A=egin{bmatrix} x&y&-z\ 1&2&3\ 1&1&2 \end{bmatrix}$$
 , where  $x,y,z\in N.$  If

 $|adj(adj(adj(adjA)))|=4^8\cdot 5^{16}$  , then the number of such (x,y,z) are

- A. 28
- B.36
- C.45
- D. 55

## Answer: B



Watch Video Solution

**28.** A be a square matrix of order 2 with  $|A| \neq 0$  such that |A+|A|adj(A)|=0, where adj(A) is a adjoint of matrix A, then the 

A. 1

B. 2

C. 3

D. 4

## Answer: D



**Watch Video Solution** 

**29.** If S is a real skew-symmetric matrix and det.  $(I-S) \neq 0$ , then prove that matrix  $A = (I+S)(I-S)^{\,-1}$  is orthogonal.

A. idempotent matrix

B. symmetric matrix

C. orthogonal matrix

D. none of these

## **Answer: C**



**30.** If 
$$A = \begin{bmatrix} 3 & -3 & 4 \\ 2 & -3 & 4 \\ 0 & -1 & 1 \end{bmatrix}$$
 , then

## Answer: A



31. If 
$$A=egin{bmatrix}1&-1&1\\0&2&-3\\2&1&0\end{bmatrix}$$
 and  $B=(adjA)$  and  $C=5A$ , then find the value of  $\cfrac{|adjB|}{|C|}$ 

**C**. 1

D. 5

## **Answer: C**



Watch Video Solution

**32.** Let A and B be two non-singular square matrices such that B 
eq Iand  $AB^2=BA$ . If  $A^3-B^{-1}A^3B^n$ , then value of n is

A. 4

B. 5

C. 8

D. 7

## **Answer: C**



**33.** If A is an idempotent matrix satisfying,  $\left(I-0.4A\right)^{-1}=I-\alpha A, where I$  is the unit matrix of the name order

 $(I-0.~4A)^{-1}=I-\alpha A, where I$  is the unit matrix of the name order as that of  $A, \,$  then th value of  $|9\alpha|$  is equal to \_\_\_\_\_.

A. 
$$-1/3$$

$$\mathsf{C.}-2/3$$

D. 
$$2/3$$

## Answer: C



**34.** If 
$$A$$
 and  $B$  are two non-singular matrices which commute, then 
$$\left(A(A+B)^{-1}B\right)^{-1}(AB) =$$

A. 
$$A+B$$

$${\rm B.}\,A^{\,-1} + B^{\,-1}$$

 $\mathsf{C.}\,A^{\,-1}+B$ 

D. none of these

Answer: A

